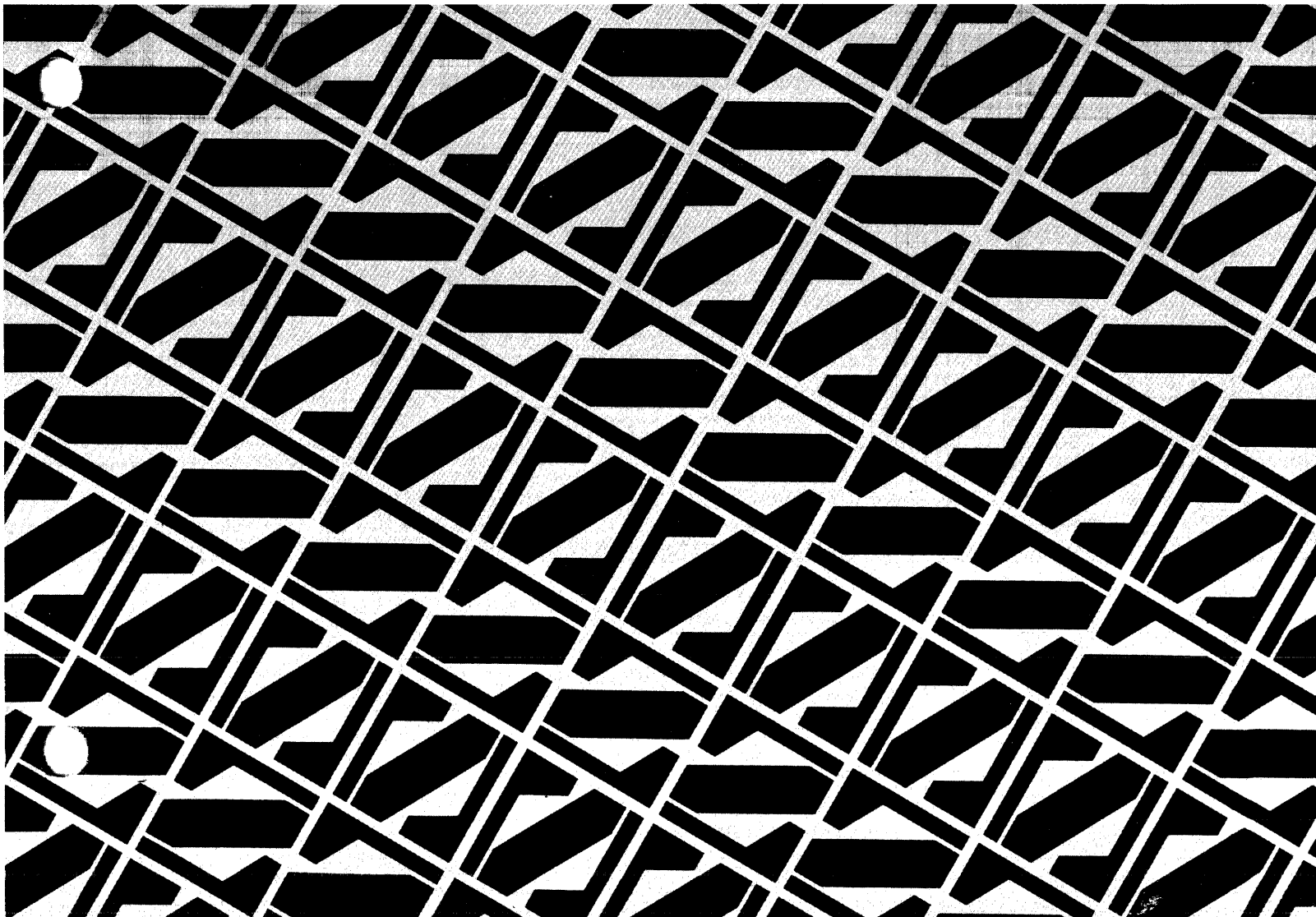


National Semiconductor

Order No. IMP-16F/972A

Pub. No. 4200072A

IMP-16F/400 Floating Point Firmware Technical Description



Order Number IMP-16F/972A
Publication Number 4200072A

Integrated MicroProcessor-16

IMP-16F/400

FLOATING POINT FIRMWARE

TECHNICAL DESCRIPTION

January 1975

National Semiconductor Corporation
2900 Semiconductor Drive
Santa Clara, California 95051

INTRODUCTION

This subroutine set provides an IMP-16 microprocessor with double-precision and floating-point capability. Double-precision and floating-point computation is very useful when additional precision is needed or the range of numbers is expected to be large. In the following pages, individual subroutines are described along with necessary user instructions. Subroutines included in the set are listed in the table below.

ARITHMETIC SUBROUTINE SET

| SUBROUTINE | MNEMONIC | ENTRY POINT |
|----------------------------------|----------|-------------|
| Single Precision Multiply | MULT | FC01 |
| Single Precision Divide | DIV | FC1A |
| Double Precision Multiply | DPMUL | FCCF |
| Positive Double Precision Divide | DPDIV | FDE3 |
| Double Precision Square | DPSQUARE | FCCD |
| Double Precision Complement | DPCOMP | FDBA |
| Double Precision Shift | DPSH | FDDB |
| Double Precision Shift Right | DPSHR | FDCE |
| Double Precision Shift Left | DPSHL | FDDB |
| Quadrant Tests | QUAD | FDA0 |
| Sine | SIN | FCFA |
| Cosine | COS | FCFC |
| Arctangent | ARCTAN | FD37 |
| Floating Point Add | FPADD | FC30 |
| Floating Point Multiply | FPMUL | FC5D |
| Floating Point Divide | FPDIV | FC6C |
| Floating Point Complement | FPCOMP | FCB9 |
| Check Zero Exponent | CZERO | FC63 |
| Extract Exponent to Stack | EXTEXP | FC7C |
| Add Exponent from Stack | ADDEXP | FCBD |
| Left Normalize | LFNOR | FC97 |
| Double Left Normalize | DLNORM | FC8A |
| Fraction to Floating Point | FLOAT | FC85 |
| Floating Point to Fraction | SFO | FCC7 |

GENERAL CHARACTERISTICS

The arithmetic subroutine set uses 512 memory words located at addresses FC00 through FFFF (64512 through 65023, decimal). All subroutines are contained wholly within the set; they require no external program code. The IMP-16 extended instruction set is required. Operands and results, in most cases, use the general registers. The only memory locations written into by the set are in the range 00E0 through 00EF. All constants are contained within the subroutine set.

EXECUTION TIMES

Execution times shown on each of the subroutine data sheets are expressed in terms of three variables, where

- R = Number of main memory read cycles
- W = Number of main memory write cycles
- N = Number of microprogram cycles

These execution time expressions can thus be used to calculate subroutine execution time for any IMP-16 implementation. A few subroutine execution times are also dependent on user-specified variables (such as shift counts in shift instructions). These are defined on the individual data sheets. All execution times are based on worst-case conditions.

NUMBER REPRESENTATION

Numbers in a computer program often represent real world parameters. In this subroutine set, four different modes of numerical representation are used: integer, fractional, double-precision, and floating-point. All four modes have important applications in IMP-16 systems.

Integer notation is the most common and obvious mode of numerical representation. It is simply an integer count of something. In the IMP-16, numbers up to 2^{16} may be represented because of the 16-bit word length. To represent both positive and negative integers, a two's-complement system is used. This gives an integer range of

$$-2^{15} \leq \text{integer} < 2^{15}$$

With two's-complement notation, the most significant bit, bit 15, can be thought of as a sign bit, and the binary point can be thought of as being to the right of bit 0.

FRACTIONAL NOTATION

Many real-world parameters are continuous rather than discrete. Such values can never be indicated with perfect precision because of the limited word length of any computer. Take the airspeed of an aircraft as an example. It may have a potential range from zero to 1000 miles per hour. We would rarely expect its speed to be an exact round number. At some instant the speed may be 556.234.... If we want to express this speed as precisely as possible given a 16-bit word length, an integer notation of 556 miles per hour would not be the best choice. A more convenient technique is to use fractional notation. The parameter, in this case speed, can be scaled so that 1000 miles per hour is equivalent to 1.0000.... This would allow the full 16-bit capacity to be utilized. After scaling, the range of numerical expression of a fractional number is

$$-1.0 \leq N < 1.0$$

With fractional notation, the binary point can be thought of as being to the right of bit 15. Thus, the largest positive binary number that can be represented is 0.11111... or almost one. Precision is about $3.1 * 10^{-5}$.

DOUBLE PRECISION

When precision greater than 16-bits is required, double-precision numbers can be used. Double-precision numbers give a precision of one part in 2^{31} or about $4.6 * 10^{-10}$. Double-precision numbers are an extended fractional notation. Note that two IMP-16 words are required.

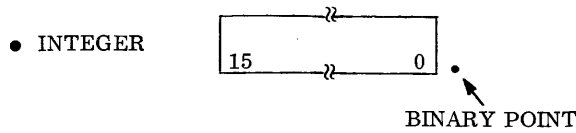
FLOATING POINT

Floating-point representation is a technique to express numbers in a form similar to scientific notation, with a fractional mantissa and an exponent. The value of any floating-point number so represented is equivalent to mantissa * (2^{exponent}). The mantissa consists of 24 bits and gives a precision of one part in 2^{23} . The exponent has 8 bits and allows exponents in the range

$$-2^7 \leq \text{exponent} < 2^7$$

The great advantage of floating-point numbers is that the scaling factor of a fractional number becomes a visible attribute which can be manipulated. Thus, the scaling factor can be altered to maintain precision or facilitate computations.

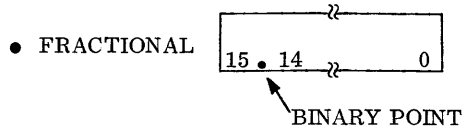
NUMBER REPRESENTATION EXAMPLES



EXAMPLES:
 $5 = 0005_{16}$
 $-5 = FFFB_{16}$

RANGE: $-32768 \leq N < 32768$
 MAXIMUM PRECISION: 1
 SMALLEST VALUE: 1

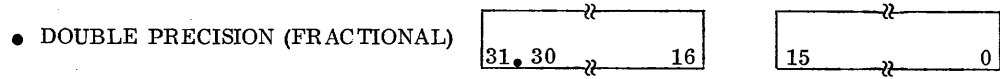
SPEED = $556.234 = 556_{10} = 022C_{16}$



EXAMPLES:
 $1/2 = 4000_{16}$
 $-1/2 = C000_{16}$
 $-1 = 8000_{16}$

RANGE: $-1 \leq N < 1$
 MAXIMUM PRECISION: $1/2^{15} = 3.1 * 10^{-5}$
 SMALLEST VALUE: 2^{-15}

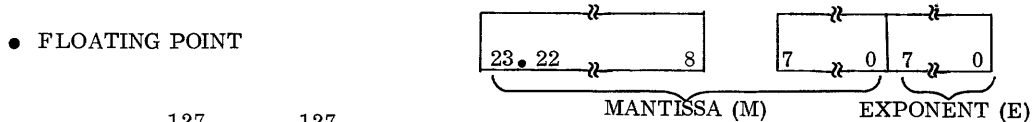
SPEED = $1000.000 = 0.556234_{10} = 4732_{16}$



EXAMPLES:
 $1/2 = 4000\ 0000_{16}$
 $-1/2 = C000\ 0000_{16}$
 $-1 = 8000\ 0000_{16}$

RANGE: $-1 \leq N < 1$
 MAXIMUM PRECISION: $1/2^{31} = 4.6 * 10^{-10}$
 SMALLEST VALUE: 2^{-31}

SPEED = $4732\ ACFB_{16}$



$N = M * 2^E$

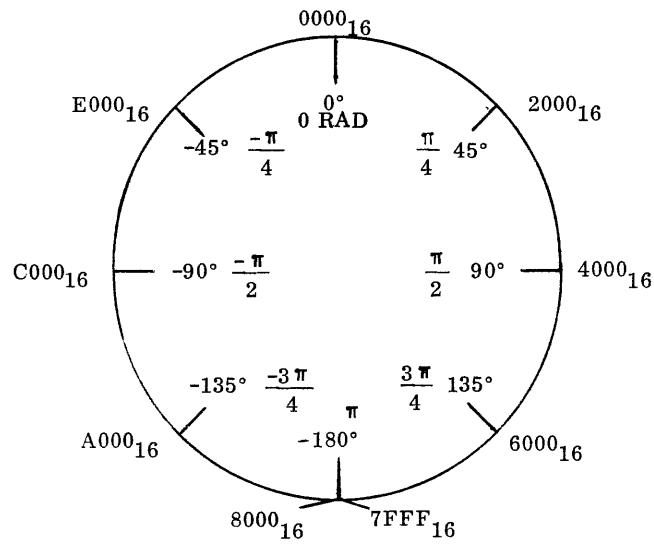
RANGE: $-2^{127} \leq N < 2^{127}$
 PRECISION: 2^{-23} (2^{EXPONENT})
 SMALLEST MAGNITUDE: 2^{-151}
 LARGEST MAGNITUDE: $(1-2^{-23}) 2^{127}$

EXAMPLES:
 $1/2 = 4000\ 00_{16}$ (00_{16})
 $1/2 = 2000\ 00_{16}$ (01_{16})
 $1/2 = 1000\ 00_{16}$ (02_{16})
 $1/4 = 2000\ 00_{16}$ (00_{16})
 $1/4 = 4000\ 00_{16}$ (FF_{16})

SPEED = $556.234 = 4587\ 7A_{16}$ ($0A_{16}$)

ANGULAR REPRESENTATION

Angles are expressed as a double-precision fraction of π radians.



NOTATION

In the descriptions which follow, R0, R1, R2, and R3 represent the contents of the four accumulators = AC0, AC1, AC2, and AC3.

Normalization of a floating point number means that the mantissa is shifted left until the most significant bit is a 1, and the exponent adjusted accordingly.

| | |
|--|-------------|
| SUBROUTINE: SINGLE PRECISION MULTIPLY | LABEL: MULT |
| DESCRIPTION: MULTIPLIES TWO SINGLE-PRECISION, SIGNED, FRACTIONAL 16-BIT NUMBERS TO GIVE A SIGN PLUS A 30-BIT RESULT | |
| ENTRY POINT: FC01 ENTRY CONDITIONS: $R_0 = X$ $R_2 = Y$ EXIT CONDITIONS: $R_0, R_1 = X * Y$ R_2 - ALTERED $R_3 =$ UNCHANGED EXECUTION TIME: $30R + 243N + W$ | |
| TEMPORARY LOCATIONS USED: 00E0 SUBROUTINES CALLED: DSHL, DPCOMP STACK WORDS NEEDED: 2 (MAXIMUM DEPTH) | |
| COMMENTS: 1. ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. 2. FRACTIONAL DIFFERS FROM AN INTEGER MULTIPLY IN THAT THE RESULT OF A FRACTIONAL MULTIPLY IS SHIFTED LEFT 1 BIT. | |

| | |
|---|------------|
| SUBROUTINE: SINGLE PRECISION DIVIDE | LABEL: DIV |
| DESCRIPTION: DIVIDES A SIGNED, FRACTIONAL 16-BIT NUMBER INTO A SIGNED, FRACTIONAL 32-BIT NUMBER, PROVIDING A QUOTIENT AND AN INTEGER REMAINDER | |
| ENTRY POINT: FC1A ENTRY CONDITIONS: $R_0, R_1 =$ DIVIDEND $R_2 =$ DIVISOR EXIT CONDITIONS: $R_0 =$ QUOTIENT $R_1 =$ REMAINDER $R_2 =$ ALTERED $R_3 =$ UNCHANGED EXECUTION TIME: $49R + W + 343N$ | |
| TEMPORARY LOCATIONS USED: 00E0 SUBROUTINES CALLED: DSHR, DPCOMP STACK WORDS NEEDED: 2 (MAXIMUM DEPTH) | |
| COMMENTS: 1. ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. 2. OVERFLOW FLAG IS SET IF MSB OF DIVIDEND \geq DIVISOR. | |

| | |
|---|--------------|
| SUBROUTINE: DOUBLE PRECISION MULTIPLY | LABEL: DPMUL |
| DESCRIPTION: MULTIPLIES DOUBLE-PRECISION OPERANDS TO GIVE A DOUBLE-PRECISION PRODUCT | |
| ENTRY POINT: FCCF ENTRY CONDITIONS: $R_0, R_1 = X$ $R_2, R_3 = Y$ EXIT CONDITIONS: $R_0, R_1 = X * Y$ R_2, R_3 ALTERED EXECUTION TIME: $200R + 8W + 1125N$ | |
| TEMPORARY LOCATIONS USED: 00E0, 00E1, 00EE, 00EF SUBROUTINES CALLED: QUAD, MULT, DPCOMP, DSHL STACK WORDS NEEDED: 4 (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. | |

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|--|--------------|
| SUBROUTINE: POSITIVE DOUBLE PRECISION DIVIDE | LABEL: DPDIV |
| DESCRIPTION: UNSIGNED FRACTIONAL DIVIDE OF R_2, R_3 INTO R_0, R_1 , BOTH DOUBLE-PRECISION POSITIVE FRACTIONS | |
| ENTRY POINT: FDE3 ENTRY CONDITIONS: $R_0, R_1 =$ POSITIVE DIVIDEND $R_2, R_3 =$ POSITIVE DIVISOR EXIT CONDITIONS: $R_0, R_1 =$ QUOTIENT $R_2, R_3 =$ REMAINDER SELF = 0 EXECUTION TIME: $510R + 97W = 2578N$ | |
| TEMPORARY LOCATIONS USED: 00E0, 00EC-00EF SUBROUTINES CALLED: NONE STACK WORDS NEEDED: 0 (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. | |

| | |
|--|-----------------|
| SUBROUTINE: DOUBLE PRECISION SQUARE | LABEL: DPSQUARE |
| DESCRIPTION: SQUARES THE DOUBLE-PRECISION NUMBER IN R ₀ , R ₁ | |
| ENTRY POINT: FCCD ENTRY CONDITIONS: R ₀ , R ₁ = X EXIT CONDITIONS: R ₀ , R ₁ = X ² R ₂ , R ₃ ALTERED EXECUTION TIME: 202R + 8W + 1137N | |
| TEMPORARY LOCATIONS USED: 00E0, 00E1, 00EE, 00EF SUBROUTINES CALLED: DPMULT, QUAD, MULT, DPCOMP, DSHL STACK WORDS NEEDED: 4 (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSED ARE EXPRESSED IN HEXADECIMAL NOTATION. | |

| | |
|--|---------------|
| SUBROUTINE: DOUBLE PRECISION COMPLEMENT | LABEL: DPCOMP |
| DESCRIPTION: COMPUTES TWOS COMPLEMENT OF A DOUBLE-PRECISION NUMBER | |
| ENTRY POINT: FDDB ENTRY CONDITIONS: R ₀ , R ₁ = X EXIT CONDITIONS: R ₀ , R ₁ = TWOS COMPLEMENT OF X R ₂ , R ₃ PRESERVED SELFF = 0 EXECUTION TIME: 16R + 53N | |
| TEMPORARY LOCATIONS USED: NONE SUBROUTINES CALLED: NONE STACK WORDS NEEDED: 0 (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. | |

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|---|-------------|
| SUBROUTINE: DOUBLE PRECISION ARITHMETIC SHIFT | LABEL: DPSH |
| DESCRIPTION: SHIFTS A DOUBLE-PRECISION NUMBER TO RIGHT OR LEFT AS SPECIFIED BY R_2 . ABSOLUTE VALUE OF R_2 INDICATES NUMBER OF BITS TO SHIFT. POSITIVE R_2 INDICATES LEFT SHIFT; NEGATIVE R_2 MEANS RIGHT SHIFT. | |
| ENTRY POINT: Fddb ENTRY CONDITIONS: $R_0, R_1 = X$ $R_2 = M$ (SHIFT COUNT) EXIT CONDITIONS: $R_0, R_1 =$ SHIFTED X $R_2 =$ ALTERED R_3 PRESERVED EXECUTION TIME: LEFT $5R + 20N + [8R + 32N]$ M RIGHT $7R + 26N + [4R + 21N]$ M | |
| TEMPORARY LOCATIONS USED: NONE SUBROUTINES CALLED: NONE STACK WORDS NEEDED: 0 (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. RIGHT SHIFT IS ARITHMETIC; THAT IS, SIGN BIT IS PRESERVED | |

| | |
|---|--------------|
| SUBROUTINE: DOUBLE PRECISION ARITHMETIC SHIFT RIGHT | LABEL: DPSHR |
| DESCRIPTION: SHIFTS DOUBLE-PRECISION NUMBER RIGHT M BITS, WHERE $R_2 = M$ | |
| ENTRY POINT: FDCE ENTRY CONDITIONS: $R_0, R_1 = X$ $R_2 = M$ (BITS TO SHIFT) EXIT CONDITIONS: $R_0, R_1 =$ RIGHT SHIFTED X R_2 ALTERED R_3 PRESERVED EXECUTION TIME: $5R + 20N + (4R + 21N)$ M | |
| TEMPORARY LOCATIONS USED: NONE SUBROUTINES CALLED: NONE STACK WORDS NEEDED: 0 (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. SIGN BIT IS PRESERVED | |

| | |
|--|--------------|
| SUBROUTINE: DOUBLE PRECISION SHIFT LEFT | LABEL: DPSHL |
| DESCRIPTION: SHIFTS DOUBLE-PRECISION NUMBER LEFT M BITS, WHERE $R_2 = M$ | |
| ENTRY POINT: FDDB ENTRY CONDITIONS: $R_0, R_1 = X$ $R_2 = M$ (NUMBER OF BITS TO SHIFT) EXIT CONDITIONS: $R_0, R_1 =$ LEFT SHIFTED X R_2 ALTERED R_3 PRESERVED EXECUTION TIME: $5R + 20N + (8R + 32N) M$ | |
| TEMPORARY LOCATIONS USED: NONE SUBROUTINES CALLED: NONE STACK WORDS NEEDED: 0 (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. | |

| | | | | | | | | | | | | | | | | |
|---|--|-------|-------|-------|----------|---|---|---|---|---|---|---|---|---|---|---|
| SUBROUTINE: QUADRANT TESTS | LABEL: QUAD | | | | | | | | | | | | | | | |
| DESCRIPTION: GIVEN TWO SIGNED DOUBLE-PRECISION NUMBERS C1 AND C2, THE INITIAL SIGN OF EACH IS INDICATED BY A FLAG IN MEMORY AND THE ABSOLUTE VALUE OF THE NUMBERS IS GIVEN. | | | | | | | | | | | | | | | | |
| ENTRY POINT: FDAO ENTRY CONDITIONS: $R_0, R_1 = C_1$ $R_2, R_3 = C_2$ EXIT CONDITIONS: $R_0, R_1 = \text{ABS}(C_1)$ $R_2, R_3 = \text{ABS}(C_2)$ | | | | | | | | | | | | | | | | |
| EXECUTION TIME: $47R + W + 175N$ | <table style="display: inline-table; border-collapse: collapse;"> <tr> <td style="border-right: 1px solid black; padding: 0 5px;"></td> <td style="padding: 0 5px;">C_1</td> <td style="padding: 0 5px;">C_2</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 0 5px;">00E1 = 0</td> <td style="padding: 0 5px;">+</td> <td style="padding: 0 5px;">+</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 0 5px;">1</td> <td style="padding: 0 5px;">+</td> <td style="padding: 0 5px;">-</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 0 5px;">2</td> <td style="padding: 0 5px;">-</td> <td style="padding: 0 5px;">-</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 0 5px;">3</td> <td style="padding: 0 5px;">-</td> <td style="padding: 0 5px;">+</td> </tr> </table> <p style="margin-left: 100px;">WHERE ZERO IS +</p> | | C_1 | C_2 | 00E1 = 0 | + | + | 1 | + | - | 2 | - | - | 3 | - | + |
| | C_1 | C_2 | | | | | | | | | | | | | | |
| 00E1 = 0 | + | + | | | | | | | | | | | | | | |
| 1 | + | - | | | | | | | | | | | | | | |
| 2 | - | - | | | | | | | | | | | | | | |
| 3 | - | + | | | | | | | | | | | | | | |
| TEMPORARY LOCATIONS USED: 00E1 SUBROUTINES CALLED: DPCOMP STACK WORDS NEEDED: 1 (MAXIMUM DEPTH) | | | | | | | | | | | | | | | | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. | | | | | | | | | | | | | | | | |

| | |
|---|------------|
| SUBROUTINE: SINE | LABEL: SIN |
| <p>DESCRIPTION: CALCULATES SINE OF DOUBLE-PRECISION ANGLE IN R₀, R₁ CALCULATION IS MADE: $\text{SIN}(X) = \text{COS}(X - \pi/2)$ ACCURACY IS 0.00000 0002₍₁₀₎</p> | |
| <p>ENTRY POINT: FCFA ENTRY CONDITIONS: R₀, R₁ = X EXIT CONDITIONS: R₀, R₁ = SIN(X) R₂, R₃ ALTERED EXECUTION TIME: 1697R + 82W + 9300 N</p> | |
| <p>TEMPORARY LOCATIONS USED: 00E0-00EB, 00EE, 00EF SUBROUTINES CALLED: DPCOMP, DPMULT, PEXPN STACK WORDS NEEDED: 6 (MAXIMUM DEPTH)</p> | |
| <p>COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION.</p> | |

| | |
|--|------------|
| SUBROUTINE: COSINE | LABEL: COS |
| <p>DESCRIPTION: CALCULATES COSINE OF DOUBLE-PRECISION ANGLE IN R₀, R₁ POLYNOMIAL APPROXIMATION USED IS: $\text{COS}(X) = 1 + X^2 (A_2 + X^2 (A_4 + X^2 (A_6 + X^2 (A_8 + X^2 (A_{10}))))))$ WHERE: A₂ = -0.49999 99963 A₈ = 0.00002 47609 A₄ = 0.04166 66418 A₁₀ = -0.00000 02605 A₆ = -0.00138 88397 FOR ANGLES IN THE FIRST QUADRANT ACCURACY IS 0.00000 0002₍₁₀₎</p> | |
| <p>ENTRY POINT: FCFC ENTRY CONDITIONS: R₀, R₁ = X EXIT CONDITIONS: R₀, R₁ = COS(X) R₂, R₃ ALTERED EXECUTION TIME: 1677R + 82W + 9285N</p> | |
| <p>TEMPORARY LOCATIONS USED: 00E0-00EB, 00EE, 00EF SUBROUTINES CALLED: DPCOMP, DPMULT, PEXPN STACK WORDS NEEDED: 6 (MAXIMUM DEPTH)</p> | |
| <p>COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION.</p> | |

| | | | | | | | | | |
|---|-----------------------------|--------------------------|-----------------------------|-------------------------|----------------------------|--------------------------|-----------------------------|-------------------------|----------------------------|
| SUBROUTINE: ARCTANGENT | LABEL: ARCTAN | | | | | | | | |
| <p>DESCRIPTION: COMPUTES ARCTANGENT (C1/C2), WHERE C1 AND C2 ARE DOUBLE-PRECISION NUMBERS IN THE RANGE:</p> $-1 \leq C1, C2 \leq 1$ <p>THE POLYNOMIAL APPROXIMATION USED WAS:</p> $\text{ARCTAN}(X) = X (1 + X^2 (A_2 + X^2 (A_4 + X^2 (A_6 + X^2 (A_8 + X^2 (A_{10} + X^2 (A_{12} + X^2 (A_{14} + X^2 (A_{16})))))))))) \quad \text{WHERE}$ <table data-bbox="418 562 1096 709"> <tr> <td>$A_2 = -0.33333 \ 14528$</td> <td>$A_{10} = -0.07528 \ 96400$</td> </tr> <tr> <td>$A_4 = 0.19993 \ 55085$</td> <td>$A_{12} = 0.04290 \ 96138$</td> </tr> <tr> <td>$A_6 = -0.14208 \ 89944$</td> <td>$A_{14} = -0.01616 \ 57367$</td> </tr> <tr> <td>$A_8 = 0.10656 \ 26393$</td> <td>$A_{16} = 0.00286 \ 62257$</td> </tr> </table> <p>ACCURACY IS 0.00000 002(10)</p> | | $A_2 = -0.33333 \ 14528$ | $A_{10} = -0.07528 \ 96400$ | $A_4 = 0.19993 \ 55085$ | $A_{12} = 0.04290 \ 96138$ | $A_6 = -0.14208 \ 89944$ | $A_{14} = -0.01616 \ 57367$ | $A_8 = 0.10656 \ 26393$ | $A_{16} = 0.00286 \ 62257$ |
| $A_2 = -0.33333 \ 14528$ | $A_{10} = -0.07528 \ 96400$ | | | | | | | | |
| $A_4 = 0.19993 \ 55085$ | $A_{12} = 0.04290 \ 96138$ | | | | | | | | |
| $A_6 = -0.14208 \ 89944$ | $A_{14} = -0.01616 \ 57367$ | | | | | | | | |
| $A_8 = 0.10656 \ 26393$ | $A_{16} = 0.00286 \ 62257$ | | | | | | | | |
| <p>ENTRY POINT: FD37</p> <p>ENTRY CONDITIONS: $R_0, R_1 = C_1 \quad R_2, R_3 = C_2$</p> <p>EXIT CONDITIONS: $R_0, R_1 = \text{ARCTAN}(C_1/C_2) \quad R_2, R_3 \text{ ALTERED}$</p> <p>EXECUTION TIME: 2985R + 231W + 15892N</p> | | | | | | | | | |
| <p>TEMPORARY LOCATIONS USED: 00E0-00EF</p> <p>SUBROUTINES CALLED: QUAD, DPCOMP, DPDIV, DPMUL, PEXPN, DSHR</p> <p>STACK WORDS NEEDED: 7</p> <p>(MAXIMUM DEPTH)</p> | | | | | | | | | |
| <p>COMMENTS: 1. ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION.</p> <p>2. SINGULARITY CASE WHERE $C1 = C2 = 0$ YIELDS $\text{ARCTAN}(C1/C2) = 0$.</p> | | | | | | | | | |

| | |
|---|--------------|
| SUBROUTINE: FLOATING POINT ADD | LABEL: FPADD |
| DESCRIPTION: ADDS TWO FLOATING-POINT NUMBERS. | |
| <p>ENTRY POINT: FC30</p> <p>ENTRY CONDITIONS: $R_0, R_1 = X \quad R_2, R_3 = Y$</p> <p>EXIT CONDITIONS: $R_0, R_1 = X + Y \quad R_2, R_3 \text{ ALTERED}$</p> <p>EXECUTION TIME: 147R + 7W + 613N</p> | |
| <p>TEMPORARY LOCATIONS USED: 00E0, 00E1, 00E2</p> <p>SUBROUTINES CALLED: EXTEXP, DSHR, CZERO, ADDEXP</p> <p>STACK WORDS NEEDED: 1</p> <p>(MAXIMUM DEPTH)</p> | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. | |

| | |
|---|--------------|
| SUBROUTINE: FLOATING POINT MULTIPLY | LABEL: FPMUL |
| DESCRIPTION: MULTIPLIES TWO FLOATING-POINT NUMBERS | |
| ENTRY POINT: FC5D ENTRY CONDITIONS: $R_0, R_1 = X$ $R_2, R_3 = Y$ EXIT CONDITIONS: $R_0, R_1 = X * Y$ R_2, R_3 ALTERED EXECUTION TIME: $1215R + 63W + 5077N$ | |
| TEMPORARY LOCATIONS USED: 00E0, 00E1, 00E5, 00E6, 00EE, 00EF SUBROUTINES CALLED: DLNORM, DPMUL, ADDEXP, CZERO STACK WORDS NEEDED: 4 (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. | |

| | |
|--|--------------|
| SUBROUTINE: POSITIVE FLOATING POINT DIVIDE | LABEL: FPDIV |
| DESCRIPTION: DIVIDES TWO POSITIVE FLOATING-POINT NUMBERS | |
| ENTRY POINT: FC6C ENTRY CONDITIONS: $R_0, R_1 = X$ $R_2, R_3 = Y$ EXIT CONDITIONS: $R_0, R_1 = X/Y$ EXECUTION TIME: $1540R + 152W + 6584N$ | |
| TEMPORARY LOCATIONS USED: 00E0, 00E1, 00E2, 00E5, 00E6, 00EC, 00ED, 00EE, 00EF SUBROUTINES CALLED: DLNORM, DSHR, DPDIV, ADDEXP, CZERO STACK WORDS NEEDED: 4 (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. | |

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|--|---------------|
| SUBROUTINE: FLOATING POINT COMPLEMENT | LABEL: FPCOMP |
| DESCRIPTION: COMPLEMENTS A FLOATING-POINT NUMBER IN R ₀ , R ₁ | |
| ENTRY POINT: FCB9 ENTRY CONDITIONS: R ₀ = X ₁ R ₁ = X ₂ , EX EXIT CONDITIONS: R ₀ = $\overline{X_1}$ R ₁ = $\overline{X_2}$, EX R ₂ , R ₃ PRESERVED EXECUTION TIME: 50R + 2W + 183N | |
| TEMPORARY LOCATIONS USED: 00E0 SUBROUTINES CALLED: EXTEXP, DPCOMP, ADDEXP STACK WORDS NEEDED: 1 (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. | |

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|--|--------------|
| SUBROUTINE: CHECK ZERO EXPONENT | LABEL: CZERO |
| DESCRIPTION: IF MANTISSA OF A FLOATING-POINT NUMBER IS ZERO, EXPONENT IS FORCED TO ZERO. | |
| ENTRY POINT: FC63 ENTRY CONDITIONS: R ₀ , R ₁ = X ₁ , X ₂ (EX) EXIT CONDITIONS: IF X ₁ , X ₂ = 0 R ₀ , R ₁ = 0,0(0) IF X ₁ , X ₂ ≠ 0 R ₀ , R ₂ = X ₁ , X ₂ (EX) } R ₂ , R ₃ PRESERVED EXECUTION TIME: 36R + 2W + 139N | |
| TEMPORARY LOCATIONS USED: 00E0 SUBROUTINES CALLED: EXTEXP, ADDEXP STACK WORDS NEEDED: 1 (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. | |

| | | |
|---|--|---------------|
| SUBROUTINE: EXTRACT EXPONENT TO STACK | | LABEL: EXTEXP |
| DESCRIPTION: EXTRACTS EXPONENT FROM A FLOATING-POINT NUMBER, STORES EXPONENT ON STACK, AND CLEARS EXPONENT FIELD OF NUMBER. | | |
| ENTRY POINT: | FC7C | |
| ENTRY CONDITIONS: | R ₀ , R ₁ = X ₁ , X ₂ (EX) | |
| EXIT CONDITIONS: | R ₀ , R ₁ = X ₁ , X ₂ (0) STACK = EX R ₂ , R ₃ PRESERVED | |
| EXECUTION TIME: | 13R + W + 51N | |
| TEMPORARY LOCATIONS USED: | 00E0 | |
| SUBROUTINES CALLED: | NONE | |
| STACK WORDS NEEDED: | 0 | |
| (MAXIMUM DEPTH) | | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. | | |

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|---|---|---------------|
| SUBROUTINE: ADD EXPONENT FROM STACK | | LABEL: ADDEXP |
| DESCRIPTION: AN EXPONENT IN THE STACK IS PLACED IN A FLOATING-POINT WORD IN R ₀ , R ₁ . | | |
| <p>The diagram illustrates the state of registers and the stack before and after the ADDEXP subroutine. BEFORE: Register R₀ contains X₁. Register R₁ contains X₂ and X₃. The STACK contains EX and NEXT. AFTER: Register R₀ contains X₁. Register R₁ contains X₂ and EX. The STACK contains NEXT₁ and NEXT₂. An arrow indicates that the value EX from the STACK is moved into the EX field of register R₁.</p> | | |
| ENTRY POINT: | FCBD | |
| ENTRY CONDITIONS: | R ₀ , R ₁ = X ₁ , X ₂ (X ₃) STACK = EX | |
| EXIT CONDITIONS: | R ₀ , R ₁ = X ₁ , X ₂ (EX) R ₂ , R ₃ PRESERVED | |
| EXECUTION TIME: | 13R + W + 51N | |
| TEMPORARY LOCATIONS USED: | N 00E0 | |
| SUBROUTINES CALLED: | NONE | |
| STACK WORDS NEEDED: | 1 FOR INPUT EXPONENT ONLY | |
| (MAXIMUM DEPTH) | | |
| COMMENTS: 1. ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. 2. <u>WARNING</u> : ACCESS THIS SUBROUTINE ONLY BY A JSR INSTRUCTION! | | |

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| SUBROUTINE: FRACTIONAL TO FLOATING POINT | LABEL: FLOAT |
| DESCRIPTION: CONVERTS DOUBLE-PRECISION FRACTIONAL NUMBER TO FLOATING-POINT FORMAT BY TRUNCATING LEAST SIGNIFICANT 8 BITS. | |
| ENTRY POINT: FC85 ENTRY CONDITIONS: $R_0, R_1 = X_1, X_2$ EXIT CONDITIONS: $R_0, R_1 = X_1, X_2' (0)$ R_2, R_3 PRESERVED EXECUTION TIME: $3R + 9N$ | |
| TEMPORARY LOCATIONS USED: NONE SUBROUTINES CALLED: NONE STACK WORDS NEEDED: NONE (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. | |

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| SUBROUTINE: FLOATING POINT TO FRACTIONAL | LABEL: SFO |
| DESCRIPTION: CONVERTS A FLOATING-POINT NUMBER TO A FRACTIONAL DOUBLE-PRECISION NUMBER | |
| <p style="text-align: center;"> R_0 R_1 <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="border: 1px solid black; padding: 5px; text-align: center;">X₁</div> <div style="border: 1px solid black; padding: 5px; text-align: center;">X₂ EX</div> </div> <div style="display: flex; justify-content: space-around; margin-top: 5px;"> MANTISSA EXPONENT </div> <p style="text-align: right;">BEFORE</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="border: 1px solid black; padding: 5px; text-align: center;">X</div> <div style="border: 1px solid black; padding: 5px; text-align: center;">X</div> </div> <div style="display: flex; justify-content: center; margin-top: 5px;"> DOUBLE PRECISION </div> <p style="text-align: right;">AFTER</p> </p> | |
| ENTRY POINT: FCC7 ENTRY CONDITIONS: $R_0, R_1 = X_1, X_2 (EX)$ EXIT CONDITIONS: $R_0, R_1 = X$ DOUBLE PREC. R_2, R_3 PRESERVED EXECUTION TIME: $207R + W + 822N$ | |
| TEMPORARY LOCATIONS USED: 00E0 SUBROUTINES CALLED: EXTEXP, DSH STACK WORDS NEEDED: 2 (MAXIMUM DEPTH) | |
| COMMENTS: ALL ADDRESSES ARE EXPRESSED IN HEXADECIMAL NOTATION. CAUTION: VALUE OF INPUT MUST BE < 1.0 IN MAGNITUDE. | |



National Semiconductor Corporation
2900 Semiconductor Drive
Santa Clara, California 95051
(408) 732-5000
TWX: 910-339-9240

NS Electronics SDN BHD
Batu Berendam
Free Trade Zone
Malacca, Malaysia
Telephone: 5171
Telex: NSELECT 519 MALACCA (c/o Kuala Lumpur)

National Semiconductor GmbH
D 808 Fuerstenfeldbruck
Industriestrasse 10
West Germany
Telephone: (08141) 1371
Telex: 05-27649

National Semiconductor (UK) Ltd.
Larkfield Industrial Estate
Greenock, Scotland
Telephone: GOUROCK 33251
Telex: 778 632

NS Electronics (PTE) Ltd.
No. 1100 Lower Delta Rd.
Singapore 3
Telephone: 630011
Telex: NATSEMI RS 21402

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Telephone: 02-478-3400
Telex: 61 007 NatSem B

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Downview, Ontario
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1051 Copenhagen
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Telex: 160 39

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ENGLAND

NATIONAL SEMICONDUCTOR (UK) LTD.
The Precinct
Broxbourne, Hertfordshire
EN 107 HY
England
Telephone: Hoddesdon 69571
Telex: 267-204

FRANCE

NATIONAL SEMICONDUCTOR FRANCE
EXPANSION 10000
28 rue de la Redoute
92-260 Fountenay Aux Roses
Telephone: 660.81.40
Telex: NSF 25956F+

GERMANY

NATIONAL SEMICONDUCTOR GmbH
8000 Munchen 81
Cosimastr. 4/1
Telephone: 089/915027
Telex: 05-22772

HONG KONG

NS ELECTRONICS (HONG KONG) Ltd.
11th Floor
4 Hing Yip Street
Kwun Tong
Kowloon, Hong Kong
Telephone: 3-411241-8
Telex: 73866 NSE HK HX
Cable: NATSEMI

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5925 Forest Lane, Suite 205
Dallas, Texas 75230
(214) 233-6801
TWX: 910-860-5091

WASHINGTON

DISTRICT OFFICE
300 120th Avenue N.E.
Building 2, Suite 205
Bellevue, Washington 98005
(206) 454-4600

ITALY

NATIONAL SEMICONDUCTOR ITALY
Via Valassina 24
20159 Milano
Telephone: (02) 688 4617
Telex: 36-540

JAPAN

*NATIONAL SEMICONDUCTOR JAPAN
Nakazawa Building
1-19 Yotsuya, Shinjuku-Ku 160
Tokyo, Japan
Telephone: 03-359-4571
Telex: J 28592

SWEDEN

NATIONAL SEMICONDUCTOR SWEDEN
Sikvagen 17
13500 Tyreso-Stockholm
Telephone: 08/7 1204 80
Telex: 11293

TAIWAN

NS ELECTRONICS (HK) LTD.
TAIWAN LIAISON OFFICE
#60 Teh Hwei Street
P.O. Box 68-332
Taipei Taiwan ROC
Telephone: 563354
Cable: NSTW TAIPEI