

UNIVERSITY OF ILLINOIS  
DIGITAL COMPUTER

LIBRARY ROUTINE HF 1 - 111

**TITLE:** Zero of a Solution of a Differential Equation  
(Using Library Routine F1) (SADOI or DOI)

**TYPE:** Closed, with one program parameter (see below)

**NUMBER OF WORDS:** 16

**TEMPORARY STORAGE:** 0, 1, 2, 3

**PRESET PARAMETERS:** S3-S5

3        OOF 00mF    Program parameter for routine F1 (SEE F1)

4        OOF 00gF    Steps proportional to N(g).

5        OOF 00hF    Routine F1 begins at h.

**PROGRAM PARAMETER:** Entry

p	50 eF   N(e) is to become zero.
	50 pF

p+1	26 xF   This routine begins at x.
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**DESCRIPTION:** This routine enters Code F1 repeatedly, adjusting the size of the steps, until one of the variables  $y_1$  vanishes. The variable which is to become zero is selected by the program parameter.

The auxiliary routine used by Library Routine F1 must be so designed that the scaled derivatives  $2^m hy_1'$  are all proportional to a scale factor stored in g. This scale factor is altered during the convergence to the zero, and must be restored if further steps are to be carried out.  $|N(g)|$  is never increased by this routine, so that if the steps are initially sufficiently small for accurate integration they will remain so. This means that several steps may be necessary to reach the neighborhood of the zero; when this has occurred, about six steps are usually sufficient for convergence.  $N(e)$  is normally reduced to 0 or to  $+ 2^{-39}$ ; if  $hy' > N(g)$  the error may be as large

as  $2^{-39} \text{hy}'/N(\xi)$  but this would be abnormal.

Integration proceeds in the direction in which  $|N(e)|$  decreases. If a non-zero minimum of  $|N(e)|$  is encountered control may be incorrectly returned to the main program, or the machine may get into a loop. This routine should therefore only be entered when the integration is near the required zero. The scaled derivative of the variable which is to vanish must be non-zero when this routine is entered.

DATE	October 5, 1953	RT: 2/25/60
PROGRAMMED BY	Stanley Gill	
APPROVED BY	J. P. Nash	

ns

LOCATION	ORDER		NOTES	PAGE 1	HF 1
	OOK(HF1)				
0	K5 F				
	46 6L				
1	42 5L		Set link etc.		
	L4 39S5				
2	46 3L		Waste		
	26 3L				
3	L5 F	By 2			
	40 F	From 14'	$2^m \text{hy}'$ to 0		
4	L3 F				
	10 S3		Form 2 <sup>-39</sup> -  hy'		
5	L4 15L				
	32 F	By 1	Link: Test for convergence		
6	50 F	By 0'			
	L0 15L		Test if $ y  \geq  hy' $		
7	S6 F				
	32 10L				
8	S5 F				
	00 S3		Near zero: Use Newton-Raphyson		
9	66 F				
	79 S4				
10	26 12L				
	71 F	From 7'	Test whether to reverse		
11	36 13L				
	L1 S4		Reverse step		
12	40 S4	From 10			
	26 13L		Waste		
13	00 S3	From 11			
	50 13L		Enter Program F1		
14	26 S5				
	26 3L				
15	00 F				
	00 1F				