Dear Reader,

Many of you have provided feedback on earlier editions of this book, and your comments and suggestions have greatly improved the book. This edition has been substantially enhanced in presentation, organization, examples, exercises, and supplements. The new edition:

- Replaces Swing with JavaFX. JavaFX is a new framework for developing Java GUI programs. JavaFX greatly simplifies GUI programming and is easier to learn than Swing.
- Introduces exception handling, abstract classes, and interfaces before GUI programming to enable the GUI chapters to be skipped completely if the instructor chooses not to cover GUI.
- Covers introductions to objects and strings earlier in Chapter 4 to enable students to use objects and strings to develop interesting programs early.
- Includes many new interesting examples and exercises to stimulate student interests. More than 100 additional programming exercises are provided to instructors only on the Companion Website.

Please visit www.pearsonhighered.com/liang for a complete list of new features as well as correlations to the previous edition.

The book is fundamentals first by introducing basic programming concepts and techniques before designing custom classes. The fundamental concepts and techniques of selection statements, loops, methods, and arrays are the foundation for programming. Building this strong foundation prepares students to learn object-oriented programming and advanced Java programming.

This book teaches programming in a problem-driven way that focuses on problem solving rather than syntax. We make introductory programming interesting by using thought-provoking problems in a broad context. The central thread of early chapters is on problem solving. Appropriate syntax and library are introduced to enable readers to write programs for solving the problems. To support the teaching of programming in a problem-driven way, the book provides a wide variety of problems at various levels of difficulty to motivate students. To appeal to students in all majors, the problems cover many application areas, including math, science, business, financial, gaming, animation, and multimedia.

The book seamlessly integrates programming, data structures, and algorithms into one text. It employs a practical approach to teach data structures. We first introduce how to use various data structures to develop efficient algorithms, and then show how to implement these data structures. Through implementation, students gain a deep understanding on the efficiency of data structures and on how and when to use certain data structures. Finally we design and implement custom data structures for trees and graphs.

The book is widely used in the introductory programming, data structures, and algorithms courses in the universities around the world. This comprehensive version covers fundamentals of programming, object-oriented programming, GUI programming, data structures, algorithms, concurrency, networking, database, and Web programming. It is designed to prepare students to become proficient Java programmers. A brief version (Introduction to Java Programming, Brief Version, Tenth Edition) is available for a first course on programming, commonly known as CS1. The brief version contains the first 18 chapters of the comprehensive version. The first 13 chapters are appropriate for preparing the AP Computer Science exam.

The best way to teach programming is by example, and the only way to learn programming is by doing. Basic concepts are explained by example and a large number of exercises...
with various levels of difficulty are provided for students to practice. For our programming courses, we assign programming exercises after each lecture.

Our goal is to produce a text that teaches problem solving and programming in a broad context using a wide variety of interesting examples. If you have any comments on and suggestions for improving the book, please email me.

Sincerely,

Y. Daniel Liang
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ACM/IEEE Curricular 2013 and ABET Course Assessment

The new ACM/IEEE Computer Science Curricular 2013 defines the Body of Knowledge organized into 18 Knowledge Areas. To help instructors design the courses based on this book, we provide sample syllabi to identify the Knowledge Areas and Knowledge Units. The sample syllabi are for a three semester course sequence and serve as an example for institutional customization. The sample syllabi are available to instructors at www.pearsonhighered.com/liang.

Many of our users are from the ABET-accredited programs. A key component of the ABET accreditation is to identify the weakness through continuous course assessment against the course outcomes. We provide sample course outcomes for the courses and sample exams for measuring course outcomes on the instructor Website accessible from www.pearsonhighered.com/liang.

What’s New in This Edition?

This edition is completely revised in every detail to enhance clarity, presentation, content, examples, and exercises. The major improvements are as follows:

■ Updated to Java 8.
■ Since Swing is replaced by JavaFX, all GUI examples and exercises are revised using JavaFX.
■ Lambda expressions are used to simplify coding in JavaFX and threads.
■ More than 100 additional programming exercises with solutions are provided to the instructor on the Companion Website. These exercises are not printed in the text.
■ Math methods are introduced earlier in Chapter 4 to enable students to write code using math functions.
■ Strings are introduced earlier in Chapter 4 to enable students to use objects and strings to develop interesting programs early.
■ The GUI chapters are moved to after abstract classes and interfaces so that these chapters can be easily skipped if the instructor chooses not to cover GUI.
■ Chapters 4, 14, 15, and 16 are brand new chapters.
■ Chapters 28 and 29 have been substantially revised with simpler implementations for minimum spanning trees and shortest paths.
Pedagogical Features

The book uses the following elements to help students get the most from the material:

- **Objectives** at the beginning of each chapter list what students should learn from the chapter. This will help them determine whether they have met the objectives after completing the chapter.

- **Introduction** opens the discussion with representative problems to give the reader an overview of what to expect from the chapter.

- **Key Points** highlight the important concepts covered in each section.

- **Check Points** provide review questions to help students track their progress as they read through the chapter and evaluate their learning.

- **Problems and Case Studies**, carefully chosen and presented in an easy-to-follow style, teach problem solving and programming concepts. The book uses many small, simple, and stimulating examples to demonstrate important ideas.

- **Chapter Summary** reviews the important subjects that students should understand and remember. It helps them reinforce the key concepts they have learned in the chapter.

- **Quizzes** are accessible online, grouped by sections, for students to do self-test on programming concepts and techniques.

- **Programming Exercises** are grouped by sections to provide students with opportunities to apply the new skills they have learned on their own. The level of difficulty is rated as easy (no asterisk), moderate (*), hard (**), or challenging (**). The trick of learning programming is practice, practice, and practice. To that end, the book provides a great many exercises. Additionally, more than 100 programming exercises with solutions are provided to the instructors on the Companion Website. These exercises are not printed in the text.

- **Notes, Tips, Cautions**, and **Design Guides** are inserted throughout the text to offer valuable advice and insight on important aspects of program development.

  - **Note**
    Provides additional information on the subject and reinforces important concepts.

  - **Tip**
    Teaches good programming style and practice.

  - **Caution**
    Helps students steer away from the pitfalls of programming errors.

  - **Design Guide**
    Provides guidelines for designing programs.

Flexible Chapter Orderings

The book is designed to provide flexible chapter orderings to enable GUI, exception handling, recursion, generics, and the Java Collections Framework to be covered earlier or later. The diagram on the next page shows the chapter dependencies.
Preface

Chapter 1 Introduction to Computers, Programs, and Java
Chapter 2 Elementary Programming
Chapter 3 Selections
Chapter 4 Mathematical Functions, Characters, and Strings
Chapter 5 Loops
Chapter 6 Methods
Chapter 7 Single-Dimensional Arrays
Chapter 8 Multidimensional Arrays
Chapter 9 Objects and Classes
Chapter 10 Thinking in Objects
Chapter 11 Inheritance and Polymorphism
Chapter 12 Exception Handling and Text I/O
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Chapter 15 Event-Driven Programming and Animations
Chapter 16 JavaFX Controls and Multimedia
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Chapter 18 Recursion
Chapter 19 Generics
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Chapter 37 Servlets
Chapter 38 JavaServer Pages
Chapter 39 Web Services
Chapter 40 2-4 Trees and B-Trees
Chapter 41 Red-Black Trees
Chapter 42 Testing Using JUnit

Note: Chapters 1–18 are in the brief version of this book.

Note: Chapters 1–33 are in the comprehensive version.

Note: Chapters 34–42 are bonus chapters available from the Companion Website.
Organization of the Book

The chapters can be grouped into five parts that, taken together, form a comprehensive introduction to Java programming, data structures and algorithms, and database and Web programming. Because knowledge is cumulative, the early chapters provide the conceptual basis for understanding programming and guide students through simple examples and exercises; subsequent chapters progressively present Java programming in detail, culminating with the development of comprehensive Java applications. The appendixes contain a mixed bag of topics, including an introduction to number systems, bitwise operations, regular expressions, and enumerated types.

Part I: Fundamentals of Programming (Chapters 1–8)

The first part of the book is a stepping stone, preparing you to embark on the journey of learning Java. You will begin to learn about Java (Chapter 1) and fundamental programming techniques with primitive data types, variables, constants, assignments, expressions, and operators (Chapter 2), selection statements (Chapter 3), mathematical functions, characters, and strings (Chapter 4), loops (Chapter 5), methods (Chapter 6), and arrays (Chapters 7–8). After Chapter 7, you can jump to Chapter 18 to learn how to write recursive methods for solving inherently recursive problems.

Part II: Object-Oriented Programming (Chapters 9–13, and 17)

This part introduces object-oriented programming. Java is an object-oriented programming language that uses abstraction, encapsulation, inheritance, and polymorphism to provide great flexibility, modularity, and reusability in developing software. You will learn programming with objects and classes (Chapters 9–10), class inheritance (Chapter 11), polymorphism (Chapter 11), exception handling (Chapter 12), abstract classes (Chapter 13), and interfaces (Chapter 13). Text I/O is introduced in Chapter 12 and binary I/O is discussed in Chapter 17.

Part III: GUI Programming (Chapters 14–16 and Bonus Chapter 34)

JavaFX is a new framework for developing Java GUI programs. It is not only useful for developing GUI programs, but also an excellent pedagogical tool for learning object-oriented programming. This part introduces Java GUI programming using JavaFX in Chapters 14–16. Major topics include GUI basics (Chapter 14), container panes (Chapter 14), drawing shapes (Chapter 14), event-driven programming (Chapter 15), animations (Chapter 15), and GUI controls (Chapter 16), and playing audio and video (Chapter 16). You will learn the architecture of JavaFX GUI programming and use the controls, shapes, panes, image, and video to develop useful applications. Chapter 34 covers advanced features in JavaFX.

Part IV: Data Structures and Algorithms (Chapters 18–29 and Bonus Chapters 40–41)

This part covers the main subjects in a typical data structures and algorithms course. Chapter 18 introduces recursion to write methods for solving inherently recursive problems. Chapter 19 presents how generics can improve software reliability. Chapters 20 and 21 introduce the Java Collection Framework, which defines a set of useful API for data structures. Chapter 22 discusses measuring algorithm efficiency in order to choose an appropriate algorithm for applications. Chapter 23 describes classic sorting algorithms. You will learn how to implement several classic data structures lists, queues, and priority queues in Chapter 24. Chapters 25 and 26 introduce binary search trees and AVL trees. Chapter 27 presents hashing and implementing maps and sets using hashing. Chapters 28 and 29 introduce graph applications. The 2-4 trees, B-trees, and red-black trees are covered in Bonus Chapters 40–41.

Part V: Advanced Java Programming (Chapters 30–33 and Bonus Chapters 35–39, 42)

This part of the book is devoted to advanced Java programming. Chapter 30 treats the use of multithreading to make programs more responsive and interactive and introduces parallel programming. Chapter 31 discusses how to write programs that talk with each other from different hosts over the Internet. Chapter 32 introduces the use of Java to develop database
preface

Chapter 33 introduces modern Web application development using JavaServer Faces. Chapter 35 delves into advanced Java database programming. Chapter 36 covers the use of internationalization support to develop projects for international audiences. Chapters 37 and 38 introduce how to use Java servlets and JavaServer Pages to generate dynamic content from Web servers. Chapter 39 discusses Web services. Chapter 42 introduces testing Java programs using JUnit.

Appendixes

This part of the book covers a mixed bag of topics. Appendix A lists Java keywords. Appendix B gives tables of ASCII characters and their associated codes in decimal and in hex. Appendix C shows the operator precedence. Appendix D summarizes Java modifiers and their usage. Appendix E discusses special floating-point values. Appendix F introduces number systems and conversions among binary, decimal, and hex numbers. Finally, Appendix G introduces bitwise operations. Appendix H introduces regular expressions. Appendix I covers enumerated types.

Java Development Tools

You can use a text editor, such as the Windows Notepad or WordPad, to create Java programs and to compile and run the programs from the command window. You can also use a Java development tool, such as NetBeans or Eclipse. These tools support an integrated development environment (IDE) for developing Java programs quickly. Editing, compiling, building, executing, and debugging programs are integrated in one graphical user interface. Using these tools effectively can greatly increase your programming productivity. NetBeans and Eclipse are easy to use if you follow the tutorials. Tutorials on NetBeans and Eclipse can be found under Tutorials on the Student Companion Website at www.pearsonhighered.com/liang.

Student Resource Website

The Student Resource Website www.pearsonhighered.com/liang provides access to some of the following resources. Other resources are available using the student access code printed on the inside front cover of this book. (For students with a used copy of this book, you can purchase access to the premium student resources through www.pearsonhighered.com/liang.)

- Answers to review questions
- Solutions to even-numbered programming exercises
- Source code for the examples in the book
- Interactive quiz (organized by sections for each chapter)
- Supplements
- Debugging tips
- Algorithm animations
- Errata

Instructor Resource Website

The Instructor Resource Website, accessible from www.pearsonhighered.com/liang, provides access to the following resources:

- Microsoft PowerPoint slides with interactive buttons to view full-color, syntax-highlighted source code and to run programs without leaving the slides.
- Solutions to all programming exercises. Students will have access to the solutions of even-numbered programming exercises.
More than 100 additional programming exercises organized by chapters. These exercises are available only to the instructors. Solutions to these exercises are provided.

Web-based quiz generator. (Instructors can choose chapters to generate quizzes from a large database of more than two thousand questions.)

Sample exams. Most exams have four parts:
- Multiple-choice questions or short-answer questions
- Correct programming errors
- Trace programs
- Write programs

ACM/IEEE Curricula 2013. The new ACM/IEEE Computer Science Curricula 2013 defines the Body of Knowledge organized into 18 Knowledge Areas. To help instructors design the courses based on this book, we provide sample syllabi to identify the Knowledge Areas and Knowledge Units. The sample syllabi are for a three semester course sequence and serve as an example for institutional customization. Instructors can access the syllabi at www.pearsonhighered.com/liang.

Sample exams with ABET course assessment.

Projects. In general, each project gives a description and asks students to analyze, design, and implement the project.

Some readers have requested the materials from the Instructor Resource Website. Please understand that these are for instructors only. Such requests will not be answered.

**Online Practice and Assessment with MyProgrammingLab**

MyProgrammingLab helps students fully grasp the logic, semantics, and syntax of programming. Through practice exercises and immediate, personalized feedback, MyProgrammingLab improves the programming competence of beginning students who often struggle with the basic concepts and paradigms of popular high-level programming languages.

A self-study and homework tool, a MyProgrammingLab course consists of hundreds of small practice problems organized around the structure of this textbook. For students, the system automatically detects errors in the logic and syntax of their code submissions and offers targeted hints that enable students to figure out what went wrong—and why. For instructors, a comprehensive gradebook tracks correct and incorrect answers and stores the code inputted by students for review.

MyProgrammingLab is offered to users of this book in partnership with Turing’s Craft, the makers of the CodeLab interactive programming exercise system. For a full demonstration, to see feedback from instructors and students, or to get started using MyProgrammingLab in your course, visit www.myprogramminglab.com.

**VideoNotes**

We are excited about the new VideoNotes feature that is found in this new edition. These videos provide additional help by presenting examples of key topics and showing how to solve problems completely, from design through coding. VideoNotes are available from www.pearsonhighered.com/liang.
Algorithm Animations

We have provided numerous animations for algorithms. These are valuable pedagogical tools to demonstrate how algorithms work. Algorithm animations can be accessed from the Companion Website.

Acknowledgments

I would like to thank Armstrong Atlantic State University for enabling me to teach what I write and for supporting me in writing what I teach. Teaching is the source of inspiration for continuing to improve the book. I am grateful to the instructors and students who have offered comments, suggestions, bug reports, and praise.

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It is a great pleasure, honor, and privilege to work with Pearson. I would like to thank Tracy Johnson and her colleagues Marcia Horton, Yez Alayan, Carole Snyder, Scott Disanno, Bob Engelhardt, Haseen Khan, and their colleagues for organizing, producing, and promoting this project.

As always, I am indebted to my wife, Samantha, for her love, support, and encouragement.
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- Chapter 34 Advanced JavaFX
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INTRODUCTION TO COMPUTERS, PROGRAMS, AND JAVA

Objectives

- To understand computer basics, programs, and operating systems (§§1.2–1.4).
- To describe the relationship between Java and the World Wide Web (§1.5).
- To understand the meaning of Java language specification, API, JDK, and IDE (§1.6).
- To write a simple Java program (§1.7).
- To display output on the console (§1.7).
- To explain the basic syntax of a Java program (§1.7).
- To create, compile, and run Java programs (§1.8).
- To use sound Java programming style and document programs properly (§1.9).
- To explain the differences between syntax errors, runtime errors, and logic errors (§1.10).
- To develop Java programs using NetBeans (§1.11).
- To develop Java programs using Eclipse (§1.12).
1.1 Introduction

The central theme of this book is to learn how to solve problems by writing a program.

This book is about programming. So, what is programming? The term *programming* means to create (or develop) software, which is also called a *program*. In basic terms, software contains the instructions that tell a computer—or a computerized device—what to do.

Software is all around you, even in devices that you might not think would need it. Of course, you expect to find and use software on a personal computer, but software also plays a role in running airplanes, cars, cell phones, and even toasters. On a personal computer, you use word processors to write documents, Web browsers to explore the Internet, and e-mail programs to send and receive messages. These programs are all examples of software. Software developers create software with the help of powerful tools called *programming languages*.

This book teaches you how to create programs by using the Java programming language. There are many programming languages, some of which are decades old. Each language was invented for a specific purpose—to build on the strengths of a previous language, for example, or to give the programmer a new and unique set of tools. Knowing that there are so many programming languages available, it would be natural for you to wonder which one is best. But, in truth, there is no “best” language. Each one has its own strengths and weaknesses. Experienced programmers know that one language might work well in some situations, whereas a different language may be more appropriate in other situations. For this reason, seasoned programmers try to master as many different programming languages as they can, giving them access to a vast arsenal of software-development tools.

If you learn to program using one language, you should find it easy to pick up other languages. The key is to learn how to solve problems using a programming approach. That is the main theme of this book.

You are about to begin an exciting journey: learning how to program. At the outset, it is helpful to review computer basics, programs, and operating systems. If you are already familiar with such terms as CPU, memory, disks, operating systems, and programming languages, you may skip Sections 1.2–1.4.

1.2 What Is a Computer?

A computer is an electronic device that stores and processes data.

A computer includes both *hardware* and *software*. In general, hardware comprises the visible, physical elements of the computer, and software provides the invisible instructions that control the hardware and make it perform specific tasks. Knowing computer hardware isn’t essential to learning a programming language, but it can help you better understand the effects that a program’s instructions have on the computer and its components. This section introduces computer hardware components and their functions.

A computer consists of the following major hardware components (Figure 1.1):

- A central processing unit (CPU)
- Memory (main memory)
- Storage devices (such as disks and CDs)
- Input devices (such as the mouse and keyboard)
- Output devices (such as monitors and printers)
- Communication devices (such as modems and network interface cards)

A computer’s components are interconnected by a subsystem called a *bus*. You can think of a bus as a sort of system of roads running among the computer’s components; data and power travel along the bus from one part of the computer to another. In personal computers,
1.2 What Is a Computer?

The bus is built into the computer’s motherboard, which is a circuit case that connects all of the parts of a computer together.

### 1.2.1 Central Processing Unit

The central processing unit (CPU) is the computer’s brain. It retrieves instructions from memory and executes them. The CPU usually has two components: a control unit and an arithmetic/logic unit. The control unit controls and coordinates the actions of the other components. The arithmetic/logic unit performs numeric operations (addition, subtraction, multiplication, division) and logical operations (comparisons).

Today’s CPUs are built on small silicon semiconductor chips that contain millions of tiny electric switches, called transistors, for processing information.

Every computer has an internal clock, which emits electronic pulses at a constant rate. These pulses are used to control and synchronize the pace of operations. A higher clock speed enables more instructions to be executed in a given period of time. The unit of measurement of clock speed is the hertz (Hz), with 1 hertz equaling 1 pulse per second. In the 1990s, computers measured clocked speed in megahertz (MHz), but CPU speed has been improving continuously; the clock speed of a computer is now usually stated in gigahertz (GHz). Intel’s newest processors run at about 3 GHz.

CPUs were originally developed with only one core. The core is the part of the processor that performs the reading and executing of instructions. In order to increase CPU processing power, chip manufacturers are now producing CPUs that contain multiple cores. A multicore CPU is a single component with two or more independent cores. Today’s consumer computers typically have two, three, and even four separate cores. Soon, CPUs with dozens or even hundreds of cores will be affordable.

### 1.2.2 Bits and Bytes

Before we discuss memory, let’s look at how information (data and programs) are stored in a computer.

A computer is really nothing more than a series of switches. Each switch exists in two states: on or off. Storing information in a computer is simply a matter of setting a sequence of switches on or off. If the switch is on, its value is 1. If the switch is off, its value is 0. These 0s and 1s are interpreted as digits in the binary number system and are called bits (binary digits).

The minimum storage unit in a computer is a byte. A byte is composed of eight bits. A small number such as 3 can be stored as a single byte. To store a number that cannot fit into a single byte, the computer uses several bytes.

Data of various kinds, such as numbers and characters, are encoded as a series of bytes. As a programmer, you don’t need to worry about the encoding and decoding of data, which the computer system performs automatically, based on the encoding scheme. An encoding scheme is a set of rules that govern how a computer translates characters, numbers, and symbols into data the computer can actually work with. Most schemes translate each character...
into a predetermined string of bits. In the popular ASCII encoding scheme, for example, the character C is represented as 01000011 in one byte.

A computer’s storage capacity is measured in bytes and multiples of the byte, as follows:

- A kilobyte (KB) is about 1,000 bytes.
- A megabyte (MB) is about 1 million bytes.
- A gigabyte (GB) is about 1 billion bytes.
- A terabyte (TB) is about 1 trillion bytes.

A typical one-page word document might take 20 KB. Therefore, 1 MB can store 50 pages of documents and 1 GB can store 50,000 pages of documents. A typical two-hour high-resolution movie might take 8 GB, so it would require 160 GB to store 20 movies.

### 1.2.3 Memory

A computer’s memory consists of an ordered sequence of bytes for storing programs as well as data that the program is working with. You can think of memory as the computer’s work area for executing a program. A program and its data must be moved into the computer’s memory before they can be executed by the CPU.

Every byte in the memory has a unique address, as shown in Figure 1.2. The address is used to locate the byte for storing and retrieving the data. Since the bytes in the memory can be accessed in any order, the memory is also referred to as random-access memory (RAM).

![Memory stores data and program instructions in uniquely addressed memory locations.](image)

Today’s personal computers usually have at least 4 gigabyte of RAM, but they more commonly have 6 to 8 GB installed. Generally speaking, the more RAM a computer has, the faster it can operate, but there are limits to this simple rule of thumb.

A memory byte is never empty, but its initial content may be meaningless to your program. The current content of a memory byte is lost whenever new information is placed in it.

Like the CPU, memory is built on silicon semiconductor chips that have millions of transistors embedded on their surface. Compared to CPU chips, memory chips are less complicated, slower, and less expensive.

### 1.2.4 Storage Devices

A computer’s memory (RAM) is a volatile form of data storage: any information that has been stored in memory (i.e., saved) is lost when the system’s power is turned off. Programs and data are permanently stored on storage devices and are moved, when the computer
1.2 What Is a Computer?

Actually uses them, to memory, which operates at much faster speeds than permanent storage devices can.

There are three main types of storage devices:

- Magnetic disk drives
- Optical disc drives (CD and DVD)
- USB flash drives

*Drives* are devices for operating a medium, such as disks and CDs. A storage medium physically stores data and program instructions. The drive reads data from the medium and writes data onto the medium.

**Disks**

A computer usually has at least one hard disk drive. *Hard disks* are used for permanently storing data and programs. Newer computers have hard disks that can store from 500 gigabytes to 1 terabyte of data. Hard disk drives are usually encased inside the computer, but removable hard disks are also available.

**CDs and DVDs**

*CD* stands for compact disc. There are two types of CD drives: CD-R and CD-RW. A CD-R is for read-only permanent storage; the user cannot modify its contents once they are recorded. A CD-RW can be used like a hard disk; that is, you can write data onto the disc, and then overwrite that data with new data. A single CD can hold up to 700 MB. Most new PCs are equipped with a CD-RW drive that can work with both CD-R and CD-RW discs.

*DVD* stands for digital versatile disc or digital video disc. DVDs and CDs look alike, and you can use either to store data. A DVD can hold more information than a CD; a standard DVD’s storage capacity is 4.7 GB. Like CDs, there are two types of DVDs: DVD-R (read-only) and DVD-RW (rewritable).

**USB Flash Drives**

*Universal serial bus* (USB) connectors allow the user to attach many kinds of peripheral devices to the computer. You can use a USB to connect a printer, digital camera, mouse, external hard disk drive, and other devices to the computer.

A USB *flash drive* is a device for storing and transporting data. A flash drive is small—about the size of a pack of gum. It acts like a portable hard drive that can be plugged into your computer’s USB port. USB flash drives are currently available with up to 256 GB storage capacity.

1.2.5 **Input and Output Devices**

Input and output devices let the user communicate with the computer. The most common input devices are *keyboards* and *mice*. The most common output devices are *monitors* and *printers*.

**The Keyboard**

A keyboard is a device for entering input. Compact keyboards are available without a numeric keypad.

*Function keys* are located across the top of the keyboard and are prefixed with the letter F. Their functions depend on the software currently being used.

A *modifier key* is a special key (such as the Shift, Alt, and Ctrl keys) that modifies the normal action of another key when the two are pressed simultaneously.

The *numeric keypad*, located on the right side of most keyboards, is a separate set of keys styled like a calculator to use for entering numbers quickly.

*Arrow keys*, located between the main keypad and the numeric keypad, are used to move the mouse pointer up, down, left, and right on the screen in many kinds of programs.
The Insert, Delete, Page Up, and Page Down keys are used in word processing and other programs for inserting text and objects, deleting text and objects, and moving up or down through a document one screen at a time.

The Mouse

A *mouse* is a pointing device. It is used to move a graphical pointer (usually in the shape of an arrow) called a *cursor* around the screen or to click on-screen objects (such as a button) to trigger them to perform an action.

The Monitor

The *monitor* displays information (text and graphics). The screen resolution and dot pitch determine the quality of the display.

The *screen resolution* specifies the number of pixels in horizontal and vertical dimensions of the display device. *Pixels* (short for “picture elements”) are tiny dots that form an image on the screen. A common resolution for a 17-inch screen, for example, is 1,024 pixels wide and 768 pixels high. The resolution can be set manually. The higher the resolution, the sharper and clearer the image is.

The *dot pitch* is the amount of space between pixels, measured in millimeters. The smaller the dot pitch, the sharper the display.

### 1.2.6 Communication Devices

Computers can be networked through communication devices, such as a dial-up modem (*modulator/demodulator*), a DSL or cable modem, a wired network interface card, or a wireless adapter.

- **Dial-up modem**: A *dial-up modem* uses a phone line and can transfer data at a speed up to 56,000 bps (bits per second).
- **Digital subscriber line (DSL)**: A *digital subscriber line (DSL)* connection also uses a standard phone line, but it can transfer data 20 times faster than a standard dial-up modem.
- **Cable modem**: A *cable modem* uses the cable TV line maintained by the cable company and is generally faster than DSL.
- **Network interface card (NIC)**: A *network interface card (NIC)* is a device that connects a computer to a *local area network (LAN)*. LANs are commonly used in universities, businesses, and government agencies. A high-speed NIC called *1000BaseT* can transfer data at 1,000 million bits per second (mbps).

Wireless networking is now extremely popular in homes, businesses, and schools. Every laptop computer sold today is equipped with a wireless adapter that enables the computer to connect to a local area network and the Internet.

---

**Note**

Answers to checkpoint questions are on the Companion Website.

1. **Check Point**
   1.1 What are hardware and software?
   1.2 List five major hardware components of a computer.
   1.3 What does the acronym “CPU” stand for?
   1.4 What unit is used to measure CPU speed?
   1.5 What is a bit? What is a byte?
   1.6 What is memory for? What does RAM stand for? Why is memory called RAM?
   1.7 What unit is used to measure memory size?
1.8 What unit is used to measure disk size?
1.9 What is the primary difference between memory and a storage device?

1.3 Programming Languages

*Computer programs, known as software, are instructions that tell a computer what to do.*

Computers do not understand human languages, so programs must be written in a language a computer can use. There are hundreds of programming languages, and they were developed to make the programming process easier for people. However, all programs must be converted into the instructions the computer can execute.

1.3.1 Machine Language

A computer’s native language, which differs among different types of computers, is its *machine language*—a set of built-in primitive instructions. These instructions are in the form of binary code, so if you want to give a computer an instruction in its native language, you have to enter the instruction as binary code. For example, to add two numbers, you might have to write an instruction in binary code, like this:

```
1101101010011010
```

1.3.2 Assembly Language

Programming in machine language is a tedious process. Moreover, programs written in machine language are very difficult to read and modify. For this reason, *assembly language* was created in the early days of computing as an alternative to machine languages. Assembly language uses a short descriptive word, known as a *mnemonic*, to represent each of the machine-language instructions. For example, the mnemonic `add` typically means to add numbers and `sub` means to subtract numbers. To add the numbers 2 and 3 and get the result, you might write an instruction in assembly code like this:

```
add 2, 3, result
```

Assembly languages were developed to make programming easier. However, because the computer cannot execute assembly language, another program—called an *assembler*—is used to translate assembly-language programs into machine code, as shown in Figure 1.3.

![Figure 1.3](image-url) An assembler translates assembly-language instructions into machine code.

Writing code in assembly language is easier than in machine language. However, it is still tedious to write code in assembly language. An instruction in assembly language essentially corresponds to an instruction in machine code. Writing in assembly requires that you know how the CPU works. Assembly language is referred to as *a low-level language*, because assembly language is close in nature to machine language and is machine dependent.
1.3.3 High-Level Language

In the 1950s, a new generation of programming languages known as high-level languages emerged. They are platform independent, which means that you can write a program in a high-level language and run it in different types of machines. High-level languages are English-like and easy to learn and use. The instructions in a high-level programming language are called statements. Here, for example, is a high-level language statement that computes the area of a circle with a radius of 5:

\[
\text{area} = 5 \times 5 \times 3.14159;
\]

There are many high-level programming languages, and each was designed for a specific purpose. Table 1.1 lists some popular ones.

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<td>Named for Ada Lovelace, who worked on mechanical general-purpose computers. The Ada language was developed for the Department of Defense and is used mainly in defense projects.</td>
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<tr>
<td>BASIC</td>
<td>Beginner’s All-purpose Symbolic Instruction Code. It was designed to be learned and used easily by beginners.</td>
</tr>
<tr>
<td>C</td>
<td>Developed at Bell Laboratories. C combines the power of an assembly language with the ease of use and portability of a high-level language.</td>
</tr>
<tr>
<td>C++</td>
<td>C++ is an object-oriented language, based on C.</td>
</tr>
<tr>
<td>C#</td>
<td>Pronounced “C Sharp.” It is a hybrid of Java and C++ and was developed by Microsoft.</td>
</tr>
<tr>
<td>COBOL</td>
<td>COmmon Business Oriented Language. Used for business applications.</td>
</tr>
<tr>
<td>FORTRAN</td>
<td>FORmula TRANslation. Popular for scientific and mathematical applications.</td>
</tr>
<tr>
<td>Java</td>
<td>Developed by Sun Microsystems, now part of Oracle. It is widely used for developing platform-independent Internet applications.</td>
</tr>
<tr>
<td>Pascal</td>
<td>Named for Blaise Pascal, who pioneered calculating machines in the seventeenth century. It is a simple, structured, general-purpose language primarily for teaching programming.</td>
</tr>
<tr>
<td>Python</td>
<td>A simple general-purpose scripting language good for writing short programs.</td>
</tr>
<tr>
<td>Visual Basic</td>
<td>Visual Basic was developed by Microsoft and it enables the programmers to rapidly develop graphical user interfaces.</td>
</tr>
</tbody>
</table>

A program written in a high-level language is called a source program or source code. Because a computer cannot execute a source program, a source program must be translated into machine code for execution. The translation can be done using another programming tool called an interpreter or a compiler.

- An interpreter reads one statement from the source code, translates it to the machine code or virtual machine code, and then executes it right away, as shown in Figure 1.4a. Note that a statement from the source code may be translated into several machine instructions.
- A compiler translates the entire source code into a machine-code file, and the machine-code file is then executed, as shown in Figure 1.4b.

**Check Points**

1.10 What language does the CPU understand?
1.11 What is an assembly language?
1.12 What is an assembler?
1.13 What is a high-level programming language?
1.14 What is a source program?
1.4 Operating Systems

The operating system (OS) is the most important program that runs on a computer. The OS manages and controls a computer’s activities.

The popular operating systems for general-purpose computers are Microsoft Windows, Mac OS, and Linux. Application programs, such as a Web browser or a word processor, cannot run unless an operating system is installed and running on the computer. Figure 1.5 shows the interrelationship of hardware, operating system, application software, and the user.

The major tasks of an operating system are as follows:

- Controlling and monitoring system activities
- Allocating and assigning system resources
- Scheduling operations
Chapter 1  Introduction to Computers, Programs, and Java

1.4.1 Controlling and Monitoring System Activities
Operating systems perform basic tasks, such as recognizing input from the keyboard, sending output to the monitor, keeping track of files and folders on storage devices, and controlling peripheral devices, such as disk drives and printers. An operating system must also ensure that different programs and users working at the same time do not interfere with each other. In addition, the OS is responsible for security, ensuring that unauthorized users and programs are not allowed to access the system.

1.4.2 Allocating and Assigning System Resources
The operating system is responsible for determining what computer resources a program needs (such as CPU time, memory space, disks, input and output devices) and for allocating and assigning them to run the program.

1.4.3 Scheduling Operations
The OS is responsible for scheduling programs’ activities to make efficient use of system resources. Many of today’s operating systems support techniques such as multiprogramming, multithreading, and multiprocessing to increase system performance.

- **Multiprogramming** allows multiple programs to run simultaneously by sharing the same CPU. The CPU is much faster than the computer’s other components. As a result, it is idle most of the time—for example, while waiting for data to be transferred from a disk or waiting for other system resources to respond. A multiprogramming OS takes advantage of this situation by allowing multiple programs to use the CPU when it would otherwise be idle. For example, multiprogramming enables you to use a word processor to edit a file at the same time as your Web browser is downloading a file.

- **Multithreading** allows a single program to execute multiple tasks at the same time. For instance, a word-processing program allows users to simultaneously edit text and save it to a disk. In this example, editing and saving are two tasks within the same application. These two tasks may run concurrently.

- **Multiprocessing**, or parallel processing, uses two or more processors together to perform subtasks concurrently and then combine solutions of the subtasks to obtain a solution for the entire task. It is like a surgical operation where several doctors work together on one patient.

1.18 What is an operating system? List some popular operating systems.
1.19 What are the major responsibilities of an operating system?
1.20 What are multiprogramming, multithreading, and multiprocessing?

1.5 Java, the World Wide Web, and Beyond

*Java is a powerful and versatile programming language for developing software running on mobile devices, desktop computers, and servers.*

This book introduces Java programming. Java was developed by a team led by James Gosling at Sun Microsystems. Sun Microsystems was purchased by Oracle in 2010. Originally called *Oak*, Java was designed in 1991 for use in embedded chips in consumer electronic appliances. In 1995, renamed *Java*, it was redesigned for developing Web applications. For the history of Java, see [www.java.com/en/javahistory/index.jsp](http://www.java.com/en/javahistory/index.jsp).

Java has become enormously popular. Its rapid rise and wide acceptance can be traced to its design characteristics, particularly its promise that you can write a program once and run it anywhere. As stated by its designer, Java is simple, object oriented, distributed,
interpreted, robust, secure, architecture neutral, portable, high performance, multi-threaded, and dynamic. For the anatomy of Java characteristics, see www.cs.armstrong.edu/liang/JavaCharacteristics.pdf.

Java is a full-featured, general-purpose programming language that can be used to develop robust mission-critical applications. Today, it is employed not only for Web programming but also for developing standalone applications across platforms on servers, desktop computers, and mobile devices. It was used to develop the code to communicate with and control the robotic rover on Mars. Many companies that once considered Java to be more hype than substance are now using it to create distributed applications accessed by customers and partners across the Internet. For every new project being developed today, companies are asking how they can use Java to make their work easier.

The World Wide Web is an electronic information repository that can be accessed on the Internet from anywhere in the world. The Internet, the Web’s infrastructure, has been around for more than forty years. The colorful World Wide Web and sophisticated Web browsers are the major reason for the Internet’s popularity.

Java initially became attractive because Java programs can be run from a Web browser. Such programs are called applets. Applets employ a modern graphical interface with buttons, text fields, text areas, radio buttons, and so on, to interact with users on the Web and process their requests. Applets make the Web responsive, interactive, and fun to use. Applets are embedded in an HTML file. HTML (Hypertext Markup Language) is a simple scripting language for laying out documents, linking documents on the Internet, and bringing images, sound, and video alive on the Web. Today, you can use Java to develop rich Internet applications. A rich Internet application (RIA) is a Web application designed to deliver the same features and functions normally associated with desktop applications.

Java is now very popular for developing applications on Web servers. These applications process data, perform computations, and generate dynamic Web pages. Many commercial Websites are developed using Java on the backend.

Java is a versatile programming language: you can use it to develop applications for desktop computers, servers, and small handheld devices. The software for Android cell phones is developed using Java.

1.21 Who invented Java? Which company owns Java now?
1.22 What is a Java applet?
1.23 What programming language does Android use?
Java is a full-fledged and powerful language that can be used in many ways. It comes in three editions:

- **Java Standard Edition (Java SE)** to develop client-side applications. The applications can run standalone or as applets running from a Web browser.
- **Java Enterprise Edition (Java EE)** to develop server-side applications, such as Java servlets, JavaServer Pages (JSP), and JavaServer Faces (JSF).
- **Java Micro Edition (Java ME)** to develop applications for mobile devices, such as cell phones.

This book uses Java SE to introduce Java programming. Java SE is the foundation upon which all other Java technology is based. There are many versions of Java SE. The latest, Java SE 8, is used in this book. Oracle releases each version with a Java Development Toolkit (JDK). For Java SE 8, the Java Development Toolkit is called JDK 1.8 (also known as Java 8 or JDK 8).

The JDK consists of a set of separate programs, each invoked from a command line, for developing and testing Java programs. Instead of using the JDK, you can use a Java development tool (e.g., NetBeans, Eclipse, and TextPad)—software that provides an integrated development environment (IDE) for developing Java programs quickly. Editing, compiling, building, debugging, and online help are integrated in one graphical user interface. You simply enter source code in one window or open an existing file in a window, and then click a button or menu item or press a function key to compile and run the program.

1.24 What is the Java language specification?
1.25 What does JDK stand for?
1.26 What does IDE stand for?
1.27 Are tools like NetBeans and Eclipse different languages from Java, or are they dialects or extensions of Java?

### 1.7 A Simple Java Program

A Java program is executed from the **main** method in the class.

Let’s begin with a simple Java program that displays the message `Welcome to Java!` on the console. (The word **console** is an old computer term that refers to the text entry and display device of a computer. **Console input** means to receive input from the keyboard, and **console output** means to display output on the monitor.) The program is shown in Listing 1.1.

**Listing 1.1 Welcome.java**

```java
public class Welcome {
    public static void main(String[] args) {
        // Display message Welcome to Java! on the console
        System.out.println("Welcome to Java!");
    }
}
```

Welcome to Java!

Note that the line numbers are for reference purposes only; they are not part of the program. So, don’t type line numbers in your program.
Line 1 defines a class. Every Java program must have at least one class. Each class has a name. By convention, class names start with an uppercase letter. In this example, the class name is Welcome.

Line 2 defines the main method. The program is executed from the main method. A class may contain several methods. The main method is the entry point where the program begins execution.

A method is a construct that contains statements. The main method in this program contains the System.out.println statement. This statement displays the string Welcome to Java! on the console (line 4). String is a programming term meaning a sequence of characters. A string must be enclosed in double quotation marks. Every statement in Java ends with a semicolon (;), known as the statement terminator.

Reserved words, or keywords, have a specific meaning to the compiler and cannot be used for other purposes in the program. For example, when the compiler sees the word class, it understands that the word after class is the name for the class. Other reserved words in this program are public, static, and void.

Line 3 is a comment that documents what the program is and how it is constructed. Comments help programmers to communicate and understand the program. They are not programming statements and thus are ignored by the compiler. In Java, comments are preceded by two slashes (//) on a line, called a line comment, or enclosed between /* and */ on one or several lines, called a block comment or paragraph comment. When the compiler sees //, it ignores all text after // on the same line. When it sees /*, it scans for the next */ and ignores any text between /* and */. Here are examples of comments:

// This application program displays Welcome to Java!
/* This application program displays Welcome to Java! */
/* This application program
displays Welcome to Java! */

A pair of curly braces in a program forms a block that groups the program’s components. In Java, each block begins with an opening brace ( { ) and ends with a closing brace ( } ). Every class has a class block that groups the data and methods of the class. Similarly, every method has a method block that groups the statements in the method. Blocks can be nested, meaning that one block can be placed within another, as shown in the following code.

```java
public class Welcome {
    public static void main(String[] args) {
        System.out.println("Welcome to Java!");
    }
}
```

Tip
An opening brace must be matched by a closing brace. Whenever you type an opening brace, immediately type a closing brace to prevent the missing-brace error. Most Java IDEs automatically insert the closing brace for each opening brace.

Caution
Java source programs are case sensitive. It would be wrong, for example, to replace main in the program with Main.

You have seen several special characters (e.g., { }, //, ;) in the program. They are used in almost every program. Table 1.2 summarizes their uses. The most common errors you will make as you learn to program will be syntax errors. Like any programming language, Java has its own syntax, and you need to write code that
conforms to the *syntax rules*. If your program violates a rule—for example, if the semicolon is missing, a brace is missing, a quotation mark is missing, or a word is misspelled—the Java compiler will report syntax errors. Try to compile the program with these errors and see what the compiler reports.

**Note**
You are probably wondering why the `main` method is defined this way and why `System.out.println(...)` is used to display a message on the console. For the time being, simply accept that this is how things are done. Your questions will be fully answered in subsequent chapters.

The program in Listing 1.1 displays one message. Once you understand the program, it is easy to extend it to display more messages. For example, you can rewrite the program to display three messages, as shown in Listing 1.2.

**LISTING 1.2 WelcomeWithThreeMessages.java**

```java
public class WelcomeWithThreeMessages {
    public static void main(String[] args) {
        System.out.println("Programming is fun!");
        System.out.println("Fundamentals First");
        System.out.println("Problem Driven");
    }
}
```

Further, you can perform mathematical computations and display the result on the console. Listing 1.3 gives an example of evaluating $\frac{10.5 + 2 \times 3}{45 - 3.5}$.

**LISTING 1.3 ComputeExpression.java**

```java
public class ComputeExpression {    public static void main(String[] args) {
    System.out.println((10.5 + 2 * 3) / (45 - 3.5));
}
```

![Display of program output](image)
The multiplication operator in Java is \( \times \). As you can see, it is a straightforward process to translate an arithmetic expression to a Java expression. We will discuss Java expressions further in Chapter 2.

1.28 What is a keyword? List some Java keywords.
1.29 Is Java case sensitive? What is the case for Java keywords?
1.30 What is a comment? Is the comment ignored by the compiler? How do you denote a comment line and a comment paragraph?
1.31 What is the statement to display a string on the console?
1.32 Show the output of the following code:

```java
public class Test {
    public static void main(String[] args) {
        System.out.println("3.5 * 4 / 2 - 2.5 is ");
        System.out.println(3.5 * 4 / 2 - 2.5);
    }
}
```

1.8 Creating, Compiling, and Executing a Java Program

You save a Java program in a .java file and compile it into a .class file. The .class file is executed by the Java Virtual Machine.

You have to create your program and compile it before it can be executed. This process is repetitive, as shown in Figure 1.6. If your program has compile errors, you have to modify the program to fix them, and then recompile it. If your program has runtime errors or does not produce the correct result, you have to modify the program, recompile it, and execute it again.

You can use any text editor or IDE to create and edit a Java source-code file. This section demonstrates how to create, compile, and run Java programs from a command window. Sections 1.10 and 1.11 will introduce developing Java programs using NetBeans and Eclipse. From the command window, you can use a text editor such as Notepad to create the Java source-code file, as shown in Figure 1.7.

Note
The source file must end with the extension .java and must have the same exact name as the public class name. For example, the file for the source code in Listing 1.1 should be named Welcome.java, since the public class name is Welcome.

A Java compiler translates a Java source file into a Java bytecode file. The following command compiles Welcome.java:

```
javac Welcome.java
```

Note
You must first install and configure the JDK before you can compile and run programs. See Supplement I.B, Installing and Configuring JDK 8, for how to install the JDK and set up the environment to compile and run Java programs. If you have trouble compiling and running programs, see Supplement I.C, Compiling and Running Java from the Command Window. This supplement also explains how to use basic DOS commands and how to use Windows Notepad to create and edit files. All the supplements are accessible from the Companion Website at www.cs.armstrong.edu/liang/intro10e/supplement.html.

If there aren’t any syntax errors, the compiler generates a bytecode file with a .class extension. Thus, the preceding command generates a file named Welcome.class, as shown
Chapter 1  Introduction to Computers, Programs, and Java

The Java language is a high-level language, but Java bytecode is a low-level language. The bytecode is similar to machine instructions but is architecture neutral and can run on any platform that has a Java Virtual Machine (JVM), as shown in Figure 1.8b. Rather than a physical machine, the virtual machine is a program that interprets Java bytecode. This is one of Java’s primary advantages: Java bytecode can run on a variety of hardware platforms and operating systems. Java source code is compiled into Java bytecode and Java bytecode is interpreted by the JVM. Your Java code may use the code in the Java library. The JVM executes your code along with the code in the library.

To execute a Java program is to run the program’s bytecode. You can execute the bytecode on any platform with a JVM, which is an interpreter. It translates the individual instructions in the bytecode into the target machine language code one at a time rather than the whole program as a single unit. Each step is executed immediately after it is translated.

The following command runs the bytecode for Listing 1.1:

```
java Welcome
```
1.8 Creating, Compiling, and Executing a Java Program

Figure 1.9 shows the `javac` command for compiling `Welcome.java`. The compiler generates the `Welcome.class` file, and this file is executed using the `java` command.

**Note**
For simplicity and consistency, all source-code and class files used in this book are placed under `c:\book` unless specified otherwise.

![Diagram](image)

**Figure 1.8** (a) Java source code is translated into bytecode. (b) Java bytecode can be executed on any computer with a Java Virtual Machine.

Figure 1.9 shows the `javac` command for compiling `Welcome.java`. The compiler generates the `Welcome.class` file, and this file is executed using the `java` command.

**Note**
For simplicity and consistency, all source-code and class files used in this book are placed under `c:\book` unless specified otherwise.

![Command Prompt](image)

**Figure 1.9** The output of Listing 1.1 displays the message “Welcome to Java!”

**Caution**
Do not use the extension `.class` in the command line when executing the program. Use `java ClassName` to run the program. If you use `java ClassName.class` in the command line, the system will attempt to fetch `ClassName.class.class`.

**Tip**
If you execute a class file that does not exist, a `NoClassDefFoundError` will occur. If you execute a class file that does not have a `main` method or you mistype the `main` method (e.g., by typing `Main` instead of `main`), a `NoSuchMethodError` will occur.

**Note**
When executing a Java program, the JVM first loads the bytecode of the class to memory using a program called the class loader. If your program uses other classes, the class loader dynamically loads them just before they are needed. After a class is loaded, the JVM uses a program called the bytecode verifier to check the validity of the bytecode and
to ensure that the bytecode does not violate Java’s security restrictions. Java enforces strict security to make sure that Java class files are not tampered with and do not harm your computer.

**Pedagogical Note**

Your instructor may require you to use packages for organizing programs. For example, you may place all programs in this chapter in a package named `chapter1`. For instructions on how to use packages, see Supplement I.F, Using Packages to Organize the Classes in the Text.

1.33 What is the Java source filename extension, and what is the Java bytecode filename extension?

1.34 What are the input and output of a Java compiler?

1.35 What is the command to compile a Java program?

1.36 What is the command to run a Java program?

1.37 What is the JVM?

1.38 Can Java run on any machine? What is needed to run Java on a computer?

1.39 If a `ClassNotFoundException` occurs when you run a program, what is the cause of the error?

1.40 If a `NoSuchMethodError` occurs when you run a program, what is the cause of the error?

### 1.9 Programming Style and Documentation

**Key Point**

**Programming style** deals with what programs look like. A program can compile and run properly even if written on only one line, but writing it all on one line would be bad programming style because it would be hard to read. **Documentation** is the body of explanatory remarks and comments pertaining to a program. Programming style and documentation are as important as coding. Good programming style and appropriate documentation reduce the chance of errors and make programs easy to read. This section gives several guidelines. For more detailed guidelines, see Supplement I.D, Java Coding Style Guidelines, on the Companion Website.

#### 1.9.1 Appropriate Comments and Comment Styles

Include a summary at the beginning of the program that explains what the program does, its key features, and any unique techniques it uses. In a long program, you should also include comments that introduce each major step and explain anything that is difficult to read. It is important to make comments concise so that they do not crowd the program or make it difficult to read.

In addition to line comments (beginning with `//`) and block comments (beginning with `/*`), Java supports comments of a special type, referred to as javadoc comments. javadoc comments begin with `/**` and end with `*/`. They can be extracted into an HTML file using the JDK’s `javadoc` command. For more information, see Supplement III.Y, javadoc Comments, on the companion Website.

Use javadoc comments (`/** ... */`) for commenting on an entire class or an entire method. These comments must precede the class or the method header in order to be extracted into a javadoc HTML file. For commenting on steps inside a method, use line comments (`//`).
1.9 Programming Style and Documentation

To see an example of a javadoc HTML file, check out [www.cs.armstrong.edu/liang/javadoc/Exercise1.html](http://www.cs.armstrong.edu/liang/javadoc/Exercise1.html). Its corresponding Java code is shown in [www.cs.armstrong.edu/liang/javadoc/Exercise1.java](http://www.cs.armstrong.edu/liang/javadoc/Exercise1.java).

1.9.2 Proper Indentation and Spacing

A consistent indentation style makes programs clear and easy to read, debug, and maintain. Indentation is used to illustrate the structural relationships between a program’s components or statements. Java can read the program even if all of the statements are on the same long line, but humans find it easier to read and maintain code that is aligned properly. Indent each subcomponent or statement at least two spaces more than the construct within which it is nested.

A single space should be added on both sides of a binary operator, as shown in the following statement:

```java
System.out.println(3+4*4);
```

**Bad style**

```java
System.out.println(3 + 4 * 4);
```

**Good style**

1.9.3 Block Styles

A block is a group of statements surrounded by braces. There are two popular styles, next-line style and end-of-line style, as shown below.

```
public class Test {
    public static void main(String[] args) {
        System.out.println("Block Styles");
    }
}
```

**Next-line style**

```
public class Test {
    public static void main(String[] args) {
        System.out.println("Block Styles");
    }
}
```

**End-of-line style**

The next-line style aligns braces vertically and makes programs easy to read, whereas the end-of-line style saves space and may help avoid some subtle programming errors. Both are acceptable block styles. The choice depends on personal or organizational preference. You should use a block style consistently—mixing styles is not recommended. This book uses the end-of-line style to be consistent with the Java API source code.

1.41 Reform the following program according to the programming style and documentation guidelines. Use the end-of-line brace style.

```java
public class Test {
    // Main method
    public static void main(String[] args) {
        System.out.println("Welcome to Java");
    }
}
```
1.10 Programming Errors

Programming errors can be categorized into three types: syntax errors, runtime errors, and logic errors.

1.10.1 Syntax Errors

Errors that are detected by the compiler are called syntax errors or compile errors. Syntax errors result from errors in code construction, such as mistyping a keyword, omitting some necessary punctuation, or using an opening brace without a corresponding closing brace. These errors are usually easy to detect because the compiler tells you where they are and what caused them. For example, the program in Listing 1.4 has a syntax error, as shown in Figure 1.10.

Listing 1.4 ShowSyntaxErrors.java

```
1  public class ShowSyntaxErrors {
2     public static main(String[] args) {
3         System.out.println("Welcome to Java");
4     }
5 }
```

Four errors are reported, but the program actually has two errors:

- The keyword `void` is missing before `main` in line 2.
- The string `Welcome to Java` should be closed with a closing quotation mark in line 3.

Since a single error will often display many lines of compile errors, it is a good practice to fix errors from the top line and work downward. Fixing errors that occur earlier in the program may also fix additional errors that occur later.

Figure 1.10 The compiler reports syntax errors.

Tip

If you don’t know how to correct it, compare your program closely, character by character, with similar examples in the text. In the first few weeks of this course, you will probably spend a lot of time fixing syntax errors. Soon you will be familiar with Java syntax and can quickly fix syntax errors.

1.10.2 Runtime Errors

Runtime errors are errors that cause a program to terminate abnormally. They occur while a program is running if the environment detects an operation that is impossible to carry out. Input mistakes typically cause runtime errors. An input error occurs when the program is
waiting for the user to enter a value, but the user enters a value that the program cannot handle. For instance, if the program expects to read in a number, but instead the user enters a string, this causes data-type errors to occur in the program.

Another example of runtime errors is division by zero. This happens when the divisor is zero for integer divisions. For instance, the program in Listing 1.5 would cause a runtime error, as shown in Figure 1.11.

**Listing 1.5 ShowRuntimeErrors.java**

```java
public class ShowRuntimeErrors {
    public static void main(String[] args) {
        System.out.println(1 / 0);
    }
}
```

![Runtime error](image)

**Figure 1.11** The runtime error causes the program to terminate abnormally.

### 1.10.3 Logic Errors

Logic errors occur when a program does not perform the way it was intended to. Errors of this kind occur for many different reasons. For example, suppose you wrote the program in Listing 1.6 to convert Celsius 35 degrees to a Fahrenheit degree:

**Listing 1.6 ShowLogicErrors.java**

```java
public class ShowLogicErrors {
    public static void main(String[] args) {
        System.out.println("Celsius 35 is Fahrenheit degree ");
        System.out.println((9 / 5) * 35 + 32);
    }
}
```

Celsius 35 is Fahrenheit degree
67

You will get Fahrenheit 67 degrees, which is wrong. It should be 95.0. In Java, the division for integers is the quotient—the fractional part is truncated—so in Java 9 / 5 is 1. To get the correct result, you need to use 9.0 / 5, which results in 1.8.

In general, syntax errors are easy to find and easy to correct because the compiler gives indications as to where the errors came from and why they are wrong. Runtime errors are not difficult to find, either, since the reasons and locations for the errors are displayed on the console when the program aborts. Finding logic errors, on the other hand, can be very challenging. In the upcoming chapters, you will learn the techniques of tracing programs and finding logic errors.

### 1.10.4 Common Errors

Missing a closing brace, missing a semicolon, missing quotation marks for strings, and misspelling names are common errors for new programmers.
**Common Error 1: Missing Braces**
The braces are used to denote a block in the program. Each opening brace must be matched by a closing brace. A common error is missing the closing brace. To avoid this error, type a closing brace whenever an opening brace is typed, as shown in the following example.

```java
public class Welcome {
    // Type this closing brace right away to match the opening brace
}
```

If you use an IDE such as NetBeans and Eclipse, the IDE automatically inserts a closing brace for each opening brace typed.

**Common Error 2: Missing Semicolons**
Each statement ends with a statement terminator (;). Often, a new programmer forgets to place a statement terminator for the last statement in a block, as shown in the following example.

```java
public static void main(String[] args) {
    System.out.println("Programming is fun!");
    System.out.println("Fundamentals First");
    System.out.println("Problem Driven")
}  // Missing a semicolon
```

**Common Error 3: Missing Quotation Marks**
A string must be placed inside the quotation marks. Often, a new programmer forgets to place a quotation mark at the end of a string, as shown in the following example.

```java
System.out.println("Problem Driven");
// Missing a quotation mark
```

If you use an IDE such as NetBeans and Eclipse, the IDE automatically inserts a closing quotation mark for each opening quotation mark typed.

**Common Error 4: Misspelling Names**
Java is case sensitive. Misspelling names is a common error for new programmers. For example, the word `main` is misspelled as `Main` and `String` is misspelled as `string` in the following code.

```java
1  public class Test {
2      public static void Main(string[] args) {
3          System.out.println((10.5 + 2 * 3) / (45 - 3.5));
4      }
5  }
```

1.42 What are syntax errors (compile errors), runtime errors, and logic errors?
1.43 Give examples of syntax errors, runtime errors, and logic errors.
1.44 If you forget to put a closing quotation mark on a string, what kind error will be raised?
1.45 If your program needs to read integers, but the user entered strings, an error would occur when running this program. What kind of error is this?
1.46 Suppose you write a program for computing the perimeter of a rectangle and you mistakenly write your program so that it computes the area of a rectangle. What kind of error is this?
1.47 Identify and fix the errors in the following code:

```java
1 public class Welcome {
2    public void Main(String[] args) {
3        System.out.println('Welcome to Java!);
4    }
5 }
```

1.11 Developing Java Programs Using NetBeans

You can edit, compile, run, and debug Java Programs using NetBeans.

NetBeans and Eclipse are two free popular integrated development environments for developing Java programs. They are easy to learn if you follow simple instructions. We recommend that you use either one for developing Java programs. This section gives the essential instructions to guide new users to create a project, create a class, compile, and run a class in NetBeans. The use of Eclipse will be introduced in the next section. For instructions on downloading and installing latest version of NetBeans, see Supplement II.B.

1.11.1 Creating a Java Project

Before you can create Java programs, you need to first create a project. A project is like a folder to hold Java programs and all supporting files. You need to create a project only once. Here are the steps to create a Java project:

1. Choose File, New Project to display the New Project dialog box, as shown in Figure 1.12.
2. Select Java in the Categories section and Java Application in the Projects section and click Next to display the New Java Application dialog box, as shown in Figure 1.13.
3. Type demo in the Project Name field and c:\michael in Project Location field. Uncheck Use Dedicated Folder for Storing Libraries and uncheck Create Main Class.
4. Click Finish to create the project, as shown in Figure 1.14.

1.11.2 Creating a Java Class

After a project is created, you can create Java programs in the project using the following steps:

1. Right-click the demo node in the project pane to display a context menu. Choose New, Java Class to display the New Java Class dialog box, as shown in Figure 1.15.

![Figure 1.12](image-url)

**Figure 1.12** The New Project dialog is used to create a new project and specify a project type.
2. Type \texttt{Welcome} in the Class Name field and select the Source Packages in the Location field. Leave the Package field blank. This will create a class in the default package.

3. Click \textit{Finish} to create the Welcome class. The source code file \texttt{Welcome.java} is placed under the <default package> node.

4. Modify the code in the Welcome class to match Listing 1.1 in the text, as shown in Figure 1.16.
1.12 Developing Java Programs Using Eclipse

You can edit, compile, run, and debug Java Programs using Eclipse.

The preceding section introduced developing Java programs using NetBeans. You can also use Eclipse to develop Java programs. This section gives the essential instructions to guide new users to create a project, create a class, and compile/run a class in Eclipse. For instructions on downloading and installing latest version of Eclipse, see Supplement II.D.

1.12.1 Creating a Java Project

Before creating Java programs in Eclipse, you need to first create a project to hold all files. Here are the steps to create a Java project in Eclipse:

1. Choose File, New, Java Project to display the New Project wizard, as shown in Figure 1.17.
2. Type demo in the Project name field. As you type, the Location field is automatically set by default. You may customize the location for your project.
3. Make sure that you selected the options Use project folder as root for sources and class files so that the .java and .class files are in the same folder for easy access.
4. Click Finish to create the project, as shown in Figure 1.18.

1.12.2 Creating a Java Class

After a project is created, you can create Java programs in the project using the following steps:

1. Choose File, New, Class to display the New Java Class wizard.
2. Type Welcome in the Name field.
3. Check the option `public static void main(String[] args)`.
4. Click Finish to generate the template for the source code Welcome.java, as shown in Figure 1.19.
1.12 Developing Java Programs Using Eclipse

1.12.3 Compiling and Running a Class

To run the program, right-click the class in the project to display a context menu. Choose Run, Java Application in the context menu to run the class. The output is displayed in the Console pane, as shown in Figure 1.20.
**Chapter Summary**

1. A computer is an electronic device that stores and processes data.

2. A computer includes both hardware and software.

3. Hardware is the physical aspect of the computer that can be touched.

4. Computer programs, known as software, are the invisible instructions that control the hardware and make it perform tasks.

5. Computer programming is the writing of instructions (i.e., code) for computers to perform.

6. The central processing unit (CPU) is a computer’s brain. It retrieves instructions from memory and executes them.

7. Computers use zeros and ones because digital devices have two stable states, referred to by convention as zero and one.
8. A bit is a binary digit 0 or 1.

9. A byte is a sequence of 8 bits.

10. A kilobyte is about 1,000 bytes, a megabyte about 1 million bytes, a gigabyte about 1 billion bytes, and a terabyte about 1,000 gigabytes.

11. Memory stores data and program instructions for the CPU to execute.

12. A memory unit is an ordered sequence of bytes.

13. Memory is volatile, because information is lost when the power is turned off.

14. Programs and data are permanently stored on storage devices and are moved to memory when the computer actually uses them.

15. The machine language is a set of primitive instructions built into every computer.

16. Assembly language is a low-level programming language in which a mnemonic is used to represent each machine-language instruction.

17. High-level languages are English-like and easy to learn and program.

18. A program written in a high-level language is called a source program.

19. A compiler is a software program that translates the source program into a machine-language program.

20. The operating system (OS) is a program that manages and controls a computer’s activities.

21. Java is platform independent, meaning that you can write a program once and run it on any computer.

22. Java programs can be embedded in HTML pages and downloaded by Web browsers to bring live animation and interaction to Web clients.

23. The Java source file name must match the public class name in the program. Java source code files must end with the .java extension.

24. Every class is compiled into a separate bytecode file that has the same name as the class and ends with the .class extension.

25. To compile a Java source-code file from the command line, use the javac command.

26. To run a Java class from the command line, use the java command.

27. Every Java program is a set of class definitions. The keyword class introduces a class definition. The contents of the class are included in a block.

28. A block begins with an opening brace ( { ) and ends with a closing brace ( } ).

29. Methods are contained in a class. To run a Java program, the program must have a main method. The main method is the entry point where the program starts when it is executed.
30. Every statement in Java ends with a semicolon (\texttt{;}), known as the \textit{statement terminator}.

31. Reserved words, or keywords, have a specific meaning to the compiler and cannot be used for other purposes in the program.

32. In Java, comments are preceded by two slashes (\texttt{//}) on a line, called a \textit{line comment}, or enclosed between \texttt{/*} and \texttt{*/} on one or several lines, called a \textit{block comment} or \textit{paragraph comment}. Comments are ignored by the compiler.

33. Java source programs are case sensitive.

34. Programming errors can be categorized into three types: \textit{syntax errors}, \textit{runtime errors}, and \textit{logic errors}. Errors reported by a compiler are called syntax errors or \textit{compile errors}. Runtime errors are errors that cause a program to terminate abnormally. Logic errors occur when a program does not perform the way it was intended to.

\section*{Quiz}

Answer the quiz for this chapter online at \url{www.cs.armstrong.edu/liang/intro10e/quiz.html}.

\section*{MyProgrammingLab\textsuperscript{\textregistered} Programming Exercises}

\begin{itemize}
  \item \textbf{Note} Solutions to even-numbered programming exercises are on the Companion Website. Solutions to all programming exercises are on the Instructor Resource Website. Additional programming exercises with solutions are provided to the instructors on the Instructor Resource Website. The level of difficulty is rated easy (no star), moderate (*), hard (**), or challenging (***)..

  \item \textbf{1.1} (Display three messages) Write a program that displays \textit{Welcome to Java}, \textit{Welcome to Computer Science}, and \textit{Programming is fun}.

  \item \textbf{1.2} (Display five messages) Write a program that displays \textit{Welcome to Java} five times.

  \item \textbf{*1.3} (Display a pattern) Write a program that displays the following pattern:

\begin{verbatim}
    J   A   V   V   A
    J   A   A   V   V   A   A
    J   J   A   A   A   V   V   A   A
\end{verbatim}

  \item \textbf{1.4} (Print a table) Write a program that displays the following table:

\begin{verbatim}
a  a^2  a^3
1   1   1
2   4   8
3   9   27
4  16  64
\end{verbatim}

  \item \textbf{1.5} (Compute expressions) Write a program that displays the result of

\[
\frac{9.5 \times 4.5 - 2.5 \times 3}{45.5 - 3.5}.
\]

  \item \textbf{1.6} (Summation of a series) Write a program that displays the result of

\[
1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 + 9.
\]
\end{itemize}
1.7 \textbf{(Approximate \pi)} \pi \text{ can be computed using the following formula:} \\
\pi = 4 \times \left( 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} - \frac{1}{11} + \ldots \right) \\
Write a program that displays the result of \(4 \times \left( 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} - \frac{1}{11} + \frac{1}{13} \right)\). Use 1.0 instead of 1 in your program.

1.8 \textbf{(Area and perimeter of a circle)} Write a program that displays the area and perimeter of a circle that has a radius of 5.5 using the following formula:

\text{perimeter} = 2 \times \text{radius} \times \pi \\
\text{area} = \text{radius} \times \text{radius} \times \pi

1.9 \textbf{(Area and perimeter of a rectangle)} Write a program that displays the area and perimeter of a rectangle with the width of 4.5 and height of 7.9 using the following formula:

\text{area} = \text{width} \times \text{height}

1.10 \textbf{(Average speed in miles)} Assume a runner runs 14 kilometers in 45 minutes and 30 seconds. Write a program that displays the average speed in miles per hour. (Note that 1 mile is 1.6 kilometers.)

*1.11 \textbf{(Population projection)} The U.S. Census Bureau projects population based on the following assumptions:

\begin{itemize}
  \item One birth every 7 seconds
  \item One death every 13 seconds
  \item One new immigrant every 45 seconds
\end{itemize}

Write a program to display the population for each of the next five years. Assume the current population is 312,032,486 and one year has 365 days. \textit{Hint:} In Java, if two integers perform division, the result is an integer. The fractional part is truncated. For example, 5 / 4 is 1 (not 1.25) and 10 / 4 is 2 (not 2.5). To get an accurate result with the fractional part, one of the values involved in the division must be a number with a decimal point. For example, 5.0 / 4 is 1.25 and 10 / 4.0 is 2.5.

1.12 \textbf{(Average speed in kilometers)} Assume a runner runs 24 miles in 1 hour, 40 minutes, and 35 seconds. Write a program that displays the average speed in kilometers per hour. (Note that 1 mile is 1.6 kilometers.)

*1.13 \textbf{(Algebra: solve 2 \times 2 linear equations)} You can use Cramer’s rule to solve the following 2 \times 2 system of linear equation:

\begin{align*}
ax + by &= e \\
.cx + dy &= f
\end{align*}

\begin{align*}
x &= \frac{ed - bf}{ad - bc} \\
y &= \frac{af - ec}{ad - bc}
\end{align*}

Write a program that solves the following equation and displays the value for \(x\) and \(y\):

\begin{align*}
3.4x + 50.2y &= 44.5 \\
2.1x + .55y &= 5.9
\end{align*}
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Elementary Programming

Objectives

- To write Java programs to perform simple computations (§2.2).
- To obtain input from the console using the Scanner class (§2.3).
- To use identifiers to name variables, constants, methods, and classes (§2.4).
- To use variables to store data (§§2.5–2.6).
- To program with assignment statements and assignment expressions (§2.6).
- To use constants to store permanent data (§2.7).
- To name classes, methods, variables, and constants by following their naming conventions (§2.8).
- To explore Java numeric primitive data types: byte, short, int, long, float, and double (§2.9.1).
- To read a byte, short, int, long, float, or double value from the keyboard (§2.9.2).
- To perform operations using operators +, -, *, /, and % (§2.9.3).
- To perform exponent operations using Math.pow(a, b) (§2.9.4).
- To write integer literals, floating-point literals, and literals in scientific notation (§2.10).
- To write and evaluate numeric expressions (§2.11).
- To obtain the current system time using System.currentTimeMillis() (§2.12).
- To use augmented assignment operators (§2.13).
- To distinguish between postincrement and preincrement and between postdecrement and predecrement (§2.14).
- To cast the value of one type to another type (§2.15).
- To describe the software development process and apply it to develop the loan payment program (§2.16).
- To write a program that converts a large amount of money into smaller units (§2.17).
- To avoid common errors and pitfalls in elementary programming (§2.18).
2.1 Introduction

The focus of this chapter is on learning elementary programming techniques to solve problems.

In Chapter 1 you learned how to create, compile, and run very basic Java programs. Now you will learn how to solve problems by writing programs. Through these problems, you will learn elementary programming using primitive data types, variables, constants, operators, expressions, and input and output.

Suppose, for example, that you need to take out a student loan. Given the loan amount, loan term, and annual interest rate, can you write a program to compute the monthly payment and total payment? This chapter shows you how to write programs like this. Along the way, you learn the basic steps that go into analyzing a problem, designing a solution, and implementing the solution by creating a program.

2.2 Writing a Simple Program

Writing a program involves designing a strategy for solving the problem and then using a programming language to implement that strategy.

Let’s first consider the simple problem of computing the area of a circle. How do we write a program for solving this problem?

Writing a program involves designing algorithms and translating algorithms into programming instructions, or code. An algorithm describes how a problem is solved by listing the actions that need to be taken and the order of their execution. Algorithms can help the programmer plan a program before writing it in a programming language. Algorithms can be described in natural languages or in pseudocode (natural language mixed with some programming code). The algorithm for calculating the area of a circle can be described as follows:

1. Read in the circle’s radius.
2. Compute the area using the following formula:
   \[ \text{area} = \text{radius} \times \text{radius} \times \pi \]
3. Display the result.

Tip
It’s always good practice to outline your program (or its underlying problem) in the form of an algorithm before you begin coding.

When you code—that is, when you write a program—you translate an algorithm into a program. You already know that every Java program begins with a class definition in which the keyword \texttt{class} is followed by the class name. Assume that you have chosen \texttt{ComputeArea} as the class name. The outline of the program would look like this:

\[
\text{public class ComputeArea} \{
  \text{  // Details to be given later}
\}
\]

As you know, every Java program must have a \texttt{main} method where program execution begins. The program is then expanded as follows:

\[
\text{public class ComputeArea} \{
  \text{  public static void main(String[] args) \{}
  \text{    // Step 1: Read in radius}
  \text{  }
  \text{    // Step 2: Compute area}
\}
\]
The program needs to read the radius entered by the user from the keyboard. This raises two important issues:

- Reading the radius.
- Storing the radius in the program.

Let’s address the second issue first. In order to store the radius, the program needs to declare a symbol called a variable. A variable represents a value stored in the computer’s memory.

Rather than using \( x \) and \( y \) as variable names, choose descriptive names: in this case, \( \text{radius} \) for radius, and \( \text{area} \) for area. To let the compiler know what \( \text{radius} \) and \( \text{area} \) are, specify their data types. That is the kind of data stored in a variable, whether integer, real number, or something else. This is known as declaring variables. Java provides simple data types for representing integers, real numbers, characters, and Boolean types. These types are known as primitive data types or fundamental types.

Real numbers (i.e., numbers with a decimal point) are represented using a method known as floating-point in computers. So, the real numbers are also called floating-point numbers. In Java, you can use the keyword \texttt{double} to declare a floating-point variable. Declare \( \text{radius} \) and \( \text{area} \) as \texttt{double}. The program can be expanded as follows:

```java
public class ComputeArea {
    public static void main(String[] args) {
        double radius; // Declare radius
        double area; // Declare area

        // Step 1: Read in radius
        // Step 2: Compute area
        // Step 3: Display the area
    }
}
```

The program declares \( \text{radius} \) and \( \text{area} \) as variables. The reserved word \texttt{double} indicates that \( \text{radius} \) and \( \text{area} \) are floating-point values stored in the computer.

The first step is to prompt the user to designate the circle’s \( \text{radius} \). You will soon learn how to prompt the user for information. For now, to learn how variables work, you can assign a fixed value to \( \text{radius} \) in the program as you write the code; later, you’ll modify the program to prompt the user for this value.

The second step is to compute \( \text{area} \) by assigning the result of the expression \( \text{radius} * \text{radius} * 3.14159 \) to \( \text{area} \).

In the final step, the program will display the value of \( \text{area} \) on the console by using the \texttt{System.out.println} method.

Listing 2.1 shows the complete program, and a sample run of the program is shown in Figure 2.1.

**Listing 2.1  ComputeArea.java**

```java
1 public class ComputeArea {
2     public static void main(String[] args) {
3         double radius; // Declare radius
4         double area; // Declare area
5
6     // Assign a radius
```

Variables such as `radius` and `area` correspond to memory locations. Every variable has a name, a type, a size, and a value. Line 3 declares that `radius` can store a `double` value. The value is not defined until you assign a value. Line 7 assigns 20 into variable `radius`. Similarly, line 4 declares variable `area`, and line 10 assigns a value into `area`. The following table shows the value in the memory for `area` and `radius` as the program is executed. Each row in the table shows the values of variables after the statement in the corresponding line in the program is executed. This method of reviewing how a program works is called **tracing a program**. Tracing programs are helpful for understanding how programs work, and they are useful tools for finding errors in programs.

The plus sign (+) has two meanings: one for addition and the other for concatenating (combining) strings. The plus sign (+) in lines 13–14 is called a **string concatenation operator**. It combines two strings into one. If a string is combined with a number, the number is converted into a string and concatenated with the other string. Therefore, the plus signs (+) in lines 13–14 concatenate strings into a longer string, which is then displayed in the output. Strings and string concatenation will be discussed further in Chapter 4.

**Caution**

A string cannot cross lines in the source code. Thus, the following statement would result in a compile error:

```
System.out.println("Introduction to Java Programming, \nby Y. Daniel Liang");
```

To fix the error, break the string into separate substrings, and use the concatenation operator (+) to combine them:

```
System.out.println("Introduction to Java Programming, " + "by Y. Daniel Liang");
```
2.1 Identify and fix the errors in the following code:

```java
public class Test {
    public void main(String[] args) {
        double i = 50.0;
        double k = i + 50.0;
        double j = k + 1;
        System.out.println("j is " + j + " and ");
        k is " + k);
    }
}
```

2.3 Reading Input from the Console

Reading input from the console enables the program to accept input from the user.

In Listing 2.1, the radius is fixed in the source code. To use a different radius, you have to modify the source code and recompile it. Obviously, this is not convenient, so instead you can use the Scanner class for console input.

Java uses System.out to refer to the standard output device and System.in to the standard input device. By default, the output device is the display monitor and the input device is the keyboard. To perform console output, you simply use the println method to display a primitive value or a string to the console. Console input is not directly supported in Java, but you can use the Scanner class to create an object to read input from System.in, as follows:

```java
Scanner input = new Scanner(System.in);
```

The syntax new Scanner(System.in) creates an object of the Scanner type. The syntax Scanner input declares that input is a variable whose type is Scanner. The whole line Scanner input = new Scanner(System.in) creates a Scanner object and assigns its reference to the variable input. An object may invoke its methods. To invoke a method on an object is to ask the object to perform a task. You can invoke the nextDouble() method to read a double value as follows:

```java
double radius = input.nextDouble();
```

This statement reads a number from the keyboard and assigns the number to radius.

Listing 2.2 rewrites Listing 2.1 to prompt the user to enter a radius.

**Listing 2.2 ComputeAreaWithConsoleInput.java**

```java
import java.util.Scanner; // Scanner is in the java.util package
public class ComputeAreaWithConsoleInput {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        System.out.print("Enter a number for radius: ");
        double radius = input.nextDouble();
        double area = radius * radius * 3.14159;
        System.out.println("Area is "+ area);
    }
}
```
Chapter 2  Elementary Programming

```java
16 System.out.println("The area for the circle of radius " +
17 radius + " is " + area);
18 }
19 }

Enter a number for radius: 2.5
The area for the circle of radius 2.5 is 19.6349375

Enter a number for radius: 23
The area for the circle of radius 23.0 is 1661.90111
```

Line 9 displays a string "Enter a number for radius: " to the console. This is
known as a prompt, because it directs the user to enter an input. Your program should always
tell the user what to enter when expecting input from the keyboard.

The print method in line 9
```
System.out.print("Enter a number for radius: ");
```
is identical to the println method except that println moves to the beginning of the next
line after displaying the string, but print does not advance to the next line when completed.

Line 6 creates a Scanner object. The statement in line 10 reads input from the keyboard.
```
double radius = input.nextDouble();
```

After the user enters a number and presses the Enter key, the program reads the number
and assigns it to radius.

More details on objects will be introduced in Chapter 9. For the time being, simply accept
that this is how to obtain input from the console.

The Scanner class is in the java.util package. It is imported in line 1. There are two
types of import statements: specific import and wildcard import. The specific import specifies
a single class in the import statement. For example, the following statement imports
Scanner from the package java.util.
```
import java.util.Scanner;
```
The wildcard import imports all the classes in a package by using the asterisk as the wildcard. For example, the following statement imports all the classes from the package java.util.
```
import java.util.*;
```
The information for the classes in an imported package is not read in at compile time or
runtime unless the class is used in the program. The import statement simply tells the compiler
where to locate the classes. There is no performance difference between a specific import and
a wildcard import declaration.

Listing 2.3 gives an example of reading multiple input from the keyboard. The program
reads three numbers and displays their average.

**LISTING 2.3  ComputeAverage.java**

import class
```
import java.util.Scanner; // Scanner is in the java.util package
```
create a Scanner
```
public class ComputeAverage {
    public static void main(String[] args) {
        // Create a Scanner object
        Scanner input = new Scanner(System.in);
    }
```
2.4 Identifiers

Identifiers are the names that identify the elements such as classes, methods, and variables in a program.

As you see in Listing 2.3, `ComputeAverage`, `main`, `input`, `number1`, `number2`, `number3`, and so on are the names of things that appear in the program. In programming terminology, such names are called identifiers. All identifiers must obey the following rules:

- An identifier is a sequence of characters that consists of letters, digits, underscores (\_), and dollar signs ($).
An identifier must start with a letter, an underscore (_), or a dollar sign ($). It cannot start with a digit.

- An identifier cannot be a reserved word. (See Appendix A for a list of reserved words.)
- An identifier cannot be `true`, `false`, or `null`.
- An identifier can be of any length.

For example, `$2`, `ComputeArea`, `area`, `radius`, and `print` are legal identifiers, whereas `2A` and `d+4` are not because they do not follow the rules. The Java compiler detects illegal identifiers and reports syntax errors.

**Note**
Since Java is case sensitive, `area`, `Area`, and `AREA` are all different identifiers.

**Tip**
Identifiers are for naming variables, methods, classes, and other items in a program. Descriptive identifiers make programs easy to read. Avoid using abbreviations for identifiers. Using complete words is more descriptive. For example, `numberOfStudents` is better than `numStuds`, `numOfStuds`, or `numOfStudents`. We use descriptive names for complete programs in the text. However, we will occasionally use variable names such as `i`, `j`, `k`, `x`, and `y` in the code snippets for brevity. These names also provide a generic tone to the code snippets.

**Tip**
Do not name identifiers with the `$` character. By convention, the `$` character should be used only in mechanically generated source code.

### 2.4 Which of the following identifiers are valid? Which are Java keywords?

- `miles`, `Test`, `a++`, `--a`, `4&R`, `$4`, `#44`, `apps`
- `class`, `public`, `int`, `x`, `y`, `radius`

### 2.5 Variables

**Variables are used to represent values that may be changed in the program.**

As you see from the programs in the preceding sections, variables are used to store values to be used later in a program. They are called variables because their values can be changed. In the program in Listing 2.2, `radius` and `area` are variables of the `double` type. You can assign any numerical value to `radius` and `area`, and the values of `radius` and `area` can be reassigned. For example, in the following code, `radius` is initially `1.0` (line 2) and then changed to `2.0` (line 7), and `area` is set to `3.14159` (line 3) and then reset to `12.56636` (line 8).

```java
1 // Compute the first area
2 radius = 1.0;                // radius: 1.0
3 area = radius * radius * 3.14159; // area: 3.14159
4 System.out.println("The area is ", area + " for radius ", radius);
5
6 // Compute the second area
7 radius = 2.0;                // radius: 2.0
8 area = radius * radius * 3.14159; // area: 12.56636
9 System.out.println("The area is ", area + " for radius ", radius);
```

Variables are for representing data of a certain type. To use a variable, you declare it by telling the compiler its name as well as what type of data it can store. The **variable declaration**
2.6 Assignment Statements and Assignment Expressions

The syntax for declaring a variable is

datatype variableName;

Here are some examples of variable declarations:

```java
tablet count; // Declare count to be an integer variable
double radius; // Declare radius to be a double variable
double interestRate; // Declare interestRate to be a double variable
```

These examples use the data types `int` and `double`. Later you will be introduced to additional data types, such as `byte`, `short`, `long`, `float`, `char`, and `boolean`.

If variables are of the same type, they can be declared together, as follows:

datatype variable1, variable2, ..., variablen;

The variables are separated by commas. For example,

```java
int i, j, k; // Declare i, j, and k as int variables
```

Variables often have initial values. You can declare a variable and initialize it in one step.

```java
int count = 1;
```

This is equivalent to the next two statements:

```java
int count;
count = 1;
```

You can also use a shorthand form to declare and initialize variables of the same type together. For example,

```java
int i = 1, j = 2;
```

**Tip**

A variable must be declared before it can be assigned a value. A variable declared in a method must be assigned a value before it can be used.

Whenever possible, declare a variable and assign its initial value in one step. This will make the program easy to read and avoid programming errors.

Every variable has a scope. The *scope of a variable* is the part of the program where the variable can be referenced. The rules that define the scope of a variable will be introduced gradually later in the book. For now, all you need to know is that a variable must be declared and initialized before it can be used.

2.5 Identify and fix the errors in the following code:

```java
public class Test {
    public static void main(String[] args) {
        int i = k + 2;
        System.out.println(i);
    }
}
```

2.6 Assignment Statements and Assignment Expressions

An assignment statement designates a value for a variable. An assignment statement can be used as an expression in Java.
After a variable is declared, you can assign a value to it by using an assignment statement. In Java, the equal sign (=) is used as the assignment operator. The syntax for assignment statements is as follows:

```
variable = expression;
```

An expression represents a computation involving values, variables, and operators that, taking them together, evaluates to a value. For example, consider the following code:

```java
int y = 1; // Assign 1 to variable y
double radius = 1.0; // Assign 1.0 to variable radius
int x = 5 * (3 / 2);         // Assign the value of the expression to x
x = y + 1; // Assign the addition of y and 1 to x
double area = radius * radius * 3.14159; // Compute area
```

You can use a variable in an expression. A variable can also be used in both sides of the = operator. For example,

```
x = x + 1;
```

In this assignment statement, the result of \(x + 1\) is assigned to \(x\). If \(x\) is 1 before the statement is executed, then it becomes 2 after the statement is executed.

To assign a value to a variable, you must place the variable name to the left of the assignment operator. Thus, the following statement is wrong:

```
1 = x; // Wrong
```

Note
In mathematics, \(x = 2 \cdot x + 1\) denotes an equation. However, in Java, \(x = 2 \cdot x + 1\) is an assignment statement that evaluates the expression \(2 \cdot x + 1\) and assigns the result to \(x\).

In Java, an assignment statement is essentially an expression that evaluates to the value to be assigned to the variable on the left side of the assignment operator. For this reason, an assignment statement is also known as an assignment expression. For example, the following statement is correct:

```
System.out.println(x = 1);
```

which is equivalent to

```
x = 1;
System.out.println(x);
```

If a value is assigned to multiple variables, you can use this syntax:

```
i = j = k = 1;
```

which is equivalent to

```
k = 1;
j = k;
i = j;
```

Note
In an assignment statement, the data type of the variable on the left must be compatible with the data type of the value on the right. For example, `int x = 1.0` would be
illegal, because the data type of \texttt{x} is \texttt{int}. You cannot assign a \texttt{double} value (1.0) to an \texttt{int} variable without using type casting. Type casting is introduced in Section 2.15.

2.6 Identify and fix the errors in the following code:

```java
public class Test {
    public static void main(String[] args) {
        int i = j = k = 2;
        System.out.println(i + " + j + " + k);
    }
}
```

2.7 Named Constants

A named constant is an identifier that represents a permanent value.

The value of a variable may change during the execution of a program, but a named constant, or simply constant, represents permanent data that never changes. In our ComputeArea program, $\pi$ is a constant. If you use it frequently, you don't want to keep typing 3.14159; instead, you can declare a constant for $\pi$. Here is the syntax for declaring a constant:

```java
final datatype CONSTANTNAME = value;
```

A constant must be declared and initialized in the same statement. The word \texttt{final} is a Java keyword for declaring a constant. For example, you can declare $\pi$ as a constant and rewrite Listing 2.1 as in Listing 2.4.

**Listing 2.4** ComputeAreaWithConstant.java

```java
import java.util.Scanner; // Scanner is in the java.util package

public class ComputeAreaWithConstant {
    public static void main(String[] args) {
        final double PI = 3.14159; // Declare a constant

        // Create a Scanner object
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter a radius
        System.out.print("Enter a number for radius: ");
        double radius = input.nextDouble();

        // Compute area
        double area = radius * radius * PI;

        // Display result
        System.out.println("The area for the circle of radius " +
                           radius + " is " + area);
    }
}
```

There are three benefits of using constants: (1) you don't have to repeatedly type the same value if it is used multiple times; (2) if you have to change the constant value (e.g., from 3.14 to 3.14159 for PI), you need to change it only in a single location in the source code; and (3) a descriptive name for a constant makes the program easy to read.
2.8 Naming Conventions

Sticking with the Java naming conventions makes your programs easy to read and avoids errors.

Make sure that you choose descriptive names with straightforward meanings for the variables, constants, classes, and methods in your program. As mentioned earlier, names are case sensitive. Listed below are the conventions for naming variables, methods, and classes.

- Use lowercase for variables and methods. If a name consists of several words, concatenate them into one, making the first word lowercase and capitalizing the first letter of each subsequent word—for example, the variables `radius` and `area` and the method `print`.

- Capitalize the first letter of each word in a class name—for example, the class names `ComputeArea` and `System`.

- Capitalize every letter in a constant, and use underscores between words—for example, the constants `PI` and `MAX_VALUE`.

It is important to follow the naming conventions to make your programs easy to read.

Caution
Do not choose class names that are already used in the Java library. For example, since the `System` class is defined in Java, you should not name your class `System`.

2.7 What are the benefits of using constants? Declare an `int` constant `SIZE` with value 20.

2.8 What are the naming conventions for class names, method names, constants, and variables? Which of the following items can be a constant, a method, a variable, or a class according to the Java naming conventions?

- `MAX_VALUE`, `Test`, `read`, `readDouble`

2.9 Translate the following algorithm into Java code:

Step 1: Declare a `double` variable named `miles` with initial value 100.

Step 2: Declare a `double` constant named `KILOMETERS_PER_MILE` with value 1.609.

Step 3: Declare a `double` variable named `kilometers`, multiply `miles` and `KILOMETERS_PER_MILE`, and assign the result to `kilometers`.

Step 4: Display `kilometers` to the console.

What is `kilometers` after Step 4?

2.9 Numeric Data Types and Operations

Java has six numeric types for integers and floating-point numbers with operators `+`, `-`, `*`, `/`, and `%`.

2.9.1 Numeric Types

Every data type has a range of values. The compiler allocates memory space for each variable or constant according to its data type. Java provides eight primitive data types for numeric values, characters, and Boolean values. This section introduces numeric data types and operators.

Table 2.1 lists the six numeric data types, their ranges, and their storage sizes.
2.9 Numeric Data Types and Operations

IEEE 754 is a standard approved by the Institute of Electrical and Electronics Engineers for representing floating-point numbers on computers. The standard has been widely adopted. Java uses the 32-bit IEEE 754 for the float type and the 64-bit IEEE 754 for the double type. The IEEE 754 standard also defines special floating-point values, which are listed in Appendix E.

Java uses four types for integers: byte, short, int, and long. Choose the type that is most appropriate for your variable. For example, if you know an integer stored in a variable is within a range of a byte, declare the variable as a byte. For simplicity and consistency, we will use int for integers most of the time in this book.

Java uses two types for floating-point numbers: float and double. The double type is twice as big as float, so the double is known as double precision and float as single precision. Normally, you should use the double type, because it is more accurate than the float type.

### 2.9.2 Reading Numbers from the Keyboard

You know how to use the nextDouble() method in the Scanner class to read a double value from the keyboard. You can also use the methods listed in Table 2.2 to read a number of the byte, short, int, long, and float type.

<table>
<thead>
<tr>
<th>Name</th>
<th>Range</th>
<th>Storage Size</th>
<th>Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>byte</td>
<td>$-2^7$ to $2^7 - 1$ ($-128$ to $127$)</td>
<td>8-bit signed</td>
<td>byte type</td>
</tr>
<tr>
<td>short</td>
<td>$-2^{15}$ to $2^{15} - 1$ ($-32768$ to $32767$)</td>
<td>16-bit signed</td>
<td>short type</td>
</tr>
<tr>
<td>int</td>
<td>$-2^{31}$ to $2^{31} - 1$ ($-2147483648$ to $2147483647$)</td>
<td>32-bit signed</td>
<td>int type</td>
</tr>
<tr>
<td>long</td>
<td>$-2^{63}$ to $2^{63} - 1$ (i.e., $-9223372036854775808$ to $9223372036854775807$)</td>
<td>64-bit signed</td>
<td>long type</td>
</tr>
<tr>
<td>float</td>
<td>Negative range: $-3.4028235E+38$ to $-1.4E-45$</td>
<td>32-bit IEEE 754</td>
<td>float type</td>
</tr>
<tr>
<td>double</td>
<td>Negative range: $-1.7976931348623157E+308$ to $-4.9E-324$</td>
<td>64-bit IEEE 754</td>
<td>double type</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>nextByte()</td>
<td>reads an integer of the byte type.</td>
</tr>
<tr>
<td>nextShort()</td>
<td>reads an integer of the short type.</td>
</tr>
<tr>
<td>nextInt()</td>
<td>reads an integer of the int type.</td>
</tr>
<tr>
<td>nextLong()</td>
<td>reads an integer of the long type.</td>
</tr>
<tr>
<td>nextFloat()</td>
<td>reads a number of the float type.</td>
</tr>
<tr>
<td>nextDouble()</td>
<td>reads a number of the double type.</td>
</tr>
</tbody>
</table>
Here are examples for reading values of various types from the keyboard:

```java
Scanner input = new Scanner(System.in);
System.out.print("Enter a byte value: ");
byte byteValue = input.nextByte();
System.out.print("Enter a short value: ");
short shortValue = input.nextShort();
System.out.print("Enter an int value: ");
int intValue = input.nextInt();
System.out.print("Enter a long value: ");
long longValue = input.nextLong();
System.out.print("Enter a float value: ");
float floatValue = input.nextFloat();
```

If you enter a value with an incorrect range or format, a runtime error would occur. For example, you enter a value 128 for line 3, an error would occur because 128 is out of range for a byte type integer.

### 2.9.3 Numeric Operators

The operators for numeric data types include the standard arithmetic operators: addition (+), subtraction (−), multiplication (∗), division (/), and remainder (%), as shown in Table 2.3. The operands are the values operated by an operator.

<table>
<thead>
<tr>
<th>Name</th>
<th>Meaning</th>
<th>Example</th>
<th>Result</th>
</tr>
</thead>
<tbody>
<tr>
<td>+</td>
<td>Addition</td>
<td>34 + 1</td>
<td>35</td>
</tr>
<tr>
<td>−</td>
<td>Subtraction</td>
<td>34.0 − 0.1</td>
<td>33.9</td>
</tr>
<tr>
<td>∗</td>
<td>Multiplication</td>
<td>300 * 30</td>
<td>9000</td>
</tr>
<tr>
<td>/</td>
<td>Division</td>
<td>1.0 / 2.0</td>
<td>0.5</td>
</tr>
<tr>
<td>%</td>
<td>Remainder</td>
<td>20 % 3</td>
<td>2</td>
</tr>
</tbody>
</table>

When both operands of a division are integers, the result of the division is the quotient and the fractional part is truncated. For example, 5 / 2 yields 2, not 2.5, and −5 / 2 yields −2, not −2.5. To perform a float-point division, one of the operands must be a floating-point number. For example, 5.0 / 2 yields 2.5.

The % operator, known as remainder or modulo operator, yields the remainder after division. The operand on the left is the dividend and the operand on the right is the divisor. Therefore, 7 % 3 yields 1, 3 % 7 yields 3, 12 % 4 yields 0, 26 % 8 yields 2, and 20 % 13 yields 7.

```
\[
\begin{array}{c}
2 \\
3 \downarrow \\
7 \ 3 \\
6 \\
1
\end{array} \quad \begin{array}{c}
0 \\
4 \downarrow \\
0 \\
2
\end{array} \quad \begin{array}{c}
3 \\
8 \downarrow \\
0 \\
2
\end{array} \quad \begin{array}{c}
3 \\
26 \\
24 \\
7
\end{array}
\]
```

The % operator is often used for positive integers, but it can also be used with negative integers and floating-point values. The remainder is negative only if the dividend is negative. For example, −7 % 3 yields −1, −12 % 4 yields 0, −26 % −8 yields −2, and 20 % −13 yields 7.
Remainder is very useful in programming. For example, an even number \( \% 2 \) is always 0 and an odd number \( \% 2 \) is always 1. Thus, you can use this property to determine whether a number is even or odd. If today is Saturday, it will be Saturday again in 7 days. Suppose you and your friends are going to meet in 10 days. What day is in 10 days? You can find that the day is Tuesday using the following expression:

\[
(6 + 10) \% 7 = 2
\]

After 10 days

Day 2 in a week is Tuesday

Note: Day 0 in a week is Sunday

The program in Listing 2.5 obtains minutes and remaining seconds from an amount of time in seconds. For example, 500 seconds contains 8 minutes and 20 seconds.

**Listing 2.5 DisplayTime.java**

```java
import java.util.Scanner;

public class DisplayTime {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        // Prompt the user for input
        System.out.print("Enter an integer for seconds: ");
        int seconds = input.nextInt();

        int minutes = seconds / 60; // Find minutes in seconds
divide
        int remainingSeconds = seconds % 60; // Seconds remaining
remainder
        System.out.println(seconds + " seconds is " + minutes + " minutes and " + remainingSeconds + " seconds");
    }
}
```

Enter an integer for seconds: 500

500 seconds is 8 minutes and 20 seconds

<table>
<thead>
<tr>
<th>line#</th>
<th>seconds</th>
<th>minutes</th>
<th>remainingSeconds</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>500</td>
<td></td>
<td></td>
</tr>
<tr>
<td>10</td>
<td></td>
<td>8</td>
<td></td>
</tr>
<tr>
<td>11</td>
<td></td>
<td></td>
<td>20</td>
</tr>
</tbody>
</table>

The `nextInt()` method (line 8) reads an integer for `seconds`. Line 10 obtains the minutes using `seconds / 60`. Line 11 `(seconds % 60)` obtains the remaining seconds after taking away the minutes.

The `+` and `-` operators can be both unary and binary. A **unary** operator has only one operand; a **binary** operator has two. For example, the `-` operator in `-5` is a unary operator to negate number 5, whereas the `-` operator in `4 - 5` is a binary operator for subtracting 5 from 4.
2.9.4 Exponent Operations

The `Math.pow(a, b)` method can be used to compute \(a^b\). The `pow` method is defined in the `Math` class in the Java API. You invoke the method using the syntax `Math.pow(a, b)` (e.g., `Math.pow(2, 3)`), which returns the result of \(2^3\). Here, \(a\) and \(b\) are parameters for the `pow` method and the numbers 2 and 3 are actual values used to invoke the method. For example,

```java
System.out.println(Math.pow(2, 3)); // Displays 8.0
System.out.println(Math.pow(4, 0.5)); // Displays 2.0
System.out.println(Math.pow(2.5, 2)); // Displays 6.25
System.out.println(Math.pow(2.5, -2)); // Displays 0.16
```

Chapter 5 introduces more details on methods. For now, all you need to know is how to invoke the `pow` method to perform the exponent operation.

2.10 Find the largest and smallest `byte`, `short`, `int`, `long`, `float`, and `double`. Which of these data types requires the least amount of memory?

2.11 Show the result of the following remainders.

- \(56 \% 6\)
- \(78 \% -4\)
- \(-34 \% 5\)
- \(-34 \% -5\)
- \(5 \% 1\)
- \(1 \% 5\)

2.12 If today is Tuesday, what will be the day in 100 days?

2.13 What is the result of \(25 / 4\)? How would you rewrite the expression if you wished the result to be a floating-point number?

2.14 Show the result of the following code:

```java
System.out.println(2 * (5 / 2 + 5 / 2));
System.out.println(2 * 5 / 2 + 2 * 5 / 2);
System.out.println(2 * (5 / 2));
System.out.println(2 * 5 / 2);
```

2.15 Are the following statements correct? If so, show the output.

```java
System.out.println("25 / 4 is " + 25 / 4);
System.out.println("25 / 4.0 is " + 25 / 4.0);
System.out.println("3 * 2 / 4 is " + 3 * 2 / 4);
System.out.println("3.0 * 2 / 4 is " + 3.0 * 2 / 4);
```

2.16 Write a statement to display the result of \(2^{3.5}\).

2.17 Suppose \(m\) and \(r\) are integers. Write a Java expression for \(m^r\) to obtain a floating-point result.

2.10 Numeric Literals

A literal is a constant value that appears directly in a program.

For example, 34 and 0.305 are literals in the following statements:

```java
int numberOfYears = 34;
double weight = 0.305;
```
2.10 Numeric Literals

2.10.1 Integer Literals

An integer literal can be assigned to an integer variable as long as it can fit into the variable. A compile error will occur if the literal is too large for the variable to hold. The statement `byte b = 128;`, for example, will cause a compile error, because 128 cannot be stored in a variable of the `byte` type. (Note that the range for a byte value is from \(-128\) to \(127\).)

An integer literal is assumed to be of the `int` type, whose value is between \(-2^{31}\) (\(-2147483648\)) and \(2^{31} - 1\) (2147483647). To denote an integer literal of the `long` type, append the letter `L` or `l` to it. For example, to write integer 2147483648 in a Java program, you have to write it as `2147483648L` or `2147483648l`, because 2147483648 exceeds the range for the `int` value. `L` is preferred because `l` (lowercase `L`) can easily be confused with 1 (the digit one).

Note

By default, an integer literal is a decimal integer number. To denote a binary integer literal, use a leading `0b` or `0B` (zero B), to denote an octal integer literal, use a leading `0` (zero), and to denote a hexadecimal integer literal, use a leading `0x` or `0X` (zero X). For example.

```
System.out.println(0B1111); // Displays 15
System.out.println(07777); // Displays 4095
System.out.println(0XFFFF); // Displays 65535
```

Hexadecimal numbers, binary numbers, and octal numbers are introduced in Appendix F.

2.10.2 Floating-Point Literals

Floating-point literals are written with a decimal point. By default, a floating-point literal is treated as a `double` type value. For example, `5.0` is considered a `double` value, not a `float` value. You can make a number a `float` by appending the letter `f` or `F`, and you can make a number a `double` by appending the letter `d` or `D`. For example, you can use `100.2f` or `100.2F` for a `float` number, and `100.2d` or `100.2D` for a `double` number.

Note

The `double` type values are more accurate than the `float` type values. For example.
```
System.out.println("1.0 / 3.0 is " + 1.0 / 3.0);
```

```
displays 1.0 / 3.0 is 0.3333333333333333
```

16 digits

```
System.out.println("1.0F / 3.0F is " + 1.0F / 3.0F);
```

```
displays 1.0F / 3.0F is 0.33333334
```

8 digits

A float value has 7 to 8 number of significant digits and a double value has 15 to 17 number of significant digits.

2.10.3 Scientific Notation

Floating-point literals can be written in scientific notation in the form of \(a \times 10^b\). For example, the scientific notation for 123.456 is \(1.23456 \times 10^2\) and for 0.0123456 is \(1.23456 \times 10^{-2}\). A special syntax is used to write scientific notation numbers. For example, 1.23456 \(\times 10^2\) is written as `1.23456E2` or `1.23456e+2` and 1.23456 \(\times 10^{-2}\) as `1.23456E-2`. E (or e) represents an exponent and can be in either lowercase or uppercase.
Why called floating-point?

**Note**
The `float` and `double` types are used to represent numbers with a decimal point. Why are they called `floating-point numbers`? These numbers are stored in scientific notation internally. When a number such as `50.534` is converted into scientific notation, such as `5.0354E+1`, its decimal point is moved (i.e., floated) to a new position.

**Note**
To improve readability, Java allows you to use underscores between two digits in a number literal. For example, the following literals are correct.

```java
long ssn = 232_45_4519;
long creditCardNumber = 232_4545_4519_3415L;
```

However, `45_` or `_45` is incorrect. The underscore must be placed between two digits.

2.18 How many accurate digits are stored in a `float` or `double` type variable?

2.19 Which of the following are correct literals for floating-point numbers?

```java
12.3, 12.3e+2, 23.4e-2, -334.4, 20.5, 39F, 40D
```

2.20 Which of the following are the same as `52.534`?

```java
5.2534e+1, 0.52534e+2, 525.34e-1, 5.2534e+0
```

2.21 Which of the following are correct literals?

```java
5_2534e+1, _2534, 5_2, _5
```

### 2.11 Evaluating Expressions and Operator Precedence

*Java expressions are evaluated in the same way as arithmetic expressions.*

Writing a numeric expression in Java involves a straightforward translation of an arithmetic expression using Java operators. For example, the arithmetic expression

\[
\frac{3 + 4x}{5} - \frac{10(y - 5)(a + b + c)}{x} + 9\left(\frac{4}{x} + \frac{9 + x}{y}\right)
\]

can be translated into a Java expression as:

```java
(3 + 4 * x) / 5 - 10 * (y - 5) * (a + b + c) / x + 9 * (4 / x + (9 + x) / y)
```

Though Java has its own way to evaluate an expression behind the scene, the result of a Java expression and its corresponding arithmetic expression is the same. Therefore, you can safely apply the arithmetic rule for evaluating a Java expression. Operators contained within pairs of parentheses are evaluated first. Parentheses can be nested, in which case the expression in the inner parentheses is evaluated first. When more than one operator is used in an expression, the following operator precedence rule is used to determine the order of evaluation.

- Multiplication, division, and remainder operators are applied first. If an expression contains several multiplication, division, and remainder operators, they are applied from left to right.
- Addition and subtraction operators are applied last. If an expression contains several addition and subtraction operators, they are applied from left to right.
Here is an example of how an expression is evaluated:

\[
3 + 4 \times 4 + 5 \times (4 + 3) - 1
\]

1. inside parentheses first

\[
3 + 4 \times 4 + 5 \times 7 - 1
\]

2. multiplication

\[
3 + 16 + 5 \times 7 - 1
\]

3. multiplication

\[
3 + 16 + 35 - 1
\]

4. addition

\[
19 + 35 - 1
\]

5. addition

\[
54 - 1
\]

6. subtraction

Listing 2.6 gives a program that converts a Fahrenheit degree to Celsius using the formula

celsius = \left(\frac{5}{9}\right)(fahrenheit - 32).

Listing 2.6 FahrenheitToCelsius.java

```java
import java.util.Scanner;

public class FahrenheitToCelsius {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);

        System.out.print("Enter a degree in Fahrenheit: ");
        double fahrenheit = input.nextDouble();

        // Convert Fahrenheit to Celsius
        double celsius = (5.0 / 9) * (fahrenheit - 32);
        System.out.println("Fahrenheit " + fahrenheit + " is " + celsius + " in Celsius");
    }
}
```

Enter a degree in Fahrenheit: 100
Fahrenheit 100.0 is 37.77777777777778 in Celsius

<table>
<thead>
<tr>
<th>line#</th>
<th>fahrenheit</th>
<th>celsius</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>100</td>
<td></td>
</tr>
<tr>
<td>11</td>
<td>37.77777777777778</td>
<td></td>
</tr>
</tbody>
</table>
2.12 Case Study: Displaying the Current Time

You can invoke `System.currentTimeMillis()` to return the current time.

The problem is to develop a program that displays the current time in GMT (Greenwich Mean Time) in the format hour:minute:second, such as 13:19:8.

The `currentTimeMillis` method in the `System` class returns the current time in milliseconds elapsed since midnight, January 1, 1970 GMT, as shown in Figure 2.2. This time is known as the `UNIX epoch`. The epoch is the point when time starts, and 1970 was the year when the UNIX operating system was formally introduced.

![Figure 2.2](image)

You can use this method to obtain the current time, and then compute the current second, minute, and hour as follows.

1. Obtain the total milliseconds since midnight, January 1, 1970, in `totalMilliseconds` by invoking `System.currentTimeMillis()` (e.g., 1203183068328 milliseconds).

2. Obtain the total seconds `totalSeconds` by dividing `totalMilliseconds` by 1000 (e.g., 1203183068328 milliseconds / 1000 = 1203183068 seconds).

3. Compute the current second from `totalSeconds % 60` (e.g., 1203183068 seconds % 60 = 8, which is the current second).

4. Obtain the total minutes `totalMinutes` by dividing `totalSeconds` by 60 (e.g., 1203183068 seconds / 60 = 20053051 minutes).

5. Compute the current minute from `totalMinutes % 60` (e.g., 20053051 minutes % 60 = 31, which is the current minute).

6. Obtain the total hours `totalHours` by dividing `totalMinutes` by 60 (e.g., 20053051 minutes / 60 = 334217 hours).

7. Compute the current hour from `totalHours % 24` (e.g., 334217 hours % 24 = 17, which is the current hour).

Listing 2.7 gives the complete program.

Listing 2.7 ShowCurrentTime.java

```java
public class ShowCurrentTime {
    public static void main(String[] args) {
        // Obtain the total milliseconds since midnight, Jan 1, 1970
        long totalMilliseconds = System.currentTimeMillis();
        // Obtain the total seconds since midnight, Jan 1, 1970
        long totalSeconds = totalMilliseconds / 1000;
        // Compute the current second in the minute in the hour
        long currentSecond = totalSeconds % 60;
    }
}
```
2.12 Case Study: Displaying the Current Time

```java
// Obtain the total minutes
long totalMinutes = totalSeconds / 60;

// Compute the current minute in the hour
long currentMinute = totalMinutes % 60;

// Obtain the total hours
long totalHours = totalMinutes / 60;

// Compute the current hour
long currentHour = totalHours % 24;

// Display results
System.out.println("Current time is "+ currentHour + ":"+
        currentMinute + ":" + currentSecond + " GMT");
```

Current time is 17:31:8 GMT

Line 4 invokes `System.currentTimeMillis()` to obtain the current time in milliseconds as a `long` value. Thus, all the variables are declared as the long type in this program. The seconds, minutes, and hours are extracted from the current time using the `/` and `%` operators (lines 6–22).

In the sample run, a single digit 8 is displayed for the second. The desirable output would be 08. This can be fixed by using a method that formats a single digit with a prefix 0 (see Exercise 6.37).

### 2.23 How do you obtain the current second, minute, and hour?
2.13 Augmented Assignment Operators

The operators +, -, *, /, and % can be combined with the assignment operator to form augmented operators.

Very often the current value of a variable is used, modified, and then reassigned back to the same variable. For example, the following statement increases the variable count by 1:

\[ \text{count} = \text{count} + 1; \]

Java allows you to combine assignment and addition operators using an augmented (or compound) assignment operator. For example, the preceding statement can be written as

\[ \text{count} += 1; \]

The += is called the addition assignment operator. Table 2.4 shows other augmented assignment operators.

<table>
<thead>
<tr>
<th>Operator</th>
<th>Name</th>
<th>Example</th>
<th>Equivalent</th>
</tr>
</thead>
<tbody>
<tr>
<td>+=</td>
<td>Addition assignment</td>
<td>i += 8</td>
<td>i = i + 8</td>
</tr>
<tr>
<td>-=</td>
<td>Subtraction assignment</td>
<td>i -= 8</td>
<td>i = i - 8</td>
</tr>
<tr>
<td>*=</td>
<td>Multiplication assignment</td>
<td>i *= 8</td>
<td>i = i * 8</td>
</tr>
<tr>
<td>/=</td>
<td>Division assignment</td>
<td>i /= 8</td>
<td>i = i / 8</td>
</tr>
<tr>
<td>%=</td>
<td>Remainder assignment</td>
<td>i %= 8</td>
<td>i = i % 8</td>
</tr>
</tbody>
</table>

The augmented assignment operator is performed last after all the other operators in the expression are evaluated. For example,

\[ x /= 4 + 5.5 * 1.5; \]

is same as

\[ x = x / (4 + 5.5 * 1.5); \]

Caution

There are no spaces in the augmented assignment operators. For example, + = should be +=.

Note

Like the assignment operator (=), the operators (+=, -=, *=, /=, %=) can be used to form an assignment statement as well as an expression. For example, in the following code, \( x += 2 \) is a statement in the first line and an expression in the second line.

\[ x += 2; // Statement \]
\[ System.out.println(x += 2); // Expression \]

2.24 Show the output of the following code:

```java
double a = 6.5;
a += a + 1;
```
2.14 Increment and Decrement Operators

The increment operator (++) and decrement operator (--) are for incrementing and decrementing a variable by 1.

The ++ and -- are two shorthand operators for incrementing and decrementing a variable by 1. These are handy because that’s often how much the value needs to be changed in many programming tasks. For example, the following code increments i by 1 and decrements j by 1.

```java
int i = 3, j = 3;
i++; // i becomes 4
j--; // j becomes 2
```

++i is pronounced as i plus plus and i-- as i minus minus. These operators are known as **postfix increment** (or postincrement) and **postfix decrement** (or postdecrement), because the operators ++ and -- are placed after the variable. These operators can also be placed before the variable. For example,

```java
int i = 3, j = 3;
++i; // i becomes 4
--j; // j becomes 2
```

++i increments i by 1 and --j decrements j by 1. These operators are known as **prefix increment** (or preincrement) and **prefix decrement** (or predecrement).

As you see, the effect of i++ and ++i or i-- and --i are the same in the preceding examples. However, their effects are different when they are used in statements that do more than just increment and decrement. Table 2.5 describes their differences and gives examples.

### Table 2.5 Increment and Decrement Operators

<table>
<thead>
<tr>
<th>Operator</th>
<th>Name</th>
<th>Description</th>
<th>Example (assume i = 1)</th>
</tr>
</thead>
<tbody>
<tr>
<td>++var</td>
<td>preincrement</td>
<td>Increment var by 1, and use the new var value in the statement</td>
<td>int j = ++i;</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>// j is 2, i is 2</td>
</tr>
<tr>
<td>var++</td>
<td>postincrement</td>
<td>Increment var by 1, but use the original var value in the statement</td>
<td>int j = i++;</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>// j is 1, i is 2</td>
</tr>
<tr>
<td>--var</td>
<td>predecrement</td>
<td>Decrement var by 1, and use the new var value in the statement</td>
<td>int j = --i;</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>// j is 0, i is 0</td>
</tr>
<tr>
<td>var--</td>
<td>postdecrement</td>
<td>Decrement var by 1, and use the original var value in the statement</td>
<td>int j = i--;</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td>// j is 1, i is 0</td>
</tr>
</tbody>
</table>

Here are additional examples to illustrate the differences between the prefix form of ++ (or --) and the postfix form of ++ (or --). Consider the following code:

```java
int i = 10;
int newNum = 10 * i++;  // Same effect as
int newNum = 10 * i;
i = i + 1;
```

```
i is 11, newNum is 100
```
In this case, \( i \) is incremented by 1, then the old value of \( i \) is used in the multiplication. So \( newNum \) becomes 100. If \( i++ \) is replaced by \( ++i \) as follows,

\[
\begin{align*}
\text{int } i &= 10; \\
\text{int } newNum &= 10 \times (++i); \quad \text{Same effect as} \\
\text{int } i &= i + 1; \\
\text{int } newNum &= 10 \times i;
\end{align*}
\]

\[
\text{System.out.print("i is "+ i} \\
\text{+ ", newNum is "+ newNum);
\]

\[
i \text{ is 11, newNum is 110}
\]

\( i \) is incremented by 1, and the new value of \( i \) is used in the multiplication. Thus \( newNum \) becomes 110.

Here is another example:

\[
\begin{align*}
\text{double } x &= 1.0; \\
\text{double } y &= 5.0; \\
\text{double } z &= x-- + (++y);
\end{align*}
\]

After all three lines are executed, \( y \) becomes 6.0, \( z \) becomes 7.0, and \( x \) becomes 0.0.

**Tip**
Using increment and decrement operators makes expressions short, but it also makes them complex and difficult to read. Avoid using these operators in expressions that modify multiple variables or the same variable multiple times, such as this one: \( \text{int } k = ++i + i \).

2.25 Which of these statements are true?

a. Any expression can be used as a statement.

b. The expression \( x++ \) can be used as a statement.

c. The statement \( x = x + 5 \) is also an expression.

d. The statement \( x = y = x = 0 \) is illegal.

2.26 Show the output of the following code:

\[
\begin{align*}
\text{int } a &= 6; \\
\text{int } b &= a++; \\
\text{System.out.println(a);} \\
\text{System.out.println(b);} \\
\text{a} &= 6; \\
\text{b} &= ++a; \\
\text{System.out.println(a);} \\
\text{System.out.println(b);} \\
\end{align*}
\]

2.15 Numeric Type Conversions

*Floating-point numbers can be converted into integers using explicit casting.*

Can you perform binary operations with two operands of different types? Yes. If an integer and a floating-point number are involved in a binary operation, Java automatically converts the integer to a floating-point value. So, \( 3 \times 4.5 \) is same as \( 3.0 \times 4.5 \).
You can always assign a value to a numeric variable whose type supports a larger range of values; thus, for instance, you can assign a `long` value to a `float` variable. You cannot, however, assign a value to a variable of a type with a smaller range unless you use type casting. Casting is an operation that converts a value of one data type into a value of another data type. Casting a type with a small range to a type with a larger range is known as **widening a type**. Casting a type with a large range to a type with a smaller range is known as **narrowing a type**. Java will automatically widen a type, but you must narrow a type explicitly.

The syntax for casting a type is to specify the target type in parentheses, followed by the variable’s name or the value to be cast. For example, the following statement

```java
System.out.println((int)1.7);
```

displays 1. When a `double` value is cast into an `int` value, the fractional part is truncated.

The following statement

```java
System.out.println((double)1 / 2);
```

displays 0.5, because 1 is cast to 1.0 first, then 1.0 is divided by 2. However, the statement

```java
System.out.println(1 / 2);
```

displays 0, because 1 and 2 are both integers and the resulting value should also be an integer.

**Caution**
Casting is necessary if you are assigning a value to a variable of a smaller type range, such as assigning a `double` value to an `int` variable. A compile error will occur if casting is not used in situations of this kind. However, be careful when using casting, as loss of information might lead to inaccurate results.

**Note**
Casting does not change the variable being cast. For example, `d` is not changed after casting in the following code:

```java
double d = 4.5;
int i = (int)d; // i becomes 4, but d is still 4.5
```

**Note**
In Java, an augmented expression of the form `x1 op= x2` is implemented as `x1 = (T)(x1 op x2)`, where `T` is the type for `x1`. Therefore, the following code is correct.

```java
int sum = 0;
sum += 4.5; // sum becomes 4 after this statement
sum += 4.5 is equivalent to sum = (int)(sum + 4.5).
```

**Note**
To assign a variable of the `int` type to a variable of the `short` or `byte` type, explicit casting must be used. For example, the following statements have a compile error:

```java
int i = 1;
byte b = i; // Error because explicit casting is required
```

However, so long as the integer literal is within the permissible range of the target variable, explicit casting is not needed to assign an integer literal to a variable of the `short` or `byte` type (see Section 2.10, Numeric Literals).

The program in Listing 2.8 displays the sales tax with two digits after the decimal point.
**LISTING 2.8  SalesTax.java**

```java
import java.util.Scanner;

public class SalesTax {
  public static void main(String[] args) {
    Scanner input = new Scanner(System.in);
    System.out.print("Enter purchase amount: ");
    double purchaseAmount = input.nextDouble();
    double tax = purchaseAmount * 0.06;
    System.out.println("Sales tax is $" + (int)(tax * 100) / 100.0);
  }
}
```

Enter purchase amount: 197.55
Sales tax is $11.85

<table>
<thead>
<tr>
<th>line#</th>
<th>purchaseAmount</th>
<th>tax</th>
<th>output</th>
</tr>
</thead>
<tbody>
<tr>
<td>8</td>
<td>197.55</td>
<td></td>
<td></td>
</tr>
<tr>
<td>10</td>
<td></td>
<td>11.853</td>
<td></td>
</tr>
<tr>
<td>11</td>
<td></td>
<td></td>
<td>11.85</td>
</tr>
</tbody>
</table>

The variable `purchaseAmount` is 197.55 (line 8). The sales tax is 6% of the purchase, so the tax is evaluated as 11.853 (line 10). Note that:

- `tax * 100` is 1185.3
- `(int)(tax * 100)` is 1185
- `(int)(tax * 100) / 100.0` is 11.85

So, the statement in line 11 displays the tax 11.85 with two digits after the decimal point.

**Check Point**

2.27 Can different types of numeric values be used together in a computation?

2.28 What does an explicit casting from a `double` to an `int` do with the fractional part of the `double` value? Does casting change the variable being cast?

2.29 Show the following output:

```java
float f = 12.5F;
int i = (int)f;
System.out.println("f is " + f);
System.out.println("i is " + i);
```

2.30 If you change `(int)(tax * 100) / 100.0` to `(int)(tax * 100) / 100` in line 11 in Listing 2.8, what will be the output for the input purchase amount of 197.55?

2.31 Show the output of the following code:

```java
double amount = 5;
System.out.println(amount / 2);
System.out.println(5 / 2);
```
Software Development Process

The software development life cycle is a multistage process that includes requirements specification, analysis, design, implementation, testing, deployment, and maintenance.

Developing a software product is an engineering process. Software products, no matter how large or how small, have the same life cycle: requirements specification, analysis, design, implementation, testing, deployment, and maintenance, as shown in Figure 2.3.

**Requirements specification** is a formal process that seeks to understand the problem that the software will address and to document in detail what the software system needs to do. This phase involves close interaction between users and developers. Most of the examples in this book are simple, and their requirements are clearly stated. In the real world, however, problems are not always well defined. Developers need to work closely with their customers (the individuals or organizations that will use the software) and study the problem carefully to identify what the software needs to do.

**System analysis** seeks to analyze the data flow and to identify the system’s input and output. When you do analysis, it helps to identify what the output is first, and then figure out what input data you need in order to produce the output.

**System design** is to design a process for obtaining the output from the input. This phase involves the use of many levels of abstraction to break down the problem into manageable components and design strategies for implementing each component. You can view each component as a subsystem that performs a specific function of the system. The essence of system analysis and design is input, process, and output (IPO).

**Implementation** involves translating the system design into programs. Separate programs are written for each component and then integrated to work together. This phase requires the use of a programming language such as Java. The implementation involves coding, self-testing, and debugging (that is, finding errors, called bugs, in the code).
Testing ensures that the code meets the requirements specification and weeds out bugs. An independent team of software engineers not involved in the design and implementation of the product usually conducts such testing.

Deployment makes the software available for use. Depending on the type of software, it may be installed on each user’s machine or installed on a server accessible on the Internet.

Maintenance is concerned with updating and improving the product. A software product must continue to perform and improve in an ever-evolving environment. This requires periodic upgrades of the product to fix newly discovered bugs and incorporate changes.

To see the software development process in action, we will now create a program that computes loan payments. The loan can be a car loan, a student loan, or a home mortgage loan. For an introductory programming course, we focus on requirements specification, analysis, design, implementation, and testing.

Stage 1: Requirements Specification

The program must satisfy the following requirements:

- It must let the user enter the interest rate, the loan amount, and the number of years for which payments will be made.
- It must compute and display the monthly payment and total payment amounts.

Stage 2: System Analysis

The output is the monthly payment and total payment, which can be obtained using the following formulas:

\[
\text{monthlyPayment} = \frac{\text{loanAmount} \times \text{monthlyInterestRate}}{1 - \frac{1}{(1 + \text{monthlyInterestRate})^{\text{numberOfYears} \times 12}}}
\]

\[
\text{totalPayment} = \text{monthlyPayment} \times \text{numberOfYears} \times 12
\]

So, the input needed for the program is the monthly interest rate, the length of the loan in years, and the loan amount.

Note

The requirements specification says that the user must enter the annual interest rate, the loan amount, and the number of years for which payments will be made. During analysis, however, it is possible that you may discover that input is not sufficient or that some values are unnecessary for the output. If this happens, you can go back and modify the requirements specification.

Note

In the real world, you will work with customers from all walks of life. You may develop software for chemists, physicists, engineers, economists, and psychologists, and of course you will not have (or need) complete knowledge of all these fields. Therefore, you don’t have to know how formulas are derived, but given the monthly interest rate, the number of years, and the loan amount, you can compute the monthly payment in this program. You will, however, need to communicate with customers and understand how a mathematical model works for the system.
Stage 3: System Design

During system design, you identify the steps in the program.

Step 1. Prompt the user to enter the annual interest rate, the number of years, and the loan amount.

(The interest rate is commonly expressed as a percentage of the principal for a period of one year. This is known as the annual interest rate.)

Step 2. The input for the annual interest rate is a number in percent format, such as 4.5%. The program needs to convert it into a decimal by dividing it by 100. To obtain the monthly interest rate from the annual interest rate, divide it by 12, since a year has 12 months. So, to obtain the monthly interest rate in decimal format, you need to divide the annual interest rate in percentage by 1200. For example, if the annual interest rate is 4.5%, then the monthly interest rate is 4.5/1200 = 0.00375.

Step 3. Compute the monthly payment using the preceding formula.

Step 4. Compute the total payment, which is the monthly payment multiplied by 12 and multiplied by the number of years.

Step 5. Display the monthly payment and total payment.

Stage 4: Implementation

Implementation is also known as coding (writing the code). In the formula, you have to compute \((1 + \text{monthlyInterestRate})^{\text{numberOfYears} \times 12}\), which can be obtained using \(\text{Math.pow}(1 + \text{monthlyInterestRate}, \text{numberOfYears} \times 12)\).

Listing 2.9 gives the complete program.

**Listing 2.9 ComputeLoan.java**

```java
import java.util.Scanner;

public class ComputeLoan {

public static void main(String[] args) {

    Scanner input = new Scanner(System.in);

    System.out.print("Enter annual interest rate, e.g., 7.25%: ");
    double annualInterestRate = input.nextDouble();

    double monthlyInterestRate = annualInterestRate / 1200;

    System.out.print("Enter number of years as an integer, e.g., 5: ");
    int numberOfYears = input.nextInt();

    double loanAmount = input.nextDouble();

    System.out.print("Enter loan amount, e.g., 120000.95: ");

    double monthlyPayment = loanAmount * monthlyInterestRate / (1 - 1 / Math.pow(1 + monthlyInterestRate, numberOfYears * 12));
```

```
double totalPayment = monthlyPayment * numberOfYears * 12;

// Display results
System.out.println("The monthly payment is "+
(int)(monthlyPayment * 100) / 100.0);
System.out.println("The total payment is "+
(int)(totalPayment * 100) / 100.0);
}

Enter annual interest rate, e.g., 5.75%: 5.75
Enter number of years as an integer, e.g., 5: 15
Enter loan amount, e.g., 120000.95: 250000
The monthly payment is $2076.02
The total payment is $373684.53

<table>
<thead>
<tr>
<th>line#</th>
<th>10</th>
<th>13</th>
<th>18</th>
<th>22</th>
<th>25</th>
<th>27</th>
</tr>
</thead>
<tbody>
<tr>
<td>variables</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>annualInterestRate</td>
<td>5.75</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>monthlyInterestRate</td>
<td>0.0047916666666</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>numberOfYears</td>
<td>15</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>loanAmount</td>
<td>250000</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>monthlyPayment</td>
<td>2076.0252175</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>totalPayment</td>
<td>373684.539</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Line 10 reads the annual interest rate, which is converted into the monthly interest rate in line 13.

Choose the most appropriate data type for the variable. For example, numberOfYears is best declared as an int (line 18), although it could be declared as a long, float, or double. Note that byte might be the most appropriate for numberOfYears. For simplicity, however, the examples in this book will use int for integer and double for floating-point values.

The formula for computing the monthly payment is translated into Java code in lines 25–27. Casting is used in lines 31 and 33 to obtain a new monthlyPayment and totalPayment with two digits after the decimal points.

The program uses the Scanner class, imported in line 1. The program also uses the Math class, and you might be wondering why that class isn’t imported into the program. The Math class is in the java.lang package, and all classes in the java.lang package are implicitly imported. Therefore, you don’t need to explicitly import the Math class.

Stage 5: Testing

After the program is implemented, test it with some sample input data and verify whether the output is correct. Some of the problems may involve many cases, as you will see in later chapters. For these types of problems, you need to design test data that cover all cases.

Tip

The system design phase in this example identified several steps. It is a good approach to code and test these steps incrementally by adding them one at a time. This approach makes it much easier to pinpoint problems and debug the program.
2.17 Case Study: Counting Monetary Units

This section presents a program that breaks a large amount of money into smaller units.

Suppose you want to develop a program that changes a given amount of money into smaller monetary units. The program lets the user enter an amount as a double value representing a total in dollars and cents, and outputs a report listing the monetary equivalent in the maximum number of dollars, quarters, dimes, nickels, and pennies, in this order, to result in the minimum number of coins.

Here are the steps in developing the program:

1. Prompt the user to enter the amount as a decimal number, such as 11.56.
2. Convert the amount (e.g., 11.56) into cents (1156).
3. Divide the cents by 100 to find the number of dollars. Obtain the remaining cents using the cents remainder.
4. Divide the remaining cents by 25 to find the number of quarters. Obtain the remaining cents using the remaining cents remainder 25.
5. Divide the remaining cents by 10 to find the number of dimes. Obtain the remaining cents using the remaining cents remainder 10.
6. Divide the remaining cents by 5 to find the number of nickels. Obtain the remaining cents using the remaining cents remainder 5.
7. The remaining cents are the pennies.
8. Display the result.

The complete program is given in Listing 2.10.

Listing 2.10 ComputeChange.java

```java
import java.util.Scanner;

public class ComputeChange {
    public static void main(String[] args) {
        // Create a Scanner
        Scanner input = new Scanner(System.in);

        // Receive the amount
        System.out.print("Enter an amount in double, for example 11.56: ");
        double amount = input.nextDouble();

        // Find the number of one dollars
        int remainingAmount = (int)(amount * 100);

        // Find the number of quarters in the remaining amount
        int numberOfQuarters = remainingAmount / 25;

        // Find the number of dimes in the remaining amount
        int numberOfDimes = (remainingAmount % 25) / 10;

        // Find the number of nickels in the remaining dimes
        int numberOfNickels = (remainingAmount % 10) / 5;

        // Find the number of pennies in the remaining nickels
        int numberOfPennies = (remainingAmount % 5);

        System.out.println("The amount " + amount + " is equivalent to ",
                          numberOfQuarters + "quarters, ",
                          numberOfDimes + "dimes, ",
                          numberOfNickels + "nickels, and ",
                          numberOfPennies + "pennies.");
    }
}
```

2.32 How would you write the following arithmetic expression?

\[-b + \sqrt{b^2 - 4ac} \over 2a\]
remainingAmount = remainingAmount % 25;

// Find the number of dimes in the remaining amount

int numberOfDimes = remainingAmount / 10;
remainingAmount = remainingAmount % 10;

// Find the number of nickels in the remaining amount

int numberOfNickels = remainingAmount / 5;
remainingAmount = remainingAmount % 5;

// Find the number of pennies in the remaining amount

int numberOfPennies = remainingAmount;

// Display results

System.out.println("Your amount " + amount + " consists of ");
System.out.println("    "+ numberOfOneDollars + " dollars ");
System.out.println("    "+ numberOfQuarters + " quarters ");
System.out.println("    "+ numberOfDimes + " dimes ");
System.out.println("    "+ numberOfNickels + " nickels ");
System.out.println("    "+ numberOfPennies + " pennies ");

Enter an amount, for example, 11.56: 11.56 Enter

Your amount 11.56 consists of
  11 dollars
  2 quarters
  0 dimes
  1 nickels
  1 pennies

<table>
<thead>
<tr>
<th>line#</th>
<th>11</th>
<th>13</th>
<th>16</th>
<th>17</th>
<th>20</th>
<th>21</th>
<th>24</th>
<th>25</th>
<th>28</th>
<th>29</th>
<th>32</th>
</tr>
</thead>
<tbody>
<tr>
<td>amount</td>
<td>11.56</td>
<td></td>
<td></td>
<td></td>
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<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>remainingAmount</td>
<td>1156</td>
<td>56</td>
<td>6</td>
<td>6</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>numberOfOneDollars</td>
<td>11</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>numberOfQuarters</td>
<td>2</td>
<td></td>
<td></td>
<td></td>
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<td></td>
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</tr>
<tr>
<td>numberOfDimes</td>
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<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>numberOfNickels</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>numberOfPennies</td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The variable `amount` stores the amount entered from the console (line 11). This variable is not changed, because the amount has to be used at the end of the program to display the results. The program introduces the variable `remainingAmount` (line 13) to store the changing remaining amount.

The variable `amount` is a double decimal representing dollars and cents. It is converted to an int variable `remainingAmount`, which represents all the cents. For instance, if `amount`
is 11.56, then the initial remainingAmount is 1156. The division operator yields the integer part of the division, so 1156 / 100 is 11. The remainder operator obtains the remainder of the division, so 1156 % 100 is 56.

The program extracts the maximum number of singles from the remaining amount and obtains a new remaining amount in the variable remainingAmount (lines 16–17). It then extracts the maximum number of quarters from remainingAmount and obtains a new remainingAmount (lines 20–21). Continuing the same process, the program finds the maximum number of dimes, nickels, and pennies in the remaining amount.

One serious problem with this example is the possible loss of precision when casting a double amount to an int remainingAmount. This could lead to an inaccurate result. If you try to enter the amount 10.03 * 100 becomes 1002.9999999999999. You will find that the program displays 10 dollars and 2 pennies. To fix the problem, enter the amount as an integer value representing cents (see Programming Exercise 2.22).

2.33 Show the output with the input value 1.99.

2.18 Common Errors and Pitfalls

Common elementary programming errors often involve undeclared variables, uninitialized variables, integer overflow, unintended integer division, and round-off errors.

Common Error 1: Undeclared/Uninitialized Variables and Unused Variables

A variable must be declared with a type and assigned a value before using it. A common error is not declaring a variable or initializing a variable. Consider the following code:

```java
double interestRate = 0.05;
double interest = interestrate * 45;
```

This code is wrong, because interestRate is assigned a value 0.05; but interestrate has not been declared and initialized. Java is case sensitive, so it considers interestRate and interestrate to be two different variables.

If a variable is declared, but not used in the program, it might be a potential programming error. So, you should remove the unused variable from your program. For example, in the following code, taxRate is never used. It should be removed from the code.

```java
double interestRate = 0.05;
double taxRate = 0.05;
double interest = interestRate * 45;
System.out.println("Interest is " + interest);
```

If you use an IDE such as Eclipse and NetBeans, you will receive a warning on unused variables.

Common Error 2: Integer Overflow

Numbers are stored with a limited numbers of digits. When a variable is assigned a value that is too large (in size) to be stored, it causes overflow. For example, executing the following statement causes overflow, because the largest value that can be stored in a variable of the int type is 2147483647. 2147483648 will be too large for an int value.

```java
int value = 2147483647 + 1;
// value will actually be -2147483648
```

Likewise, executing the following statement causes overflow, because the smallest value that can be stored in a variable of the int type is -2147483648. -2147483649 is too large in size to be stored in an int variable.
int value = -2147483648 - 1;
// value will actually be 2147483647

Java does not report warnings or errors on overflow, so be careful when working with numbers close to the maximum or minimum range of a given type.

When a floating-point number is too small (i.e., too close to zero) to be stored, it causes underflow. Java approximates it to zero, so normally you don’t need to be concerned about underflow.

**Common Error 3: Round-off Errors**

A round-off error, also called a rounding error, is the difference between the calculated approximation of a number and its exact mathematical value. For example, 1/3 is approximately 0.333 if you keep three decimal places, and is 0.3333333 if you keep seven decimal places. Since the number of digits that can be stored in a variable is limited, round-off errors are inevitable. Calculations involving floating-point numbers are approximated because these numbers are not stored with complete accuracy. For example,

```java
System.out.println(1.0 - 0.1 - 0.1 - 0.1 - 0.1 - 0.1);
```
displays 0.5000000000000001, not 0.5, and

```java
System.out.println(1.0 - 0.9);
```
displays 0.09999999999999998, not 0.1. Integers are stored precisely. Therefore, calculations with integers yield a precise integer result.

**Common Error 4: Unintended Integer Division**

Java uses the same divide operator, namely /, to perform both integer and floating-point division. When two operands are integers, the / operator performs an integer division. The result of the operation is an integer. The fractional part is truncated. To force two integers to perform a floating-point division, make one of the integers into a floating-point number. For example, the code in (a) displays that average is 1 and the code in (b) displays that average is 1.5.

```java
int number1 = 1;
int number2 = 2;
double average = (number1 + number2) / 2;
System.out.println(average);
```
(a)

```java
int number1 = 1;
int number2 = 2;
double average = (number1 + number2) / 2.0;
System.out.println(average);
```
(b)

**Common Pitfall 1: Redundant Input Objects**

New programmers often write the code to create multiple input objects for each input. For example, the following code reads an integer and a double value.

```java
Scanner input = new Scanner(System.in);
System.out.print("Enter an integer: ");
int v1 = input.nextInt();

Scanner input1 = new Scanner(System.in);
System.out.print("Enter a double value: ");
double v2 = input1.nextDouble();
```
BAD CODE
The code is not wrong, but inefficient. It creates two input objects unnecessarily and may lead to some subtle errors. You should rewrite the code as follows:

```java
Scanner input = new Scanner(System.in);
System.out.print("Enter an integer: ");
int v1 = input.nextInt();
System.out.print("Enter a double value: ");
double v2 = input.nextDouble();
```

2.34 Can you declare a variable as `int` and later redeclare it as `double`?

2.35 What is an integer overflow? Can floating-point operations cause overflow?

2.36 Will overflow cause a runtime error?

2.37 What is a round-off error? Can integer operations cause round-off errors? Can floating-point operations cause round-off errors?

---

### Key Terms

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---

### Chapter Summary

1. **Identifiers** are names for naming elements such as variables, constants, methods, classes, packages in a program.

2. An identifier is a sequence of characters that consists of letters, digits, underscores (_), and dollar signs ($). An identifier must start with a letter or an underscore. It cannot start with a digit. An identifier cannot be a reserved word. An identifier can be of any length.

3. **Variables** are used to store data in a program. To declare a variable is to tell the compiler what type of data a variable can hold.
4. There are two types of import statements: specific import and wildcard import. The specific import specifies a single class in the import statement; the wildcard import imports all the classes in a package.

5. In Java, the equal sign (=) is used as the assignment operator.

6. A variable declared in a method must be assigned a value before it can be used.

7. A named constant (or simply a constant) represents permanent data that never changes.

8. A named constant is declared by using the keyword final.

9. Java provides four integer types (byte, short, int, and long) that represent integers of four different sizes.

10. Java provides two floating-point types (float and double) that represent floating-point numbers of two different precisions.

11. Java provides operators that perform numeric operations: + (addition), − (subtraction), * (multiplication), / (division), and % (remainder).

12. Integer arithmetic (/) yields an integer result.

13. The numeric operators in a Java expression are applied the same way as in an arithmetic expression.

14. Java provides the augmented assignment operators += (addition assignment), −= (subtraction assignment), *= (multiplication assignment), /= (division assignment), and %= (remainder assignment).

15. The increment operator (++) and the decrement operator (––) increment or decrement a variable by 1.

16. When evaluating an expression with values of mixed types, Java automatically converts the operands to appropriate types.

17. You can explicitly convert a value from one type to another using the (type)value notation.

18. Casting a variable of a type with a small range to a variable of a type with a larger range is known as widening a type.

19. Casting a variable of a type with a large range to a variable of a type with a smaller range is known as narrowing a type.

20. Widening a type can be performed automatically without explicit casting. Narrowing a type must be performed explicitly.

21. In computer science, midnight of January 1, 1970, is known as the UNIX epoch.

Quiz

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.
Programming Exercises

Debugging TIP
The compiler usually gives a reason for a syntax error. If you don’t know how to correct it, compare your program closely, character by character, with similar examples in the text.

Pedagogical Note
Instructors may ask you to document your analysis and design for selected exercises. Use your own words to analyze the problem, including the input, output, and what needs to be computed, and describe how to solve the problem in pseudocode.

Sections 2.2–2.12

2.1 (Convert Celsius to Fahrenheit) Write a program that reads a Celsius degree in a double value from the console, then converts it to Fahrenheit and displays the result. The formula for the conversion is as follows:

\[ \text{fahrenheit} = \left(\frac{9}{5}\right) \times \text{celsius} + 32 \]

Hint: In Java, \( \frac{9}{5} \) is 1, but \( \frac{9.0}{5} \) is 1.8.
Here is a sample run:

Enter a degree in Celsius: 43
43 Celsius is 109.4 Fahrenheit

2.2 (Compute the volume of a cylinder) Write a program that reads in the radius and length of a cylinder and computes the area and volume using the following formulas:

\[ \text{area} = \text{radius} \times \text{radius} \times \pi \]
\[ \text{volume} = \text{area} \times \text{length} \]

Here is a sample run:

Enter the radius and length of a cylinder: 5.5 12
The area is 95.0331
The volume is 1140.4

2.3 (Convert feet into meters) Write a program that reads a number in feet, converts it to meters, and displays the result. One foot is 0.305 meter. Here is a sample run:

Enter a value for feet: 16.5
16.5 feet is 5.0325 meters
2.4 (Convert pounds into kilograms) Write a program that converts pounds into kilograms. The program prompts the user to enter a number in pounds, converts it to kilograms, and displays the result. One pound is 0.454 kilograms. Here is a sample run:

```
Enter a number in pounds: 55.5
55.5 pounds is 25.197 kilograms
```

*2.5 (Financial application: calculate tips) Write a program that reads the subtotal and the gratuity rate, then computes the gratuity and total. For example, if the user enters 10 for subtotal and 15% for gratuity rate, the program displays $1.5 as gratuity and $11.5 as total. Here is a sample run:

```
Enter the subtotal and a gratuity rate: 10 15
The gratuity is $1.5 and total is $11.5
```

**2.6 (Sum the digits in an integer) Write a program that reads an integer between 0 and 1000 and adds all the digits in the integer. For example, if an integer is 932, the sum of all its digits is 14.

Hint: Use the % operator to extract digits, and use the / operator to remove the extracted digit. For instance, 932 % 10 = 2 and 932 / 10 = 93.

Here is a sample run:

```
Enter a number between 0 and 1000: 999
The sum of the digits is 27
```

*2.7 (Find the number of years) Write a program that prompts the user to enter the minutes (e.g., 1 billion), and displays the number of years and days for the minutes. For simplicity, assume a year has 365 days. Here is a sample run:

```
Enter the number of minutes: 1000000000
1000000000 minutes is approximately 1902 years and 214 days
```

*2.8 (Current time) Listing 2.7, ShowCurrentTime.java, gives a program that displays the current time in GMT. Revise the program so that it prompts the user to enter the time zone offset to GMT and displays the time in the specified time zone. Here is a sample run:

```
Enter the time zone offset to GMT: -5
The current time is 4:50:34
```
2.9 (Physics: acceleration) Average acceleration is defined as the change of velocity divided by the time taken to make the change, as shown in the following formula:

\[ a = \frac{v_1 - v_0}{t} \]

Write a program that prompts the user to enter the starting velocity \( v_0 \) in meters/second, the ending velocity \( v_1 \) in meters/second, and the time span \( t \) in seconds, and displays the average acceleration. Here is a sample run:

Enter \( v_0, v_1, \) and \( t \): 5.5 50.9 4.5
The average acceleration is 10.0889

2.10 (Science: calculating energy) Write a program that calculates the energy needed to heat water from an initial temperature to a final temperature. Your program should prompt the user to enter the amount of water in kilograms and the initial and final temperatures of the water. The formula to compute the energy is

\[ Q = M \times (\text{finalTemperature} - \text{initialTemperature}) \times 4184 \]

where \( M \) is the weight of water in kilograms, temperatures are in degrees Celsius, and energy \( Q \) is measured in joules. Here is a sample run:

Enter the amount of water in kilograms: 55.5
Enter the initial temperature: 3.5
Enter the final temperature: 10.5
The energy needed is 1625484.0

2.11 (Population projection) Rewrite Programming Exercise 1.11 to prompt the user to enter the number of years and displays the population after the number of years. Use the hint in Programming Exercise 1.11 for this program. The population should be cast into an integer. Here is a sample run of the program:

Enter the number of years: 5
The population in 5 years is 325932970

2.12 (Physics: finding runway length) Given an airplane’s acceleration \( a \) and take-off speed \( v \), you can compute the minimum runway length needed for an airplane to take off using the following formula:

\[ \text{length} = \frac{v^2}{2a} \]

Write a program that prompts the user to enter \( v \) in meters/second (m/s) and the acceleration \( a \) in meters/second squared (m/s^2), and displays the minimum runway length. Here is a sample run:

Enter speed and acceleration: 60 3.5
The minimum runway length for this airplane is 514.286
**2.13 (Financial application: compound value) Suppose you save $100 each month into a savings account with the annual interest rate 5%. Thus, the monthly interest rate is 0.05/12 = 0.00417. After the first month, the value in the account becomes

\[ 100 \times (1 + 0.00417) = 100.417 \]

After the second month, the value in the account becomes

\[ (100 + 100.417) \times (1 + 0.00417) = 201.252 \]

After the third month, the value in the account becomes

\[ (100 + 201.252) \times (1 + 0.00417) = 302.507 \]

and so on.

Write a program that prompts the user to enter a monthly saving amount and displays the account value after the sixth month. (In Exercise 5.30, you will use a loop to simplify the code and display the account value for any month.)

---

Enter the monthly saving amount: 100  
After the sixth month, the account value is $608.81

---

*2.14 (Health application: computing BMI) Body Mass Index (BMI) is a measure of health on weight. It can be calculated by taking your weight in kilograms and dividing by the square of your height in meters. Write a program that prompts the user to enter a weight in pounds and height in inches and displays the BMI. Note that one pound is 0.45359237 kilograms and one inch is 0.0254 meters. Here is a sample run:

Enter weight in pounds: 95.5  
Enter height in inches: 50  
BMI is 26.8573

---

2.15 (Geometry: distance of two points) Write a program that prompts the user to enter two points \((x_1, y_1)\) and \((x_2, y_2)\) and displays their distance between them. The formula for computing the distance is \(\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2}\). Note that you can use \(\text{Math.pow(a, 0.5)}\) to compute \(\sqrt{a}\). Here is a sample run:

Enter x1 and y1: 1.5 -3.4  
Enter x2 and y2: 4.5  
The distance between the two points is 8.764131445842194

---

2.16 (Geometry: area of a hexagon) Write a program that prompts the user to enter the side of a hexagon and displays its area. The formula for computing the area of a hexagon is

\[
\text{Area} = \frac{3\sqrt{3}}{2} s^2,
\]
*2.17 (Science: wind-chill temperature) How cold is it outside? The temperature alone is not enough to provide the answer. Other factors including wind speed, relative humidity, and sunshine play important roles in determining coldness outside. In 2001, the National Weather Service (NWS) implemented the new wind-chill temperature to measure the coldness using temperature and wind speed. The formula is

\[
t_{wc} = 35.74 + 0.6215t_a - 35.75v^{0.16} + 0.4275t_a v^{0.16}
\]

where \( t_a \) is the outside temperature measured in degrees Fahrenheit and \( v \) is the speed measured in miles per hour. \( t_{wc} \) is the wind-chill temperature. The formula cannot be used for wind speeds below 2 mph or temperatures below \(-58^\circ F\) or above \(41^\circ F\).

Write a program that prompts the user to enter a temperature between \(-58^\circ F\) and \(41^\circ F\) and a wind speed greater than or equal to 2 and displays the wind-chill temperature. Use `Math.pow(a, b)` to compute \( v^{0.16} \). Here is a sample run:

```
Enter the temperature in Fahrenheit between -58°F and 41°F: 5.3
Enter the wind speed (>=2) in miles per hour: 6
The wind chill index is -5.56707
```

2.18 (Print a table) Write a program that displays the following table. Cast floating-point numbers into integers.

<table>
<thead>
<tr>
<th>a</th>
<th>b</th>
<th>pow(a, b)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>8</td>
</tr>
<tr>
<td>3</td>
<td>4</td>
<td>81</td>
</tr>
<tr>
<td>4</td>
<td>5</td>
<td>1024</td>
</tr>
<tr>
<td>5</td>
<td>6</td>
<td>15625</td>
</tr>
</tbody>
</table>

*2.19 (Geometry: area of a triangle) Write a program that prompts the user to enter three points \((x_1, y_1), (x_2, y_2), (x_3, y_3)\) of a triangle and displays its area. The formula for computing the area of a triangle is

\[
s = (side1 + side2 + side3)/2;
\]

\[
area = \sqrt{s(s - side1)(s - side2)(s - side3)}
\]

Here is a sample run:

```
Enter three points for a triangle: 1.5 -3.4 4.6 5 9.5 -3.4
The area of the triangle is 33.6
```
(Financial application: calculate interest) If you know the balance and the annual percentage interest rate, you can compute the interest on the next monthly payment using the following formula:

\[ \text{interest} = \text{balance} \times \left(\frac{\text{annualInterestRate}}{1200}\right) \]

Write a program that reads the balance and the annual percentage interest rate and displays the interest for the next month. Here is a sample run:

Enter balance and interest rate (e.g., 3 for 3%): 1000 3.5
The interest is 2.91667

(Financial application: calculate future investment value) Write a program that reads in investment amount, annual interest rate, and number of years, and displays the future investment value using the following formula:

\[ \text{futureInvestmentValue} = \text{investmentAmount} \times (1 + \text{monthlyInterestRate})^{\text{numberOfYears}} \times 12 \]

For example, if you enter amount 1000, annual interest rate 3.25%, and number of years 1, the future investment value is 1032.98.

Here is a sample run:

Enter investment amount: 1000.56
Enter annual interest rate in percentage: 4.25
Enter number of years: 1
Accumulated value is $1043.92

(Financial application: monetary units) Rewrite Listing 2.10, ComputeChange.java, to fix the possible loss of accuracy when converting a double value to an int value. Enter the input as an integer whose last two digits represent the cents. For example, the input 1156 represents 11 dollars and 56 cents.

(Cost of driving) Write a program that prompts the user to enter the distance to drive, the fuel efficiency of the car in miles per gallon, and the price per gallon, and displays the cost of the trip. Here is a sample run:

Enter the driving distance: 900.5
Enter miles per gallon: 25.5
Enter price per gallon: 3.55
The cost of driving is $125.36
Objectives

- To declare boolean variables and write Boolean expressions using relational operators (§3.2).
- To implement selection control using one-way if statements (§3.3).
- To implement selection control using two-way if-else statements (§3.4).
- To implement selection control using nested if and multi-way if statements (§3.5).
- To avoid common errors and pitfalls in if statements (§3.6).
- To generate random numbers using the Math.random() method (§3.7).
- To program using selection statements for a variety of examples (SubtractionQuiz, BMI, ComputeTax) (§§3.7–3.9).
- To combine conditions using logical operators (!, &&, ||, and ^) (§3.10).
- To program using selection statements with combined conditions (LeapYear, Lottery) (§§3.11–3.12).
- To implement selection control using switch statements (§3.13).
- To write expressions using the conditional expression (§3.14).
- To examine the rules governing operator precedence and associativity (§3.15).
- To apply common techniques to debug errors (§3.16).
3.1 Introduction

*The program can decide which statements to execute based on a condition.*

If you enter a negative value for `radius` in Listing 2.2, `ComputeAreaWithConsoleInput.java`, the program displays an invalid result. If the radius is negative, you don’t want the program to compute the area. How can you deal with this situation?

Like all high-level programming languages, Java provides *selection statements*: statements that let you choose actions with alternative courses. You can use the following selection statement to replace lines 12–17 in Listing 2.2:

```java
if (radius < 0) {
    System.out.println("Incorrect input");
} else {
    area = radius * radius * 3.14159;
    System.out.println("Area is " + area);
}
```

Selection statements use conditions that are Boolean expressions. A *Boolean expression* is an expression that evaluates to a *Boolean value*: `true` or `false`. We now introduce Boolean types and relational operators.

### 3.2 boolean Data Type

*The boolean data type declares a variable with the value either true or false.*

How do you compare two values, such as whether a radius is greater than `0`, equal to `0`, or less than `0`? Java provides six *relational operators* (also known as *comparison operators*), shown in Table 3.1, which can be used to compare two values (assume radius is `5` in the table).

<table>
<thead>
<tr>
<th>Java Operator</th>
<th>Mathematics Symbol</th>
<th>Name</th>
<th>Example (radius is 5)</th>
<th>Result</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>&lt;</code></td>
<td><code>&lt;</code></td>
<td>less than</td>
<td>radius &lt; 0</td>
<td>false</td>
</tr>
<tr>
<td><code>&lt;=</code></td>
<td><code>≤</code></td>
<td>less than or equal to</td>
<td>radius &lt;= 0</td>
<td>false</td>
</tr>
<tr>
<td><code>&gt;</code></td>
<td><code>&gt;</code></td>
<td>greater than</td>
<td>radius &gt; 0</td>
<td>true</td>
</tr>
<tr>
<td><code>&gt;=</code></td>
<td><code>≥</code></td>
<td>greater than or equal to</td>
<td>radius &gt;= 0</td>
<td>true</td>
</tr>
<tr>
<td><code>==</code></td>
<td><code>=</code></td>
<td>equal to</td>
<td>radius == 0</td>
<td>false</td>
</tr>
<tr>
<td><code>!=</code></td>
<td><code>≠</code></td>
<td>not equal to</td>
<td>radius != 0</td>
<td>true</td>
</tr>
</tbody>
</table>

**Caution**

The equality testing operator is two equal signs (`==`), not a single equal sign (`=`). The latter symbol is for assignment.

The result of the comparison is a Boolean value: `true` or `false`. For example, the following statement displays `true`:

```java
double radius = 1;
System.out.println(radius > 0);
```

A variable that holds a Boolean value is known as a *Boolean variable*. The `boolean` data type is used to declare Boolean variables. A `boolean` variable can hold one of the
two values: **true** or **false**. For example, the following statement assigns **true** to the variable `lightsOn`:

```java
boolean lightsOn = true;
```

**true** and **false** are literals, just like a number such as **10**. They are treated as reserved words and cannot be used as identifiers in the program.

Suppose you want to develop a program to let a first-grader practice addition. The program randomly generates two single-digit integers, `number1` and `number2`, and displays to the student a question such as “What is 1 + 7?,” as shown in the sample run in Listing 3.1. After the student types the answer, the program displays a message to indicate whether it is true or false.

There are several ways to generate random numbers. For now, generate the first integer using `System.currentTimeMillis() % 10` and the second using `System.currentTimeMillis() / 7 % 10`. Listing 3.1 gives the program. Lines 5–6 generate two numbers, `number1` and `number2`. Line 14 obtains an answer from the user. The answer is graded in line 18 using a Boolean expression `number1 + number2 == answer`.

**LISTING 3.1** AdditionQuiz.java

```java
import java.util.Scanner;

public class AdditionQuiz {
    public static void main(String[] args) {
        int number1 = (int)(System.currentTimeMillis() % 10);
        int number2 = (int)(System.currentTimeMillis() / 7 % 10);

        // Create a Scanner
        Scanner input = new Scanner(System.in);

        System.out.print("What is ", number1 + " + ", number2 + "?");
        int number = input.nextInt();

        System.out.println(number1 + " + ", number2 + " = ", answer + " is " +
                        (number1 + number2 == answer));
    }
}
```

<table>
<thead>
<tr>
<th>line</th>
<th>number1</th>
<th>number2</th>
<th>answer</th>
<th>output</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>4</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>6</td>
<td></td>
<td>8</td>
<td></td>
<td></td>
</tr>
<tr>
<td>14</td>
<td></td>
<td></td>
<td>9</td>
<td></td>
</tr>
<tr>
<td>16</td>
<td></td>
<td></td>
<td></td>
<td>4 + 8 = 9 is false</td>
</tr>
</tbody>
</table>
List six relational operators.

Assuming that \( x \) is 1, show the result of the following Boolean expressions:

\[(x > 0)\]
\[(x < 0)\]
\[(x != 0)\]
\[(x >= 0)\]
\[(x != 1)\]

Can the following conversions involving casting be allowed? Write a test program to verify your answer.

```java
boolean b = true;
i = (int)b;

int i = 1;
boolean b = (boolean)i;
```

An if statement is a construct that enables a program to specify alternative paths of execution.

The preceding program displays a message such as “6 + 2 = 7 is false.” If you wish the message to be “6 + 2 = 7 is incorrect,” you have to use a selection statement to make this minor change.

Java has several types of selection statements: one-way if statements, two-way if-else statements, nested if statements, multi-way if-else statements, switch statements, and conditional expressions.

A one-way if statement executes an action if and only if the condition is true. The syntax for a one-way if statement is:

```java
if (boolean-expression) {
    statement(s);
}
```

The flowchart in Figure 3.1a illustrates how Java executes the syntax of an if statement. A flowchart is a diagram that describes an algorithm or process, showing the steps as boxes of various kinds, and their order by connecting these with arrows. Process operations are represented in these boxes, and arrows connecting them represent the flow of control. A diamond box denotes a Boolean condition and a rectangle box represents statements.

Figure 3.1 An if statement executes statements if the boolean-expression evaluates to true.
If the **boolean-expression** evaluates to **true**, the statements in the block are executed. As an example, see the following code:

```java
if (radius >= 0) {
    area = radius * radius * PI;
    System.out.println("The area for the circle of radius " + radius + " is " + area);
}
```

The flowchart of the preceding statement is shown in Figure 3.1b. If the value of **radius** is greater than or equal to **0**, then the **area** is computed and the result is displayed; otherwise, the two statements in the block will not be executed.

The **boolean-expression** is enclosed in parentheses. For example, the code in (a) is wrong. It should be corrected, as shown in (b).

![Wrong and Correct Code](image)

The block braces can be omitted if they enclose a single statement. For example, the following statements are equivalent.

```java
if (i > 0) {
    System.out.println("i is positive");
}
```

(a) Wrong

```java
if (i > 0) {
    System.out.println("i is positive");
}
```

(b) Correct

---

**Note**

Omitting braces makes the code shorter, but it is prone to errors. It is a common mistake to forget the braces when you go back to modify the code that omits the braces.

---

Listing 3.2 gives a program that prompts the user to enter an integer. If the number is a multiple of 5, the program displays **HiFive**. If the number is divisible by 2, it displays **HiEven**.

**LISTING 3.2 SimpleIfDemo.java**

```java
import java.util.Scanner;

public class SimpleIfDemo {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        System.out.println("Enter an integer: ");
        int number = input.nextInt();

        if (number % 5 == 0)  // check 5
            System.out.println("HiFive");
        if (number % 2 == 0)  // check even
            System.out.println("HiEven");
    }
}
```
Enter an integer: 4
HiEven

Enter an integer: 30
HiFive
HiEven

3.4 Write an if statement that assigns 1 to x if y is greater than 0.

3.5 Write an if statement that increases pay by 3% if score is greater than 90.

3.4 Two-Way if-else Statements

An if-else statement decides the execution path based on whether the condition is true or false.

A one-way if statement performs an action if the specified condition is true. If the condition is false, nothing is done. But what if you want to take alternative actions when the condition is false? You can use a two-way if-else statement. The actions that a two-way if-else statement specifies differ based on whether the condition is true or false.

Here is the syntax for a two-way if-else statement:

```java
if (boolean-expression) {
    statement(s)-for-the-true-case;
} else {
    statement(s)-for-the-false-case;
}
```

The flowchart of the statement is shown in Figure 3.2.

**Figure 3.2** An if-else statement executes statements for the true case if the Boolean-expression evaluates to true; otherwise, statements for the false case are executed.
If the boolean-expression evaluates to true, the statement(s) for the true case are executed; otherwise, the statement(s) for the false case are executed. For example, consider the following code:

```java
if (radius >= 0) {
    area = radius * radius * PI;
    System.out.println("The area for the circle of radius " + radius + " is " + area);
} else {
    System.out.println("Negative input");
}
```

If radius >= 0 is true, area is computed and displayed; if it is false, the message "Negative input" is displayed.

As usual, the braces can be omitted if there is only one statement within them. The braces enclosing the System.out.println("Negative input") statement can therefore be omitted in the preceding example.

Here is another example of using the if-else statement. The example checks whether a number is even or odd, as follows:

```java
if (number % 2 == 0)
    System.out.println(number + " is even.");
else
    System.out.println(number + " is odd.");
```

3.6 Write an if statement that increases pay by 3% if score is greater than 90, otherwise increases pay by 1%.

3.7 What is the output of the code in (a) and (b) if number is 30? What if number is 35?

3.5 Nested if and Multi-Way if-else Statements

An if statement can be inside another if statement to form a nested if statement.

The statement in an if or if-else statement can be any legal Java statement, including another if or if-else statement. The inner if statement is said to be nested inside the outer if statement. The inner if statement can contain another if statement; in fact, there is no limit to the depth of the nesting. For example, the following is a nested if statement:

```java
if (i > k) {
    if (j > k)
        System.out.println("i and j are greater than k");
} else
    System.out.println("i is less than or equal to k");
```

The if (j > k) statement is nested inside the if (i > k) statement.

The nested if statement can be used to implement multiple alternatives. The statement given in Figure 3.3a, for instance, prints a letter grade according to the score, with multiple alternatives.
The execution of this `if` statement proceeds as shown in Figure 3.4. The first condition `score >= 90.0` is tested. If it is `true`, the grade is `A`. If it is `false`, the second condition `score >= 80.0` is tested. If the second condition is `true`, the grade is `B`. If that condition is `false`, the third condition and the rest of the conditions (if necessary) are tested until a condition is met or all of the conditions prove to be `false`. If all of the conditions are `false`, the grade is `F`. Note that a condition is tested only when all of the conditions that come before it are `false`.

**Figure 3.3** A preferred format for multiple alternatives is shown in (b) using a multi-way `if-else` statement.

**Figure 3.4** You can use a multi-way `if-else` statement to assign a grade.
The if statement in Figure 3.3a is equivalent to the if statement in Figure 3.3b. In fact, Figure 3.3b is the preferred coding style for multiple alternative if statements. This style, called multi-way if-else statements, avoids deep indentation and makes the program easy to read.

3.8 Suppose \( x = 3 \) and \( y = 2 \); show the output, if any, of the following code. What is the output if \( x = 3 \) and \( y = 4 \)? What is the output if \( x = 2 \) and \( y = 2 \)? Draw a flowchart of the code.

```java
if (x > 2) {
    if (y > 2) {
        z = x + y;
        System.out.println("z is " + z);
    }
} else
    System.out.println("x is " + x);
```

3.9 Suppose \( x = 2 \) and \( y = 3 \). Show the output, if any, of the following code. What is the output if \( x = 3 \) and \( y = 2 \)? What is the output if \( x = 3 \) and \( y = 3 \)?

```java
if (x > 2)
    if (y > 2) {
        int z = x + y;
        System.out.println("z is " + z);
    }
else
    System.out.println("x is " + x);
```

3.10 What is wrong in the following code?

```java
if (score >= 60.0)
    System.out.println("D");
else if (score >= 70.0)
    System.out.println("C");
else if (score >= 80.0)
    System.out.println("B");
else if (score >= 90.0)
    System.out.println("A");
else
    System.out.println("F");
```

3.6 Common Errors and Pitfalls

Forgetting necessary braces, ending an if statement in the wrong place, mistaking == for =, and dangling else clauses are common errors in selection statements. Duplicated statements in if-else statements and testing equality of double values are common pitfalls.

The following errors are common among new programmers.

Common Error 1: Forgetting Necessary Braces

The braces can be omitted if the block contains a single statement. However, forgetting the braces when they are needed for grouping multiple statements is a common programming error. If you modify the code by adding new statements in an if statement without braces, you will have to insert the braces. For example, the following code in (a) is wrong. It should be written with braces to group multiple statements, as shown in (b).
Chapter 3  Selections

Common Error 2: Wrong Semicolon at the if Line

Adding a semicolon at the end of an if line, as shown in (a) below, is a common mistake.

![Image of code example]

(a) Wrong

```
if (radius >= 0) {
    area = radius * radius * PI;
    System.out.println("The area " + " is " + area);
}
```

(b) Correct

```
if (radius >= 0) {
    area = radius * radius * PI;
    System.out.println("The area " + " is " + area);
}
```

This mistake is hard to find, because it is neither a compile error nor a runtime error; it is a logic error. The code in (a) is equivalent to that in (b) with an empty block.

This error often occurs when you use the next-line block style. Using the end-of-line block style can help prevent this error.

Common Error 3: Redundant Testing of Boolean Values

To test whether a boolean variable is true or false in a test condition, it is redundant to use the equality testing operator like the code in (a):

```
if (even == true)
    System.out.println("It is even.");
```

(a) Equivalent

```
if (even)
    System.out.println("It is even.");
```

(b) This is better

Instead, it is better to test the boolean variable directly, as shown in (b). Another good reason for doing this is to avoid errors that are difficult to detect. Using the = operator instead of the == operator to compare the equality of two items in a test condition is a common error. It could lead to the following erroneous statement:

```
if (even = true)
    System.out.println("It is even.");
```

This statement does not have compile errors. It assigns true to even, so that even is always true.

Common Error 4: Dangling else Ambiguity

The code in (a) below has two if clauses and one else clause. Which if clause is matched by the else clause? The indentation indicates that the else clause matches the first if clause.
However, the else clause actually matches the second if clause. This situation is known as the dangling else ambiguity. The else clause always matches the most recent unmatched if clause in the same block. So, the statement in (a) is equivalent to the code in (b).

```
int i = 1, j = 2, k = 3;
if (i > j)
    if (i > k)
        System.out.println("A");
else
    System.out.println("B");
```

Equivalent

```
int i = 1, j = 2, k = 3;
if (i > j)
    if (i > k)
        System.out.println("A");
else
    System.out.println("B");
```

This is better with correct indentation

Since (i > j) is false, nothing is displayed from the statements in (a) and (b). To force the else clause to match the first if clause, you must add a pair of braces:

```
int i = 1, j = 2, k = 3;
if (i > j) {
    if (i > k)
        System.out.println("A");
} else
    System.out.println("B");
```

This statement displays B.

**Common Error 5: Equality Test of Two Floating-Point Values**

As discussed in Common Error 3 in Section 2.18, floating-point numbers have a limited precision and calculations; involving floating-point numbers can introduce round-off errors. So, equality test of two floating-point values is not reliable. For example, you expect the following code to display true, but surprisingly it displays false.

```
double x = 1.0 - 0.1 - 0.1 - 0.1 - 0.1 - 0.1;
System.out.println(x == 0.5);
```

Here, x is not exactly 0.5, but is 0.5000000000000001. You cannot reliably test equality of two floating-point values. However, you can compare whether they are close enough by testing whether the difference of the two numbers is less than some threshold. That is, two numbers x and y are very close if |x−y| < ε for a very small value, ε, ε, a Greek letter pronounced epsilon, is commonly used to denote a very small value. Normally, you set ε to 10⁻¹⁴ for comparing two values of the double type and to 10⁻⁷ for comparing two values of the float type. For example, the following code

```
final double EPSILON = 1E-14;
double x = 1.0 - 0.1 - 0.1 - 0.1 - 0.1 - 0.1;
if (Math.abs(x - 0.5) < EPSILON)
    System.out.println(x + " is approximately 0.5");
```

will display that

0.5000000000000001 is approximately 0.5

The Math.abs(a) method can be used to return the absolute value of a.
Common Pitfall 1: Simplifying Boolean Variable Assignment

Often, new programmers write the code that assigns a test condition to a `boolean` variable like the code in (a):

```java
if (number % 2 == 0)
    even = true;
else
    even = false;
```

This is not an error, but it should be better written as shown in (b).

```
boolean even = number % 2 == 0;
```

Common Pitfall 2: Avoiding Duplicate Code in Different Cases

Often, new programmers write the duplicate code in different cases that should be combined in one place. For example, the highlighted code in the following statement is duplicated.

```java
if (inState) {
    tuition = 5000;
    System.out.println("The tuition is "+ tuition);
} else {
    tuition = 15000;
    System.out.println("The tuition is "+ tuition);
}
```

This is not an error, but it should be better written as follows:

```java
if (inState) {
    tuition = 5000;
} else {
    tuition = 15000;
}
System.out.println("The tuition is "+ tuition);
```

The new code removes the duplication and makes the code easy to maintain, because you only need to change in one place if the print statement is modified.

3.11 Which of the following statements are equivalent? Which ones are correctly indented?

(a) `if (i > 0) if (j > 0) x = 0; else if (k > 0) y = 0; else z = 0;`

(b) `if (i > 0) {
    if (j > 0) x = 0;
    else if (k > 0) y = 0;
} else
    z = 0;`

(c) `if (i > 0) {
    if (j > 0) x = 0;
    else if (k > 0) y = 0;
    else
        z = 0;
}
```

3.12 Rewrite the following statement using a Boolean expression:

```java
if (count % 10 == 0)
    newLine = true;
else
    newLine = false;
```
3.13 Are the following statements correct? Which one is better?

(a)  
```java
if (age < 16)  
    System.out.println("Cannot get a driver's license");  
else  
    System.out.println("Can get a driver's license");
```

(b)  
```java
if (age < 16)  
    System.out.println("Cannot get a driver's license");  
else if (age >= 16)  
    System.out.println("Can get a driver's license");
```

3.14 What is the output of the following code if `number` is 14, 15, or 30?

(a)  
```java
if (number % 2 == 0)  
    System.out.println(number + " is even");  
else if (number % 5 == 0)  
    System.out.println(number + " is multiple of 5");
```

(b)  
```java
if (number % 2 == 0)  
    System.out.println(number + " is even");  
else if (number % 5 == 0)  
    System.out.println(number + " is multiple of 5");
```

3.7 Generating Random Numbers

You can use `Math.random()` to obtain a random double value between 0.0 and 1.0, excluding 1.0.

Suppose you want to develop a program for a first-grader to practice subtraction. The program randomly generates two single-digit integers, `number1` and `number2`, with `number1 >= number2`, and it displays to the student a question such as “What is 9 − 2?” After the student enters the answer, the program displays a message indicating whether it is correct.

The previous programs generate random numbers using `System.currentTimeMillis()`. A better approach is to use the `random()` method in the `Math` class. Invoking this method returns a random double value `d` such that 0.0 ≤ `d` < 1.0. Thus, `(int)(Math.random() * 10)` returns a random single-digit integer (i.e., a number between 0 and 9).

The program can work as follows:

1. Generate two single-digit integers into `number1` and `number2`.
2. If `number1 < number2`, swap `number1` with `number2`.
3. Prompt the student to answer, "What is number1 − number2?"
4. Check the student’s answer and display whether the answer is correct.

The complete program is shown in Listing 3.3.

**Listing 3.3 SubtractionQuiz.java**

```java
import java.util.Scanner;

public class SubtractionQuiz {
    public static void main(String[] args) {
        // 1. Generate two random single-digit integers
        int number1 = (int)(Math.random() * 10);
        int number2 = (int)(Math.random() * 10);

        // 2. If number1 < number2, swap number1 with number2
        if (number1 < number2) {
            int temp = number1;
            number1 = number2;
            number2 = temp;
        }
```
To swap two variables `number1` and `number2`, a temporary variable `temp` (line 11) is used to first hold the value in `number1`. The value in `number2` is assigned to `number1` (line 12), and the value in `temp` is assigned to `number2` (line 13).

3.15 Which of the following is a possible output from invoking `Math.random()`?

- 323.4, 0.5, 34, 1.0, 0.0, 0.234

3.16 a. How do you generate a random integer `i` such that $0 \leq i < 20$?

b. How do you generate a random integer `i` such that $10 \leq i < 20$?

c. How do you generate a random integer `i` such that $10 \leq i \leq 50$?

d. Write an expression that returns 0 or 1 randomly.
3.8 Case Study: Computing Body Mass Index

You can use nested if statements to write a program that interprets body mass index.

Body Mass Index (BMI) is a measure of health based on height and weight. It can be calculated by taking your weight in kilograms and dividing it by the square of your height in meters. The interpretation of BMI for people 20 years or older is as follows:

<table>
<thead>
<tr>
<th>BMI</th>
<th>Interpretation</th>
</tr>
</thead>
<tbody>
<tr>
<td>BMI &lt; 18.5</td>
<td>Underweight</td>
</tr>
<tr>
<td>18.5 ≤ BMI &lt; 25.0</td>
<td>Normal</td>
</tr>
<tr>
<td>25.0 ≤ BMI &lt; 30.0</td>
<td>Overweight</td>
</tr>
<tr>
<td>30.0 ≤ BMI</td>
<td>Obese</td>
</tr>
</tbody>
</table>

Write a program that prompts the user to enter a weight in pounds and height in inches and displays the BMI. Note that one pound is 0.45359237 kilograms and one inch is 0.0254 meters. Listing 3.4 gives the program.

**LISTING 3.4 ComputeAndInterpretBMI.java**

```java
import java.util.Scanner;

public class ComputeAndInterpretBMI {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter weight in pounds
        System.out.print("Enter weight in pounds: ");
        double weight = input.nextDouble();

        // Prompt the user to enter height in inches
        System.out.print("Enter height in inches: ");
        double height = input.nextDouble();

        final double KILOGRAMS_PER_POUND = 0.45359237; // Constant
        final double METERS_PER_INCH = 0.0254; // Constant

        // Compute BMI
        double weightInKilograms = weight * KILOGRAMS_PER_POUND;
        double heightInMeters = height * METERS_PER_INCH;
        double bmi = weightInKilograms / (heightInMeters * heightInMeters);

        // Display result
        System.out.println("BMI is " + bmi);
        if (bmi < 18.5) System.out.println("Underweight");
        else if (bmi < 25) System.out.println("Normal");
        else if (bmi < 30) System.out.println("Overweight");
        else System.out.println("Obese");
    }
}
```
You should test the input that covers all possible cases for BMI to ensure that the program works for all cases.

3.9 Case Study: Computing Taxes

*You can use nested if statements to write a program for computing taxes.*

The United States federal personal income tax is calculated based on filing status and taxable income. There are four filing statuses: single filers, married filing jointly or qualified widow(er), married filing separately, and head of household. The tax rates vary every year. Table 3.2 shows the rates for 2009. If you are, say, single with a taxable income of $10,000, the first $8,350 is taxed at 10% and the other $1,650 is taxed at 15%, so, your total tax is $1,082.50.

<table>
<thead>
<tr>
<th>Table 3.2 2009 U.S. Federal Personal Tax Rates</th>
</tr>
</thead>
<tbody>
<tr>
<td>Marginal Tax Rate</td>
</tr>
<tr>
<td>10%</td>
</tr>
<tr>
<td>15%</td>
</tr>
<tr>
<td>35%</td>
</tr>
</tbody>
</table>

You are to write a program to compute personal income tax. Your program should prompt the user to enter the filing status and taxable income and compute the tax. Enter 0 for single filers, 1 for married filing jointly or qualified widow(er), 2 for married filing separately, and 3 for head of household.
Your program computes the tax for the taxable income based on the filing status. The filing status can be determined using if statements outlined as follows:

```java
if (status == 0) {
    // Compute tax for single filers
} else if (status == 1) {
    // Compute tax for married filing jointly or qualifying widow(er)
} else if (status == 2) {
    // Compute tax for married filing separately
} else if (status == 3) {
    // Compute tax for head of household
} else {
    // Display wrong status
}
```

For each filing status there are six tax rates. Each rate is applied to a certain amount of taxable income. For example, of a taxable income of $400,000 for single filers, $8,350 is taxed at 10%, $(33,950 – 8,350)$ at 15%, $(82,250 – 33,950)$ at 25%, $(171,550 – 82,250)$ at 28%, $(372,950 – 171,550)$ at 33%, and $(400,000 – 372,950)$ at 35%.

Listing 3.5 gives the solution for computing taxes for single filers. The complete solution is left as an exercise.

**LISTING 3.5 ComputeTax.java**

```java
import java.util.Scanner;

public class ComputeTax {
    public static void main(String[] args) {
        // Create a Scanner
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter filing status
        System.out.print("(0-single filer, 1-married jointly or qualifying widow(er), 2-married separately, 3-head of " +
                        "household) Enter the filing status: ");

        int status = input.nextInt();

        // Prompt the user to enter taxable income
        System.out.print("Enter the taxable income: ");
        double income = input.nextDouble();

        // Compute tax
        double tax = 0;

        if (status == 0) { // Compute tax for single filers
            if (income <= 8350)
                tax = income * 0.10;
            else if (income <= 33950)
                tax = 8350 * 0.10 + (income - 8350) * 0.15;
            else if (income <= 82250)
                tax = 8350 * 0.10 + (33950 - 8350) * 0.15 +
                         (income - 33950) * 0.25;
            else if (income <= 171550)
                tax = 8350 * 0.10 + (33950 - 8350) * 0.15 +
                         (82250 - 33950) * 0.25 + (income - 82250) * 0.28;
```
else if (income <= 372950)
    tax = 8350 * 0.10 + (33950 - 8350) * 0.15 + 
        (82250 - 33950) * 0.25 + (171550 - 82250) * 0.28 + 
        (income - 171550) * 0.33;
else
    tax = 8350 * 0.10 + (33950 - 8350) * 0.15 + 
        (82250 - 33950) * 0.25 + (171550 - 82250) * 0.28 + 
        (372950 - 171550) * 0.33 + (income - 372950) * 0.35;
}
else if (status == 1) { // Left as an exercise
    // Compute tax for married file jointly or qualifying widow(er)
}
else if (status == 2) { // Compute tax for married separately
    // Left as an exercise
}
else if (status == 3) { // Compute tax for head of household
    // Left as an exercise
} else {
    System.out.println("Error: invalid status");
    System.exit(1);
}

// Display the result
System.out.println("Tax is "+(int)(tax * 100) / 100.0);
}

(0-single filer, 1-married jointly or qualifying widow(er),
2-married separately, 3-head of household)
Enter the filing status: 0
Enter the taxable income: 400000
Tax is 117683.5

<table>
<thead>
<tr>
<th>line#</th>
<th>status</th>
<th>income</th>
<th>tax</th>
<th>output</th>
</tr>
</thead>
<tbody>
<tr>
<td>13</td>
<td>0</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>17</td>
<td></td>
<td>400000</td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td></td>
<td></td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>38</td>
<td></td>
<td></td>
<td>117683.5</td>
<td></td>
</tr>
<tr>
<td>57</td>
<td></td>
<td></td>
<td></td>
<td>Tax is 117683.5</td>
</tr>
</tbody>
</table>

The program receives the filing status and taxable income. The multi-way if-else statements (lines 22, 42, 45, 48, 51) check the filing status and compute the tax based on the filing status.

System.exit(status) (line 53) is defined in the System class. Invoking this method terminates the program. The status 0 indicates that the program is terminated normally. A nonzero status code indicates abnormal termination.

An initial value of 0 is assigned to tax (line 20). A compile error would occur if it had no initial value, because all of the other statements that assign values to tax are within the if statement. The compiler thinks that these statements may not be executed and therefore reports a compile error.
3.10 Logical Operators

To test a program, you should provide the input that covers all cases. For this program, your input should cover all statuses (0, 1, 2, 3). For each status, test the tax for each of the six brackets. So, there are a total of 24 cases.

Tip
For all programs, you should write a small amount of code and test it before moving on to add more code. This is called incremental development and testing. This approach makes testing easier, because the errors are likely in the new code you just added.

3.17 Are the following two statements equivalent?

```
if (income <= 10000)
  tax = income * 0.1;
else if (income <= 20000)
  tax = 1000 + (income - 10000) * 0.15;
```

```
if (income <= 10000)
  tax = income * 0.1;
else if (income > 10000 && income <= 20000)
  tax = 1000 + (income - 10000) * 0.15;
```

3.10 Logical Operators

The logical operators !, &&, ||, and ^ can be used to create a compound Boolean expression.

Sometimes, whether a statement is executed is determined by a combination of several conditions. You can use logical operators to combine these conditions to form a compound Boolean expression. Logical operators, also known as Boolean operators, operate on Boolean values to create a new Boolean value. Table 3.3 lists the Boolean operators. Table 3.4 defines the not (!) operator, which negates true to false and false to true. Table 3.5 defines the and (&&) operator. The and (&&) of two Boolean operands is true if and only if both operands are true. Table 3.6 defines the or (||) operator. The or (||) of two Boolean operands is true if at least one of the operands is true. Table 3.7 defines the exclusive or (^) operator. The exclusive or (^) of two Boolean operands is true if and only if the two operands have different Boolean values. Note that p1 ^ p2 is the same as p1 != p2.

<table>
<thead>
<tr>
<th>Table 3.3</th>
<th>Boolean Operators</th>
</tr>
</thead>
<tbody>
<tr>
<td>Operator</td>
<td>Name</td>
</tr>
<tr>
<td>!</td>
<td>not</td>
</tr>
<tr>
<td>&amp;&amp;</td>
<td>and</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>^</td>
<td>exclusive or</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Table 3.4</th>
<th>Truth Table for Operator !</th>
</tr>
</thead>
<tbody>
<tr>
<td>p</td>
<td>!p</td>
</tr>
<tr>
<td>true</td>
<td>false</td>
</tr>
<tr>
<td>false</td>
<td>true</td>
</tr>
</tbody>
</table>
Table 3.5 Truth Table for Operator &&

<table>
<thead>
<tr>
<th>p1</th>
<th>p2</th>
<th>p1 &amp;&amp; p2</th>
<th>Example (assume age = 24, weight = 140)</th>
</tr>
</thead>
<tbody>
<tr>
<td>false</td>
<td>false</td>
<td>false</td>
<td>(age &gt; 28) &amp;&amp; (weight &lt;= 140) is true, because (age &gt; 28) is false.</td>
</tr>
<tr>
<td>false</td>
<td>true</td>
<td>false</td>
<td></td>
</tr>
<tr>
<td>true</td>
<td>false</td>
<td>false</td>
<td></td>
</tr>
<tr>
<td>true</td>
<td>true</td>
<td>true</td>
<td>(age &gt; 18) &amp;&amp; (weight &gt;= 140) is true, because (age &gt; 18) and (weight &gt;= 140) are both true.</td>
</tr>
</tbody>
</table>

Table 3.6 Truth Table for Operator ||

| p1  | p2  | p1 || p2 | Example (assume age = 24, weight = 140) |
|-----|-----|------|------|----------------------------------------|
| false | false | false | (age > 34) || (weight >= 150) is false, because (age > 34) and (weight >= 150) are both false. |
| false | true | true  | |
| true  | false | true  | (age > 18) || (weight < 140) is true, because (age > 18) is true. |
| true  | true | true  | |

Table 3.7 Truth Table for Operator ^

<table>
<thead>
<tr>
<th>p1</th>
<th>p2</th>
<th>p1 ^ p2</th>
<th>Example (assume age = 24, weight = 140)</th>
</tr>
</thead>
<tbody>
<tr>
<td>false</td>
<td>false</td>
<td>false</td>
<td>(age &gt; 34) ^ (weight &gt; 140) is false, because (age &gt; 34) and (weight &gt; 140) are both false.</td>
</tr>
<tr>
<td>false</td>
<td>true</td>
<td>true</td>
<td>(age &gt; 34) ^ (weight &gt;= 140) is true, because (age &gt; 34) is false but (weight &gt;= 140) is true.</td>
</tr>
<tr>
<td>true</td>
<td>false</td>
<td>true</td>
<td></td>
</tr>
<tr>
<td>true</td>
<td>true</td>
<td>false</td>
<td></td>
</tr>
</tbody>
</table>

Listing 3.6 gives a program that checks whether a number is divisible by 2 and 3, by 2 or 3, and by 2 or 3 but not both:

Listing 3.6 TestBooleanOperators.java

```java
import java.util.Scanner;

public class TestBooleanOperators {
    public static void main(String[] args) {
        // Create a Scanner
        Scanner input = new Scanner(System.in);

        // Receive an input
        System.out.print("Enter an integer: ");
        int number = input.nextInt();

        if (number % 2 == 0 && number % 3 == 0)
            System.out.println(number + " is divisible by 2 and 3.");
```
3.10 Logical Operators

```java
if (number % 2 == 0 || number % 3 == 0)
    System.out.println(number + " is divisible by 2 or 3.");
else
    System.out.println(number + " is divisible by 2 or 3, but not both.");
```

Enter an integer: 4
4 is divisible by 2 or 3.
4 is divisible by 2 or 3, but not both.

Enter an integer: 18
18 is divisible by 2 and 3.
18 is divisible by 2 or 3.

**(number % 2 == 0 && number % 3 == 0)** (line 12) checks whether the number is divisible by both 2 and 3. **(number % 2 == 0 || number % 3 == 0)** (line 15) checks whether the number is divisible by 2 or by 3. **(number % 2 == 0 ^ number % 3 == 0)** (line 18) checks whether the number is divisible by 2 or 3, but not both.

**Caution**
In mathematics, the expression

```
1 <= numberOfDaysInAMonth <= 31
```

is correct. However, it is incorrect in Java, because `1 <= numberOfDaysInAMonth` is evaluated to a `boolean` value, which cannot be compared with `31`. Here, two operands (a `boolean` value and a numeric value) are **incompatible**. The correct expression in Java is

```
(1 <= numberOfDaysInAMonth) && (numberOfDaysInAMonth <= 31)
```

**Note**
De Morgan’s law, named after Indian-born British mathematician and logician Augustus De Morgan (1806–1871), can be used to simplify Boolean expressions. The law states:

```
!(condition1 && condition2) is the same as
!condition1 || !condition2
!(condition1 || condition2) is the same as
!condition1 && !condition2
```

For example,

```
!(number % 2 == 0 && number % 3 == 0)
```

can be simplified using an equivalent expression:

```
(number % 2 != 0 || number % 3 != 0)
```

As another example,

```
!(number == 2 || number == 3)
```

is better written as

```
number != 2 && number != 3
```
If one of the operands of an \&\& operator is \texttt{false}, the expression is \texttt{false}; if one of the operands of an || operator is \texttt{true}, the expression is \texttt{true}. Java uses these properties to improve the performance of these operators. When evaluating \texttt{p1 \&\& p2}, Java first evaluates \texttt{p1} and then, if \texttt{p1} is \texttt{true}, evaluates \texttt{p2}; if \texttt{p1} is \texttt{false}, it does not evaluate \texttt{p2}. When evaluating \texttt{p1 || p2}, Java first evaluates \texttt{p1} and then, if \texttt{p1} is \texttt{false}, evaluates \texttt{p2}; if \texttt{p1} is \texttt{true}, it does not evaluate \texttt{p2}. In programming language terminology, \&\& and || are known as the short-circuit or lazy operators. Java also provides the unconditional AND (\&) and OR (|) operators, which are covered in Supplement III.C for advanced readers.

3.18 Assuming that \texttt{x} is \texttt{1}, show the result of the following Boolean expressions.

\begin{align*}
(\text{true}) & \& (3 > 4) \\
!(x > 0) & \&\& (x > 0) \\
(x > 0) & || (x < 0) \\
(x != 0) & || (x == 0) \\
(x >= 0) & || (x < 0) \\
(x != 1) & == !(x == 1)
\end{align*}

3.19 (a) Write a Boolean expression that evaluates to \texttt{true} if a number stored in variable \texttt{num} is between 1 and 100. (b) Write a Boolean expression that evaluates to \texttt{true} if a number stored in variable \texttt{num} is between 1 and 100 or the number is negative.

3.20 (a) Write a Boolean expression for |x - 5| < 4.5. (b) Write a Boolean expression for |x - 5| > 4.5.

3.21 Assume that \texttt{x} and \texttt{y} are \texttt{int} type. Which of the following are legal Java expressions?

\begin{align*}
x > y > 0 \\
x = y \&\& y \\
x /= y \\
x \text{ or } y \\
x \text{ and } y \\
(x != 0) & || (x = 0)
\end{align*}

3.22 Are the following two expressions the same?

**a.** \texttt{x \% 2 == 0 \&\& x \% 3 == 0} \\
**b.** \texttt{x \% 6 == 0}

3.23 What is the value of the expression \texttt{x >= 50 \&\& x <= 100} if \texttt{x} is 45, 67, or 101?

3.24 Suppose, when you run the following program, you enter the input 2 3 6 from the console. What is the output?

```java
public class Test {
    public static void main(String[] args) {
        java.util.Scanner input = new java.util.Scanner(System.in);
        double x = input.nextDouble();
        double y = input.nextDouble();
        double z = input.nextDouble();

        System.out.println("(x < y \&\& y < z) is "+ (x < y \&\& y < z));
        System.out.println("(x < y || y < z) is "+ (x < y || y < z));
        System.out.println("!(x < y) is "+ !(x < y));
        System.out.println("(x + y < z) is "+ (x + y < z));
        System.out.println("(x + y > z) is "+ (x + y > z));
    }
}
```

3.25 Write a Boolean expression that evaluates to \texttt{true} if \texttt{age} is greater than 13 and less than 18.
3.26 Write a Boolean expression that evaluates to true if weight is greater than 50 pounds or height is greater than 60 inches.

3.27 Write a Boolean expression that evaluates to true if weight is greater than 50 pounds and height is greater than 60 inches.

3.28 Write a Boolean expression that evaluates to true if either weight is greater than 50 pounds or height is greater than 60 inches, but not both.

3.11 Case Study: Determining Leap Year

A year is a leap year if it is divisible by 4 but not by 100, or if it is divisible by 400.

You can use the following Boolean expressions to check whether a year is a leap year:

```java
// A leap year is divisible by 4
boolean isLeapYear = (year % 4 == 0);

// A leap year is divisible by 4 but not by 100
isLeapYear = isLeapYear && (year % 100 != 0);

// A leap year is divisible by 4 but not by 100 or divisible by 400
isLeapYear = isLeapYear || (year % 400 == 0);
```

Or you can combine all these expressions into one like this:

```java
isLeapYear = (year % 4 == 0 && year % 100 != 0) || (year % 400 == 0);
```

Listing 3.7 gives the program that lets the user enter a year and checks whether it is a leap year.

**LISTING 3.7 LeapYear.java**

```java
import java.util.Scanner;

public class LeapYear {
    public static void main(String[] args) {
        // Create a Scanner
        Scanner input = new Scanner(System.in);
        System.out.print("Enter a year: ");
        int year = input.nextInt();

        // Check if the year is a leap year
        boolean isLeapYear = (year % 4 == 0 && year % 100 != 0) || (year % 400 == 0);

        // Display the result
        System.out.println(year + " is a leap year? " + isLeapYear);
    }
}
```

**Enter a year: 2008**

2008 is a leap year? true

**Enter a year: 1900**

1900 is a leap year? false
3.12 Case Study: Lottery

The lottery program involves generating random numbers, comparing digits, and using Boolean operators.

Suppose you want to develop a program to play lottery. The program randomly generates a lottery of a two-digit number, prompts the user to enter a two-digit number, and determines whether the user wins according to the following rules:

1. If the user input matches the lottery number in the exact order, the award is $10,000.
2. If all digits in the user input match all digits in the lottery number, the award is $3,000.
3. If one digit in the user input matches a digit in the lottery number, the award is $1,000.

Note that the digits of a two-digit number may be 0. If a number is less than 10, we assume the number is preceded by a 0 to form a two-digit number. For example, number 8 is treated as 08 and number 0 is treated as 00 in the program. Listing 3.8 gives the complete program.

**LISTING 3.8 Lottery.java**

```java
import java.util.Scanner;

public class Lottery {
    public static void main(String[] args) {
        // Generate a lottery number
        int lottery = (int)(Math.random() * 100);

        // Prompt the user to enter a guess
        Scanner input = new Scanner(System.in);
        System.out.print("Enter your lottery pick (two digits): ");
        int guess = input.nextInt();

        // Get digits from lottery
        int lotteryDigit1 = lottery / 10;
        int lotteryDigit2 = lottery % 10;

        // Get digits from guess
        int guessDigit1 = guess / 10;
        int guessDigit2 = guess % 10;

        System.out.println("The lottery number is " + lottery);

        // Check the guess
        if (guess == lottery)
            System.out.println("Exact match: you win $10,000");
        else if (guessDigit2 == lotteryDigit1
            && guessDigit1 == lotteryDigit2)
            System.out.println("Match all digits: you win $3,000");
        else if (guessDigit1 == lotteryDigit1
            || guessDigit1 == lotteryDigit2
            || guessDigit2 == lotteryDigit1
            || guessDigit2 == lotteryDigit2)
            System.out.println("Match one digit: you win $1,000");
```
The program generates a lottery using the `random()` method (line 6) and prompts the user to enter a guess (line 11). Note that `guess % 10` obtains the last digit from `guess` and `guess / 10` obtains the first digit from `guess`, since `guess` is a two-digit number (lines 18–19).

The program checks the guess against the lottery number in this order:

1. First, check whether the guess matches the lottery exactly (line 24).
2. If not, check whether the reversal of the guess matches the lottery (lines 26–27).
3. If not, check whether one digit is in the lottery (lines 29–32).
4. If not, nothing matches and display "Sorry, no match" (lines 34–35).
### 3.13 switch Statements

A switch statement executes statements based on the value of a variable or an expression.

The if statement in Listing 3.5, ComputeTax.java, makes selections based on a single true or false condition. There are four cases for computing taxes, which depend on the value of status. To fully account for all the cases, nested if statements were used. Overuse of nested if statements makes a program difficult to read. Java provides a switch statement to simplify coding for multiple conditions. You can write the following switch statement to replace the nested if statement in Listing 3.5:

```java
switch (status) {
    case 0:  compute tax for single filers;
             break;
    case 1:  compute tax for married jointly or qualifying widow(er);
             break;
    case 2:  compute tax for married filing separately;
             break;
    case 3:  compute tax for head of household;
             break;
    default: System.out.println("Error: invalid status");
             System.exit(1);
}
```

The flowchart of the preceding switch statement is shown in Figure 3.5.

**Figure 3.5** The switch statement checks all cases and executes the statements in the matched case.

This statement checks to see whether the status matches the value 0, 1, 2, or 3, in that order. If matched, the corresponding tax is computed; if not matched, a message is displayed. Here is the full syntax for the switch statement:

```java
switch (switch-expression) {
    case value1:  statement(s)1;
                  break;
```
case value2: statement(s)2;
break;
...
case valueN: statement(s)N;
break;
default: statement(s)-for-default;
}

The switch statement observes the following rules:

- The switch-expression must yield a value of char, byte, short, int, or String type and must always be enclosed in parentheses. (The char and String types will be introduced in the next chapter.)
- The value1, . . . , and valueN must have the same data type as the value of the switch-expression. Note that value1, . . . , and valueN are constant expressions, meaning that they cannot contain variables, such as 1 + x.
- When the value in a case statement matches the value of the switch-expression, the statements starting from this case are executed until either a break statement or the end of the switch statement is reached.
- The default case, which is optional, can be used to perform actions when none of the specified cases matches the switch-expression.
- The keyword break is optional. The break statement immediately ends the switch statement.

Caution
Do not forget to use a break statement when one is needed. Once a case is matched, the statements starting from the matched case are executed until a break statement or the end of the switch statement is reached. This is referred to as fall-through behavior.

For example, the following code displays Weekdays for day of 1 to 5 and Weekends for day 0 and 6.

```
switch (day) {
    case 1:
    case 2:
    case 3:
    case 4:
    case 5: System.out.println("Weekday"); break;
    case 0:
    case 6: System.out.println("Weekend");
}
```

Tip
To avoid programming errors and improve code maintainability, it is a good idea to put a comment in a case clause if break is purposely omitted.

Now let us write a program to find out the Chinese Zodiac sign for a given year. The Chinese Zodiac is based on a twelve-year cycle, with each year represented by an animal—monkey, rooster, dog, pig, rat, ox, tiger, rabbit, dragon, snake, horse, or sheep—in this cycle, as shown in Figure 3.6.

Note that year % 12 determines the Zodiac sign. 1900 is the year of the rat because 1900 % 12 is 4. Listing 3.9 gives a program that prompts the user to enter a year and displays the animal for the year.
import java.util.Scanner;

public class ChineseZodiac {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        System.out.print("Enter a year: ");
        int year = input.nextInt();

        switch (year % 12) {
            case 0: System.out.println("monkey"); break;
            case 1: System.out.println("rooster"); break;
            case 2: System.out.println("dog"); break;
            case 3: System.out.println("pig"); break;
            case 4: System.out.println("rat"); break;
            case 5: System.out.println("ox"); break;
            case 6: System.out.println("tiger"); break;
            case 7: System.out.println("rabbit"); break;
            case 8: System.out.println("dragon"); break;
            case 9: System.out.println("snake"); break;
            case 10: System.out.println("horse"); break;
            case 11: System.out.println("sheep");
        }
    }
}

Enter a year: 1963 Enter
rabbit

Enter a year: 1877 Enter
ox

3.29 What data types are required for a switch variable? If the keyword break is not used after a case is processed, what is the next statement to be executed? Can you convert a switch statement to an equivalent if statement, or vice versa? What are the advantages of using a switch statement?
3.30 What is $y$ after the following `switch` statement is executed? Rewrite the code using an `if-else` statement.

```java
x = 3; y = 3;
switch (x + 3) {
    case 6: y = 1;
    default: y += 1;
}
```

3.31 What is $x$ after the following `if-else` statement is executed? Use a `switch` statement to rewrite it and draw the flowchart for the new `switch` statement.

```java
int x = 1, a = 3;
if (a == 1)
    x += 5;
else if (a == 2)
    x += 10;
else if (a == 3)
    x += 16;
else if (a == 4)
    x += 34;
```

3.32 Write a `switch` statement that displays Sunday, Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, if `day` is 0, 1, 2, 3, 4, 5, 6, accordingly.

3.14 Conditional Expressions

A conditional expression evaluates an expression based on a condition.

You might want to assign a value to a variable that is restricted by certain conditions. For example, the following statement assigns 1 to $y$ if $x$ is greater than 0, and -1 to $y$ if $x$ is less than or equal to 0.

```java
if (x > 0)
    y = 1;
else
    y = -1;
```

Alternatively, as in the following example, you can use a conditional expression to achieve the same result.

```java
y = (x > 0) ? 1 : -1;
```

Conditional expressions are in a completely different style, with no explicit `if` in the statement. The syntax is:

```java
boolean-expression ? expression1 : expression2;
```

The result of this conditional expression is `expression1` if `boolean-expression` is true; otherwise the result is `expression2`.

Suppose you want to assign the larger number of variable `num1` and `num2` to `max`. You can simply write a statement using the conditional expression:

```java
max = (num1 > num2) ? num1 : num2;
```

For another example, the following statement displays the message “num is even” if `num` is even, and otherwise displays “num is odd.”

```java
System.out.println((num % 2 == 0) ? "num is even" : "num is odd");
```
As you can see from these examples, conditional expressions enable you to write short and concise code.

**Note**
The symbols `?` and `:` appear together in a conditional expression. They form a *conditional operator* and also called a *ternary operator* because it uses three operands. It is the only ternary operator in Java.

### 3.33 Check Point
Suppose that, when you run the following program, you enter the input `2 3 6` from the console. What is the output?

```java
public class Test {
    public static void main(String[] args) {
        java.util.Scanner input = new java.util.Scanner(System.in);
        double x = input.nextDouble();
        double y = input.nextDouble();
        double z = input.nextDouble();
        System.out.println((x < y && y < z) ? "sorted" : "not sorted");
    }
}
```

### 3.34 Rewrite the following *if* statements using the conditional operator.

```java
if (ages >= 16)
    ticketPrice = 20;
else
    ticketPrice = 10;
```

### 3.35 Rewrite the following conditional expressions using *if-else* statements.

a. `score = (x > 10) ? 3 * scale : 4 * scale;`
b. `tax = (income > 10000) ? income * 0.2 : income * 0.17 + 1000;`
c. `System.out.println((number % 3 == 0) ? i : j);`

### 3.36 Write conditional expression that returns `-1` or `1` randomly.

### 3.15 Operator Precedence and Associativity

*Operator precedence and associativity determine the order in which operators are evaluated.*

Section 2.11 introduced operator precedence involving arithmetic operators. This section discusses operator precedence in more detail. Suppose that you have this expression:

```
3 + 4 * 4 > 5 * (4 + 3) - 1 && (4 - 3 > 5)
```

What is its value? What is the execution order of the operators?

The expression within parentheses is evaluated first. (Parentheses can be nested, in which case the expression within the inner parentheses is executed first.) When evaluating an expression without parentheses, the operators are applied according to the precedence rule and the associativity rule.

The precedence rule defines precedence for operators, as shown in Table 3.8, which contains the operators you have learned so far. Operators are listed in decreasing order of precedence from top to bottom. The logical operators have lower precedence than the relational operators and the relational operators have lower precedence than the arithmetic operators. Operators with the same precedence appear in the same group. (See Appendix C, *Operator Precedence Chart*, for a complete list of Java operators and their precedence.)
3.15 Operator Precedence and Associativity

If operators with the same precedence are next to each other, their associativity determines the order of evaluation. All binary operators except assignment operators are left associative. For example, since + and – are of the same precedence and are left associative, the expression

\[ a - b + c - d \]

is equivalent to

\[ ((a - b) + c) - d \]

Assignment operators are right associative. Therefore, the expression

\[ a = b += c = 5 \]

is equivalent to

\[ a = (b += (c = 5)) \]

Suppose \( a, b, \) and \( c \) are 1 before the assignment; after the whole expression is evaluated, \( a \) becomes 6, \( b \) becomes 6, and \( c \) becomes 5. Note that left associativity for the assignment operator would not make sense.

**Note**

Java has its own way to evaluate an expression internally. The result of a Java evaluation is the same as that of its corresponding arithmetic evaluation. Advanced readers may refer to Supplement III.B for more discussions on how an expression is evaluated in Java behind the scenes.

3.37 List the precedence order of the Boolean operators. Evaluate the following expressions:

- \( \text{true} \ || \ \text{true} \ &\& \ false \)
- \( \text{false} \ &\& \ true \ || \ false \)

3.38 True or false? All the binary operators except = are left associative.

3.39 Evaluate the following expressions:

- \( 2 * 2 - 3 > 2 \ &\& \ 4 - 2 > 5 \)
- \( 2 * 2 - 3 > 2 \ || \ 4 - 2 > 5 \)
Is \((x > 0 \land x < 10)\) the same as \(((x > 0) \land (x < 10))\)? Is \((x > 0 \lor \lnot x < 10)\) the same as \(((x > 0) \lor \lnot (x < 10))\)? Is \((x > 0 \lor (x < 10 \land y < 0))\) the same as \(((x > 0) \lor (x < 10 \land y < 0))\)?

### 3.16 Debugging

Debugging is the process of finding and fixing errors in a program.

As mentioned in Section 1.10.1, syntax errors are easy to find and easy to correct because the compiler gives indications as to where the errors came from and why they are there. Runtime errors are not difficult to find either, because the Java interpreter displays them on the console when the program aborts. Finding logic errors, on the other hand, can be very challenging.

Logic errors are called **bugs**. The process of finding and correcting errors is called **debugging**. A common approach to debugging is to use a combination of methods to help pinpoint the part of the program where the bug is located. You can **hand-trace** the program (i.e., catch errors by reading the program), or you can insert print statements in order to show the values of the variables or the execution flow of the program. These approaches might work for debugging a short, simple program, but for a large, complex program, the most effective approach is to use a debugger utility.

JDK includes a command-line debugger, jdb, which is invoked with a class name. jdb is itself a Java program, running its own copy of Java interpreter. All the Java IDE tools, such as Eclipse and NetBeans, include integrated debuggers. The debugger utilities let you follow the execution of a program. They vary from one system to another, but they all support most of the following helpful features.

- **Executing a single statement at a time**: The debugger allows you to execute one statement at a time so that you can see the effect of each statement.

- **Tracing into or stepping over a method**: If a method is being executed, you can ask the debugger to enter the method and execute one statement at a time in the method, or you can ask it to step over the entire method. You should step over the entire method if you know that the method works. For example, always step over system-supplied methods, such as `System.out.println`.

- **Setting breakpoints**: You can also set a breakpoint at a specific statement. Your program pauses when it reaches a breakpoint. You can set as many breakpoints as you want. Breakpoints are particularly useful when you know where your programming error starts. You can set a breakpoint at that statement and have the program execute until it reaches the breakpoint.

- **Displaying variables**: The debugger lets you select several variables and display their values. As you trace through a program, the content of a variable is continuously updated.

- **Displaying call stacks**: The debugger lets you trace all of the method calls. This feature is helpful when you need to see a large picture of the program-execution flow.

- **Modifying variables**: Some debuggers enable you to modify the value of a variable when debugging. This is convenient when you want to test a program with different samples but do not want to leave the debugger.

**Tip**

If you use an IDE such as Eclipse or NetBeans, please refer to *Learning Java Effectively with Eclipse/NetBeans* in Supplements II.C and II.E on the Companion Website. The supplement shows you how to use a debugger to trace programs and how debugging can help in learning Java effectively.
1. A boolean type variable can store a true or false value.

2. The relational operators (<, <=, ==, !=, >, =>) yield a Boolean value.

3. Selection statements are used for programming with alternative courses of actions. There are several types of selection statements: one-way if statements, two-way if-else statements, nested if statements, multi-way if-else statements, switch statements, and conditional expressions.

4. The various if statements all make control decisions based on a Boolean expression. Based on the true or false evaluation of the expression, these statements take one of two possible courses.

5. The Boolean operators &&, ||, !, and ^ operate with Boolean values and variables.

6. When evaluating p1 && p2, Java first evaluates p1 and then evaluates p2 if p1 is true; if p1 is false, it does not evaluate p2. When evaluating p1 || p2, Java first evaluates p1 and then evaluates p2 if p1 is false; if p1 is true, it does not evaluate p2. Therefore, && is referred to as the conditional or short-circuit AND operator, and || is referred to as the conditional or short-circuit OR operator.

7. The switch statement makes control decisions based on a switch expression of type char, byte, short, int, or String.

8. The keyword break is optional in a switch statement, but it is normally used at the end of each case in order to skip the remainder of the switch statement. If the break statement is not present, the next case statement will be executed.

9. The operators in expressions are evaluated in the order determined by the rules of parentheses, operator precedence, and operator associativity.

10. Parentheses can be used to force the order of evaluation to occur in any sequence.

11. Operators with higher precedence are evaluated earlier. For operators of the same precedence, their associativity determines the order of evaluation.

12. All binary operators except assignment operators are left-associative; assignment operators are right-associative.
Test Questions

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

Programming Exercises

Pedagogical Note
For each exercise, carefully analyze the problem requirements and design strategies for solving the problem before coding.

Debugging Tip
Before you ask for help, read and explain the program to yourself, and trace it using several representative inputs by hand or using an IDE debugger. You learn how to program by debugging your own mistakes.

Section 3.2

*3.1  (Algebra: solve quadratic equations) The two roots of a quadratic equation \( ax^2 + bx + c = 0 \) can be obtained using the following formula:

\[
 r_1 = \frac{-b + \sqrt{b^2 - 4ac}}{2a} \quad \text{and} \quad r_2 = \frac{-b - \sqrt{b^2 - 4ac}}{2a}
\]

\( b^2 - 4ac \) is called the discriminant of the quadratic equation. If it is positive, the equation has two real roots. If it is zero, the equation has one root. If it is negative, the equation has no real roots.

Write a program that prompts the user to enter values for \( a \), \( b \), and \( c \) and displays the result based on the discriminant. If the discriminant is positive, display two roots. If the discriminant is 0, display one root. Otherwise, display “The equation has no real roots”.

Note that you can use `Math.pow(x, 0.5)` to compute \( \sqrt{x} \). Here are some sample runs.

```
Enter a, b, c: 1.0 3 1
The equation has two roots -0.381966 and -2.61803

Enter a, b, c: 1.2 0 1
The equation has one root -1

Enter a, b, c: 1 2 3
The equation has no real roots
```

3.2  (Game: add three numbers) The program in Listing 3.1, AdditionQuiz.java, generates two integers and prompts the user to enter the sum of these two integers. Revise the program to generate three single-digit integers and prompt the user to enter the sum of these three integers.
Sections 3.3–3.7

*3.3 (Algebra: solve $2 \times 2$ linear equations) A linear equation can be solved using Cramer’s rule given in Programming Exercise 1.13. Write a program that prompts the user to enter $a$, $b$, $c$, $d$, $e$, and $f$ and displays the result. If $ad - bc$ is 0, report that “The equation has no solution.”

Enter $a$, $b$, $c$, $d$, $e$, $f$: 9.0 4.0 3.0 -5.0 -6.0 -21.0

$x$ is -2.0 and $y$ is 3.0

Enter $a$, $b$, $c$, $d$, $e$, $f$: 1.0 2.0 2.0 4.0 4.0 5.0

The equation has no solution

**3.4 (Random month) Write a program that randomly generates an integer between 1 and 12 and displays the English month name January, February, …, December for the number 1, 2, …, 12, accordingly.

**3.5 (Find future dates) Write a program that prompts the user to enter an integer for today’s day of the week (Sunday is 0, Monday is 1, …, and Saturday is 6). Also prompt the user to enter the number of days after today for a future day and display the future day of the week. Here is a sample run:

Enter today’s day: 1
Enter the number of days elapsed since today: 3
Today is Monday and the future day is Thursday

Enter today’s day: 0
Enter the number of days elapsed since today: 31
Today is Sunday and the future day is Wednesday

*3.6 (Health application: BMI) Revise Listing 3.4, ComputeAndInterpretBMI.java, to let the user enter weight, feet, and inches. For example, if a person is 5 feet and 10 inches, you will enter 5 for feet and 10 for inches. Here is a sample run:

Enter weight in pounds: 140
Enter feet: 5
Enter inches: 10
BMI is 20.087702275404553
Normal

3.7 (Financial application: monetary units) Modify Listing 2.10, ComputeChange.java, to display the nonzero denominations only, using singular words for single units such as 1 dollar and 1 penny, and plural words for more than one unit such as 2 dollars and 3 pennies.
**3.8** *(Sort three integers)* Write a program that prompts the user to enter three integers and display the integers in non-decreasing order.

**3.9** *(Business: check ISBN-10)* An **ISBN-10** (International Standard Book Number) consists of 10 digits: \(d_1d_2d_3d_4d_5d_6d_7d_8d_9d_{10}\). The last digit, \(d_{10}\), is a checksum, which is calculated from the other nine digits using the following formula:

\[
(d_1 \times 1 + d_2 \times 2 + d_3 \times 3 + d_4 \times 4 + d_5 \times 5 + \\
d_6 \times 6 + d_7 \times 7 + d_8 \times 8 + d_9 \times 9) \mod 11
\]

If the checksum is 10, the last digit is denoted as X according to the ISBN-10 convention. Write a program that prompts the user to enter the first 9 digits and displays the 10-digit ISBN (including leading zeros). Your program should read the input as an integer. Here are sample runs:

Enter the first 9 digits of an ISBN as integer: 013601267
The ISBN-10 number is 0136012671

Enter the first 9 digits of an ISBN as integer: 013031997
The ISBN-10 number is 013031997X

**3.10** *(Game: addition quiz)* Listing 3.3, SubtractionQuiz.java, randomly generates a subtraction question. Revise the program to randomly generate an addition question with two integers less than 100.

**Sections 3.8–3.16**

*3.11** *(Find the number of days in a month)* Write a program that prompts the user to enter the month and year and displays the number of days in the month. For example, if the user entered month 2 and year 2012, the program should display that February 2012 had 29 days. If the user entered month 3 and year 2015, the program should display that March 2015 had 31 days.

*3.12** *(Palindrome number)* Write a program that prompts the user to enter a three-digit integer and determines whether it is a palindrome number. A number is palindrome if it reads the same from right to left and from left to right. Here is a sample run of this program:

Enter a three-digit integer: 121
121 is a palindrome

Enter a three-digit integer: 123
123 is not a palindrome

*3.13** *(Financial application: compute taxes)* Listing 3.5, ComputeTax.java, gives the source code to compute taxes for single filers. Complete Listing 3.5 to compute the taxes for all filing statuses.

*3.14** *(Game: heads or tails)* Write a program that lets the user guess whether the flip of a coin results in heads or tails. The program randomly generates an integer 0 or 1, which represents head or tail. The program prompts the user to enter a guess and reports whether the guess is correct or incorrect.
**3.15** *(Game: lottery)* Revise Listing 3.8, Lottery.java, to generate a lottery of a three-digit number. The program prompts the user to enter a three-digit number and determines whether the user wins according to the following rules:

1. If the user input matches the lottery number in the exact order, the award is $10,000.
2. If all digits in the user input match all digits in the lottery number, the award is $3,000.
3. If one digit in the user input matches a digit in the lottery number, the award is $1,000.

3.16 *(Random point)* Write a program that displays a random coordinate in a rectangle. The rectangle is centered at (0, 0) with width 100 and height 200.

*3.17* *(Game: scissor, rock, paper)* Write a program that plays the popular scissor-rock-paper game. (A scissor can cut a paper, a rock can knock a scissor, and a paper can wrap a rock.) The program randomly generates a number 0, 1, or 2 representing scissor, rock, and paper. The program prompts the user to enter a number 0, 1, or 2 and displays a message indicating whether the user or the computer wins, loses, or draws. Here are sample runs:

```
scissor (0), rock (1), paper (2): 1
The computer is scissor. You are rock. You won
```

```
scissor (0), rock (1), paper (2): 2
The computer is paper. You are paper too. It is a draw
```

*3.18* *(Cost of shipping)* A shipping company uses the following function to calculate the cost (in dollars) of shipping based on the weight of the package (in pounds).

\[
c(w) = \begin{cases} 
3.5, & \text{if } 0 < w \leq 1 \\
5.5, & \text{if } 1 < w \leq 3 \\
8.5, & \text{if } 3 < w \leq 10 \\
10.5, & \text{if } 10 < w \leq 20 
\end{cases}
\]

Write a program that prompts the user to enter the weight of the package and display the shipping cost. If the weight is greater than 50, display a message “the package cannot be shipped.”

**3.19** *(Compute the perimeter of a triangle)* Write a program that reads three edges for a triangle and computes the perimeter if the input is valid. Otherwise, display that the input is invalid. The input is valid if the sum of every pair of two edges is greater than the remaining edge.

*3.20* *(Science: wind-chill temperature)* Programming Exercise 2.17 gives a formula to compute the wind-chill temperature. The formula is valid for temperatures in the range between −58°F and 41°F and wind speed greater than or equal to 2. Write a program that prompts the user to enter a temperature and a wind speed. The program displays the wind-chill temperature if the input is valid; otherwise, it displays a message indicating whether the temperature and/or wind speed is invalid.
Comprehensive

**3.21** *(Science: day of the week)* Zeller’s congruence is an algorithm developed by Christian Zeller to calculate the day of the week. The formula is

\[
h = \left( q + \frac{26(m + 1)}{10} + k + \frac{j}{4} + \frac{5j}{4} \right) \mod 7
\]

where

- **h** is the day of the week (0: Saturday, 1: Sunday, 2: Monday, 3: Tuesday, 4: Wednesday, 5: Thursday, 6: Friday).
- **q** is the day of the month.
- **m** is the month (3: March, 4: April, ..., 12: December). January and February are counted as months 13 and 14 of the previous year.
- **j** is the century (i.e., \( \frac{\text{year}}{100} \)).
- **k** is the year of the century (i.e., \( \text{year} \mod 100 \)).

Note that the division in the formula performs an integer division. Write a program that prompts the user to enter a year, month, and day of the month, and displays the name of the day of the week. Here are some sample runs:

```
Enter year: (e.g., 2012): 2015
Enter month: 1-12: 1
Enter the day of the month: 1-31: 25
Day of the week is Sunday
```

```
Enter year: (e.g., 2012): 2012
Enter month: 1-12: 5
Enter the day of the month: 1-31: 12
Day of the week is Saturday
```

*(Hint: January and February are counted as 13 and 14 in the formula, so you need to convert the user input 1 to 13 and 2 to 14 for the month and change the year to the previous year.)*

**3.22** *(Geometry: point in a circle?)* Write a program that prompts the user to enter a point \((x, y)\) and checks whether the point is within the circle centered at \((0, 0)\) with radius 10. For example, \((4, 5)\) is inside the circle and \((9, 9)\) is outside the circle, as shown in Figure 3.7a.

*(Hint: A point is in the circle if its distance to \((0, 0)\) is less than or equal to 10. The formula for computing the distance is \(\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}\). Test your program to cover all cases.)* Two sample runs are shown below.

```
Enter a point with two coordinates: 4 5
Point (4.0, 5.0) is in the circle
```

```
Enter a point with two coordinates: 9 9
Point (9.0, 9.0) is not in the circle
```
**3.23** (Geometry: point in a rectangle?) Write a program that prompts the user to enter a point \((x, y)\) and checks whether the point is within the rectangle centered at \((0, 0)\) with width 10 and height 5. For example, \((2, 2)\) is inside the rectangle and \((6, 4)\) is outside the rectangle, as shown in Figure 3.7b. (Hint: A point is in the rectangle if its horizontal distance to \((0, 0)\) is less than or equal to \(10/2\) and its vertical distance to \((0, 0)\) is less than or equal to \(5.0/2\). Test your program to cover all cases.) Here are two sample runs.

**3.24** (Game: pick a card) Write a program that simulates picking a card from a deck of 52 cards. Your program should display the rank (Ace, 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, King) and suit (Clubs, Diamonds, Hearts, Spades) of the card. Here is a sample run of the program:

*3.25* (Geometry: intersecting point) Two points on line 1 are given as \((x_1, y_1)\) and \((x_2, y_2)\) and on line 2 as \((x_3, y_3)\) and \((x_4, y_4)\), as shown in Figure 3.8a–b. The intersecting point of the two lines can be found by solving the following linear equation:

\[
\begin{align*}
(y_1 - y_2)x &- (x_1 - x_2)y = (y_1 - y_2)x_1 - (x_1 - x_2)y_1 \\
(y_3 - y_4)x &- (x_3 - x_4)y = (y_3 - y_4)x_3 - (x_3 - x_4)y_3
\end{align*}
\]

This linear equation can be solved using Cramer’s rule (see Programming Exercise 3.3). If the equation has no solutions, the two lines are parallel (Figure 3.8c).
Write a program that prompts the user to enter four points and displays the intersecting point. Here are sample runs:

![Diagram showing three cases: (a) two lines intersect, (b) two lines are parallel, (c) two lines are parallel.](image)

**Figure 3.8** Two lines intersect in (a and b) and two lines are parallel in (c).

Enter \(x_1, y_1, x_2, y_2, x_3, y_3, x_4, y_4:\) 2 2 5 -1.0 4.0 2.0 -1.0 -2.0
The intersecting point is at (2.88889, 1.1111)

Enter \(x_1, y_1, x_2, y_2, x_3, y_3, x_4, y_4:\) 2 2 7 6.0 4.0 2.0 -1.0 -2.0
The two lines are parallel

**3.26** (Use the \(&\&\), | and ^ operators) Write a program that prompts the user to enter an integer and determines whether it is divisible by 5 and 6, whether it is divisible by 5 or 6, and whether it is divisible by 5 or 6, but not both. Here is a sample run of this program:

Enter an integer: 10
Is 10 divisible by 5 and 6? false
Is 10 divisible by 5 or 6? true
Is 10 divisible by 5 or 6, but not both? true

**3.27** (Geometry: points in triangle?) Suppose a right triangle is placed in a plane as shown below. The right-angle point is placed at (0, 0), and the other two points are placed at (200, 0), and (0, 100). Write a program that prompts the user to enter a point with \(x\)- and \(y\)-coordinates and determines whether the point is inside the triangle. Here are the sample runs:

Enter a point's \(x\)- and \(y\)-coordinates: 100.5 25.5
The point is in the triangle
**3.28**  
*(Geometry: two rectangles)* Write a program that prompts the user to enter the center \(x\)-, \(y\)-coordinates, width, and height of two rectangles and determines whether the second rectangle is inside the first or overlaps with the first, as shown in Figure 3.9. Test your program to cover all cases.

![Figure 3.9](image)

(a) A rectangle is inside another one.  
(b) A rectangle overlaps another one.

Here are the sample runs:

Enter \(r1\)'s center \(x\)-, \(y\)-coordinates, width, and height: 2.5 4 2.5 43  
Enter \(r2\)'s center \(x\)-, \(y\)-coordinates, width, and height: 1.5 5 0.5 3  
r2 is inside \(r1\)

Enter \(r1\)'s center \(x\)-, \(y\)-coordinates, width, and height: 1 2 3 5.5  
Enter \(r2\)'s center \(x\)-, \(y\)-coordinates, width, and height: 3 4 4.5 5  
r2 overlaps \(r1\)

Enter \(r1\)'s center \(x\)-, \(y\)-coordinates, width, and height: 1 2 3 3  
Enter \(r2\)'s center \(x\)-, \(y\)-coordinates, width, and height: 40 45 3 2  
r2 does not overlap \(r1\)

**3.29**  
*(Geometry: two circles)* Write a program that prompts the user to enter the center coordinates and radii of two circles and determines whether the second circle is inside the first or overlaps with the first, as shown in Figure 3.10. *(Hint: circle2 is inside circle1 if the distance between the two centers \(\leq |r1 - r2|\) and circle2 overlaps circle1 if the distance between the two centers \(\leq r1 + r2\). Test your program to cover all cases.)*

Here are the sample runs:

Enter \(circle1\)'s center \(x\)-, \(y\)-coordinates, and radius: 0.5 5.1 13  
Enter \(circle2\)'s center \(x\)-, \(y\)-coordinates, and radius: 1 1.7 4.5  
circle2 is inside \(circle1\)
3.30 (Current time) Revise Programming Exercise 2.8 to display the hour using a 12-hour clock. Here is a sample run:

```
Enter the time zone offset to GMT: -5
The current time is 4:50:34 AM
```

*3.31 (Financials: currency exchange) Write a program that prompts the user to enter the exchange rate from currency in U.S. dollars to Chinese RMB. Prompt the user to enter 0 to convert from U.S. dollars to Chinese RMB and 1 to convert from Chinese RMB and U.S. dollars. Prompt the user to enter the amount in U.S. dollars or Chinese RMB to convert it to Chinese RMB or U.S. dollars, respectively. Here are the sample runs:

```
Enter the exchange rate from dollars to RMB: 6.81
Enter 0 to convert dollars to RMB and 1 vice versa: 0
Enter the dollar amount: 100
$100.0 is 681.0 yuan
```

```
Enter the exchange rate from dollars to RMB: 6.81
Enter 0 to convert dollars to RMB and 1 vice versa: 5
Enter the RMB amount: 10000
10000.0 yuan is $1468.43
```
Given a directed line from point $p_0(x_0, y_0)$ to $p_1(x_1, y_1)$, you can use the following condition to decide whether a point $p_2(x_2, y_2)$ is on the left of the line, on the right, or on the same line (see Figure 3.11):

$$(x_1 - x_0)(y_2 - y_0) - (x_2 - x_0)(y_1 - y_0)$$

- $>0$ if $p_2$ is on the left side of the line
- $=0$ if $p_2$ is on the same line
- $<0$ if $p_2$ is on the right side of the line

![Figure 3.11](https://example.com/figure3_11.png)

**Figure 3.11** (a) $p_2$ is on the left side of the line. (b) $p_2$ is on the right side of the line. (c) $p_2$ is on the same line.

Write a program that prompts the user to enter the three points for $p_0$, $p_1$, and $p_2$ and displays whether $p_2$ is on the left of the line from $p_0$ to $p_1$, on the right, or on the same line. Here are some sample runs:

**The exchange rate from dollars to RMB:** 6.81

Enter 0 to convert dollars to RMB and 1 vice versa: 5

Incorrect input

*3.32* *(Geometry: point position)* Given a directed line from point $p_0(x_0, y_0)$ to $p_1(x_1, y_1)$, you can use the following condition to decide whether a point $p_2(x_2, y_2)$ is on the left of the line, on the right, or on the same line (see Figure 3.11):

$$(x_1 - x_0)(y_2 - y_0) - (x_2 - x_0)(y_1 - y_0)$$

- $>0$ if $p_2$ is on the left side of the line
- $=0$ if $p_2$ is on the same line
- $<0$ if $p_2$ is on the right side of the line

![Figure 3.11](https://example.com/figure3_11.png)

**Figure 3.11** (a) $p_2$ is on the left side of the line. (b) $p_2$ is on the right side of the line. (c) $p_2$ is on the same line.

Write a program that prompts the user to enter the three points for $p_0$, $p_1$, and $p_2$ and displays whether $p_2$ is on the left of the line from $p_0$ to $p_1$, on the right, or on the same line. Here are some sample runs:

Enter the exchange rate from dollars to RMB: 6.81
Enter 0 to convert dollars to RMB and 1 vice versa: 5

Incorrect input

Enter weight and price for package 1: 50 24.59
Enter weight and price for package 2: 25 11.99
Package 2 has a better price.

*3.33* *(Financial: compare costs)* Suppose you shop for rice in two different packages. You would like to write a program to compare the cost. The program prompts the user to enter the weight and price of the each package and displays the one with the better price. Here is a sample run:

Enter weight and price for package 1: 50 24.59
Enter weight and price for package 2: 25 11.99
Package 2 has a better price.
Programming Exercise 3.32 shows how to test whether a point is on an unbounded line. Revise Programming Exercise 3.32 to test whether a point is on a line segment. Write a program that prompts the user to enter the three points for p0, p1, and p2 and displays whether p2 is on the line segment from p0 to p1. Here are some sample runs:

Enter weight and price for package 1: 50 25
Enter weight and price for package 2: 25 12.5
Two packages have the same price.

*3.34 (Geometry: point on line segment) Programming Exercise 3.32 shows how to test whether a point is on an unbounded line. Revise Programming Exercise 3.32 to test whether a point is on a line segment. Write a program that prompts the user to enter the three points for p0, p1, and p2 and displays whether p2 is on the line segment from p0 to p1. Here are some sample runs:

Enter three points for p0, p1, and p2: 1.0 1.0 2.5 2.5 1.5 1.5
(1.5, 1.5) is on the line segment from (1.0, 1.0) to (2.5, 2.5)

Enter three points for p0, p1, and p2: 1.0 2.0 2.5 4.0 3.5 3.5
(3.5, 3.5) is not on the line segment from (1.0, 1.0) to (2.0, 2.0)
MATHEMATICAL FUNCTIONS, CHARACTERS, AND STRINGS

Objectives

- To solve mathematical problems by using the methods in the Math class (§4.2).
- To represent characters using the char type (§4.3).
- To encode characters using ASCII and Unicode (§4.3.1).
- To represent special characters using the escape sequences (§4.4.2).
- To cast a numeric value to a character and cast a character to an integer (§4.3.3).
- To compare and test characters using the static methods in the Character class (§4.3.4).
- To introduce objects and instance methods (§4.4).
- To represent strings using the String object (§4.4).
- To return the string length using the length() method (§4.4.1).
- To return a character in the string using the charAt(i) method (§4.4.2).
- To use the + operator to concatenate strings (§4.4.3).
- To return an uppercase string or a lowercase string and to trim a string (§4.4.4).
- To read strings from the console (§4.4.5).
- To read a character from the console (§4.4.6).
- To compare strings using the equals method and the compareTo methods (§4.4.7).
- To obtain substrings (§4.4.8).
- To find a character or a substring in a string using the indexOf method (§4.4.9).
- To program using characters and strings (GuessBirthday) (§4.5.1).
- To convert a hexadecimal character to a decimal value (HexDigit2Dec) (§4.5.2).
- To revise the lottery program using strings (LotteryUsingStrings) (§4.5.3).
- To format output using the System.out.printf method (§4.6).
4.1 Introduction

The focus of this chapter is to introduce mathematical functions, characters, string objects, and use them to develop programs.

The preceding chapters introduced fundamental programming techniques and taught you how to write simple programs to solve basic problems using selection statements. This chapter introduces methods for performing common mathematical operations. You will learn how to create custom methods in Chapter 6.

Suppose you need to estimate the area enclosed by four cities, given the GPS locations (latitude and longitude) of these cities, as shown in the following diagram. How would you write a program to solve this problem? You will be able to write such a program after completing this chapter.

Because strings are frequently used in programming, it is beneficial to introduce strings early so that you can begin to use them to develop useful programs. This chapter gives a brief introduction to string objects; you will learn more on objects and strings in Chapters 9 and 10.

4.2 Common Mathematical Functions

Java provides many useful methods in the Math class for performing common mathematical functions.

A method is a group of statements that performs a specific task. You have already used the pow(a, b) method to compute \(a^b\) in Section 2.9.4, Exponent Operations and the random() method for generating a random number in Section 3.7. This section introduces other useful methods in the Math class. They can be categorized as trigonometric methods, exponent methods, and service methods. Service methods include the rounding, min, max, absolute, and random methods. In addition to methods, the Math class provides two useful double constants, PI and E (the base of natural logarithms). You can use these constants as Math.PI and Math.E in any program.

4.2.1 Trigonometric Methods

The Math class contains the following methods as shown in Table 4.1 for performing trigonometric functions:

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>sin(radians)</td>
<td>Returns the trigonometric sine of an angle in radians.</td>
</tr>
<tr>
<td>cos(radians)</td>
<td>Returns the trigonometric cosine of an angle in radians.</td>
</tr>
<tr>
<td>tan(radians)</td>
<td>Returns the trigonometric tangent of an angle in radians.</td>
</tr>
<tr>
<td>toRadians(degree)</td>
<td>Returns the angle in radians for the angle in degree.</td>
</tr>
<tr>
<td>toDegree(radians)</td>
<td>Returns the angle in degrees for the angle in radians.</td>
</tr>
<tr>
<td>asin(a)</td>
<td>Returns the angle in radians for the inverse of sine.</td>
</tr>
<tr>
<td>acos(a)</td>
<td>Returns the angle in radians for the inverse of cosine.</td>
</tr>
<tr>
<td>atan(a)</td>
<td>Returns the angle in radians for the inverse of tangent.</td>
</tr>
</tbody>
</table>
The parameter for \( \sin, \cos, \) and \( \tan \) is an angle in radians. The return value for \( \text{asin}, \text{acos}, \) and \( \text{atan} \) is a degree in radians in the range between \( -\pi/2 \) and \( \pi/2 \). One degree is equal to \( \pi/180 \) in radians, 90 degrees is equal to \( \pi/2 \) in radians, and 30 degrees is equal to \( \pi/6 \) in radians.

For example,

\[
\begin{align*}
\text{Math.toDegrees}(\text{Math.PI} / 2) & \text{ returns } 90.0 \\
\text{Math.toRadians}(30) & \text{ returns } 0.5236 \text{ (same as } \pi/6) \\
\text{Math.sin}(0) & \text{ returns } 0.0 \\
\text{Math.sin(Math.toRadians(270))} & \text{ returns } -1.0 \\
\text{Math.sin(Math.PI} / 6) & \text{ returns } 0.5 \\
\text{Math.sin(Math.PI} / 2) & \text{ returns } 1.0 \\
\text{Math.cos}(0) & \text{ returns } 1.0 \\
\text{Math.cos(Math.PI} / 6) & \text{ returns } 0.866 \\
\text{Math.cos(Math.PI} / 2) & \text{ returns } 0 \\
\text{Math.asin}(0.5) & \text{ returns } 0.523598333 \text{ (same as } \pi/6) \\
\text{Math.acos}(0.5) & \text{ returns } 1.0472 \text{ (same as } \pi/3) \\
\text{Math.atan}(1.0) & \text{ returns } 0.785398 \text{ (same as } \pi/4)
\end{align*}
\]

### 4.2.2 Exponent Methods

There are five methods related to exponents in the **Math** class as shown in Table 4.2.

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>\text{exp}(x)</td>
<td>Returns ( e ) raised to power of ( x ) (( e^x )).</td>
</tr>
<tr>
<td>\text{log}(x)</td>
<td>Returns the natural logarithm of ( x ) (( \ln(x) = \log_e(x) )).</td>
</tr>
<tr>
<td>\text{log10}(x)</td>
<td>Returns the base 10 logarithm of ( x ) (( \log_{10}(x) )).</td>
</tr>
<tr>
<td>\text{pow}(a, b)</td>
<td>Returns ( a ) raised to the power of ( b ) (( a^b )).</td>
</tr>
<tr>
<td>\text{sqrt}(x)</td>
<td>Returns the square root of ( x ) (( \sqrt{x} )) for ( x \geq 0 ).</td>
</tr>
</tbody>
</table>

For example,

\[
\begin{align*}
\text{Math.exp}(1) & \text{ returns } 2.71828 \\
\text{Math.log(Math.E)} & \text{ returns } 1.0 \\
\text{Math.log10}(10) & \text{ returns } 1.0 \\
\text{Math.pow}(2, 3) & \text{ returns } 8.0 \\
\text{Math.pow}(3, 2) & \text{ returns } 9.0 \\
\text{Math.pow}(4.5, 2.5) & \text{ returns } 22.91765 \\
\text{Math.sqrt}(4) & \text{ returns } 2.0 \\
\text{Math.sqrt}(10.5) & \text{ returns } 4.24
\end{align*}
\]

### 4.2.3 The Rounding Methods

The **Math** class contains five rounding methods as shown in Table 4.3.

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>\text{ceil}(x)</td>
<td>( x ) is rounded up to its nearest integer. This integer is returned as a double value.</td>
</tr>
<tr>
<td>\text{floor}(x)</td>
<td>( x ) is rounded down to its nearest integer. This integer is returned as a double value.</td>
</tr>
<tr>
<td>\text{rint}(x)</td>
<td>( x ) is rounded up to its nearest integer. If ( x ) is equally close to two integers, the even one is returned as a double value.</td>
</tr>
<tr>
<td>\text{round}(x)</td>
<td>Returns ((\text{int})\text{Math.floor}(x + 0.5)) if ( x ) is a float and returns ((\text{long})\text{Math.floor}(x + 0.5)) if ( x ) is a double.</td>
</tr>
</tbody>
</table>
For example,

- Math.ceil(2.1) returns 4.0
- Math.ceil(2.0) returns 2.0
- Math.ceil(-2.0) returns -2.0
- Math.ceil(-2.1) returns -2.0
- Math.floor(2.1) returns 2.0
- Math.floor(2.0) returns 2.0
- Math.floor(-2.0) returns -2.0
- Math.floor(-2.1) returns -2.0
- Math.rint(2.1) returns 2.0
- Math.rint(-2.0) returns -2.0
- Math.rint(-2.1) returns -2.0
- Math.rint(2.5) returns 2.0
- Math.rint(4.5) returns 4.0
- Math.rint(-2.5) returns -2.0
- Math.round(2.6f) returns 3 // Returns int
- Math.round(2.0) returns 2 // Returns long
- Math.round(-2.0f) returns -2 // Returns int
- Math.round(-2.6) returns -3 // Returns long
- Math.round(-2.4) returns -2 // Returns long

4.2.4 The \texttt{min}, \texttt{max}, and \texttt{abs} Methods

The \texttt{min} and \texttt{max} methods return the minimum and maximum numbers of two numbers (\texttt{int}, \texttt{long}, \texttt{float}, or \texttt{double}). For example, \texttt{max(4.4, 5.0)} returns 5.0, and \texttt{min(3, 2)} returns 2.

The \texttt{abs} method returns the absolute value of the number (\texttt{int}, \texttt{long}, \texttt{float}, or \texttt{double}). For example,

- Math.max(2, 3) returns 3
- Math.max(2.5, 3) returns 4.0
- Math.min(2.5, 4.6) returns 2.5
- Math.abs(-2) returns 2
- Math.abs(-2.1) returns 2.1

4.2.5 The \texttt{random} Method

You have used the \texttt{random()} method in the preceding chapter. This method generates a random \texttt{double} value greater than or equal to 0.0 and less than 1.0 (0 \(\leq\) Math.random() < 1.0). You can use it to write a simple expression to generate random numbers in any range. For example,

- \((\texttt{int})(\texttt{Math.random()} \times 10)\) Returns a random integer between 0 and 9.
- \(50 + (\texttt{int})(\texttt{Math.random()} \times 50)\) Returns a random integer between 50 and 99.

In general,

- \(a + \texttt{Math.random()} \times b\) Returns a random number between \(a\) and \(a + b\), excluding \(a + b\).
4.2.6 Case Study: Computing Angles of a Triangle

You can use the math methods to solve many computational problems. Given the three sides of a triangle, for example, you can compute the angles by using the following formula:

\[
\begin{align*}
A &= \text{acos}((a \cdot a - b \cdot b - c \cdot c) / (-2 \cdot b \cdot c)) \\
B &= \text{acos}((b \cdot b - a \cdot a - c \cdot c) / (-2 \cdot a \cdot c)) \\
C &= \text{acos}((c \cdot c - b \cdot b - a \cdot a) / (-2 \cdot a \cdot b))
\end{align*}
\]

Don’t be intimidated by the mathematic formula. As we discussed early in Listing 2.9, ComputeLoan.java, you don’t have to know how the mathematical formula is derived in order to write a program for computing the loan payments. Here in this example, given the length of three sides, you can use this formula to write a program to compute the angles without having to know how the formula is derived. In order to compute the lengths of the sides, we need to know the coordinates of three corner points and compute the distances between the points.

Listing 4.1 is an example of a program that prompts the user to enter the x- and y-coordinates of the three corner points in a triangle and then displays the three angles.

**Listing 4.1 ComputeAngles.java**

```java
import java.util.Scanner;

public class ComputeAngles {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter three points
        System.out.print("Enter three points: ");
        double x1 = input.nextDouble();
        double y1 = input.nextDouble();
        double x2 = input.nextDouble();
        double y2 = input.nextDouble();
        double x3 = input.nextDouble();
        double y3 = input.nextDouble();

        // Compute three sides
        double a = Math.sqrt((x2 - x3) * (x2 - x3) + (y2 - y3) * (y2 - y3));
        double b = Math.sqrt((x1 - x3) * (x1 - x3) + (y1 - y3) * (y1 - y3));
        double c = Math.sqrt((x1 - x2) * (x1 - x2) + (y1 - y2) * (y1 - y2));

        // Compute three angles
        double A = Math.toDegrees(Math.acos((a * a - b * b - c * c) / (-2 * b * c)));
        double B = Math.toDegrees(Math.acos((b * b - a * a - c * c) / (-2 * a * c)));
        double C = Math.toDegrees(Math.acos((c * c - b * b - a * a) / (-2 * a * b)));

        // Display results
        System.out.println("The three angles are "+
                         Math.round(A * 100) / 100.0 + " " +
                         Math.round(B * 100) / 100.0 + " " +
                         Math.round(C * 100) / 100.0);
    }
}
```

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Chapter 4  Mathematical Functions, Characters, and Strings

35    Math.round(B * 100) / 100.0 + " " +
36    Math.round(C * 100) / 100.0);
37  }
38  }

Enter three points: 1 1 6.5 1 6.5 2.5
The three angles are 15.26 90.0 74.74

The program prompts the user to enter three points (line 8). This prompting message is not clear. You should give the user explicit instructions on how to enter these points as follows:

System.out.print("Enter the coordinates of three points separated "
   + "by spaces like x1 y1 x2 y2 x3 y3: ");

Note that the distance between two points \((x_1, y_1)\) and \((x_2, y_2)\) can be computed using the formula \(\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}\). The program computes the distances between two points (lines 17–22), and applies the formula to compute the angles (lines 25–30). The angles are rounded to display up to two digits after the decimal point (lines 34–36).

The `Math` class is used in the program, but not imported, because it is in the `java.lang` package. All the classes in the `java.lang` package are implicitly imported in a Java program.

4.1 Evaluate the following method calls:

(a) Math.sqrt(4)  
(b) Math.sin(2 * Math.PI)  
(c) Math.cos(2 * Math.PI)  
(d) Math.pow(2, 2)  
(e) Math.log(Math.E)  
(f) Math.exp(1)  
(g) Math.max(2, Math.min(3, 4))  
(h) Math.rint(-2.5)  
(i) Math.ceil(-2.5)  
(j) Math.floor(-2.5)  
(k) Math.round(-2.5F)  
(l) Math.round(-2.5)  
(m) Math.round(2.5)  
(n) Math.ceil(2.5)  
(o) Math.floor(2.5)  
(p) Math.round(2.5F)  
(q) Math.round(2.5)  
(r) Math.round(Math.abs(-2.5))

4.2 True or false? The argument for trigonometric methods is an angle in radians.

4.3 Write a statement that converts 47 degrees to radians and assigns the result to a variable.

4.4 Write a statement that converts \(\pi / 7\) to an angle in degrees and assigns the result to a variable.

4.5 Write an expression that obtains a random integer between 34 and 55. Write an expression that obtains a random integer between 0 and 999. Write an expression that obtains a random number between 5.5 and 55.5.

4.6 Why does the `Math` class not need to be imported?

4.7 What is `Math.log(Math.exp(5.5))`? What is `Math.exp(Math.log(5.5))`? What is `Math.asin(Math.sin(Math.PI / 6))`? What is `Math.sin(Math.asin(Math.PI / 6))`?
4.3 Character Data Type and Operations

A character data type represents a single character.

In addition to processing numeric values, you can process characters in Java. The character data type, `char`, is used to represent a single character. A character literal is enclosed in single quotation marks. Consider the following code:

```java
char letter = 'A';
char numChar = '4';
```

The first statement assigns character `A` to the `char` variable `letter`. The second statement assigns digit character `4` to the `char` variable `numChar`.

**Caution**

A string literal must be enclosed in quotation marks (" "). A character literal is a single character enclosed in single quotation marks (’ ’). Therefore, "A" is a string, but 'A' is a character.

### 4.3.1 Unicode and ASCII code

Computers use binary numbers internally. A character is stored in a computer as a sequence of 0s and 1s. Mapping a character to its binary representation is called encoding. There are different ways to encode a character. How characters are encoded is defined by an encoding scheme.

Java supports Unicode, an encoding scheme established by the Unicode Consortium to support the interchange, processing, and display of written texts in the world’s diverse languages. Unicode was originally designed as a 16-bit character encoding. The primitive data type `char` was intended to take advantage of this design by providing a simple data type that could hold any character. However, it turned out that the 65,536 characters possible in a 16-bit encoding are not sufficient to represent all the characters in the world. The Unicode standard therefore has been extended to allow up to 1,112,064 characters. Those characters that go beyond the original 16-bit limit are called supplementary characters. Java supports the supplementary characters. The processing and representing of supplementary characters are beyond the scope of this book. For simplicity, this book considers only the original 16-bit Unicode characters. These characters can be stored in a `char` type variable.

A 16-bit Unicode takes two bytes, preceded by \u, expressed in four hexadecimal digits that run from \u0000 to \uFFFF. Hexadecimal numbers are introduced in Appendix F, Number Systems. For example, the English word welcome is translated into Chinese using two characters, 欢迎. The Unicodes of these two characters are \u6B22\u8FCE. The Unicodes for the Greek letters α β γ are \u03b1 \u03b2 \u03b4.

Most computers use ASCII (American Standard Code for Information Interchange), an 8-bit encoding scheme for representing all uppercase and lowercase letters, digits, punctuation marks, and control characters. Unicode includes ASCII code, with \u0000 to \u007F corresponding to the 128 ASCII characters. Table 4.4 shows the ASCII code for some commonly used characters. Appendix B, ‘The ASCII Character Set,’ gives a complete list of ASCII characters and their decimal and hexadecimal codes.

<table>
<thead>
<tr>
<th>Characters</th>
<th>Code Value in Decimal</th>
<th>Unicode Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>'0' to '9'</td>
<td>48 to 57</td>
<td>\u0030 to \u0039</td>
</tr>
<tr>
<td>'A' to 'Z'</td>
<td>65 to 90</td>
<td>\u0041 to \u005A</td>
</tr>
<tr>
<td>'a' to 'z'</td>
<td>97 to 122</td>
<td>\u0061 to \u007A</td>
</tr>
</tbody>
</table>
You can use ASCII characters such as 'X', '1', and '$' in a Java program as well as Unicodes. Thus, for example, the following statements are equivalent:

```java
char letter = 'A';
char letter = '\u0041'; // Character A's Unicode is 0041
```

Both statements assign character A to the char variable `letter`.

**Note**
The increment and decrement operators can also be used on char variables to get the next or preceding Unicode character. For example, the following statements display character b.

```java
char ch = 'a';
System.out.println(++ch);
```

### 4.3.2 Escape Sequences for Special Characters

Suppose you want to print a message with quotation marks in the output. Can you write a statement like this?

```java
System.out.println("He said "Java is fun"";)
```

No, this statement has a compile error. The compiler thinks the second quotation character is the end of the string and does not know what to do with the rest of characters.

To overcome this problem, Java uses a special notation to represent special characters, as shown in Table 4.5. This special notation, called an escape sequence, consists of a backslash (\) followed by a character or a combination of digits. For example, \t is an escape sequence for the Tab character and an escape sequence such as \u03b1 is used to represent a Unicode. The symbols in an escape sequence are interpreted as a whole rather than individually. An escape sequence is considered as a single character.

So, now you can print the quoted message using the following statement:

```java
System.out.println("He said "Java is fun"");
```

The output is

He said "Java is fun"

Note that the symbols \ and " together represent one character.

**Table 4.5 Escape Sequences**

<table>
<thead>
<tr>
<th>Escape Sequence</th>
<th>Name</th>
<th>Unicode Code</th>
<th>Decimal Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>\b</td>
<td>Backspace</td>
<td>\u0008</td>
<td>8</td>
</tr>
<tr>
<td>\t</td>
<td>Tab</td>
<td>\u0009</td>
<td>9</td>
</tr>
<tr>
<td>\n</td>
<td>Linefeed</td>
<td>\u000A</td>
<td>10</td>
</tr>
<tr>
<td>\f</td>
<td>Formfeed</td>
<td>\u000C</td>
<td>12</td>
</tr>
<tr>
<td>\r</td>
<td>Carriage Return</td>
<td>\u000D</td>
<td>13</td>
</tr>
<tr>
<td>\</td>
<td>Backslash</td>
<td>\u005C</td>
<td>92</td>
</tr>
<tr>
<td>&quot;</td>
<td>Double Quote</td>
<td>\u0022</td>
<td>34</td>
</tr>
</tbody>
</table>

The backslash \ is called an escape character. It is a special character. To display this character, you have to use an escape sequence \\. For example, the following code

```java
System.out.println("\t is a tab character");
```

displays

\t is a tab character
4.3.3 Casting between char and Numeric Types

A char can be cast into any numeric type, and vice versa. When an integer is cast into a char, only its lower 16 bits of data are used; the other part is ignored. For example:

```java
char ch = (char)0XAB0041; // The lower 16 bits hex code 0041 is assigned to ch
System.out.println(ch); // ch is character A
```

When a floating-point value is cast into a char, the floating-point value is first cast into an int, which is then cast into a char.

```java
char ch = (char)65.25; // Decimal 65 is assigned to ch
System.out.println(ch); // ch is character A
```

When a char is cast into a numeric type, the character’s Unicode is cast into the specified numeric type.

```java
int i = (int)'A'; // The Unicode of character A is assigned to i
System.out.println(i); // i is 65
```

Implicit casting can be used if the result of a casting fits into the target variable. Otherwise, explicit casting must be used. For example, since the Unicode of 'a' is 97, which is within the range of a byte, these implicit castings are fine:

```java
byte b = 'a';
int i = 'a';
```

But the following casting is incorrect, because the Unicode \uFFF4 cannot fit into a byte:

```java
byte b = '\uFFF4';
```

To force this assignment, use explicit casting, as follows:

```java
byte b = (byte)'\uFFF4';
```

Any positive integer between 0 and FFFF in hexadecimal can be cast into a character implicitly. Any number not in this range must be cast into a char explicitly.

All numeric operators can be applied to char operands. A char operand is automatically cast into a number if the other operand is a number or a character. If the other operand is a string, the character is concatenated with the string. For example, the following statements display:

```java
int i = '2' + '3'; // (int)'2' is 50 and (int)'3' is 51
System.out.println("i is " + i); // i is 101
int j = 2 + 'a'; // (int)'a' is 97
System.out.println("j is " + j); // j is 99
System.out.println(j + " is the Unicode for character " + (char)j); // 99 is the Unicode for character c
System.out.println("Chapter " + '2');
```

```
i is 101
j is 99
99 is the Unicode for character c
Chapter 2
```
4.3.4 Comparing and Testing Characters

Two characters can be compared using the relational operators just like comparing two numbers. This is done by comparing the Unicodes of the two characters. For example,

'\texttt{a}' < '\texttt{b}' is true because the Unicode for '\texttt{a}' (97) is less than the Unicode for '\texttt{b}' (98).

'\texttt{a}' < '\texttt{A}' is false because the Unicode for '\texttt{a}' (97) is greater than the Unicode for '\texttt{A}' (65).

'\texttt{1}' < '\texttt{8}' is true because the Unicode for '\texttt{1}' (49) is less than the Unicode for '\texttt{8}' (56).

Often in the program, you need to test whether a character is a number, a letter, an uppercase letter, or a lowercase letter. As shown in Appendix B, the ASCII character set, the Unicodes for lowercase letters are consecutive integers starting from the Unicode for '\texttt{a}', then for '\texttt{b}', '\texttt{c}',..., and '\texttt{z}'. The same is true for the uppercase letters and for numeric characters. This property can be used to write the code to test characters. For example, the following code tests whether a character \texttt{ch} is an uppercase letter, a lowercase letter, or a digital character.

\begin{verbatim}
if (ch >= 'A' && ch <= 'Z')
    System.out.println(ch + " is an uppercase letter");
else if (ch >= 'a' && ch <= 'z')
    System.out.println(ch + " is a lowercase letter");
else if (ch >= '0' && ch <= '9')
    System.out.println(ch + " is a numeric character");
\end{verbatim}

For convenience, Java provides the following methods in the \texttt{Character} class for testing characters as shown in Table 4.6.

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>isDigit(ch)</td>
<td>Returns true if the specified character is a digit.</td>
</tr>
<tr>
<td>isLetter(ch)</td>
<td>Returns true if the specified character is a letter.</td>
</tr>
<tr>
<td>isLetterOrDigit(ch)</td>
<td>Returns true if the specified character is a letter or digit.</td>
</tr>
<tr>
<td>isLowerCase(ch)</td>
<td>Returns true if the specified character is a lowercase letter.</td>
</tr>
<tr>
<td>isUpperCase(ch)</td>
<td>Returns true if the specified character is an uppercase letter.</td>
</tr>
<tr>
<td>toLowerCase(ch)</td>
<td>Returns the lowercase of the specified character.</td>
</tr>
<tr>
<td>toUpperCase(ch)</td>
<td>Returns the uppercase of the specified character.</td>
</tr>
</tbody>
</table>

For example,

\begin{verbatim}
System.out.println("isDigit('a') is "+ Character.isDigit('a'));
System.out.println("isLetter('a') is "+ Character.isLetter('a'));
System.out.println("isLowerCase('a') is "+ Character.isLowerCase('a'));
System.out.println("isUpperCase('a') is "+ Character.isUpperCase('a'));
System.out.println("toLowerCase('T') is "+ Character.toLowerCase('T'));
System.out.println("toUpperCase('q') is "+ Character.toUpperCase('q'));
\end{verbatim}

displays

isDigit('a') is false
isLetter('a') is true
isLowerCase('a') is true
isUpperCase('a') is false
toLowerCase('T') is t
toUpperCase('q') is Q

4.8 Use print statements to find out the ASCII code for '1', 'A', 'B', 'a', and 'b'. Use print statements to find out the character for the decimal codes 40, 59, 79, 85, and 90. Use print statements to find out the character for the hexadecimal code 40, 5A, 71, 72, and 7A.

4.9 Which of the following are correct literals for characters?
'1', '㑝E', '㿺', '', '	'

4.10 How do you display the characters \ and "?

4.11 Evaluate the following:
int i = '1';
int j = '1' + '2' * ('4' - '3') + 'b' / 'a';
int k = 'a';
char c = 90;

4.12 Can the following conversions involving casting be allowed? If so, find the converted result.
char c = 'A';
int i = (int)c;
float f = 1000.34f;
int i = (int)f;

double d = 1000.34;
int i = (int)d;

int i = 97;
char c = (char)i;

4.13 Show the output of the following program:

public class Test {
    public static void main(String[] args) {
        char x = 'a';
        char y = 'c';
        System.out.println(++x);
        System.out.println(y++);
        System.out.println(x - y);
    }
}

4.14 Write the code that generates a random lowercase letter.

4.15 Show the output of the following statements:
System.out.println('a' < 'b');
System.out.println('a' <= 'A');
System.out.println('a' > 'b');
System.out.println('a' >= 'A');
System.out.println('a' == 'a');
System.out.println('a' != 'b');
4.4 The String Type

A string is a sequence of characters.

The char type represents only one character. To represent a string of characters, use the data type called String. For example, the following code declares message to be a string with the value "Welcome to Java".

```java
String message = "Welcome to Java";
```

String is a predefined class in the Java library, just like the classes System and Scanner. The String type is not a primitive type. It is known as a reference type. Any Java class can be used as a reference type for a variable. The variable declared by a reference type is known as a reference variable that references an object. Here, message is a reference variable that references a string object with contents Welcome to Java.

Reference data types will be discussed in detail in Chapter 9, Objects and Classes. For the time being, you need to know only how to declare a String variable, how to assign a string to the variable, and how to use the methods in the String class. More details on using strings will be covered in Chapter 10.

Table 4.7 lists the String methods for obtaining string length, for accessing characters in the string, for concatenating strings, for converting a string to upper or lowercases, and for trimming a string.

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>length()</td>
<td>Returns the number of characters in this string.</td>
</tr>
<tr>
<td>charAt(index)</td>
<td>Returns the character at the specified index from this string.</td>
</tr>
<tr>
<td>concat(s1)</td>
<td>Returns a new string that concatenates this string with string s1.</td>
</tr>
<tr>
<td>toUpperCase()</td>
<td>Returns a new string with all letters in uppercase.</td>
</tr>
<tr>
<td>toLowerCase()</td>
<td>Returns a new string with all letters in lowercase.</td>
</tr>
<tr>
<td>trim()</td>
<td>Returns a new string with whitespace characters trimmed on both sides.</td>
</tr>
</tbody>
</table>

Strings are objects in Java. The methods in Table 4.7 can only be invoked from a specific string instance. For this reason, these methods are called instance methods. A non-instance method is called a static method. A static method can be invoked without using an object. All the methods defined in the Math class are static methods. They are not tied to a specific object instance. The syntax to invoke an instance method is reference-Variable.methodName(arguments). A method may have many arguments or no arguments. For example, the charAt(index) method has one argument, but the length() method has no arguments. Recall that the syntax to invoke a static method is ClassName.methodName(arguments). For example, the pow method in the Math class can be invoked using Math.pow(2, 2.5).

4.4.1 Getting String Length

You can use the length() method to return the number of characters in a string. For example, the following code

```java
String message = "Welcome to Java";
System.out.println("The length of " + message + " is " + message.length());
```
The length of Welcome to Java is 15

**Note**
When you use a string, you often know its literal value. For convenience, Java allows you to use the string literal to refer directly to strings without creating new variables. Thus, "Welcome to Java".length() is correct and returns 15. Note that "" denotes an empty string and "".length() is 0.

### 4.4.2 Getting Characters from a String

The `s.charAt(index)` method can be used to retrieve a specific character in a string `s`, where the index is between 0 and `s.length()-1`. For example, `message.charAt(0)` returns the character W, as shown in Figure 4.1. Note that the index for the first character in the string is 0.

![Figure 4.1](image)

**Figure 4.1** The characters in a `String` object can be accessed using its index.

**Caution**
Attempting to access characters in a string `s` out of bounds is a common programming error. To avoid it, make sure that you do not use an index beyond `s.length() - 1`. For example, `s.charAt(s.length())` would cause a `StringIndexOutOfBoundsException`.

### 4.4.3 Concatenating Strings

You can use the `concat` method to concatenate two strings. The statement shown below, for example, concatenates strings `s1` and `s2` into `s3`:

```
String s3 = s1.concat(s2);
```

Because string concatenation is heavily used in programming, Java provides a convenient way to accomplish it. You can use the plus (+) operator to concatenate two strings, so the previous statement is equivalent to

```
String s3 = s1 + s2;
```

The following code combines the strings `message`, " and ", and "HTML" into one string:

```
String myString = message + " and "+ "HTML";
```

Recall that the + operator can also concatenate a number with a string. In this case, the number is converted into a string and then concatenated. Note that at least one of the operands must be a string in order for concatenation to take place. If one of the operands is a nonstring...
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(e.g., a number), the nonstring value is converted into a string and concatenated with the other string. Here are some examples:

```java
// Three strings are concatenated
String message = "Welcome " + "to " + "Java";

// String Chapter is concatenated with number 2
String s = "Chapter" + 2;  // s becomes Chapter2

// String Supplement is concatenated with character B
String s1 = "Supplement" + 'B';  // s1 becomes SupplementB
```

If neither of the operands is a string, the plus sign (+) is the addition operator that adds two numbers.

The augmented += operator can also be used for string concatenation. For example, the following code appends the string "and Java is fun" with the string "Welcome to Java" in message.

```java
message += " and Java is fun";
```

So the new message is "Welcome to Java and Java is fun".

If i = 1 and j = 2, what is the output of the following statement?

```java
System.out.println("i + j is " + i + j);
```

The output is "i + j is 12" because "i + j is " is concatenated with the value of i first. To force i + j to be executed first, enclose i + j in the parentheses, as follows:

```java
System.out.println("i + j is " + (i + j));
```

### 4.4.4 Converting Strings

The `toLowerCase()` method returns a new string with all lowercase letters and the `toUpperCase()` method returns a new string with all uppercase letters. For example,

```java
"Welcome".toLowerCase() returns a new string welcome.
"Welcome".toUpperCase() returns a new string WELCOME.
```

The `trim()` method returns a new string by eliminating whitespace characters from both ends of the string. The characters ' ', \t, \f, \r, or \n are known as whitespace characters. For example,

```java
"\t Good Night \n".trim() returns a new string Good Night.
```

### 4.4.5 Reading a String from the Console

To read a string from the console, invoke the `next()` method on a `Scanner` object. For example, the following code reads three strings from the keyboard:

```java
Scanner input = new Scanner(System.in);
System.out.println("Enter three words separated by spaces: ");
String s1 = input.next();
String s2 = input.next();
String s3 = input.next();
System.out.println("s1 is " + s1);
System.out.println("s2 is " + s2);
System.out.println("s3 is " + s3);
```
4.4 The String Type

The `next()` method reads a string that ends with a whitespace character. You can use the `nextLine()` method to read an entire line of text. The `nextLine()` method reads a string that ends with the `Enter` key pressed. For example, the following statements read a line of text.

```java
Scanner input = new Scanner(System.in);
System.out.println("Enter a line: ");
String s = input.nextLine();
System.out.println("The line entered is " + s);
```

Enter a line: Welcome to Java
The line entered is Welcome to Java

**Important Caution**
To avoid input errors, do not use `nextLine()` after `nextByte()`, `nextShort()`, `nextInt()`, `nextLong()`, `nextFloat()`, `nextDouble()`, or `next()`. The reasons will be explained in Section 12.11.4, ‘How Does Scanner Work?’

4.4.6 Reading a Character from the Console

To read a character from the console, use the `nextLine()` method to read a string and then invoke the `charAt(0)` method on the string to return a character. For example, the following code reads a character from the keyboard:

```java
Scanner input = new Scanner(System.in);
System.out.print("Enter a character: ");
String s = input.nextLine();
char ch = s.charAt(0);
System.out.println("The character entered is " + ch);
```

4.4.7 Comparing Strings

The `String` class contains the methods as shown in Table 4.8 for comparing two strings.

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>equals(s1)</code></td>
<td>Returns true if this string is equal to string s1.</td>
</tr>
<tr>
<td><code>equalsIgnoreCase(s1)</code></td>
<td>Returns true if this string is equal to string s1; it is case insensitive.</td>
</tr>
<tr>
<td><code>compareTo(s1)</code></td>
<td>Returns an integer greater than 0, equal to 0, or less than 0 to indicate whether this string is greater than, equal to, or less than s1.</td>
</tr>
<tr>
<td><code>compareToIgnoreCase(s1)</code></td>
<td>Same as <code>compareTo</code> except that the comparison is case insensitive.</td>
</tr>
<tr>
<td><code>startsWith(prefix)</code></td>
<td>Returns true if this string starts with the specified prefix.</td>
</tr>
<tr>
<td><code>endsWith(suffix)</code></td>
<td>Returns true if this string ends with the specified suffix.</td>
</tr>
<tr>
<td><code>contains(s1)</code></td>
<td>Returns true if s1 is a substring in this string.</td>
</tr>
</tbody>
</table>
How do you compare the contents of two strings? You might attempt to use the == operator, as follows:

```java
if (string1 == string2)
    System.out.println("string1 and string2 are the same object");
else
    System.out.println("string1 and string2 are different objects");
```

However, the == operator checks only whether string1 and string2 refer to the same object; it does not tell you whether they have the same contents. Therefore, you cannot use the == operator to find out whether two string variables have the same contents. Instead, you should use the equals method. The following code, for instance, can be used to compare two strings:

```java
if (string1.equals(string2))
    System.out.println("string1 and string2 have the same contents");
else
    System.out.println("string1 and string2 are not equal");
```

For example, the following statements display true and then false.

```java
String s1 = "Welcome to Java";
String s2 = "Welcome to Java";
String s3 = "Welcome to C++";
System.out.println(s1.equals(s2)); // true
System.out.println(s1.equals(s3)); // false
```

The compareTo method can also be used to compare two strings. For example, consider the following code:

```java
s1.compareTo(s2)
```

The method returns the value 0 if s1 is equal to s2, a value less than 0 if s1 is lexicographically (i.e., in terms of Unicode ordering) less than s2, and a value greater than 0 if s1 is lexicographically greater than s2.

The actual value returned from the compareTo method depends on the offset of the first two distinct characters in s1 and s2 from left to right. For example, suppose s1 is abc and s2 is abg, and s1.compareTo(s2) returns -4. The first two characters (a vs. a) from s1 and s2 are compared. Because they are equal, the second two characters (b vs. b) are compared. Because they are also equal, the third two characters (c vs. g) are compared. Since the character c is 4 less than g, the comparison returns -4.

**Caution**

Syntax errors will occur if you compare strings by using relational operators >, >=, <, or <=. Instead, you have to use s1.compareTo(s2).

**Note**

The equals method returns true if two strings are equal and false if they are not. The compareTo method returns 0, a positive integer, or a negative integer, depending on whether one string is equal to, greater than, or less than the other string.

The String class also provides the equalsIgnoreCase and compareToIgnoreCase methods for comparing strings. The equalsIgnoreCase and compareToIgnoreCase methods ignore the case of the letters when comparing two strings. You can also use str.startsWith(prefix) to check whether string str starts with a specified prefix, str.endsWith(suffix) to check whether string str ends with a specified suffix, and str.contains(s1) to check whether string str contains string s1. For example,

```
"Welcome to Java".startsWith("We") returns true.
"Welcome to Java".startsWith("we") returns false.
"Welcome to Java".endsWith("va") returns true.
```

"Welcome to Java".endsWith("v") returns false.
"Welcome to Java".contains("to") returns true.
"Welcome to Java".contains("To") returns false.

Listing 4.2 gives a program that prompts the user to enter two cities and displays them in alphabetical order.

**Listing 4.2 OrderTwoCities.java**

```java
import java.util.Scanner;

public class OrderTwoCities {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter two cities
        System.out.print("Enter the first city: ");
        String city1 = input.nextLine();
        System.out.print("Enter the second city: ");
        String city2 = input.nextLine();

        if (city1.compareTo(city2) < 0)
            System.out.println("The cities in alphabetical order are "+
                                 city1 + " " + city2);
        else
            System.out.println("The cities in alphabetical order are "+
                                 city2 + " " + city1);
    }
}
```

Enter the first city: New York
Enter the second city: Boston
The cities in alphabetical order are Boston New York

The program reads two strings for two cities (lines 9, 11). If `input.nextLine()` is replaced by `input.next()` (line 9), you cannot enter a string with spaces for `city1`. Since a city name may contain multiple words separated by spaces, the program uses the `nextLine` method to read a string (lines 9, 11). Invoking `city1.compareTo(city2)` compares two strings `city1` with `city2` (line 13). A negative return value indicates that `city1` is less than `city2`.

### 4.4.8 Obtaining Substrings

You can obtain a single character from a string using the `charAt` method. You can also obtain a substring from a string using the `substring` method in the `String` class, as shown in Table 4.9.

For example,

```java
String message = "Welcome to Java";
String message = message.substring(0, 11) + "HTML";
```

The string `message` now becomes `Welcome to HTML`.

**Table 4.9** The `String` class contains the methods for obtaining substrings.

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>substring(beginIndex)</td>
<td>Returns this string’s substring that begins with the character at the specified beginIndex and extends to the end of the string, as shown in Figure 4.2.</td>
</tr>
<tr>
<td>substring(beginIndex, endIndex)</td>
<td>Returns this string’s substring that begins at the specified beginIndex and extends to the character at index endIndex - 1, as shown in Figure 4.2. Note that the character at endIndex is not part of the substring.</td>
</tr>
</tbody>
</table>
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Note
If beginIndex is endIndex, substring(beginIndex, endIndex) returns an empty string with length 0. If beginIndex > endIndex, it would be a runtime error.

4.4.9 Finding a Character or a Substring in a String
The String class provides several versions of indexOf and lastIndexOf methods to find a character or a substring in a string, as shown in Table 4.10.

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>index(ch)</td>
<td>Returns the index of the first occurrence of ch in the string. Returns -1 if not matched.</td>
</tr>
<tr>
<td>indexOf(ch, fromIndex)</td>
<td>Returns the index of the first occurrence of ch after fromIndex in the string. Returns -1 if not matched.</td>
</tr>
<tr>
<td>indexOf(s)</td>
<td>Returns the index of the first occurrence of string s in this string. Returns -1 if not matched.</td>
</tr>
<tr>
<td>indexOf(s, fromIndex)</td>
<td>Returns the index of the first occurrence of string s in this string after fromIndex. Returns -1 if not matched.</td>
</tr>
<tr>
<td>lastIndexOf(ch)</td>
<td>Returns the index of the last occurrence of ch in the string. Returns -1 if not matched.</td>
</tr>
<tr>
<td>lastIndexOf(ch, fromIndex)</td>
<td>Returns the index of the last occurrence of ch before fromIndex in this string. Returns -1 if not matched.</td>
</tr>
<tr>
<td>lastIndexOf(s)</td>
<td>Returns the index of the last occurrence of string s. Returns -1 if not matched.</td>
</tr>
<tr>
<td>lastIndexOf(s, fromIndex)</td>
<td>Returns the index of the last occurrence of string s before fromIndex. Returns -1 if not matched.</td>
</tr>
</tbody>
</table>

For example,

```java
String message = "Welcome to Java";
int beginIndex = 0, endIndex = 11;

String substring = message.substring(beginIndex, endIndex);
```

### Table 4.10 The String class contains the methods for finding substrings.

For example,

```java
int k = s.indexOf(' ');
String firstName = s.substring(0, k);
String lastName = s.substring(k + 1);
```
For example, if \( s \) is **Kim Jones**, the following diagram illustrates how the first name and last name are extracted.

```
Indices Message
0 1 2 3 4 5 6 7 8
K i m J o n e s s
k is 3
```

\( s.\text{substring}(0, k) \) is **Kim**

\( s.\text{substring}(k + 1) \) is **Jones**

### 4.4.10 Conversion between Strings and Numbers

You can convert a numeric string into a number. To convert a string into an \textit{int} value, use the 
\texttt{Integer.parseInt} method, as follows:

\[
\text{int intValue} = \text{Integer.parseInt(intString);} 
\]

where \texttt{intString} is a numeric string such as "123".

To convert a string into a \textit{double} value, use the \texttt{Double.parseDouble} method, as follows:

\[
\text{double doubleValue} = \text{Double.parseDouble(doubleString);} 
\]

where \texttt{doubleValue} is a numeric string such as "123.45".

If the string is not a numeric string, the conversion would cause a runtime error. The 
\texttt{Integer} and \texttt{Double} classes are both included in the \texttt{java.lang} package, and thus they are 
automatically imported.

You can convert a number into a string, simply use the string concatenating operator as 
follows:

\[
\text{String s = number} + \text{"";} 
\]

### 4.16

Suppose that \( s_1, s_2, \) and \( s_3 \) are three strings, given as follows:

```
String s1 = "Welcome to Java";
String s2 = "Programming is fun";
String s3 = "Welcome to Java";
```

What are the results of the following expressions?

(a) \( s_1 \equiv s_2 \)  
(b) \( s_2 \equiv s_3 \)  
(c) \( s_1.\text{equals}(s_2) \)  
(d) \( s_1.\text{equals}(s_3) \)  
(e) \( s_1.\text{compareTo}(s_2) \)  
(f) \( s_2.\text{compareTo}(s_3) \)  
(g) \( s_1.\text{indexOf}(\text{"to"}) \)  
(h) \( s_1.\text{charAt}(0) \)  
(i) \( s_1.\text{indexOf}(\text{"j"}) \)  
(j) \( s_1.\text{indexOf}(\text{"to"}) \)  
(k) \( s_1.\text{lastIndexOf}(\text{"a"}) \)  
(l) \( s_1.\text{indexOf}(\text{"o"}, 15) \)  
(m) \( s_1.\text{length()} \)  
(n) \( s_1.\text{substring}(5) \)  
(o) \( s_1.\text{substring}(5, 11) \)  
(p) \( s_1.\text{startsWith}(\text{"Wel"}) \)  
(q) \( s_1.\text{endsWith}(\text{"Java"}) \)  
(r) \( s_1.\text{toLowerCase()} \)  
(s) \( s_1.\text{toUpperCamse()} \)  
(t) \( s_1.\text{concat}(s_2) \)  
(u) \( s_1.\text{contains}(s_2) \)  
(v) \( \text{"\t Wel \t".trim()} \)
4.17 Suppose that \( s_1 \) and \( s_2 \) are two strings. Which of the following statements or expressions are incorrect?

```java
String s = "Welcome to Java";
String s3 = s1 + s2;
String s3 = s1 - s2;
s1 == s2;
s1 >= s2;
s1.compareTo(s2);
int i = s1.length();
char c = s1(0);
char c = s1.charAt(s1.length());
```

4.18 Show the output of the following statements (write a program to verify your results):

```java
System.out.println("1" + 1);
System.out.println('1' + 1);
System.out.println("1" + 1 + 1);
System.out.println("1" + (1 + 1));
System.out.println('1' + 1 + 1);
```

4.19 Evaluate the following expressions (write a program to verify your results):

```java
1 + "Welcome " + 1 + 1
1 + "Welcome " + (1 + 1)
1 + "Welcome " + ('\u0001' + 1)
1 + "Welcome " + 'a' + 1
```

4.20 Let \( s_1 \) be " Welcome " and \( s_2 \) be " welcome ". Write the code for the following statements:

(a) Check whether \( s_1 \) is equal to \( s_2 \) and assign the result to a Boolean variable `isEqual`.

(b) Check whether \( s_1 \) is equal to \( s_2 \), ignoring case, and assign the result to a Boolean variable `isEqual`.

(c) Compare \( s_1 \) with \( s_2 \) and assign the result to an int variable `x`.

(d) Compare \( s_1 \) with \( s_2 \), ignoring case, and assign the result to an int variable `x`.

(e) Check whether \( s_1 \) has the prefix AAA and assign the result to a Boolean variable `b`.

(f) Check whether \( s_1 \) has the suffix AAA and assign the result to a Boolean variable `b`.

(g) Assign the length of \( s_1 \) to an int variable `x`.

(h) Assign the first character of \( s_1 \) to a char variable `x`.

(i) Create a new string \( s_3 \) that combines \( s_1 \) with \( s_2 \).

(j) Create a substring of \( s_1 \) starting from index 1.

(k) Create a substring of \( s_1 \) from index 1 to index 4.

(l) Create a new string \( s_3 \) that converts \( s_1 \) to lowercase.

(m) Create a new string \( s_3 \) that converts \( s_1 \) to uppercase.

(n) Create a new string \( s_3 \) that trims whitespace characters on both ends of \( s_1 \).
4.5 Case Studies

Strings are fundamental in programming. The ability to write programs using strings is essential in learning Java programming.

You will frequently use strings to write useful programs. This section presents three examples of solving problems using strings.

4.5.1 Case Study: Guessing Birthdays

You can find out the date of the month when your friend was born by asking five questions. Each question asks whether the day is in one of the five sets of numbers.

The birthday is the sum of the first numbers in the sets where the day appears. For example, if the birthday is 19, it appears in Set1, Set2, and Set5. The first numbers in these three sets are 1, 2, and 16. Their sum is 19.

Listing 4.3 gives a program that prompts the user to answer whether the day is in Set1 (lines 41–44), in Set2 (lines 50–53), in Set3 (lines 59–62), in Set4 (lines 68–71), and in Set5 (lines 77–80). If the number is in the set, the program adds the first number in the set to day (lines 47, 56, 65, 74, 83).

**Listing 4.3 GuessBirthday.java**

```java
import java.util.Scanner;

public class GuessBirthday {
    public static void main(String[] args) {
        String set1 = "1 3 5 7
10 11 13 15
17 19 21 23
25 27 29 31";
        String set2 = "2 3 6 7
10 11 13 15
18 19 22 23
26 27 30 31"
        String set3 = "4 5 6 7
12 13 14 15
20 21 22 23
28 29 30 31"
        String set4 = "8 9 10 11
12 13 14 15
24 25 26 27
28 29 30 31"
        String set5 = "16 17 18 19
20 21 22 23
24 25 26 27
28 29 30 31"

        String set1 = "1 3 5 7
10 11 13 15
17 19 21 23
25 27 29 31"
        String set2 = "2 3 6 7
10 11 13 15
18 19 22 23
26 27 30 31"
        String set3 = "4 5 6 7
12 13 14 15
20 21 22 23
28 29 30 31"
        String set4 = "8 9 10 11
12 13 14 15
24 25 26 27
28 29 30 31"
        String set5 = "16 17 18 19
20 21 22 23
24 25 26 27
28 29 30 31"

        int day = 0;
        Scanner scanner = new Scanner(System.in);

        if (set1.contains(scanner.nextLine()))
            day += 1;
        if (set2.contains(scanner.nextLine()))
            day += 2;
        if (set3.contains(scanner.nextLine()))
            day += 3;
        if (set4.contains(scanner.nextLine()))
            day += 4;
        if (set5.contains(scanner.nextLine()))
            day += 5;

        System.out.println("The birthday is "+day);
    }
}
```

(o) Assign the index of the first occurrence of the character e in s1 to an int variable x.

(p) Assign the index of the last occurrence of the string abc in s1 to an int variable x.
Chapter 4  Mathematical Functions, Characters, and Strings

"10 11 14 15\n" +
"18 19 22 23\n" +
"26 27 30 31";

String set3 =
" 4  5  6  7\n" +
"12 13 14 15\n" +
"20 21 22 23\n" +
"28 29 30 31";

String set4 =
" 8  9 10 11\n" +
"12 13 14 15\n" +
"24 25 26 27\n" +
"28 29 30 31";

String set5 =
"16 17 18 19\n" +
"20 21 22 23\n" +
"24 25 26 27\n" +
"28 29 30 31";

// Create a Scanner
Scanner input = new Scanner(System.in);

// Prompt the user to answer questions
System.out.print("Is your birthday in Set1?\n");
System.out.print(set1);
System.out.print("Enter 0 for No and 1 for Yes: ");
int answer = input.nextInt();

if (answer == 1)
    day += 1;

// Prompt the user to answer questions
System.out.print("Is your birthday in Set2?\n");
System.out.print(set2);
System.out.print("Enter 0 for No and 1 for Yes: ");
answer = input.nextInt();

if (answer == 1)
    day += 2;

// Prompt the user to answer questions
System.out.print("Is your birthday in Set3?\n");
System.out.print(set3);
System.out.print("Enter 0 for No and 1 for Yes: ");
answer = input.nextInt();

if (answer == 1)
    day += 4;

// Prompt the user to answer questions
System.out.print("Is your birthday in Set4?\n");
System.out.print(set4);
System.out.print("Enter 0 for No and 1 for Yes: ");
answer = input.nextInt();

int day = 0;
if (answer == 1)
    day += 8;

// Prompt the user to answer questions
System.out.print("Is your birthday in Set5?\n");
System.out.print(set5);
System.out.print("Enter 0 for No and 1 for Yes: ");
answer = input.nextInt();

if (answer == 1)
    day += 16;

System.out.println("Your birthday is "+ day + "!");

Is your birthday in Set1?
1 3 5 7
9 11 13 15
17 19 21 23
25 27 29 31
Enter 0 for No and 1 for Yes: 1

Is your birthday in Set2?
2 3 6 7
10 11 14 15
18 19 22 23
26 27 30 31
Enter 0 for No and 1 for Yes: 1

Is your birthday in Set3?
4 5 6 7
12 13 14 15
20 21 22 23
28 29 30 31
Enter 0 for No and 1 for Yes: 0

Is your birthday in Set4?
8 9 10 11
12 13 14 15
24 25 26 27
28 29 30 31
Enter 0 for No and 1 for Yes: 0

Is your birthday in Set5?
16 17 18 19
20 21 22 23
24 25 26 27
28 29 30 31
Enter 0 for No and 1 for Yes: 1
Your birthday is 19!
This game is easy to program. You may wonder how the game was created. The mathematics behind the game is actually quite simple. The numbers are not grouped together by accident—the way they are placed in the five sets is deliberate. The starting numbers in the five sets are 1, 2, 4, 8, and 16, which correspond to 1, 10, 100, 1000, and 10000 in binary (binary numbers are introduced in Appendix F, Number Systems). A binary number for decimal integers between 1 and 31 has at most five digits, as shown in Figure 4.3a. Let it be \( b_5b_4b_3b_2b_1 \). Thus, \( b_5b_4b_3b_2b_1 = b_50000 + b_4000 + b_300 + b_20 + b_1 \), as shown in Figure 4.3b. If a day’s binary number has a digit 1 in \( b_k \), the number should appear in Set\( k \). For example, number 19 is binary 10011, so it appears in Set1, Set2, and Set5. It is binary \( 1 + 2 + 16 = 19 \) or decimal 19. Number 31 is binary 11111, so it appears in Set1, Set2, Set3, Set4, and Set5. It is binary \( 1 + 2 + 4 + 8 + 16 = 31 \).

![Figure 4.3](image)

<table>
<thead>
<tr>
<th>day</th>
<th>answer</th>
<th>output</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>0</td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>1</td>
<td></td>
</tr>
</tbody>
</table>

This table shows the lines of code and the corresponding outputs. The output for line 83 is 19, indicating the birthday is 19.

4.21 If you run Listing 4.3 GuessBirthday.java with input 1 for Set1, Set3, and Set4 and 0 for Set2 and Set5, what will be the birthday?

4.5.2 Case Study: Converting a Hexadecimal Digit to a Decimal Value

The hexadecimal number system has 16 digits: 0–9, A–F. The letters A, B, C, D, E, and F correspond to the decimal numbers 10, 11, 12, 13, 14, and 15. We now write a program that prompts the user to enter a hex digit and display its corresponding decimal value, as shown in Listing 4.4.
4.5 Case Studies

LISTING 4.4 HexDigit2Dec.java

```java
import java.util.Scanner;

public class HexDigit2Dec {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        System.out.print("Enter a hex digit: ");
        String hexString = input.nextLine();

        // Check if the hex string has exactly one character
        if (hexString.length() != 1) {
            System.out.println("You must enter exactly one character");
            System.exit(1);
        }

        // Display decimal value for the hex digit
        char ch = hexString.charAt(0);
        if (ch <= 'F' && ch >= 'A') {
            int value = ch - 'A' + 10;
            System.out.println("The decimal value for hex digit " + ch + " is " + value);
        } else if (Character.isDigit(ch)) {
            System.out.println("The decimal value for hex digit " + ch + " is " + ch);
        } else {
            System.out.println(ch + " is an invalid input");
        }
    }
}
```

Enter a hex digit: AB7C
You must enter exactly one character

Enter a hex digit: B
The decimal value for hex digit B is 11

Enter a hex digit: 8
The decimal value for hex digit 8 is 8

Enter a hex digit: T
T is an invalid input

The program reads a string from the console (line 7) and checks if the string contains a single character (line 10). If not, report an error and exit the program (line 12).

The program invokes the `Character.toUpperCase` method to obtain the character `ch` as an uppercase letter (line 16). If `ch` is between 'A' and 'F' (line 17), the corresponding decimal value is `ch - 'A' + 10` (line 18). Note that `ch - 'A'` is 0 if `ch` is 'A', `ch - 'A'` is 1
if `ch` is 'B', and so on. When two characters perform a numerical operation, the characters’ Unicodes are used in the computation.

The program invokes the `Character.isDigit(ch)` method to check if `ch` is between '0' and '9' (line 22). If so, the corresponding decimal digit is the same as `ch` (lines 23–24). If `ch` is not between 'A' and 'F' nor a digit character, the program displays an error message (line 27).

### 4.5.3 Case Study: Revising the Lottery Program Using Strings

The lottery program in Listing 3.8, `Lottery.java`, generates a random two-digit number, prompts the user to enter a two-digit number, and determines whether the user wins according to the following rule:

1. If the user input matches the lottery number in the exact order, the award is $10,000.
2. If all the digits in the user input match all the digits in the lottery number, the award is $3,000.
3. If one digit in the user input matches a digit in the lottery number, the award is $1,000.

The program in Listing 3.8 uses an integer to store the number. Listing 4.5 gives a new program that generates a random two-digit string instead of a number and receives the user input as a string instead of a number.

#### Listing 4.5 LotteryUsingStrings.java

```java
import java.util.Scanner;

public class LotteryUsingStrings {
    public static void main(String[] args) {
        // Generate a lottery as a two-digit string
        String lottery = "" + (int)(Math.random() * 10) + (int)(Math.random() * 10);

        // Prompt the user to enter a guess
        Scanner input = new Scanner(System.in);
        System.out.print("Enter your lottery pick (two digits): ");
        String guess = input.nextLine();

        // Get digits from lottery
        char lotteryDigit1 = lottery.charAt(0);
        char lotteryDigit2 = lottery.charAt(1);

        // Get digits from guess
        char guessDigit1 = guess.charAt(0);
        char guessDigit2 = guess.charAt(1);

        System.out.println("The lottery number is " + lottery);

        // Check the guess
        if (guess.equals(lottery))
            System.out.println("Exact match: you win $10,000");
        else if (guessDigit2 == lotteryDigit1 && guessDigit1 == lotteryDigit2)
            System.out.println("Match all digits: you win $3,000");
        else if (guessDigit1 == lotteryDigit1 || guessDigit1 == lotteryDigit2
                 || guessDigit2 == lotteryDigit1 || guessDigit2 == lotteryDigit2)
            System.out.println("Match one digit: you win $1,000");
```
else
System.out.println("Sorry, no match");
}

Enter your lottery pick (two digits): 00
The lottery number is 00
Exact match: you win $10,000

Enter your lottery pick (two digits): 45
The lottery number is 54
Match all digits: you win $3,000

Enter your lottery pick: 23
The lottery number is 34
Match one digit: you win $1,000

Enter your lottery pick: 23
The lottery number is 14
Sorry: no match

The program generates two random digits and concatenates them into the string `lottery` (lines 6–7). After this, `lottery` contains two random digits.

The program prompts the user to enter a guess as a two-digit string (line 12) and checks the guess against the lottery number in this order:

- First check whether the guess matches the lottery exactly (line 25).
- If not, check whether the reversal of the guess matches the lottery (line 27).
- If not, check whether one digit is in the lottery (lines 30–33).
- If not, nothing matches and display “Sorry, no match” (line 36).

### 4.6 Formatting Console Output

You can use the `System.out.printf` method to display formatted output on the console.

Often, it is desirable to display numbers in a certain format. For example, the following code computes interest, given the amount and the annual interest rate.

```java
double amount = 12618.98;
double interestRate = 0.0013;
double interest = amount * interestRate;
System.out.println("Interest is $" + interest);
```

Interest is $16.404674
Because the interest amount is currency, it is desirable to display only two digits after the decimal point. To do this, you can write the code as follows:

```java
double amount = 12618.98;
double interestRate = 0.0013;
double interest = amount * interestRate;
System.out.println("Interest is "+ (int)(interest * 100) / 100.0);
```

Interest is $16.4

However, the format is still not correct. There should be two digits after the decimal point: **16.40** rather than **16.4**. You can fix it by using the `printf` method, like this:

```java
double amount = 12618.98;
double interestRate = 0.0013;
double interest = amount * interestRate;
System.out.printf("Interest is $%4.2f", interest);
```

Interest is $16.40

The syntax to invoke this method is

```
System.out.printf(format, item1, item2, ..., itemk)
```

where `format` is a string that may consist of substrings and format specifiers.

A `format specifier` specifies how an item should be displayed. An item may be a numeric value, a character, a Boolean value, or a string. A simple format specifier consists of a percent sign (`%`) followed by a conversion code. Table 4.11 lists some frequently used simple format specifiers.

**Table 4.11** Frequently Used Format Specifiers

<table>
<thead>
<tr>
<th>Format Specifier</th>
<th>Output</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>%b</td>
<td>a Boolean value</td>
<td>true or false</td>
</tr>
<tr>
<td>%c</td>
<td>a character</td>
<td>'a'</td>
</tr>
<tr>
<td>%d</td>
<td>a decimal integer</td>
<td>200</td>
</tr>
<tr>
<td>%f</td>
<td>a floating-point number</td>
<td>45.460000</td>
</tr>
<tr>
<td>%e</td>
<td>a number in standard scientific notation</td>
<td>4.556000e+01</td>
</tr>
<tr>
<td>%s</td>
<td>a string</td>
<td>&quot;Java is cool&quot;</td>
</tr>
</tbody>
</table>

Here is an example:

```java
int count = 5;
double amount = 45.56;
System.out.printf("count is %d and amount is %f", count, amount);
```

display count is 5 and amount is 45.560000
Items must match the format specifiers in order, in number, and in exact type. For example, the format specifier for `count` is `%d` and for `amount` is `%f`. By default, a floating-point value is displayed with six digits after the decimal point. You can specify the width and precision in a format specifier, as shown in the examples in Table 4.12.

### Table 4.12   Examples of Specifying Width and Precision

<table>
<thead>
<tr>
<th>Example</th>
<th>Output</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>%5c</code></td>
<td>Output the character and add four spaces before the character item, because the width is 5.</td>
</tr>
<tr>
<td><code>%6b</code></td>
<td>Output the Boolean value and add one space before the false value and two spaces before the true value.</td>
</tr>
<tr>
<td><code>%5d</code></td>
<td>Output the integer item with width at least 5. If the number of digits in the item is &lt; 5, add spaces before the number. If the number of digits in the item is &gt; 5, the width is automatically increased.</td>
</tr>
<tr>
<td><code>%10.2f</code></td>
<td>Output the floating-point item with width at least 10 including a decimal point and two digits after the point. Thus, there are 7 digits allocated before the decimal point. If the number of digits before the decimal point in the item is &gt; 7, add spaces before the number. If the number of digits before the decimal point in the item is &gt; 7, the width is automatically increased.</td>
</tr>
<tr>
<td><code>%10.2e</code></td>
<td>Output the floating-point item with width at least 10 including a decimal point, two digits after the point and the exponent part. If the displayed number in scientific notation has width less than 10, add spaces before the number.</td>
</tr>
<tr>
<td><code>%12s</code></td>
<td>Output the string with width at least 12 characters. If the string item has fewer than 12 characters, add spaces before the string. If the string item has more than 12 characters, the width is automatically increased.</td>
</tr>
</tbody>
</table>

If an item requires more spaces than the specified width, the width is automatically increased. For example, the following code

```java
System.out.printf("%3d#%2s#%4.2f\n", 1234, "Java", 51.6653);
```

displays

```
1234#Java#51.67
```

The specified width for `int` item `1234` is `3`, which is smaller than its actual size `4`. The width is automatically increased to `4`. The specified width for string item `Java` is `2`, which is smaller than its actual size `4`. The width is automatically increased to `4`. The specified width for `double` item `51.6653` is `4`, but it needs width `5` to display `51.67`, so the width is automatically increased to `5`.

By default, the output is right justified. You can put the minus sign (`-`) in the format specifier to specify that the item is left justified in the output within the specified field. For example, the following statements

```java
System.out.printf("%8d%8s%8.1f\n", 1234, "Java", 5.63);
System.out.printf("%-8d%-8s%-8.1f \n", 1234, "Java", 5.63);
```

display

```
|[←8]─[←8]─[←8]─[←8]─
1234  Java  5.6
1234  Java  5.6
```

where the square box (□) denotes a blank space.
Caution
The items must match the format specifiers in exact type. The item for the format specifier \%f or \%e must be a floating-point type value such as 40.0, not 40. Thus, an int variable cannot match \%f or \%e.

Tip
The \% sign denotes a format specifier. To output a literal \% in the format string, use \%\%.

Listing 4.6 gives a program that uses printf to display a table.

**LISTING 4.6 FormatDemo.java**

```java
public class FormatDemo {
    public static void main(String[] args) {
        // Display the header of the table
        System.out.printf("%-10s%-10s%-10s%-10s%-10s\n", "Degrees", "Radians", "Sine", "Cosine", "Tangent");

        // Display values for 30 degrees
        System.out.printf("%-10d%-10.4f%-10.4f%-10.4f%-10.4f\n", degrees, radians, Math.sin(radians), Math.cos(radians), Math.tan(radians));

        // Display values for 60 degrees
        System.out.printf("%-10d%-10.4f%-10.4f%-10.4f%-10.4f\n", degrees, radians, Math.sin(radians), Math.cos(radians), Math.tan(radians));
    }
}
```

<table>
<thead>
<tr>
<th>Degrees</th>
<th>Radians</th>
<th>Sine</th>
<th>Cosine</th>
<th>Tangent</th>
</tr>
</thead>
<tbody>
<tr>
<td>30</td>
<td>0.5236</td>
<td>0.5000</td>
<td>0.8660</td>
<td>0.5773</td>
</tr>
<tr>
<td>60</td>
<td>1.0472</td>
<td>0.8660</td>
<td>0.5000</td>
<td>1.7320</td>
</tr>
</tbody>
</table>

The statement in lines 4–5 displays the column names of the table. The column names are strings. Each string is displayed using the specifier \%-10s, which left-justifies the string. The statement in lines 10–12 displays the degrees as an integer and four float values. The integer is displayed using the specifier \%-10d and each float is displayed using the specifier \%-10.4f, which specifies four digits after the decimal point.

4.22 What are the format specifiers for outputting a Boolean value, a character, a decimal integer, a floating-point number, and a string?

4.23 What is wrong in the following statements?

(a) System.out.printf("%5d %d", 1, 2, 3);
(b) System.out.printf("%5d %f", 1);
(c) System.out.printf("%5d %f", 1, 2);
Show the output of the following statements.

(a) `System.out.printf("amount is %f %e\n", 32.32, 32.32);
(b) `System.out.printf("amount is %5.2f %5.4e\n", 32.327, 32.32);
(c) `System.out.printf("%6b\n", (1 > 2));
(d) `System.out.printf("%6s\n", "Java");
(e) `System.out.printf("%-6b%s\n", (1 > 2), "Java");
(f) `System.out.printf("%6b%-8s\n", (1 > 2), "Java");

### Key Terms

<table>
<thead>
<tr>
<th>Term</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>char type</td>
<td>125</td>
</tr>
<tr>
<td>encoding</td>
<td>125</td>
</tr>
<tr>
<td>escape character</td>
<td>127</td>
</tr>
<tr>
<td>escape sequence</td>
<td>126</td>
</tr>
<tr>
<td>format specifier</td>
<td>146</td>
</tr>
<tr>
<td>instance method</td>
<td>130</td>
</tr>
<tr>
<td>static method</td>
<td>130</td>
</tr>
<tr>
<td>supplementary Unicode</td>
<td>125</td>
</tr>
<tr>
<td>Unicode</td>
<td>125</td>
</tr>
<tr>
<td>whitespace character</td>
<td>133</td>
</tr>
</tbody>
</table>

### Chapter Summary

1. Java provides the mathematical methods `sin`, `cos`, `tan`, `asin`, `acos`, `atan`, `toRadians`, `toDegree`, `exp`, `log`, `log10`, `pow`, `sqrt`, `ceil`, `floor`, `rint`, `round`, `min`, `max`, `abs`, and `random` in the `Math` class for performing mathematical functions.

2. The character type `char` represents a single character.

3. An escape sequence consists of a backslash (\) followed by a character or a combination of digits.

4. The character \ is called the escape character.

5. The characters ``, `\t`, `\f`, `\r`, and `\n` are known as the whitespace characters.

6. Characters can be compared based on their Unicode using the relational operators.

7. The `Character` class contains the methods `isDigit`, `isLetter`, `isLetterOrDigit`, `isLowerCase`, `isUpperCase` for testing whether a character is a digit, letter, lowercase, and uppercase. It also contains the `toLowerCase` and `toUpperCase` methods for returning a lowercase or uppercase letter.

8. A `string` is a sequence of characters. A string value is enclosed in matching double quotes (`"`). A character value is enclosed in matching single quotes (`'`).

9. Strings are objects in Java. A method that can only be invoked from a specific object is called an instance method. A non-instance method is called a static method, which can be invoked without using an object.
10. You can get the length of a string by invoking its `length()` method, retrieve a character at the specified index in the string using the `charAt(index)` method, and use the `indexOf` and `lastIndexOf` methods to find a character or a substring in a string.

11. You can use the `concat` method to concatenate two strings, or the plus (+) operator to concatenate two or more strings.

12. You can use the `substring` method to obtain a substring from the string.

13. You can use the `equals` and `compareTo` methods to compare strings. The `equals` method returns `true` if two strings are equal, and `false` if they are not equal. The `compareTo` method returns 0, a positive integer, or a negative integer, depending on whether one string is equal to, greater than, or less than the other string.

14. The `printf` method can be used to display a formatted output using format specifiers.

**Quiz**

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

**Programming Exercises**

Section 4.2

4.1  
*(Geometry: area of a pentagon)* Write a program that prompts the user to enter the length from the center of a pentagon to a vertex and computes the area of the pentagon, as shown in the following figure.

![Pentagon Diagram]

The formula for computing the area of a pentagon is \[ \text{Area} = \frac{5 \times s^2}{4 \times \tan \left( \frac{\pi}{5} \right)} \], where

\( s \) is the length of a side. The side can be computed using the formula \( s = 2r \sin \frac{\pi}{5} \), where \( r \) is the length from the center of a pentagon to a vertex. Round up two digits after the decimal point. Here is a sample run:

```
Enter the length from the center to a vertex: 5.5
The area of the pentagon is 71.92
```
*4.2  (Geometry: great circle distance) The great circle distance is the distance between two points on the surface of a sphere. Let \((x_1, y_1)\) and \((x_2, y_2)\) be the geographical latitude and longitude of two points. The great circle distance between the two points can be computed using the following formula:

\[
d = \text{radius} \times \arccos(\sin(x_1) \times \sin(x_2) + \cos(x_1) \times \cos(x_2) \times \cos(y_1 - y_2))
\]

Write a program that prompts the user to enter the latitude and longitude of two points on the earth in degrees and displays its great circle distance. The average earth radius is 6,371.01 km. Note that you need to convert the degrees into radians using the `Math.toRadians` method since the Java trigonometric methods use radians. The latitude and longitude degrees in the formula are for north and west. Use negative to indicate south and east degrees. Here is a sample run:

Enter point 1 (latitude and longitude) in degrees: 39.55, -116.25
Enter point 2 (latitude and longitude) in degrees: 41.5, 87.37
The distance between the two points is 10691.79183231593 km

*4.3  (Geography: estimate areas) Find the GPS locations for Atlanta, Georgia; Orlando, Florida; Savannah, Georgia; and Charlotte, North Carolina from www.gps-data-team.com/map/ and compute the estimated area enclosed by these four cities. (Hint: Use the formula in Programming Exercise 4.2 to compute the distance between two cities. Divide the polygon into two triangles and use the formula in Programming Exercise 2.19 to compute the area of a triangle.)

4.4  (Geometry: area of a hexagon) The area of a hexagon can be computed using the following formula (\(s\) is the length of a side):

\[
\text{Area} = \frac{6 \times s^2}{4 \times \tan\left(\frac{\pi}{6}\right)}
\]

Write a program that prompts the user to enter the side of a hexagon and displays its area. Here is a sample run:

Enter the side: 5.5
The area of the hexagon is 78.59

*4.5  (Geometry: area of a regular polygon) A regular polygon is an \(n\)-sided polygon in which all sides are of the same length and all angles have the same degree (i.e., the polygon is both equilateral and equiangular). The formula for computing the area of a regular polygon is

\[
\text{Area} = \frac{n \times s^2}{4 \times \tan\left(\frac{\pi}{n}\right)}
\]
Here, \( s \) is the length of a side. Write a program that prompts the user to enter the number of sides and their length of a regular polygon and displays its area. Here is a sample run:

\[
\text{Enter the number of sides: 5} \quad \text{Enter the side: 6.5} \quad \text{The area of the polygon is 74.69017017488385} \]

\*4.6 (Random points on a circle) Write a program that generates three random points on a circle centered at \((0, 0)\) with radius 40 and display three angles in a triangle formed by these three points, as shown in Figure 4.7a. (Hint: Generate a random angle \( \alpha \) in radians between 0 and \( 2\pi \), as shown in Figure 4.7b and the point determined by this angle is \((r\cos(\alpha), r\sin(\alpha))\).

\[ x = r \cos(\alpha) \text{ and } y = r \sin(\alpha) \]

\[ 0 \text{ o’clock position} \]

\( x = r \cos(\alpha) \text{ and } y = r \sin(\alpha) \]

Figure 4.7 (a) A triangle is formed from three random points on the circle. (b) A random point on the circle can be generated using a random angle \( \alpha \). (c) A pentagon is centered at \((0, 0)\) with one point at the 0 o’clock position.

\*4.7 (Corner point coordinates) Suppose a pentagon is centered at \((0, 0)\) with one point at the 0 o’clock position, as shown in Figure 4.7c. Write a program that prompts the user to enter the radius of the bounding circle of a pentagon and displays the coordinates of the five corner points on the pentagon. Here is a sample run:

\[
\text{Enter the radius of the bounding circle: 100} \quad \text{Enter the radius of the bounding circle: 100} \quad \text{The coordinates of five points on the pentagon are} \\
(95.1057, 30.9017) \quad (0.00132679, 100) \quad (-95.1056, 30.9019) \quad (-58.7788, -80.9015) \quad (58.7782, -80.902) \\
\]

\textbf{Sections 4.3–4.6}

\*4.8 (Find the character of an ASCII code) Write a program that receives an ASCII code (an integer between 0 and 127) and displays its character. Here is a sample run:

\[
\text{Enter an ASCII code: 69} \quad \text{Enter an ASCII code: 69} \quad \text{The character for ASCII code 69 is E} \\
\]
*4.9  *(Find the Unicode of a character)* Write a program that receives a character and displays its Unicode. Here is a sample run:

```
Enter a character: E
The Unicode for the character E is 69
```

*4.10  *(Guess birthday)* Rewrite Listing 4.3, GuessBirthday.java, to prompt the user to enter the character Y for Yes and N for No rather than entering 1 for Yes and 0 for No.

*4.11  *(Decimal to hex)* Write a program that prompts the user to enter an integer between 0 and 15 and displays its corresponding hex number. Here are some sample runs:

```
Enter a decimal value (0 to 15): 11
The hex value is B
```

```
Enter a decimal value (0 to 15): 5
The hex value is 5
```

```
Enter a decimal value (0 to 15): 31
31 is an invalid input
```

4.12  *(Hex to binary)* Write a program that prompts the user to enter a hex digit and displays its corresponding binary number. Here is a sample run:

```
Enter a hex digit: B
The binary value is 1011
```

```
Enter a hex digit: G
G is an invalid input
```

*4.13  *(Vowel or consonant?)* Write a program that prompts the user to enter a letter and check whether the letter is a vowel or consonant. Here is a sample run:

```
Enter a letter: B
B is a consonant
```

```
Enter a letter grade: a
a is a vowel
```

```
Enter a letter grade: #
# is an invalid input
```
*4.14 (Convert letter grade to number) Write a program that prompts the user to enter a letter grade A, B, C, D, or F and displays its corresponding numeric value 4, 3, 2, 1, or 0. Here is a sample run:

Enter a letter grade: B
The numeric value for grade B is 3

Enter a letter grade: T
T is an invalid grade

*4.15 (Phone key pads) The international standard letter/number mapping found on the telephone is shown below:

Write a program that prompts the user to enter a letter and displays its corresponding number.

Enter a letter: A
The corresponding number is 2

Enter a letter: a
The corresponding number is 2

Enter a letter: +
+ is an invalid input

4.16 (Random character) Write a program that displays a random uppercase letter using the `Math.random()` method.

*4.17 (Days of a month) Write a program that prompts the user to enter a year and the first three letters of a month name (with the first letter in uppercase) and displays the number of days in the month. Here is a sample run:

Enter a year: 2001
Enter a month: Jan
Jan 2001 has 31 days
**4.18** *(Student major and status)* Write a program that prompts the user to enter two
characters and displays the major and status represented in the characters. The first
character indicates the major and the second is number character 1, 2, 3, 4, which
indicates whether a student is a freshman, sophomore, junior, or senior. Suppose
the following characters are used to denote the majors:

M: Mathematics
C: Computer Science
I: Information Technology

Here is a sample run:

Enter two characters: M1
Mathematics Freshman

Enter two characters: C3
Computer Science Junior

Enter two characters: T3
Invalid input

**4.19** *(Business: check ISBN-10)* Rewrite the Programming Exercise 3.9 by entering the
ISBN number as a string.

**4.20** *(Process a string)* Write a program that prompts the user to enter a string and dis-
plays its length and its first character.

**4.21** *(Check SSN)* Write a program that prompts the user to enter a Social Security
number in the format DDD-DD-DDDD, where D is a digit. Your program should
check whether the input is valid. Here are sample runs:

Enter a SSN: 232-23-5435
232-23-5435 is a valid social security number

Enter a SSN: 23-23-5435
23-23-5435 is an invalid social security number

**4.22** *(Check substring)* Write a program that prompts the user to enter two strings and
reports whether the second string is a substring of the first string.

Enter string s1: ABCD
Enter string s2: BC
BC is a substring of ABCD
**4.23** *(Financial application: payroll)* Write a program that reads the following information and prints a payroll statement:

- Employee’s name (e.g., Smith)
- Number of hours worked in a week (e.g., 10)
- Hourly pay rate (e.g., 9.75)
- Federal tax withholding rate (e.g., 20%)
- State tax withholding rate (e.g., 9%)

A sample run is shown below:

```
Enter employee's name: Smith
Enter number of hours worked in a week: 10
Enter hourly pay rate: 9.75
Enter federal tax withholding rate: 0.20
Enter state tax withholding rate: 0.09

Employee Name: Smith
Hours Worked: 10.0
Pay Rate: $9.75
Gross Pay: $97.5
Deductions:
  Federal Withholding (20.0%): $19.5
  State Withholding (9.0%): $8.77
  Total Deduction: $28.27
Net Pay: $69.22
```

**4.24** *(Order three cities)* Write a program that prompts the user to enter three cities and displays them in ascending order. Here is a sample run:

```
Enter the first city: Chicago
Enter the second city: Los Angeles
Enter the third city: Atlanta
The three cities in alphabetical order are Atlanta Chicago Los Angeles
```

**4.25** *(Generate vehicle plate numbers)* Assume a vehicle plate number consists of three uppercase letters followed by four digits. Write a program to generate a plate number.

**4.26** *(Financial application: monetary units)* Rewrite Listing 2.10, ComputeChange.java, to fix the possible loss of accuracy when converting a float value to an int value. Read the input as a string such as "11.56". Your program should extract the dollar amount before the decimal point and the cents after the decimal amount using the indexOf and substring methods.
LOOPS

Objectives

- To write programs for executing statements repeatedly using a `while` loop (§5.2).
- To follow the loop design strategy to develop loops (§§5.2.1–5.2.3).
- To control a loop with a sentinel value (§5.2.4).
- To obtain large input from a file using input redirection rather than typing from the keyboard (§5.2.5).
- To write loops using `do-while` statements (§5.3).
- To write loops using `for` statements (§5.4).
- To discover the similarities and differences of three types of loop statements (§5.5).
- To write nested loops (§5.6).
- To learn the techniques for minimizing numerical errors (§5.7).
- To learn loops from a variety of examples (`GCD`, `FutureTuition`, `Dec2Hex`) (§5.8).
- To implement program control with `break` and `continue` (§5.9).
- To process characters in a string using a loop in a case study for checking palindrome (§5.10).
- To write a program that displays prime numbers (§5.11).
5.1 Introduction

A loop can be used to tell a program to execute statements repeatedly.

Suppose that you need to display a string (e.g., Welcome to Java!) a hundred times. It would be tedious to have to write the following statement a hundred times:

```
System.out.println("Welcome to Java!");
System.out.println("Welcome to Java!");
...
System.out.println("Welcome to Java!");
```

So, how do you solve this problem?

Java provides a powerful construct called a loop that controls how many times an operation or a sequence of operations is performed in succession. Using a loop statement, you simply tell the computer to display a string a hundred times without having to code the print statement a hundred times, as follows:

```java
int count = 0;
while (count < 100) {
    System.out.println("Welcome to Java!");
    count++;
}
```

The variable `count` is initially 0. The loop checks whether `count < 100` is true. If so, it executes the loop body to display the message Welcome to Java! and increments `count` by 1. It repeatedly executes the loop body until `count < 100` becomes false. When `count < 100` is false (i.e., when `count` reaches 100), the loop terminates and the next statement after the while loop is executed.

Loops are constructs that control repeated executions of a block of statements. The concept of looping is fundamental to programming. Java provides three types of loop statements: while loops, do-while loops, and for loops.

5.2 The while Loop

A while loop executes statements repeatedly while the condition is true.

The syntax for the while loop is:

```java
while (loop-continuation-condition) {
    // Loop body
    Statement(s);
}
```

Figure 5.1a shows the while-loop flowchart. The part of the loop that contains the statements to be repeated is called the loop body. A one-time execution of a loop body is referred to as an iteration (or repetition) of the loop. Each loop contains a loop-continuation-condition, a Boolean expression that controls the execution of the body. It is evaluated each time to determine if the loop body is executed. If its evaluation is true, the loop body is executed; if its evaluation is false, the entire loop terminates and the program control turns to the statement that follows the while loop.

The loop for displaying Welcome to Java! a hundred times introduced in the preceding section is an example of a while loop. Its flowchart is shown in Figure 5.1b. The
In this example, you know exactly how many times the loop body needs to be executed because the control variable `count` is used to count the number of executions. This type of loop is known as a **counter-controlled loop**.

Note

The **loop-continuation-condition** must always appear inside the parentheses. The braces enclosing the loop body can be omitted only if the loop body contains one or no statement.

Here is another example to help understand how a loop works.

```java
int sum = 0, i = 1;
while (i < 10) {
    sum = sum + i;
    i++;
} System.out.println("sum is " + sum); // sum is 45
```

If `i < 10` is **true**, the program adds `i` to `sum`. Variable `i` is initially set to `1`, then is incremented to `2`, `3`, and up to `10`. When `i` is `10`, `i < 10` is **false**, so the loop exits. Therefore, the sum is `1 + 2 + 3 + ... + 9 = 45`.

What happens if the loop is mistakenly written as follows?

```java
int sum = 0, i = 1;
while (i < 10) {
    sum = sum + i;
}
```

This loop is infinite, because `i` is always `1` and `i < 10` will always be **true**.
Note
Make sure that the loop-continuation-condition eventually becomes false so that the loop will terminate. A common programming error involves infinite loops (i.e., the loop runs forever). If your program takes an unusually long time to run and does not stop, it may have an infinite loop. If you are running the program from the command window, press CTRL+C to stop it.

Caution
Programmers often make the mistake of executing a loop one more or less time. This is commonly known as the off-by-one error. For example, the following loop displays Welcome to Java 101 times rather than 100 times. The error lies in the condition, which should be count < 100 rather than count <= 100.

```java
int count = 0;
while (count <= 100) {
    System.out.println("Welcome to Java!");
    count++;
}
```

Recall that Listing 3.1, AdditionQuiz.java, gives a program that prompts the user to enter an answer for a question on addition of two single digits. Using a loop, you can now rewrite the program to let the user repeatedly enter a new answer until it is correct, as shown in Listing 5.1.

**LISTING 5.1  RepeatAdditionQuiz.java**

```java
import java.util.Scanner;

public class RepeatAdditionQuiz {
    public static void main(String[] args) {
        int number1 = (int)(Math.random() * 10);
        int number2 = (int)(Math.random() * 10);
        // Create a Scanner
        Scanner input = new Scanner(System.in);
        System.out.print("What is "+ number1 +" + "+ number2 +"? ");
        int answer = input.nextInt();
        while (number1 + number2 != answer) {
            System.out.print("Wrong answer. Try again. What is "
                    + number1 +" + "+ number2 +"? ");
            answer = input.nextInt();
        }
        System.out.println("You got it!");
    }
}
```

```
What is 5 + 9? 12
Wrong answer. Try again. What is 5 + 9? 34
Wrong answer. Try again. What is 5 + 9? 14
You got it!
```
The loop in lines 15–19 repeatedly prompts the user to enter an answer when number1 + number2 != answer is true. Once number1 + number2 != answer is false, the loop exits.

5.2.1 Case Study: Guessing Numbers

The problem is to guess what number a computer has in mind. You will write a program that randomly generates an integer between 0 and 100, inclusive. The program prompts the user to enter a number continuously until the number matches the randomly generated number. For each user input, the program tells the user whether the input is too low or too high, so the user can make the next guess intelligently. Here is a sample run:

```
Guess a magic number between 0 and 100
Enter your guess: 50
Your guess is too high
Enter your guess: 25
Your guess is too low
Enter your guess: 42
Your guess is too high
Enter your guess: 39
Yes, the number is 39
```

The magic number is between 0 and 100. To minimize the number of guesses, enter 50 first. If your guess is too high, the magic number is between 0 and 49. If your guess is too low, the magic number is between 51 and 100. So, you can eliminate half of the numbers from further consideration after one guess.

How do you write this program? Do you immediately begin coding? No. It is important to think before coding. Think how you would solve the problem without writing a program. You need first to generate a random number between 0 and 100, inclusive, then to prompt the user to enter a guess, and then to compare the guess with the random number.

It is a good practice to code incrementally one step at a time. For programs involving loops, if you don’t know how to write a loop right away, you may first write the code for executing the loop one time, and then figure out how to repeatedly execute the code in a loop. For this program, you may create an initial draft, as shown in Listing 5.2.

```
import java.util.Scanner;

public class GuessNumberOneTime {
    public static void main(String[] args) {
        // Generate a random number to be guessed
        int number = (int)(Math.random() * 101);

        Scanner input = new Scanner(System.in);
        System.out.println("Guess a magic number between 0 and 100");

        // Prompt the user to guess the number
        System.out.print("\nEnter your guess: ");
        int guess = input.nextInt();

        if (guess == number)
            System.out.println("Yes, the number is "+ number);
    }
}
```
When you run this program, it prompts the user to enter a guess only once. To let the user enter a guess repeatedly, you may wrap the code in lines 11–20 in a loop as follows:

```java
while (true) {
    // Prompt the user to guess the number
    System.out.print("Enter your guess: ");
    guess = input.nextInt();
    if (guess == number)
        System.out.println("Yes, the number is " + number);
    else if (guess > number)
        System.out.println("Your guess is too high");
    else
        System.out.println("Your guess is too low");
} // End of loop
```

This loop repeatedly prompts the user to enter a guess. However, this loop is not correct, because it never terminates. When `guess` matches `number`, the loop should end. So, the loop can be revised as follows:

```java
while (guess != number) {
    // Prompt the user to guess the number
    System.out.print("Enter your guess: ");
    guess = input.nextInt();
    if (guess == number)
        System.out.println("Yes, the number is " + number);
    else if (guess > number)
        System.out.println("Your guess is too high");
    else
        System.out.println("Your guess is too low");
} // End of loop
```

The complete code is given in Listing 5.3.

**Listing 5.3 GuessNumber.java**

```java
import java.util.Scanner;

public class GuessNumber {
    public static void main(String[] args) {
        // Generate a random number to be guessed
        int number = (int)(Math.random() * 101);
        Scanner input = new Scanner(System.in);
        System.out.println("Guess a magic number between 0 and 100");
        int guess = -1;
        while (guess != number) {
            // Prompt the user to guess the number
            System.out.println("Enter your guess: ");
            guess = input.nextInt();
            if (guess == number)
                System.out.println("Yes, the number is " + number);
            else if (guess > number)
                System.out.println("Your guess is too high");
            else
                System.out.println("Your guess is too low");
        } // End of loop
    }
}
```
5.2 The **while** Loop

The program generates the magic number in line 6 and prompts the user to enter a guess continuously in a loop (lines 12–23). For each guess, the program checks whether the guess is correct, too high, or too low (lines 17–22). When the guess is correct, the program exits the loop (line 12). Note that `guess` is initialized to `-1`. Initializing it to a value between 0 and 100 would be wrong, because that could be the number to be guessed.

### 5.2.2 Loop Design Strategies

Writing a correct loop is not an easy task for novice programmers. Consider three steps when writing a loop.

1. **Step 1:** Identify the statements that need to be repeated.
2. **Step 2:** Wrap these statements in a loop like this:
   ```java
   while (true) {
       Statements;
   }
   ```
3. **Step 3:** Code the `loop-continuation-condition` and add appropriate statements for controlling the loop.
   ```java
   while (loop-continuation-condition) {
       Statements;
       Additional statements for controlling the loop;
   }
   ```

---

<table>
<thead>
<tr>
<th>line#</th>
<th>number</th>
<th>guess</th>
<th>output</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>39</td>
<td></td>
<td></td>
</tr>
<tr>
<td>11</td>
<td>-1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>15</td>
<td>50</td>
<td></td>
<td></td>
</tr>
<tr>
<td>20</td>
<td></td>
<td></td>
<td>Your guess is too high</td>
</tr>
<tr>
<td>15</td>
<td>25</td>
<td></td>
<td>Your guess is too low</td>
</tr>
<tr>
<td>22</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>15</td>
<td>42</td>
<td></td>
<td>Your guess is too low</td>
</tr>
<tr>
<td>20</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>15</td>
<td>39</td>
<td></td>
<td>Yes, the number is 39</td>
</tr>
<tr>
<td>18</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
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Loops

5.2.3
VideoNote

Multiple subtraction quiz

Case Study: Multiple Subtraction Quiz

The Math subtraction learning tool program in Listing 3.3, SubtractionQuiz.java, generates just
one question for each run. You can use a loop to generate questions repeatedly. How do you
write the code to generate five questions? Follow the loop design strategy. First identify the
statements that need to be repeated. These are the statements for obtaining two random numbers,
prompting the user with a subtraction question, and grading the question. Second, wrap the statements in a loop. Third, add a loop control variable and the loop-continuation-condition
to execute the loop five times.
Listing 5.4 gives a program that generates five questions and, after a student answers all
five, reports the number of correct answers. The program also displays the time spent on the
test and lists all the questions.

LISTING 5.4 SubtractionQuizLoop.java

get start time

loop

display a question

grade an answer
increase correct count

increase control variable
prepare output

1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21
22
23
24
25
26
27
28
29
30
31
32
33
34
35
36
37
38
39
40
41
42

import java.util.Scanner;
public class SubtractionQuizLoop {
public static void main(String[] args) {
final int NUMBER_OF_QUESTIONS = 5; // Number of questions
int correctCount = 0; // Count the number of correct answers
int count = 0; // Count the number of questions
long startTime = System.currentTimeMillis();
String output = " "; // output string is initially empty
Scanner input = new Scanner(System.in);
while (count < NUMBER_OF_QUESTIONS) {
// 1. Generate two random single-digit integers
int number1 = (int)(Math.random() * 10);
int number2 = (int)(Math.random() * 10);
// 2. If number1 < number2, swap number1 with number2
if (number1 < number2) {
int temp = number1;
number1 = number2;
number2 = temp;
}
// 3. Prompt the student to answer "What is number1 – number2?"
System.out.print(
"What is " + number1 + " - " + number2 + "? ");
int answer = input.nextInt();
// 4. Grade the answer and display the result
if (number1 - number2 == answer) {
System.out.println("You are correct!");
correctCount++; // Increase the correct answer count
}
else
System.out.println("Your answer is wrong.\n" + number1
+ " - " + number2 + " should be " + (number1 - number2));
// Increase the question count
count++;
output += "\n" + number1 + "-" + number2 + "=" + answer +
((number1 - number2 == answer) ? " correct" : " wrong");


What is 9 – 2? 7
You are correct!
What is 3 – 0? 3
You are correct!
What is 3 – 2? 1
You are correct!
What is 7 – 4? 4
Your answer is wrong.
7 – 4 should be 3
What is 7 – 5? 4
Your answer is wrong.
7 – 5 should be 2
Correct count is 3
Test time is 1021 seconds
9–2=7 correct
3–0=3 correct
3–2=1 correct
7–4=4 wrong
7–5=4 wrong

The program uses the control variable count to control the execution of the loop. count is initially 0 (line 7) and is increased by 1 in each iteration (line 39). A subtraction question is displayed and processed in each iteration. The program obtains the time before the test starts in line 8 and the time after the test ends in line 45, and computes the test time in line 46. The test time is in milliseconds and is converted to seconds in line 49.

5.2.4 Controlling a Loop with a Sentinel Value

Another common technique for controlling a loop is to designate a special value when reading and processing a set of values. This special input value, known as a sentinel value, signifies the end of the input. A loop that uses a sentinel value to control its execution is called a sentinel-controlled loop.

Listing 5.5 writes a program that reads and calculates the sum of an unspecified number of integers. The input 0 signifies the end of the input. Do you need to declare a new variable for each input value? No. Just use one variable named data (line 12) to store the input value and use a variable named sum (line 15) to store the total. Whenever a value is read, assign it to data and, if it is not zero, add it to sum (line 17).
**Listing 5.5 SentinelValue.java**

```java
import java.util.Scanner;

public class SentinelValue {

    // Main method
    public static void main(String[] args) {
        // Create a Scanner
        Scanner input = new Scanner(System.in);

        // Read an initial data
        System.out.print("Enter an integer (the input ends if it is 0): ");
        int data = input.nextInt();

        // Keep reading data until the input is 0
        int sum = 0;
        while (data != 0) {
            sum += data;
            System.out.print("Enter an integer (the input ends if it is 0): ");
            data = input.nextInt();
        }

        // Display the result
        System.out.println("The sum is "+sum);
    }
}
```

<table>
<thead>
<tr>
<th>line#</th>
<th>Data</th>
<th>sum</th>
<th>output</th>
</tr>
</thead>
<tbody>
<tr>
<td>12</td>
<td>2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>15</td>
<td></td>
<td>0</td>
<td></td>
</tr>
<tr>
<td>17</td>
<td>2</td>
<td></td>
<td></td>
</tr>
<tr>
<td>22</td>
<td>3</td>
<td></td>
<td></td>
</tr>
<tr>
<td>17</td>
<td>2</td>
<td>5</td>
<td></td>
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<td>22</td>
<td>4</td>
<td></td>
<td></td>
</tr>
<tr>
<td>17</td>
<td>2</td>
<td>9</td>
<td></td>
</tr>
<tr>
<td>22</td>
<td>0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>25</td>
<td></td>
<td></td>
<td>The sum is 9</td>
</tr>
</tbody>
</table>

If `data` is not `0`, it is added to `sum` (line 17) and the next item of input data is read (lines 20–22). If `data` is `0`, the loop body is no longer executed and the `while` loop terminates. The input value `0` is the sentinel value for this loop. Note that if the first input read is `0`, the loop body never executes, and the resulting sum is `0`.
**Caution**
Don’t use floating-point values for equality checking in a loop control. Because floating-point values are approximations for some values, using them could result in imprecise counter values and inaccurate results.

Consider the following code for computing \(1 + 0.9 + 0.8 + \ldots + 0.1\):

```java
double item = 1; double sum = 0;
while (item != 0) { // No guarantee item will be 0
    sum += item;
    item -= 0.1;
}
System.out.println(sum);
```

Variable \(item\) starts with 1 and is reduced by 0.1 every time the loop body is executed. The loop should terminate when \(item\) becomes 0. However, there is no guarantee that \(item\) will be exactly 0, because the floating-point arithmetic is approximated. This loop seems okay on the surface, but it is actually an infinite loop.

---

### 5.2.5 Input and Output Redirections

In the preceding example, if you have a large number of data to enter, it would be cumbersome to type from the keyboard. You can store the data separated by whitespaces in a text file, say **input.txt**, and run the program using the following command:

```
java SentinelValue < input.txt
```

This command is called **input redirection**. The program takes the input from the file **input.txt** rather than having the user type the data from the keyboard at runtime. Suppose the contents of the file are

```
2 3 4 5 6 7 8 9 12 23 32
23 45 67 89 92 12 34 35 3 1 2 4 0
```

The program should get **sum** to be 518.

Similarly, there is **output redirection**, which sends the output to a file rather than displaying it on the console. The command for output redirection is:

```
java ClassName > output.txt
```

Input and output redirection can be used in the same command. For example, the following command gets input from **input.txt** and sends output to **output.txt**:

```
java SentinelValue output.txt
```

Try running the program to see what contents are in **output.txt**.

### 5.1

Analyze the following code. Is \(\text{count} < 100\) always **true**, always **false**, or sometimes **true** or sometimes **false** at Point A, Point B, and Point C?

```java
int count = 0;
while (count < 100) {
    // Point A
    System.out.println("Welcome to Java!");
    count++;
    // Point B
}
// Point C
```
Chapter 5  Loops

5.2 What is wrong if `guess` is initialized to 0 in line 11 in Listing 5.3?

5.3 How many times are the following loop bodies repeated? What is the output of each loop?

(a) `int i = 1; while (i < 10) if (i % 2 == 0) System.out.println(i);`

(b) `int i = 1; while (i < 10) if (i % 2 == 0) System.out.println(i++);`

(c) `int i = 1; while (i < 10) if ((i++) % 2 == 0) System.out.println(i);`

5.4 Suppose the input is 2 3 4 5 0. What is the output of the following code?

```java
import java.util.Scanner;

public class Test {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        int number, max;
        number = input.nextInt();
        max = number;
        while (number != 0) {
            number = input.nextInt();
            if (number > max)
                max = number;
        }
        System.out.println("max is " + max);
        System.out.println("number " + number);
    }
}
```

5.5 What is the output of the following code? Explain the reason.

```java
int x = 80000000;
while (x > 0)
x++;
System.out.println("x is " + x);
```

5.3 The do-while Loop

A do-while loop is the same as a while loop except that it executes the loop body first and then checks the loop continuation condition.

The do-while loop is a variation of the while loop. Its syntax is:

```java
do {
    // Loop body;
    Statement(s);
} while (loop-continuation-condition);
```

Its execution flowchart is shown in Figure 5.2.

The loop body is executed first, and then the loop-continuation-condition is evaluated. If the evaluation is true, the loop body is executed again; if it is false, the do-while
loop terminates. The difference between a **while** loop and a **do-while** loop is the order in which the **loop-continuation-condition** is evaluated and the loop body executed. You can write a loop using either the **while** loop or the **do-while** loop. Sometimes one is a more convenient choice than the other. For example, you can rewrite the **while** loop in Listing 5.5 using a **do-while** loop, as shown in Listing 5.6.

**LISTING 5.6 TestDoWhile.java**

```java
import java.util.Scanner;

public class TestDoWhile {
  public static void main(String[] args) {
    int data;
    int sum = 0;

    // Create a Scanner
    Scanner input = new Scanner(System.in);

    // Keep reading data until the input is 0
    do {
      // Read the next data
      System.out.print("Enter an integer (the input ends if it is 0): ");
      data = input.nextInt();
      sum += data;
    } while (data != 0);

    System.out.println("The sum is "+ sum);
  }
}
```

Enter an integer (the input ends if it is 0): 3
Enter an integer (the input ends if it is 0): 5
Enter an integer (the input ends if it is 0): 6
Enter an integer (the input ends if it is 0): 0
The sum is 14
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Tip
Use a do-while loop if you have statements inside the loop that must be executed at least once, as in the case of the do-while loop in the preceding TestDoWhile program. These statements must appear before the loop as well as inside it if you use a while loop.

5.6 Suppose the input is 2 3 4 5 0. What is the output of the following code?

```java
import java.util.Scanner;

public class Test {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        int number, max;
        number = input.nextInt();
        max = number;
        do {
            number = input.nextInt();
            if (number > max)
                max = number;
        } while (number != 0);
        System.out.println("max is " + max);
        System.out.println("number " + number);
    }
}
```

5.7 What are the differences between a while loop and a do-while loop? Convert the following while loop into a do-while loop.

```java
Scanner input = new Scanner(System.in);
int sum = 0;
System.out.println("Enter an integer " + "(the input ends if it is 0)");
int number = input.nextInt();
while (number != 0) {
    sum += number;
    System.out.println("Enter an integer " + "(the input ends if it is 0)");
    number = input.nextInt();
}
```

5.4 The for Loop

A for loop has a concise syntax for writing loops.

Often you write a loop in the following common form:

```java
i = initialValue;  // Initialize loop control variable
while (i < endValue)
    // Loop body
    ...
    i++;  // Adjust loop control variable
```
A **for** loop can be used to simplify the preceding loop as:

```java
for (i = initialValue; i < endValue; i++)
// Loop body
...
}
```

In general, the syntax of a **for** loop is:

```java
for (initial-action; loop-continuation-condition; action-after-each-iteration) {
// Loop body;
Statement(s);
}
```

The flowchart of the **for** loop is shown in Figure 5.3a.

**Figure 5.3** A **for** loop performs an initial action once, then repeatedly executes the statements in the loop body, and performs an action after an iteration when the **loop-continuation-condition** evaluates to **true**.

The **for** loop statement starts with the keyword **for**, followed by a pair of parentheses enclosing the control structure of the loop. This structure consists of **initial-action**, **loop-continuation-condition**, and **action-after-each-iteration**. The control structure is followed by the loop body enclosed inside braces. The **initial-action**, **loop-continuation-condition**, and **action-after-each-iteration** are separated by semicolons.

A **for** loop generally uses a variable to control how many times the loop body is executed and when the loop terminates. This variable is referred to as a **control variable**. The **initial-action** often initializes a control variable, the **action-after-each-iteration** usually increments or decrements the control variable, and the **loop-continuation-condition** keeps track of whether the loop should continue.
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tests whether the control variable has reached a termination value. For example, the following for loop prints Welcome to Java! a hundred times:

```java
int i;
for (i = 0; i < 100; i++) {
    System.out.println("Welcome to Java!");
}
```

The flowchart of the statement is shown in Figure 5.3b. The for loop initializes i to 0, then repeatedly executes the println statement and evaluates i++ while i is less than 100.

The initial-action, i = 0, initializes the control variable, i. The loop-continuation-condition, i < 100, is a Boolean expression. The expression is evaluated right after the initialization and at the beginning of each iteration. If this condition is true, the loop body is executed. If it is false, the loop terminates and the program control turns to the line following the loop.

The action-after-each-iteration, i++, is a statement that adjusts the control variable. This statement is executed after each iteration and increments the control variable. Eventually, the value of the control variable should force the loop-continuation-condition to become false; otherwise, the loop is infinite.

The loop control variable can be declared and initialized in the for loop. Here is an example:

```java
for (int i = 0; i < 100; i++) {
    System.out.println("Welcome to Java!");
}
```

If there is only one statement in the loop body, as in this example, the braces can be omitted.

**Tip**
The control variable must be declared inside the control structure of the loop or before the loop. If the loop control variable is used only in the loop, and not elsewhere, it is a good programming practice to declare it in the initial-action of the for loop. If the variable is declared inside the loop control structure, it cannot be referenced outside the loop. In the preceding code, for example, you cannot reference i outside the for loop, because it is declared inside the for loop.

**Note**
The initial-action in a for loop can be a list of zero or more comma-separated variable declaration statements or assignment expressions. For example:

```java
for (int i = 0, j = 0; i + j < 10; i++, j++) {
    // Do something
}
```

The action-after-each-iteration in a for loop can be a list of zero or more comma-separated statements. For example:

```java
for (int i = 1; i < 100; System.out.println(i), i++);
```

This example is correct, but it is a bad example, because it makes the code difficult to read. Normally, you declare and initialize a control variable as an initial action and increment or decrement the control variable as an action after each iteration.

**Note**
If the loop-continuation-condition in a for loop is omitted, it is implicitly true. Thus the statement given below in (a), which is an infinite loop, is the same as in (b). To avoid confusion, though, it is better to use the equivalent loop in (c).
5.8 Do the following two loops result in the same value in \texttt{sum}?

\begin{verbatim}
for (int i = 0; i < 10; ++i) {
    sum += i;
}
\end{verbatim}

\begin{verbatim}
for (int i = 0; i < 10; i++) {
    sum += i;
}
\end{verbatim}

\(\checkmark\) "Point"

5.9 What are the three parts of a \texttt{for} loop control? Write a \texttt{for} loop that prints the numbers from 1 to 100.

5.10 Suppose the input is 2 3 4 5 0. What is the output of the following code?

```java
import java.util.Scanner;

public class Test {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        int number, sum = 0, count;
        for (count = 0; count < 5; count++) {
            number = input.nextInt();
            sum += number;
        }
        System.out.println("sum is " + sum);
        System.out.println("count is " + count);
    }
}
```

5.11 What does the following statement do?

```java
for (; ; ) {
    // Do something
}
```

5.12 If a variable is declared in a \texttt{for} loop control, can it be used after the loop exits?

5.13 Convert the following \texttt{for} loop statement to a \texttt{while} loop and to a \texttt{do-while} loop:

```java
long sum = 0;
for (int i = 0; i <= 1000; i++)
    sum = sum + i;
```

5.14 Count the number of iterations in the following loops.

\begin{verbatim}
int count = 0;
while (count < n) {
    count++;
}
\end{verbatim}

\begin{verbatim}
for (int count = 0; count <= n; count++) {
}
\end{verbatim}
5.5 Which Loop to Use?

You can use a for loop, a while loop, or a do-while loop, whichever is convenient.

The while loop and for loop are called pretest loops because the continuation condition is checked before the loop body is executed. The do-while loop is called a posttest loop because the condition is checked after the loop body is executed. The three forms of loop statements—while, do-while, and for—are expressively equivalent; that is, you can write a loop in any of these three forms. For example, a while loop in (a) in the following figure can always be converted into the for loop in (b).

```
while (loop-continuation-condition) {
    // Loop body
}
```

(a) Equivalent
```
for ( ; loop-continuation-condition; ) {
    // Loop body
}
```

(b)

A for loop in (a) in the next figure can generally be converted into the while loop in (b) except in certain special cases (see Checkpoint Question 5.25 for such a case).

```
for (initial-action;
    loop-continuation-condition;
    action-after-each-iteration) {
    // Loop body;
}
```

(a) Equivalent
```
initial-action;
while (loop-continuation-condition) {
    // Loop body;
    action-after-each-iteration;
}
```

(b)

Use the loop statement that is most intuitive and comfortable for you. In general, a for loop may be used if the number of repetitions is known in advance, as, for example, when you need to display a message a hundred times. A while loop may be used if the number of repetitions is not fixed, as in the case of reading the numbers until the input is 0. A do-while loop can be used to replace a while loop if the loop body has to be executed before the continuation condition is tested.

Caution

Adding a semicolon at the end of the for clause before the loop body is a common mistake, as shown below in (a). In (a), the semicolon signifies the end of the loop prematurely. The loop body is actually empty, as shown in (b). (a) and (b) are equivalent. Both are incorrect.

```
for (int i = 0; i < 10; i++) {
    System.out.println("i is " + i);
}
```

(a)
```
for (int i = 0; i < 10; i++) {
    ;
    System.out.println("i is " + i);
}
```

(b)
Similarly, the loop in (c) is also wrong. (c) is equivalent to (d). Both are incorrect.

```
int i = 0;
while (i < 10) {
    System.out.println("i is "+i);
    i++;
}
```

(c)

```
int i = 0;
while (i < 10) { };
{
    System.out.println("i is "+i);
    i++;
}
```

(d)

These errors often occur when you use the next-line block style. Using the end-of-line block style can avoid errors of this type.

In the case of the `do-while` loop, the semicolon is needed to end the loop.

```
int i = 0;
do {
    System.out.println("i is "+i);
    i++;
} while (i < 10);
```

Correct

5.15 Can you convert a `for` loop to a `while` loop? List the advantages of using `for` loops.

5.16 Can you always convert a `while` loop into a `for` loop? Convert the following `while` loop into a `for` loop.

```
int i = 1;
int sum = 0;
while (sum < 10000) {
    sum = sum + i;
    i++;
}
```

5.17 Identify and fix the errors in the following code:

```
public class Test {
    public void main(String[] args) {
        for (int i = 0; i < 10; i++){
            sum += i;
        }
        if (i < j);
        System.out.println(i);
        else
            System.out.println(j);
        while (j < 10);
        {
            j++;
        }
        do {
            j++;
        } while (j < 10)
    }
}
```
5.18 What is wrong with the following programs?

(a)```java
public class ShowErrors {
    public static void main(String[] args) {
        int i = 0;
        do {
            System.out.println(i + 4);
            i++;
        } while (i < 10)
    }
}
```(b)```java
public class ShowErrors {
    public static void main(String[] args) {
        for (int i = 0; i < 10; i++) {
            System.out.println(i + 4);
        }
    }
}
```

5.6 Nested Loops

A loop can be nested inside another loop.

Nested loops consist of an outer loop and one or more inner loops. Each time the outer loop is repeated, the inner loops are reentered, and started anew.

Listing 5.7 presents a program that uses nested for loops to display a multiplication table.

**Listing 5.7 MultiplicationTable.java**

```java
public class MultiplicationTable {
    /** Main method */
    public static void main(String[] args) {
        // Display the table heading
        System.out.println("Multiplication Table");
        // Display the number title
        System.out.print("    ");
        for (int j = 1; j <= 9; j++)
            System.out.print("   "+j);
        System.out.println("n——————————————————————————————————————————";
        for (int i = 1; i <= 9; i++) {
            // Display the product and align properly
            System.out.printf("%4d", i * j);
        }
    }
}
```

```
<table>
<thead>
<tr>
<th>Multiplication Table</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
</tr>
<tr>
<td>----------------------</td>
</tr>
<tr>
<td>1</td>
</tr>
<tr>
<td>2</td>
</tr>
<tr>
<td>3</td>
</tr>
<tr>
<td>4</td>
</tr>
<tr>
<td>5</td>
</tr>
<tr>
<td>6</td>
</tr>
<tr>
<td>7</td>
</tr>
<tr>
<td>8</td>
</tr>
<tr>
<td>9</td>
</tr>
</tbody>
</table>
```
The program displays a title (line 5) on the first line in the output. The first `for` loop (lines 9–10) displays the numbers 1 through 9 on the second line. A dashed (–) line is displayed on the third line (line 12).

The next loop (lines 15–22) is a nested `for` loop with the control variable `i` in the outer loop and `j` in the inner loop. For each `i`, the product `i * j` is displayed on a line in the inner loop, with `j` being 1, 2, 3, ..., 9.

**Note**

Be aware that a nested loop may take a long time to run. Consider the following loop nested in three levels:

```java
for (int i = 0; i < 10000; i++)
    for (int j = 0; j < 10000; j++)
        for (int k = 0; k < 10000; k++)
            Perform an action
```

The action is performed one trillion times. If it takes 1 microsecond to perform the action, the total time to run the loop would be more than 277 hours. Note that 1 microsecond is one millionth (10⁻⁶) of a second.

5.19 How many times is the `println` statement executed?

```java
for (int i = 0; i < 10; i++)
    for (int j = 0; j < i; j++)
        System.out.println(i * j)
```

5.20 Show the output of the following programs. (*Hint:* Draw a table and list the variables in the columns to trace these programs.)

```java
public class Test {
    public static void main(String[] args) {
        for (int i = 1; i < 5; i++) {
            int j = 0;
            while (j < i) {
                System.out.print(j + " ");
                j++;
            }
        }
    }
}
```

```
public class Test {
    public static void main(String[] args) {
        int i = 0;
        while (i < 5) {
            for (int j = i; j > 1; j--)
                System.out.print(j + " ");
            System.out.println("****");
            i++;
        }
    }
}
```

```
public class Test {
    public static void main(String[] args) {
        int i = 5;
        while (i >= 1) {
            int num = 1;
            for (int j = 1; j <= i; j++) {
                System.out.print(num + "xxx");
                num *= 2;
            }
            System.out.println();
            i--;
        }
    }
}
```

```
public class Test {
    public static void main(String[] args) {
        int i = 1;
        do {
            int num = 1;
            for (int j = 1; j <= i; j++) {
                System.out.print(num + "G");
                num += 2;
            }
            System.out.println();
            i++;
        } while (i <= 5);
    }
}
```
5.7 Minimizing Numeric Errors

Using floating-point numbers in the loop continuation condition may cause numeric errors.

Numeric errors involving floating-point numbers are inevitable, because floating-point numbers are represented in approximation in computers by nature. This section discusses how to minimize such errors through an example.

Listing 5.8 presents an example summing a series that starts with 0.01 and ends with 1.0. The numbers in the series will increment by 0.01, as follows: 0.01 + 0.02 + 0.03, and so on.

Listing 5.8 TestSum.java

```java
public class TestSum {
    public static void main(String[] args) {
        // Initialize sum
        float sum = 0;

        // Add 0.01, 0.02, ..., 0.99, 1 to sum
        for (float i = 0.01f; i <= 1.0f; i = i + 0.01f)
            sum += i;

        // Display result
        System.out.println("The sum is " + sum);
    }
}
```

The sum is 50.499985

The for loop (lines 7–8) repeatedly adds the control variable i to sum. This variable, which begins with 0.01, is incremented by 0.01 after each iteration. The loop terminates when i exceeds 1.0.

The for loop initial action can be any statement, but it is often used to initialize a control variable. From this example, you can see that a control variable can be a float type. In fact, it can be any data type.

The exact sum should be 50.50, but the answer is 50.499985. The result is imprecise because computers use a fixed number of bits to represent floating-point numbers, and thus they cannot represent some floating-point numbers exactly. If you change float in the program to double, as follows, you should see a slight improvement in precision, because a double variable holds 64 bits, whereas a float variable holds 32 bits.

```java
// Initialize sum
double sum = 0;

// Add 0.01, 0.02, ..., 0.99, 1 to sum
for (double i = 0.01; i <= 1.0; i = i + 0.01)
    sum += i;
```

However, you will be stunned to see that the result is actually 49.50000000000003. What went wrong? If you display i for each iteration in the loop, you will see that the last i is slightly larger than 1 (not exactly 1). This causes the last i not to be added into sum. The fundamental problem is that the floating-point numbers are represented by approximation. To fix the problem, use an integer count to ensure that all the numbers are added to sum. Here is the new loop:

```java
double currentValue = 0.01;

for (int count = 0; count < 100; count++) {
    sum += currentValue;
```

Key Point

Minimize numeric errors

VideoNote

Minimize numeric errors

 numeric error
5.8 Case Studies

Loops are fundamental in programming. The ability to write loops is essential in learning Java programming.

If you can write programs using loops, you know how to program! For this reason, this section presents four additional examples of solving problems using loops.

5.8.1 Case Study: Finding the Greatest Common Divisor

The greatest common divisor (gcd) of the two integers 4 and 2 is 2. The greatest common divisor of the two integers 16 and 24 is 8. How would you write this program to find the greatest common divisor? Would you immediately begin to write the code? No. It is important to think before you code. Thinking enables you to generate a logical solution for the problem without concern about how to write the code.

Let the two input integers be n1 and n2. You know that number 1 is a common divisor, but it may not be the greatest common divisor. So, you can check whether k (for k = 2, 3, 4, and so on) is a common divisor for n1 and n2, until k is greater than n1 or n2. Store the common divisor in a variable named gcd. Initially, gcd is 1. Whenever a new common divisor is found, it becomes the new gcd. When you have checked all the possible common divisors from 2 up to n1 or n2, the value in variable gcd is the greatest common divisor. Once you have a logical solution, type the code to translate the solution into a Java program as follows:

```java
int gcd = 1; // Initial gcd is 1
int k = 2; // Possible gcd

while (k <= n1 && k <= n2) {
    if (n1 % k == 0 && n2 % k == 0) {
        gcd = k; // Update gcd
        k++; // Next possible gcd
    }
}

// After the loop, gcd is the greatest common divisor for n1 and n2
```

Listing 5.9 presents the program that prompts the user to enter two positive integers and finds their greatest common divisor.

5.8.2 Case Study: Summing a Sequence of Numbers

After this loop, sum is 50.50000000000003. This loop adds the numbers from smallest to biggest. What happens if you add numbers from biggest to smallest (i.e., 1.0, 0.99, 0.98, . . . , 0.02, 0.01 in this order) as follows:

```java
double currentValue = 1.0;

for (int count = 0; count < 100; count++) {
    sum += currentValue;
    currentValue -= 0.01;
}
```

After this loop, sum is 50.49999999999995. Adding from biggest to smallest is less accurate than adding from smallest to biggest. This phenomenon is an artifact of the finite-precision arithmetic. Adding a very small number to a very big number can have no effect if the result requires more precision than the variable can store. For example, the inaccurate result of 100000000.0 + 0.000000001 is 100000000.0. To obtain more accurate results, carefully select the order of computation. Adding smaller numbers before bigger numbers is one way to minimize errors.

5.8.3 Case Study: Finding the Greatest Common Divisor

The greatest common divisor (gcd) of the two integers 4 and 2 is 2. The greatest common divisor of the two integers 16 and 24 is 8. How would you write this program to find the greatest common divisor? Would you immediately begin to write the code? No. It is important to think before you code. Thinking enables you to generate a logical solution for the problem without concern about how to write the code.

Let the two input integers be n1 and n2. You know that number 1 is a common divisor, but it may not be the greatest common divisor. So, you can check whether k (for k = 2, 3, 4, and so on) is a common divisor for n1 and n2, until k is greater than n1 or n2. Store the common divisor in a variable named gcd. Initially, gcd is 1. Whenever a new common divisor is found, it becomes the new gcd. When you have checked all the possible common divisors from 2 up to n1 or n2, the value in variable gcd is the greatest common divisor. Once you have a logical solution, type the code to translate the solution into a Java program as follows:

```java
int gcd = 1; // Initial gcd is 1
int k = 2; // Possible gcd

while (k <= n1 && k <= n2) {
    if (n1 % k == 0 && n2 % k == 0) {
        gcd = k; // Update gcd
        k++; // Next possible gcd
    }
}

// After the loop, gcd is the greatest common divisor for n1 and n2
```

Listing 5.9 presents the program that prompts the user to enter two positive integers and finds their greatest common divisor.
LISTING 5.9 GreatestCommonDivisor.java

```java
import java.util.Scanner;

public class GreatestCommonDivisor {
    public static void main(String[] args) {
        System.out.print("Enter first integer: ");
        int n1 = input.nextInt();
        System.out.print("Enter second integer: ");
        int n2 = input.nextInt();

        int gcd = 1; // Initial gcd is 1
        int k = 2; // Possible gcd
        while (k <= n1 && k <= n2) {
            if (n1 % k == 0 && n2 % k == 0) {
                gcd = k; // Update gcd
                k++;
            }
        }

        System.out.println("The greatest common divisor for "+ n1 + " and "+ n2 + " is "+ gcd);
    }
}
```

Enter first integer: 125  
Enter second integer: 2525  
The greatest common divisor for 125 and 2525 is 25

Translating a logical solution to Java code is not unique. For example, you could use a `for` loop to rewrite the code as follows:

```java
for (int k = 2; k <= n1 && k <= n2; k++) {
    if (n1 % k == 0 && n2 % k == 0) {
        gcd = k;
    }
}
```

A problem often has multiple solutions, and the gcd problem can be solved in many ways. Programming Exercise 5.14 suggests another solution. A more efficient solution is to use the classic Euclidean algorithm (see Section 22.6).

You might think that a divisor for a number `n1` cannot be greater than `n1 / 2` and would attempt to improve the program using the following loop:

```java
for (int k = 2; k <= n1 / 2 && k <= n2 / 2; k++) {
    if (n1 % k == 0 && n2 % k == 0) {
        gcd = k;
    }
}
```
This revision is wrong. Can you find the reason? See Checkpoint Question 5.21 for the answer.

### 5.8.2 Case Study: Predicting the Future Tuition

Suppose that the tuition for a university is $10,000 this year and tuition increases 7% every year. In how many years will the tuition be doubled?

Before you can write a program to solve this problem, first consider how to solve it by hand. The tuition for the second year is the tuition for the first year * 1.07. The tuition for a future year is the tuition of its preceding year * 1.07. Thus, the tuition for each year can be computed as follows:

```java
    double tuition = 10000;  // Year 0
    int year = 0; // Year 0
    tuition = tuition * 1.07; // Year 1
    tuition = tuition * 1.07; // Year 2
    tuition = tuition * 1.07; // Year 3
    ...
```

Keep computing the tuition for a new year until it is at least $20000. By then you will know how many years it will take for the tuition to be doubled. You can now translate the logic into the following loop:

```java
    double tuition = 10000; // Year 0
    int year = 0;
    while (tuition < 20000) {
        tuition = tuition * 1.07;
        year++;
    }
```

The complete program is shown in Listing 5.10.

### Listing 5.10 FutureTuition.java

```java
public class FutureTuition {
    public static void main(String[] args) {
        double tuition = 10000; // Year 0
        int year = 0;
        while (tuition < 20000) {
            tuition = tuition * 1.07;
            year++;
        }
        System.out.println("Tuition will be doubled in " + year + " years");
        System.out.printf("Tuition will be $%.2f in %1d years", tuition, year);
    }
}
```

The **while** loop (lines 5–8) is used to repeatedly compute the tuition for a new year. The loop terminates when the tuition is greater than or equal to 20000.
5.8.3 Case Study: Converting Decimals to Hexadecimals

Hexadecimals are often used in computer systems programming (see Appendix F for an introduction to number systems). How do you convert a decimal number to a hexadecimal number? To convert a decimal number \(d\) to a hexadecimal number is to find the hexadecimal digits \(h_n, h_{n-1}, h_{n-2}, \ldots, h_1, h_0\) such that

\[
d = h_n \times 16^n + h_{n-1} \times 16^{n-1} + h_{n-2} \times 16^{n-2} + \cdots + h_2 \times 16^2 + h_1 \times 16^1 + h_0 \times 16^0
\]

These hexadecimal digits can be found by successively dividing \(d\) by 16 until the quotient is 0. The remainders are \(h_0, h_1, h_2, \ldots, h_{n-2}, h_{n-1},\) and \(h_n\). The hexadecimal digits include the decimal digits 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9, plus A, which is the decimal value 10; B, which is the decimal value 11; C, which is 12; D, which is 13; E, which is 14; and F, which is 15.

For example, the decimal number 123 is \(7B\) in hexadecimal. The conversion is done as follows. Divide 123 by 16. The remainder is 11 (\(B\) in hexadecimal) and the quotient is 7. Continue divide 7 by 16. The remainder is 7 and the quotient is 0. Therefore \(7B\) is the hexadecimal number for 123.

Listing 5.11 gives a program that prompts the user to enter a decimal number and converts it into a hex number as a string.

**Listing 5.11  Dec2Hex.java**

```java
import java.util.Scanner;

public class Dec2Hex {
    /** Main method */
    public static void main(String[] args) {
        // Create a Scanner
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter a decimal integer
        System.out.print("Enter a decimal number: ");
        int decimal = input.nextInt();

        // Convert decimal to hex
        String hex = "";

        while (decimal != 0) {
            int hexValue = decimal % 16;

            // Convert a decimal value to a hex digit
            char hexDigit = (hexValue <= 9 && hexValue >= 0) ? (char)(hexValue + '0') : (char)(hexValue - 10 + 'A');
            hex = hexDigit + hex;

            System.out.print(hex);
            decimal = decimal / 16;
        }
    }
}
```
The program prompts the user to enter a decimal integer (line 11), converts it to a hex number as a string (lines 14–25), and displays the result (line 27). To convert a decimal to a hex number, the program uses a loop to successively divide the decimal number by 16 and obtain its remainder (line 17). The remainder is converted into a hex character (lines 20–21). The character is then appended to the hex string (line 23). The hex string is initially empty (line 14). Divide the decimal number by 16 to remove a hex digit from the number (line 24). The loop ends when the remaining decimal number becomes 0.

The program converts a hexValue between 0 and 15 into a hex character. If hexValue is between 0 and 9, it is converted to (char)(hexValue + '0') (line 21). Recall that when adding a character with an integer, the character’s Unicode is used in the evaluation. For example, if hexValue is 5, (char)(hexValue + '0') returns 5. Similarly, if hexValue is between 10 and 15, it is converted to (char)(hexValue - 10 + 'A') (line 21). For instance, if hexValue is 11, (char)(hexValue - 10 + 'A') returns B.

5.21 Will the program work if n1 and n2 are replaced by n1 / 2 and n2 / 2 in line 17 in Listing 5.9?

5.22 In Listing 5.11, why is it wrong if you change the code (char)(hexValue + '0') to hexValue + '0' in line 21?

5.23 In Listing 5.11, how many times the loop body is executed for a decimal number 245 and how many times the loop body is executed for a decimal number 3245?
5.9 Keywords **break** and **continue**

The **break** and **continue** keywords provide additional controls in a loop.

**Pedagogical Note**

Two keywords, **break** and **continue**, can be used in loop statements to provide additional controls. Using **break** and **continue** can simplify programming in some cases. Overusing or improperly using them, however, can make programs difficult to read and debug. *(Note to instructors: You may skip this section without affecting students' understanding of the rest of the book.)*

**break statement**

You have used the keyword **break** in a **switch** statement. You can also use **break** in a loop to immediately terminate the loop. Listing 5.12 presents a program to demonstrate the effect of using **break** in a loop.

**Listing 5.12  TestBreak.java**

```java
1  public class TestBreak {
2      public static void main(String[] args) {
3          int sum = 0;
4          int number = 0;
5          while (number < 20) {
6              number++;
7              sum += number;
8              if (sum >= 100)
9                  break;
10          }
11          System.out.println("The number is " + number);
12          System.out.println("The sum is " + sum);
13      }
14  }
```

The number is 14
The sum is 105

The program in Listing 5.12 adds integers from 1 to 20 in this order to **sum** until **sum** is greater than or equal to 100. Without the **if** statement (line 9), the program calculates the sum of the numbers from 1 to 20. But with the **if** statement, the loop terminates when **sum** becomes greater than or equal to 100. Without the **if** statement, the output would be:

The number is 20
The sum is 210

**continue statement**

You can also use the **continue** keyword in a loop. When it is encountered, it ends the current iteration and program control goes to the end of the loop body. In other words, **continue** breaks out of an iteration while the **break** keyword breaks out of a loop. Listing 5.13 presents a program to demonstrate the effect of using **continue** in a loop.

**Listing 5.13  TestContinue.java**

```java
1  public class TestContinue {
2      public static void main(String[] args) {
3          int sum = 0;
```
```java
4    int number = 0;
5    while (number < 20) {
6        number++;
7        if (number == 10 || number == 11)
8            continue;  // continue
9        sum += number;
10    }
11    System.out.println("The sum is " + sum);
12 }
13 }
```

The sum is 189

The program in Listing 5.13 adds integers from 1 to 20 except 10 and 11 to sum. With the if statement in the program (line 8), the continue statement is executed when number becomes 10 or 11. The continue statement ends the current iteration so that the rest of the statement in the loop body is not executed; therefore, number is not added to sum when it is 10 or 11. Without the if statement in the program, the output would be as follows:

The sum is 210

In this case, all of the numbers are added to sum, even when number is 10 or 11. Therefore, the result is 210, which is 21 more than it was with the if statement.

Note
The continue statement is always inside a loop. In the while and do-while loops, the loop-continuation-condition is evaluated immediately after the continue statement. In the for loop, the action-after-each-iteration is performed, then the loop-continuation-condition is evaluated, immediately after the continue statement.

You can always write a program without using break or continue in a loop (see Checkpoint Question 5.26). In general, though, using break and continue is appropriate if it simplifies coding and makes programs easier to read.

Suppose you need to write a program to find the smallest factor other than 1 for an integer n (assume n >= 2). You can write a simple and intuitive code using the break statement as follows:

```java
int factor = 2;
while (factor <= n) {
    if (n % factor == 0)
        break;
    factor++;
} System.out.println("The smallest factor other than 1 for " + n + " is " + factor);
```

You may rewrite the code without using break as follows:

```java
boolean found = false;
int factor = 2;
while (factor <= n && !found) {
    if (n % factor == 0) {
```

5.9 Keywords break and continue 185
Chapter 5  Loops

```java
found = true;
else
    factor++;
}
System.out.println("The smallest factor other than 1 for " + n + " is " + factor);
```

Obviously, the `break` statement makes this program simpler and easier to read in this case. However, you should use `break` and `continue` with caution. Too many `break` and `continue` statements will produce a loop with many exit points and make the program difficult to read.

**Note**

Some programming languages have a `goto` statement. The `goto` statement indiscriminately transfers control to any statement in the program and executes it. This makes your program vulnerable to errors. The `break` and `continue` statements in Java are different from `goto` statements. They operate only in a loop or a `switch` statement. The `break` statement breaks out of the loop, and the `continue` statement breaks out of the current iteration in the loop.

**Note**

Programming is a creative endeavor. There are many different ways to write code. In fact, you can find a smallest factor using a rather simple code as follows:

```java
int factor = 2;
while (factor <= n && n % factor != 0)
    factor++;
```

### 5.24

What is the keyword `break` for? What is the keyword `continue` for? Will the following programs terminate? If so, give the output.

(a)

```java
int balance = 10;
while (true) {
    if (balance < 9)
        break;
    balance = balance - 9;
}
System.out.println("Balance is " + balance);
```

(b)

```java
int balance = 10;
while (true) {
    if (balance < 9)
        continue;
    balance = balance - 9;
}
System.out.println("Balance is " + balance);
```

### 5.25

The `for` loop on the left is converted into the `while` loop on the right. What is wrong? Correct it.

```java
int sum = 0;
for (int i = 0; i < 4; i++) {
    if (i % 3 == 0) continue;
    sum += 1;
}
```

### 5.26

Rewrite the programs `TestBreak` and `TestContinue` in Listings 5.12 and 5.13 without using `break` and `continue`. 
5.27 After the **break** statement in (a) is executed in the following loop, which statement is executed? Show the output. After the **continue** statement in (b) is executed in the following loop, which statement is executed? Show the output.

```java
for (int i = 1; i < 4; i++) {
    for (int j = 1; j < 4; j++) {
        if (i * j > 2)
            break;
        System.out.println(i * j);
    }
    System.out.println(i);
}
```

(a)

```java
for (int i = 1; i < 4; i++) {
    for (int j = 1; j < 4; j++) {
        if (i * j > 2)
            continue;
        System.out.println(i * j);
    }
    System.out.println(i);
}
```

(b)

5.10 Case Study: Checking Palindromes

*This section presents a program that checks whether a string is a palindrome.*

A string is a palindrome if it reads the same forward and backward. The words “mom,” “dad,” and “noon,” for instance, are all palindromes.

The problem is to write a program that prompts the user to enter a string and reports whether the string is a palindrome. One solution is to check whether the first character in the string is the same as the last character. If so, check whether the second character is the same as the second-to-last character. This process continues until a mismatch is found or all the characters in the string are checked, except for the middle character if the string has an odd number of characters.

Listing 5.14 gives the program.

**Listing 5.14** Palindrome.java

```java
import java.util.Scanner;

public class Palindrome {

    /** Main method */
    public static void main(String[] args) {
        // Create a Scanner
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter a string
        System.out.print("Enter a string: ");
        String s = input.nextLine();

        // The index of the first character in the string
        int low = 0;

        // The index of the last character in the string
        int high = s.length() - 1;

        boolean isPalindrome = true;
        while (low < high) {
            if (s.charAt(low) != s.charAt(high)) {
                isPalindrome = false;
                break;
            }
            low++;
            high--;
        }

        if (isPalindrome) {
            System.out.println("The string is a palindrome.");
        } else {
            System.out.println("The string is not a palindrome.");
        }
    }
}
```
update indices

```java
26    low++;  
27    high--;  
28 }
29
30 if (isPalindrome)
31 System.out.println(s + " is a palindrome");
32 else
33 System.out.println(s + " is not a palindrome");
34 }
35 }
```

Enter a string: noon
noon is a palindrome

Enter a string: moon
moon is not a palindrome

The program uses two variables, low and high, to denote the position of the two characters at the beginning and the end in a string s (lines 14, 17). Initially, low is 0 and high is s.length() - 1. If the two characters at these positions match, increment low by 1 and decrement high by 1 (lines 26–27). This process continues until (low >= high) or a mismatch is found (line 21).

The program uses a boolean variable isPalindrome to denote whether the string s is palindrome. Initially, it is set to true (line 19). When a mismatch is discovered (line 21), isPalindrome is to false (line 22) and the loop is terminated with a break statement (line 23).

5.11 Case Study: Displaying Prime Numbers

This section presents a program that displays the first fifty prime numbers in five lines, each containing ten numbers.

An integer greater than 1 is prime if its only positive divisor is 1 or itself. For example, 2, 3, 5, and 7 are prime numbers, but 4, 6, 8, and 9 are not.

The problem is to display the first 50 prime numbers in five lines, each of which contains ten numbers. The problem can be broken into the following tasks:

- Determine whether a given number is prime.
- For number = 2, 3, 4, 5, 6, ..., test whether it is prime.
- Count the prime numbers.
- Display each prime number, and display ten numbers per line.

Obviously, you need to write a loop and repeatedly test whether a new number is prime. If the number is prime, increase the count by 1. The count is 0 initially. When it reaches 50, the loop terminates.

Here is the algorithm for the problem:

Set the number of prime numbers to be printed as a constant NUMBER_OF_PRIMES;
Use count to track the number of prime numbers and set an initial count to 0;
Set an initial number to 2;
while (count < NUMBER_OF_PRIMES) {
    Test whether number is prime;

    if number is prime {
        Display the prime number and increase the count;
    }

    Increment number by 1;
}

To test whether a number is prime, check whether it is divisible by 2, 3, 4, and so on up to number/2. If a divisor is found, the number is not a prime. The algorithm can be described as follows:

Use a boolean variable isPrime to denote whether the number is prime; Set isPrime to true initially;

for (int divisor = 2; divisor <= number / 2; divisor++) {
    if (number % divisor == 0) {
        Set isPrime to false
        Exit the loop;
    }
}

The complete program is given in Listing 5.15.

**Listing 5.15  PrimeNumber.java**

```java
public class PrimeNumber {
    public static void main(String[] args) {
        final int NUMBER_OF_PRIMES = 50; // Number of primes to display
        final int NUMBER_OF_PRIMES_PER_LINE = 10; // Display 10 per line
        int count = 0; // Count the number of prime numbers
        int number = 2; // A number to be tested for primeness

        System.out.println("The first 50 prime numbers are 
");

        // Repeatedly find prime numbers
        while (count < NUMBER_OF_PRIMES) {
            // Assume the number is prime
            boolean isPrime = true; // Is the current number prime?

            // Test whether number is prime
            for (int divisor = 2; divisor <= number / 2; divisor++) {
                if (number % divisor == 0) { // If true, number is not prime
                    isPrime = false; // Set isPrime to false
                    break; // Exit the for loop
                }
            }

            // Display the prime number and increase the count
            if (isPrime) {
                count++; // Increase the count

                if (count % NUMBER_OF_PRIMES_PER_LINE == 0) {
                    // Display the number and advance to the new line
                    System.out.println(number);
                } else
                    System.out.print(number + " ");
        }
    }
}
```
The first 50 prime numbers are
2 3 5 7 11 13 17 19 23 29
31 37 41 43 47 53 59 61 67 71
73 79 83 89 97 101 103 107 109 113
127 131 137 139 149 151 157 163 167 173
179 181 191 193 197 199 211 223 227 229

This is a complex program for novice programmers. The key to developing a programmatic solution for this problem, and for many other problems, is to break it into subproblems and develop solutions for each of them in turn. Do not attempt to develop a complete solution in the first trial. Instead, begin by writing the code to determine whether a given number is prime, then expand the program to test whether other numbers are prime in a loop.

To determine whether a number is prime, check whether it is divisible by a number between 2 and number/2 inclusive (lines 16–21). If so, it is not a prime number (line 18); otherwise, it is a prime number. For a prime number, display it. If the count is divisible by 10 (lines 27–30), advance to a new line. The program ends when the count reaches 50.

The program uses the break statement in line 19 to exit the for loop as soon as the number is found to be a nonprime. You can rewrite the loop (lines 16–21) without using the break statement, as follows:

```c
for (int divisor = 2; divisor <= number / 2 && isPrime; divisor++) {
    // If true, the number is not prime
    if (number % divisor == 0) {
        // Set isPrime to false, if the number is not prime
        isPrime = false;
    }
}
```

However, using the break statement makes the program simpler and easier to read in this case.

**Key Terms**

- break statement 184
- continue statement 184
- do-while loop 168
- for loop 171
- infinite loop 160
- input redirection 167
- iteration 158
- loop 158
- loop body 158
- nested loop 176
- off-by-one error 160
- output redirection 167
- posttest loop 174
- pretest loop 174
- sentinel value 165
- while loop 158
CHAPTER SUMMARY

1. There are three types of repetition statements: the while loop, the do-while loop, and the for loop.

2. The part of the loop that contains the statements to be repeated is called the loop body.

3. A one-time execution of a loop body is referred to as an iteration of the loop.

4. An infinite loop is a loop statement that executes infinitely.

5. In designing loops, you need to consider both the loop control structure and the loop body.

6. The while loop checks the loop-continuation-condition first. If the condition is true, the loop body is executed; if it is false, the loop terminates.

7. The do-while loop is similar to the while loop, except that the do-while loop executes the loop body first and then checks the loop-continuation-condition to decide whether to continue or to terminate.

8. The while loop and the do-while loop often are used when the number of repetitions is not predetermined.

9. A sentinel value is a special value that signifies the end of the loop.

10. The for loop generally is used to execute a loop body a fixed number of times.

11. The for loop control has three parts. The first part is an initial action that often initializes a control variable. The second part, the loop-continuation-condition, determines whether the loop body is to be executed. The third part is executed after each iteration and is often used to adjust the control variable. Usually, the loop control variables are initialized and changed in the control structure.

12. The while loop and for loop are called pretest loops because the continuation condition is checked before the loop body is executed.

13. The do-while loop is called a posttest loop because the condition is checked after the loop body is executed.

14. Two keywords, break and continue, can be used in a loop.

15. The break keyword immediately ends the innermost loop, which contains the break.

16. The continue keyword only ends the current iteration.

Quiz

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

Programming Exercises

Pedagogical Note
Read each problem several times until you understand it. Think how to solve the problem before starting to write code. Translate your logic into a program.

A problem often can be solved in many different ways. Students are encouraged to explore various solutions.
Sections 5.2–5.7

*5.1 (Count positive and negative numbers and compute the average of numbers) Write a program that reads an unspecified number of integers, determines how many positive and negative values have been read, and computes the total and average of the input values (not counting zeros). Your program ends with the input 0. Display the average as a floating-point number. Here is a sample run:

Enter an integer, the input ends if it is 0: 1 2 -1 3 0
The number of positives is 3
The number of negatives is 1
The total is 5.0
The average is 1.25

Enter an integer, the input ends if it is 0: 0
No numbers are entered except 0

5.2 (Repeat additions) Listing 5.4, SubtractionQuizLoop.java, generates five random subtraction questions. Revise the program to generate ten random addition questions for two integers between 1 and 15. Display the correct count and test time.

5.3 (Conversion from kilograms to pounds) Write a program that displays the following table (note that 1 kilogram is 2.2 pounds):

<table>
<thead>
<tr>
<th>Kilograms</th>
<th>Pounds</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2.2</td>
</tr>
<tr>
<td>3</td>
<td>6.6</td>
</tr>
<tr>
<td>...</td>
<td></td>
</tr>
<tr>
<td>197</td>
<td>433.4</td>
</tr>
<tr>
<td>199</td>
<td>437.8</td>
</tr>
</tbody>
</table>

5.4 (Conversion from miles to kilometers) Write a program that displays the following table (note that 1 mile is 1.609 kilometers):

<table>
<thead>
<tr>
<th>Miles</th>
<th>Kilometers</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1.609</td>
</tr>
<tr>
<td>2</td>
<td>3.218</td>
</tr>
<tr>
<td>...</td>
<td></td>
</tr>
<tr>
<td>9</td>
<td>14.481</td>
</tr>
<tr>
<td>10</td>
<td>16.090</td>
</tr>
</tbody>
</table>

5.5 (Conversion from kilograms to pounds and pounds to kilograms) Write a program that displays the following two tables side by side:

<table>
<thead>
<tr>
<th>Kilograms</th>
<th>Pounds</th>
<th>Kilograms</th>
<th>Pounds</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2.2</td>
<td>20</td>
<td>9.09</td>
</tr>
<tr>
<td>3</td>
<td>6.6</td>
<td>25</td>
<td>11.36</td>
</tr>
<tr>
<td>...</td>
<td></td>
<td>...</td>
<td></td>
</tr>
<tr>
<td>197</td>
<td>433.4</td>
<td>510</td>
<td>231.82</td>
</tr>
<tr>
<td>199</td>
<td>437.8</td>
<td>515</td>
<td>234.09</td>
</tr>
</tbody>
</table>

5.6 (Conversion from miles to kilometers) Write a program that displays the following two tables side by side:
### 5.7 (Financial application: compute future tuition)
Suppose that the tuition for a university is $10,000 this year and increases 5% every year. In one year, the tuition will be $10,500. Write a program that computes the tuition in ten years and the total cost of four years’ worth of tuition after the tenth year.

### 5.8 (Find the highest score)
Write a program that prompts the user to enter the number of students and each student’s name and score, and finally displays the name of the student with the highest score.

### 5.9 (Find the two highest scores)
Write a program that prompts the user to enter the number of students and each student’s name and score, and finally displays the student with the highest score and the student with the second-highest score.

### 5.10 (Find numbers divisible by 5 and 6)
Write a program that displays all the numbers from 100 to 1,000, ten per line, that are divisible by 5 and 6. Numbers are separated by exactly one space.

### 5.11 (Find numbers divisible by 5 or 6, but not both)
Write a program that displays all the numbers from 100 to 200, ten per line, that are divisible by 5 or 6, but not both. Numbers are separated by exactly one space.

### 5.12 (Find the smallest \( n \) such that \( n^2 > 12,000 \))
Use a `while` loop to find the smallest integer \( n \) such that \( n^2 \) is greater than 12,000.

### 5.13 (Find the largest \( n \) such that \( n^3 < 12,000 \))
Use a `while` loop to find the largest integer \( n \) such that \( n^3 \) is less than 12,000.

#### Sections 5.8–5.10

### 5.14 (Compute the greatest common divisor)
Another solution for Listing 5.9 to find the greatest common divisor of two integers \( n1 \) and \( n2 \) is as follows: First find \( d \) to be the minimum of \( n1 \) and \( n2 \), then check whether \( d, d-1, d-2, \ldots, 2, \) or 1 is a divisor for both \( n1 \) and \( n2 \) in this order. The first such common divisor is the greatest common divisor for \( n1 \) and \( n2 \). Write a program that prompts the user to enter two positive integers and displays the gcd.

### 5.15 (Display the ASCII character table)
Write a program that prints the characters in the ASCII character table from 1 to ~. Display ten characters per line. The ASCII table is shown in Appendix B. Characters are separated by exactly one space.

### 5.16 (Find the factors of an integer)
Write a program that reads an integer and displays all its smallest factors in increasing order. For example, if the input integer is 120, the output should be as follows: 2, 2, 2, 3, 5.

### 5.17 (Display pyramid)
Write a program that prompts the user to enter an integer from 1 to 15 and displays a pyramid, as shown in the following sample run:
5.18 (Display four patterns using loops) Use nested loops that display the following patterns in four separate programs:

<table>
<thead>
<tr>
<th>Pattern A</th>
<th>Pattern B</th>
<th>Pattern C</th>
<th>Pattern D</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1 2 3 4 5 6</td>
<td>1</td>
<td>1 2 3 4 5 6</td>
</tr>
<tr>
<td>1 2</td>
<td>1 2 3 4 5</td>
<td>2 1</td>
<td>1 2 3 4 5</td>
</tr>
<tr>
<td>1 2 3</td>
<td>1 2 3 4</td>
<td>3 2 1</td>
<td>1 2 3 4</td>
</tr>
<tr>
<td>1 2 3 4</td>
<td>1 2 3</td>
<td>4 3 2 1</td>
<td>1 2 3</td>
</tr>
<tr>
<td>1 2 3 4 5</td>
<td>1 2</td>
<td>5 4 3 2 1</td>
<td>1 2</td>
</tr>
<tr>
<td>1 2 3 4 5 6</td>
<td>1</td>
<td>6 5 4 3 2 1</td>
<td>1</td>
</tr>
</tbody>
</table>

5.19 (Display numbers in a pyramid pattern) Write a nested for loop that prints the following output:

```
    1
   1 2 1
  1 2 4 2 1
 1 2 4 8 4 2 1
1 2 4 8 16 8 4 2 1
1 2 4 8 16 32 16 8 4 2 1
1 2 4 8 16 32 64 32 16 8 4 2 1
1 2 4 8 16 32 64 128 64 32 16 8 4 2 1
```

5.20 (Display prime numbers between 2 and 1,000) Modify Listing 5.15 to display all the prime numbers between 2 and 1,000, inclusive. Display eight prime numbers per line. Numbers are separated by exactly one space.

Comprehensive

5.21 (Financial application: compare loans with various interest rates) Write a program that lets the user enter the loan amount and loan period in number of years and displays the monthly and total payments for each interest rate starting from 5% to 8%, with an increment of 1/8. Here is a sample run:

```
Loan Amount: 10000
Number of Years: 5

Interest Rate: 5.000%  Monthly Payment: 188.71  Total Payment: 11322.74
Interest Rate: 5.125%  Monthly Payment: 189.29  Total Payment: 11357.13
Interest Rate: 5.250%  Monthly Payment: 189.86  Total Payment: 11391.59
...  
Interest Rate: 7.875%  Monthly Payment: 202.17  Total Payment: 12129.97
Interest Rate: 8.000%  Monthly Payment: 202.76  Total Payment: 12165.84
```

For the formula to compute monthly payment, see Listing 2.9, ComputeLoan.java.

5.22 (Financial application: loan amortization schedule) The monthly payment for a given loan pays the principal and the interest. The monthly interest is computed by multiplying the monthly interest rate and the balance (the remaining principal). The principal paid for the month is therefore the monthly payment minus the monthly interest. Write a program that lets the user enter the loan amount,
number of years, and interest rate and displays the amortization schedule for the loan. Here is a sample run:

```
Loan Amount: 10000
Number of Years: 1
Annual Interest Rate: 7

Monthly Payment: 865.26
Total Payment: 10383.21

<table>
<thead>
<tr>
<th>Payment#</th>
<th>Interest</th>
<th>Principal</th>
<th>Balance</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>58.33</td>
<td>806.93</td>
<td>9193.07</td>
</tr>
<tr>
<td>2</td>
<td>53.62</td>
<td>811.64</td>
<td>8381.43</td>
</tr>
<tr>
<td>...</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>11</td>
<td>10.0</td>
<td>855.26</td>
<td>860.27</td>
</tr>
<tr>
<td>12</td>
<td>5.01</td>
<td>860.25</td>
<td>0.01</td>
</tr>
</tbody>
</table>
```

**Note**

The balance after the last payment may not be zero. If so, the last payment should be the normal monthly payment plus the final balance.

**Hint:** Write a loop to display the table. Since the monthly payment is the same for each month, it should be computed before the loop. The balance is initially the loan amount. For each iteration in the loop, compute the interest and principal, and update the balance. The loop may look like this:

```java
for (i = 1; i <= numberOfYears * 12; i++) {
    interest = monthlyInterestRate * balance;
    principal = monthlyPayment - interest;
    balance = balance - principal;
    System.out.println(i + "	" + interest + "	" + principal + "	" + balance);
}
```

*5.23* *(Demonstrate cancellation errors)* A cancellation error occurs when you are manipulating a very large number with a very small number. The large number may cancel out the smaller number. For example, the result of \(100000000.0 + 0.000000001\) is equal to \(100000000.0\). To avoid cancellation errors and obtain more accurate results, carefully select the order of computation. For example, in computing the following series, you will obtain more accurate results by computing from right to left rather than from left to right:

\[
1 + \frac{1}{2} + \frac{1}{3} + \ldots + \frac{1}{n}
\]

Write a program that compares the results of the summation of the preceding series, computing from left to right and from right to left with \(n = 50000\).

*5.24* *(Sum a series)* Write a program to sum the following series:

\[
\frac{1}{3} + \frac{3}{5} + \frac{5}{7} + \frac{7}{9} + \frac{9}{11} + \frac{11}{13} + \ldots + \frac{95}{97} + \frac{97}{99}
\]
**5.25 (Compute \( \pi \)) You can approximate \( \pi \) by using the following series:

\[
\pi = 4 \left( 1 - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \frac{1}{9} - \frac{1}{11} + \cdots + \frac{(-1)^{i+1}}{2i - 1} \right)
\]

Write a program that displays the \( \pi \) value for \( i = 10000, 20000, \ldots \), and \( 100000 \).

**5.26 (Compute \( e \)) You can approximate \( e \) using the following series:

\[
e = 1 + \frac{1}{1!} + \frac{1}{2!} + \frac{1}{3!} + \frac{1}{4!} + \cdots + \frac{1}{i!}
\]

Write a program that displays the \( e \) value for \( i = 10000, 20000, \ldots \), and \( 100000 \). (Hint: Because \( i! = i \times (i - 1) \times \ldots \times 2 \times 1 \), then

\[
\frac{1}{i!} \text{ is } \frac{1}{i(i - 1)!}
\]

Initialize \( e \) and item to be 1 and keep adding a new item to \( e \). The new item is the previous item divided by \( i \) for \( i = 2, 3, 4, \ldots \.).

**5.27 (Display leap years) Write a program that displays all the leap years, ten per line, from 101 to 2100, separated by exactly one space. Also display the number of leap years in this period.

**5.28 (Display the first days of each month) Write a program that prompts the user to enter the year and first day of the year, and displays the first day of each month in the year. For example, if the user entered the year 2013, and 2 for Tuesday, January 1, 2013, your program should display the following output:

January 1, 2013 is Tuesday

... 

December 1, 2013 is Sunday

**5.29 (Display calendars) Write a program that prompts the user to enter the year and first day of the year and displays the calendar table for the year on the console. For example, if the user entered the year 2013, and 2 for Tuesday, January 1, 2013, your program should display the calendar for each month in the year, as follows:

<table>
<thead>
<tr>
<th>January 2013</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sun</td>
</tr>
<tr>
<td>1</td>
</tr>
<tr>
<td>8</td>
</tr>
<tr>
<td>15</td>
</tr>
<tr>
<td>22</td>
</tr>
<tr>
<td>29</td>
</tr>
</tbody>
</table>
*5.30  (Financial application: compound value) Suppose you save $100 each month into a savings account with the annual interest rate 5%. So, the monthly interest rate is $0.05 / 12 = 0.00417$. After the first month, the value in the account becomes

$$100 \times (1 + 0.00417) = 100.417$$

After the second month, the value in the account becomes

$$(100 + 100.417) \times (1 + 0.00417) = 201.252$$

After the third month, the value in the account becomes

$$(100 + 201.252) \times (1 + 0.00417) = 302.507$$

and so on.

Write a program that prompts the user to enter an amount (e.g., 100), the annual interest rate (e.g., 5), and the number of months (e.g., 6) and displays the amount in the savings account after the given month.

*5.31  (Financial application: compute CD value) Suppose you put $10,000 into a CD with an annual percentage yield of 5.75%. After one month, the CD is worth

$$10000 + 10000 \times 5.75 / 1200 = 10047.92$$

After two months, the CD is worth

$$10047.91 + 10047.91 \times 5.75 / 1200 = 10096.06$$

After three months, the CD is worth

$$10096.06 + 10096.06 \times 5.75 / 1200 = 10144.44$$

and so on.

Write a program that prompts the user to enter an amount (e.g., 10000), the annual percentage yield (e.g., 5.75), and the number of months (e.g., 18) and displays a table as shown in the sample run.
**5.32** (Game: lottery) Revise Listing 3.8, Lottery.java, to generate a lottery of a two-digit number. The two digits in the number are distinct. (*Hint*: Generate the first digit. Use a loop to continuously generate the second digit until it is different from the first digit.)

**5.33** (Perfect number) A positive integer is called a *perfect number* if it is equal to the sum of all of its positive divisors, excluding itself. For example, 6 is the first perfect number because $6 = 3 + 2 + 1$. The next is $28 = 14 + 7 + 4 + 2 + 1$. There are four perfect numbers less than 10,000. Write a program to find all these four numbers.

**5.34** (Game: scissor, rock, paper) Programming Exercise 3.17 gives a program that plays the scissor-rock-paper game. Revise the program to let the user continuously play until either the user or the computer wins more than two times than its opponent.

**5.35** (Summation) Write a program to compute the following summation.

$$\frac{1}{1 + \sqrt{2}} + \frac{1}{\sqrt{2} + \sqrt{3}} + \frac{1}{\sqrt{3} + \sqrt{4}} + \ldots + \frac{1}{\sqrt{624} + \sqrt{625}}$$


**5.37** (Decimal to binary) Write a program that prompts the user to enter a decimal integer and displays its corresponding binary value. Don’t use Java’s `Integer.toBinaryString(int)` in this program.

**5.38** (Decimal to octal) Write a program that prompts the user to enter a decimal integer and displays its corresponding octal value. Don’t use Java’s `Integer.toOctalString(int)` in this program.

**5.39** (Financial application: find the sales amount) You have just started a sales job in a department store. Your pay consists of a base salary and a commission. The base salary is $5,000. The scheme shown below is used to determine the commission rate.

<table>
<thead>
<tr>
<th>Sales Amount</th>
<th>Commission Rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>$0.01–$5,000</td>
<td>8 percent</td>
</tr>
<tr>
<td>$5,000.01–$10,000</td>
<td>10 percent</td>
</tr>
<tr>
<td>$10,000.01 and above</td>
<td>12 percent</td>
</tr>
</tbody>
</table>

Note that this is a graduated rate. The rate for the first $5,000 is at 8%, the next $5000 is at 10%, and the rest is at 12%. If the sales amount is 25,000, the commission is $5,000 * 8% + 5,000 * 10% + 15,000 * 12% = 2,700.
Your goal is to earn $30,000 a year. Write a program that finds the minimum sales you have to generate in order to make $30,000.

**5.40** (Simulation: heads or tails) Write a program that simulates flipping a coin one million times and displays the number of heads and tails.

**5.41** (Occurrence of max numbers) Write a program that reads integers, finds the largest of them, and counts its occurrences. Assume that the input ends with number 0. Suppose that you entered 3 5 2 5 5 5 0; the program finds that the largest is 5 and the occurrence count for 5 is 4.

(Hint: Maintain two variables, max and count. max stores the current max number, and count stores its occurrences. Initially, assign the first number to max and 1 to count. Compare each subsequent number with max. If the number is greater than max, assign it to max and reset count to 1. If the number is equal to max, increment count by 1.)

```
Enter numbers: 3 5 2 5 5 5 0
The largest number is 5
The occurrence count of the largest number is 4
```

**5.42** (Financial application: find the sales amount) Rewrite Programming Exercise 5.39 as follows:

- Use a for loop instead of a do-while loop.
- Let the user enter COMMISSION_Sought instead of fixing it as a constant.

**5.43** (Math: combinations) Write a program that displays all possible combinations for picking two numbers from integers 1 to 7. Also display the total number of all combinations.

```
1 2
1 3
...
...

The total number of all combinations is 21
```

**5.44** (Computer architecture: bit-level operations) A short value is stored in 16 bits. Write a program that prompts the user to enter a short integer and displays the 16 bits for the integer. Here are sample runs:

```
Enter an integer: 5
The bits are 0000000000000101
```

```
Enter an integer: -5
The bits are 1111111111111011
```

(Hint: You need to use the bitwise right shift operator (>>) and the bitwise AND operator (&), which are covered in Appendix G, Bitwise Operations.)

**5.45** (Statistics: compute mean and standard deviation) In business applications, you are often asked to compute the mean and standard deviation of data. The mean is simply the average of the numbers. The standard deviation is a statistic that tells
you how tightly all the various data are clustered around the mean in a set of data. For example, what is the average age of the students in a class? How close are the ages? If all the students are the same age, the deviation is 0.

Write a program that prompts the user to enter ten numbers, and displays the mean and standard deviations of these numbers using the following formula:

\[
\text{mean} = \frac{\sum_{i=1}^{n} x_i}{n} = \frac{x_1 + x_2 + \cdots + x_n}{n}
\]

\[
\text{deviation} = \sqrt{\frac{\sum_{i=1}^{n} x_i^2 - \left( \frac{\sum_{i=1}^{n} x_i}{n} \right)^2}{n - 1}}
\]

Here is a sample run:

Enter ten numbers: 1 2 3 4.5 5.6 6 7 8 9 10
The mean is 5.61
The standard deviation is 2.99794

*5.46 (Reverse a string) Write a program that prompts the user to enter a string and displays the string in reverse order.

Enter a string: ABCD
The reversed string is DCBA

*5.47 (Business: check ISBN-13) ISBN-13 is a new standard for indentifying books. It uses 13 digits \(d_1d_2d_3d_4d_5d_6d_7d_8d_9d_{10}d_{11}d_{12}d_{13}\). The last digit \(d_{13}\) is a checksum, which is calculated from the other digits using the following formula:

\[
10 - (d_1 + 3d_2 + d_3 + 3d_4 + d_5 + 3d_6 + d_7 + 3d_8 + d_9 + 3d_{10} + d_{11} + 3d_{12}) \equiv 10
\]

If the checksum is 10, replace it with 0. Your program should read the input as a string. Here are sample runs:

Enter the first 12 digits of an ISBN-13 as a string: 978013213080
The ISBN-13 number is 9780132130806

Enter the first 12 digits of an ISBN-13 as a string: 978013213079
The ISBN-13 number is 9780132130790

Enter the first 12 digits of an ISBN-13 as a string: 97801320
97801320 is an invalid input

*5.48 (Process string) Write a program that prompts the user to enter a string and displays the characters at odd positions. Here is a sample run:

Enter a string: Beijing Chicago
BiigCiao
*5.49 (Count vowels and consonants) Assume letters A, E, I, O, and U as the vowels. Write a program that prompts the user to enter a string and displays the number of vowels and consonants in the string.

Enter a string: Programming is fun
The number of vowels is 5
The number of consonants is 11

*5.50 (Count uppercase letters) Write a program that prompts the user to enter a string and displays the number of the uppercase letters in the string.

Enter a string: Welcome to Java
The number of uppercase letters is 2

*5.51 (Longest common prefix) Write a program that prompts the user to enter two strings and displays the largest common prefix of the two strings. Here are some sample runs:

Enter the first string: Welcome to C++
Enter the second string: Welcome to programming
The common prefix is Welcome to

Enter the first string: Atlanta
Enter the second string: Macon
Atlanta and Macon have no common prefix
This page intentionally left blank
METHODS

Objectives
- To define methods with formal parameters (§6.2).
- To invoke methods with actual parameters (i.e., arguments) (§6.2).
- To define methods with a return value (§6.3).
- To define methods without a return value (§6.4).
- To pass arguments by value (§6.5).
- To develop reusable code that is modular, easy to read, easy to debug, and easy to maintain (§6.6).
- To write a method that converts hexadecimals to decimals (§6.7).
- To use method overloading and understand ambiguous overloading (§6.8).
- To determine the scope of variables (§6.9).
- To apply the concept of method abstraction in software development (§6.10).
- To design and implement methods using stepwise refinement (§6.10).
6.1 Introduction

Methods can be used to define reusable code and organize and simplify coding.

Suppose that you need to find the sum of integers from 1 to 10, from 20 to 37, and from 35 to 49, respectively. You may write the code as follows:

```java
int sum = 0;
for (int i = 1; i <= 10; i++)
    sum += i;
System.out.println("Sum from 1 to 10 is " + sum);

sum = 0;
for (int i = 20; i <= 37; i++)
    sum += i;
System.out.println("Sum from 20 to 37 is " + sum);

sum = 0;
for (int i = 35; i <= 49; i++)
    sum += i;
System.out.println("Sum from 35 to 49 is " + sum);
```

You may have observed that computing these sums from 1 to 10, from 20 to 37, and from 35 to 49 are very similar except that the starting and ending integers are different. Wouldn’t it be nice if we could write the common code once and reuse it? We can do so by defining a method and invoking it.

The preceding code can be simplified as follows:

```java
public static int sum(int i1, int i2) {
    int result = 0;
    for (int i = i1; i <= i2; i++)
        result += i;
    return result;
}
```

```java
public static void main(String[] args) {
    System.out.println("Sum from 1 to 10 is " + sum(1, 10));
    System.out.println("Sum from 20 to 37 is " + sum(20, 37));
    System.out.println("Sum from 35 to 49 is " + sum(35, 49));
}
```

Lines 1–7 define the method named `sum` with two parameters `i1` and `i2`. The statements in the `main` method invoke `sum(1, 10)` to compute the sum from 1 to 10, `sum(20, 37)` to compute the sum from 20 to 37, and `sum(35, 49)` to compute the sum from 35 to 49.

A method is a collection of statements grouped together to perform an operation. In earlier chapters you have used predefined methods such as `System.out.println`, `System.exit`, `Math.pow`, and `Math.random`. These methods are defined in the Java library. In this chapter, you will learn how to define your own methods and apply method abstraction to solve complex problems.

6.2 Defining a Method

A method definition consists of its method name, parameters, return value type, and body.

The syntax for defining a method is as follows:

```java
modifier returnType methodName(list of parameters) {
    // Method body;
}
```
Let's look at a method defined to find the larger between two integers. This method, named `max`, has two `int` parameters, `num1` and `num2`, the larger of which is returned by the method. Figure 6.1 illustrates the components of this method.

![Diagram](attachment:image.jpg)

**Figure 6.1** A method definition consists of a method header and a method body.

The method header specifies the modifiers, return value type, method name, and parameters of the method. The `static` modifier is used for all the methods in this chapter. The reason for using it will be discussed in Chapter 8, Objects and Classes.

A method may return a value. The `returnValueType` is the data type of the value the method returns. Some methods perform desired operations without returning a value. In this case, the `returnValueType` is the keyword `void`. For example, the `returnValueType` is `void` in the `main` method, as well as in `System.exit`, and `System.out.println`. If a method returns a value, it is called a value-returning method; otherwise it is called a void method.

The variables defined in the method header are known as formal parameters or simply parameters. A parameter is like a placeholder: when a method is invoked, you pass a value to the parameter. This value is referred to as an actual parameter or argument. The parameter list refers to the method’s type, order, and number of the parameters. The method name and the parameter list together constitute the method signature. Parameters are optional; that is, a method may contain no parameters. For example, the `Math.random()` method has no parameters.

The method body contains a collection of statements that implement the method. The method body of the `max` method uses an if statement to determine which number is larger and return the value of that number. In order for a value-returning method to return a result, a return statement using the keyword `return` is required. The method terminates when a return statement is executed.

**Note**
Some programming languages refer to methods as procedures and functions. In those languages, a value-returning method is called a function and a void method is called a procedure.

**Caution**
In the method header, you need to declare each parameter separately. For instance, `max(int num1, int num2)` is correct, but `max(int num1, num2)` is wrong.
Note
We say “define a method” and “declare a variable.” We are making a subtle distinction here. A definition defines what the defined item is, but a declaration usually involves allocating memory to store data for the declared item.

6.3 Calling a Method

Calling a method executes the code in the method.

In a method definition, you define what the method is to do. To execute the method, you have to call or invoke it. There are two ways to call a method, depending on whether the method returns a value or not.

If a method returns a value, a call to the method is usually treated as a value. For example,

```java
int larger = max(3, 4);
```

calls `max(3, 4)` and assigns the result of the method to the variable `larger`. Another example of a call that is treated as a value is

```java
System.out.println(max(3, 4));
```

which prints the return value of the method call `max(3, 4)`.

If a method returns `void`, a call to the method must be a statement. For example, the method `println` returns `void`. The following call is a statement:

```java
System.out.println("Welcome to Java!");
```

Note
A value-returning method can also be invoked as a statement in Java. In this case, the caller simply ignores the return value. This is not often done, but it is permissible if the caller is not interested in the return value.

When a program calls a method, program control is transferred to the called method. A called method returns control to the caller when its return statement is executed or when its method-ending closing brace is reached.

Listing 6.1 shows a complete program that is used to test the `max` method.

Listing 6.1  TestMax.java

```java
public class TestMax {
    // Main method
    public static void main(String[] args) {
        int i = 5;
        int j = 2;
        int k = max(i, j);
        System.out.println("The maximum of " + i + " and " + j + " is " + k);
    }

    // Return the max of two numbers
    public static int max(int num1, int num2) {
        int result;
        if (num1 > num2)
            result = num1;
        else
            result = num2;
        return result;
    }
}
```
This program contains the `main` method and the `max` method. The `main` method is just like any other method except that it is invoked by the JVM to start the program.

The `main` method’s header is always the same. Like the one in this example, it includes the modifiers `public` and `static`, return value type `void`, method name `main`, and a parameter of the `String[]` type. `String[]` indicates that the parameter is an array of `String`, a subject addressed in Chapter 7.

The statements in `main` may invoke other methods that are defined in the class that contains the `main` method or in other classes. In this example, the `main` method invokes `max(i, j)`, which is defined in the same class with the `main` method.

When the `max` method is invoked (line 6), variable `i`’s value 5 is passed to `num1`, and variable `j`’s value 2 is passed to `num2` in the `max` method. The flow of control transfers to the `max` method, and the `max` method is executed. When the return statement in the `max` method is executed, the `max` method returns the control to its caller (in this case the caller is the `main` method). This process is illustrated in Figure 6.2.

### Figure 6.2
When the `max` method is invoked, the flow of control transfers to it. Once the `max` method is finished, it returns control back to the caller.

**Caution**

A `return` statement is required for a value-returning method. The method shown below in (a) is logically correct, but it has a compile error because the Java compiler thinks that this method might not return a value.
Chapter 6 Methods

To fix this problem, delete `if (n < 0)` in (a), so the compiler will see a `return` statement to be reached regardless of how the `if` statement is evaluated.

**Note**
Methods enable code sharing and reuse. The `max` method can be invoked from any class, not just `TestMax`. If you create a new class, you can invoke the `max` method using `ClassName.methodName` (i.e., `TestMax.max`).

Each time a method is invoked, the system creates an *activation record* (also called an *activation frame*) that stores parameters and variables for the method and places the activation record in an area of memory known as a *call stack*. A call stack is also known as an *execution stack*, *runtime stack*, or *machine stack*, and it is often shortened to just “the stack.” When a method calls another method, the caller’s activation record is kept intact, and a new activation record is created for the new method called. When a method finishes its work and returns to its caller, its activation record is removed from the call stack.

A call stack stores the activation records in a last-in, first-out fashion: The activation record for the method that is invoked last is removed first from the stack. For example, suppose method `m1` calls method `m2`, and `m2` calls method `m3`. The runtime system pushes `m1`’s activation record into the stack, then `m2`’s, and then `m3`’s. After `m3` is finished, its activation record is removed from the stack. After `m2` is finished, its activation record is removed from the stack. After `m1` is finished, its activation record is removed from the stack.

Understanding call stacks helps you to comprehend how methods are invoked. The variables defined in the `main` method in Listing 6.1 are `i`, `j`, and `k`. The variables defined in the `max` method are `num1`, `num2`, and `result`. The variables `num1` and `num2` are defined in the method signature and are parameters of the `max` method. Their values are passed through method invocation. Figure 6.3 illustrates the activation records for method calls in the stack.

![Figure 6.3](image-url)

Figure 6.3 When the `max` method is invoked, the flow of control transfers to the `max` method. Once the `max` method is finished, it returns control back to the caller.
6.4 void Method Example

A void method does not return a value.

The preceding section gives an example of a value-returning method. This section shows how to define and invoke a void method. Listing 6.2 gives a program that defines a method named printGrade and invokes it to print the grade for a given score.

**LISTING 6.2 TestVoidMethod.java**

```java
public class TestVoidMethod {
    public static void main(String[] args) {
        System.out.print("The grade is ");
        printGrade(78.5);
        System.out.print("The grade is ");
        printGrade(59.5);
    }

    public static void printGrade(double score) {
        if (score >= 90.0) {
            System.out.println('A');
        } else if (score >= 80.0) {
            System.out.println('B');
        } else if (score >= 70.0) {
            System.out.println('C');
        } else if (score >= 60.0) {
            System.out.println('D');
        } else {
            System.out.println('F');
        }
    }
}
```

```
The grade is C
The grade is F
```

The printGrade method is a void method because it does not return any value. A call to a void method must be a statement. Therefore, it is invoked as a statement in line 4 in the main method. Like any Java statement, it is terminated with a semicolon.

To see the differences between a void and value-returning method, let’s redesign the printGrade method to return a value. The new method, which we call getGrade, returns the grade as shown in Listing 6.3.

**LISTING 6.3 TestReturnGradeMethod.java**

```java
public class TestReturnGradeMethod {
    public static void main(String[] args) {
        System.out.print("The grade is " + getGrade(78.5));
        System.out.print("The grade is " + getGrade(59.5));
    }
}
```

The void vs. value-returning method.
The `getGrade` method defined in lines 7–18 returns a character grade based on the numeric score value. The caller invokes this method in lines 3–4.

The `getGrade` method can be invoked by a caller wherever a character may appear. The `printGrade` method does not return any value, so it must be invoked as a statement.

### Note

A `return` statement is not needed for a `void` method, but it can be used for terminating the method and returning to the method’s caller. The syntax is simply

```java
return;
```

This is not often done, but sometimes it is useful for circumventing the normal flow of control in a `void` method. For example, the following code has a return statement to terminate the method when the score is invalid.

```java
public static void printGrade(double score) {
    if (score < 0 || score > 100) {
        System.out.println("Invalid score");
        return;
    }
    if (score >= 90.0) {
        System.out.println('A');
    } else if (score >= 80.0) {
        System.out.println('B');
    } else if (score >= 70.0) {
        System.out.println('C');
    } else if (score >= 60.0) {
        System.out.println('D');
    } else {
        System.out.println('F');
    }
}
```
6.1 What are the benefits of using a method?

6.2 How do you define a method? How do you invoke a method?

6.3 How do you simplify the **max** method in Listing 6.1 using the conditional operator?

6.4 True or false? A call to a method with a **void** return type is always a statement itself, but a call to a value-returning method cannot be a statement by itself.

6.5 What is the **return** type of a **main** method?

6.6 What would be wrong with not writing a **return** statement in a value-returning method? Can you have a **return** statement in a **void** method? Does the **return** statement in the following method cause syntax errors?

```java
public static void xMethod(double x, double y) {
    System.out.println(x + y);
```

6.7 Define the terms parameter, argument, and method signature.

6.8 Write method headers (not the bodies) for the following methods:
   a. Return a sales commission, given the sales amount and the commission rate.
   b. Display the calendar for a month, given the month and year.
   c. Return a square root of a number.
   d. Test whether a number is even, and returning **true** if it is.
   e. Display a message a specified number of times.
   f. Return the monthly payment, given the loan amount, number of years, and annual interest rate.
   g. Return the corresponding uppercase letter, given a lowercase letter.

6.9 Identify and correct the errors in the following program:

```
public class Test {
    public static method1(int n, m) {
        n += m;
        method2(3.4);
    }

    public static int method2(int n) {
        if (n > 0) return 1;
        else if (n == 0) return 0;
        else if (n < 0) return -1;
    }
}
```

6.10 Reformat the following program according to the programming style and documentation guidelines proposed in Section 1.9, Programming Style and Documentation. Use the next-line brace style.

```
public class Test {
    public static double method(double i, double j) {
        while (i < j) {
            j--;
        }
        return j;
    }
}
```
6.5 Passing Arguments by Values

The arguments are passed by value to parameters when invoking a method.

The power of a method is its ability to work with parameters. You can use `println` to print any string and `max` to find the maximum of any two `int` values. When calling a method, you need to provide arguments, which must be given in the same order as their respective parameters in the method signature. This is known as parameter order association. For example, the following method prints a message `n` times:

```java
public static void nPrintln(String message, int n) {
    for (int i = 0; i < n; i++)
        System.out.println(message);
}
```

You can use `nPrintln("Hello", 3)` to print `Hello` three times. The `nPrintln("Hello", 3)` statement passes the actual string parameter `Hello` to the parameter `message`, passes 3 to `n`, and prints `Hello` three times. However, the statement `nPrintln(3, "Hello")` would be wrong. The data type of 3 does not match the data type for the first parameter, `message`, nor does the second argument, `Hello`, match the second parameter, `n`.

**Caution**
The arguments must match the parameters in order, number, and compatible type, as defined in the method signature. Compatible type means that you can pass an argument to a parameter without explicit casting, such as passing an `int` value argument to a `double` value parameter.

When you invoke a method with an argument, the value of the argument is passed to the parameter. This is referred to as pass-by-value. If the argument is a variable rather than a literal value, the value of the variable is passed to the parameter. The variable is not affected, regardless of the changes made to the parameter inside the method. As shown in Listing 6.4, the value of `x` (1) is passed to the parameter `n` to invoke the `increment` method (line 5). The parameter `n` is incremented by 1 in the method (line 10), but `x` is not changed no matter what the method does.

**Listing 6.4 Increment.java**

```java
public class Increment {
    public static void main(String[] args) {
      int x = 1;
      System.out.println("Before the call, x is " + x);
      increment(x);
      System.out.println("After the call, x is " + x);
    }

    public static void increment(int n) {
      n++;
      System.out.println("n inside the method is " + n);
    }
}
```

<table>
<thead>
<tr>
<th>Before the call, x is 1</th>
</tr>
</thead>
<tbody>
<tr>
<td>n inside the method is 2</td>
</tr>
<tr>
<td>After the call, x is 1</td>
</tr>
</tbody>
</table>
Listing 6.5 gives another program that demonstrates the effect of passing by value. The program creates a method for swapping two variables. The `swap` method is invoked by passing two arguments. Interestingly, the values of the arguments are not changed after the method is invoked.

**Listing 6.5  TestPassByValue.java**

```java
public class TestPassByValue {
    /** Main method */
    public static void main(String[] args) {
        // Declare and initialize variables
        int num1 = 1;
        int num2 = 2;

        System.out.println("Before invoking the swap method, num1 is " +
                          num1 + " and num2 is " + num2);

        // Invoke the swap method to attempt to swap two variables
        swap(num1, num2);

        System.out.println("After invoking the swap method, num1 is " +
                          num1 + " and num2 is " + num2);
    }

    /** Swap two variables */
    public static void swap(int n1, int n2) {
        System.out.println("Inside the swap method");
        System.out.println("Before swapping, n1 is " + n1
                          + " and n2 is " + n2);

        // Swap n1 with n2
        int temp = n1;
        n1 = n2;
        n2 = temp;

        System.out.println("After swapping, n1 is " + n1
                          + " and n2 is " + n2);
    }
}
```

Before invoking the swap method, num1 is 1 and num2 is 2

Before the `swap` method is invoked (line 12), num1 is 1 and num2 is 2. After the `swap` method is invoked, num1 is still 1 and num2 is still 2. Their values have not been swapped. As shown in Figure 6.4, the values of the arguments num1 and num2 are passed to n1 and n2, but n1 and n2 have their own memory locations independent of num1 and num2. Therefore, changes in n1 and n2 do not affect the contents of num1 and num2.

Another twist is to change the parameter name n1 in `swap` to num1. What effect does this have? No change occurs, because it makes no difference whether the parameter and the argument have the same name. The parameter is a variable in the method with its own memory space. The variable is allocated when the method is invoked, and it disappears when the method is returned to its caller.
Chapter 6  Methods

Note
For simplicity, Java programmers often say passing \( x \) to \( y \), which actually means passing the value of argument \( x \) to parameter \( y \).

6.11 How is an argument passed to a method? Can the argument have the same name as its parameter?

6.12 Identify and correct the errors in the following program:

```java
public class Test {
    public static void main(String[] args) {
        nPrintln(5, "Welcome to Java!");
    }
    public static void nPrintln(String message, int n) {
        int n = 1;
        for (int i = 0; i < n; i++)
            System.out.println(message);
    }
}
```

6.13 What is pass-by-value? Show the result of the following programs.

```java
public class Test {
    public static void main(String[] args) {
        int max = 0;
        max(1, 2, max);
        System.out.println(max);
    }
    public static void max(int value1, int value2, int max) {
        if (value1 > value2)
            max = value1;
        else
            max = value2;
    }
}
```

(a)

```java
public class Test {
    public static void main(String[] args) {
        int i = 1;
        while (i <= 6) {
            method1(i, 2);
            i++;
        }
    }
    public static void method1(int i, int num) {
        for (int j = 1; j <= i; j++)
            System.out.println(num + " ");
        num *= 2;
    }
    System.out.println();
}
```

(b)
6.14 For (a) in the preceding question, show the contents of the activation records in the call stack just before the method max is invoked, just as max is entered, just before max is returned, and right after max is returned.

6.6 Modularizing Code

Modularizing makes the code easy to maintain and debug and enables the code to be reused.

Methods can be used to reduce redundant code and enable code reuse. Methods can also be used to modularize code and improve the quality of the program.

Listing 5.9 gives a program that prompts the user to enter two integers and displays their greatest common divisor. You can rewrite the program using a method, as shown in Listing 6.6.

Listing 6.6 GreatestCommonDivisorMethod.java

```java
public class GreatestCommonDivisorMethod {
    public static void main(String[] args) {
        // Initialize times
        int times = 3;
        System.out.println("Before the call," + " variable times is " + times);

        // Invoke nPrintln and display times
        nPrintln("Welcome to Java!", times);
        System.out.println("After the call," + " variable times is " + times);
    }

    // Print the message n times
    public static void nPrintln(String message, int n) {
        while (n > 0) {
            System.out.println("n = " + n);
            System.out.println(message);
            n--;
        }
    }
}
```

(c)
By encapsulating the code for obtaining the gcd in a method, this program has several advantages:

1. It isolates the problem for computing the gcd from the rest of the code in the main method. Thus, the logic becomes clear and the program is easier to read.

2. The errors on computing the gcd are confined in the gcd method, which narrows the scope of debugging.

3. The gcd method now can be reused by other programs.

Listing 6.7 applies the concept of code modularization to improve Listing 5.15, PrimeNumber.java.

### Listing 6.7  PrimeNumberMethod.java

```java
public class PrimeNumberMethod {
  public static void main(String[] args) {
    System.out.println("The first 50 prime numbers are \n");
    printPrimeNumbers(50);
  }

  public static void printPrimeNumbers(int numberOfPrimes) {
    final int NUMBER_OF_PRIMES_PER_LINE = 10; // Display 10 per line
    int count = 0; // Count the number of prime numbers
    int number = 2; // A number to be tested for primeness

    // Repeatedly find prime numbers
    while (count < numberOfPrimes) {
      // Print the prime number and increase the count
      if (isPrime(number)) {
        count++; // Increase the count
        // Print the next prime number
      }
    }
  }

  public static boolean isPrime(int number) {
    // Return true if the given number is prime.
    if (number <= 1) {
      return false;
    }
    for (int i = 2; i <= Math.sqrt(number); i++) {
      if (number % i == 0) {
        return false;
      }
    }
    return true;
  }
```

Enter first integer: 45
Enter second integer: 75
The greatest common divisor for 45 and 75 is 15
6.7 Case Study: Converting Hexadecimals to Decimals

The first 50 prime numbers are

\[
\begin{array}{cccccccccccc}
2 & 3 & 5 & 7 & 11 & 13 & 17 & 19 & 23 & 29 \\
31 & 37 & 41 & 43 & 47 & 53 & 59 & 61 & 67 & 71 \\
73 & 79 & 83 & 89 & 97 & 101 & 103 & 107 & 109 & 113 \\
127 & 131 & 137 & 139 & 149 & 151 & 157 & 163 & 167 & 173 \\
179 & 181 & 191 & 193 & 197 & 199 & 211 & 223 & 227 & 229 \\
\end{array}
\]

We divided a large problem into two subproblems: determining whether a number is a prime and printing the prime numbers. As a result, the new program is easier to read and easier to debug. Moreover, the methods `printPrimeNumbers` and `isPrime` can be reused by other programs.

6.7 Case Study: Converting Hexadecimals to Decimals

This section presents a program that converts a hexadecimal number into a decimal number.

Listing 5.11, Dec2Hex.java, gives a program that converts a decimal to a hexadecimal. How would you convert a hex number into a decimal?

Given a hexadecimal number \( h_n h_{n-1} h_{n-2} \ldots h_2 h_1 h_0 \), the equivalent decimal value is

\[
\begin{align*}
& h_n \times 16^n + h_{n-1} \times 16^{n-1} + h_{n-2} \times 16^{n-2} + \ldots \\
& + h_2 \times 16^2 + h_1 \times 16^1 + h_0 \times 16^0
\end{align*}
\]

For example, the hex number \( AB8C \) is

\[
10 \times 16^3 + 11 \times 16^2 + 8 \times 16^1 + 12 \times 16^0 = 43916
\]

Our program will prompt the user to enter a hex number as a string and convert it into a decimal using the following method:

```java
public static int hexToDecimal(String hex)
```
A brute-force approach is to convert each hex character into a decimal number, multiply it by $16^i$ for a hex digit at the $i$’s position, and then add all the items together to obtain the equivalent decimal value for the hex number.

Note that

$$h_n \times 16^n + h_{n-1} \times 16^{n-1} + h_{n-2} \times 16^{n-2} + \ldots + h_1 \times 16^1 + h_0 \times 16^0$$

$$= (\ldots((h_n \times 16 + h_{n-1}) \times 16 + h_{n-2}) \times 16 + \ldots + h_1) \times 16 + h_0$$

This observation, known as the Horner’s algorithm, leads to the following efficient code for converting a hex string to a decimal number:

```java
int decimalValue = 0;
for (int i = 0; i < hex.length(); i++) {
    char hexChar = hex.charAt(i);
    decimalValue = decimalValue * 16 + hexCharToDecimal(hexChar);
}
```

Here is a trace of the algorithm for hex number `AB8C`:

<table>
<thead>
<tr>
<th>i</th>
<th>hexChar</th>
<th>hexCharToDecimal (hexChar)</th>
<th>decimalValue</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td></td>
<td></td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>A</td>
<td>10</td>
<td>10</td>
</tr>
<tr>
<td>2</td>
<td>B</td>
<td>11</td>
<td>10 * 16 + 11</td>
</tr>
<tr>
<td>3</td>
<td>8</td>
<td>8</td>
<td>(10 * 16 + 11) * 16 + 8</td>
</tr>
<tr>
<td>4</td>
<td>C</td>
<td>12</td>
<td>((10 * 16 + 11) * 16 + 8) * 16 + 12</td>
</tr>
</tbody>
</table>

Listing 6.8 gives the complete program.

**LISTING 6.8 Hex2Dec.java**

```java
import java.util.Scanner;

public class Hex2Dec {
    public static void main(String[] args) {
        // Create a Scanner
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter a string
        System.out.print("Enter a hex number: ");
        String hex = input.nextLine();

        System.out.println("The decimal value for hex number 
        + hex + " + hexToDecimal(hex.toUpperCase()));
    }

    public static int hexToDecimal(String hex) {
        int decimalValue = 0;
        for (int i = 0; i < hex.length(); i++) {
            char hexChar = hex.charAt(i);
            decimalValue = decimalValue * 16 + hexCharToDecimal(hexChar);
        }
    }
}
```
6.8 Overloading Methods

Overloading methods enables you to define the methods with the same name as long as their signatures are different.

The `max` method that was used earlier works only with the `int` data type. But what if you need to determine which of two floating-point numbers has the maximum value? The solution is to create another method with the same name but different parameters, as shown in the following code:

```java
public static double max(double num1, double num2) {
    if (num1 > num2)
        return num1;
    else
        return num2;
}
```

If you call `max` with `int` parameters, the `max` method that expects `int` parameters will be invoked; if you call `max` with `double` parameters, the `max` method that expects `double` parameters will be invoked. This is referred to as method overloading; that is, two methods have the same name but different parameter lists within one class. The Java compiler determines which method to use based on the method signature.
Listing 6.9 is a program that creates three methods. The first finds the maximum integer, the second finds the maximum double, and the third finds the maximum among three double values. All three methods are named `max`.

```java
public class TestMethodOverloading {
    // Main method
    public static void main(String[] args) {
        // Invoke the max method with int parameters
        System.out.println("The maximum of 3 and 4 is "+ max(3, 4));

        // Invoke the max method with the double parameters
        System.out.println("The maximum of 3.0 and 5.4 is "+ max(3.0, 5.4));

        // Invoke the max method with three double parameters
        System.out.println("The maximum of 3.0, 5.4, and 10.14 is "+ max(3.0, 5.4, 10.14));
    }

    // Return the max of two int values
    public static int max(int num1, int num2) {
        if (num1 > num2)
            return num1;
        else
            return num2;
    }

    // Find the max of two double values
    public static double max(double num1, double num2) {
        if (num1 > num2)
            return num1;
        else
            return num2;
    }

    // Return the max of three double values
    public static double max(double num1, double num2, double num3) {
        return max(max(num1, num2), num3);
    }
}
```

The maximum of 3 and 4 is 4
The maximum of 3.0 and 5.4 is 5.4
The maximum of 3.0, 5.4, and 10.14 is 10.14

When calling `max(3, 4)` (line 6), the `max` method for finding the maximum of two integers is invoked. When calling `max(3.0, 5.4)` (line 10), the `max` method for finding the maximum of two doubles is invoked. When calling `max(3.0, 5.4, 10.14)` (line 14), the `max` method for finding the maximum of three double values is invoked.

Can you invoke the `max` method with an `int` value and a `double` value, such as `max(2, 2.5)`? If so, which of the `max` methods is invoked? The answer to the first question is yes. The answer to the second question is that the `max` method for finding the maximum of two `double` values is invoked. The argument value 2 is automatically converted into a `double` value and passed to this method.
You may be wondering why the method `max(double, double)` is not invoked for the call `max(3, 4)`. Both `max(double, double)` and `max(int, int)` are possible matches for `max(3, 4)`. The Java compiler finds the method that best matches a method invocation. Since the method `max(int, int)` is a better matches for `max(3, 4)` than `max(double, double)`, `max(int, int)` is used to invoke `max(3, 4).

**Tip**
Overloading methods can make programs clearer and more readable. Methods that perform the same function with different types of parameters should be given the same name.

**Note**
Overloaded methods must have different parameter lists. You cannot overload methods based on different modifiers or return types.

**Note**
Sometimes there are two or more possible matches for the invocation of a method, but the compiler cannot determine the best match. This is referred to as *ambiguous invocation*. Ambiguous invocation causes a compile error. Consider the following code:

```java
public class AmbiguousOverloading {
    public static void main(String[] args) {
        System.out.println(max(1, 2));
    }

    public static double max(int num1, double num2) {
        if (num1 > num2)
            return num1;
        else
            return num2;
    }

    public static double max(double num1, int num2) {
        if (num1 > num2)
            return num1;
        else
            return num2;
    }
}
```

Both `max(int, double)` and `max(double, int)` are possible candidates to match `max(1, 2)`. Because neither is better than the other, the invocation is ambiguous, resulting in a compile error.

6.15 What is method overloading? Is it permissible to define two methods that have the same name but different parameter types? Is it permissible to define two methods in a class that have identical method names and parameter lists but different return value types or different modifiers?

6.16 What is wrong in the following program?

```java
public class Test {
    public static void method(int x) {
    }

    public static int method(int y) {
```
6.17 Given two method definitions,

```java
public static double m(double x, double y)
public static double m(int x, double y)
```
tell which of the two methods is invoked for:

a. `double z = m(4, 5);`
b. `double z = m(4, 5.4);`
c. `double z = m(4.5, 5.4);`

6.9 The Scope of Variables

The scope of a variable is the part of the program where the variable can be referenced.

Section 2.5 introduced the scope of a variable. This section discusses the scope of variables in detail. A variable defined inside a method is referred to as a local variable. The scope of a local variable starts from its declaration and continues to the end of the block that contains the variable. A local variable must be declared and assigned a value before it can be used.

A parameter is actually a local variable. The scope of a method parameter covers the entire method. A variable declared in the initial-action part of a `for`-loop header has its scope in the entire loop. However, a variable declared inside a `for`-loop body has its scope limited in the loop body from its declaration to the end of the block that contains the variable, as shown in Figure 6.5.

```java
public static void method1() {
  int j;
  for (int i = 1; i < 10; i++) {
    int j;
    }
}
```

**Figure 6.5** A variable declared in the initial action part of a `for`-loop header has its scope in the entire loop.

You can declare a local variable with the same name in different blocks in a method, but you cannot declare a local variable twice in the same block or in nested blocks, as shown in Figure 6.6.
6.10 Case Study: Generating Random Characters

A character is coded using an integer. Generating a random character is to generate an integer.

Computer programs process numerical data and characters. You have seen many examples that involve numerical data. It is also important to understand characters and how to process them. This section presents an example of generating random characters.

As introduced in Section 4.3, every character has a unique Unicode between 0 and FFFF in hexadecimal (65535 in decimal). To generate a random character is to generate a random integer between 0 and 65535 using the following expression (note that since $0 \leq \text{Math.random()} < 1.0$, you have to add 1 to 65535):

$\text{(int)}(\text{Math.random()} \times (65535 + 1))$

Now let’s consider how to generate a random lowercase letter. The Unicodes for lowercase letters are consecutive integers starting from the Unicode for a, then that for b, c, ..., and z. The Unicode for a is

$\text{(int)'}a'$

Thus, a random integer between $\text{(int)'}a'$ and $\text{(int)'}z'$ is

$\text{(int)}((\text{int)'}a' + \text{Math.random()} \times ((\text{int)'}z' - (\text{int)'}a' + 1))$
As discussed in Section 4.3.3, all numeric operators can be applied to the \texttt{char} operands. The \texttt{char} operand is cast into a number if the other operand is a number or a character. Therefore, the preceding expression can be simplified as follows:

\begin{verbatim}
'a' + Math.random() * ('z' - 'a' + 1)
\end{verbatim}

and a random lowercase letter is

\begin{verbatim}
(char)('a' + Math.random() * ('z' - 'a' + 1))
\end{verbatim}

Hence, a random character between any two characters \texttt{ch1} and \texttt{ch2} with \texttt{ch1 < ch2} can be generated as follows:

\begin{verbatim}
(char)(ch1 + Math.random() * (ch2 - ch1 + 1))
\end{verbatim}

This is a simple but useful discovery. Listing 6.10 defines a class named \texttt{RandomCharacter} with five overloaded methods to get a certain type of character randomly. You can use these methods in your future projects.

**Listing 6.10 RandomCharacter.java**

```java
public class RandomCharacter {
    /** Generate a random character between ch1 and ch2 */
    public static char getRandomCharacter(char ch1, char ch2) {
        return (char)(ch1 + Math.random() * (ch2 - ch1 + 1));
    }

    /** Generate a random lowercase letter */
    public static char getRandomLowerCaseLetter() {
        return getRandomCharacter('a', 'z');
    }

    /** Generate a random uppercase letter */
    public static char getRandomUpperCaseLetter() {
        return getRandomCharacter('A', 'Z');
    }

    /** Generate a random digit character */
    public static char getRandomDigitCharacter() {
        return getRandomCharacter('0', '9');
    }

    /** Generate a random character */
    public static char getRandomCharacter() {
        return getRandomCharacter(' ', '￿');
    }
}
```

Listing 6.11 gives a test program that displays 175 random lowercase letters.

**Listing 6.11 TestRandomCharacter.java**

```java
public class TestRandomCharacter {
    /** Main method */
    public static void main(String[] args) {
        final int NUMBER_OF_CHARS = 175;
        final int CHARS_PER_LINE = 25;

        // Print random characters between 'a' and 'z', 25 chars per line
        for (int i = 0; i < NUMBER_OF_CHARS; i++) {
```
6.11 Method Abstraction and Stepwise Refinement

The key to developing software is to apply the concept of abstraction.

You will learn many levels of abstraction from this book. Method abstraction is achieved by separating the use of a method from its implementation. The client can use a method without knowing how it is implemented. The details of the implementation are encapsulated in the method and hidden from the client who invokes the method. This is also known as information hiding or encapsulation. If you decide to change the implementation, the client program will not be affected, provided that you do not change the method signature. The implementation of the method is hidden from the client in a “black box,” as shown in Figure 6.7.

![Figure 6.7](image)

The method body can be thought of as a black box that contains the detailed implementation for the method.

You have already used the `System.out.print` method to display a string and the `max` method to find the maximum number. You know how to write the code to invoke these methods in your program, but as a user of these methods, you are not required to know how they are implemented.

The concept of method abstraction can be applied to the process of developing programs. When writing a large program, you can use the `divide-and-conquer` strategy, also known as stepwise refinement, to decompose it into subproblems. The subproblems can be further decomposed into smaller, more manageable problems.

Suppose you write a program that displays the calendar for a given month of the year. The program prompts the user to enter the year and the month, then displays the entire calendar for the month, as shown in the following sample run.

```java
char ch = RandomCharacter.getRandomLowerCaseLetter();

if ((i + 1) % CHARS_PER_LINE == 0)
    System.out.println(ch);
else
    System.out.print(ch);
}
}
```
Let us use this example to demonstrate the divide-and-conquer approach.

### 6.1.1 Top-Down Design

How would you get started on such a program? Would you immediately start coding? Beginning programmers often start by trying to work out the solution to every detail. Although details are important in the final program, concern for detail in the early stages may block the problem-solving process. To make problem solving flow as smoothly as possible, this example begins by using method abstraction to isolate details from design and only later implements the details.

For this example, the problem is first broken into two subproblems: get input from the user and print the calendar for the month. At this stage, you should be concerned with what the subproblems will achieve, not with how to get input and print the calendar for the month. You can draw a structure chart to help visualize the decomposition of the problem (see Figure 6.8a).

![Figure 6.8](image)

**Figure 6.8** The structure chart shows that the `printCalendar` problem is divided into two subproblems, `readInput` and `printMonth` in (a), and that `printMonth` is divided into two smaller subproblems, `printMonthTitle` and `printMonthBody` in (b).

You can use `Scanner` to read input for the year and the month. The problem of printing the calendar for a given month can be broken into two subproblems: print the month title and print the month body, as shown in Figure 6.8b. The month title consists of three lines: month and year, a dashed line, and the names of the seven days of the week. You need to get the month name (e.g., January) from the numeric month (e.g., 1). This is accomplished in `getMonthName` (see Figure 6.9a).

In order to print the month body, you need to know which day of the week is the first day of the month (`getStartDay`) and how many days the month has (`getNumberOfDaysInMonth`),
as shown in Figure 6.9b. For example, December 2013 has 31 days, and December 1, 2013, is a Sunday.

How would you get the start day for the first date in a month? There are several ways to do so. For now, we’ll use an alternative approach. Assume you know that the start day for January 1, 1800, was a Wednesday (START_DAY_FOR_JAN_1_1800 = 3). You could compute the total number of days (totalNumberOfDays) between January 1, 1800, and the first date of the calendar month. The start day for the calendar month is (totalNumberOfDays + START_DAY_FOR_JAN_1_1800) % 7, since every week has seven days. Thus, the getStartDay problem can be further refined as getTotalNumberOfDays, as shown in Figure 6.10a.

To get the total number of days, you need to know whether the year is a leap year and the number of days in each month. Thus, getTotalNumberOfDays can be further refined into two subproblems: isLeapYear and getNumberOfDaysInMonth, as shown in Figure 6.10b. The complete structure chart is shown in Figure 6.11.

### 6.11.2 Top-Down and/or Bottom-Up Implementation

Now we turn our attention to implementation. In general, a subproblem corresponds to a method in the implementation, although some are so simple that this is unnecessary. You would need to decide which modules to implement as methods and which to combine with other methods. Decisions of this kind should be based on whether the overall program will be easier to read as a result of your choice. In this example, the subproblem readInput can be simply implemented in the main method.

You can use either a “top-down” or a “bottom-up” approach. The top-down approach implements one method in the structure chart at a time from the top to the bottom. Stubs—a simple but incomplete version of a method—can be used for the methods waiting to be implemented. The use of stubs enables you to quickly build the framework of the program. Implement the main method first, and then use a stub for the printMonth method. For example,
FIGURE 6.11 The structure chart shows the hierarchical relationship of the subproblems in the program.

```
let **printMonth** display the year and the month in the stub. Thus, your program may begin like this:

```java
public class PrintCalendar {
    /** Main method */
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter year
        System.out.print("Enter full year (e.g., 2012): ");
        int year = input.nextInt();

        // Prompt the user to enter month
        System.out.print("Enter month as a number between 1 and 12: ");
        int month = input.nextInt();

        // Print calendar for the month of the year
        printMonth(year, month);
    }

    /** A stub for printMonth may look like this */
    public static void printMonth(int year, int month){
        System.out.print(month + " " + year);
    }

    /** A stub for printMonthTitle may look like this */
    public static void printMonthTitle(int year, int month){
    }

    /** A stub for getMonthBody may look like this */
    public static void printMonthBody(int year, int month){
    }
```
/** A stub for getMonthName may look like this */
public static String getMonthName(int month) {
    return "January"; // A dummy value
}

/** A stub for getStartDay may look like this */
public static int getStartDay(int year, int month) {
    return 1; // A dummy value
}

/** A stub for getTotalNumberOfDays may look like this */
public static int getTotalNumberOfDays(int year, int month) {
    return 10000; // A dummy value
}

/** A stub for getNumberOfDaysInMonth may look like this */
public static int getNumberOfDaysInMonth(int year, int month) {
    return 31; // A dummy value
}

/** A stub for isLeapYear may look like this */
public static Boolean isLeapYear(int year) {
    return true; // A dummy value
}

Compile and test the program, and fix any errors. You can now implement the printMonth method. For methods invoked from the printMonth method, you can again use stubs.

The bottom-up approach implements one method in the structure chart at a time, from the bottom to the top. For each method implemented, write a test program, known as the driver, to test it. The top-down and bottom-up approaches are equally good: Both approaches implement methods incrementally, help to isolate programming errors, and make debugging easy. They can be used together.

6.11.3 Implementation Details

The isLeapYear(int year) method can be implemented using the following code from Section 3.11:

return year % 400 == 0 || (year % 4 == 0 && year % 100 != 0);

Use the following facts to implement getTotalNumberOfDaysInMonth(int year, int month):

- January, March, May, July, August, October, and December have 31 days.
- April, June, September, and November have 30 days.
- February has 28 days during a regular year and 29 days during a leap year. A regular year, therefore, has 365 days, a leap year 366 days.

To implement getTotalNumberOfDays(int year, int month), you need to compute the total number of days (totalNumberOfDays) between January 1, 1800, and the first day of the calendar month. You could find the total number of days between the year 1800 and the calendar year and then figure out the total number of days prior to the calendar month in the calendar year. The sum of these two totals is totalNumberOfDays.

To print a body, first pad some space before the start day and then print the lines for every week.

The complete program is given in Listing 6.12.
import java.util.Scanner;

public class PrintCalendar {
  /** Main method */
  public static void main(String[] args) {
    Scanner input = new Scanner(System.in);
    System.out.print("Enter full year (e.g., 2012): ");
    int year = input.nextInt();
    System.out.print("Enter month as a number between 1 and 12: ");
    int month = input.nextInt();
    // Print calendar for the month of the year
    printMonth(year, month);
  }
  
  public static void printMonth(int year, int month) {
    // Print the headings of the calendar
    printMonthTitle(year, month);
    // Print the body of the calendar
    printMonthBody(year, month);
  }

  public static void printMonthTitle(int year, int month) {
    System.out.println("  "+getMonthName(month)
                     +"  "+year);
    System.out.println("-----------------------------");
    System.out.println(" Sun Mon Tue Wed Thu Fri Sat");
  }

  public static String getMonthName(int month) {
    String monthName = "";
    switch (month) {
      case 1: monthName = "January"; break;
      case 2: monthName = "February"; break;
      case 3: monthName = "March"; break;
      case 4: monthName = "April"; break;
      case 5: monthName = "May"; break;
      case 6: monthName = "June"; break;
      case 7: monthName = "July"; break;
      case 8: monthName = "August"; break;
      case 9: monthName = "September"; break;
      case 10: monthName = "October"; break;
      case 11: monthName = "November"; break;
      case 12: monthName = "December";
    }
    return monthName;
  }

  /* Print month body */
public static void printMonthBody(int year, int month) {
    // Get start day of the week for the first date in the month
    int startDay = getStartDay(year, month);
    // Get number of days in the month
    int numberOfDaysInMonth = getNumberOfDaysInMonth(year, month);
    // Pad space before the first day of the month
    int i = 0;
    for (i = 0; i < startDay; i++)
        System.out.print("    ");
    for (i = 1; i <= numberOfDaysInMonth; i++) {
        System.out.printf("%4d", i);
        if ((i + startDay) % 7 == 0)
            System.out.println();
    }
    System.out.println();
}
/** Get the start day of month/1/year */
public static int getStartDay(int year, int month) {
    final int START_DAY_FOR_JAN_1_1800 = 3;
    // Get total number of days from 1/1/1800 to month/1/year
    int totalNumberOfDays = getTotalNumberOfDays(year, month);
    // Return the start day for month/1/year
    return (totalNumberOfDays + START_DAY_FOR_JAN_1_1800) % 7;
}
/** Get the total number of days since January 1, 1800 */
public static int getTotalNumberOfDays(int year, int month) {
    int total = 0;
    // Get the total days from 1800 to 1/1/year
    for (int i = 1800; i < year; i++)
        if (isLeapYear(i))
            total = total + 366;
        else
            total = total + 365;
    // Add days from Jan to the month prior to the calendar month
    for (int i = 1; i < month; i++)
        total = total + getNumberOfDaysInMonth(year, i);
    return total;
}
/** Get the number of days in a month */
public static int getNumberOfDaysInMonth(int year, int month) {
    if (month == 1 || month == 3 || month == 5 || month == 7 ||
        month == 8 || month == 10 || month == 12)
        return 31;
    if (month == 4 || month == 6 || month == 9 || month == 11)
        return 30;
    if (month == 2) return isLeapYear(year) ? 29 : 28;
The program does not validate user input. For instance, if the user enters either a month not in the range between 1 and 12 or a year before 1800, the program displays an erroneous calendar. To avoid this error, add an if statement to check the input before printing the calendar.

This program prints calendars for a month but could easily be modified to print calendars for a whole year. Although it can print months only after January 1800, it could be modified to print months before 1800.

6.11.4 Benefits of Stepwise Refinement

Stepwise refinement breaks a large problem into smaller manageable subproblems. Each subproblem can be implemented using a method. This approach makes the program easier to write, reuse, debug, test, modify, and maintain.

Simpler Program

The print calendar program is long. Rather than writing a long sequence of statements in one method, stepwise refinement breaks it into smaller methods. This simplifies the program and makes the whole program easier to read and understand.

Reusing Methods

Stepwise refinement promotes code reuse within a program. The isLeapYear method is defined once and invoked from the getTotalNumberOfDays and getNumberOfDayInMonth methods. This reduces redundant code.

Easier Developing, Debugging, and Testing

Since each subproblem is solved in a method, a method can be developed, debugged, and tested individually. This isolates the errors and makes developing, debugging, and testing easier.

When implementing a large program, use the top-down and/or bottom-up approach. Do not write the entire program at once. Using these approaches seems to take more development time (because you repeatedly compile and run the program), but it actually saves time and makes debugging easier.

Better Facilitating Teamwork

When a large problem is divided into subprograms, subproblems can be assigned to different programmers. This makes it easier for programmers to work in teams.

**Key Terms**

- actual parameter 205
- ambiguous invocation 221
- argument 205
- divide and conquer 225
- formal parameter (i.e., parameter) 205
- information hiding 225
- method 204
- method abstraction 225
- method overloading 219
- method signature 205
- modifier 205
- parameter 205
- pass-by-value 212
- scope of a variable 222
- stepwise refinement 225
- stub 227
1. Making programs modular and reusable is one of the central goals in software engineering. Java provides many powerful constructs that help to achieve this goal. Methods are one such construct.

2. The method header specifies the modifiers, return value type, method name, and parameters of the method. The `static` modifier is used for all the methods in this chapter.

3. A method may return a value. The `returnValue` is the data type of the value the method returns. If the method does not return a value, the `returnValue` is the keyword `void`.

4. The `parameter list` refers to the type, order, and number of a method’s parameters. The method name and the parameter list together constitute the `method signature`. Parameters are optional; that is, a method doesn’t need to contain any parameters.

5. A return statement can also be used in a `void` method for terminating the method and returning to the method’s caller. This is useful occasionally for circumventing the normal flow of control in a method.

6. The arguments that are passed to a method should have the same number, type, and order as the parameters in the method signature.

7. When a program calls a method, program control is transferred to the called method. A called method returns control to the caller when its return statement is executed or when its method-ending closing brace is reached.

8. A value-returning method can also be invoked as a statement in Java. In this case, the caller simply ignores the return value.

9. A method can be overloaded. This means that two methods can have the same name, as long as their method parameter lists differ.

10. A variable declared in a method is called a local variable. The `scope of a local variable` starts from its declaration and continues to the end of the block that contains the variable. A local variable must be declared and initialized before it is used.

11. Method abstraction is achieved by separating the use of a method from its implementation. The client can use a method without knowing how it is implemented. The details of the implementation are encapsulated in the method and hidden from the client who invokes the method. This is known as information hiding or encapsulation.

12. Method abstraction modularizes programs in a neat, hierarchical manner. Programs written as collections of concise methods are easier to write, debug, maintain, and modify than would otherwise be the case. This writing style also promotes method reusability.

13. When implementing a large program, use the top-down and/or bottom-up coding approach. Do not write the entire program at once. This approach may seem to take more time for coding (because you are repeatedly compiling and running the program), but it actually saves time and makes debugging easier.
QUIZ

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

PROGRAMMING EXERCISES

Note
A common error for the exercises in this chapter is that students don’t implement the methods to meet the requirements even though the output from the main program is correct. For an example of this type of error see www.cs.armstrong.edu/liang/CommonMethodErrorJava.pdf.

Sections 6.2–6.9

6.1 (Math: pentagonal numbers) A pentagonal number is defined as \( n(3n-1)/2 \) for \( n = 1, 2, \ldots \), and so on. Therefore, the first few numbers are 1, 5, 12, 22, . . . . Write a method with the following header that returns a pentagonal number:

```java
public static int getPentagonalNumber(int n)
```

Write a test program that uses this method to display the first 100 pentagonal numbers with 10 numbers on each line.

*6.2 (Sum the digits in an integer) Write a method that computes the sum of the digits in an integer. Use the following method header:

```java
public static int sumDigits(long n)
```

For example, `sumDigits(234)` returns 9 (2 + 3 + 4). (Hint: Use the `%` operator to extract digits, and the `/` operator to remove the extracted digit. For instance, to extract 4 from 234, use `234 % 10` (= 4). To remove 4 from 234, use `234 / 10` (= 23). Use a loop to repeatedly extract and remove the digit until all the digits are extracted. Write a test program that prompts the user to enter an integer and displays the sum of all its digits.

**6.3 (Palindrome integer) Write the methods with the following headers

// Return the reversal of an integer, i.e., reverse(456) returns 654
public static int reverse(int number)

// Return true if number is a palindrome
public static boolean isPalindrome(int number)

Use the `reverse` method to implement `isPalindrome`. A number is a palindrome if its reversal is the same as itself. Write a test program that prompts the user to enter an integer and reports whether the integer is a palindrome.

*6.4 (Display an integer reversed) Write a method with the following header to display an integer in reverse order:

```java
public static void reverse(int number)
```

For example, `reverse(3456)` displays 6543. Write a test program that prompts the user to enter an integer and displays its reversal.

*6.5 (Sort three numbers) Write a method with the following header to display three numbers in increasing order:

```java
public static void displaySortedNumbers(
    double num1, double num2, double num3)
```
Write a test program that prompts the user to enter three numbers and invokes the method to display them in increasing order.

*6.6 (Display patterns) Write a method to display a pattern as follows:

```
  1
  2 1
  3 2 1 
... 
n n-1 ... 3 2 1
```

The method header is

```
public static void displayPattern(int n)
```

*6.7 (Financial application: compute the future investment value) Write a method that computes future investment value at a given interest rate for a specified number of years. The future investment is determined using the formula in Programming Exercise 2.21.

Use the following method header:

```
public static double futureInvestmentValue(
    double investmentAmount, double monthlyInterestRate, int years)
```

For example, `futureInvestmentValue(10000, 0.05/12, 5)` returns 12833.59.

Write a test program that prompts the user to enter the investment amount (e.g., 1000) and the interest rate (e.g., 9%) and prints a table that displays future value for the years from 1 to 30, as shown below:

<table>
<thead>
<tr>
<th>Years</th>
<th>Future Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1093.80</td>
</tr>
<tr>
<td>2</td>
<td>1196.41</td>
</tr>
<tr>
<td>...</td>
<td></td>
</tr>
<tr>
<td>29</td>
<td>13467.25</td>
</tr>
<tr>
<td>30</td>
<td>14730.57</td>
</tr>
</tbody>
</table>

6.8 (Conversions between Celsius and Fahrenheit) Write a class that contains the following two methods:

```
/** Convert from Celsius to Fahrenheit */
public static double celsiusToFahrenheit(double celsius)

/** Convert from Fahrenheit to Celsius */
public static double fahrenheitToCelsius(double fahrenheit)
```

The formula for the conversion is:

\[
\text{fahrenheit} = \frac{9.0}{5} \times \text{celsius} + 32 \\
\text{celsius} = \frac{5.0}{9} \times (\text{fahrenheit} - 32)
\]
Write a test program that invokes these methods to display the following tables:

<table>
<thead>
<tr>
<th>Celsius</th>
<th>Fahrenheit</th>
<th>Fahrenheit</th>
<th>Celsius</th>
</tr>
</thead>
<tbody>
<tr>
<td>40.0</td>
<td>104.0</td>
<td>120.0</td>
<td>48.89</td>
</tr>
<tr>
<td>39.0</td>
<td>102.2</td>
<td>110.0</td>
<td>43.33</td>
</tr>
</tbody>
</table>

...  

| 32.0    | 89.6       | 40.0       | 4.44    |
| 31.0    | 87.8       | 30.0       | -1.11   |

6.9 (Conversions between feet and meters) Write a class that contains the following two methods:

```java
/** Convert from feet to meters */
public static double footToMeter(double foot)

/** Convert from meters to feet */
public static double meterToFoot(double meter)
```

The formula for the conversion is:

\[
\text{meter} = 0.305 \times \text{foot} \\
\text{foot} = 3.279 \times \text{meter}
\]

Write a test program that invokes these methods to display the following tables:

<table>
<thead>
<tr>
<th>Feet</th>
<th>Meters</th>
<th>Meters</th>
<th>Feet</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.0</td>
<td>0.305</td>
<td>20.0</td>
<td>65.574</td>
</tr>
<tr>
<td>2.0</td>
<td>0.610</td>
<td>25.0</td>
<td>81.967</td>
</tr>
<tr>
<td>...</td>
<td>...</td>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td>9.0</td>
<td>2.745</td>
<td>60.0</td>
<td>196.721</td>
</tr>
<tr>
<td>10.0</td>
<td>3.050</td>
<td>65.0</td>
<td>213.115</td>
</tr>
</tbody>
</table>

6.10 (Use the isPrime Method) Listing 6.7, PrimeNumberMethod.java, provides the `isPrime(int number)` method for testing whether a number is prime. Use this method to find the number of prime numbers less than 10000.

6.11 (Financial application: compute commissions) Write a method that computes the commission, using the scheme in Programming Exercise 5.39. The header of the method is as follows:

```java
public static double computeCommission(double salesAmount)
```

Write a test program that displays the following table:

<table>
<thead>
<tr>
<th>Sales Amount</th>
<th>Commission</th>
</tr>
</thead>
<tbody>
<tr>
<td>10000</td>
<td>900.0</td>
</tr>
<tr>
<td>15000</td>
<td>1500.0</td>
</tr>
<tr>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td>95000</td>
<td>11100.0</td>
</tr>
<tr>
<td>100000</td>
<td>11700.0</td>
</tr>
</tbody>
</table>
6.12 (Display characters) Write a method that prints characters using the following header:

```
public static void printChars(char ch1, char ch2, int numberPerLine)
```

This method prints the characters between ch1 and ch2 with the specified numbers per line. Write a test program that prints ten characters per line from 1 to Z. Characters are separated by exactly one space.

*6.13 (Sum series) Write a method to compute the following series:

\[ m(i) = \frac{1}{2} + \frac{2}{3} + \ldots + \frac{i}{i+1} \]

Write a test program that displays the following table:

<table>
<thead>
<tr>
<th>i</th>
<th>m(i)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.5000</td>
</tr>
<tr>
<td>2</td>
<td>1.1667</td>
</tr>
<tr>
<td>...</td>
<td></td>
</tr>
<tr>
<td>19</td>
<td>16.4023</td>
</tr>
<tr>
<td>20</td>
<td>17.3546</td>
</tr>
</tbody>
</table>

*6.14 (Estimate π) π can be computed using the following series:

\[ m(i) = 4 \left( \frac{1}{3} - \frac{1}{5} + \frac{1}{7} - \frac{1}{9} + \frac{1}{11} + \ldots + \frac{(-1)^{i+1}}{2i-1} \right) \]

Write a method that returns m(i) for a given i and write a test program that displays the following table:

<table>
<thead>
<tr>
<th>i</th>
<th>m(i)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>4.0000</td>
</tr>
<tr>
<td>101</td>
<td>3.1515</td>
</tr>
<tr>
<td>201</td>
<td>3.1466</td>
</tr>
<tr>
<td>301</td>
<td>3.1449</td>
</tr>
<tr>
<td>401</td>
<td>3.1441</td>
</tr>
<tr>
<td>501</td>
<td>3.1436</td>
</tr>
<tr>
<td>601</td>
<td>3.1433</td>
</tr>
<tr>
<td>701</td>
<td>3.1430</td>
</tr>
<tr>
<td>801</td>
<td>3.1428</td>
</tr>
<tr>
<td>901</td>
<td>3.1427</td>
</tr>
</tbody>
</table>

*6.15 (Financial application: print a tax table) Listing 3.5 gives a program to compute tax. Write a method for computing tax using the following header:

```
public static double computeTax(int status, double taxableIncome)
```
Use this method to write a program that prints a tax table for taxable income from $50,000 to $60,000 with intervals of $50 for all the following statuses:

<table>
<thead>
<tr>
<th>Taxable Income</th>
<th>Single</th>
<th>Married Joint or Qualifying Widow(er)</th>
<th>Married Separate</th>
<th>Head of a House</th>
</tr>
</thead>
<tbody>
<tr>
<td>50000</td>
<td>8688</td>
<td>6665</td>
<td>8688</td>
<td>7353</td>
</tr>
<tr>
<td>50050</td>
<td>8700</td>
<td>6673</td>
<td>8700</td>
<td>7365</td>
</tr>
<tr>
<td>...</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>59950</td>
<td>11175</td>
<td>8158</td>
<td>11175</td>
<td>9840</td>
</tr>
<tr>
<td>60000</td>
<td>11188</td>
<td>8165</td>
<td>11188</td>
<td>9853</td>
</tr>
</tbody>
</table>

Hint: round the tax into integers using Math.round (i.e., Math.round(computeTax(status, taxableIncome)).

*6.16 (Number of days in a year) Write a method that returns the number of days in a year using the following header:

```java
public static int numberOfDaysInAYear(int year)
```

Write a test program that displays the number of days in year from 2000 to 2020.

Sections 6.10–6.11

*6.17 (Display matrix of 0s and 1s) Write a method that displays an n-by-n matrix using the following header:

```java
public static void printMatrix(int n)
```

Each element is 0 or 1, which is generated randomly. Write a test program that prompts the user to enter n and displays an n-by-n matrix. Here is a sample run:

```
Enter n: 3
0 1 0
0 0 0
1 1 1
```

**6.18 (Check password) Some websites impose certain rules for passwords. Write a method that checks whether a string is a valid password. Suppose the password rules are as follows:

- A password must have at least eight characters.
- A password consists of only letters and digits.
- A password must contain at least two digits.

Write a program that prompts the user to enter a password and displays Valid Password if the rules are followed or Invalid Password otherwise.

*6.19 (The MyTriangle class) Create a class named MyTriangle that contains the following two methods:

```java
/** Return true if the sum of any two sides is greater than the third side. */
public static boolean isValid(double side1, double side2, double side3)
```
/** Return the area of the triangle. */
public static double area(
    double side1, double side2, double side3)

Write a test program that reads three sides for a triangle and computes the area if
the input is valid. Otherwise, it displays that the input is invalid. The formula for
computing the area of a triangle is given in Programming Exercise 2.19.

*6.20  (Count the letters in a string) Write a method that counts the number of letters in
a string using the following header:

public static int countLetters(String s)

Write a test program that prompts the user to enter a string and displays the num-
ber of letters in the string.

*6.21  (Phone keypads) The international standard letter/number mapping for telephones
is shown in Programming Exercise 4.15. Write a method that returns a number,
given an uppercase letter, as follows:

int getNumber(char uppercaseLetter)

Write a test program that prompts the user to enter a phone number as a string.
The input number may contain letters. The program translates a letter (uppercase
or lowercase) to a digit and leaves all other characters intact. Here is a sample run
of the program:

Enter a string: 1-800-Flowers
1-800-3569377

Enter a string: 1800flowers
18003569377

**6.22  (Math: approximate the square root) There are several techniques for implement-
ating the \texttt{sqrt} method in the \texttt{Math} class. One such technique is known as the
Babylonian method. It approximates the square root of a number, \( n \), by repeatedly
performing a calculation using the following formula:

\[
\text{nextGuess} = \frac{(\text{lastGuess} + n / \text{lastGuess})}{2}
\]

When \texttt{nextGuess} and \texttt{lastGuess} are almost identical, \texttt{nextGuess} is the
approximated square root. The initial guess can be any positive value (e.g., \( 1 \)).
This value will be the starting value for \texttt{lastGuess}. If the difference between
\texttt{nextGuess} and \texttt{lastGuess} is less than a very small number, such as \( 0.0001 \),
you can claim that \texttt{nextGuess} is the approximated square root of \( n \). If not, \texttt{next-
Guess} becomes \texttt{lastGuess} and the approximation process continues. Implement
the following method that returns the square root of \( n \).

public static double sqrt(long n)

*6.23  (Occurrences of a specified character) Write a method that finds the number of
occurrences of a specified character in a string using the following header:

public static int count(String str, char a)
For example, `count("Welcome", 'e')` returns 2. Write a test program that prompts the user to enter a string followed by a character and displays the number of occurrences of the character in the string.

**Sections 6.10–6.12**

**6.24** *(Display current date and time)* Listing 2.7, ShowCurrentTime.java, displays the current time. Improve this example to display the current date and time. The calendar example in Listing 6.12, PrintCalendar.java, should give you some ideas on how to find the year, month, and day.

**6.25** *(Convert milliseconds to hours, minutes, and seconds)* Write a method that converts milliseconds to hours, minutes, and seconds using the following header:

```java
public static String convertMillis(long millis)
```

The method returns a string as `hours:minutes:seconds`. For example, `convertMillis(5500)` returns a string `0:0:5`, `convertMillis(100000)` returns a string `0:1:40`, and `convertMillis(555550000)` returns a string `154:19:10`.

**Comprehensive**

**6.26** *(Palindromic prime)* A palindromic prime is a prime number and also palindromic. For example, 131 is a prime and also a palindromic prime, as are 313 and 757. Write a program that displays the first 100 palindromic prime numbers. Display 10 numbers per line, separated by exactly one space, as follows:

2 3 5 7 11 101 131 151 181 191
313 353 373 383 727 757 787 797 919 929
...

**6.27** *(Emirp)* An emirp (prime spelled backward) is a nonpalindromic prime number whose reversal is also a prime. For example, 17 is a prime and 71 is a prime, so 17 and 71 are emirps. Write a program that displays the first 100 emirps. Display 10 numbers per line, separated by exactly one space, as follows:

13 17 31 37 71 73 79 97 107 113
149 157 167 179 199 311 337 347 359 389
...

**6.28** *(Mersenne prime)* A prime number is called a Mersenne prime if it can be written in the form $2^p - 1$ for some positive integer $p$. Write a program that finds all Mersenne primes with $p \leq 31$ and displays the output as follows:

<table>
<thead>
<tr>
<th>p</th>
<th>$2^p - 1$</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>3</td>
<td>7</td>
</tr>
<tr>
<td>5</td>
<td>31</td>
</tr>
<tr>
<td></td>
<td>...</td>
</tr>
</tbody>
</table>

**6.29** *(Twin primes)* Twin primes are a pair of prime numbers that differ by 2. For example, 3 and 5 are twin primes, 5 and 7 are twin primes, and 11 and 13 are twin primes. Write a program to find all twin primes less than 1,000. Display the output as follows:

(3, 5)
(5, 7)
...
**6.30 (Game: craps) Craps is a popular dice game played in casinos. Write a program to play a variation of the game, as follows:

Roll two dice. Each die has six faces representing values 1, 2, …, and 6, respectively. Check the sum of the two dice. If the sum is 2, 3, or 12 (called craps), you lose; if the sum is 7 or 11 (called natural), you win; if the sum is another value (i.e., 4, 5, 6, 8, 9, or 10), a point is established. Continue to roll the dice until either a 7 or the same point value is rolled. If 7 is rolled, you lose. Otherwise, you win.

Your program acts as a single player. Here are some sample runs.

You rolled 5 + 6 = 11
You win

You rolled 1 + 2 = 3
You lose

You rolled 4 + 4 = 8
point is 8
You rolled 6 + 2 = 8
You win

You rolled 3 + 2 = 5
point is 5
You rolled 2 + 5 = 7
You lose

**6.31 (Financial: credit card number validation) Credit card numbers follow certain patterns. A credit card number must have between 13 and 16 digits. It must start with:

- 4 for Visa cards
- 5 for Master cards
- 37 for American Express cards
- 6 for Discover cards

In 1954, Hans Luhn of IBM proposed an algorithm for validating credit card numbers. The algorithm is useful to determine whether a card number is entered correctly or whether a credit card is scanned correctly by a scanner. Credit card numbers are generated following this validity check, commonly known as the Luhn check or the Mod 10 check, which can be described as follows (for illustration, consider the card number 4388576018402626):

1. Double every second digit from right to left. If doubling of a digit results in a two-digit number, add up the two digits to get a single-digit number.

![Diagram of Luhn check calculations]

2. Add all the digits of the modified number.

3. If the total from step 2 is divisible by 10, the credit card number is valid.
2. Now add all single-digit numbers from Step 1.
   \[4 + 4 + 8 + 2 + 3 + 1 + 7 + 8 = 37\]
3. Add all digits in the odd places from right to left in the card number.
   \[6 + 6 + 0 + 8 + 0 + 7 + 8 + 3 = 38\]
4. Sum the results from Step 2 and Step 3.
   \[37 + 38 = 75\]
5. If the result from Step 4 is divisible by 10, the card number is valid; otherwise, it is invalid. For example, the number 4388576018402626 is invalid, but the number 4388576018410707 is valid.

Write a program that prompts the user to enter a credit card number as a long integer. Display whether the number is valid or invalid. Design your program to use the following methods:

```java
/** Return true if the card number is valid */
public static boolean isValid(long number)

/** Get the result from Step 2 */
public static int sumOfDoubleEvenPlace(long number)

/** Return this number if it is a single digit, otherwise, return the sum of the two digits */
public static int getDigit(int number)

/** Return sum of odd-place digits in number */
public static int sumOfOddPlace(long number)

/** Return true if the digit d is a prefix for number */
public static boolean prefixMatched(long number, int d)

/** Return the number of digits in d */
public static int getSize(long d)

/** Return the first k number of digits from number. If the number of digits in number is less than k, return number. */
public static long getPrefix(long number, int k)
```

Here are sample runs of the program: (You may also implement this program by reading the input as a string and processing the string to validate the credit card.)

```
Enter a credit card number as a long integer:
4388576018410707
4388576018410707 is valid
```

```
Enter a credit card number as a long integer:
4388576018402626
4388576018402626 is invalid
```

**6.32** (Game: chance of winning at craps) Revise Exercise 6.30 to run it 10,000 times and display the number of winning games.

**6.33** (Current date and time) Invoking `System.currentTimeMillis()` returns the elapsed time in milliseconds since midnight of January 1, 1970. Write a program that displays the date and time. Here is a sample run:

```
Current date and time is May 16, 2012 10:34:23
```
**6.34**  *Print calendar* Programming Exercise 3.21 uses Zeller’s congruence to calculate the day of the week. Simplify Listing 6.12, PrintCalendar.java, using Zeller’s algorithm to get the start day of the month.

6.35  *Geometry: area of a pentagon* The area of a pentagon can be computed using the following formula:

\[
Area = \frac{5 \times s^2}{4 \times \tan\left(\frac{\pi}{5}\right)}
\]

Write a method that returns the area of a pentagon using the following header:

```java
public static double area(double side)
```

Write a main method that prompts the user to enter the side of a pentagon and displays its area. Here is a sample run:

```
Enter the side: 5.5
The area of the pentagon is 52.0444136781625
```

*6.36*  *Geometry: area of a regular polygon* A regular polygon is an \( n \)-sided polygon in which all sides are of the same length and all angles have the same degree (i.e., the polygon is both equilateral and equiangular). The formula for computing the area of a regular polygon is

\[
Area = \frac{n \times s^2}{4 \times \tan\left(\frac{\pi}{n}\right)}
\]

Write a method that returns the area of a regular polygon using the following header:

```java
public static double area(int n, double side)
```

Write a main method that prompts the user to enter the number of sides and the side of a regular polygon and displays its area. Here is a sample run:

```
Enter the number of sides: 5
Enter the side: 6.5
The area of the polygon is 72.69017017488385
```

6.37  *Format an integer* Write a method with the following header to format the integer with the specified width.

```java
public static String format(int number, int width)
```

The method returns a string for the number with one or more prefix 0s. The size of the string is the width. For example, `format(34, 4)` returns `0034` and `format(34, 5)` returns `00034`. If the number is longer than the width, the method...
returns the string representation for the number. For example, \texttt{format(34, 1)} returns 34.

Write a test program that prompts the user to enter a number and its width and displays a string returned by invoking \texttt{format(number, width)}.

*6.38*  
(Generate random characters) Use the methods in \texttt{RandomCharacter} in Listing 6.10 to print 100 uppercase letters and then 100 single digits, printing ten per line.

6.39  
(Geometry: point position) Programming Exercise 3.32 shows how to test whether a point is on the left side of a directed line, on the right, or on the same line. Write the methods with the following headers:

\begin{verbatim}
/** Return true if point \((x2, y2)\) is on the left side of the *
* directed line from \((x0, y0)\) to \((x1, y1)\) */
public static boolean leftOfTheLine(double x0, double y0,
   double x1, double y1, double x2, double y2)

/** Return true if point \((x2, y2)\) is on the same *
* line from \((x0, y0)\) to \((x1, y1)\) */
public static boolean onTheSameLine(double x0, double y0,
   double x1, double y1, double x2, double y2)

/** Return true if point \((x2, y2)\) is on the *
* line segment from \((x0, y0)\) to \((x1, y1)\) */
public static boolean onTheLineSegment(double x0, double y0,
   double x1, double y1, double x2, double y2)
\end{verbatim}

Write a program that prompts the user to enter the three points for \texttt{p0}, \texttt{p1}, and \texttt{p2} and displays whether \texttt{p2} is on the left of the line from \texttt{p0} to \texttt{p1}, right, the same line, or on the line segment. Here are some sample runs:

Enter three points for \texttt{p0}, \texttt{p1}, and \texttt{p2}: \texttt{1 1 2 1.5 1.5}  
(1.5, 1.5) is on the line segment from (1.0, 1.0) to (2.0, 2.0)

Enter three points for \texttt{p0}, \texttt{p1}, and \texttt{p2}: \texttt{1 1 2 3 3}  
(3.0, 3.0) is on the same line from (1.0, 1.0) to (2.0, 2.0)

Enter three points for \texttt{p0}, \texttt{p1}, and \texttt{p2}: \texttt{1 1 2 1.5}  
(1.0, 1.5) is on the left side of the line from (1.0, 1.0) to (2.0, 2.0)

Enter three points for \texttt{p0}, \texttt{p1}, and \texttt{p2}: \texttt{1 1 2 1 -1}  
(1.0, -1.0) is on the right side of the line from (1.0, 1.0) to (2.0, 2.0)
Objectives

- To describe why arrays are necessary in programming (§7.1).
- To declare array reference variables and create arrays (§§7.2.1–7.2.2).
- To obtain array size using `arrayRefVar.length` and know default values in an array (§7.2.3).
- To access array elements using indexes (§7.2.4).
- To declare, create, and initialize an array using an array initializer (§7.2.5).
- To program common array operations (displaying arrays, summing all elements, finding the minimum and maximum elements, random shuffling, and shifting elements) (§7.2.6).
- To simplify programming using the for each loops (§7.2.7).
- To apply arrays in application development (`AnalyzeNumbers`, `DeckOfCards`) (§§7.3–7.4).
- To copy contents from one array to another (§7.5).
- To develop and invoke methods with array arguments and return values (§§7.6–7.8).
- To define a method with a variable-length argument list (§7.9).
- To search elements using the linear (§7.10.1) or binary (§7.10.2) search algorithm.
- To sort an array using the selection sort approach (§7.11).
- To use the methods in the `java.util.Arrays` class (§7.12).
- To pass arguments to the main method from the command line (§7.13).
Chapter 7  Single-Dimensional Arrays

7.1 Introduction

A single array variable can reference a large collection of data.

Often you will have to store a large number of values during the execution of a program. Suppose, for instance, that you need to read 100 numbers, compute their average, and find out how many numbers are above the average. Your program first reads the numbers and computes their average, then compares each number with the average to determine whether it is above the average. In order to accomplish this task, the numbers must all be stored in variables. You have to declare 100 variables and repeatedly write almost identical code 100 times. Writing a program this way would be impractical. So, how do you solve this problem?

An efficient, organized approach is needed. Java and most other high-level languages provide a data structure, the array, which stores a fixed-size sequential collection of elements of the same type. In the present case, you can store all 100 numbers into an array and access them through a single array variable.

This chapter introduces single-dimensional arrays. The next chapter will introduce two-dimensional and multidimensional arrays.

7.2 Array Basics

Once an array is created, its size is fixed. An array reference variable is used to access the elements in an array using an index.

An array is used to store a collection of data, but often we find it more useful to think of an array as a collection of variables of the same type. Instead of declaring individual variables, such as number0, number1, . . . , and number99, you declare one array variable such as numbers and use numbers[0], numbers[1], . . . , and numbers[99] to represent individual variables. This section introduces how to declare array variables, create arrays, and process arrays using indexes.

7.2.1 Declaring Array Variables

To use an array in a program, you must declare a variable to reference the array and specify the array’s element type. Here is the syntax for declaring an array variable:

```java
elementType[] arrayRefVar;
```

The elementType can be any data type, and all elements in the array will have the same data type. For example, the following code declares a variable myList that references an array of double elements.

```java
double[] myList;
```

Note
You can also use `elementType_arrayRefVar[]` to declare an array variable. This style comes from the C/C++ language and was adopted in Java to accommodate C/C++ programmers. The style `elementType[] arrayRefVar` is preferred.

7.2.2 Creating Arrays

Unlike declarations for primitive data type variables, the declaration of an array variable does not allocate any space in memory for the array. It creates only a storage location for the reference to an array. If a variable does not contain a reference to an array, the value of the variable is null. You cannot assign elements to an array unless it has already been created. After an
array variable is declared, you can create an array by using the `new` operator and assign its reference to the variable with the following syntax:

```java
arrayRefVar = new elementType[arraySize];
```

This statement does two things: (1) it creates an array using `new elementType[arraySize]`, (2) it assigns the reference of the newly created array to the variable `arrayRefVar`.

Declaring an array variable, creating an array, and assigning the reference of the array to the variable can be combined in one statement as:

```java
elementType[] arrayRefVar = new elementType[arraySize];
```
or

```java
elementType arrayRefVar[] = new elementType[arraySize];
```

Here is an example of such a statement:

```java
double[] myList = new double[10];
```

This statement declares an array variable, `myList`, creates an array of ten elements of `double` type, and assigns its reference to `myList`. To assign values to the elements, use the syntax:

```java
arrayRefVar[index] = value;
```

For example, the following code initializes the array.

```java
myList[0] = 5.6;
myList[1] = 4.5;
myList[2] = 3.3;
myList[3] = 13.2;
myList[4] = 4.0;
myList[5] = 34.33;
myList[6] = 34.0;
myList[7] = 45.45;
myList[8] = 99.993;
myList[9] = 11123;
```

This array is illustrated in Figure 7.1.

![Figure 7.1](image-url)
Note
An array variable that appears to hold an array actually contains a reference to that array. Strictly speaking, an array variable and an array are different, but most of the time the distinction can be ignored. Thus it is all right to say, for simplicity, that `myList` is an array, instead of stating, at greater length, that `myList` is a variable that contains a reference to an array of ten double elements.

7.2.3 Array Size and Default Values
When space for an array is allocated, the array size must be given, specifying the number of elements that can be stored in it. The size of an array cannot be changed after the array is created. Size can be obtained using `arrayRefVar.length`. For example, `myList.length` is 10.

When an array is created, its elements are assigned the default value of 0 for the numeric primitive data types, \\u0000 for `char` types, and `false` for `boolean` types.

7.2.4 Accessing Array Elements
The array elements are accessed through the index. Array indices are 0 based; that is, they range from 0 to `arrayRefVar.length-1`. In the example in Figure 7.1, `myList` holds ten `double` values, and the indices are from 0 to 9.

Each element in the array is represented using the following syntax, known as an indexed variable:

```
arrayRefVar[index];
```

For example, `myList[9]` represents the last element in the array `myList`.

Caution
Some programming languages use parentheses to reference an array element, as in `myList[9]`, but Java uses brackets, as in `myList[9]`.

An indexed variable can be used in the same way as a regular variable. For example, the following code adds the values in `myList[0]` and `myList[1]` to `myList[2]`.

```
myList[2] = myList[0] + myList[1];
```

The following loop assigns 0 to `myList[0]`, 1 to `myList[1]`, ..., and 9 to `myList[9]`:

```
for (int i = 0; i < myList.length; i++) {
    myList[i] = i;
}
```

7.2.5 Array Initializers
Java has a shorthand notation, known as the array initializer, which combines the declaration, creation, and initialization of an array in one statement using the following syntax:

```
elementType[] arrayRefVar = {value0, value1, ..., valuek};
```

For example, the statement

```
double[] myList = {1.9, 2.9, 3.4, 3.5};
```
declares, creates, and initializes the array `myList` with four elements, which is equivalent to the following statements:

```
double[] myList = new double[4];
myList[0] = 1.9;
myList[1] = 2.9;
```
7.2 Array Basics

Caution
The **new** operator is not used in the array-initializer syntax. Using an array initializer, you have to declare, create, and initialize the array all in one statement. Splitting it would cause a syntax error. Thus, the next statement is wrong:

```java
double[] myList;
myList = {1.9, 2.9, 3.4, 3.5};
```

7.2.6 Processing Arrays

When processing array elements, you will often use a **for** loop—for two reasons:

- All of the elements in an array are of the same type. They are evenly processed in the same fashion repeatedly using a loop.
- Since the size of the array is known, it is natural to use a **for** loop.

Assume the array is created as follows:

```java
double[] myList = new double[10];
```

The following are some examples of processing arrays.

1. **Initializing arrays with input values:** The following loop initializes the array `myList` with user input values.

   ```java
   java.util.Scanner input = new java.util.Scanner(System.in);
   System.out.print("Enter " + myList.length + " values: ");
   for (int i = 0; i < myList.length; i++)
   myList[i] = input.nextDouble();
   ```

2. **Initializing arrays with random values:** The following loop initializes the array `myList` with random values between 0.0 and 100.0, but less than 100.0.

   ```java
   for (int i = 0; i < myList.length; i++) {
   myList[i] = Math.random() * 100;
   }
   ```

3. **Displaying arrays:** To print an array, you have to print each element in the array using a loop like the following:

   ```java
   for (int i = 0; i < myList.length; i++)
   System.out.print(myList[i] + " ");
   ```

   **Tip**
   For an array of the `char[]` type, it can be printed using one print statement. For example, the following code displays **Dallas**:

   ```java
   char[] city = {'D', 'a', 'l', 'l', 'a', 's'};
   System.out.println(city);
   ```

4. **Summing all elements:** Use a variable named `total` to store the sum. Initially `total` is 0. Add each element in the array to `total` using a loop like this:

   ```java
double total = 0;
for (int i = 0; i < myList.length; i++) {
   total += myList[i];
}
5. **Finding the largest element:** Use a variable named `max` to store the largest element. Initially `max` is `myList[0]`. To find the largest element in the array `myList`, compare each element with `max`, and update `max` if the element is greater than `max`.

   ```java
double max = myList[0];
for (int i = 1; i < myList.length; i++) {
    if (myList[i] > max) max = myList[i];
}
```

6. **Finding the smallest index of the largest element:** Often you need to locate the largest element in an array. If an array has multiple elements with the same largest value, find the smallest index of such an element. Suppose the array `myList` is `{1, 5, 3, 4, 5, 5}`. The largest element is `5` and the smallest index for `5` is `1`. Use a variable named `max` to store the largest element and a variable named `indexOfMax` to denote the index of the largest element. Initially `max` is `myList[0]`, and `indexOfMax` is `0`. Compare each element in `myList` with `max`, and update `max` and `indexOfMax` if the element is greater than `max`.

   ```java
double max = myList[0];
int indexOfMax = 0;
for (int i = 1; i < myList.length; i++) {
    if (myList[i] > max) {
        max = myList[i];
        indexOfMax = i;
    }
}
```

7. **Random shuffling:** In many applications, you need to randomly reorder the elements in an array. This is called shuffling. To accomplish this, for each element `myList[i]`, randomly generate an index `j` and swap `myList[i]` with `myList[j]`, as follows:

   ```java
for (int i = myList.length - 1; i > 0; i--) {
    int j = (int)(Math.random() * (i + 1));
    // Swap myList[i] with myList[j]
    double temp = myList[i];
    myList[i] = myList[j];
    myList[j] = temp;
}
```

8. **Shifting elements:** Sometimes you need to shift the elements left or right. Here is an example of shifting the elements one position to the left and filling the last element with the first element:

   ```java
double temp = myList[0]; // Retain the first element

// Shift elements left
for (int i = 1; i < myList.length; i++) {
    myList[i - 1] = myList[i];
}

// Move the first element to fill in the last position
myList[myList.length - 1] = temp;
```

9. **Simplifying coding:** Arrays can be used to greatly simplify coding for certain tasks. For example, suppose you wish to obtain the English name of a given month by its number. If the month names are stored in an array, the month name for a given month can be
accessed simply via the index. The following code prompts the user to enter a month number and displays its month name:

```java
String[] months = {"January", "February", ..., "December"};
System.out.print("Enter a month number (1 to 12): ");
int monthNumber = input.nextInt();
System.out.println("The month is " + months[monthNumber - 1]);
```

If you didn’t use the `months` array, you would have to determine the month name using a lengthy multi-way `if-else` statement as follows:

```java
if (monthNumber == 1)
    System.out.println("The month is January");
else if (monthNumber == 2)
    System.out.println("The month is February");
...
else
    System.out.println("The month is December");
```

### 7.2.7 Foreach Loops

Java supports a convenient `for` loop, known as a `foreach loop`, which enables you to traverse the array sequentially without using an index variable. For example, the following code displays all the elements in the array `myList`:

```java
for (double e: myList) {
    System.out.println(e);
}
```

You can read the code as “for each element `e` in `myList`, do the following.” Note that the variable, `e`, must be declared as the same type as the elements in `myList`.

In general, the syntax for a foreach loop is

```java
for (elementType element: arrayRefVar) {
    // Process the element
}
```

You still have to use an index variable if you wish to traverse the array in a different order or change the elements in the array.

#### Caution

Accessing an array out of bounds is a common programming error that throws a runtime `ArrayIndexOutOfBoundsException`. To avoid it, make sure that you do not use an index beyond `arrayRefVar.length - 1`.

Programmers often mistakenly reference the first element in an array with index `1`, but it should be `0`. This is called the off-by-one error. Another common off-by-one error in a loop is using `<=` where `<` should be used. For example, the following loop is wrong.

```java
for (int i = 0; i <= list.length; i++)
    System.out.print(list[i] + " ");
```

The `<=` should be replaced by `<`.

### Check Point

**7.1** How do you declare an array reference variable and how do you create an array?

**7.2** When is the memory allocated for an array?
7.3 What is the output of the following code?

```java
int x = 30;
int[] numbers = new int[x];
x = 60;
System.out.println("x is " + x);
System.out.println("The size of numbers is " + numbers.length);
```

7.4 Indicate true or false for the following statements:

- Every element in an array has the same type. **true**
- The array size is fixed after an array reference variable is declared. **false**
- The array size is fixed after it is created. **true**
- The elements in an array must be a primitive data type. **false**

7.5 Which of the following statements are valid?

```java
int i = new int(30);
double d[] = new double[30];
char[] r = new char[1..30];
int i[] = (3, 4, 3, 2);
float f[] = {2.3, 4.5, 6.6};
char[] c = new char();
```

7.6 How do you access elements in an array?

7.7 What is the array index type? What is the lowest index? What is the representation of the third element in an array named `a`?

7.8 Write statements to do the following:

a. Create an array to hold 10 double values.
b. Assign the value 5.5 to the last element in the array.
c. Display the sum of the first two elements.
d. Write a loop that computes the sum of all elements in the array.
e. Write a loop that finds the minimum element in the array.
f. Randomly generate an index and display the element of this index in the array.
g. Use an array initializer to create another array with the initial values 3.5, 5.5, 4.52, and 5.6.

7.9 What happens when your program attempts to access an array element with an invalid index?

7.10 Identify and fix the errors in the following code:

```java
public class Test {
    public static void main(String[] args) {
        double[100] r;
        for (int i = 0; i < r.length(); i++);
        r(i) = Math.random * 100;
    }
}
```

7.11 What is the output of the following code?

```java
public class Test {
    public static void main(String[] args) {
        int list[] = {1, 2, 3, 4, 5, 6};
    }
```
7.3 Case Study: Analyzing Numbers

The problem is to write a program that finds the number of items above the average of all items.

Now you can write a program using arrays to solve the problem proposed at the beginning of this chapter. The problem is to read 100 numbers, get the average of these numbers, and find the number of the items greater than the average. To be flexible for handling any number of input, we will let the user enter the number of input, rather than fixing it to 100. Listing 7.1 gives a solution.

LISTING 7.1 AnalyzeNumbers.java

```java
public class AnalyzeNumbers {
    public static void main(String[] args) {
        java.util.Scanner input = new java.util.Scanner(System.in);
        System.out.print("Enter the number of items: ");
        int n = input.nextInt();
        double[] numbers = new double[n];
        double sum = 0;
        System.out.print("Enter the numbers: ");
        for (int i = 0; i < n; i++) {
            numbers[i] = input.nextDouble();
            sum += numbers[i];
        }
        double average = sum / n;
        int count = 0; // The number of elements above average
        for (int i = 0; i < n; i++)
            if (numbers[i] > average)
                count++;
        System.out.println("Average is "+average);
        System.out.println("Number of elements above the average is "+count);
    }
}
```

The program prompts the user to enter the array size (line 5) and creates an array with the specified size (line 6). The program reads the input, stores numbers into the array (line 11), adds each number to `sum` in line 11, and obtains the average (line 15). It then compares
each number in the array with the average to count the number of values above the average (lines 17–20).

### 7.4 Case Study: Deck of Cards

*The problem is to create a program that will randomly select four cards from a deck of cards.*

Say you want to write a program that will pick four cards at random from a deck of 52 cards. All the cards can be represented using an array named `deck`, filled with initial values 0 to 51, as follows:

```java
int[] deck = new int[52];
```

```java
// Initialize cards
for (int i = 0; i < deck.length; i++)
    deck[i] = i;
```

Card numbers 0 to 12, 13 to 25, 26 to 38, and 39 to 51 represent 13 Spades, 13 Hearts, 13 Diamonds, and 13 Clubs, respectively, as shown in Figure 7.2. `cardNumber / 13` determines the suit of the card and `cardNumber % 13` determines the rank of the card, as shown in Figure 7.3. After shuffling the array `deck`, pick the first four cards from `deck`. The program displays the cards from these four card numbers.

**Figure 7.2** 52 cards are stored in an array named `deck`.

**Figure 7.3** `CardNumber` identifies a card's suit and rank number.
Listing 7.2 gives the solution to the problem.

**LISTING 7.2 DeckOfCards.java**

```java
public class DeckOfCards {
    public static void main(String[] args) {
        int[] deck = new int[52]; create array deck
        String[] suits = {"Spades", "Hearts", "Diamonds", "Clubs"}; array of strings
        String[] ranks = {"Ace", "2", "3", "4", "5", "6", "7", "8", "9", "10", "Jack", "Queen", "King"}; array of strings

        // Initialize the cards
        for (int i = 0; i < deck.length; i++) initialize deck
            deck[i] = i;

        // Shuffle the cards
        for (int i = 0; i < deck.length; i++) shuffle deck
            int index = (int)(Math.random() * deck.length);
            int temp = deck[i];
            deck[i] = deck[index];
            deck[index] = temp;

        // Display the first four cards
        for (int i = 0; i < 4; i++) suit of a card
            String suit = suits[deck[i] / 13];
            String rank = ranks[deck[i] % 13]; rank of a card
            System.out.println("Card number " + deck[i] + ": ");
            System.out.println("" + rank + " of " + suit);
    }
}
```

The program creates an array `suits` for four suits (line 4) and an array `ranks` for 13 cards in a suit (lines 5–6). Each element in these arrays is a string. The program initializes `deck` with values 0 to 51 in lines 9–10. The `deck` value 0 represents the card Ace of Spades, 1 represents the card 2 of Spades, 13 represents the card Ace of Hearts, and 14 represents the card 2 of Hearts.

Lines 13–19 randomly shuffle the deck. After a deck is shuffled, `deck[i]` contains an arbitrary value. `deck[i] / 13` is 0, 1, 2, or 3, which determines the suit (line 23). `deck[i] % 13` is a value between 0 and 12, which determines the rank (line 24). If the `suits` array is not defined, you would have to determine the suit using a lengthy multi-way `if-else` statement as follows:

```java
if (deck[i] / 13 == 0)
    System.out.print("suit is Spades");
else if (deck[i] / 13 == 1)
    System.out.print("suit is Hearts");
else if (deck[i] / 13 == 2)
    System.out.print("suit is Diamonds");
else
    System.out.print("suit is Clubs");
```

7.12 Will the program pick four random cards if you replace lines 22–27 in Listing 7.2 DeckOfCards.java with the following code?

```java
for (int i = 0; i < 4; i++) {
    int cardNumber = (int)(Math.random() * deck.length);
    String suit = suits[cardNumber / 13];
    String rank = ranks[cardNumber % 13];
    System.out.println("Card number "+ cardNumber + ": "+ rank + " of " + suit);
}
```

7.5 Copying Arrays

To copy the contents of one array into another, you have to copy the array’s individual elements into the other array.

Often, in a program, you need to duplicate an array or a part of an array. In such cases you could attempt to use the assignment statement (=), as follows:

```java
list2 = list1;
```

However, this statement does not copy the contents of the array referenced by `list1` to `list2`, but instead merely copies the reference value from `list1` to `list2`. After this statement, `list1` and `list2` reference the same array, as shown in Figure 7.4. The array previously referenced by `list2` is no longer referenced; it becomes garbage, which will be automatically collected by the Java Virtual Machine (this process is called garbage collection).

In Java, you can use assignment statements to copy primitive data type variables, but not arrays. Assigning one array variable to another array variable actually copies one reference to another and makes both variables point to the same memory location.

There are three ways to copy arrays:

- Use a loop to copy individual elements one by one.
- Use the static `arraycopy` method in the `System` class.
- Use the `clone` method to copy arrays; this will be introduced in Chapter 13, Abstract Classes and Interfaces.
You can write a loop to copy every element from the source array to the corresponding element in the target array. The following code, for instance, copies `sourceArray` to `targetArray` using a `for` loop.

```java
int[] sourceArray = {2, 3, 1, 5, 10};
int[] targetArray = new int[sourceArray.length];
for (int i = 0; i < sourceArray.length; i++) {
    targetArray[i] = sourceArray[i];
}
```

Another approach is to use the `arraycopy` method in the `java.lang.System` class to copy arrays instead of using a loop. The syntax for `arraycopy` is:

```java
arraycopy(sourceArray, srcPos, targetArray, tarPos, length);
```

The parameters `srcPos` and `tarPos` indicate the starting positions in `sourceArray` and `targetArray`, respectively. The number of elements copied from `sourceArray` to `targetArray` is indicated by `length`. For example, you can rewrite the loop using the following statement:

```java
System.arraycopy(sourceArray, 0, targetArray, 0, sourceArray.length);
```

The `arraycopy` method does not allocate memory space for the target array. The target array must have already been created with its memory space allocated. After the copying takes place, `targetArray` and `sourceArray` have the same content but independent memory locations.

**Note**
The `arraycopy` method violates the Java naming convention. By convention, this method should be named `arrayCopy` (i.e., with an uppercase C).

7.13 Use the `arraycopy` method to copy the following array to a target array `t`:

```java
int[] source = {3, 4, 5};
```

7.14 Once an array is created, its size cannot be changed. Does the following code resize the array?

```java
int[] myList;
myList = new int[10];
// Sometime later you want to assign a new array to myList
myList = new int[20];
```

7.6 Passing Arrays to Methods

*When passing an array to a method, the reference of the array is passed to the method.*

Just as you can pass primitive type values to methods, you can also pass arrays to methods. For example, the following method displays the elements in an `int` array:

```java
public static void printArray(int[] array) {
    for (int i = 0; i < array.length; i++) {
        System.out.print(array[i] + " ");
    }
}
```

You can invoke it by passing an array. For example, the following statement invokes the `printArray` method to display 3, 1, 2, 6, 4, and 2.

```java
printArray(new int[]{3, 1, 2, 6, 4, 2});
```
The preceding statement creates an array using the following syntax:

```java
new elementType[]{value0, value1, ..., valuek};
```

**Note**

There is no explicit reference variable for the array. Such array is called an **anonymous array**.

Java uses **pass-by-value** to pass arguments to a method. There are important differences between passing the values of variables of primitive data types and passing arrays.

- For an argument of a primitive type, the argument’s value is passed.
- For an argument of an array type, the value of the argument is a reference to an array; this reference value is passed to the method. Semantically, it can be best described as **pass-by-sharing**, that is, the array in the method is the same as the array being passed. Thus, if you change the array in the method, you will see the change outside the method.

Take the following code, for example:

```java
public class Test {
    public static void main(String[] args) {
        int x = 1; // x represents an int value
        int[] y = new int[10]; // y represents an array of int values
        m(x, y); // Invoke m with arguments x and y
        System.out.println("x is " + x);
        System.out.println("y[0] is " + y[0]);
    }

    public static void m(int number, int[] numbers) {
        number = 1001; // Assign a new value to number
        numbers[0] = 5555; // Assign a new value to numbers[0]
    }
}
```

You may wonder why after `m` is invoked, `x` remains `1`, but `y[0]` become `5555`. This is because `y` and `numbers`, although they are independent variables, reference the same array, as illustrated in Figure 7.5. When `m(x, y)` is invoked, the values of `x` and `y` are passed to `number` and `numbers`. Since `y` contains the reference value to the array, `numbers` now contains the same reference value to the same array.

**Figure 7.5** The primitive type value in `x` is passed to `number`, and the reference value in `y` is passed to `numbers`. 
Note

Arrays are objects in Java (objects are introduced in Chapter 9). The JVM stores the objects in an area of memory called the heap, which is used for dynamic memory allocation.

Listing 7.3 gives another program that shows the difference between passing a primitive data type value and an array reference variable to a method.

The program contains two methods for swapping elements in an array. The first method, named swap, fails to swap two int arguments. The second method, named swapFirstTwoInArray, successfully swaps the first two elements in the array argument.

Listing 7.3 TestPassArray.java

```java
public class TestPassArray {
    // Main method */
    public static void main(String[] args) {
        int[] a = {1, 2};

        // Swap elements using the swap method
        System.out.println("Before invoking swap");
        System.out.println("array is {" + a[0] + ", " + a[1] + "}");
        swap(a[0], a[1]);
        System.out.println("After invoking swap");
        System.out.println("array is {" + a[0] + ", " + a[1] + "}");

        // Swap elements using the swapFirstTwoInArray method
        System.out.println("Before invoking swapFirstTwoInArray");
        System.out.println("array is {" + a[0] + ", " + a[1] + "}");
        swapFirstTwoInArray(a);
        System.out.println("After invoking swapFirstTwoInArray");
        System.out.println("array is {" + a[0] + ", " + a[1] + "}");
    }

    /** Swap two variables */
    public static void swap(int n1, int n2) {
        int temp = n1;
        n1 = n2;
        n2 = temp;
    }

    /** Swap the first two elements in the array */
    public static void swapFirstTwoInArray(int[] array) {
        int temp = array[0];
        array[0] = array[1];
        array[1] = temp;
    }
}
```

Before invoking swap
array is {1, 2}
After invoking swap
array is {1, 2}
Before invoking swapFirstTwoInArray
array is {1, 2}
After invoking swapFirstTwoInArray
array is {2, 1}
As shown in Figure 7.6, the two elements are not swapped using the `swap` method. However, they are swapped using the `swapFirstTwoInArray` method. Since the parameters in the `swap` method are primitive type, the values of `a[0]` and `a[1]` are passed to `n1` and `n2` inside the method when invoking `swap(a[0], a[1])`. The memory locations for `n1` and `n2` are independent of the ones for `a[0]` and `a[1]`. The contents of the array are not affected by this call.

![Figure 7.6](image)

**Figure 7.6** When passing an array to a method, the reference of the array is passed to the method.

The parameter in the `swapFirstTwoInArray` method is an array. As shown in Figure 7.6, the reference of the array is passed to the method. Thus the variables `a` (outside the method) and `array` (inside the method) both refer to the same array in the same memory location. Therefore, swapping `array[0]` with `array[1]` inside the method `swapFirstTwoInArray` is the same as swapping `a[0]` with `a[1]` outside of the method.

### 7.7 Returning an Array from a Method

*When a method returns an array, the reference of the array is returned.*

You can pass arrays when invoking a method. A method may also return an array. For example, the following method returns an array that is the reversal of another array.

```java
public static int[] reverse(int[] list) {
    int[] result = new int[list.length];
    for (int i = 0, j = result.length - 1; i < list.length; i++, j--)
        result[j] = list[i];
    return result;
}
```

Line 2 creates a new array `result`. Lines 4–7 copy elements from array `list` to array `result`. Line 9 returns the array. For example, the following statement returns a new array `list2` with elements 6, 5, 4, 3, 2, 1.

```java
int[] list1 = {1, 2, 3, 4, 5, 6};
int[] list2 = reverse(list1);
```
7.15 Suppose the following code is written to reverse the contents in an array, explain why it is wrong. How do you fix it?

```java
int[] list = {1, 2, 3, 5, 4};
for (int i = 0, j = list.length - 1; i < list.length; i++, j--) {
    int temp = list[i];
    list[i] = list[j];
    list[j] = temp;
}
```

7.8 Case Study: Counting the Occurrences of Each Letter

This section presents a program to count the occurrences of each letter in an array of characters.

The program given in Listing 7.4 does the following:

1. Generates 100 lowercase letters randomly and assigns them to an array of characters, as shown in Figure 7.7a. You can obtain a random letter by using the `getRandomLowerCaseLetter()` method in the `RandomCharacter` class in Listing 6.10.

2. Count the occurrences of each letter in the array. To do so, create an array, say `counts`, of 26 int values, each of which counts the occurrences of a letter, as shown in Figure 7.7b. That is, `counts[0]` counts the number of a’s, `counts[1]` counts the number of b’s, and so on.

![Figure 7.7](image)

**Figure 7.7** The `chars` array stores 100 characters, and the `counts` array stores 26 counts, each of which counts the occurrences of a letter.

**Listing 7.4 CountLettersInArray.java**

```java
public class CountLettersInArray {
    /** Main method */
    public static void main(String[] args) {
        // Declare and create an array
        char[] chars = createArray();
        // Display the array
        System.out.println("The lowercase letters are:");
        displayArray(chars);
    }
}
```
// Count the occurrences of each letter
int[] counts = countLetters(chars);

// Display counts
System.out.println();
System.out.println("The occurrences of each letter are:");
displayCounts(counts);

/** Create an array of characters */
public static char[] createArray() {
    // Declare an array of characters and create it
    char[] chars = new char[100];

    // Create lowercase letters randomly and assign
    // them to the array
    for (int i = 0; i < chars.length; i++)
        chars[i] = RandomCharacter.getRandomLowerCaseLetter();

    // Return the array
    return chars;
}

/** Display the array of characters */
public static void displayArray(char[] chars) {
    // Display the characters in the array 20 on each line
    for (int i = 0; i < chars.length; i++) {
        if ((i + 1) % 20 == 0)
            System.out.println(chars[i]);
        else
            System.out.print(chars[i] + " ");
    }
}

/** Count the occurrences of each letter */
public static int[] countLetters(char[] chars) {
    // Declare and create an array of 26 int
    int[] counts = new int[26];

    // For each lowercase letter in the array, count it
    for (int i = 0; i < chars.length; i++)
        counts[chars[i] - 'a']++;

    return counts;
}

/** Display counts */
public static void displayCounts(int[] counts) {
    for (int i = 0; i < counts.length; i++) {
        if ((i + 1) % 10 == 0)
            System.out.println(counts[i] + " " + (char)(i + 'a'));
        else
            System.out.print(counts[i] + " " + (char)(i + 'a') + " ");
    }
}
The `createArray` method (lines 21–32) generates an array of 100 random lowercase letters. Line 5 invokes the method and assigns the array to `chars`. What would be wrong if you rewrote the code as follows?

```java
char[] chars = new char[100];
chars = createArray();
```

You would be creating two arrays. The first line would create an array by using `new char[100]`. The second line would create an array by invoking `createArray()` and assign the reference of the array to `chars`. The array created in the first line would be garbage because it is no longer referenced, and as mentioned earlier Java automatically collects garbage behind the scenes. Your program would compile and run correctly, but it would create an array unnecessarily.

Invoking `getRandomLowerCaseLetter()` (line 28) returns a random lowercase letter. This method is defined in the `RandomCharacter` class in Listing 6.10.

The `countLetters` method (lines 46–55) returns an array of 26 int values, each of which stores the number of occurrences of a letter. The method processes each letter in the array and increases its count by one. A brute-force approach to count the occurrences of each letter might be as follows:

```java
for (int i = 0; i < chars.length; i++)
    if (chars[i] == 'a')
        counts[0]++;
    else if (chars[i] == 'b')
        counts[1]++;
    ...
```

But a better solution is given in lines 51–52.

```java
for (int i = 0; i < chars.length; i++)
    counts[chars[i] - 'a']++;
```

If the letter (`chars[i]`) is `a`, the corresponding count is `counts['a' - 'a']` (i.e., `counts[0]`). If the letter is `b`, the corresponding count is `counts['b' - 'a']` (i.e., `counts[1]`), since the Unicode of `b` is one more than that of `a`. If the letter is `z`, the corresponding count is `counts['z' - 'a']` (i.e., `counts[25]`), since the Unicode of `z` is 25 more than that of `a`.

Figure 7.8 shows the call stack and heap during and after executing `createArray`. See Checkpoint Question 7.18 to show the call stack and heap for other methods in the program.
7.16 True or false? When an array is passed to a method, a new array is created and passed to the method.

7.17 Show the output of the following two programs:

```java
public class Test {
    public static void main(String[] args) {
        int[] numbers = new int[1];
        m(number, numbers);
        System.out.println("number is "+ number + " and numbers[0] is "+ numbers[0]);
    }

    public static void m(int x, int[] y) {
        y[0] = 3;
    }
}
```

```java
public class Test {
    public static void main(String[] args) {
        int[] list = {1, 2, 3, 4, 5};
        reverse(list);
        for (int i = 0; i < list.length; i++)
            System.out.print(list[i] + " ");
    }

    public static void reverse(int[] list) {
        int[] newList = new int[list.length];
        for (int i = 0; i < list.length; i++)
            newList[i] = list[list.length - 1 - i];
        list = newList;
    }
}
```

7.18 Where are the arrays stored during execution? Show the contents of the stack and heap during and after executing `displayArray`, `countLetters`, `displayCounts` in Listing 7.4.

### 7.9 Variable-Length Argument Lists

A variable number of arguments of the same type can be passed to a method and treated as an array.

You can pass a variable number of arguments of the same type to a method. The parameter in the method is declared as follows:

```
typeName... parameterName
```

In the method declaration, you specify the type followed by an ellipsis (...). Only one variable-length parameter may be specified in a method, and this parameter must be the last parameter. Any regular parameters must precede it.
Java treats a variable-length parameter as an array. You can pass an array or a variable number of arguments to a variable-length parameter. When invoking a method with a variable number of arguments, Java creates an array and passes the arguments to it. Listing 7.5 contains a method that prints the maximum value in a list of an unspecified number of values.

**Listing 7.5 VarArgsDemo.java**

```java
public class VarArgsDemo {
    public static void main(String[] args) {
        printMax(34, 3, 3, 2, 56.5);
        printMax(new double[]{1, 2, 3});
    }

    public static void printMax(double... numbers) {
        if (numbers.length == 0) {
            System.out.println("No argument passed");
            return;
        }
        double result = numbers[0];
        for (int i = 1; i < numbers.length; i++)
            if (numbers[i] > result) result = numbers[i];
        System.out.println("The max value is "+ result);
    }
}
```

Line 3 invokes the `printMax` method with a variable-length argument list passed to the array `numbers`. If no arguments are passed, the length of the array is 0 (line 8).

Line 4 invokes the `printMax` method with an array.

7.19 What is wrong in the following method header?

- `public static void print(String... strings, double... numbers)`
- `public static void print(double... numbers, String name)`
- `public static double... print(double d1, double d2)`

7.20 Can you invoke the `printMax` method in Listing 7.5 using the following statements?

- `printMax(1, 2, 2, 1, 4);`
- `printMax(new double[]{1, 2, 3});`
- `printMax(new int[]{1, 2, 3});`

### 7.10 Searching Arrays

If an array is sorted, binary search is more efficient than linear search for finding an element in the array.

Searching is the process of looking for a specific element in an array—for example, discovering whether a certain score is included in a list of scores. Searching is a common task in computer programming. Many algorithms and data structures are devoted to searching. This section discusses two commonly used approaches, linear search and binary search.

#### 7.10.1 The Linear Search Approach

The linear search approach compares the key element `key` sequentially with each element in the array. It continues to do so until the key matches an element in the array or the array is exhausted without a match being found. If a match is made, the linear search returns the index...
of the element in the array that matches the key. If no match is found, the search returns -1.
The `linearSearch` method in Listing 7.6 gives the solution.

**LISTING 7.6 LinearSearch.java**

```java
class LinearSearch {
    /** The method for finding a key in the list */
    public static int linearSearch(int[] list, int key) {
        for (int i = 0; i < list.length; i++) {
            if (key == list[i])
                return i;
        }
        return -1;
    }
}
```

To better understand this method, trace it with the following statements:

```java
int[] list = {1, 4, 4, 2, 5, -3, 6, 2};
int i = linearSearch(list, 4); // Returns 1
int j = linearSearch(list, -4); // Returns -1
int k = linearSearch(list, -3); // Returns 5
```

The linear search method compares the key with each element in the array. The elements can be in any order. On average, the algorithm will have to examine half of the elements in an array before finding the key, if it exists. Since the execution time of a linear search increases linearly as the number of array elements increases, linear search is inefficient for a large array.

### 7.10.2 The Binary Search Approach

Binary search is the other common search approach for a list of values. For binary search to work, the elements in the array must already be ordered. Assume that the array is in ascending order. The binary search first compares the key with the element in the middle of the array. Consider the following three cases:

- If the key is less than the middle element, you need to continue to search for the key only in the first half of the array.
- If the key is equal to the middle element, the search ends with a match.
- If the key is greater than the middle element, you need to continue to search for the key only in the second half of the array.

Clearly, the binary search method eliminates at least half of the array after each comparison. Sometimes you eliminate half of the elements, and sometimes you eliminate half plus one. Suppose that the array has \( n \) elements. For convenience, let \( n \) be a power of 2. After the first comparison, \( n/2 \) elements are left for further search; after the second comparison, \( (n/2)/2 \) elements are left. After the \( k \)th comparison, \( n/2^k \) elements are left for further search. When \( k = \log_2 n \), only one element is left in the array, and you need only one more comparison. Therefore, in the worst case when using the binary search approach, you need \( \log_2 n + 1 \) comparisons to find an element in the sorted array. In the worst case for a list of 1024 (\( 2^{10} \)) elements, binary search requires only 11 comparisons, whereas a linear search requires 1023 comparisons in the worst case.

The portion of the array being searched shrinks by half after each comparison. Let \( \text{low} \) and \( \text{high} \) denote, respectively, the first index and last index of the array that is currently being searched. Initially, \( \text{low} \) is 0 and \( \text{high} \) is \( \text{list.length} - 1 \). Let \( \text{mid} \) denote the index of the middle element, so \( \text{mid} = (\text{low} + \text{high})/2 \). Figure 7.9 shows how to find key 11 in the list \( \{2, 4, 7, 10, 11, 45, 50, 59, 60, 66, 69, 70, 79\} \) using binary search.
You now know how the binary search works. The next task is to implement it in Java. Don’t rush to give a complete implementation. Implement it incrementally, one step at a time. You may start with the first iteration of the search, as shown in Figure 7.10a. It compares the key with the middle element in the list whose low index is 0 and high index is list.length - 1. If key < list[mid], set the high index to mid - 1; if key == list[mid], a match is found and return mid; if key > list[mid], set the low index to mid + 1.

Next consider implementing the method to perform the search repeatedly by adding a loop, as shown in Figure 7.10b. The search ends if the key is found, or if the key is not found when low > high.

When the key is not found, low is the insertion point where a key would be inserted to maintain the order of the list. It is more useful to return the insertion point than -1. The method must return a negative value to indicate that the key is not in the list. Can it simply return -low? No. If the key is less than list[0], low would be 0. -0 is 0. This would indicate that the key matches list[0]. A good choice is to let the method return -low - 1 if the key is not in the list. Returning -low - 1 indicates not only that the key is not in the list, but also where the key would be inserted.

![Figure 7.9](image.png)

**Figure 7.9** Binary search eliminates half of the list from further consideration after each comparison.

```java
public static int binarySearch(int[] list, int key) {
    int low = 0;
    int high = list.length - 1;

    int mid = (low + high) / 2;
    if (key < list[mid])
        high = mid - 1;
    else if (key == list[mid])
        return mid;
    else
        low = mid + 1;

    return -1; // Not found
}
```

(a) Version 1

```java
public static int binarySearch(int[] list, int key) {
    int low = 0;
    int high = list.length - 1;

    while (high >= low) {
        int mid = (low + high) / 2;
        if (key < list[mid])
            high = mid - 1;
        else if (key == list[mid])
            return mid;
        else
            low = mid + 1;
    }

    return -1; // Not found
}
```

(b) Version 2

**Figure 7.10** Binary search is implemented incrementally.
The complete program is given in Listing 7.7.

**Listing 7.7  BinarySearch.java**

```java
public class BinarySearch {
    /** Use binary search to find the key in the list */
    public static int binarySearch(int[] list, int key) {
        int low = 0;
        int high = list.length - 1;
        while (high >= low) {
            int mid = (low + high) / 2;
            if (key < list[mid])
                high = mid - 1;
            else if (key == list[mid])
                return mid;
            else
                low = mid + 1;
        }
        return -low - 1;  // Now high < low, key not found
    }
}
```

The binary search returns the index of the search key if it is contained in the list (line 12). Otherwise, it returns \(-low - 1\) (line 17).

What would happen if we replaced \((high >= low)\) in line 7 with \((high > low)\)? The search would miss a possible matching element. Consider a list with just one element. The search would miss the element.

Does the method still work if there are duplicate elements in the list? Yes, as long as the elements are sorted in increasing order. The method returns the index of one of the matching elements if the element is in the list.

To better understand this method, trace it with the following statements and identify \(\text{low}\) and \(\text{high}\) when the method returns.

```java
int[] list = {2, 4, 7, 10, 11, 45, 50, 59, 60, 66, 69, 70, 79};
int i = BinarySearch.binarySearch(list, 2); // Returns 0
int j = BinarySearch.binarySearch(list, 11); // Returns 4
int k = BinarySearch.binarySearch(list, 12); // Returns -6
int l = BinarySearch.binarySearch(list, 1); // Returns -1
int m = BinarySearch.binarySearch(list, 3); // Returns -2
```

Here is the table that lists the \(\text{low}\) and \(\text{high}\) values when the method exits and the value returned from invoking the method.

<table>
<thead>
<tr>
<th>Method</th>
<th>Low</th>
<th>High</th>
<th>Value Returned</th>
</tr>
</thead>
<tbody>
<tr>
<td>binarySearch(list, 2)</td>
<td>0</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>binarySearch(list, 11)</td>
<td>3</td>
<td>5</td>
<td>4</td>
</tr>
<tr>
<td>binarySearch(list, 12)</td>
<td>5</td>
<td>4</td>
<td>-6</td>
</tr>
<tr>
<td>binarySearch(list, 1)</td>
<td>0</td>
<td>-1</td>
<td>-1</td>
</tr>
<tr>
<td>binarySearch(list, 3)</td>
<td>1</td>
<td>0</td>
<td>-2</td>
</tr>
</tbody>
</table>

**Note**

Linear search is useful for finding an element in a small array or an unsorted array, but it is inefficient for large arrays. Binary search is more efficient, but it requires that the array be presorted.
7.21 If high is a very large integer such as the maximum int value 2147483647, \((\text{low} + \text{high})/2\) may cause overflow. How do you fix it to avoid overflow?

7.22 Use Figure 7.9 as an example to show how to apply the binary search approach to a search for key 10 and key 12 in list \(\{2, 4, 7, 10, 11, 45, 50, 59, 60, 66, 69, 70, 79\}\).

7.23 If the binary search method returns -4, is the key in the list? Where should the key be inserted if you wish to insert the key into the list?

7.11 Sorting Arrays

Sorting, like searching, is a common task in computer programming. Many different algorithms have been developed for sorting. This section introduces an intuitive sorting algorithm: selection sort.

Suppose that you want to sort a list in ascending order. Selection sort finds the smallest number in the list and swaps it with the first element. It then finds the smallest number remaining and swaps it with the second element, and so on, until only a single number remains. Figure 7.11 shows how to sort the list \(\{2, 9, 5, 4, 8, 1, 6\}\) using selection sort.

You know how the selection-sort approach works. The task now is to implement it in Java. Beginners find it difficult to develop a complete solution on the first attempt. Start by writing the code for the first iteration to find the smallest element in the list and swap it with the first element, and then observe what would be different for the second iteration, the third, and so on. The insight this gives will enable you to write a loop that generalizes all the iterations.
The solution can be described as follows:

```java
for (int i = 0; i < list.length - 1; i++) {
    select the smallest element in list[i..list.length-1];
    swap the smallest with list[i], if necessary;
    // list[i] is in its correct position.
    // The next iteration applies on list[i+1..list.length-1]
}
```

Listing 7.8 implements the solution.

LISTING 7.8 SelectionSort.java

```java
public class SelectionSort {
    /** The method for sorting the numbers */
    public static void selectionSort(double[] list) {
        for (int i = 0; i < list.length - 1; i++) {
            // Find the minimum in the list[i..list.length-1]
            double currentMin = list[i];
            int currentMinIndex = i;

            for (int j = i + 1; j < list.length; j++) {
                if (currentMin > list[j]) {
                    currentMin = list[j];
                    currentMinIndex = j;
                }
            }

            // Swap list[i] with list[currentMinIndex] if necessary
            if (currentMinIndex != i) {
                list[currentMinIndex] = list[i];
                list[i] = currentMin;
            }
        }
    }
}
```

The `selectionSort(double[] list)` method sorts any array of `double` elements. The method is implemented with a nested `for` loop. The outer loop (with the loop control variable `i`) (line 4) is iterated in order to find the smallest element in the list, which ranges from `list[i]` to `list[list.length-1]`, and exchange it with `list[i]`.

The variable `i` is initially 0. After each iteration of the outer loop, `list[i]` is in the right place. Eventually, all the elements are put in the right place; therefore, the whole list is sorted.

To understand this method better, trace it with the following statements:

```java
double[] list = {1, 9, 4.5, 6.6, 5.7, -4.5};
SelectionSort.selectionSort(list);
```

7.24 Use Figure 7.11 as an example to show how to apply the selection-sort approach to sort `{3.4, 5.3, 3.5, 2.2, 1.9, 2}`.

7.25 How do you modify the `selectionSort` method in Listing 7.8 to sort numbers in decreasing order?

7.12 The Arrays Class

The `java.util.Arrays` class contains useful methods for common array operations such as sorting and searching.
The `java.util.Arrays` class contains various static methods for sorting and searching arrays, comparing arrays, filling array elements, and returning a string representation of the array. These methods are overloaded for all primitive types.

You can use the `sort` or `parallelSort` method to sort a whole array or a partial array. For example, the following code sorts an array of numbers and an array of characters.

```java
double[] numbers = {6.0, 4.4, 1.9, 2.9, 3.4, 3.5};
java.util.Arrays.sort(numbers); // Sort the whole array
java.util.Arrays.parallelSort(numbers); // Sort the whole array

char[] chars = {'a', 'A', '4', 'F', 'D', 'P'};
java.util.Arrays.sort(chars, 1, 3); // Sort part of the array
java.util.Arrays.parallelSort(chars, 1, 3); // Sort part of the array
```

Invoking `sort(numbers)` sorts the whole array `numbers`. Invoking `sort(chars, 1, 3)` sorts a partial array from `chars[1]` to `chars[3-1]`. `parallelSort` is more efficient if your computer has multiple processors.

You can use the `binarySearch` method to search for a key in an array. The array must be pre-sorted in increasing order. If the key is not in the array, the method returns `-(insertionIndex + 1)`. For example, the following code searches the keys in an array of integers and an array of characters.

```java
int[] list = {2, 4, 7, 10, 11, 45, 50, 59, 60, 66, 69, 70, 79};
System.out.println("1. Index is " + java.util.Arrays.binarySearch(list, 11));
System.out.println("2. Index is " + java.util.Arrays.binarySearch(list, 12));

char[] chars = {'a', 'c', 'g', 'x', 'y', 'z'};
System.out.println("3. Index is " + java.util.Arrays.binarySearch(chars, 'a'));
System.out.println("4. Index is " + java.util.Arrays.binarySearch(chars, 't'));
```

The output of the preceding code is

1. Index is 4
2. Index is -6
3. Index is 0
4. Index is -4

You can use the `equals` method to check whether two arrays are strictly equal. Two arrays are strictly equal if their corresponding elements are the same. In the following code, `list1` and `list2` are equal, but `list2` and `list3` are not.

```java
int[] list1 = {2, 4, 7, 10};
int[] list2 = {2, 4, 7, 10};
int[] list3 = {4, 2, 7, 10};
System.out.println(java.util.Arrays.equals(list1, list2)); // true
System.out.println(java.util.Arrays.equals(list2, list3)); // false
```

You can use the `fill` method to fill in all or part of the array. For example, the following code fills `list1` with 5 and fills `8` into elements `list2[1]` through `list2[5-1]`.

```java
int[] list1 = {2, 4, 7, 10};
int[] list2 = {2, 4, 7, 7, 10};
java.util.Arrays.fill(list1, 5); // Fill 5 to the whole array
java.util.Arrays.fill(list2, 1, 5, 8); // Fill 8 to a partial array
```
You can also use the `toString` method to return a string that represents all elements in the array. This is a quick and simple way to display all elements in the array. For example, the following code

```java
int[] list = {2, 4, 7, 10};
System.out.println(Arrays.toString(list));
```

displays `[2, 4, 7, 10]`.

### 7.26 Check Point
What types of array can be sorted using the `java.util.Arrays.sort` method? Does this `sort` method create a new array?

### 7.27 Check Point
To apply `java.util.Arrays.binarySearch(array, key)`, should the array be sorted in increasing order, in decreasing order, or neither?

### 7.28 Check Point
Show the output of the following code:

```java
int[] list1 = {2, 4, 7, 10};
java.util.Arrays.fill(list1, 7);
System.out.println(java.util.Arrays.toString(list1));

int[] list2 = {2, 4, 7, 10};
System.out.println(java.util.Arrays.toString(list2));
System.out.println(java.util.Arrays.equals(list1, list2));
```

### 7.13 Command-Line Arguments

*The main method can receive string arguments from the command line.*

Perhaps you have already noticed the unusual header for the `main` method, which has the parameter `args` of `String[]` type. It is clear that `args` is an array of strings. The `main` method is just like a regular method with a parameter. You can call a regular method by passing actual parameters. Can you pass arguments to `main`? Yes, of course you can. In the following examples, the `main` method in class `TestMain` is invoked by a method in `A`.

```java
public class A {
    public static void main(String[] args) {
        String[] strings = {"New York", "Boston", "Atlanta"};
        TestMain.main(strings);
    }
}
```

```java
public class TestMain {
    public static void main(String[] args) {
        for (int i = 0; i < args.length; i++)
            System.out.println(args[i]);
    }
}
```

A `main` method is just a regular method. Furthermore, you can pass arguments from the command line.

#### 7.13.1 Passing Strings to the `main` Method

You can pass strings to a `main` method from the command line when you run the program. The following command line, for example, starts the program `TestMain` with three strings: `arg0`, `arg1`, and `arg2`:

```
java TestMain arg0 arg1 arg2
```

`arg0`, `arg1`, and `arg2` are strings, but they don’t have to appear in double quotes on the command line. The strings are separated by a space. A string that contains a space must be enclosed in double quotes. Consider the following command line:

```
java TestMain "First num" alpha 53
```
It starts the program with three strings: `First num`, `alpha`, and `53`. Since `First num` is a string, it is enclosed in double quotes. Note that `53` is actually treated as a string. You can use "53" instead of `53` in the command line.

When the `main` method is invoked, the Java interpreter creates an array to hold the command-line arguments and pass the array reference to `args`. For example, if you invoke a program with `n` arguments, the Java interpreter creates an array like this one:

```java
args = new String[n];
```

The Java interpreter then passes `args` to invoke the `main` method.

**Note**
If you run the program with no strings passed, the array is created with `new String[0]`. In this case, the array is empty with length `0`. `args` references to this empty array. Therefore, `args` is not `null`, but `args.length` is `0`.

### 7.13.2 Case Study: Calculator

Suppose you are to develop a program that performs arithmetic operations on integers. The program receives an expression in one string argument. The expression consists of an integer followed by an operator and another integer. For example, to add two integers, use this command:

```java
java Calculator 2 + 3
```

The program will display the following output:

```
2 + 3 = 5
```

Figure 7.12 shows sample runs of the program.

The strings passed to the main program are stored in `args`, which is an array of strings. The first string is stored in `args[0]`, and `args.length` is the number of strings passed.

Here are the steps in the program:

1. Use `args.length` to determine whether the expression has been provided as three arguments in the command line. If not, terminate the program using `System.exit(1)`.

![Figure 7.12](image)

The program takes three arguments (`operand1 operator operand2`) from the command line and displays the expression and the result of the arithmetic operation.
The program is shown in Listing 7.9.

**Listing 7.9   Calculator.java**

```java
public class Calculator {
    /* Main method */
    public static void main(String[] args) {
        // Check number of strings passed
        if (args.length != 3) {
            System.out.println("Usage: java Calculator operand1 operator operand2");
            System.exit(0);
        }
        // The result of the operation
        int result = 0;
        // Determine the operator
        switch (args[1].charAt(0)) {
            case '+': result = Integer.parseInt(args[0]) + Integer.parseInt(args[2]);
                break;
            case '-': result = Integer.parseInt(args[0]) - Integer.parseInt(args[2]);
                break;
            case '.': result = Integer.parseInt(args[0]) * Integer.parseInt(args[2]);
                break;
            case '/': result = Integer.parseInt(args[0]) / Integer.parseInt(args[2]);
                break;
        }
        // Display result
        System.out.println(args[0] + ' ' + args[1] + ' ' + args[2] + " = " + result);
    }
}
```

*Integer.parseInt(args[0])* (line 16) converts a digital string into an integer. The string must consist of digits. If not, the program will terminate abnormally.

We used the . symbol for multiplication, not the common * symbol. The reason for this is that the * symbol refers to all the files in the current directory when it is used on a command line. The following program displays all the files in the current directory when issuing the command *java Test*:

```java
public class Test {
    public static void main(String[] args) {
        for (int i = 0; i < args.length; i++)
            System.out.println(args[i]);
    }
}
```

To circumvent this problem, we will have to use a different symbol for the multiplication operator.

**7.29   Check Point**

This book declares the *main* method as

```
public static void main(String[] args)
```

Can it be replaced by one of the following lines?

```
public static void main(String args[])
public static void main(String[] x)
```
public static void main(String x[])
static void main(String x[])

7.30 Show the output of the following program when invoked using

1. java Test I have a dream
2. java Test “1 2 3”
3. java Test

public class Test {
    public static void main(String[] args) {
        System.out.println("Number of strings is "+ args.length);
        for (int i = 0; i < args.length; i++)
            System.out.println(args[i]);
    }
}

Key Terms

anonymous array 258  index 246
array 246  indexed variable 248
array initializer 248  linear search 265
binary search 265  off-by-one error 251
garbage collection 256  selection sort 269

Chapter Summary

1. A variable is declared as an array type using the syntax `elementType[] arrayRefVar` or `elementType arrayRefVar[]`. The style `elementType[] arrayRefVar` is preferred, although `elementType arrayRefVar[]` is legal.

2. Unlike declarations for primitive data type variables, the declaration of an array variable does not allocate any space in memory for the array. An array variable is not a primitive data type variable. An array variable contains a reference to an array.

3. You cannot assign elements to an array unless it has already been created. You can create an array by using the new operator with the following syntax: `new elementType[arraySize]`.

4. Each element in the array is represented using the syntax `arrayRefVar[index]`. An index must be an integer or an integer expression.

5. After an array is created, its size becomes permanent and can be obtained using `arrayRefVar.length`. Since the index of an array always begins with 0, the last index is always `arrayRefVar.length - 1`. An out-of-bounds error will occur if you attempt to reference elements beyond the bounds of an array.

6. Programmers often mistakenly reference the first element in an array with index 1, but it should be 0. This is called the index off-by-one error.
7. When an array is created, its elements are assigned the default value of 0 for the numeric primitive data types, \( \text{\texttt{\textbackslash u0000}} \) for char types, and \texttt{false} for \texttt{boolean} types.

8. Java has a shorthand notation, known as the \textit{array initializer}, which combines declaring an array, creating an array, and initializing an array in one statement, using the syntax \texttt{elementType[]} \texttt{arrayRefVar} = \{value0, value1, ..., valuek\}.

9. When you pass an array argument to a method, you are actually passing the reference of the array; that is, the called method can modify the elements in the caller’s original array.

10. If an array is sorted, \textit{binary search} is more efficient than \textit{linear search} for finding an element in the array.

11. \textit{Selection sort} finds the smallest number in the list and swaps it with the first element. It then finds the smallest number remaining and swaps it with the first element in the remaining list, and so on, until only a single number remains.

**Quiz**

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

**PROGRAMMING EXERCISES**

Sections 7.2–7.5

*7.1 \textit{(Assign grades)} Write a program that reads student scores, gets the best score, and then assigns grades based on the following scheme:
Grade is A if score is \( \geq \text{best} - 10 \)
Grade is B if score is \( \geq \text{best} - 20; \)
Grade is C if score is \( \geq \text{best} - 30; \)
Grade is D if score is \( \geq \text{best} - 40; \)
Grade is F otherwise.

The program prompts the user to enter the total number of students, then prompts the user to enter all of the scores, and concludes by displaying the grades. Here is a sample run:

```
Enter the number of students: 4
Enter 4 scores: 40 55 70 58
Student 0 score is 40 and grade is C
Student 1 score is 55 and grade is B
Student 2 score is 70 and grade is A
Student 3 score is 58 and grade is B
```

7.2 \textit{(Reverse the numbers entered)} Write a program that reads ten integers and displays them in the reverse of the order in which they were read.
**7.3  (Count occurrence of numbers) Write a program that reads the integers between 1 and 100 and counts the occurrences of each. Assume the input ends with 0. Here is a sample run of the program:

```
Enter the integers between 1 and 100: 2 5 6 5 4 3 23 43 2 0
2 occurs 2 times
3 occurs 1 time
4 occurs 1 time
5 occurs 2 times
6 occurs 1 time
23 occurs 1 time
43 occurs 1 time
```

Note that if a number occurs more than one time, the plural word “times” is used in the output.

7.4  (Analyze scores) Write a program that reads an unspecified number of scores and determines how many scores are above or equal to the average and how many scores are below the average. Enter a negative number to signify the end of the input. Assume that the maximum number of scores is 100.

**7.5  (Print distinct numbers) Write a program that reads in ten numbers and displays the number of distinct numbers and the distinct numbers separated by exactly one space (i.e., if a number appears multiple times, it is displayed only once). (Hint: Read a number and store it to an array if it is new. If the number is already in the array, ignore it.) After the input, the array contains the distinct numbers. Here is the sample run of the program:

```
Enter ten numbers: 1 2 3 2 1 6 3 4 5 2
The number of distinct number is 6
The distinct numbers are: 1 2 3 6 4 5
```

7.6  (Revise Listing 5.15, PrimeNumber.java) Listing 5.15 determines whether a number \( n \) is prime by checking whether \( 2, 3, 4, 5, 6, \ldots, n/2 \) is a divisor. If a divisor is found, \( n \) is not prime. A more efficient approach is to check whether any of the prime numbers less than or equal to \( \sqrt{n} \) can divide \( n \) evenly. If not, \( n \) is prime. Rewrite Listing 5.15 to display the first 50 prime numbers using this approach. You need to use an array to store the prime numbers and later use them to check whether they are possible divisors for \( n \).

7.7  (Count single digits) Write a program that generates 100 random integers between 0 and 9 and displays the count for each number. (Hint: Use an array of ten integers, say `counts`, to store the counts for the number of 0s, 1s, \ldots, 9s.)

Sections 7.6–7.8

7.8  (Average an array) Write two overloaded methods that return the average of an array with the following headers:

```
public static int average(int[] array)
public static double average(double[] array)
```

Write a test program that prompts the user to enter ten double values, invokes this method, and displays the average value.
7.9 (Find the smallest element) Write a method that finds the smallest element in an array of double values using the following header:

```
public static double min(double[] array)
```

Write a test program that prompts the user to enter ten numbers, invokes this method to return the minimum value, and displays the minimum value. Here is a sample run of the program:

```
Enter ten numbers: 1.9 2.5 3.7 2 1.5 6 3 4 5 2
The minimum number is: 1.5
```

7.10 (Find the index of the smallest element) Write a method that returns the index of the smallest element in an array of integers. If the number of such elements is greater than 1, return the smallest index. Use the following header:

```
public static int indexOfSmallestElement(double[] array)
```

Write a test program that prompts the user to enter ten numbers, invokes this method to return the index of the smallest element, and displays the index.

7.11 (Statistics: compute deviation) Programming Exercise 5.45 computes the standard deviation of numbers. This exercise uses a different but equivalent formula to compute the standard deviation of \( n \) numbers.

\[
\text{mean} = \frac{\sum_{i=1}^{n} x_i}{n} = \frac{x_1 + x_2 + \cdots + x_n}{n} \quad \text{deviation} = \sqrt{\frac{\sum_{i=1}^{n} (x_i - \text{mean})^2}{n - 1}}
\]

To compute the standard deviation with this formula, you have to store the individual numbers using an array, so that they can be used after the mean is obtained. Your program should contain the following methods:

```
/** Compute the deviation of double values */
public static double deviation(double[] x)

/** Compute the mean of an array of double values */
public static double mean(double[] x)
```

Write a test program that prompts the user to enter ten numbers and displays the mean and standard deviation, as shown in the following sample run:

```
Enter ten numbers: 1.9 2.5 3.7 2 1.6 3 4 5 2
The mean is 3.11
The standard deviation is 1.55738
```

7.12 (Reverse an array) The `reverse` method in Section 7.7 reverses an array by copying it to a new array. Rewrite the method that reverses the array passed in the argument and returns this array. Write a test program that prompts the user to
enter ten numbers, invokes the method to reverse the numbers, and displays the numbers.

Section 7.9

**7.13** (Random number chooser) Write a method that returns a random number between 1 and 54, excluding the numbers passed in the argument. The method header is specified as follows:

```java
public static int getRandom(int... numbers)
```

**7.14** (Computing gcd) Write a method that returns the gcd of an unspecified number of integers. The method header is specified as follows:

```java
public static int gcd(int... numbers)
```

Write a test program that prompts the user to enter five numbers, invokes the method to find the gcd of these numbers, and displays the result.

Sections 7.10–7.12

**7.15** (Eliminate duplicates) Write a method that returns a new array by eliminating the duplicate values in the array using the following method header:

```java
public static int[] eliminateDuplicates(int[] list)
```

Write a test program that reads in ten integers, invokes the method, and displays the result. Here is the sample run of the program:

```
Enter ten numbers: 1 2 3 2 1 6 3 4 5 2
The distinct numbers are: 1 2 3 6 4 5
```

**7.16** (Execution time) Write a program that randomly generates an array of 100,000 integers and a key. Estimate the execution time of invoking the `linearSearch` method in Listing 7.6. Sort the array and estimate the execution time of invoking the `binarySearch` method in Listing 7.7. You can use the following code template to obtain the execution time:

```java
long startTime = System.currentTimeMillis();
// perform the task;
long endTime = System.currentTimeMillis();
long executionTime = endTime - startTime;
```

**7.17** (Sort students) Write a program that prompts the user to enter the number of students, the students’ names, and their scores, and prints student names in decreasing order of their scores.

**7.18** (Bubble sort) Write a sort method that uses the bubble-sort algorithm. The bubble-sort algorithm makes several passes through the array. On each pass, successive neighboring pairs are compared. If a pair is not in order, its values are swapped; otherwise, the values remain unchanged. The technique is called a bubble sort or sinking sort because the smaller values gradually “bubble” their way to the top and the larger values “sink” to the bottom. Write a test program that reads in ten double numbers, invokes the method, and displays the sorted numbers.
**7.19**: Write the following method that returns true if the list is already sorted in increasing order.

```java
public static boolean isSorted(int[] list)
```

Write a test program that prompts the user to enter a list and displays whether the list is sorted or not. Here is a sample run. Note that the first number in the input indicates the number of the elements in the list. This number is not part of the list.

Enter list: 8 10 1 5 16 61 9 11 1
The list is not sorted

Enter list: 10 1 1 3 4 4 5 7 9 11 21
The list is already sorted

*7.20**: In Section 7.11, you used selection sort to sort an array. The selection-sort method repeatedly finds the smallest number in the current array and swaps it with the first. Rewrite this program by finding the largest number and swapping it with the last. Write a test program that reads in ten double numbers, invokes the method, and displays the sorted numbers.

***7.21**: The bean machine, also known as a quincunx or the Galton box, is a device for statistics experiments named after English scientist Sir Francis Galton. It consists of an upright board with evenly spaced nails (or pegs) in a triangular form, as shown in Figure 7.13.

![Figure 7.13](image)

**Figure 7.13** Each ball takes a random path and falls into a slot.

Balls are dropped from the opening of the board. Every time a ball hits a nail, it has a 50% chance of falling to the left or to the right. The piles of balls are accumulated in the slots at the bottom of the board.

Write a program that simulates the bean machine. Your program should prompt the user to enter the number of the balls and the number of the slots in the machine. Simulate the falling of each ball by printing its path. For example, the path for the ball in Figure 7.13b is LLRLLR and the path for the ball in Figure 7.13c is...
RLRRLRR. Display the final buildup of the balls in the slots in a histogram. Here is a sample run of the program:

```
Enter the number of balls to drop: 5
Enter the number of slots in the bean machine: 8
LRLRLRR
RRLLRR
LLRLLRR
RRLLLLL
LRLRLR

0
0
000
```

(Hint: Create an array named slots. Each element in slots stores the number of balls in a slot. Each ball falls into a slot via a path. The number of Rs in a path is the position of the slot where the ball falls. For example, for the path LRLRLRR, the ball falls into slots[4], and for the path is RRLLLLL, the ball falls into slots[2].)

***7.22 (Game: Eight Queens) The classic Eight Queens puzzle is to place eight queens on a chessboard such that no two queens can attack each other (i.e., no two queens are on the same row, same column, or same diagonal). There are many possible solutions. Write a program that displays one such solution. A sample output is shown below:

```
|Q| | | | | | |
| | | | |Q| | | |
| | | | | | | |Q|
| | |Q| | | | | |
| | | | | |Q| | |
| | | | | | |Q| |
|Q| | | | | | |
| | | | |Q| | |
```

***7.23 (Game: locker puzzle) A school has 100 lockers and 100 students. All lockers are closed on the first day of school. As the students enter, the first student, denoted S1, opens every locker. Then the second student, S2, begins with the second locker, denoted L2, and closes every other locker. Student S3 begins with the third locker and changes every third locker (closes it if it was open, and opens it if it was closed). Student S4 begins with locker L4 and changes every fourth locker. Student S5 starts with L5 and changes every fifth locker, and so on, until student S100 changes L100.

After all the students have passed through the building and changed the lockers, which lockers are open? Write a program to find your answer and display all open locker numbers separated by exactly one space.

(Hint: Use an array of 100 Boolean elements, each of which indicates whether a locker is open (true) or closed (false). Initially, all lockers are closed.)

***7.24 (Simulation: coupon collector’s problem) Coupon collector is a classic statistics problem with many practical applications. The problem is to pick objects from a set of objects repeatedly and find out how many picks are needed for all the
objects to be picked at least once. A variation of the problem is to pick cards from a shuffled deck of 52 cards repeatedly and find out how many picks are needed before you see one of each suit. Assume a picked card is placed back in the deck before picking another. Write a program to simulate the number of picks needed to get four cards from each suit and display the four cards picked (it is possible a card may be picked twice). Here is a sample run of the program:

Queen of Spades
5 of Clubs
Queen of Hearts
4 of Diamonds
Number of picks: 12

7.25 (Algebra: solve quadratic equations) Write a method for solving a quadratic equation using the following header:

```java
public static int solveQuadratic(double[] eqn, double[] roots)
```

The coefficients of a quadratic equation $ax^2 + bx + c = 0$ are passed to the array `eqn` and the real roots are stored in `roots`. The method returns the number of real roots. See Programming Exercise 3.1 on how to solve a quadratic equation.

Write a program that prompts the user to enter values for $a$, $b$, and $c$ and displays the number of real roots and all real roots.

7.26 (Strictly identical arrays) The arrays `list1` and `list2` are strictly identical if their corresponding elements are equal. Write a method that returns `true` if `list1` and `list2` are strictly identical, using the following header:

```java
public static boolean equals(int[] list1, int[] list2)
```

Write a test program that prompts the user to enter two lists of integers and displays whether the two are strictly identical. Here are the sample runs. Note that the first number in the input indicates the number of the elements in the list. This number is not part of the list.

```
Enter list1: 5 2 5 6 1 6
Enter list2: 5 2 5 6 1 6
Two lists are strictly identical
```

```
Enter list1: 5 2 5 6 6 1
Enter list2: 5 2 5 6 1 6
Two lists are not strictly identical
```

7.27 (Identical arrays) The arrays `list1` and `list2` are identical if they have the same contents. Write a method that returns `true` if `list1` and `list2` are identical, using the following header:

```java
public static boolean equals(int[] list1, int[] list2)
```
Write a test program that prompts the user to enter two lists of integers and displays whether they are identical. Here are the sample runs. Note that the first number in the input indicates the number of the elements in the list. This number is not part of the list.

Enter list1: 5 2 5 6 6 1
Enter list2: 5 5 2 6 1 6
Two lists are identical

Enter list1: 5 5 6 6 1
Enter list2: 5 2 5 6 1 6
Two lists are not identical

*7.28 (Math: combinations) Write a program that prompts the user to enter 10 integers and displays all combinations of picking two numbers from the 10.

*7.29 (Game: pick four cards) Write a program that picks four cards from a deck of 52 cards and computes their sum. An Ace, King, Queen, and Jack represent 1, 13, 12, and 11, respectively. Your program should display the number of picks that yields the sum of 24.

*7.30 (Pattern recognition: consecutive four equal numbers) Write the following method that tests whether the array has four consecutive numbers with the same value.

```java
public static boolean isConsecutiveFour(int[] values)
```

Write a test program that prompts the user to enter a series of integers and displays if the series contains four consecutive numbers with the same value. Your program should first prompt the user to enter the input size—i.e., the number of values in the series. Here are sample runs:

Enter the number of values: 8
Enter the values: 3 4 5 5 5 4 5
The list has consecutive fours

Enter the number of values: 9
Enter the values: 3 4 5 5 6 5 5 4 5
The list has no consecutive fours

**7.31 (Merge two sorted lists) Write the following method that merges two sorted lists into a new sorted list.

```java
public static int[] merge(int[] list1, int[] list2)
```
Implement the method in a way that takes at most \( \text{list1.length + list2.length} \) comparisons. Write a test program that prompts the user to enter two sorted lists and displays the merged list. Here is a sample run. Note that the first number in the input indicates the number of the elements in the list. This number is not part of the list.

```
Enter list1: 5 1 5 16 61 111
Enter list2: 4 2 4 5 6
The merged list is 1 2 4 5 5 6 16 61 111
```

**7.32 (Partition of a list) Write the following method that partitions the list using the first element, called a pivot.

```
public static int partition(int[] list)
```

After the partition, the elements in the list are rearranged so that all the elements before the pivot are less than or equal to the pivot and the elements after the pivot are greater than the pivot. The method returns the index where the pivot is located in the new list. For example, suppose the list is \{ 5, 2, 9, 3, 6, 8 \}. After the partition, the list becomes \{ 3, 2, 5, 9, 6, 8 \}. Implement the method in a way that takes at most \( \text{list.length} \) comparisons. Write a test program that prompts the user to enter a list and displays the list after the partition. Here is a sample run. Note that the first number in the input indicates the number of the elements in the list. This number is not part of the list.

```
Enter list: 8 10 1 5 16 61 9 11 1
After the partition, the list is 9 1 5 1 10 61 11 16
```

*7.33 (Culture: Chinese Zodiac) Simplify Listing 3.9 using an array of strings to store the animal names.

**7.34 (Sort characters in a string) Write a method that returns a sorted string using the following header:

```
public static String sort(String s)
```

For example, \text{sort("acb")} returns \text{abc}.

Write a test program that prompts the user to enter a string and displays the sorted string.

***7.35 (Game: hangman) Write a hangman game that randomly generates a word and prompts the user to guess one letter at a time, as shown in the sample run. Each letter in the word is displayed as an asterisk. When the user makes a correct guess, the actual letter is then displayed. When the user finishes a word, display
the number of misses and ask the user whether to continue to play with another word. Declare an array to store words, as follows:

```java
// Add any words you wish in this array
String[] words = {"write", "that", ...};
```

(Guess) Enter a letter in word ******* > p
(Guess) Enter a letter in word p****** > r
(Guess) Enter a letter in word pr**r** > p
   p is already in the word
(Guess) Enter a letter in word pr**r** > o
(Guess) Enter a letter in word pro*r** > g
(Guess) Enter a letter in word progr** > n
   n is not in the word
(Guess) Enter a letter in word progr** > m
(Guess) Enter a letter in word progr*m > a
The word is program. You missed 1 time
Do you want to guess another word? Enter y or n>
This page intentionally left blank
Objectives

- To give examples of representing data using two-dimensional arrays (§8.1).
- To declare variables for two-dimensional arrays, create arrays, and access array elements in a two-dimensional array using row and column indexes (§8.2).
- To program common operations for two-dimensional arrays (displaying arrays, summing all elements, finding the minimum and maximum elements, and random shuffling) (§8.3).
- To pass two-dimensional arrays to methods (§8.4).
- To write a program for grading multiple-choice questions using two-dimensional arrays (§8.5).
- To solve the closest-pair problem using two-dimensional arrays (§8.6).
- To check a Sudoku solution using two-dimensional arrays (§8.7).
- To use multidimensional arrays (§8.8).
8.1 Introduction

Data in a table or a matrix can be represented using a two-dimensional array.

The preceding chapter introduced how to use one-dimensional arrays to store linear collections of elements. You can use a two-dimensional array to store a matrix or a table. For example, the following table that lists the distances between cities can be stored using a two-dimensional array named `distances`.

<table>
<thead>
<tr>
<th></th>
<th>Chicago</th>
<th>Boston</th>
<th>New York</th>
<th>Atlanta</th>
<th>Miami</th>
<th>Dallas</th>
<th>Houston</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chicago</td>
<td>0</td>
<td>983</td>
<td>787</td>
<td>714</td>
<td>1375</td>
<td>967</td>
<td>1087</td>
</tr>
<tr>
<td>Boston</td>
<td>983</td>
<td>0</td>
<td>214</td>
<td>1102</td>
<td>1763</td>
<td>1723</td>
<td>1842</td>
</tr>
<tr>
<td>New York</td>
<td>787</td>
<td>214</td>
<td>0</td>
<td>888</td>
<td>1549</td>
<td>1548</td>
<td>1627</td>
</tr>
<tr>
<td>Atlanta</td>
<td>714</td>
<td>1102</td>
<td>888</td>
<td>0</td>
<td>661</td>
<td>781</td>
<td>810</td>
</tr>
<tr>
<td>Miami</td>
<td>1375</td>
<td>1763</td>
<td>1549</td>
<td>661</td>
<td>0</td>
<td>1426</td>
<td>1187</td>
</tr>
<tr>
<td>Dallas</td>
<td>967</td>
<td>1723</td>
<td>1548</td>
<td>781</td>
<td>1426</td>
<td>0</td>
<td>239</td>
</tr>
<tr>
<td>Houston</td>
<td>1087</td>
<td>1842</td>
<td>1627</td>
<td>810</td>
<td>1187</td>
<td>239</td>
<td>0</td>
</tr>
</tbody>
</table>

```java
double[][] distances = {
    {0, 983, 787, 714, 1375, 967, 1087},
    {983, 0, 214, 1102, 1763, 1723, 1842},
    {787, 214, 0, 888, 1549, 1548, 1627},
    {714, 1102, 888, 0, 661, 781, 810},
    {1375, 1763, 1549, 661, 0, 1426, 1187},
    {967, 1723, 1548, 781, 1426, 0, 239},
    {1087, 1842, 1627, 810, 1187, 239, 0},
};
```

8.2 Two-Dimensional Array Basics

An element in a two-dimensional array is accessed through a row and column index.

How do you declare a variable for two-dimensional arrays? How do you create a two-dimensional array? How do you access elements in a two-dimensional array? This section addresses these issues.

8.2.1 Declaring Variables of Two-Dimensional Arrays and Creating Two-Dimensional Arrays

The syntax for declaring a two-dimensional array is:

```java
elementType[][] arrayRefVar;
```
or

```java
elementType arrayRefVar[][]; // Allowed, but not preferred
```

As an example, here is how you would declare a two-dimensional array variable `matrix` of `int` values:

```java
int[][] matrix;
```
or

```java
int matrix[][]; // This style is allowed, but not preferred
```

You can create a two-dimensional array of 5-by-5 `int` values and assign it to `matrix` using this syntax:

```java
matrix = new int[5][5];
```

Two subscripts are used in a two-dimensional array, one for the row and the other for the column. As in a one-dimensional array, the index for each subscript is of the `int` type and starts from 0, as shown in Figure 8.1a.

![Figure 8.1](image)

**Figure 8.1** The index of each subscript of a two-dimensional array is an `int` value, starting from 0.

To assign the value 7 to a specific element at row 2 and column 1, as shown in Figure 8.1b, you can use the following syntax:

```java
matrix[2][1] = 7;
```

**Caution**

It is a common mistake to use `matrix[2, 1]` to access the element at row 2 and column 1. In Java, each subscript must be enclosed in a pair of square brackets.

You can also use an array initializer to declare, create, and initialize a two-dimensional array. For example, the following code in (a) creates an array with the specified initial values, as shown in Figure 8.1c. This is equivalent to the code in (b).

```java
int[][] array = {
    {1, 2, 3},
    {4, 5, 6},
    {7, 8, 9},
    {10, 11, 12}
};
```

```java
int[][] array = new int[4][3];
array[0][0] = 1; array[0][1] = 2; array[0][2] = 3;
array[1][0] = 4; array[1][1] = 5; array[1][2] = 6;
array[2][0] = 7; array[2][1] = 8; array[2][2] = 9;
array[3][0] = 10; array[3][1] = 11; array[3][2] = 12;
```

**Equivalent**

8.2.2 Obtaining the Lengths of Two-Dimensional Arrays

A two-dimensional array is actually an array in which each element is a one-dimensional array. The length of an array `x` is the number of elements in the array, which can be obtained using `x.length`, `x[0]`, `x[1]`, ..., and `x[x.length-1]` are arrays. Their lengths can be obtained using `x[0].length`, `x[1].length`, ..., and `x[x.length-1].length`. 
For example, suppose \( x = \text{new int}[3][4] \), \( x[0] \), \( x[1] \), and \( x[2] \) are one-dimensional arrays and each contains four elements, as shown in Figure 8.2. \( x\.\text{length} \) is 3, and \( x[0].\text{length} \), \( x[1].\text{length} \), and \( x[2].\text{length} \) are 4.

\[
\begin{array}{cccc}
\text{x} & x[0] & x[1] & x[2] \\
\text{x[0]} & x[0][0] & x[0][1] & x[0][2] & x[0][3] & x[0].\text{length is} & 4 \\
\text{x[1]} & x[1][0] & x[1][1] & x[1][2] & x[1][3] & x[1].\text{length is} & 4 \\
\end{array}
\]

**Figure 8.2** A two-dimensional array is a one-dimensional array in which each element is another one-dimensional array.

### 8.2.3 Ragged Arrays

Each row in a two-dimensional array is itself an array. Thus, the rows can have different lengths. An array of this kind is known as a *ragged array*. Here is an example of creating a ragged array:

```java
int[][] triangleArray = {
    {1, 2, 3, 4, 5},
    {2, 3, 4, 5},
    {3, 4, 5},
    {4, 5},
    {5}
};
```

As you can see, \( \text{triangleArray}[0].\text{length} \) is 5, \( \text{triangleArray}[1].\text{length} \) is 4, \( \text{triangleArray}[2].\text{length} \) is 3, \( \text{triangleArray}[3].\text{length} \) is 2, and \( \text{triangleArray}[4].\text{length} \) is 1.

If you don’t know the values in a ragged array in advance, but do know the sizes—say, the same as before—you can create a ragged array using the following syntax:

```java
int[][] triangleArray = \text{new int}[5][];  
triangleArray[0] = \text{new int}[5];  
triangleArray[1] = \text{new int}[4];  
triangleArray[2] = \text{new int}[3];  
triangleArray[3] = \text{new int}[2];  
triangleArray[4] = \text{new int}[1];  
```

You can now assign values to the array. For example,

\[
\begin{align*}
\text{triangleArray}[0][3] &= 50; \\
\text{triangleArray}[4][0] &= 45;
\end{align*}
\]

**Note**

The syntax `\text{new int}[5][]` for creating an array requires the first index to be specified. The syntax `\text{new int}[][]` would be wrong.
8.1 Declare an array reference variable for a two-dimensional array of `int` values, create a 4-by-5 `int` matrix, and assign it to the variable.

8.2 Can the rows in a two-dimensional array have different lengths?

8.3 What is the output of the following code?

```java
int[][] array = new int[5][6];
int[] x = {1, 2};
array[0] = x;
System.out.println("array[0][1] is " + array[0][1]);
```

8.4 Which of the following statements are valid?

```java
int[][] r = new int[2];
int[] x = new int[];
int[][] y = new int[3][];
int[][] z = {{1, 2}};
int[][][] n = {{1, 2}, {2, 3}, };
```

### 8.3 Processing Two-Dimensional Arrays

*Nested for loops are often used to process a two-dimensional array.*

Suppose an array `matrix` is created as follows:

```java
int[][] matrix = new int[10][10];
```

The following are some examples of processing two-dimensional arrays.

1. **Initializing arrays with input values.** The following loop initializes the array with user input values:

```java
java.util.Scanner input = new Scanner(System.in);
System.out.println("Enter " + matrix.length + " rows and " + matrix[0].length + " columns: ");
for (int row = 0; row < matrix.length; row++) {
    for (int column = 0; column < matrix[row].length; column++) {
        matrix[row][column] = input.nextInt();
    }
}
```

2. **Initializing arrays with random values.** The following loop initializes the array with random values between 0 and 99:

```java
for (int row = 0; row < matrix.length; row++) {
    for (int column = 0; column < matrix[row].length; column++) {
        matrix[row][column] = (int)(Math.random() * 100);
    }
}
```

3. **Printing arrays.** To print a two-dimensional array, you have to print each element in the array using a loop like the following:

```java
for (int row = 0; row < matrix.length; row++) {
    for (int column = 0; column < matrix[row].length; column++) {
        System.out.print(matrix[row][column] + " ");
    }
    System.out.println();
}
```
4. **Summing all elements.** Use a variable named `total` to store the sum. Initially `total` is 0. Add each element in the array to `total` using a loop like this:

```java
int total = 0;
for (int row = 0; row < matrix.length; row++) {
    for (int column = 0; column < matrix[row].length; column++) {
        total += matrix[row][column];
    }
}
```

5. **Summing elements by column.** For each column, use a variable named `total` to store its sum. Add each element in the column to `total` using a loop like this:

```java
for (int column = 0; column < matrix[0].length; column++) {
    int total = 0;
    for (int row = 0; row < matrix.length; row++) {
        total += matrix[row][column];
    }
    System.out.println("Sum for column " + column + " is " + total);
}
```

6. **Which row has the largest sum?** Use variables `maxRow` and `indexOfMaxRow` to track the largest sum and index of the row. For each row, compute its sum and update `maxRow` and `indexOfMaxRow` if the new sum is greater.

```java
int maxRow = 0;
int indexOfMaxRow = 0;

// Get sum of the first row in maxRow
for (int column = 0; column < matrix[0].length; column++) {
    maxRow += matrix[0][column];
}

for (int row = 1; row < matrix.length; row++) {
    int totalOfThisRow = 0;
    for (int column = 0; column < matrix[row].length; column++) {
        totalOfThisRow += matrix[row][column];
    }
    if (totalOfThisRow > maxRow) {
        maxRow = totalOfThisRow;
        indexOfMaxRow = row;
    }
}
System.out.println("Row " + indexOfMaxRow + " has the maximum sum of " + maxRow);
```

7. **Random shuffling.** Shuffling the elements in a one-dimensional array was introduced in Section 7.2.6. How do you shuffle all the elements in a two-dimensional array? To accomplish this, for each element `matrix[i][j]`, randomly generate indices `i1` and `j1` and swap `matrix[i][j]` with `matrix[i1][j1]`, as follows:

```java
for (int i = 0; i < matrix.length; i++) {
    for (int j = 0; j < matrix[i].length; j++) {
        int i1 = (int) (Math.random() * matrix.length);
        int j1 = (int) (Math.random() * matrix[i].length);
        // Swap matrix[i][j] with matrix[i1][j1]
```
8.4 Passing Two-Dimensional Arrays to Methods

When passing a two-dimensional array to a method, the reference of the array is passed to the method.

You can pass a two-dimensional array to a method just as you pass a one-dimensional array. You can also return an array from a method. Listing 8.1 gives an example with two methods. The first method, `getArray()`, returns a two-dimensional array, and the second method, `sum(int[][] m)`, returns the sum of all the elements in a matrix.

Listing 8.1  PassTwoDimensionalArray.java

```java
import java.util.Scanner;

public class PassTwoDimensionalArray {

    public static void main(String[] args) {
        int[][] m = getArray(); // Get an array

        // Display sum of elements
        System.out.println("Sum of all elements is " + sum(m));
    }

    public static int[][] getArray() {
        // Create a Scanner
        Scanner input = new Scanner(System.in);

        // Enter array values
        int[][] m = new int[3][4];
        System.out.println("Enter " + m.length + " rows and " + m[0].length + " columns: ");

        for (int i = 0; i < m.length; i++)
            for (int j = 0; j < m[i].length; j++)
                m[i][j] = input.nextInt();
        return m;
    }

    public static int sum(int[][] m) {
        int sum = 0;
        for (int i = 0; i < m.length; i++)
            for (int j = 0; j < m[i].length; j++)
                sum += m[i][j];
        return sum;
    }
}
```

8.5 Show the output of the following code:

```java
int[][] array = {{1, 2}, {3, 4}, {5, 6}};
for (int i = array.length - 1; i >= 0; i--)
    for (int j = array[i].length - 1; j >= 0; j--)
        System.out.print(array[i][j] + " ");
System.out.println();
```

8.6 Show the output of the following code:

```java
int[][] array = {{1, 2}, {3, 4}, {5, 6}};
int sum = 0;
for (int i = 0; i < array.length; i++)
    sum += array[i][0];
System.out.println(sum);
```
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```java
return m;
}

public static int sum(int[][] m) {
    int total = 0;
    for (int row = 0; row < m.length; row++) {
        for (int column = 0; column < m[row].length; column++) {
            total += m[row][column];
        }
    }
    return total;
}
```

Enter 3 rows and 4 columns:
1 2 3 4
5 6 7 8
9 10 11 12
Sum of all elements is 78

The method `getArray` prompts the user to enter values for the array (lines 11–24) and returns the array (line 23).

The method `sum` (lines 26–35) has a two-dimensional array argument. You can obtain the number of rows using `m.length` (line 28) and the number of columns in a specified row using `m[row].length` (line 29).

8.7 Show the output of the following code:

```java
public class Test {
    public static void main(String[] args) {
        int[][] array = {{1, 2, 3, 4}, {5, 6, 7, 8}};
        System.out.println(m1(array)[0]);
        System.out.println(m1(array)[1]);
    }

    public static int[] m1(int[][] m) {
        int[] result = new int[2];
        result[0] = m.length;
        result[1] = m[0].length;
        return result;
    }
}
```

8.5 Case Study: Grading a Multiple-Choice Test

The problem is to write a program that will grade multiple-choice tests.

Suppose you need to write a program that grades multiple-choice tests. Assume there are eight students and ten questions, and the answers are stored in a two-dimensional array. Each row records a student’s answers to the questions, as shown in the following array.
8.5 Case Study: Grading a Multiple-Choice Test

Students' Answers to the Questions:

```
 0 1 2 3 4 5 6 7 8 9
Student 0 | A | B | A | C | D | E | E | A | D
Student 1 | D | B | A | B | C | A | E | E | A | D
Student 2 | E | D | A | C | B | E | E | A | D
Student 3 | C | B | A | E | D | C | E | E | A | D
Student 4 | A | B | D | C | C | D | E | E | A | D
Student 5 | B | B | E | C | C | D | E | E | A | D
Student 6 | B | B | A | C | C | D | E | E | A | D
Student 7 | E | B | E | C | C | D | E | E | A | D
```

The key is stored in a one-dimensional array:

```
Key to the Questions:
 0 1 2 3 4 5 6 7 8 9
Key        | D | B | D | C | C | D | A | E | A | D
```

Your program grades the test and displays the result. It compares each student’s answers with the key, counts the number of correct answers, and displays it. Listing 8.2 gives the program.

**Listing 8.2 GradeExam.java**

```java
public class GradeExam {
    public static void main(String[] args) {
        // Students' answers to the questions
        char[][] answers = {
            {'A', 'B', 'A', 'C', 'D', 'E', 'E', 'A', 'D'},
            {'E', 'D', 'D', 'A', 'C', 'B', 'E', 'E', 'A', 'D'},
            {'C', 'B', 'A', 'E', 'D', 'C', 'E', 'E', 'A', 'D'},
            {'A', 'B', 'D', 'C', 'C', 'D', 'E', 'E', 'A', 'D'},
            {'B', 'B', 'E', 'C', 'C', 'D', 'E', 'E', 'A', 'D'},
            {'B', 'B', 'A', 'C', 'C', 'D', 'E', 'E', 'A', 'D'},
            {'E', 'B', 'C', 'C', 'D', 'E', 'E', 'A', 'D'}
        };

        // Key to the questions

        // Grade all answers
        for (int i = 0; i < answers.length; i++) {
            for (int j = 0; j < answers[i].length; j++) {
                if (answers[i][j] == keys[j])
                    correctCount++; // compare with key
            }
            System.out.println("Student "+i+"'s correct count is "+correctCount);
        }
    }
}
```
The statement in lines 5–13 declares, creates, and initializes a two-dimensional array of characters and assigns the reference to answers of the char[][] type.

The statement in line 16 declares, creates, and initializes an array of char values and assigns the reference to keys of the char[] type.

Each row in the array answers stores a student’s answer, which is graded by comparing it with the key in the array keys. The result is displayed immediately after a student’s answer is graded.

8.6 Case Study: Finding the Closest Pair

This section presents a geometric problem for finding the closest pair of points.

Given a set of points, the closest-pair problem is to find the two points that are nearest to each other. In Figure 8.3, for example, points (1, 1) and (2, 0.5) are closest to each other. There are several ways to solve this problem. An intuitive approach is to compute the distances between all pairs of points and find the one with the minimum distance, as implemented in Listing 8.3.

```
import java.util.Scanner;

public class FindNearestPoints {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        System.out.print("Enter the number of points: ");
        int numberOfPoints = input.nextInt();
        // Create an array to store points
```

![Figure 8.3](image_url) Points can be represented in a two-dimensional array.
double[][] points = new double[numberOfPoints][2];
System.out.print("Enter " + numberOfPoints + " points: ");
for (int i = 0; i < points.length; i++) {
    points[i][0] = input.nextDouble();
    points[i][1] = input.nextDouble();
}

// p1 and p2 are the indices in the points' array
int p1 = 0, p2 = 1; // Initial two points
double shortestDistance = distance(points[p1][0], points[p1][1],
    points[p2][0], points[p2][1]); // Initialize shortestDistance

// Compute distance for every two points
for (int i = 0; i < points.length; i++) {
    for (int j = i + 1; j < points.length; j++) {
        double distance = distance(points[i][0], points[i][1],
            points[j][0], points[j][1]); // Find distance

        if (shortestDistance > distance) {
            p1 = i; // Update p1
            p2 = j; // Update p2
            shortestDistance = distance; // Update shortestDistance
        }
    }
}

// Display result
System.out.println("The closest two points are " +
    "(" + points[p1][0] + ", " + points[p1][1] + ") and (" +
    points[p2][0] + ", " + points[p2][1] + ")");

/** Compute the distance between two points (x1, y1) and (x2, y2)*/
public static double distance(
    double x1, double y1, double x2, double y2) {
    return Math.sqrt((x2 - x1) * (x2 - x1) + (y2 - y1) * (y2 - y1));
}

Enter the number of points: 8
Enter 8 points: -1 3 -1 1 1 2 0.5 2 -1 3 3 4 2 4 -0.5
The closest two points are (1, 1) and (2, 0.5)

The program prompts the user to enter the number of points (lines 6–7). The points are read from the console and stored in a two-dimensional array named points (lines 12–15). The program uses the variable shortestDistance (line 19) to store the distance between the two nearest points, and the indices of these two points in the points array are stored in p1 and p2 (line 18).

For each point at index i, the program computes the distance between points[i] and points[j] for all j > i (lines 23–34). Whenever a shorter distance is found, the variable shortestDistance and p1 and p2 are updated (lines 28–32).

The distance between two points (x1, y1) and (x2, y2) can be computed using the formula \( \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2} \) (lines 43–46).

The program assumes that the plane has at least two points. You can easily modify the program to handle the case if the plane has zero or one point.
Note that there might be more than one closest pair of points with the same minimum distance. The program finds one such pair. You may modify the program to find all closest pairs in Programming Exercise 8.8.

**Tip**
It is cumbersome to enter all points from the keyboard. You may store the input in a file, say `FindNearestPoints.txt`, and compile and run the program using the following command:

```
java FindNearestPoints < FindNearestPoints.txt
```

### 8.7 Case Study: Sudoku

The problem is to check whether a given Sudoku solution is correct.

This section presents an interesting problem of a sort that appears in the newspaper every day. It is a number-placement puzzle, commonly known as **Sudoku**. This is a very challenging problem. To make it accessible to the novice, this section presents a simplified version of the Sudoku problem, which is to verify whether a Sudoku solution is correct. The complete program for finding a Sudoku solution is presented in Supplement VI.A.

Sudoku is a $9 \times 9$ grid divided into smaller $3 \times 3$ boxes (also called **regions** or **blocks**), as shown in Figure 8.4a. Some cells, called **fixed cells**, are populated with numbers from 1 to 9. The objective is to fill the empty cells, also called **free cells**, with the numbers 1 to 9 so that every row, every column, and every $3 \times 3$ box contains the numbers 1 to 9, as shown in Figure 8.4b.

![Figure 8.4](image)

(a) Puzzle  
(b) Solution

**Figure 8.4** The Sudoku puzzle in (a) is solved in (b).

For convenience, we use value 0 to indicate a free cell, as shown in Figure 8.5a. The grid can be naturally represented using a two-dimensional array, as shown in Figure 8.5b.

![Figure 8.5](image)

(a)  
(b)

**Figure 8.5** A grid can be represented using a two-dimensional array.
To find a solution for the puzzle, we must replace each 0 in the grid with an appropriate number from 1 to 9. For the solution to the puzzle in Figure 8.5, the grid should be as shown in Figure 8.6.

Once a solution to a Sudoku puzzle is found, how do you verify that it is correct? Here are two approaches:

- Check if every row has numbers from 1 to 9, every column has numbers from 1 to 9, and every small box has numbers from 1 to 9.
- Check each cell. Each cell must be a number from 1 to 9 and the cell must be unique on every row, every column, and every small box.

```
A solution grid is
{{5, 3, 4, 6, 7, 8, 9, 1, 2},
 {6, 7, 2, 1, 9, 5, 3, 4, 8},
 {1, 9, 8, 3, 4, 2, 5, 6, 7},
 {8, 5, 9, 7, 6, 1, 4, 2, 3},
 {4, 2, 6, 8, 5, 3, 7, 9, 1},
 {7, 1, 3, 9, 2, 4, 8, 5, 6},
 {9, 6, 1, 5, 3, 7, 2, 8, 4},
 {2, 8, 7, 4, 1, 9, 6, 3, 5},
 {3, 4, 5, 2, 8, 6, 1, 7, 9}};
```

![Figure 8.6](image)

A solution is stored in grid.

The program in Listing 8.4 prompts the user to enter a solution and reports whether it is valid. We use the second approach in the program to check whether the solution is correct.

**Listing 8.4 CheckSudokuSolution.java**

```java
import java.util.Scanner;

public class CheckSudokuSolution {
    public static void main(String[] args) {
        // Read a Sudoku solution
        int[][] grid = readASolution();
        System.out.println(isValid(grid) ? "Valid solution" : "Invalid solution");
    }

    /** Read a Sudoku solution from the console */
    public static int[][] readASolution() {
        Scanner input = new Scanner(System.in);
        System.out.println("Enter a Sudoku puzzle solution:");
        int[][] grid = new int[9][9];
        for (int i = 0; i < 9; i++)
            for (int j = 0; j < 9; j++)
                grid[i][j] = input.nextInt();
        return grid;
    }

    /** Check whether a solution is valid */
    public static boolean isValid(int[][] grid) {
```

```
for (int i = 0; i < 9; i++)
    for (int j = 0; j < 9; j++)
        if (grid[i][j] < 1 || grid[i][j] > 9 || !isValid(i, j, grid))
            return false;
    return true; // The solution is valid
}

/** Check whether grid[i][j] is valid in the grid */
public static boolean isValid(int i, int j, int[][] grid) {
    // Check whether grid[i][j] is unique in i's row
    for (int column = 0; column < 9; column++)
        if (column != j && grid[i][column] == grid[i][j])
            return false;
    // Check whether grid[i][j] is unique in j's column
    for (int row = 0; row < 9; row++)
        if (row != i && grid[row][j] == grid[i][j])
            return false;
    // Check whether grid[i][j] is unique in the 3-by-3 box
    for (int row = (i / 3) * 3; row < (i / 3) * 3 + 3; row++)
        for (int col = (j / 3) * 3; col < (j / 3) * 3 + 3; col++)
            if (row != i && col != j && grid[row][col] == grid[i][j])
                return false;
    return true; // The current value at grid[i][j] is valid
}

Enter a Sudoku puzzle solution:
9 6 3 1 7 4 2 5 8
1 7 8 3 2 5 6 4 9
2 5 4 6 8 9 7 3 1
8 2 1 4 3 7 5 9 6
4 9 6 8 5 2 3 1 7
7 3 5 9 6 1 8 2 4
5 8 9 7 1 3 4 6 2
3 1 7 2 4 6 9 8 5
6 4 2 5 9 8 1 7 3
Valid solution

The program invokes the readASolution() method (line 6) to read a Sudoku solution and return a two-dimensional array representing a Sudoku grid.

isValid method
The isValid(grid) method checks whether the values in the grid are valid by verifying that each value is between 1 and 9 and that each value is valid in the grid (lines 27–34).

overloaded isValid method
The isValid(i, j, grid) method checks whether the value at grid[i][j] is valid. It checks whether grid[i][j] appears more than once in row i (lines 39–41), in column j (lines 44–46), and in the 3 × 3 box (lines 49–52).

How do you locate all the cells in the same box? For any grid[i][j], the starting cell of the 3 × 3 box that contains it is grid[(i / 3) * 3][(j / 3) * 3], as illustrated in Figure 8.7.
With this observation, you can easily identify all the cells in the box. For instance, if \(\text{grid}[r][c]\) is the starting cell of a 3 \(\times\) 3 box, the cells in the box can be traversed in a nested loop as follows:

```java
// Get all cells in a 3-by-3 box starting at grid[r][c]
for (int row = r; row < r + 3; row++)
    for (int col = c; col < c + 3; col++)
        // grid[row][col] is in the box
```

It is cumbersome to enter 81 numbers from the console. When you test the program, you may store the input in a file, say `CheckSudokuSolution.txt` (see [www.cs.armstrong.edu/liang/data/CheckSudokuSolution.txt](http://www.cs.armstrong.edu/liang/data/CheckSudokuSolution.txt)), and run the program using the following command:

```
java CheckSudokuSolution < CheckSudokuSolution.txt
```

### 8.8 Multidimensional Arrays

A two-dimensional array consists of an array of one-dimensional arrays and a three-dimensional array consists of an array of two-dimensional arrays.

In the preceding section, you used a two-dimensional array to represent a matrix or a table. Occasionally, you will need to represent \(n\)-dimensional data structures. In Java, you can create \(n\)-dimensional arrays for any integer \(n\).

The way to declare two-dimensional array variables and create two-dimensional arrays can be generalized to declare \(n\)-dimensional array variables and create \(n\)-dimensional arrays for \(n \geq 3\). For example, you may use a three-dimensional array to store exam scores for a class of six students with five exams, and each exam has two parts (multiple-choice and essay). The following syntax declares a three-dimensional array variable `scores`, creates an array, and assigns its reference to `scores`.

```java
double[][][] scores = new double[6][5][2];
```

You can also use the short-hand notation to create and initialize the array as follows:

```java
double[][][] scores = {
    {{7.5, 20.5}, {9.0, 22.5}},
    {{4.5, 21.5}, {9.0, 22.5}},
    {{6.5, 30.5}, {9.4, 10.5}},
    {{6.5, 23.5}, {9.4, 32.5}},
    {{8.5, 26.5}, {9.4, 52.5}},
    {{9.5, 20.5}, {9.4, 42.5}}
};
```
scores[0][1][0] refers to the multiple-choice score for the first student’s second exam, which is 9.0. scores[0][1][1] refers to the essay score for the first student’s second exam, which is 22.5. This is depicted in the following figure:

Which student  
Which exam  
Multiple-choice or essay

scores [i] [j] [k]

A multidimensional array is actually an array in which each element is another array. A three-dimensional array consists of an array of two-dimensional arrays. A two-dimensional array consists of an array of one-dimensional arrays. For example, suppose x = new int[2][2][5], and x[0] and x[1] are two-dimensional arrays. X[0][0], x[0][1], x[1][0], and x[1][1] are one-dimensional arrays and each contains five elements. x.length is 2, x[0].length and x[1].length are 2, and X[0][0].length, x[0][1].length, x[1][0].length, and x[1][1].length are 5.

8.8.1 Case Study: Daily Temperature and Humidity

Suppose a meteorology station records the temperature and humidity every hour of every day and stores the data for the past ten days in a text file named Weather.txt (see www.cs.armstrong.edu/liang/data/Weather.txt). Each line of the file consists of four numbers that indicate the day, hour, temperature, and humidity. The contents of the file may look like the one in (a).

Note that the lines in the file are not necessarily in increasing order of day and hour. For example, the file may appear as shown in (b).

Your task is to write a program that calculates the average daily temperature and humidity for the 10 days. You can use the input redirection to read the file and store the data in a three-dimensional array named data. The first index of data ranges from 0 to 9 and represents 10 days, the second index ranges from 0 to 23 and represents 24 hours, and the third index ranges from 0 to 1 and represents temperature and humidity, as depicted in the following figure:
Note that the days are numbered from 1 to 10 and the hours from 1 to 24 in the file. Because the array index starts from 0, data[0][0][0] stores the temperature in day 1 at hour 1 and data[9][23][1] stores the humidity in day 10 at hour 24.

The program is given in Listing 8.5.

**Listing 8.5 Weather.java**

```java
import java.util.Scanner;

public class Weather {
    public static void main(String[] args) {
        final int NUMBER_OF_DAYS = 10;
        final int NUMBER_OF_HOURS = 24;
        double[][][] data = new double[NUMBER_OF_DAYS][NUMBER_OF_HOURS][2];

        Scanner input = new Scanner(System.in);
        for (int k = 0; k < NUMBER_OF_DAYS * NUMBER_OF_HOURS; k++) {
            int day = input.nextInt();
            int hour = input.nextInt();
            double temperature = input.nextDouble();
            double humidity = input.nextDouble();
            data[day - 1][hour - 1][0] = temperature;
            data[day - 1][hour - 1][1] = humidity;
        }

        for (int i = 0; i < NUMBER_OF_DAYS; i++) {
            double dailyTemperatureTotal = 0, dailyHumidityTotal = 0;
            for (int j = 0; j < NUMBER_OF_HOURS; j++) {
                dailyTemperatureTotal += data[i][j][0];
                dailyHumidityTotal += data[i][j][1];
            }
            System.out.println("Day " + i + ", average temperature is 
                           + dailyTemperatureTotal / NUMBER_OF_HOURS);
            System.out.println("Day " + i + ", average humidity is 
                           + dailyHumidityTotal / NUMBER_OF_HOURS);
        }
    }
}
```

Day 0's average temperature is 77.7708
Day 0's average humidity is 0.929583
Day 1's average temperature is 77.3125
Day 1's average humidity is 0.929583

Day 9's average temperature is 79.3542
Day 9's average humidity is 0.9125

You can use the following command to run the program:

```bash
java Weather < Weather.txt
```

A three-dimensional array for storing temperature and humidity is created in line 8. The loop in lines 12–19 reads the input to the array. You can enter the input from the keyboard, but
doing so will be awkward. For convenience, we store the data in a file and use input redirection to read the data from the file. The loop in lines 24–27 adds all temperatures for each hour in a day to `dailyTemperatureTotal` and all humidity for each hour to `dailyHumidityTotal`. The average daily temperature and humidity are displayed in lines 30–33.

### 8.8.2 Case Study: Guessing Birthdays

Listing 3.3, `GuessBirthday.java`, gives a program that guesses a birthday. The program can be simplified by storing the numbers in five sets in a three-dimensional array, and it prompts the user for the answers using a loop, as shown in Listing 8.6. The sample run of the program can be the same as shown in Listing 4.3.

**Listing 8.6  GuessBirthdayUsingArray.java**

```java
import java.util.Scanner;

public class GuessBirthdayUsingArray {
    public static void main(String[] args) {
        int day = 0; // Day to be determined
        int answer;

        int[][][] dates = {
            {{1, 3, 5, 7},
             {9, 11, 13, 15},
             {17, 19, 21, 23},
             {25, 27, 29, 31}},
            {{2, 3, 6, 7},
             {10, 11, 14, 15},
             {18, 19, 22, 23},
             {26, 27, 30, 31}},
            {{4, 5, 6, 7},
             {12, 13, 14, 15},
             {20, 21, 22, 23},
             {28, 29, 30, 31}},
            {{8, 9, 10, 11},
             {12, 13, 14, 15},
             {24, 25, 26, 27},
             {28, 29, 30, 31}},
            {{16, 17, 18, 19},
             {20, 21, 22, 23},
             {24, 25, 26, 27},
             {28, 29, 30, 31}}};

        // Create a Scanner
        Scanner input = new Scanner(System.in);

        for (int i = 0; i < 5; i++) {
            System.out.println("Is your birthday in Set" + (i + 1) + "?"); // Set i
            for (int j = 0; j < 4; j++) {
                for (int k = 0; k < 4; k++)
                    System.out.printf("%4d", dates[i][j][k]);
                System.out.println();
            }
            System.out.print("Enter 0 for No and 1 for Yes: ");
            answer = input.nextInt();

            if (answer == 1) // add to day
                day += dates[i][0][0];
        }
    }
}
```

This code implements the program described in the case study, using a three-dimensional array to store the possible birthdays and a loop to prompt the user for the answers. The average daily temperature and humidity are calculated and displayed, and the program calculates the user’s birthday by adding the days from the sets based on the user’s input.
A three-dimensional array `dates` is created in Lines 8–28. This array stores five sets of numbers. Each set is a 4-by-4 two-dimensional array.

The loop starting from line 33 displays the numbers in each set and prompts the user to answer whether the birthday is in the set (lines 41–42). If the day is in the set, the first number (`dates[i][0][0]`) in the set is added to variable `day` (line 45).

**8.8** Declare an array variable for a three-dimensional array, create a $4 \times 6 \times 5$ `int` array, and assign its reference to the variable. **Check Point**

**8.9** Assume `int[][][] x = new char[12][5][2]`, how many elements are in the array? What are `x.length`, `x[2].length`, and `x[0][0].length`?

**8.10** Show the output of the following code:

```java
int[][][] array = {{{1, 2}, {3, 4}}, {{5, 6}, {7, 8}}};
System.out.println(array[0][0][0]);
System.out.println(array[1][1][1]);
```

**CHAPTER SUMMARY**

1. A two-dimensional array can be used to store a table.

2. A variable for two-dimensional arrays can be declared using the syntax:
   `elementType[][] arrayVar`.

3. A two-dimensional array can be created using the syntax:
   `new elementType[ROW_SIZE][COLUMN_SIZE]`.

4. Each element in a two-dimensional array is represented using the syntax:
   `arrayVar[rowIndex][columnIndex]`.

5. You can create and initialize a two-dimensional array using an array initializer with the syntax:
   `elementType[][] arrayVar = {{row values}, . . . , {row values}}`.

6. You can use arrays of arrays to form multidimensional arrays. For example, a variable for three-dimensional arrays can be declared as `elementType[][][] arrayVar`, and a three-dimensional array can be created using `new elementType[size1][size2][size3]`.

**Quiz**

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

**PROGRAMMING EXERCISES**

*8.1 (Sum elements column by column) Write a method that returns the sum of all the elements in a specified column in a matrix using the following header:

```java
public static double sumColumn(double[][] m, int columnIndex)
```
Write a test program that reads a 3-by-4 matrix and displays the sum of each column. Here is a sample run:

```
Enter a 3-by-4 matrix row by row:
1.5 2 3 4
5.5 6 7 8
9.5 1 3 1
Sum of the elements at column 0 is 16.5
Sum of the elements at column 1 is 9.0
Sum of the elements at column 2 is 13.0
Sum of the elements at column 3 is 13.0
```

**8.2** *(Sum the major diagonal in a matrix)* Write a method that sums all the numbers in the major diagonal in an \( n \times n \) matrix of `double` values using the following header:

```java
public static double sumMajorDiagonal(double[][] m)
```

Write a test program that reads a 4-by-4 matrix and displays the sum of all its elements on the major diagonal. Here is a sample run:

```
Enter a 4-by-4 matrix row by row:
1 2 3 4.0
5 6.5 7 8
9 10 11 12
13 14 15 16
Sum of the elements in the major diagonal is 34.5
```

**8.3** *(Sort students on grades)* Rewrite Listing 8.2, GradeExam.java, to display the students in increasing order of the number of correct answers.

**8.4** *(Compute the weekly hours for each employee)* Suppose the weekly hours for all employees are stored in a two-dimensional array. Each row records an employee’s seven-day work hours with seven columns. For example, the following array stores the work hours for eight employees. Write a program that displays employees and their total hours in decreasing order of the total hours.

<table>
<thead>
<tr>
<th>Employee</th>
<th>Su</th>
<th>M</th>
<th>T</th>
<th>W</th>
<th>Th</th>
<th>F</th>
<th>Sa</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>2</td>
<td>4</td>
<td>3</td>
<td>4</td>
<td>5</td>
<td>8</td>
<td>8</td>
</tr>
<tr>
<td>1</td>
<td>7</td>
<td>3</td>
<td>4</td>
<td>3</td>
<td>4</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
<td>3</td>
<td>4</td>
<td>3</td>
<td>3</td>
<td>2</td>
<td>2</td>
</tr>
<tr>
<td>3</td>
<td>9</td>
<td>3</td>
<td>4</td>
<td>7</td>
<td>3</td>
<td>4</td>
<td>1</td>
</tr>
<tr>
<td>4</td>
<td>3</td>
<td>5</td>
<td>4</td>
<td>3</td>
<td>6</td>
<td>3</td>
<td>8</td>
</tr>
<tr>
<td>5</td>
<td>3</td>
<td>4</td>
<td>4</td>
<td>6</td>
<td>3</td>
<td>4</td>
<td>4</td>
</tr>
<tr>
<td>6</td>
<td>3</td>
<td>7</td>
<td>4</td>
<td>8</td>
<td>3</td>
<td>8</td>
<td>4</td>
</tr>
<tr>
<td>7</td>
<td>6</td>
<td>3</td>
<td>5</td>
<td>9</td>
<td>2</td>
<td>7</td>
<td>9</td>
</tr>
</tbody>
</table>

**8.5** *(Algebra: add two matrices)* Write a method to add two matrices. The header of the method is as follows:

```java
public static double[][] addMatrix(double[][] a, double[][] b)
```
In order to be added, the two matrices must have the same dimensions and the same or compatible types of elements. Let \( c \) be the resulting matrix. Each element \( c_{ij} \) is \( a_{ij} + b_{ij} \). For example, for two \( 3 \times 3 \) matrices \( a \) and \( b \), \( c \) is

\[
\begin{pmatrix}
  a_{11} & a_{12} & a_{13} \\
  a_{21} & a_{22} & a_{23} \\
  a_{31} & a_{32} & a_{33}
\end{pmatrix}
+ 
\begin{pmatrix}
  b_{11} & b_{12} & b_{13} \\
  b_{21} & b_{22} & b_{23} \\
  b_{31} & b_{32} & b_{33}
\end{pmatrix}
= 
\begin{pmatrix}
  a_{11} + b_{11} & a_{12} + b_{12} & a_{13} + b_{13} \\
  a_{21} + b_{21} & a_{22} + b_{22} & a_{23} + b_{23} \\
  a_{31} + b_{31} & a_{32} + b_{32} & a_{33} + b_{33}
\end{pmatrix}
\]

Write a test program that prompts the user to enter two \( 3 \times 3 \) matrices and displays their sum. Here is a sample run:

Enter matrix1: 1 2 3 4 5 6 7 8 9
Enter matrix2: 0 2 4 1 4.5 2.2 1.1 4.3 5.2
The matrices are added as follows
1.0 2.0 3.0 0.0 2.0 4.0 1.0 4.0 7.0
4.0 5.0 6.0 + 1.0 4.5 2.2 = 5.0 9.5 8.2
7.0 8.0 9.0 1.1 4.3 5.2 = 8.1 12.3 14.2

**8.6 (Algebra: multiply two matrices)** Write a method to multiply two matrices. The header of the method is:

```java
public static double[][] multiplyMatrix(double[][] a, double[][] b)
```

To multiply matrix \( a \) by matrix \( b \), the number of columns in \( a \) must be the same as the number of rows in \( b \), and the two matrices must have elements of the same or compatible types. Let \( c \) be the result of the multiplication. Assume the column size of matrix \( a \) is \( n \). Each element \( c_{ij} \) is \( a_{i1} \times b_{1j} + a_{i2} \times b_{2j} + \ldots + a_{in} \times b_{nj} \). For example, for two \( 3 \times 3 \) matrices \( a \) and \( b \), \( c \) is

\[
\begin{pmatrix}
  a_{11} & a_{12} & a_{13} \\
  a_{21} & a_{22} & a_{23} \\
  a_{31} & a_{32} & a_{33}
\end{pmatrix}
\times 
\begin{pmatrix}
  b_{11} & b_{12} & b_{13} \\
  b_{21} & b_{22} & b_{23} \\
  b_{31} & b_{32} & b_{33}
\end{pmatrix}
= 
\begin{pmatrix}
  c_{11} & c_{12} & c_{13} \\
  c_{21} & c_{22} & c_{23} \\
  c_{31} & c_{32} & c_{33}
\end{pmatrix}
\]

where \( c_{ij} = a_{i1} \times b_{1j} + a_{i2} \times b_{2j} + a_{i3} \times b_{3j} \).

Write a test program that prompts the user to enter two \( 3 \times 3 \) matrices and displays their product. Here is a sample run:

Enter matrix1: 1 2 3 4 5 6 7 8 9
Enter matrix2: 0 2 4 1 4.5 2.2 1.1 4.3 5.2
The multiplication of the matrices is
1 2 3 0.2 4.0 5.3 23.9 24
4 5 6 1.4 5.2 11.6 56.3 58.2
7 8 9 1.1 4.3 5.2 17.9 88.7 92.4

**8.7 (Points nearest to each other)** Listing 8.3 gives a program that finds two points in a two-dimensional space nearest to each other. Revise the program so that it finds two points in a three-dimensional space nearest to each other. Use a two-dimensional array to represent the points. Test the program using the following points:

```java
double[][] points = {{-1, 0, 3}, {-1, -1, -1}, {4, 1, 1}, {2, 0.5, 9}, {3.5, 2, -1}, {3, 1.5, 3}, {-1.5, 4, -2}, {5.5, 4, -0.5}};
```
The formula for computing the distance between two points \((x_1, y_1, z_1)\) and \((x_2, y_2, z_2)\) is \(\sqrt{(x_2-x_1)^2 + (y_2-y_1)^2 + (z_2-z_1)^2}\).

**8.8** *(All closest pairs of points)* Revise Listing 8.3, FindNearestPoints.java, to display all closest pairs of points with the same minimum distance. Here is a sample run:

```
Enter the number of points: 8
Enter 8 points: 0 0 1 1 -1 -1  2 2 -2 -2 -3 -3 -4 -4  5 5
The closest two points are (0.0, 0.0) and (1.0, 1.0)
The closest two points are (0.0, 0.0) and (-1.0, -1.0)
The closest two points are (1.0, 1.0) and (2.0, 2.0)
The closest two points are (-1.0, -1.0) and (-2.0, -2.0)
The closest two points are (-2.0, -2.0) and (-3.0, -3.0)
The closest two points are (-3.0, -3.0) and (-4.0, -4.0)
Their distance is 1.4142135623730951
```

**8.9** *(Game: play a tic-tac-toe game)* In a game of tic-tac-toe, two players take turns marking an available cell in a 3 \(\times\) 3 grid with their respective tokens (either X or O). When one player has placed three tokens in a horizontal, vertical, or diagonal row on the grid, the game is over and that player has won. A draw (no winner) occurs when all the cells on the grid have been filled with tokens and neither player has achieved a win. Create a program for playing tic-tac-toe.

The program prompts two players to enter an X token and O token alternately. Whenever a token is entered, the program redisplays the board on the console and determines the status of the game (win, draw, or continue). Here is a sample run:

```
Enter a row (0, 1, or 2) for player X: 1
Enter a column (0, 1, or 2) for player X: 1

| | | |
| | | |
| | | |
Enter a row (0, 1, or 2) for player X: 1
Enter a column (0, 1, or 2) for player X: 1

| | | |
| | | |
| | | |
Enter a row (0, 1, or 2) for player 0: 1
Enter a column (0, 1, or 2) for player 0: 2

| | | |
| | | |
| | | |
```
*8.10  (Largest row and column) Write a program that randomly fills in 0s and 1s into a 4-by-4 matrix, prints the matrix, and finds the first row and column with the most 1s. Here is a sample run of the program:

```
0011
0011
1101
1010
The largest row index: 2
The largest column index: 2
```

**8.11  (Game: nine heads and tails) Nine coins are placed in a 3-by-3 matrix with some face up and some face down. You can represent the state of the coins using a 3-by-3 matrix with values 0 (heads) and 1 (tails). Here are some examples:

```
0 0 0   1 0 1   1 1 0   1 0 1   1 0 0
0 1 0   0 0 1   1 0 0   1 1 0   1 1 1
0 0 0   1 0 0   0 0 1   1 0 0   1 1 0
```

Each state can also be represented using a binary number. For example, the preceding matrices correspond to the numbers

```
000010000 101001100 110100001 101110100 100111110
```

There are a total of 512 possibilities, so you can use decimal numbers 0, 1, 2, 3, . . . , and 511 to represent all states of the matrix. Write a program that prompts the user to enter a number between 0 and 511 and displays the corresponding matrix with the characters H and T. Here is a sample run:

```
Enter a number between 0 and 511: 7
H H H
H H H
T T T
```

The user entered 7, which corresponds to 000000111. Since 0 stands for H and 1 for T, the output is correct.

**8.12  (Financial application: compute tax) Rewrite Listing 3.5, ComputeTax.java, using arrays. For each filing status, there are six tax rates. Each rate is applied to a certain amount of taxable income. For example, from the taxable income of $400,000 for a single filer, $8,350 is taxed at 10%, (33,950 − 8,350) at 15%,
The brackets for each rate for all the filing statuses can be represented in a two-dimensional array as follows:

```java
int[][] brackets = {
    {8350, 33950, 82250, 171550, 372950}, // Single filer
    {16700, 67900, 137050, 20885, 372950}, // Married jointly
    // or qualifying widow(er)
    {8350, 33950, 68525, 104425, 186475}, // Married separately
    {11950, 45500, 117450, 190200, 372950} // Head of household
};
```

Suppose the taxable income is $400,000 for single filers. The tax can be computed as follows:

```java
tax = brackets[0][0] * rates[0] +
    (brackets[0][1] - brackets[0][0]) * rates[1] +
    (brackets[0][2] - brackets[0][1]) * rates[2] +
    (brackets[0][3] - brackets[0][2]) * rates[3] +
    (brackets[0][4] - brackets[0][3]) * rates[4] +
    (400000 - brackets[0][4]) * rates[5]
```

*(Locate the largest element)* Write the following method that returns the location of the largest element in a two-dimensional array.

```java
public static int[] locateLargest(double[][] a)
```

The return value is a one-dimensional array that contains two elements. These two elements indicate the row and column indices of the largest element in the two-dimensional array. Write a test program that prompts the user to enter a two-dimensional array and displays the location of the largest element in the array. Here is a sample run:

```
Enter the number of rows and columns of the array: 3 4
Enter the array:
23.5 35 2 10
4.5 3 45 3.5
35 44 5.5 9.6
The location of the largest element is at (1, 2)
```

*(Explore matrix)* Write a program that prompts the user to enter the length of a square matrix, randomly fills in 0s and 1s into the matrix, prints the matrix, and finds the rows, columns, and diagonals with all 0s or 1s. Here is a sample run of the program:
8.15 (Geometry: same line?) Programming Exercise 6.39 gives a method for testing whether three points are on the same line. Write the following method to test whether all the points in the array `points` are on the same line.

```java
public static boolean sameLine(double[][] points)
```

Write a program that prompts the user to enter five points and displays whether they are on the same line. Here are sample runs:

```
Enter the size for the matrix: 4
0111
0000
0100
1111
All 0s on row 1
All 1s on row 3
No same numbers on a column
No same numbers on the major diagonal
No same numbers on the sub-diagonal
```

```
Enter five points: 3.4 2 6.5 9.5 2.3 2.3 5.5 5 -5 4
The five points are not on the same line
```

```
Enter five points: 1 1 2 2 3 3 4 4 5 5
The five points are on the same line
```

8.16 (Sort two-dimensional array) Write a method to sort a two-dimensional array using the following header:

```java
public static void sort(int m[][])```

The method performs a primary sort on rows and a secondary sort on columns. For example, the following array

```
{{4, 2}, {1, 7}, {4, 5}, {1, 2}, {1, 1}, {4, 1}}
```

will be sorted to

```
{{1, 1}, {1, 2}, {1, 7}, {4, 1}, {4, 2}, {4, 5}}.
```

8.17 (Financial tsunami) Banks lend money to each other. In tough economic times, if a bank goes bankrupt, it may not be able to pay back the loan. A bank's total assets are its current balance plus its loans to other banks. The diagram in Figure 8.8 shows five banks. The banks' current balances are 25, 125, 175, 75, and 181 million dollars, respectively. The directed edge from node 1 to node 2 indicates that bank 1 lends 40 million dollars to bank 2.
If a bank’s total assets are under a certain limit, the bank is unsafe. The money it borrowed cannot be returned to the lender, and the lender cannot count the loan in its total assets. Consequently, the lender may also be unsafe, if its total assets are under the limit. Write a program to find all the unsafe banks. Your program reads the input as follows. It first reads two integers \( n \) and \( \text{limit} \), where \( n \) indicates the number of banks and \( \text{limit} \) is the minimum total assets for keeping a bank safe. It then reads \( n \) lines that describe the information for \( n \) banks with IDs from 0 to \( n-1 \).

The first number in the line is the bank’s balance, the second number indicates the number of banks that borrowed money from the bank, and the rest are pairs of two numbers. Each pair describes a borrower. The first number in the pair is the borrower’s ID and the second is the amount borrowed. For example, the input for the five banks in Figure 8.8 is as follows (note that the limit is 201):

```
5 201
25 2 1 100.5 4 320.5
125 2 2 40 3 85
175 2 0 125 3 75
75 1 0 125
181 1 2 125
```

The total assets of bank 3 are \((75 + 125)\), which is under 201, so bank 3 is unsafe. After bank 3 becomes unsafe, the total assets of bank 1 fall below \((125 + 40)\). Thus, bank 1 is also unsafe. The output of the program should be

Unsafe banks are 3 1

(Hint: Use a two-dimensional array \( \text{borrowers} \) to represent loans. \( \text{borrowers}[i][j] \) indicates the loan that bank \( i \) lends to bank \( j \). Once bank \( j \) becomes unsafe, \( \text{borrowers}[i][j] \) should be set to 0.)

*8.18 (Shuffle rows) Write a method that shuffles the rows in a two-dimensional \( \text{int} \) array using the following header:

```java
public static void shuffle(int[][] m)
```

Write a test program that shuffles the following matrix:

```
int[][] m = {{1, 2}, {3, 4}, {5, 6}, {7, 8}, {9, 10}};
```

**8.19 (Pattern recognition: four consecutive equal numbers) Write the following method that tests whether a two-dimensional array has four consecutive numbers of the same value, either horizontally, vertically, or diagonally.

```java
public static boolean isConsecutiveFour(int[][] values)
```
Write a test program that prompts the user to enter the number of rows and columns of a two-dimensional array and then the values in the array and displays true if the array contains four consecutive numbers with the same value. Otherwise, display false. Here are some examples of the true cases:

\[
\begin{array}{cccccc}
0 & 1 & 0 & 3 & 1 & 6 \\
0 & 1 & 6 & 8 & 6 & 0 \\
5 & 6 & 2 & 1 & 8 & 2 \\
6 & 5 & 6 & 1 & 1 & 9 \\
1 & 3 & 6 & 1 & 4 & 0 \\
3 & 3 & 3 & 3 & 4 & 0 \\
\end{array}
\quad
\begin{array}{cccccc}
0 & 1 & 0 & 3 & 1 & 6 \\
0 & 1 & 6 & 8 & 6 & 0 \\
5 & 5 & 2 & 1 & 8 & 2 \\
6 & 5 & 6 & 1 & 1 & 9 \\
1 & 5 & 6 & 1 & 4 & 0 \\
3 & 5 & 3 & 3 & 4 & 0 \\
\end{array}
\quad
\begin{array}{cccccc}
0 & 1 & 0 & 3 & 1 & 6 \\
0 & 1 & 6 & 8 & 6 & 0 \\
5 & 6 & 2 & 1 & 6 & 2 \\
6 & 5 & 6 & 1 & 1 & 9 \\
1 & 3 & 6 & 1 & 4 & 0 \\
3 & 6 & 3 & 3 & 4 & 0 \\
\end{array}
\quad
\begin{array}{cccccc}
0 & 1 & 0 & 3 & 1 & 6 \\
0 & 1 & 6 & 8 & 6 & 0 \\
6 & 6 & 2 & 1 & 8 & 2 \\
6 & 5 & 6 & 1 & 1 & 9 \\
1 & 3 & 6 & 1 & 4 & 0 \\
3 & 3 & 9 & 3 & 4 & 0 \\
\end{array}
\]

***8.20 (Game: connect four) Connect four is a two-player board game in which the players alternately drop colored disks into a seven-column, six-row vertically suspended grid, as shown below.

The objective of the game is to connect four same-colored disks in a row, a column, or a diagonal before your opponent can do likewise. The program prompts two players to drop a red or yellow disk alternately. In the preceding figure, the red disk is shown in a dark color and the yellow in a light color. Whenever a disk is dropped, the program redisplays the board on the console and determines the status of the game (win, draw, or continue). Here is a sample run:

```
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |
-----------------------
Drop a red disk at column (0-6): 0
```

```
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |
-----------------------
```
*8.21* (Central city) Given a set of cities, the central city is the city that has the shortest total distance to all other cities. Write a program that prompts the user to enter the number of the cities and the locations of the cities (coordinates), and finds the central city and its total distance to all other cities.

Enter the number of cities: 5
Enter the coordinates of the cities: 2.5 5 5.1 3 1 9 5.4 54 5.5 2.1
The central city is at (2.5, 5.0)
The total distance to all other cities is 60.81

*8.22* (Even number of 1s) Write a program that generates a 6-by-6 two-dimensional matrix filled with 0s and 1s, displays the matrix, and checks if every row and every column have an even number of 1s.

*8.23* (Game: find the flipped cell) Suppose you are given a 6-by-6 matrix filled with 0s and 1s. All rows and all columns have an even number of 1s. Let the user flip one cell (i.e., flip from 1 to 0 or from 0 to 1) and write a program to find which cell was flipped. Your program should prompt the user to enter a 6-by-6 array with 0s and 1s and find the first row \( r \) and first column \( c \) where the even number of the 1s property is violated (i.e., the number of 1s is not even). The flipped cell is at \((r, c)\). Here is a sample run:

Enter a 6-by-6 matrix row by row:
1 1 1 0 1 1
1 1 1 1 0 0
0 1 0 1 1 1
1 1 1 1 1 1
0 1 1 1 1 0
1 0 0 0 0 1
The flipped cell is at (0, 1)
*8.24 (Check Sudoku solution) Listing 8.4 checks whether a solution is valid by checking whether every number is valid in the board. Rewrite the program by checking whether every row, every column, and every small box has the numbers 1 to 9.

*8.25 (Markov matrix) An \( n \times n \) matrix is called a positive Markov matrix if each element is positive and the sum of the elements in each column is 1. Write the following method to check whether a matrix is a Markov matrix.

\[
\text{public static boolean isMarkovMatrix(double[][] m)}
\]

Write a test program that prompts the user to enter a \( 3 \times 3 \) matrix of double values and tests whether it is a Markov matrix. Here are sample runs:

Enter a 3-by-3 matrix row by row:
0.15 0.875 0.375
0.55 0.005 0.225
0.30 0.12 0.4
It is a Markov matrix

Enter a 3-by-3 matrix row by row:
0.95 -0.875 0.375
0.65 0.005 0.225
0.30 0.22 -0.4
It is not a Markov matrix

*8.26 (Row sorting) Implement the following method to sort the rows in a two-dimensional array. A new array is returned and the original array is intact.

\[
\text{public static double[][] sortRows(double[][] m)}
\]

Write a test program that prompts the user to enter a \( 3 \times 3 \) matrix of double values and displays a new row-sorted matrix. Here is a sample run:

Enter a 3-by-3 matrix row by row:
0.15 0.875 0.375
0.55 0.005 0.225
0.30 0.12 0.4

The row-sorted array is
0.15 0.375 0.875
0.005 0.225 0.55
0.12 0.30 0.4

*8.27 (Column sorting) Implement the following method to sort the columns in a two-dimensional array. A new array is returned and the original array is intact.

\[
\text{public static double[][] sortColumns(double[][] m)}
\]
Write a test program that prompts the user to enter a $3 \times 3$ matrix of double values and displays a new column-sorted matrix. Here is a sample run:

Enter a 3-by-3 matrix row by row:
0.15 0.875 0.375
0.55 0.005 0.225
0.30 0.12 0.4

The column-sorted array is
0.15 0.005 0.225
0.3 0.12 0.375
0.55 0.875 0.4

8.28 \textbf{(Strictly identical arrays)} The two-dimensional arrays $m_1$ and $m_2$ are strictly identical if their corresponding elements are equal. Write a method that returns true if $m_1$ and $m_2$ are strictly identical, using the following header:

\begin{verbatim}
public static boolean equals(int[][] m1, int[][] m2)
\end{verbatim}

Write a test program that prompts the user to enter two $3 \times 3$ arrays of integers and displays whether the two are strictly identical. Here are the sample runs.

Enter list1: 51 22 25 6 1 4 24 54 6
Enter list2: 51 22 25 6 1 4 24 54 6
The two arrays are strictly identical

Enter list1: 51 22 25 6 1 4 24 54 6
Enter list2: 51 22 25 6 1 4 24 54 6
The two arrays are not strictly identical

8.29 \textbf{(Identical arrays)} The two-dimensional arrays $m_1$ and $m_2$ are identical if they have the same contents. Write a method that returns true if $m_1$ and $m_2$ are identical, using the following header:

\begin{verbatim}
public static boolean equals(int[][] m1, int[][] m2)
\end{verbatim}

Write a test program that prompts the user to enter two $3 \times 3$ arrays of integers and displays whether the two are identical. Here are the sample runs.

Enter list1: 51 25 22 6 1 4 24 54 6
Enter list2: 51 22 25 6 1 4 24 54 6
The two arrays are identical

Enter list1: 51 5 22 6 1 4 24 54 6
Enter list2: 51 22 25 6 1 4 24 54 6
The two arrays are not identical
*8.30 (Algebra: solve linear equations) Write a method that solves the following 2 \times 2 system of linear equations:

\[
\begin{align*}
    a_{00}x + a_{01}y &= b_0 \\
    a_{10}x + a_{11}y &= b_1 
\end{align*}
\]

\[
\begin{align*}
    x &= \frac{b_0a_{11} - b_1a_{01}}{a_{00}a_{11} - a_{01}a_{10}} \\
    y &= \frac{b_0a_{10} - b_1a_{00}}{a_{00}a_{11} - a_{01}a_{10}}
\end{align*}
\]

The method header is:

```java
public static double[] linearEquation(double[][] a, double[] b)
```

The method returns `null` if \(a_{00}a_{11} - a_{01}a_{10}\) is 0. Write a test program that prompts the user to enter \(a_{00}, a_{01}, a_{10}, a_{11}, b_0, \) and \(b_1\), and displays the result. If \(a_{00}a_{11} - a_{01}a_{10}\) is 0, report that “The equation has no solution.” A sample run is similar to Programming Exercise 3.3.

*8.31 (Geometry: intersecting point) Write a method that returns the intersecting point of two lines. The intersecting point of the two lines can be found by using the formula shown in Programming Exercise 3.25. Assume that \((x_1, y_1)\) and \((x_2, y_2)\) are the two points on line 1 and \((x_3, y_3)\) and \((x_4, y_4)\) are on line 2. The method header is:

```java
public static double[] getIntersectingPoint(double[][] points)
```

The points are stored in a 4-by-2 two-dimensional array `points` with `points[0][0]` and `points[0][1]` for \((x_1, y_1)\). The method returns the intersecting point or `null` if the two lines are parallel. Write a program that prompts the user to enter four points and displays the intersecting point. See Programming Exercise 3.25 for a sample run.

*8.32 (Geometry: area of a triangle) Write a method that returns the area of a triangle using the following header:

```java
public static double getTriangleArea(double[][] points)
```

The points are stored in a 3-by-2 two-dimensional array `points` with `points[0][0]` and `points[0][1]` for \((x_1, y_1)\). The triangle area can be computed using the formula in Programming Exercise 2.19. The method returns 0 if the three points are on the same line. Write a program that prompts the user to enter three points of a triangle and displays the triangle’s area. Here is a sample run of the program:

Enter \(x_1, y_1, x_2, y_2, x_3, y_3\): 2.5 2 5 -1.0 4.0 2.0
The area of the triangle is 2.25

Enter \(x_1, y_1, x_2, y_2, x_3, y_3\): 2 2 4.5 4.5 6 6
The three points are on the same line

*8.33 (Geometry: polygon subareas) A convex 4-vertex polygon is divided into four triangles, as shown in Figure 8.9.

Write a program that prompts the user to enter the coordinates of four vertices and displays the areas of the four triangles in increasing order. Here is a sample run:

Enter \(x_1, y_1, x_2, y_2, x_3, y_3, x_4, y_4\): -2.5 2 4 4 3 -2 -2 -3.5
The areas are 6.17 7.96 8.08 10.42
*8.34  \textit{(Geometry: rightmost lowest point)} In computational geometry, often you need to find the rightmost lowest point in a set of points. Write the following method that returns the rightmost lowest point in a set of points.

\begin{verbatim}
public static double[] getRightmostLowestPoint(double[][] points)
\end{verbatim}

Write a test program that prompts the user to enter the coordinates of six points and displays the rightmost lowest point. Here is a sample run:

\begin{verbatim}
Enter 6 points: 1.5 2.5 -3 4.5 5.6 -7 6.5 -7 8 1 10 2.5
The rightmost lowest point is (6.5, -7.0)
\end{verbatim}

**8.35  \textit{(Largest block)} Given a square matrix with the elements 0 or 1, write a program to find a maximum square submatrix whose elements are all 1s. Your program should prompt the user to enter the number of rows in the matrix. The program then displays the location of the first element in the maximum square submatrix and the number of the rows in the submatrix. Here is a sample run:

\begin{verbatim}
Enter the number of rows in the matrix: 5
Enter the matrix row by row:
1 0 1 0 1
1 1 1 0 1
1 0 1 1 1
1 0 1 1 1
1 0 1 1 1
The maximum square submatrix is at (2, 2) with size 3
\end{verbatim}

Your program should implement and use the following method to find the maximum square submatrix:

\begin{verbatim}
public static int[] findLargestBlock(int[][] m)
\end{verbatim}

The return value is an array that consists of three values. The first two values are the row and column indices for the first element in the submatrix, and the third value is the number of the rows in the submatrix.

**8.36  \textit{(Latin square)} A Latin square is an \(n\)-by-\(n\) array filled with \(n\) different Latin letters, each occurring exactly once in each row and once in each column. Write a
program that prompts the user to enter the number \( n \) and the array of characters, as shown in the sample output, and checks if the input array is a Latin square. The characters are the first \( n \) characters starting from A.

```
Enter number \( n \): 4
Enter 4 rows of letters separated by spaces:
A B C D
B A D C
C D B A
D C A B
The input array is a Latin square
```

```
Enter number \( n \): 3
Enter 3 rows of letters separated by spaces:
A F D
Wrong input: the letters must be from A to C
```

**8.37** (Guess the capitals) Write a program that repeatedly prompts the user to enter a capital for a state. Upon receiving the user input, the program reports whether the answer is correct. Assume that 50 states and their capitals are stored in a two-dimensional array, as shown in Figure 8.10. The program prompts the user to answer all states’ capitals and displays the total correct count. The user’s answer is not case-sensitive.

![Figure 8.10](image-url) A two-dimensional array stores states and their capitals.

Here is a sample run:

```
What is the capital of Alabama? Montgomery
The correct answer should be Montgomery
What is the capital of Alaska? Juneau
Your answer is correct
What is the capital of Arizona? ...
... The correct count is 35
```
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OBJECTS AND CLASSES

Objectives

- To describe objects and classes, and use classes to model objects (§9.2).
- To use UML graphical notation to describe classes and objects (§9.2).
- To demonstrate how to define classes and create objects (§9.3).
- To create objects using constructors (§9.4).
- To access objects via object reference variables (§9.5).
- To define a reference variable using a reference type (§9.5.1).
- To access an object’s data and methods using the object member access operator (. ) (§9.5.2).
- To define data fields of reference types and assign default values for an object's data fields (§9.5.3).
- To distinguish between object reference variables and primitive data type variables (§9.5.4).
- To use the Java library classes `Date`, `Random`, and `Point2D` (§9.6).
- To distinguish between instance and static variables and methods (§9.7).
- To define private data fields with appropriate getter and setter methods (§9.8).
- To encapsulate data fields to make classes easy to maintain (§9.9).
- To develop methods with object arguments and differentiate between primitive-type arguments and object-type arguments (§9.10).
- To store and process objects in arrays (§9.11).
- To create immutable objects from immutable classes to protect the contents of objects (§9.12).
- To determine the scope of variables in the context of a class (§9.13).
- To use the keyword `this` to refer to the calling object itself (§9.14).
9.1 Introduction

Object-oriented programming enables you to develop large-scale software and GUIs effectively.

Having learned the material in the preceding chapters, you are able to solve many programming problems using selections, loops, methods, and arrays. However, these Java features are not sufficient for developing graphical user interfaces and large-scale software systems. Suppose you want to develop a graphical user interface (GUI, pronounced goo-ee) as shown in Figure 9.1. How would you program it?

Key Point

why OOP?

Figure 9.1 The GUI objects are created from classes.

This chapter introduces object-oriented programming, which you can use to develop GUI and large-scale software systems.

9.2 Defining Classes for Objects

A class defines the properties and behaviors for objects.

Object-oriented programming (OOP) involves programming using objects. An object represents an entity in the real world that can be distinctly identified. For example, a student, a desk, a circle, a button, and even a loan can all be viewed as objects. An object has a unique identity, state, and behavior.

- The state of an object (also known as its properties or attributes) is represented by data fields with their current values. A circle object, for example, has a data field radius, which is the property that characterizes a circle. A rectangle object has the data fields width and height, which are the properties that characterize a rectangle.

- The behavior of an object (also known as its actions) is defined by methods. To invoke a method on an object is to ask the object to perform an action. For example, you may define methods named getArea() and getPerimeter() for circle objects. A circle object may invoke getArea() to return its area and getPerimeter() to return its perimeter. You may also define the setRadius(radius) method. A circle object can invoke this method to change its radius.

Objects of the same type are defined using a common class. A class is a template, blueprint, or contract that defines what an object’s data fields and methods will be. An object is an instance of a class. You can create many instances of a class. Creating an instance is referred to as instantiation. The terms object and instance are often interchangeable. The relationship between classes and objects is analogous to that between an apple-pie recipe and apple pies: You can make as many apple pies as you want from a single recipe. Figure 9.2 shows a class named Circle and its three objects.

A Java class uses variables to define data fields and methods to define actions. Additionally, a class provides methods of a special type, known as constructors, which are invoked to create a new object. A constructor can perform any action, but constructors are designed to perform initializing actions, such as initializing the data fields of objects. Figure 9.3 shows an example of defining the class for circle objects.
The \texttt{Circle} class is different from all of the other classes you have seen thus far. It does not have a \texttt{main} method and therefore cannot be run; it is merely a definition for circle objects. The class that contains the \texttt{main} method will be referred to in this book, for convenience, as the \texttt{main class}.

The illustration of class templates and objects in Figure 9.2 can be standardized using \textit{Unified Modeling Language (UML)} notation. This notation, as shown in Figure 9.4, is called a \textit{UML class diagram}, or simply a \textit{class diagram}. In the class diagram, the data field is denoted as

\[\text{dataFieldName: dataFieldType}\]

The constructor is denoted as

\[\text{ClassName}(\text{parameterName: parameterType})\]
The method is denoted as

```
methodName(parameterName: parameterType): returnType
```

### 9.3 Example: Defining Classes and Creating Objects

**Classes are definitions for objects and objects are created from classes.**

This section gives two examples of defining classes and uses the classes to create objects. Listing 9.1 is a program that defines the `Circle` class and uses it to create objects. The program constructs three circle objects with radius 1, 25, and 125 and displays the radius and area of each of the three circles. It then changes the radius of the second object to 100 and displays its new radius and area.

#### Key Point

To avoid a naming conflict with several enhanced versions of the `Circle` class introduced later in the chapter, the `Circle` class in this example is named `SimpleCircle`. For simplicity, we will still refer to the class in the text as `Circle`.

#### Listing 9.1 TestSimpleCircle.java

```java
public class TestSimpleCircle {
    public static void main(String[] args) {
        // Create a circle with radius 1
        SimpleCircle circle1 = new SimpleCircle();
        System.out.println("The area of the circle of radius "+ circle1.radius + " is " + circle1.getArea());

        // Create a circle with radius 25
        SimpleCircle circle2 = new SimpleCircle(25);
        System.out.println("The area of the circle of radius "+ circle2.radius + " is " + circle2.getArea());

        // Create a circle with radius 125
        SimpleCircle circle3 = new SimpleCircle(125);
        System.out.println("The area of the circle of radius "+ circle3.radius + " is " + circle3.getArea());

        // Modify circle radius
        circle2.radius = 100; // or circle2.setRadius(100)
        System.out.println("The area of the circle of radius "+ circle2.radius + " is " + circle2.getArea());
    }
}
```
9.3 Example: Defining Classes and Creating Objects

```java
// Define the circle class with two constructors
class SimpleCircle {
    double radius;

    /** Construct a circle with radius 1 */
    SimpleCircle() {
        radius = 1;
    }

    /** Construct a circle with a specified radius */
    SimpleCircle(double newRadius) {
        radius = newRadius;
    }

    /** Return the area of this circle */
    double getArea() {
        return radius * radius * Math.PI;
    }

    /** Return the perimeter of this circle */
    double getPerimeter() {
        return 2 * radius * Math.PI;
    }

    /** Set a new radius for this circle */
    void setRadius(double newRadius) {
        radius = newRadius;
    }
}
```

The program contains two classes. The first of these, `TestSimpleCircle`, is the main class. Its sole purpose is to test the second class, `SimpleCircle`. Such a program that uses the class is often referred to as a client of the class. When you run the program, the Java runtime system invokes the `main` method in the main class.

You can put the two classes into one file, but only one class in the file can be a public class. Furthermore, the public class must have the same name as the file name. Therefore, the file name is `TestSimpleCircle.java`, since `TestSimpleCircle` is public. Each class in the source code is compiled into a .class file. When you compile `TestSimpleCircle.java`, two class files `TestSimpleCircle.class` and `SimpleCircle.class` are generated, as shown in Figure 9.5.

![Figure 9.5](image)

FIGURE 9.5 Each class in the source code file is compiled into a .class file.
The main class contains the `main` method (line 3) that creates three objects. As in creating an array, the `new` operator is used to create an object from the constructor: `new SimpleCircle()` creates an object with radius 1 (line 5), `new SimpleCircle(25)` creates an object with radius 25 (line 10), and `new SimpleCircle(125)` creates an object with radius 125 (line 15).

These three objects (referenced by `circle1`, `circle2`, and `circle3`) have different data but the same methods. Therefore, you can compute their respective areas by using the `getArea()` method. The data fields can be accessed via the reference of the object using `circle1.radius`, `circle2.radius`, and `circle3.radius`, respectively. The object can invoke its method via the reference of the object using `circle1.getArea()`, `circle2.getArea()`, and `circle3.getArea()`, respectively.

These three objects are independent. The radius of `circle2` is changed to 100 in line 20. The object’s new radius and area are displayed in lines 21–22.

There are many ways to write Java programs. For instance, you can combine the two classes in the example into one, as shown in Listing 9.2.

**LISTING 9.2 SimpleCircle.java**

```
public class SimpleCircle {

    /** Main method */
    public static void main(String[] args) {
        // Create a circle with radius 1
        SimpleCircle circle1 = new SimpleCircle();
        System.out.println("The area of the circle of radius " + circle1.radius + " is " + circle1.getArea());

        // Create a circle with radius 25
        SimpleCircle circle2 = new SimpleCircle(25);
        System.out.println("The area of the circle of radius " + circle2.radius + " is " + circle2.getArea());

        // Create a circle with radius 125
        SimpleCircle circle3 = new SimpleCircle(125);
        System.out.println("The area of the circle of radius " + circle3.radius + " is " + circle3.getArea());

        // Modify circle radius
        circle2.radius = 100;
        System.out.println("The area of the circle of radius " + circle2.radius + " is " + circle2.getArea());
    }

    // data field
    double radius;

    /** No-arg constructor */
    SimpleCircle() {
        radius = 1;
    }

    /** Second constructor */
    SimpleCircle(double newRadius) {
        radius = newRadius;
    }

    /** Method */
    double getArea() {
        return radius * radius * Math.PI;
    }
}
```
Since the combined class has a `main` method, it can be executed by the Java interpreter. The `main` method is the same as that in Listing 9.1. This demonstrates that you can test a class by simply adding a `main` method in the same class.

As another example, consider television sets. Each TV is an object with states (current channel, current volume level, power on or off) and behaviors (change channels, adjust volume, turn on/off). You can use a class to model TV sets. The UML diagram for the class is shown in Figure 9.6.

Listing 9.3 gives a program that defines the `TV` class.

### Listing 9.3  TV.java

```java
public class TV {
    int channel = 1;  // Default channel is 1
    int volumeLevel = 1;  // Default volume level is 1
    boolean on = false;  // TV is off

    public TV() {
    }

    public void turnOn() {
        on = true;
    }

    public void turnOff() {
    }
}
```
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```java
    on = false;

    public void setChannel(int newChannel) {
        if (on && newChannel >= 1 && newChannel <= 120)
            channel = newChannel;
    }

    public void setVolume(int newVolumeLevel) {
        if (on && newVolumeLevel >= 1 && newVolumeLevel <= 7)
            volumeLevel = newVolumeLevel;
    }

    public void channelUp() {
        if (on && channel < 120)
            channel++;
    }

    public void channelDown() {
        if (on && channel > 1)
            channel--;
    }

    public void volumeUp() {
        if (on && volumeLevel < 7)
            volumeLevel++;
    }

    public void volumeDown() {
        if (on && volumeLevel > 1)
            volumeLevel--;
    }

    The constructor and methods in the TV class are defined public so they can be accessed from
other classes. Note that the channel and volume level are not changed if the TV is not on. Before
either of these is changed, its current value is checked to ensure that it is within the correct range.

Listing 9.4 gives a program that uses the TV class to create two objects.

**LISTING 9.4  TestTV.java**

```java
    public class TestTV {
        public static void main(String[] args) {
            TV tv1 = new TV();
            tv1.turnOn();
            tv1.setChannel(30);
            tv1.setVolume(3);

            TV tv2 = new TV();
            tv2.turnOn();
            tv2.channelUp();
            tv2.channelUp();
            tv2.volumeUp();

            System.out.println("tv1's channel is " + tv1.channel
            + " and volume level is " + tv1.volumeLevel);
            System.out.println("tv2's channel is " + tv2.channel
            + " and volume level is " + tv2.volumeLevel);
        }
    }
```
9.4 Constructing Objects Using Constructors

A constructor is invoked to create an object using the new operator.

Constructors are a special kind of method. They have three peculiarities:

- A constructor must have the same name as the class itself.
- Constructors do not have a return type—not even void.
- Constructors are invoked using the new operator when an object is created.

Constructors play the role of initializing objects.

The constructor has exactly the same name as its defining class. Like regular methods, constructors can be overloaded (i.e., multiple constructors can have the same name but different signatures), making it easy to construct objects with different initial data values.

It is a common mistake to put the void keyword in front of a constructor. For example,

```java
public void Circle() {
}
```

In this case, `Circle()` is a method, not a constructor.

Constructors are used to construct objects. To construct an object from a class, invoke a constructor of the class using the new operator, as follows:

```java
new ClassName(arguments);
```

For example, `new Circle()` creates an object of the `Circle` class using the first constructor defined in the `Circle` class, and `new Circle(25)` creates an object using the second constructor defined in the `Circle` class.

A class normally provides a constructor without arguments (e.g., `Circle()`). Such a constructor is referred to as a no-arg or no-argument constructor.

A class may be defined without constructors. In this case, a public no-arg constructor with an empty body is implicitly defined in the class. This constructor, called a default constructor, is provided automatically only if no constructors are explicitly defined in the class.

9.5 What are the differences between constructors and methods?

9.6 When will a class have a default constructor?
9.5 Accessing Objects via Reference Variables

An object’s data and methods can be accessed through the dot (.) operator via the object’s reference variable.

Newly created objects are allocated in the memory. They can be accessed via reference variables.

9.5.1 Reference Variables and Reference Types

Objects are accessed via the object’s reference variables, which contain references to the objects. Such variables are declared using the following syntax:

```java
ClassName objectRefVar;
```

A class is essentially a programmer-defined type. A class is a reference type, which means that a variable of the class type can reference an instance of the class. The following statement declares the variable `myCircle` to be of the `Circle` type:

```java
Circle myCircle;
```

The variable `myCircle` can reference a `Circle` object. The next statement creates an object and assigns its reference to `myCircle`:

```java
myCircle = new Circle();
```

You can write a single statement that combines the declaration of an object reference variable, the creation of an object, and the assigning of an object reference to the variable with the following syntax:

```java
ClassName objectRefVar = new ClassName();
```

Here is an example:

```java
Circle myCircle = new Circle();
```

The variable `myCircle` holds a reference to a `Circle` object.

**Note**

An object reference variable that appears to hold an object actually contains a reference to that object. Strictly speaking, an object reference variable and an object are different, but most of the time the distinction can be ignored. Therefore, it is fine, for simplicity, to say that `myCircle` is a `Circle` object rather than use the longer-winded description that `myCircle` is a variable that contains a reference to a `Circle` object.

**Note**

Arrays are treated as objects in Java. Arrays are created using the `new` operator. An array variable is actually a variable that contains a reference to an array.

9.5.2 Accessing an Object’s Data and Methods

In OOP terminology, an object’s member refers to its data fields and methods. After an object is created, its data can be accessed and its methods can be invoked using the dot operator (.), also known as the object member access operator:

- `objectRefVar.dataField` references a data field in the object.
- `objectRefVar.method(arguments)` invokes a method on the object.
For example, `myCircle.radius` references the radius in `myCircle`, and `myCircle.getArea()` invokes the `getArea` method on `myCircle`. Methods are invoked as operations on objects.

The data field `radius` is referred to as an *instance variable*, because it is dependent on a specific instance. For the same reason, the method `getArea` is referred to as an *instance method*, because you can invoke it only on a specific instance. The object on which an instance method is invoked is called a *calling object*.

### Caution
Recall that you use `Math.methodName(arguments)` (e.g., `Math.pow(3, 2.5)`) to invoke a method in the `Math` class. Can you invoke `getArea()` using `Circle.getArea()`? The answer is no. All the methods in the `Math` class are static methods, which are defined using the `static` keyword. However, `getArea()` is an instance method, and thus nonstatic. It must be invoked from an object using `objectRefVar.methodName(arguments)` (e.g., `myCircle.getArea()`). Further explanation is given in Section 9.7, Static Variables, Constants, and Methods.

### Note
Usually you create an object and assign it to a variable, and then later you can use the variable to reference the object. Occasionally an object does not need to be referenced later. In this case, you can create an object without explicitly assigning it to a variable using the syntax:

```java
new Circle();
```

or

```java
System.out.println("Area is " + new Circle(5).getArea());
```

The former statement creates a `Circle` object. The latter creates a `Circle` object and invokes its `getArea` method to return its area. An object created in this way is known as an *anonymous object*.

### 9.5.3 Reference Data Fields and the `null` Value

The data fields can be of reference types. For example, the following `Student` class contains a data field `name` of the `String` type. `String` is a predefined Java class.

```java
class Student {
    String name; // name has the default value null
    int age; // age has the default value 0
    boolean isScienceMajor; // isScienceMajor has default value false
    char gender; // gender has default value '\u0000'
}
```

If a data field of a reference type does not reference any object, the data field holds a special Java value, `null`. `null` is a literal just like `true` and `false`. While `true` and `false` are Boolean literals, `null` is a literal for a reference type.

The default value of a data field is `null` for a reference type, `0` for a numeric type, `false` for a `boolean` type, and `\u0000` for a `char` type. However, Java assigns no default value to a local variable inside a method. The following code displays the default values of the data fields `name`, `age`, `isScienceMajor`, and `gender` for a `Student` object:

```java
class Test {
    public static void main(String[] args) {
        Student student = new Student();
        System.out.println("name? " + student.name);
        System.out.println("age? " + student.age);
        System.out.println("isScienceMajor? " + student.isScienceMajor);
        System.out.println("gender? " + student.gender);
    }
}
```
The following code has a compile error, because the local variables `x` and `y` are not initialized:

```java
class Test {
    public static void main(String[] args) {
        int x; // x has no default value
        String y; // y has no default value
        System.out.println("x is " + x);
        System.out.println("y is " + y);
    }
}
```

**Caution**

NullPointerException is a common runtime error. It occurs when you invoke a method on a reference variable with a null value. Make sure you assign an object reference to the variable before invoking the method through the reference variable (See Checkpoint Question 9.11c).

### 9.5.4 Differences between Variables of Primitive Types and Reference Types

Every variable represents a memory location that holds a value. When you declare a variable, you are telling the compiler what type of value the variable can hold. For a variable of a primitive type, the value is of the primitive type. For a variable of a reference type, the value is a reference to where an object is located. For example, as shown in Figure 9.7, the value of `int` variable `i` is `int` value 1, and the value of `Circle` object `c` holds a reference to where the contents of the `Circle` object are stored in memory.

When you assign one variable to another, the other variable is set to the same value. For a variable of a primitive type, the real value of one variable is assigned to the other variable. For a variable of a reference type, the reference of one variable is assigned to the other variable. As shown in Figure 9.8, the assignment statement `i = j` copies the contents of `j` into `i`.

**Figure 9.7** A variable of a primitive type holds a value of the primitive type, and a variable of a reference type holds a reference to where an object is stored in memory.

**Figure 9.8** Primitive variable `j` is copied to variable `i`.
for primitive variables. As shown in Figure 9.9, the assignment statement $c_1 = c_2$ copies the reference of $c_2$ into $c_1$ for reference variables. After the assignment, variables $c_1$ and $c_2$ refer to the same object.

Object type assignment $c_1 = c_2$

Before:

$\begin{array}{c}
\text{c1} \\
\text{c2}
\end{array}$

After:

$\begin{array}{c}
\text{c1: Circle} \\
\text{c2: Circle}
\end{array}$

$\begin{array}{c}
\text{radius} = 9 \\
\text{radius} = 5
\end{array}$

$\begin{array}{c}
\text{c1: Circle} \\
\text{c2: Circle}
\end{array}$

$\begin{array}{c}
\text{radius} = 5 \\
\text{radius} = 9
\end{array}$

**Figure 9.9** Reference variable $c_2$ is copied to variable $c_1$.

**Note** As illustrated in Figure 9.9, after the assignment statement $c_1 = c_2$, $c_1$ points to the same object referenced by $c_2$. The object previously referenced by $c_1$ is no longer useful and therefore is now known as garbage. Garbage occupies memory space, so the Java runtime system detects garbage and automatically reclaims the space it occupies. This process is called garbage collection.

**Tip** If you know that an object is no longer needed, you can explicitly assign `null` to a reference variable for the object. The JVM will automatically collect the space if the object is not referenced by any reference variable.

9.7 Which operator is used to access a data field or invoke a method from an object?

9.8 What is an anonymous object?

9.9 What is `NullPointerException`?

9.10 Is an array an object or a primitive type value? Can an array contain elements of an object type? Describe the default value for the elements of an array.

9.11 What is wrong with each of the following programs?

```java
(a) 1 public class ShowErrors {
    2     public static void main(String[] args) {
    3         ShowErrors t = new ShowErrors();
    4     }
    5 }

(b) 1 public class ShowErrors {
    2     public static void main(String[] args) {
    3         ShowErrors t = new ShowErrors();
    4         t.x();
    5     }
    6 }

(c) 1 public class ShowErrors {
    2     public void method1() {
    3         Circle c;
    4         System.out.println("What is radius 
    5             + c.getRadius());
    6         c = new Circle();
    7     }
    8 }

(d) 1 public class ShowErrors {
    2     public static void main(String[] args) {
    3         ShowErrors t = new ShowErrors();
    4         t.x();
    5     }
    6 }
    7 8 class C {
    9     int value = 2;
   10 }
```
9.12 What is wrong in the following code?

```java
class Test {
    public static void main(String[] args) {
        A a = new A();
        a.print();
    }
}

class A {
    String s;
    A(String newS) {
        s = newS;
    }
    public void print() {
        System.out.print(s);
    }
}
```

9.13 What is the output of the following code?

```java
public class A {
    boolean x;
    
    public static void main(String[] args) {
        A a = new A();
        System.out.println(a.x);
    }
}
```

9.6 Using Classes from the Java Library

The Java API contains a rich set of classes for developing Java programs.

Listing 9.1 defined the SimpleCircle class and created objects from the class. You will frequently use the classes in the Java library to develop programs. This section gives some examples of the classes in the Java library.

9.6.1 The Date Class

In Listing 2.7, ShowCurrentTime.java, you learned how to obtain the current time using System.currentTimeMillis(). You used the division and remainder operators to extract the current second, minute, and hour. Java provides a system-independent encapsulation of date and time in the java.util.Date class, as shown in Figure 9.10.

```java
java.util.Date
+Date()
+Date(elapseTime: long)
+toString(): String
+getTime(): long
+setTime(elapseTime: long): void
```

**Figure 9.10** A Date object represents a specific date and time.
You can use the no-arg constructor in the `Date` class to create an instance for the current date and time, the `getTime()` method to return the elapsed time since January 1, 1970, GMT, and the `toString()` method to return the date and time as a string. For example, the following code

```java
java.util.Date date = new java.util.Date();
System.out.println("The elapsed time since Jan 1, 1970 is "+
date.getTime() + " milliseconds");
System.out.println(date.toString());
```

displays the output like this:

```
The elapsed time since Jan 1, 1970 is 1324903419651 milliseconds
Mon Dec 26 07:43:39 EST 2011
```

The `Date` class has another constructor, `Date(long elapsedTime)`, which can be used to construct a `Date` object for a given time in milliseconds elapsed since January 1, 1970, GMT.

### 9.6.2 The `Random` Class

You have used `Math.random()` to obtain a random `double` value between `0.0` and `1.0` (excluding `1.0`). Another way to generate random numbers is to use the `java.util.Random` class, as shown in Figure 9.11, which can generate a random `int`, `long`, `double`, `float`, and `boolean` value.

![Figure 9.11](image)

**Figure 9.11** A `Random` object can be used to generate random values.

When you create a `Random` object, you have to specify a seed or use the default seed. A seed is a number used to initialize a random number generator. The no-arg constructor creates a `Random` object using the current elapsed time as its seed. If two `Random` objects have the same seed, they will generate identical sequences of numbers. For example, the following code creates two `Random` objects with the same seed, `3`.

```java
Random random1 = new Random(3);
System.out.print("From random1: ");
for (int i = 0; i < 10; i++)
    System.out.print(random1.nextInt(1000) + " ");

Random random2 = new Random(3);
System.out.print("\nFrom random2: ");
for (int i = 0; i < 10; i++)
    System.out.print(random2.nextInt(1000) + " ");
```
The code generates the same sequence of random int values:

From random1: 734 660 210 581 128 202 549 564 459 961
From random2: 734 660 210 581 128 202 549 564 459 961

Note
The ability to generate the same sequence of random values is useful in software testing and many other applications. In software testing, often you need to reproduce the test cases from a fixed sequence of random numbers.

9.6.3 The Point2D Class
Java API has a convenient Point2D class in the javafx.geometry package for representing a point in a two-dimensional plane. The UML diagram for the class is shown in Figure 9.12.

<table>
<thead>
<tr>
<th>javafx.geometry.Point2D</th>
</tr>
</thead>
<tbody>
<tr>
<td>+Point2D(x: double, y: double)</td>
</tr>
<tr>
<td>+distance(x: double, y: double): double</td>
</tr>
<tr>
<td>+distance(p: Point2D): double</td>
</tr>
<tr>
<td>+getX(): double</td>
</tr>
<tr>
<td>+getY(): double</td>
</tr>
<tr>
<td>+toString(): String</td>
</tr>
</tbody>
</table>

Constructs a Point2D object with the specified x- and y-coordinates.
Returns the distance between this point and the specified point (x, y).
Returns the distance between this point and the specified point p.
Returns the x-coordinate from this point.
Returns the y-coordinate from this point.
Returns a string representation for the point.

Figure 9.12 A Point2D object represents a point with x- and y-coordinates.

You can create a Point2D object for a point with the specified x- and y-coordinates, use the distance method to compute the distance from this point to another point, and use the toString() method to return a string representation of the point. Listing 9.5 gives an example of using this class.

Listing 9.5 TestPoint2D.java

```java
import java.util.Scanner;
import javafx.geometry.Point2D;

public class TestPoint2D {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);

        System.out.print("Enter point1's x-, y-coordinates: ");
        double x1 = input.nextDouble();
        double y1 = input.nextDouble();
        System.out.print("Enter point2's x-, y-coordinates: ");
        double x2 = input.nextDouble();
        double y2 = input.nextDouble();

        Point2D p1 = new Point2D(x1, y1);
        Point2D p2 = new Point2D(x2, y2);

        System.out.println("p1 is " + p1.toString());
        System.out.println("p2 is " + p2.toString());
        System.out.println("The distance between p1 and p2 is " + p1.distance(p2));
    }
}
```
This program creates two objects of the `Point2D` class (lines 15–16). The `toString()` method returns a string that describes the object (lines 17–18). Invoking `p1.distance(p2)` returns the distance between the two points (line 20).

**9.14** How do you create a `Date` for the current time? How do you display the current time?

**9.15** How do you create a `Point2D`? Suppose `p1` and `p2` are two instances of `Point2D`? How do you obtain the distance between the two points?

**9.16** Which packages contain the classes `Date`, `Random`, `Point2D`, `System`, and `Math`?

### 9.7 Static Variables, Constants, and Methods

A static variable is shared by all objects of the class. A static method cannot access instance members of the class.

The data field `radius` in the circle class is known as an *instance variable*. An instance variable is tied to a specific instance of the class; it is not shared among objects of the same class. For example, suppose that you create the following objects:

```java
circle1 = new Circle();
circle2 = new Circle(5);
```

The `radius` in `circle1` is independent of the `radius` in `circle2` and is stored in a different memory location. Changes made to `circle1`'s `radius` do not affect `circle2`'s `radius`, and vice versa.

If you want all the instances of a class to share data, use *static variables*, also known as *class variables*. Static variables store values for the variables in a common memory location. Because of this common location, if one object changes the value of a static variable, all objects of the same class are affected. Java supports static methods as well as static variables. *Static methods* can be called without creating an instance of the class.

Let's modify the `Circle` class by adding a static variable `numberOfObjects` to count the number of circle objects created. When the first object of this class is created, `numberOfObjects` is 1. When the second object is created, `numberOfObjects` becomes 2. The UML of the new circle class is shown in Figure 9.13. The `Circle` class defines the instance variable `radius` and the static variable `numberOfObjects`, the instance methods `getRadius`, `setRadius`, and `getArea`, and the static method `getNumberOfObjects`. (Note that static variables and methods are underlined in the UML class diagram.)

To declare a static variable or define a static method, put the modifier `static` in the variable or method declaration. The static variable `numberOfObjects` and the static method `getNumberOfObjects()` can be declared as follows:

```java
static int numberOfObjects;
static int getNumberOfObjects() {  
   return numberOfObjects;
}
```
Constants in a class are shared by all objects of the class. Thus, constants should be declared as `final static`. For example, the constant `PI` in the `Math` class is defined as:

```
final static double PI = 3.14159265358979323846;
```

The new circle class, named `CircleWithStaticMembers`, is defined in Listing 9.6:

```
public class CircleWithStaticMembers {
    /** The radius of the circle */
    double radius;

    /** The number of objects created */
    static int numberOfObjects = 0;

    /** Construct a circle with radius 1 */
    CircleWithStaticMembers() {
        radius = 1;
        numberOfObjects++;
    }

    /** Construct a circle with a specified radius */
    CircleWithStaticMembers(double newRadius) {
        radius = newRadius;
        numberOfObjects++;
    }

    /** Return numberOfObjects */
    static int getNumberOfObjects() {
        return numberOfObjects;
    }

    /** Return the area of this circle */
    double getArea() {
        return radius * radius * Math.PI;
    }
}
```

Method `getNumberOfObjects()` in `CircleWithStaticMembers` is a static method. All the methods in the `Math` class are static. The `main` method is static, too.
Instance methods (e.g., `getArea()` and instance data (e.g., `radius`) belong to instances and can be used only after the instances are created. They are accessed via a reference variable. Static methods (e.g., `getNumberOfObjects()` and static data (e.g., `numberOfObjects`) can be accessed from a reference variable or from their class name.

The program in Listing 9.7 demonstrates how to use instance and static variables and methods and illustrates the effects of using them.

**LISTING 9.7 TestCircleWithStaticMembers.java**

```java
public class TestCircleWithStaticMembers {
    // Main method
    public static void main(String[] args) {
        System.out.println("Before creating objects");
        System.out.println("The number of Circle objects is " + CircleWithStaticMembers.numberOfObjects);

        // Create c1
        CircleWithStaticMembers c1 = new CircleWithStaticMembers();

        // Display c1 BEFORE c2 is created
        System.out.println("After creating c1");
        System.out.println("c1: radius (" + c1.radius + ") and number of Circle objects (" + c1.numberOfObjects + ")");

        // Create c2
        CircleWithStaticMembers c2 = new CircleWithStaticMembers(5);

        // Display c1 and c2 AFTER c2 was created
        System.out.println("After creating c2 and modifying c1");
        System.out.println("c1: radius (" + c1.radius + ") and number of Circle objects (" + c1.numberOfObjects + ")");
    }
}
```

Before creating objects
The number of Circle objects is 0
After creating c1
  c1: radius (1.0) and number of Circle objects (1)
After creating c2 and modifying c1
  c1: radius (9.0) and number of Circle objects (2)
  c2: radius (5.0) and number of Circle objects (2)

When you compile `TestCircleWithStaticMembers.java`, the Java compiler automatically compiles `CircleWithStaticMembers.java` if it has not been compiled since the last change.

Static variables and methods can be accessed without creating objects. Line 6 displays the number of objects, which is 0, since no objects have been created.
The `main` method creates two circles, `c1` and `c2` (lines 9, 18). The instance variable `radius` in `c1` is modified to become 9 (line 21). This change does not affect the instance variable `radius` in `c2`, since these two instance variables are independent. The static variable `numberOfObjects` becomes 1 after `c1` is created (line 9), and it becomes 2 after `c2` is created (line 18).

Note that `PI` is a constant defined in `Math`, and `Math.PI` references the constant. `c1.numberOfObjects` (line 27) and `c2.numberOfObjects` (line 30) are better replaced by `CircleWithStaticMembers.numberOfObjects`. This improves readability, because other programmers can easily recognize the static variable. You can also replace `CircleWithStaticMembers.numberOfObjects` with `CircleWithStaticMembers.getNumberOfObjects()`.

**Tip**

Use `ClassName.methodName(arguments)` to invoke a static method and `ClassName.staticVariable` to access a static variable. This improves readability, because this makes the static method and data easy to spot.

An instance method can invoke an instance or static method and access an instance or static data field. A static method can invoke a static method and access a static data field. However, a static method cannot invoke an instance method or access an instance data field, since static methods and static data fields don’t belong to a particular object. The relationship between static and instance members is summarized in the following diagram:

For example, the following code is wrong.

```java
public class A {
    int i = 5;
    static int k = 2;

    public static void main(String[] args) {
        int j = i; // Wrong because i is an instance variable
        ml(); // Wrong because ml() is an instance method
    }

    public void ml() {
        // Correct since instance and static variables and methods
        // can be used in an instance method
        i = i + k + m2(i, k);
    }

    public static int m2(int i, int j) {
        return (int)(Math.pow(i, j));
    }
}
```
Note that if you replace the preceding code with the following new code, the program would be fine, because the instance data field \( i \) and method \( m1 \) are now accessed from an object \( a \) (lines 7–8):

```java
public class A {
    int i = 5;
    static int k = 2;

    public static void main(String[] args) {
        A a = new A();
        int j = a.i; // OK, a.i accesses the object's instance variable
        a.m1(); // OK. a.m1() invokes the object's instance method
    }
}
```

**Design Guide**
How do you decide whether a variable or a method should be an instance one or a static one? A variable or a method that is dependent on a specific instance of the class should be an instance variable or method. A variable or a method that is not dependent on a specific instance of the class should be a static variable or method. For example, every circle has its own radius, so the radius is dependent on a specific circle. Therefore, \( \text{radius} \) is an instance variable of the \( \text{Circle} \) class. Since the \( \text{getArea} \) method is dependent on a specific circle, it is an instance method. None of the methods in the \( \text{Math} \) class, such as \( \text{random}, \text{pow}, \text{sin}, \) and \( \text{cos} \), is dependent on a specific instance. Therefore, these methods are static methods. The \( \text{main} \) method is static and can be invoked directly from a class.

**Caution**
It is a common design error to define an instance method that should have been defined as static. For example, the method \( \text{factorial(int n)} \) should be defined as static, as shown next, because it is independent of any specific instance.

```java
public class Test {
    public int factorial(int n) {
        int result = 1;
        for (int i = 1; i <= n; i++)
            result *= i;

        return result;
    }
}
```

(a) Wrong design

```java
public class Test {
    public static int factorial(int n) {
        int result = 1;
        for (int i = 1; i <= n; i++)
            result *= i;

        return result;
    }
}
```

(b) Correct design

9.17 Suppose that the class \( F \) is defined in (a). Let \( f \) be an instance of \( F \). Which of the statements in (b) are correct?
9.18 Add the `static` keyword in the place of `?` if appropriate.

```java
public class Test {
    int count;

    public static void main(String[] args) {
        ...
    }

    public int getCount() {
        return count;
    }

    public int factorial(int n) {
        int result = 1;
        for (int i = 1; i <= n; i++)
            result *= i;
        return result;
    }
}
```

9.19 Can you invoke an instance method or reference an instance variable from a static method? Can you invoke a static method or reference a static variable from an instance method? What is wrong in the following code?

```java
1 public class C {
2     public static void main(String[] args) {
3         method1();
4     }
5
6     public void method1() {
7         method2();
8     }
9
10     public static void method2() {
11         System.out.println("What is radius "+ c.getRadius());
12     }
13
14     Circle c = new Circle();
15 }
```

9.8 Visibility Modifiers

Visibility modifiers can be used to specify the visibility of a class and its members.

You can use the `public` visibility modifier for classes, methods, and data fields to denote that they can be accessed from any other classes. If no visibility modifier is used, then by default the classes, methods, and data fields are accessible by any class in the same package. This is known as `package-private` or `package-access`.

```java
package-private (or package-access)
```
9.8 Visibility Modifiers

Note
Packages can be used to organize classes. To do so, you need to add the following line as the first noncomment and nonblank statement in the program:

```java
package packageName;
```

If a class is defined without the package statement, it is said to be placed in the default package.

Java recommends that you place classes into packages rather than using a default package. For simplicity, however, this book uses default packages. For more information on packages, see Supplement III.E. Packages.

In addition to the public and default visibility modifiers, Java provides the private and protected modifiers for class members. This section introduces the private modifier. The protected modifier will be introduced in Section 11.14, The protected Data and Methods.

The private modifier makes methods and data fields accessible only from within its own class. Figure 9.14 illustrates how a public, default, and private data field or method in class C1 can be accessed from a class C2 in the same package and from a class C3 in a different package.

```java
package p1;
public class C1 {
    public int x;
    int y;
    private int z;
    public void m1() {
        }
    void m2() {
        }
    private void m3() {
        }
}
package p1;
public class C2 {
    void aMethod() {
        C1 o = new C1();
        can access o.x;
        can access o.y;
        cannot access o.z;
        can invoke o.m1();
        can invoke o.m2();
        cannot invoke o.m3();
        }
}
package p2;
public class C3 {
    void aMethod() {
        C1 o = new C1();
        can access o.x;
        cannot access o.y;
        cannot access o.z;
        can invoke o.m1();
        cannot invoke o.m2();
        cannot invoke o.m3();
        }
}
```

**Figure 9.14** The private modifier restricts access to its defining class, the default modifier restricts access to a package, and the public modifier enables unrestricted access.

If a class is not defined as public, it can be accessed only within the same package. As shown in Figure 9.15, C1 can be accessed from C2 but not from C3.

```java
package p1;
class C1 {
    ...
}
package p1;
public class C2 {
    void aMethod() {
        C1 o = new C1();
        can access C1
    }
}
package p2;
public class C3 {
    void aMethod() {
        C1 o = new C1();
        cannot access C1;
        can access C2;
    }
}
```

**Figure 9.15** A nonpublic class has package-access.

A visibility modifier specifies how data fields and methods in a class can be accessed from outside the class. There is no restriction on accessing data fields and methods from inside the class. As shown in Figure 9.16b, an object c of class C cannot access its private members, because c is in the Test class. As shown in Figure 9.16a, an object c of class C can access its private members, because c is defined inside its own class.
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Caution

The `private` modifier applies only to the members of a class. The `public` modifier can apply to a class or members of a class. Using the modifiers `public` and `private` on local variables would cause a compile error.

Note

In most cases, the constructor should be public. However, if you want to prohibit the user from creating an instance of a class, use a `private constructor`. For example, there is no reason to create an instance from the `Math` class, because all of its data fields and methods are static. To prevent the user from creating objects from the `Math` class, the constructor in `java.lang.Math` is defined as follows:

```java
private Math() {
}
```

9.9 Data Field Encapsulation

Making data fields private protects data and makes the class easy to maintain.

The data fields `radius` and `numberOfObjects` in the `CircleWithStaticMembers` class in Listing 9.6 can be modified directly (e.g., `cl.radius = 5` or `CircleWithStaticMembers.numberOfObjects = 10`). This is not a good practice—for two reasons:

- First, data may be tampered with. For example, `numberOfObjects` is to count the number of objects created, but it may be mistakenly set to an arbitrary value (e.g., `CircleWithStaticMembers.numberOfObjects = 10`).

- Second, the class becomes difficult to maintain and vulnerable to bugs. Suppose you want to modify the `CircleWithStaticMembers` class to ensure that the radius is nonnegative after other programs have already used the class. You have to change not only the `CircleWithStaticMembers` class but also the programs that use it, because the clients may have modified the radius directly (e.g., `cl.radius = -5`).

To prevent direct modifications of data fields, you should declare the data fields private, using the `private` modifier. This is known as *data field encapsulation*. 
A private data field cannot be accessed by an object from outside the class that defines the private field. However, a client often needs to retrieve and modify a data field. To make a private data field accessible, provide a getter method to return its value. To enable a private data field to be updated, provide a setter method to set a new value. A getter method is also referred to as an accessor and a setter to a mutator.

A getter method has the following signature:

```java
public returnType getPropertyName()
```

If the returnType is boolean, the getter method should be defined as follows by convention:

```java
public boolean isPropertyName()
```

A setter method has the following signature:

```java
public void setPropertyName(dataType propertyValue)
```

Let’s create a new circle class with a private data-field radius and its associated accessor and mutator methods. The class diagram is shown in Figure 9.17. The new circle class, named `CircleWithPrivateDataFields`, is defined in Listing 9.8:

```java
public class CircleWithPrivateDataFields {
    /** The radius of the circle */
    private double radius = 1;

    /** The number of objects created */
    private static int numberOfObjects = 0;

    /* Construct a circle with radius 1 */
    public CircleWithPrivateDataFields() {
        numberOfObjects++;
    }

    /* Construct a circle with a specified radius */
    public CircleWithPrivateDataFields(double newRadius) {
        radius = newRadius;
        numberOfObjects++;
    }

    public double getRadius() {
        return radius;
    }

    public void setRadius(double newRadius) {
        radius = newRadius;
    }

    public int getNumberOfObjects() {
        return numberOfObjects;
    }
}
```

**Figure 9.17** The `Circle` class encapsulates circle properties and provides getter/setter and other methods.
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The `getRadius()` method (lines 20–22) returns the radius, and the `setRadius(newRadius)` method (line 25–27) sets a new radius for the object. If the new radius is negative, 0 is set as the radius for the object. Since these methods are the only ways to read and modify the radius, you have total control over how the `radius` property is accessed. If you have to change the implementation of these methods, you don’t need to change the client programs. This makes the class easy to maintain.

Listing 9.9 gives a client program that uses the `Circle` class to create a `Circle` object and modifies the radius using the `setRadius` method.

**Listing 9.9  TestCircleWithPrivateDataFields.java**

```java
public class TestCircleWithPrivateDataFields {
    /** Main method */
    public static void main(String[] args) {
        // Create a circle with radius 5.0
        CircleWithPrivateDataFields myCircle = new CircleWithPrivateDataFields(5.0);
        System.out.println("The area of the circle of radius "+ myCircle.getRadius() + " is " + myCircle.getArea());

        // Increase myCircle's radius by 10%
        myCircle.setRadius(myCircle.getRadius() * 1.1);
        System.out.println("The area of the circle of radius "+ myCircle.getRadius() + " is " + myCircle.getArea());

        // The number of objects created is "+ CircleWithPrivateDataFields.getNumberOfObjects());
    }
}
```

The data field `radius` is declared private. Private data can be accessed only within their defining class, so you cannot use `myCircle.radius` in the client program. A compile error would occur if you attempted to access private data from a client.

Since `numberOfObjects` is private, it cannot be modified. This prevents tampering. For example, the user cannot set `numberOfObjects` to 100. The only way to make it 100 is to create 100 objects of the `Circle` class.
Suppose you combined TestCircleWithPrivateDataFields and Circle into one class by moving the main method in TestCircleWithPrivateDataFields into Circle. Could you use myCircle.radius in the main method? See Checkpoint Question 9.22 for the answer.

**Design Guide**

To prevent data from being tampered with and to make the class easy to maintain, declare data fields private.

**Check Point**

9.20 What is an accessor method? What is a mutator method? What are the naming conventions for accessor methods and mutator methods?

9.21 What are the benefits of data field encapsulation?

9.22 In the following code, radius is private in the Circle class, and myCircle is an object of the Circle class. Does the highlighted code cause any problems? If so, explain why.

```java
public class Circle {
    private double radius = 1;

    /** Find the area of this circle */
    public double getArea() {
        return radius * radius * Math.PI;
    }

    public static void main(String[] args) {
        Circle myCircle = new Circle();
        System.out.println("Radius is "+ myCircle.radius);
    }
}
```

9.10 Passing Objects to Methods

*Passing an object to a method is to pass the reference of the object.*

You can pass objects to methods. Like passing an array, passing an object is actually passing the reference of the object. The following code passes the myCircle object as an argument to the printCircle method:

```java
public class Test {
    public static void main(String[] args) {
        // CircleWithPrivateDataFields is defined in Listing 9.8
        CircleWithPrivateDataFields myCircle = new CircleWithPrivateDataFields(5.0);
        printCircle(myCircle);
    }

    public static void printCircle(CircleWithPrivateDataFields c) {
        System.out.println("The area of the circle of radius "+ c.getRadius() + " is "+ c.getArea());
    }
}
```

Java uses exactly one mode of passing arguments: pass-by-value. In the preceding code, the value of myCircle is passed to the printCircle method. This value is a reference to a Circle object.

The program in Listing 9.10 demonstrates the difference between passing a primitive type value and passing a reference value.
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**Listing 9.10**  TestPassObject.java

```java
public class TestPassObject {
    /** Main method */
    public static void main(String[] args) {
        // Create a Circle object with radius 1
        CircleWithPrivateDataFields myCircle = new CircleWithPrivateDataFields(1);
        // Print areas for radius 1, 2, 3, 4, and 5.
        int n = 5;
        printAreas(myCircle, n);
        // See myCircle.radius and times
        System.out.println("Radius is " + myCircle.getRadius());
        System.out.println("n is " + n);
    }

    /** Print a table of areas for radius */
    public static void printAreas(CircleWithPrivateDataFields c, int times) {
        System.out.println("Radius \t\tArea");
        while (times >= 1) {
            System.out.println(c.getRadius() + "\t" + c.getArea());
            c.setRadius(c.getRadius() + 1);
            times--;
        }
    }
}
```

<table>
<thead>
<tr>
<th>Radius</th>
<th>Area</th>
</tr>
</thead>
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<tr>
<td>1.0</td>
<td>3.141592653589793</td>
</tr>
<tr>
<td>2.0</td>
<td>12.566370614359172</td>
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<td>3.0</td>
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</tr>
<tr>
<td>5.0</td>
<td>79.53981633974483</td>
</tr>
</tbody>
</table>

Radius is 6.0
n is 5

The CircleWithPrivateDataFields class is defined in Listing 9.8. The program passes a CircleWithPrivateDataFields object myCircle and an integer value from n to invoke printAreas(myCircle, n) (line 10), which prints a table of areas for radii 1, 2, 3, 4, 5, as shown in the sample output.

Figure 9.18 shows the call stack for executing the methods in the program. Note that the objects are stored in a heap (see Section 7.6).

When passing an argument of a primitive data type, the value of the argument is passed. In this case, the value of n (5) is passed to times. Inside the printAreas method, the content of times is changed; this does not affect the content of n.

When passing an argument of a reference type, the reference of the object is passed. In this case, c contains a reference for the object that is also referenced via myCircle. Therefore, changing the properties of the object through c inside the printAreas method has the same effect as doing so outside the method through the variable myCircle. Pass-by-value on references can be best described semantically as pass-by-sharing; that is, the object referenced in the method is the same as the object being passed.
9.23 Describe the difference between passing a parameter of a primitive type and passing a parameter of a reference type. Show the output of the following programs:

```java
public class Test {
    public static void main(String[] args) {
        Count myCount = new Count();
        int times = 0;
        for (int i = 0; i < 100; i++)
            increment(myCount, times);
        System.out.println("count is "+ myCount.count);
        System.out.println("times is "+ times);
    }
    public static void increment(Count c, int times) {
        c.count++;
        times++;
    }
}
```

```java
public class Count {
    public int count;
    public Count(int c) {
        count = c;
    }
    public Count() {
        count = 1;
    }
}
```

9.24 Show the output of the following program:

```java
public class Test {
    public static void main(String[] args) {
        Circle circle1 = new Circle(1);
        Circle circle2 = new Circle(2);
        swap1(circle1, circle2);
        System.out.println("After swap1: circle1 = " +
                           circle1.radius + ", circle2 = " + circle2.radius);
        swap2(circle1, circle2);
        System.out.println("After swap2: circle1 = " +
                           circle1.radius + ", circle2 = " + circle2.radius);
    }
    public static void swap1(Circle x, Circle y) {
        Circle temp = x;
        x = y;
        y = temp;
    }
    public static void swap2(Circle x, Circle y) {
        x.radius = y.radius;
        y.radius = x.radius;
    }
}
```
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```java
public static void swap2(Circle x, Circle y) {
    double temp = x.radius;
    x.radius = y.radius;
    y.radius = temp;
}

class Circle {
    double radius;
    Circle(double newRadius) {
        radius = newRadius;
    }
}
```

9.25 Show the output of the following code:

(a) ```java
public class Test {
    public static void main(String[] args) {
        int[] a = {1, 2};
        swap(a[0], a[1]);
        System.out.println("a[0] = " + a[0] + " a[1] = " + a[1]);
    }
    public static void swap(int n1, int n2) {
        int temp = n1;
        n1 = n2;
        n2 = temp;
    }
}
```

(b) ```java
public class Test {
    public static void main(String[] args) {
        int[] a = {1, 2};
        swap(a);
        System.out.println("a[0] = " + a[0] + " a[1] = " + a[1]);
    }
    public static void swap(int[] a) {
        int temp = a[0];
        a[0] = a[1];
        a[1] = temp;
    }
}
```

(c) ```java
public class Test {
    public static void main(String[] args) {
        T t = new T();
        swap(t);
        System.out.println("e1 = " + t.e1 + " e2 = " + t.e2);
    }
    public static void swap(T t) {
        int temp = t.e1;
        t.e1 = t.e2;
        t.e2 = temp;
    }
}
class T {
    int e1 = 1;
    int e2 = 2;
}
```

(d) ```java
public class Test {
    public static void main(String[] args) {
        T t1 = new T();
        T t2 = new T();
        System.out.println("t1's i = " + t1.i + " and j = " + t1.j);
        System.out.println("t2's i = " + t2.i + " and j = " + t2.j);
    }
}
class T {
    static int i = 0;
    int j = 0;
    T() {
        i++;
        j = 1;
    }
}
```
9.11 Array of Objects

An array can hold objects as well as primitive type values.

Chapter 7, Single-Dimensional Arrays, described how to create arrays of primitive type elements. You can also create arrays of objects. For example, the following statement declares and creates an array of ten Circle objects:

```java
Circle[] circleArray = new Circle[10];
```

To initialize `circleArray`, you can use a `for` loop like this one:

```java
for (int i = 0; i < circleArray.length; i++) {
    circleArray[i] = new Circle();
}
```

An array of objects is actually an *array of reference variables*. So, invoking `circleArray[1].getArea()` involves two levels of referencing, as shown in Figure 9.19. `circleArray` references the entire array; `circleArray[1]` references a Circle object.

**Note**

When an array of objects is created using the `new` operator, each element in the array is a reference variable with a default value of `null`.
Listing 9.11 gives an example that demonstrates how to use an array of objects. The program summarizes the areas of an array of circles. The program creates `circleArray`, an array composed of five `Circle` objects; it then initializes circle radii with random values and displays the total area of the circles in the array.

Listing 9.11  TotalArea.java

```java
public class TotalArea {
    /** Main method */
    public static void main(String[] args) {
        // Declare circleArray
        CircleWithPrivateDataFields[] circleArray;

        // Create circleArray
        circleArray = createCircleArray();

        // Print circleArray and total areas of the circles
        printCircleArray(circleArray);
    }

    /** Create an array of Circle objects */
    public static CircleWithPrivateDataFields[] createCircleArray() {
        CircleWithPrivateDataFields[] circleArray = new CircleWithPrivateDataFields[5];

        for (int i = 0; i < circleArray.length; i++) {
            circleArray[i] = new CircleWithPrivateDataFields(Math.random() * 100);
        }

        // Return Circle array
        return circleArray;
    }

    /** Print an array of circles and their total area */
    public static void printCircleArray(CircleWithPrivateDataFields[] circleArray) {
        System.out.printf("%-30s%-15s
", "Radius", "Area");
        for (int i = 0; i < circleArray.length; i++) {
            System.out.printf("%-30f%-15f
", circleArray[i].getRadius(), circleArray[i].getArea());
        }
        System.out.println("------------------------------------------");
        System.out.printf("%-30s%-15f\n", "The total area of circles is", sum(circleArray));
    }
}
```

Figure 9.19  In an array of objects, an element of the array contains a reference to an object.
/* Add circle areas */
public static double sum(CircleWithPrivateDataFields[] circleArray) {
    // Initialize sum
    double sum = 0;
    // Add areas to sum
    for (int i = 0; i < circleArray.length; i++)
        sum += circleArray[i].getArea();
    return sum;
}

Radius                      Area
70.577708                   15649.941866
44.152266                   6124.291736
24.867853                   1942.792644
5.680718                    101.380949
36.734246                   4239.280350
---------------------------------------------------------------------
The total area of circles is 28056.687544

The program invokes createCircleArray() (line 8) to create an array of five circle objects. Several circle classes were introduced in this chapter. This example uses the CircleWithPrivateDataFields class introduced in Section 9.9, Data Field Encapsulation.

The circle radii are randomly generated using the Math.random() method (line 21). The createCircleArray method returns an array of CircleWithPrivateDataFields objects (line 25). The array is passed to the printCircleArray method, which displays the radius and area of each circle and the total area of the circles.

The sum of the circle areas is computed by invoking the sum method (line 41), which takes the array of CircleWithPrivateDataFields objects as the argument and returns a double value for the total area.

What is wrong in the following code?

```java
public class Test {
    public static void main(String[] args) {
        java.util.Date[] dates = new java.util.Date[10];
        System.out.println(dates[0].toString());
    }
}
```

You can define immutable classes to create immutable objects. The contents of immutable objects cannot be changed.

Normally, you create an object and allow its contents to be changed later. However, occasionally it is desirable to create an object whose contents cannot be changed once the object has been created. We call such an object an immutable object and its class as an immutable class. The String class, for example, is immutable. If you deleted the setter method in the CircleWithPrivateDataFields class in Listing 9.9, the class would be immutable, because radius is private and cannot be changed without a setter method.
If a class is immutable, then all its data fields must be private and it cannot contain public setter methods for any data fields. A class with all private data fields and no mutators is not necessarily immutable. For example, the following `Student` class has all private data fields and no setter methods, but it is not an immutable class.

```java
public class Student {
    private int id;
    private String name;
    private java.util.Date dateCreated;

    public Student(int ssn, String newName) {
        id = ssn;
        name = newName;
        dateCreated = new java.util.Date();
    }

    public int getId() {
        return id;
    }

    public String getName() {
        return name;
    }

    public java.util.Date getDateCreated() {
        return dateCreated;
    }
}
```

As shown in the following code, the data field `dateCreated` is returned using the `getDateCreated()` method. This is a reference to a `Date` object. Through this reference, the content for `dateCreated` can be changed.

```java
public class Test {
    public static void main(String[] args) {
        Student student = new Student(111223333, "John");
        java.util.Date dateCreated = student.getDateCreated();
        dateCreated.setTime(200000); // Now dateCreated field is changed!
    }
}
```

For a class to be immutable, it must meet the following requirements:

- All data fields must be private.
- There can’t be any mutator methods for data fields.
- No accessor methods can return a reference to a data field that is mutable.

Interested readers may refer to Supplement III.U for an extended discussion on immutable objects.

**Check Point**

9.28 If a class contains only private data fields and no setter methods, is the class immutable?

9.29 If all the data fields in a class are private and of primitive types, and the class doesn’t contain any setter methods, is the class immutable?

9.30 Is the following class immutable?

```java
public class A {
    private int[] values;

    public int[] getValues() {
```
9.13 The Scope of Variables

The scope of instance and static variables is the entire class, regardless of where the variables are declared.

Section 6.9 discussed local variables and their scope rules. Local variables are declared and used inside a method locally. This section discusses the scope rules of all the variables in the context of a class.

Instance and static variables in a class are referred to as the class’s variables or data fields. A variable defined inside a method is referred to as a local variable. The scope of a class’s variables is the entire class, regardless of where the variables are declared. A class’s variables and methods can appear in any order in the class, as shown in Figure 9.20a. The exception is when a data field is initialized based on a reference to another data field. In such cases, the other data field must be declared first, as shown in Figure 9.20b. For consistency, this book declares data fields at the beginning of the class.

### Key Point

- **class’s variables**

You can declare a class’s variable only once, but you can declare the same variable name in a method many times in different nonnesting blocks.

If a local variable has the same name as a class’s variable, the local variable takes precedence and the class’s variable with the same name is hidden. For example, in the following program, \( x \) is defined both as an instance variable and as a local variable in the method.

```
public class F {
    private int x = 0; // Instance variable
    private int y = 0;

    public F() {
    }

    public void p() {
        int x = 1; // Local variable
        System.out.println("x = " + x);
        System.out.println("y = " + y);
    }
}
```

What is the output for \( f.p() \), where \( f \) is an instance of \( F \)? The output for \( f.p() \) is \( 1 \) for \( x \) and \( 0 \) for \( y \). Here is why:

- \( x \) is declared as a data field with the initial value of \( 0 \) in the class, but it is also declared in the method \( p() \) with an initial value of \( 1 \). The latter \( x \) is referenced in the `System.out.println` statement.

- \( y \) is declared outside the method \( p() \), but \( y \) is accessible inside the method.
9.31 What is the output of the following program?

```java
public class Test {
    private static int i = 0;
    private static int j = 0;

    public static void main(String[] args) {
        int i = 2;
        int k = 3;

        int j = 3;
        System.out.println("i + j is "+ i + j);
    }

    k = i + j;
    System.out.println("k is "+ k);
    System.out.println("j is "+ j);
}
```

9.14 The this Reference

The keyword `this` refers to the object itself. It can also be used inside a constructor to invoke another constructor of the same class.

The `this` keyword is the name of a reference that an object can use to refer to itself. You can use the `this` keyword to reference the object’s instance members. For example, the following code in (a) uses `this` to reference the object’s `radius` and invokes its `getArea()` method explicitly. The `this` reference is normally omitted, as shown in (b). However, the `this` reference is needed to reference hidden data fields or invoke an overloaded constructor.

```java
public class Circle {
    private double radius;

    public double getArea() {
        return this.radius * this.radius * Math.PI;
    }

    public String toString() {
        return "radius: "+ this.radius + "area: "+ this.getArea() ;
    }
}
```

Equivalence:

```java
public class Circle {
    private double radius;

    public double getArea() {
        return radius * radius * Math.PI;
    }

    public String toString() {
        return "radius: " + radius + "area: " + getArea() ;
    }
}
```

9.14.1 Using this to Reference Hidden Data Fields

The `this` keyword can be used to reference a class’s hidden data fields. For example, a data-field name is often used as the parameter name in a setter method for the data field. In this case, the data field is hidden in the setter method. You need to reference the hidden data-field name in the method in order to set a new value to it. A hidden static variable can be accessed...
simply by using the ClassName.staticVariable reference. A hidden instance variable can be accessed by using the keyword this, as shown in Figure 9.21a.

```
public class F {
    private int i = 5;
    private static double k = 0;
    public void setI(int i) {
        this.i = i;
    }
    public static void setK(double k) {
        F.k = k;
    }
    // Other methods omitted
}
```

Suppose that f1 and f2 are two objects of F. Invoking f1.setI(10) is to execute this.i = 10, where this refers f1 Invoking f2.setI(45) is to execute this.i = 45, where this refers f2 Invoking F.setK(33) is to execute F.k = 33. setK is a static method

![Figure 9.21](image)

The keyword **this** refers to the calling object that invokes the method.

The **this** keyword gives us a way to reference the object that invokes an instance method. To invoke `f1.setI(10)`, `this.i = i` is executed, which assigns the value of parameter `i` to the data field `i` of this calling object `f1`. The keyword **this** refers to the object that invokes the instance method `setI`, as shown in Figure 9.21b. The line `F.k = k` means that the value in parameter `k` is assigned to the static data field `k` of the class, which is shared by all the objects of the class.

### 9.14.2 Using **this** to Invoke a Constructor

The **this** keyword can be used to invoke another constructor of the same class. For example, you can rewrite the **Circle** class as follows:

```
public class Circle {
    private double radius;
    public Circle(double radius) {
        this.radius = radius;
    }
    // Other methods omitted
}
```

The line `this(1.0)` in the second constructor invokes the first constructor with a `double` value argument.

**Note**

Java requires that the **this**(arg-list) statement appear first in the constructor before any other executable statements.

**Tip**

If a class has multiple constructors, it is better to implement them using **this**(arg-list) as much as possible. In general, a constructor with no or fewer arguments can invoke a constructor with more arguments using **this**(arg-list). This syntax often simplifies coding and makes the class easier to read and to maintain.
9.32 Describe the role of the `this` keyword.

9.33 What is wrong in the following code?

```java
class C {
    private int p;

    public C() {
        System.out.println("C's no-arg constructor invoked");
        this(0);
    }

    public C(int p) {
        p = p;
    }

    public void setP(int p) {
        p = p;
    }
}
```

9.34 What is wrong in the following code?

```java
class Test {
    private int id;

    public void m1() {
        this.id = 45;
    }

    public void m2() {
        Test.id = 45;
    }
}
```

**Key Terms**

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Chapter Summary

1. A class is a template for objects. It defines the properties of objects and provides constructors for creating objects and methods for manipulating them.

2. A class is also a data type. You can use it to declare object reference variables. An object reference variable that appears to hold an object actually contains a reference to that object. Strictly speaking, an object reference variable and an object are different, but most of the time the distinction can be ignored.

3. An object is an instance of a class. You use the new operator to create an object, and the dot operator (.) to access members of that object through its reference variable.

4. An instance variable or method belongs to an instance of a class. Its use is associated with individual instances. A static variable is a variable shared by all instances of the same class. A static method is a method that can be invoked without using instances.

5. Every instance of a class can access the class’s static variables and methods. For clarity, however, it is better to invoke static variables and methods using ClassName.variable and ClassName.method.

6. Visibility modifiers specify how the class, method, and data are accessed. A public class, method, or data is accessible to all clients. A private method or data is accessible only inside the class.

7. You can provide a getter (accessor) method or a setter (mutator) method to enable clients to see or modify the data.

8. A getter method has the signature public returnType getPropertyName(). If the returnType is boolean, the get method should be defined as public boolean isPropertyName(). A setter method has the signature public void setPropertyName(dataType propertyValue).

9. All parameters are passed to methods using pass-by-value. For a parameter of a primitive type, the actual value is passed; for a parameter of a reference type, the reference for the object is passed.

10. A Java array is an object that can contain primitive type values or object type values. When an array of objects is created, its elements are assigned the default value of null.

11. Once it is created, an immutable object cannot be modified. To prevent users from modifying an object, you can define immutable classes.

12. The scope of instance and static variables is the entire class, regardless of where the variables are declared. Instance and static variables can be declared anywhere in the class. For consistency, they are declared at the beginning of the class in this book.

13. The keyword this can be used to refer to the calling object. It can also be used inside a constructor to invoke another constructor of the same class.

Quiz

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.
Pedagogical Note
The exercises in Chapters 9–13 help you achieve three objectives:
■ Design classes and draw UML class diagrams.
■ Implement classes from the UML.
■ Use classes to develop applications.

Students can download solutions for the UML diagrams for the even-numbered exercises from the Companion Website, and instructors can download all solutions from the same site.

Sections 9.2–9.5

9.1 (The Rectangle class) Following the example of the Circle class in Section 9.2, design a class named Rectangle to represent a rectangle. The class contains:
■ Two double data fields named width and height that specify the width and height of the rectangle. The default values are 1 for both width and height.
■ A no-arg constructor that creates a default rectangle.
■ A constructor that creates a rectangle with the specified width and height.
■ A method named getArea() that returns the area of this rectangle.
■ A method named getPerimeter() that returns the perimeter.

Draw the UML diagram for the class and then implement the class. Write a test program that creates two Rectangle objects—one with width 4 and height 40 and the other with width 3.5 and height 35.9. Display the width, height, area, and perimeter of each rectangle in this order.

9.2 (The Stock class) Following the example of the Circle class in Section 9.2, design a class named Stock that contains:
■ A string data field named symbol for the stock’s symbol.
■ A string data field named name for the stock’s name.
■ A double data field named previousClosingPrice that stores the stock price for the previous day.
■ A double data field named currentPrice that stores the stock price for the current time.
■ A constructor that creates a stock with the specified symbol and name.
■ A method named getChangePercent() that returns the percentage changed from previousClosingPrice to currentPrice.

Draw the UML diagram for the class and then implement the class. Write a test program that creates a Stock object with the stock symbol ORCL, the name Oracle Corporation, and the previous closing price of 34.5. Set a new current price to 34.35 and display the price-change percentage.

Section 9.6

*9.3 (Use the Date class) Write a program that creates a Date object, sets its elapsed time to 10000, 100000, 1000000, 10000000, 100000000, 1000000000, and 10000000000, and displays the date and time using the toString() method, respectively.

*9.4 (Use the Random class) Write a program that creates a Random object with seed 1000 and displays the first 50 random integers between 0 and 100 using the nextInt(100) method.
*9.5 (Use the GregorianCalendar class) Java API has the GregorianCalendar class in the java.util package, which you can use to obtain the year, month, and day of a date. The no-arg constructor constructs an instance for the current date, and the methods get(GregorianCalendar.YEAR), get(GregorianCalendar.MONTH), and get(GregorianCalendar.DAY_OF_MONTH) return the year, month, and day. Write a program to perform two tasks:

- Display the current year, month, and day.
- The GregorianCalendar class has the setTimeInMillis(long), which can be used to set a specified elapsed time since January 1, 1970. Set the value to 1234567898765L and display the year, month, and day.

Sections 9.7–9.9

*9.6 (Stopwatch) Design a class named StopWatch. The class contains:

- Private data fields startTime and endTime with getter methods.
- A no-arg constructor that initializes startTime with the current time.
- A method named start() that resets the startTime to the current time.
- A method named stop() that sets the endTime to the current time.
- A method named getElapsedTime() that returns the elapsed time for the stopwatch in milliseconds.

Draw the UML diagram for the class and then implement the class. Write a test program that measures the execution time of sorting 100,000 numbers using selection sort.

9.7 (The Account class) Design a class named Account that contains:

- A private int data field named id for the account (default 0).
- A private double data field named balance for the account (default 0).
- A private double data field named annualInterestRate that stores the current interest rate (default 0). Assume all accounts have the same interest rate.
- A private Date data field named dateCreated that stores the date when the account was created.
- A no-arg constructor that creates a default account.
- A constructor that creates an account with the specified id and initial balance.
- The accessor and mutator methods for id, balance, and annualInterestRate.
- The accessor method for dateCreated.
- A method named getMonthlyInterestRate() that returns the monthly interest rate.
- A method named getMonthlyInterest() that returns the monthly interest.
- A method named withdraw that withdraws a specified amount from the account.
- A method named deposit that deposits a specified amount to the account.

Draw the UML diagram for the class and then implement the class. (Hint: The method getMonthlyInterest() is to return monthly interest, not the interest rate. Monthly interest is balance * monthlyInterestRate. monthlyInterestRate is annualInterestRate / 12. Note that annualInterestRate is a percentage, e.g., like 4.5%. You need to divide it by 100.)

Write a test program that creates an Account object with an account ID of 1122, a balance of $20,000, and an annual interest rate of 4.5%. Use the withdraw method to withdraw $2,500, use the deposit method to deposit $3,000, and print the balance, the monthly interest, and the date when this account was created.
9.8 \textit{(The Fan class)} Design a class named \texttt{Fan} to represent a fan. The class contains:

- Three constants named \texttt{SLOW}, \texttt{MEDIUM}, and \texttt{FAST} with the values 1, 2, and 3 to denote the fan speed.
- A private \texttt{int} data field named \texttt{speed} that specifies the speed of the fan (the default is \texttt{SLOW}).
- A private \texttt{boolean} data field named \texttt{on} that specifies whether the fan is on (the default is \texttt{false}).
- A private \texttt{double} data field named \texttt{radius} that specifies the radius of the fan (the default is 5).
- A string data field named \texttt{color} that specifies the color of the fan (the default is \texttt{blue}).
- The accessor and mutator methods for all four data fields.
- A no-arg constructor that creates a default fan.
- A method named \texttt{toString()} that returns a string description for the fan. If the fan is on, the method returns the fan speed, color, and radius in one combined string. If the fan is not on, the method returns the fan color and radius along with the string “fan is off” in one combined string.

Draw the UML diagram for the class and then implement the class. Write a test program that creates two \texttt{Fan} objects. Assign maximum speed, radius 10, color \texttt{yellow}, and turn it on to the first object. Assign medium speed, radius 5, color \texttt{blue}, and turn it off to the second object. Display the objects by invoking their \texttt{toString} method.

**9.9 \textit{(Geometry: n-sided regular polygon)} In an \textit{n}-sided regular polygon, all sides have the same length and all angles have the same degree (i.e., the polygon is both equilateral and equiangular). Design a class named \texttt{RegularPolygon} that contains:

- A private \texttt{int} data field named \texttt{n} that defines the number of sides in the polygon with default value 3.
- A private \texttt{double} data field named \texttt{side} that stores the length of the side with default value 1.
- A private \texttt{double} data field named \texttt{x} that defines the \texttt{x}-coordinate of the polygon’s center with default value 0.
- A private \texttt{double} data field named \texttt{y} that defines the \texttt{y}-coordinate of the polygon’s center with default value 0.
- A no-arg constructor that creates a regular polygon with default values.
- A constructor that creates a regular polygon with the specified number of sides and length of side, centered at \texttt{(0, 0)}.
- A constructor that creates a regular polygon with the specified number of sides, length of side, and \texttt{x}- and \texttt{y}-coordinates.
- The accessor and mutator methods for all data fields.
- The method \texttt{getPerimeter()} that returns the perimeter of the polygon.
- The method \texttt{getArea()} that returns the area of the polygon. The formula for computing the area of a regular polygon is \( \text{Area} = \frac{n \times s^2}{4 \times \tan\left(\frac{\pi}{n}\right)} \).

Draw the UML diagram for the class and then implement the class. Write a test program that creates three \texttt{RegularPolygon} objects, created using the no-arg constructor, using \texttt{RegularPolygon(6, 4)}, and using \texttt{RegularPolygon(10, 4, 5.6, 7.8)}. For each object, display its perimeter and area.
**9.10 (Algebra: quadratic equations)** Design a class named `QuadraticEquation` for a quadratic equation $ax^2 + bx + c = 0$. The class contains:

- Private data fields `a`, `b`, and `c` that represent three coefficients.
- A constructor for the arguments for `a`, `b`, and `c`.
- Three getter methods for `a`, `b`, and `c`.
- A method named `getDiscriminant()` that returns the discriminant, which is $b^2 - 4ac$.
- The methods named `getRoot1()` and `getRoot2()` for returning two roots of the equation

\[
\begin{align*}
    r_1 &= \frac{-b + \sqrt{b^2 - 4ac}}{2a} \\
    r_2 &= \frac{-b - \sqrt{b^2 - 4ac}}{2a}
\end{align*}
\]

These methods are useful only if the discriminant is nonnegative. Let these methods return 0 if the discriminant is negative.

Draw the UML diagram for the class and then implement the class. Write a test program that prompts the user to enter values for `a`, `b`, and `c` and displays the result based on the discriminant. If the discriminant is positive, display the two roots. If the discriminant is 0, display the one root. Otherwise, display “The equation has no roots.” See Programming Exercise 3.1 for sample runs.

**9.11 (Algebra: 2 × 2 linear equations)** Design a class named `LinearEquation` for a 2 × 2 system of linear equations:

\[
\begin{align*}
    ax + by &= e \\
    cx + dy &= f
\end{align*}
\]

The class contains:

- Private data fields `a`, `b`, `c`, `d`, `e`, and `f`.
- A constructor with the arguments for `a`, `b`, `c`, `d`, `e`, and `f`.
- Six getter methods for `a`, `b`, `c`, `d`, `e`, and `f`.
- A method named `isSolvable()` that returns true if $ad - bc$ is not 0.
- Methods `getX()` and `getY()` that return the solution for the equation.

Draw the UML diagram for the class and then implement the class. Write a test program that prompts the user to enter `a`, `b`, `c`, `d`, `e`, and `f` and displays the result. If $ad - bc$ is 0, report that “The equation has no solution.” See Programming Exercise 3.3 for sample runs.

**9.12 (Geometry: intersecting point)** Suppose two line segments intersect. The two endpoints for the first line segment are $(x_1, y_1)$ and $(x_2, y_2)$ and for the second line segment are $(x_3, y_3)$ and $(x_4, y_4)$. Write a program that prompts the user to enter these four endpoints and displays the intersecting point. As discussed in Programming Exercise 3.25, the intersecting point can be found by solving a linear equation. Use the `LinearEquation` class in Programming Exercise 9.11 to solve this equation. See Programming Exercise 3.25 for sample runs.

**9.13 (The Location class)** Design a class named `Location` for locating a maximal value and its location in a two-dimensional array. The class contains public data fields `row`, `column`, and `maxValue` that store the maximal value and its indices in a two-dimensional array with `row` and `column` as `int` types and `maxValue` as a `double` type.

Write the following method that returns the location of the largest element in a two-dimensional array:

```java
public static Location locateLargest(double[][] a)
```
The return value is an instance of `Location`. Write a test program that prompts the user to enter a two-dimensional array and displays the location of the largest element in the array. Here is a sample run:

Enter the number of rows and columns in the array: 3 4
Enter the array:
23.5 35 2 10
4.5 3 45 3.5
35 44 5.5 9.6
The location of the largest element is 45 at (1, 2)
OBJECT-ORIENTED THINKING

Objectives

■ To apply class abstraction to develop software (§10.2).
■ To explore the differences between the procedural paradigm and object-oriented paradigm (§10.3).
■ To discover the relationships between classes (§10.4).
■ To design programs using the object-oriented paradigm (§§10.5–10.6).
■ To create objects for primitive values using the wrapper classes (Byte, Short, Integer, Long, Float, Double, Character, and Boolean) (§10.7).
■ To simplify programming using automatic conversion between primitive types and wrapper class types (§10.8).
■ To use the BigInteger and BigDecimal classes for computing very large numbers with arbitrary precisions (§10.9).
■ To use the String class to process immutable strings (§10.10).
■ To use the StringBuilder and StringBuffer classes to process mutable strings (§10.11).
10.1 Introduction

The focus of this chapter is on class design and explores the differences between procedural programming and object-oriented programming.

The preceding chapter introduced objects and classes. You learned how to define classes, create objects, and use objects from several classes in the Java API (e.g., Circle, Date, Random, and Point2D). This book’s approach is to teach problem solving and fundamental programming techniques before object-oriented programming. This chapter shows how procedural and object-oriented programming differ. You will see the benefits of object-oriented programming and learn to use it effectively.

Our focus here is on class design. We will use several examples to illustrate the advantages of the object-oriented approach. The examples involve designing new classes and using them in applications and introducing new classes in the Java API.

10.2 Class Abstraction and Encapsulation

Class abstraction is the separation of class implementation from the use of a class. The details of implementation are encapsulated and hidden from the user. This is known as class encapsulation.

In Chapter 6, you learned about method abstraction and used it in stepwise refinement. Java provides many levels of abstraction, and class abstraction separates class implementation from how the class is used. The creator of a class describes the functions of the class and lets the user know how the class can be used. The collection of methods and fields that are accessible from outside the class, together with the description of how these members are expected to behave, serves as the class’s contract. As shown in Figure 10.1, the user of the class does not need to know how the class is implemented. The details of implementation are encapsulated and hidden from the user. This is called class encapsulation. For example, you can create a Circle object and find the area of the circle without knowing how the area is computed. For this reason, a class is also known as an abstract data type (ADT).

Class abstraction and encapsulation are two sides of the same coin. Many real-life examples illustrate the concept of class abstraction. Consider, for instance, building a computer system. Your personal computer has many components—a CPU, memory, disk, motherboard, fan, and so on. Each component can be viewed as an object that has properties and methods. To get the components to work together, you need know only how each component is used and how it interacts with the others. You don’t need to know how the components work internally. The internal implementation is encapsulated and hidden from you. You can build a computer without knowing how a component is implemented.

The computer-system analogy precisely mirrors the object-oriented approach. Each component can be viewed as an object of the class for the component. For example, you might have a class that models all kinds of fans for use in a computer, with properties such as fan size and speed and methods such as start and stop. A specific fan is an instance of this class with specific property values.

As another example, consider getting a loan. A specific loan can be viewed as an object of a Loan class. The interest rate, loan amount, and loan period are its data properties, and
computing the monthly payment and total payment are its methods. When you buy a car, a loan object is created by instantiating the class with your loan interest rate, loan amount, and loan period. You can then use the methods to find the monthly payment and total payment of your loan. As a user of the Loan class, you don’t need to know how these methods are implemented.

Listing 2.9, ComputeLoan.java, presented a program for computing loan payments. That program cannot be reused in other programs because the code for computing the payments is in the main method. One way to fix this problem is to define static methods for computing the monthly payment and total payment. However, this solution has limitations. Suppose you wish to associate a date with the loan. There is no good way to tie a date with a loan without using objects. The traditional procedural programming paradigm is action-driven, and data are separated from actions. The object-oriented programming paradigm focuses on objects, and actions are defined along with the data in objects. To tie a date with a loan, you can define a loan class with a date along with the loan’s other properties as data fields. A loan object now contains data and actions for manipulating and processing data, and the loan data and actions are integrated in one object. Figure 10.2 shows the UML class diagram for the Loan class.

<table>
<thead>
<tr>
<th>Loan</th>
<th>The annual interest rate of the loan (default: 2.5).</th>
</tr>
</thead>
<tbody>
<tr>
<td>-annualInterestRate: double</td>
<td>The number of years for the loan (default: 1).</td>
</tr>
<tr>
<td>-numberOfYears: int</td>
<td>The loan amount (default: 1000).</td>
</tr>
<tr>
<td>-loanAmount: double</td>
<td>The date this loan was created.</td>
</tr>
<tr>
<td>-loanDate: java.util.Date</td>
<td>Constructs a default Loan object.</td>
</tr>
<tr>
<td>+Loan()</td>
<td>Constructs a loan with specified interest rate, years, and loan amount.</td>
</tr>
<tr>
<td>+Loan(annualInterestRate: double, numberOfYears: int, loanAmount: double)</td>
<td>Returns the annual interest rate of this loan.</td>
</tr>
<tr>
<td>+getAnnualInterestRate(): double</td>
<td>Returns the number of the years of this loan.</td>
</tr>
<tr>
<td>+getNumberOfYears(): int</td>
<td>Returns the amount of this loan.</td>
</tr>
<tr>
<td>+getLoanAmount(): double</td>
<td>Returns the date of the creation of this loan.</td>
</tr>
<tr>
<td>+getLoanDate(): java.util.Date</td>
<td>Sets a new annual interest rate for this loan.</td>
</tr>
<tr>
<td>+setAnnualInterestRate(annualInterestRate: double): void</td>
<td>Sets a new number of years for this loan.</td>
</tr>
<tr>
<td>+setNumberOfYears(numberOfYears: int): void</td>
<td>Returns the monthly payment for this loan.</td>
</tr>
<tr>
<td>+setLoanAmount(loanAmount: double): void</td>
<td>Returns the total payment for this loan.</td>
</tr>
<tr>
<td>+getMonthlyPayment(): double</td>
<td></td>
</tr>
<tr>
<td>+getTotalPayment(): double</td>
<td></td>
</tr>
</tbody>
</table>

**Figure 10.2** The Loan class models the properties and behaviors of loans.

The UML diagram in Figure 10.2 serves as the contract for the Loan class. Throughout this book, you will play the roles of both class user and class developer. Remember that a class user can use the class without knowing how the class is implemented.

Assume that the Loan class is available. The program in Listing 10.1 uses that class.

**Listing 10.1 TestLoanClass.java**

```java
import java.util.Scanner;

public class TestLoanClass {
    /** Main method */
    public static void main(String[] args) {
```
The `main` method reads the interest rate, the payment period (in years), and the loan amount; creates a `Loan` object; and then obtains the monthly payment (line 29) and the total payment (line 30) using the instance methods in the `Loan` class.

The `Loan` class can be implemented as in Listing 10.2.

### Listing 10.2  Loan.java

```java
public class Loan {
    private double annualInterestRate;
    private int numberOfYears;
    private double loanAmount;
    private java.util.Date loanDate;

    /** Default constructor */
    public Loan() {
        this(2.5, 1, 1000);
    }

    /** Construct a loan with specified annual interest rate,
```
13 */
14 public Loan(double annualInterestRate, int numberOfYears,
15 double loanAmount) {
16  this.annualInterestRate = annualInterestRate;
17  this.numberOfYears = numberOfYears;
18  this.loanAmount = loanAmount;
19  loanDate = new java.util.Date();
20 }
21
22 /** Return annualInterestRate */
23 public double getAnnualInterestRate() {
24  return annualInterestRate;
25 }
26
27 /** Set a new annualInterestRate */
28 public void setAnnualInterestRate(double annualInterestRate) {
29  this.annualInterestRate = annualInterestRate;
30 }
31
32 /** Return numberOfYears */
33 public int getNumberOfYears() {
34  return numberOfYears;
35 }
36
37 /** Set a new numberOfYears */
38 public void setNumberOfYears(int numberOfYears) {
39  this.numberOfYears = numberOfYears;
40 }
41
42 /** Return loanAmount */
43 public double getLoanAmount() {
44  return loanAmount;
45 }
46
47 /** Set a new loanAmount */
48 public void setLoanAmount(double loanAmount) {
49  this.loanAmount = loanAmount;
50 }
51
52 /** Find monthly payment */
53 public double getMonthlyPayment() {
54  double monthlyInterestRate = annualInterestRate / 1200;
55  double monthlyPayment = loanAmount \* monthlyInterestRate / (1 -
56  (1 / Math.pow(1 + monthlyInterestRate, numberOfYears \* 12)));
57  return monthlyPayment;
58 }
59
60 /** Find total payment */
61 public double getTotalPayment() {
62  double totalPayment = getMonthlyPayment() \* numberOfYears \* 12;
63  return totalPayment;
64 }
65
66 /** Return loan date */
67 public java.util.Date getLoanDate() {
68  return loanDate;
69 }
70 }
From a class developer’s perspective, a class is designed for use by many different customers. In order to be useful in a wide range of applications, a class should provide a variety of ways for customization through constructors, properties, and methods.

The Loan class contains two constructors, four getter methods, three setter methods, and the methods for finding the monthly payment and the total payment. You can construct a Loan object by using the no-arg constructor or the constructor with three parameters: annual interest rate, number of years, and loan amount. When a loan object is created, its date is stored in the loanDate field. The getLoanDate method returns the date. The methods—getAnnualInterest, getNumberOfYears, and getLoanAmount—return the annual interest rate, payment years, and loan amount, respectively. All the data properties and methods in this class are tied to a specific instance of the Loan class. Therefore, they are instance variables and methods.

**Important Pedagogical Tip**
Use the UML diagram for the Loan class shown in Figure 10.2 to write a test program that uses the Loan class even though you don’t know how the Loan class is implemented. This has three benefits:

- It demonstrates that developing a class and using a class are two separate tasks.
- It enables you to skip the complex implementation of certain classes without interrupting the sequence of this book.
- It is easier to learn how to implement a class if you are familiar with it by using the class.

For all the class examples from now on, create an object from the class and try using its methods before turning your attention to its implementation.

**10.1 Check Point**

If you redefine the Loan class in Listing 10.2 without setter methods, is the class immutable?

**10.3 Thinking in Objects**

The procedural paradigm focuses on designing methods. The object-oriented paradigm couples data and methods together into objects. Software design using the object-oriented paradigm focuses on objects and operations on objects.

Chapters 1–8 introduced fundamental programming techniques for problem solving using loops, methods, and arrays. Knowing these techniques lays a solid foundation for object-oriented programming. Classes provide more flexibility and modularity for building reusable software. This section improves the solution for a problem introduced in Chapter 3 using the object-oriented approach. From these improvements, you will gain insight into the differences between procedural and object-oriented programming and see the benefits of developing reusable code using objects and classes.

Listing 3.4, ComputeAndInterpretBMI.java, presented a program for computing body mass index. The code cannot be reused in other programs, because the code is in the main method. To make it reusable, define a static method to compute body mass index as follows:

```
public static double getBMI(double weight, double height)
```

This method is useful for computing body mass index for a specified weight and height. However, it has limitations. Suppose you need to associate the weight and height with a person’s name and birth date. You could declare separate variables to store these values, but these values would not be tightly coupled. The ideal way to couple them is to create an object that contains them all. Since these values are tied to individual objects, they should be stored in instance data fields. You can define a class named BMI as shown in Figure 10.3.
Assume that the `BMI` class is available. Listing 10.3 gives a test program that uses this class.

**LISTING 10.3  UseBMIClass.java**

```java
public class UseBMIClass {
  public static void main(String[] args) {
    BMI bmi1 = new BMI("Kim Yang", 18, 145, 70); // create an object
    System.out.println("The BMI for " + bmi1.getName() + " is " + bmi1.getBMI() + " " + bmi1.getStatus()); // invoke instance method
    BMI bmi2 = new BMI("Susan King", 215, 70); // create an object
    System.out.println("The BMI for " + bmi2.getName() + " is " + bmi2.getBMI() + " " + bmi2.getStatus()); // invoke instance method
  }
}
```

The BMI for Kim Yang is 20.81 Normal
The BMI for Susan King is 30.85 Obese

Line 3 creates the object `bmi1` for **Kim Yang** and line 7 creates the object `bmi2` for **Susan King**. You can use the instance methods `getName()`, `getBMI()`, and `getStatus()` to return the BMI information in a `BMI` object.

The `BMI` class can be implemented as in Listing 10.4.

**LISTING 10.4  BMI.java**

```java
public class BMI {
  private String name;
  private int age;
  private double weight; // in pounds
  private double height; // in inches
  public static final double KILOGRAMS_PER_POUND = 0.45359237;
  public static final double METERS_PER_INCH = 0.0254;

  public BMI(String name, int age, double weight, double height) { // constructor
    this.name = name;
  }
}
```
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```java
    this.age = age;
    this.weight = weight;
    this.height = height;
}

public BMI(String name, double weight, double height) {
    this(name, 20, weight, height);
}

public double getBMI() {
    double bmi = weight * KILOGRAMS_PER_POUND /
                 ((height * METERS_PER_INCH) * (height * METERS_PER_INCH));
    return Math.round(bmi * 100) / 100.0;
}

public String getStatus() {
    double bmi = getBMI();
    if (bmi < 18.5)
        return "Underweight";
    else if (bmi < 25)
        return "Normal";
    else if (bmi < 30)
        return "Overweight";
    else
        return "Obese";
}

public String getName() {
    return name;
}

public int getAge() {
    return age;
}

public double getWeight() {
    return weight;
}

public double getHeight() {
    return height;
}
```

The mathematical formula for computing the BMI using weight and height is given in Section 3.8. The instance method `getBMI()` returns the BMI. Since the weight and height are instance data fields in the object, the `getBMI()` method can use these properties to compute the BMI for the object.

The instance method `getStatus()` returns a string that interprets the BMI. The interpretation is also given in Section 3.8.

This example demonstrates the advantages of the object-oriented paradigm over the procedural paradigm. The procedural paradigm focuses on designing methods. The object-oriented paradigm couples data and methods together into objects. Software design using the object-oriented paradigm focuses on objects and operations on objects. The object-oriented approach combines the power of the procedural paradigm with an added dimension that integrates data with operations into objects.

In procedural programming, data and operations on the data are separate, and this methodology requires passing data to methods. Object-oriented programming places data and
the operations that pertain to them in an object. This approach solves many of the problems inherent in procedural programming. The object-oriented programming approach organizes programs in a way that mirrors the real world, in which all objects are associated with both attributes and activities. Using objects improves software reusability and makes programs easier to develop and easier to maintain. Programming in Java involves thinking in terms of objects; a Java program can be viewed as a collection of cooperating objects.

10.2 Is the BMI class defined in Listing 10.4 immutable?

10.4 Class Relationships

To design classes, you need to explore the relationships among classes. The common relationships among classes are association, aggregation, composition, and inheritance.

This section explores association, aggregation, and composition. The inheritance relationship will be introduced in the next chapter.

10.4.1 Association

Association is a general binary relationship that describes an activity between two classes. For example, a student taking a course is an association between the Student class and the Course class, and a faculty member teaching a course is an association between the Faculty class and the Course class. These associations can be represented in UML graphical notation, as shown in Figure 10.4.

![Figure 10.4](image)

This UML diagram shows that a student may take any number of courses, a faculty member may teach at most three courses, a course may have from five to sixty students, and a course is taught by only one faculty member.

An association is illustrated by a solid line between two classes with an optional label that describes the relationship. In Figure 10.4, the labels are Take and Teach. Each relationship may have an optional small black triangle that indicates the direction of the relationship. In this figure, the direction indicates that a student takes a course (as opposed to a course taking a student).

Each class involved in the relationship may have a role name that describes the role it plays in the relationship. In Figure 10.4, teacher is the role name for Faculty.

Each class involved in an association may specify a multiplicity, which is placed at the side of the class to specify how many of the class’s objects are involved in the relationship in UML. A multiplicity could be a number or an interval that specifies how many of the class’s objects are involved in the relationship. The character * means an unlimited number of objects, and the interval m..n indicates that the number of objects is between m and n, inclusively. In Figure 10.4, each student may take any number of courses, and each course must have at least five and at most sixty students. Each course is taught by only one faculty member, and a faculty member may teach from zero to three courses per semester.

In Java code, you can implement associations by using data fields and methods. For example, the relationships in Figure 10.4 may be implemented using the classes in Figure 10.5. The
relation “a student takes a course” is implemented using the `addCourse` method in the `Student` class and the `addStudent` method in the `Course` class. The relation “a faculty teaches a course” is implemented using the `addCourse` method in the `Faculty` class and the `setFaculty` method in the `Course` class. The `Student` class may use a list to store the courses that the student is taking, the `Faculty` class may use a list to store the courses that the faculty is teaching, and the `Course` class may use a list to store students enrolled in the course and a data field to store the instructor who teaches the course.

```java
public class Student {
    private Course[] courseList;
    public void addCourse(Course s) { ... }
}
```

```java
public class Course {
    private Student[]classList;
    private Faculty faculty;
    public void addStudent(Student s) { ... }
    public void setFaculty(Faculty faculty) { ... }
}
```

```java
public class Faculty {
    private Course[] courseList;
    public void addCourse(Course c) { ... }
}
```

**Figure 10.5** The association relations are implemented using data fields and methods in classes.

Note
There are many possible ways to implement relationships. For example, the student and faculty information in the `Course` class can be omitted, since they are already in the `Student` and `Faculty` class. Likewise, if you don’t need to know the courses a student takes or a faculty member teaches, the data field `courseList` and the `addCourse` method in `Student` or `Faculty` can be omitted.

### 10.4.2 Aggregation and Composition

Aggregation is a special form of association that represents an ownership relationship between two objects. Aggregation models `has-a` relationships. The owner object is called an *aggregating object*, and its class is called an *aggregating class*. The subject object is called an *aggregated object*, and its class is called an *aggregated class*.

An object can be owned by several other aggregating objects. If an object is exclusively owned by an aggregating object, the relationship between the object and its aggregating object is referred to as a *composition*. For example, “a student has a name” is a composition relationship between the `Student` class and the `Name` class, whereas “a student has an address” is an aggregation relationship between the `Student` class and the `Address` class, since an address can be shared by several students. In UML, a filled diamond is attached to an aggregating class (in this case, `Student`) to denote the composition relationship with an aggregated class (`Name`), and an empty diamond is attached to an aggregating class (`Address`) to denote the aggregation relationship with an aggregated class (`Student`), as shown in Figure 10.6.

**Figure 10.6** Each student has a name and an address.

In Figure 10.6, each student has only one multiplicity—address—and each address can be shared by up to 3 students. Each student has one name, and a name is unique for each student.
An aggregation relationship is usually represented as a data field in the aggregating class. For example, the relationships in Figure 10.6 may be implemented using the classes in Figure 10.7. The relation “a student has a name” and “a student has an address” are implemented in the data field name and address in the Student class.

![Aggregation diagram](image)

**Figure 10.7** The composition relations are implemented using data fields in classes.

Aggregation may exist between objects of the same class. For example, a person may have a supervisor. This is illustrated in Figure 10.8.

![Aggregation diagram](image)

**Figure 10.8** A person may have a supervisor.

In the relationship “a person has a supervisor,” a supervisor can be represented as a data field in the Person class, as follows:

```java
public class Person {
    // The type for the data is the class itself
    private Person supervisor;

    ...
}
```

If a person can have several supervisors, as shown in Figure 10.9a, you may use an array to store supervisors, as shown in Figure 10.9b.

![Aggregation diagram](image)

**Figure 10.9** A person can have several supervisors.

**Note**
Since aggregation and composition relationships are represented using classes in the same way, we will not differentiate them and call both compositions for simplicity.

### Check Point

10.3 What are common relationships among classes?
10.4 What is association? What is aggregation? What is composition?
10.5 What is UML notation of aggregation and composition?
10.6 Why both aggregation and composition are together referred to as composition?
Chapter 10  Object-Oriented Thinking

10.5 Case Study: Designing the Course Class

This section designs a class for modeling courses.

This book’s philosophy is teaching by example and learning by doing. The book provides a wide variety of examples to demonstrate object-oriented programming. This section and the next offer additional examples on designing classes.

Suppose you need to process course information. Each course has a name and has students enrolled. You should be able to add/drop a student to/from the course. You can use a class to model the courses, as shown in Figure 10.10.

![Figure 10.10](Image)

**Figure 10.10** The Course class models the courses.

A Course object can be created using the constructor `Course(String name)` by passing a course name. You can add students to the course using the `addStudent(String student)` method, drop a student from the course using the `dropStudent(String student)` method, and return all the students in the course using the `getStudents()` method. Suppose the Course class is available; Listing 10.5 gives a test class that creates two courses and adds students to them.

**Listing 10.5** TestCourse.java

```
public class TestCourse {
    public static void main(String[] args) {
        Course course1 = new Course("Data Structures");
        Course course2 = new Course("Database Systems");

        course1.addStudent("Peter Jones");
        course1.addStudent("Kim Smith");
        course1.addStudent("Anne Kennedy");

        course2.addStudent("Peter Jones");
        course2.addStudent("Steve Smith");

        System.out.println("Number of students in course1: " + course1.getNumberOfStudents());
        String[] students = course1.getStudents();
        for (int i = 0; i < course1.getNumberOfStudents(); i++)
            System.out.print(students[i] + " , ");
        System.out.println();

        System.out.println("Number of students in course2: " + course2.getNumberOfStudents());
    }
}
```
The `Course` class is implemented in Listing 10.6. It uses an array to store the students in the course. For simplicity, assume that the maximum course enrollment is 100. The array is created using `new String[100]` in line 3. The `addStudent` method (line 10) adds a student to the array. Whenever a new student is added to the course, `numberOfStudents` is increased (line 12). The `getStudents` method returns the array. The `dropStudent` method (line 27) is left as an exercise.

**LISTING 10.6 Course.java**

```java
public class Course {
    private String courseName;
    private String[] students = new String[100];
    private int numberOfStudents;

    public Course(String courseName) {
        this.courseName = courseName;
    }

    public void addStudent(String student) {
        students[numberOfStudents] = student;
        numberOfStudents++;
    }

    public String[] getStudents() {
        return students;
    }

    public int getNumberOfStudents() {
        return numberOfStudents;
    }

    public String getCourseName() {
        return courseName;
    }

    public void dropStudent(String student) {
        // Left as an exercise in Programming Exercise 10.9
    }
}
```

The array size is fixed to be 100 (line 3), so you cannot have more than 100 students in the course. You can improve the class by automatically increasing the array size in Programming Exercise 10.9.

When you create a `Course` object, an array object is created. A `Course` object contains a reference to the array. For simplicity, you can say that the `Course` object contains the array.

The user can create a `Course` object and manipulate it through the public methods `addStudent`, `dropStudent`, `getNumberOfStudents`, and `getStudents`. However, the user doesn’t need to know how these methods are implemented. The `Course` class encapsulates the internal implementation. This example uses an array to store students, but you could use a different data structure to store students. The program that uses `Course` does not need to change as long as the contract of the public methods remains unchanged.
10.6 Case Study: Designing a Class for Stacks

Recall that a stack is a data structure that holds data in a last-in, first-out fashion, as shown in Figure 10.11.

Stacks have many applications. For example, the compiler uses a stack to process method invocations. When a method is invoked, its parameters and local variables are pushed into a stack. When a method calls another method, the new method’s parameters and local variables are pushed into the stack. When a method finishes its work and returns to its caller, its associated space is released from the stack.

You can define a class to model stacks. For simplicity, assume the stack holds the int values. So name the stack class StackOfIntegers. The UML diagram for the class is shown in Figure 10.12.

Suppose that the class is available. The test program in Listing 10.7 uses the class to create a stack (line 3), store ten integers 0, 1, 2, . . . , and 9 (line 6), and displays them in reverse order (line 9).

Listing 10.7 TestStackOfIntegers.java

```java
public class TestStackOfIntegers {
    public static void main(String[] args) {
        StackOfIntegers stack = new StackOfIntegers();
```
10.6 Case Study: Designing a Class for Stacks

for (int i = 0; i < 10; i++)
    stack.push(i);

while (!stack.empty())
    System.out.print(stack.pop() + " ");

How do you implement the StackOfIntegers class? The elements in the stack are stored in an array named elements. When you create a stack, the array is also created. The no-arg constructor creates an array with the default capacity of 16. The variable size counts the number of elements in the stack, and size - 1 is the index of the element at the top of the stack, as shown in Figure 10.13. For an empty stack, size is 0.

The StackOfIntegers class is implemented in Listing 10.8. The methods empty(), peek(), pop(), and getSize() are easy to implement. To implement push(int value), assign value to elements[size] if size < capacity (line 24). If the stack is full (i.e., size >= capacity), create a new array of twice the current capacity (line 19), copy the contents of the current array to the new array (line 20), and assign the reference of the new array to the current array in the stack (line 21). Now you can add the new value to the array (line 24).

LISTING 10.8 StackOfIntegers.java

```java
1  public class StackOfIntegers {
2     private int[] elements;
3     private int size;
4     public static final int DEFAULT_CAPACITY = 16;  
5  }
6  /** Construct a stack with the default capacity 16 */
7  public StackOfIntegers() {
8     this (DEFAULT_CAPACITY);
9  }
10  /** Construct a stack with the specified maximum capacity */
11  public StackOfIntegers(int capacity) {
12     elements = new int[capacity];
13  }
```
Chapter 10  Object-Oriented Thinking

10.7 Processing Primitive Data Type Values as Objects

A primitive type value is not an object, but it can be wrapped in an object using a wrapper class in the Java API.

Owing to performance considerations, primitive data type values are not objects in Java. Because of the overhead of processing objects, the language’s performance would be adversely affected if primitive data type values were treated as objects. However, many Java methods require the use of objects as arguments. Java offers a convenient way to incorporate, or wrap, a primitive data type into an object (e.g., wrapping `int` into the `Integer` class, wrapping `double` into the `Double` class, and wrapping `char` into the `Character` class,). By using a wrapper class, you can process primitive data type values as objects. Java provides `Boolean`, `Character`, `Double`, `Float`, `Byte`, `Short`, `Integer`, and `Long` wrapper classes in the `java.lang` package for primitive data types. The `Boolean` class wraps a Boolean value `true` or `false`. This section uses `Integer` and `Double` as examples to introduce the numeric wrapper classes.

why wrapper class?

Key Point

Most wrapper class names for a primitive type are the same as the primitive data type name with the first letter capitalized. The exceptions are `Integer` and `Character`.

naming convention

Numeric wrapper classes are very similar to each other. Each contains the methods `doubleValue()`, `floatValue()`, `intValue()`, `longValue()`, `shortValue()`, and `byteValue()`. These methods “convert” objects into primitive type values. The key features of `Integer` and `Double` are shown in Figure 10.14.
10.7 Processing Primitive Data Type Values as Objects

You can construct a wrapper object either from a primitive data type value or from a string representing the numeric value—for example, `new Double(5.0), new Double("5.0"), new Integer(5), and new Integer("5").` The wrapper classes do not have no-arg constructors. The instances of all wrapper classes are immutable; this means that, once the objects are created, their internal values cannot be changed.

Each numeric wrapper class has the constants `MAX_VALUE` and `MIN_VALUE`. `MAX_VALUE` represents the maximum value of the corresponding primitive data type. For `Byte, Short, Integer, and Long`, `MIN_VALUE` represents the minimum `byte, short, int, and long` values. For `Float` and `Double`, `MIN_VALUE` represents the minimum `positive float` and `double` values. The following statements display the maximum integer `(2,147,483,647)`, the minimum positive float `(1.4E–45)`, and the maximum double floating-point number `(1.79769313486231570e+308d).

```
System.out.println("The maximum integer is " + Integer.MAX_VALUE);
System.out.println("The minimum positive float is " + Float.MIN_VALUE);
System.out.println("The maximum double-precision floating-point number is " + Double.MAX_VALUE);
```

Each numeric wrapper class contains the methods `doubleValue(), floatValue(), intValue(), longValue(), and shortValue()` for returning a `double, float, int, long, or short` value for the wrapper object. For example,

- `new Double(12.4).intValue()` returns `12`;
- `new Integer(12).doubleValue()` returns `12.0`;

Recall that the `String` class contains the `compareTo` method for comparing two strings. The numeric wrapper classes contain the `compareTo` method for comparing two numbers.
and returns 1, 0, or -1, if this number is greater than, equal to, or less than the other number. For example,

```java
new Double(12.4).compareTo(new Double(12.3)) returns 1;
new Double(12.3).compareTo(new Double(12.3)) returns 0;
new Double(12.3).compareTo(new Double(12.51)) returns -1;
```

The numeric wrapper classes have a useful static method, `valueOf(String s)`. This method creates a new object initialized to the value represented by the specified string. For example,

```java
Double doubleObject = Double.valueOf("12.4");
Integer integerObject = Integer.valueOf("12");
```

You have used the `parseInt` method in the `Integer` class to parse a numeric string into an `int` value and the `parseDouble` method in the `Double` class to parse a numeric string into a `double` value. Each numeric wrapper class has two overloaded parsing methods to parse a numeric string into an appropriate numeric value based on 10 (decimal) or any specified radix (e.g., 2 for binary, 8 for octal, and 16 for hexadecimal).

```java
// These two methods are in the Byte class
public static byte parseByte(String s)
public static byte parseByte(String s, int radix)

// These two methods are in the Short class
public static short parseShort(String s)
public static short parseShort(String s, int radix)

// These two methods are in the Integer class
public static int parseInt(String s)
public static int parseInt(String s, int radix)

// These two methods are in the Long class
public static long parseLong(String s)
public static long parseLong(String s, int radix)

// These two methods are in the Float class
public static float parseFloat(String s)
public static float parseFloat(String s, int radix)

// These two methods are in the Double class
public static double parseDouble(String s)
public static double parseDouble(String s, int radix)
```

For example,

```java
Integer.parseInt("11", 2) returns 3;
Integer.parseInt("12", 8) returns 10;
Integer.parseInt("13", 10) returns 13;
Integer.parseInt("1A", 16) returns 26;
```

`Integer.parseInt("12", 2) would raise a runtime exception because 12 is not a binary number. Note that you can convert a decimal number into a hex number using the `format` method. For example,

```java
String.format("%x", 26) returns 1A;
```
10.8 Automatic Conversion between Primitive Types and Wrapper Class Types

A primitive type value can be automatically converted to an object using a wrapper class, and vice versa, depending on the context.

Converting a primitive value to a wrapper object is called boxing. The reverse conversion is called unboxing. Java allows primitive types and wrapper classes to be converted automatically. The compiler will automatically box a primitive value that appears in a context requiring an object, and will unbox an object that appears in a context requiring a primitive value. This is called autoboxing and autounboxing.
For instance, the following statement in (a) can be simplified as in (b) due to autoboxing.

\[
\begin{array}{ll}
\text{Integer intObject = new Integer(2);} & \text{Equivalent Integer intObject = 2;}
\end{array}
\]

Consider the following example:

```java
1  Integer[] intArray = {1, 2, 3};
2  System.out.println(intArray[0] + intArray[1] + intArray[2]);
```

In line 1, the primitive values 1, 2, and 3 are automatically boxed into objects new Integer(1), new Integer(2), and new Integer(3). In line 2, the objects intArray[0], intArray[1], and intArray[2] are automatically unboxed into int values that are added together.

10.12 What are autoboxing and autounboxing? Are the following statements correct?

a. `Integer x = 3 + new Integer(5);`

b. `Integer x = 3;`

c. `Double x = 3;`

d. `Double x = 3.0;`

e. `int x = new Integer(3);`

f. `int x = new Integer(3) + new Integer(4);`

10.13 Show the output of the following code?

```java
public class Test {
    public static void main(String[] args) {
        Double x = 3.5;
        System.out.println(x.intValue());
        System.out.println(x.compareTo(4.5));
    }
}
```

10.9 The BigInteger and BigDecimal Classes

The `BigInteger` and `BigDecimal` classes can be used to represent integers or decimal numbers of any size and precision.

If you need to compute with very large integers or high-precision floating-point values, you can use the `BigInteger` and `BigDecimal` classes in the `java.math` package. Both are immutable. The largest integer of the `long` type is `Long.MAX_VALUE` (i.e., `9223372036854775807`). An instance of `BigInteger` can represent an integer of any size. You can use `new BigInteger(String)` and `new BigDecimal(String)` to create an instance of `BigInteger` and `BigDecimal`, use the `add`, `subtract`, `multiply`, `divide`, and `remainder` methods to perform arithmetic operations, and use the `compareTo` method to compare two big numbers. For example, the following code creates two `BigInteger` objects and multiplies them.

```java
BigInteger a = new BigInteger("9223372036854775807");
BigInteger b = new BigInteger("2");
BigInteger c = a.multiply(b); // 9223372036854775807 * 2
System.out.println(c);
```
10.9 The `BigInteger` and `BigDecimal` Classes

There is no limit to the precision of a `BigDecimal` object. The `divide` method may throw an `ArithmeticException` if the result cannot be terminated. However, you can use the overloaded `divide(BigDecimal d, int scale, int roundingMode)` method to specify a scale and a rounding mode to avoid this exception, where `scale` is the maximum number of digits after the decimal point. For example, the following code creates two `BigDecimal` objects and performs division with scale 20 and rounding mode `BigDecimal.ROUND_UP`.

```java
BigDecimal a = new BigDecimal(1.0);
BigDecimal b = new BigDecimal(3);
BigDecimal c = a.divide(b, 20, BigDecimal.ROUND_UP);
System.out.println(c);
```

The output is `0.33333333333333333334`.

Note that the factorial of an integer can be very large. Listing 10.9 gives a method that can return the factorial of any integer.

**Listing 10.9 LargeFactorial.java**

```java
import java.math.*;

public class LargeFactorial {
    public static void main(String[] args) {
        System.out.println("50! is \n" + factorial(50));
    }

    public static BigInteger factorial(long n) {
        BigInteger result = BigInteger.ONE;
        for (int i = 1; i <= n; i++)
            result = result.multiply(new BigInteger(i + "");
        return result;
    }
}
```

**BigInteger.ONE** (line 9) is a constant defined in the `BigInteger` class. `BigInteger.ONE` is the same as `new BigInteger("1")`.

A new result is obtained by invoking the `multiply` method (line 11).

10.14 What is the output of the following code?

```java
public class Test {
    public static void main(String[] args) {
        java.math.BigInteger x = new java.math.BigInteger("3");
        java.math.BigInteger y = new java.math.BigInteger("7");
        java.math.BigInteger z = x.add(y);
        System.out.println("x is " + x);
        System.out.println("y is " + y);
        System.out.println("z is " + z);
    }
}
```
10.10 The String Class

A String object is immutable: Its content cannot be changed once the string is created.

Strings were introduced in Section 4.4. You know strings are objects. You can invoke the `charAt(index)` method to obtain a character at the specified index from a string, the `length()` method to return the size of a string, the `substring` method to return a substring in a string, and the `indexOf` and `lastIndexOf` methods to return the first or last index of a matching character or a substring. We will take a closer look at strings in this section.

The `String` class has 13 constructors and more than 40 methods for manipulating strings. Not only is it very useful in programming, but it is also a good example for learning classes and objects.

10.10.1 Constructing a String

You can create a string object from a string literal or from an array of characters. To create a string from a string literal, use the syntax:

```java
String newString = new String(stringLiteral);
```

The argument `stringLiteral` is a sequence of characters enclosed inside double quotes. The following statement creates a `String` object `message` for the string literal "Welcome to Java":

```java
String message = new String("Welcome to Java");
```

Java treats a string literal as a `String` object. Thus, the following statement is valid:

```java
String message = "Welcome to Java";
```

You can also create a string from an array of characters. For example, the following statements create the string "Good Day":

```java
char[] charArray = {'G', 'o', 'o', 'd', ' ', 'D', 'a', 'y'};
String message = new String(charArray);
```

Note

A `String` variable holds a reference to a `String` object that stores a string value. Strictly speaking, the terms `String variable`, `String object`, and `string value` are different, but most of the time the distinctions between them can be ignored. For simplicity, the term `string` will often be used to refer to `String variable`, `String object`, and string value.

10.10.2 Immutable Strings and Interned Strings

A `String` object is immutable; its contents cannot be changed. Does the following code change the contents of the string?

```java
String s = "Java";
s = "HTML";
```

The answer is no. The first statement creates a `String` object with the content "Java" and assigns its reference to `s`. The second statement creates a new `String` object with the content "HTML" and assigns its reference to `s`. The first `String` object still exists after the assignment, but it can no longer be accessed, because variable `s` now points to the new object, as shown in Figure 10.15.
Because strings are immutable and are ubiquitous in programming, the JVM uses a unique instance for string literals with the same character sequence in order to improve efficiency and save memory. Such an instance is called an interned string. For example, the following statements:

```java
String s1 = "Welcome to Java";
String s2 = new String("Welcome to Java");
String s3 = "Welcome to Java";
System.out.println("s1 == s2 is " + (s1 == s2));
System.out.println("s1 == s3 is " + (s1 == s3));
```

display

```
s1 == s2 is false
s1 == s3 is true
```

In the preceding statements, `s1` and `s3` refer to the same interned string—"Welcome to Java"—so `s1 == s3` is true. However, `s1 == s2` is false, because `s1` and `s2` are two different string objects, even though they have the same contents.

### 10.10.3 Replacing and Splitting Strings

The `String` class provides the methods for replacing and splitting strings, as shown in Figure 10.16.

```
java.lang.String
+replace(oldChar: char, newChar: char): String
+replaceFirst(oldString: String, newString: String): String
+replaceAll(oldString: String, newString: String): String
+split(delimiter: String): String[]
```

Returns a new string that replaces all matching characters in this string with the new character.

Returns a new string that replaces the first matching substring in this string with the new substring.

Returns a new string that replaces all matching substrings in this string with the new substring.

Returns an array of strings consisting of the substrings split by the delimiter.

**FIGURE 10.15** Strings are immutable; once created, their contents cannot be changed.

**FIGURE 10.16** The `String` class contains the methods for replacing and splitting strings.
Once a string is created, its contents cannot be changed. The methods \texttt{replace}, \texttt{replaceFirst}, and \texttt{replaceAll} return a new string derived from the original string (without changing the original string!). Several versions of the \texttt{replace} methods are provided to replace a character or a substring in the string with a new character or a new substring.

For example,

\begin{verbatim}
"Welcome".replace('e', 'A') returns a new string, WAlcomA.
"Welcome".replaceFirst("e", "AB") returns a new string, WABlcome.
"Welcome".replace("e", "AB") returns a new string, WAbicomAB.
"Welcome".replace("el", "AB") returns a new string, WABcome.
\end{verbatim}

The \texttt{split} method can be used to extract tokens from a string with the specified delimiters. For example, the following code

\begin{verbatim}
String[] tokens = "Java#HTML#Perl".split("#");
for (int i = 0; i < tokens.length; i++)
    System.out.print(tokens[i] + " ");
\end{verbatim}

displays

Java HTML Perl

\subsection*{10.10.4 \textbf{Matching, Replacing and Splitting by Patterns}}

Often you will need to write code that validates user input, such as to check whether the input is a number, a string with all lowercase letters, or a Social Security number. How do you write this type of code? A simple and effective way to accomplish this task is to use the regular expression.

A \textit{regular expression} (abbreviated \textit{regex}) is a string that describes a pattern for matching a set of strings. You can match, replace, or split a string by specifying a pattern. This is an extremely useful and powerful feature.

Let us begin with the \texttt{matches} method in the \texttt{String} class. At first glance, the \texttt{matches} method is very similar to the \texttt{equals} method. For example, the following two statements both evaluate to \texttt{true}.

\begin{verbatim}
"Java".matches("Java");
"Java".equals("Java");
\end{verbatim}

However, the \texttt{matches} method is more powerful. It can match not only a fixed string, but also a set of strings that follow a pattern. For example, the following statements all evaluate to \texttt{true}:

\begin{verbatim}
"Java is fun".matches("Java.*")
"Java is cool".matches("Java.*")
"Java is powerful".matches("Java.*")
\end{verbatim}

\texttt{Java.*} in the preceding statements is a regular expression. It describes a string pattern that begins with Java followed by \textit{any} zero or more characters. Here, the substring matches any zero or more characters.

The following statement evaluates to \texttt{true}.

\begin{verbatim}
"440-02-4534".matches("\\d{3}-\\d{2}-\\d{4}")
\end{verbatim}

Here \texttt{\d} represents a single digit, and \texttt{\d{3}} represents three digits.
The `replaceAll`, `replaceFirst`, and `split` methods can be used with a regular expression. For example, the following statement returns a new string that replaces $, +, or # in `a+b$#c` with the string `NNN`.

```java
String s = "a+b$#c".replaceAll("[$+#]", "NNN");
System.out.println(s);
```

Here the regular expression `[$+#]` specifies a pattern that matches $, +, or #. So, the output is `aNNNbNNNNNC`.

The following statement splits the string into an array of strings delimited by punctuation marks.

```java
String[] tokens = "Java,C?C#,C++".split("[.,:;?]");
for (int i = 0; i < tokens.length; i++)
  System.out.println(tokens[i]);
```

In this example, the regular expression `[,;?:]` specifies a pattern that matches , , , ; , or ?. Each of these characters is a delimiter for splitting the string. Thus, the string is split into `Java`, `C`, `C#`, and `C++`, which are stored in array `tokens`.

Regular expression patterns are complex for beginning students to understand. For this reason, simple patterns are introduced in this section. Please refer to Appendix H, Regular Expressions, to learn more about these patterns.

### 10.10.5 Conversion between Strings and Arrays

Strings are not arrays, but a string can be converted into an array, and vice versa. To convert a string into an array of characters, use the `toCharArray` method. For example, the following statement converts the string `Java` to an array.

```java
char[] chars = "Java".toCharArray();
```

Thus, `chars[0]` is `J`, `chars[1]` is `a`, `chars[2]` is `v`, and `chars[3]` is `a`.

You can also use the `getChars(int srcBegin, int srcEnd, char[] dst, int dstBegin)` method to copy a substring of the string from index `srcBegin` to index `srcEnd-1` into a character array `dst` starting from index `dstBegin`. For example, the following code copies a substring "3720" in "CS3720" from index 2 to index 6-1 into the character array `dst` starting from index 4.

```java
char[] dst = {'J', 'a', 'v', 'a', '3', '7', '2', '0'};
"CS3720".getChars(2, 6, dst, 4);
```

Thus, `dst` becomes `{J', 'a', 'v', 'A', '3', '7', '2', '0'}`.

To convert an array of characters into a string, use the `String(char[])` constructor or the `valueOf(char[])` method. For example, the following statement constructs a string from an array using the `String` constructor.

```java
String str = new String(new char[]{'J', 'a', 'v', 'a'});
```

The next statement constructs a string from an array using the `valueOf` method.

```java
String str = String.valueOf(new char[]{'J', 'a', 'v', 'a'});
```

### 10.10.6 Converting Characters and Numeric Values to Strings

Recall that you can use `Double.parseDouble(str)` or `Integer.parseInt(str)` to convert a string to a `double` value or an `int` value and you can convert a character or a number into a string by using the string concatenating operator. Another way of converting a
number into a string is to use the overloaded static `valueOf` method. This method can also be used to convert a character or an array of characters into a string, as shown in Figure 10.17.

<table>
<thead>
<tr>
<th>overloaded <code>valueOf</code></th>
<th>Returns a string consisting of the character c.</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>valueOf(data: char[])</code>: String</td>
<td>Returns a string consisting of the characters in the array.</td>
</tr>
<tr>
<td><code>valueOf(d: double)</code>: String</td>
<td>Returns a string representing the <code>double</code> value.</td>
</tr>
<tr>
<td><code>valueOf(f: float)</code>: String</td>
<td>Returns a string representing the <code>float</code> value.</td>
</tr>
<tr>
<td><code>valueOf(i: int)</code>: String</td>
<td>Returns a string representing the <code>int</code> value.</td>
</tr>
<tr>
<td><code>valueOf(l: long)</code>: String</td>
<td>Returns a string representing the <code>long</code> value.</td>
</tr>
<tr>
<td><code>valueOf(b: boolean)</code>: String</td>
<td>Returns a string representing the <code>boolean</code> value.</td>
</tr>
</tbody>
</table>

**Figure 10.17** The `String` class contains the static methods for creating strings from primitive type values.

For example, to convert a `double` value 5.44 to a string, use `String.valueOf(5.44)`. The return value is a string consisting of the characters '5', '.', '4', and '4'.

### 10.10.7 Formatting Strings

The `String` class contains the static `format` method to return a formatted string. The syntax to invoke this method is:

```java
String.format(format, item1, item2, ..., itemk)
```

This method is similar to the `printf` method except that the `format` method returns a formatted string, whereas the `printf` method displays a formatted string. For example,

```java
String s = String.format("%7.2f%6d%-4s", 45.556, 14, "AB");
System.out.println(s);
```

Displays

```
45.56 14AB
```

Note that

```java
System.out.printf(format, item1, item2, ..., itemk);
```

is equivalent to

```java
System.out.print(
    String.format(format, item1, item2, ..., itemk));
```

where the square box (□) denotes a blank space.

### Check Point

10.15 Suppose that `s1`, `s2`, `s3`, and `s4` are four strings, given as follows:

```java
String s1 = "Welcome to Java";
String s2 = s1;
String s3 = new String("Welcome to Java");
String s4 = "Welcome to Java";
```

What are the results of the following expressions?

a. `s1 == s2`

b. `s1 == s3`
c. \( s_1 == s_4 \)
d. \( s_1.equals(s_3) \)
e. \( s_1.equals(s_4) \)
f. "Welcome to Java".replace("Java", "HTML")
g. \( s_1.replace('o', 'T') \)
h. \( s_1.replaceAll("o", "T") \)
i. \( s_1.replaceFirst("o", "T") \)
j. \( s_1.toCharArray() \)

10.16 To create the string \textit{Welcome to Java}, you may use a statement like this:

\begin{verbatim}
String s = "Welcome to Java";
\end{verbatim}

or:

\begin{verbatim}
String s = new String("Welcome to Java");
\end{verbatim}

Which one is better? Why?

10.17 What is the output of the following code?

\begin{verbatim}
String s1 = "Welcome to Java";
String s2 = s1.replace("o", "abc");
System.out.println(s1);
System.out.println(s2);
\end{verbatim}

10.18 Let \( s_1 \) be "Welcome" and \( s_2 \) be "welcome". Write the code for the following statements:

a. Replace all occurrences of the character \textit{e} with \textit{E} in \( s_1 \) and assign the new string to \( s_2 \).

b. Split \textit{Welcome to Java and HTML} into an array \textit{tokens} delimited by a space and assign the first two tokens into \( s_1 \) and \( s_2 \).

10.19 Does any method in the \textit{String} class change the contents of the string?

10.20 Suppose string \( s \) is created using \textit{new String()}; what is \( s.length() \)?

10.21 How do you convert a \textit{char}, an array of characters, or a number to a string?

10.22 Why does the following code cause a \textit{NullPointerException}?

\begin{verbatim}
1 public class Test {
2     private String text;
3
4     public Test(String s) {
5         String text = s;
6     }
7
8     public static void main(String[] args) {
9         Test test = new Test("ABC");
10        System.out.println(test.text.toLowerCase());
11     }
12 }
\end{verbatim}

10.23 What is wrong in the following program?

\begin{verbatim}
1 public class Test {
2     String text;
3
4     public Test(String s) {
5         String text = s;
6     }
7
8     public static void main(String[] args) {
9         Test test = new Test("ABC");
10        System.out.println(test.text.toLowerCase());
11     }
12 }
\end{verbatim}
Chapter 10  Object-Oriented Thinking

```java
public void Test(String s) {
    text = s;
}

public static void main(String[] args) {
    Test test = new Test("ABC");
    System.out.println(test);
}
```

10.24 Show the output of the following code.

```java
public class Test {
    public static void main(String[] args) {
        System.out.println("Hi, ABC, good".matches("ABC "));
        System.out.println("Hi, ABC, good".matches(".*ABC.*"));
        System.out.println("A,B;C".replaceAll("\[,;\]", ", "));
        System.out.println("A,B;C".replaceAll("\[,;\]", "#"));
    }
}
```

10.25 Show the output of the following code.

```java
public class Test {
    public static void main(String[] args) {
        String s = "Hi, Good Morning";
        System.out.println(m(s));
    }

    public static int m(String s) {
        int count = 0;
        for (int i = 0; i < s.length(); i++)
            if (Character.isUpperCase(s.charAt(i)))
                count++;
        return count;
    }
}
```

10.11 The StringBuilder and StringBuffer Classes

*Key Point*

The `StringBuilder` and `StringBuffer` classes are similar to the `String` class except that the `String` class is immutable.

In general, the `StringBuilder` and `StringBuffer` classes can be used wherever a string is used. `StringBuilder` and `StringBuffer` are more flexible than `String`. You can add, insert, or append new contents into `StringBuilder` and `StringBuffer` objects, whereas the value of a `String` object is fixed once the string is created.

The `StringBuilder` class is similar to `StringBuffer` except that the methods for modifying the buffer in `StringBuffer` are synchronized, which means that only one task is allowed to execute the methods. Use `StringBuffer` if the class might be accessed by multiple tasks concurrently, because synchronization is needed in this case to prevent corruptions to...
10.11 The **StringBuilder** and **StringBuffer** Classes 393

**StringBuilder**. Concurrent programming will be introduced in Chapter 30. Using **StringBuilder** is more efficient if it is accessed by just a single task, because no synchronization is needed in this case. The constructors and methods in **StringBuffer** and **StringBuilder** are almost the same. This section covers **StringBuilder**. You can replace **StringBuilder** in all occurrences in this section by **StringBuffer**. The program can compile and run without any other changes.

The **StringBuilder** class has three constructors and more than 30 methods for managing the builder and modifying strings in the builder. You can create an empty string builder or a string builder from a string using the constructors, as shown in Figure 10.18.

**StringBuilder constructors**

<table>
<thead>
<tr>
<th>java.lang.StringBuilder</th>
</tr>
</thead>
<tbody>
<tr>
<td>+StringBuilder()</td>
</tr>
<tr>
<td>+StringBuilder(capacity: int)</td>
</tr>
<tr>
<td>+StringBuilder(s: String)</td>
</tr>
</tbody>
</table>

Constructs an empty string builder with capacity 16.
Constructs a string builder with the specified capacity.
Constructs a string builder with the specified string.

**Figure 10.18** The **StringBuilder** class contains the constructors for creating instances of **StringBuilder**.

### 10.11.1 Modifying Strings in the **StringBuilder**

You can append new contents at the end of a string builder, insert new contents at a specified position in a string builder, and delete or replace characters in a string builder, using the methods listed in Figure 10.19.

**StringBuilder methods**

<table>
<thead>
<tr>
<th>java.lang.StringBuilder</th>
</tr>
</thead>
<tbody>
<tr>
<td>+append(data: char[]): StringBuilder</td>
</tr>
<tr>
<td>+append(data: char[], offset: int, len: int): StringBuilder</td>
</tr>
<tr>
<td>+append(v: aPrimitiveType): StringBuilder</td>
</tr>
<tr>
<td>+append(s: String): StringBuilder</td>
</tr>
<tr>
<td>+delete(startIndex: int, endIndex: int): StringBuilder</td>
</tr>
<tr>
<td>+deleteCharAt(index: int): StringBuilder</td>
</tr>
<tr>
<td>+insert(index: int, data: char[], offset: int, len: int): StringBuilder</td>
</tr>
<tr>
<td>+insert(offset: int, data: char[]): StringBuilder</td>
</tr>
<tr>
<td>+insert(offset: int, b: aPrimitiveType): StringBuilder</td>
</tr>
<tr>
<td>+insert(offset: int, s: String): StringBuilder</td>
</tr>
<tr>
<td>+replace(startIndex: int, endIndex: int, s: String): StringBuilder</td>
</tr>
<tr>
<td>+reverse(): StringBuilder</td>
</tr>
<tr>
<td>+setCharAt(index: int, ch: char): void</td>
</tr>
</tbody>
</table>

Appends a char array into this string builder.
Appends a subarray in data into this string builder.
Appends a primitive type value as a string to this builder.
Appends a string to this string builder.
Deletes characters from startIndex to endIndex-1.
Deletes a character at the specified index.
Inserts a subarray of the data in the array into the builder at the specified index.
Inserts data into this builder at the position offset.
Inserts a value converted to a string into this builder.
Inserts a string into this builder at the position offset.
Replaces the characters in this builder from startIndex to endIndex-1 with the specified string.
Reverses the characters in the builder.
Sets a new character at the specified index in this builder.

**Figure 10.19** The **StringBuilder** class contains the methods for modifying string builders.
The `StringBuilder` class provides several overloaded methods to append `boolean`, `char`, `char[]`, `double`, `float`, `int`, `long`, and `String` into a string builder. For example, the following code appends strings and characters into `stringBuilder` to form a new string, `Welcome to Java`.

```java
StringBuilder stringBuilder = new StringBuilder();
stringBuilder.append("Welcome");
stringBuilder.append(' ');
stringBuilder.append("to");
stringBuilder.append(' ');
stringBuilder.append("Java");
```

The `StringBuilder` class also contains overloaded methods to insert `boolean`, `char`, `char[]`, `double`, `float`, `int`, `long`, and `String` into a string builder. Consider the following code:

```java
stringBuilder.insert(11, "HTML and ");
```

Suppose `stringBuilder` contains `Welcome to Java` before the `insert` method is applied. This code inserts "HTML and " at position 11 in `stringBuilder` (just before the J). The new `StringBuilder` is `Welcome to HTML and Java`.

You can also delete characters from a string in the builder using the two `delete` methods, reverse the string using the `reverse` method, replace characters using the `replace` method, or set a new character in a string using the `setCharAt` method.

For example, suppose `stringBuilder` contains `Welcome to Java` before each of the following methods is applied:

- `stringBuilder.delete(8, 11)` changes the builder to `Welcome Java`.
- `stringBuilder.deleteCharAt(8)` changes the builder to `Welcome o Java`.
- `stringBuilder.reverse()` changes the builder to `avaJ ot emocleW`.
- `stringBuilder.replace(11, 15, "HTML")` changes the builder to `Welcome to HTML`.
- `stringBuilder.setCharAt(0, 'w')` sets the builder to `welcome to Java`.

All these modification methods except `setCharAt` do two things:
- Change the contents of the string builder
- Return the reference of the string builder

For example, the following statement

```java
StringBuilder stringBuilder1 = stringBuilder.reverse();
```

reverses the string in the builder and assigns the builder's reference to `stringBuilder1`. Thus, `stringBuilder` and `stringBuilder1` both point to the same `StringBuilder` object. Recall that a value-returning method can be invoked as a statement, if you are not interested in the return value of the method. In this case, the return value is simply ignored. For example, in the following statement

```java
stringBuilder.reverse();
```

the return value is ignored.

**Tip**
If a string does not require any change, use `String` rather than `StringBuilder`.
Java can perform some optimizations for `String`, such as sharing interned strings.
10.11.2 The **toString**, **capacity**, **length**, **setLength**, and **charAt** Methods

The **StringBuilder** class provides the additional methods for manipulating a string builder and obtaining its properties, as shown in Figure 10.20.

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>toString()</code></td>
<td>Returns a string object from the string builder.</td>
</tr>
<tr>
<td><code>capacity()</code></td>
<td>Returns the capacity of this string builder.</td>
</tr>
<tr>
<td><code>charAt(index)</code></td>
<td>Returns the character at the specified index.</td>
</tr>
<tr>
<td><code>length()</code></td>
<td>Returns the number of characters in this builder.</td>
</tr>
<tr>
<td><code>setLength(newLength)</code></td>
<td>Sets a new length in this builder.</td>
</tr>
<tr>
<td><code>substring(startIndex)</code></td>
<td>Returns a substring starting at <code>startIndex</code>.</td>
</tr>
<tr>
<td><code>substring(startIndex, endIndex)</code></td>
<td>Returns a substring from <code>startIndex</code> to <code>endIndex-1</code>.</td>
</tr>
<tr>
<td><code>trimToSize()</code></td>
<td>Reduces the storage size used for the string builder.</td>
</tr>
</tbody>
</table>

**Note**

The **length** and **capacity** are always less than or equal to the capacity of the builder. The **length** is the actual size of the string stored in the builder, and the capacity is the current size of the builder. The builder’s capacity is automatically increased if more characters are added to exceed its capacity. Internally, a string builder is an array of characters, so the builder’s capacity is the size of the array. If the builder’s capacity is exceeded, the array is replaced by a new array. The new array size is $2 \times \text{(the previous array size} + 1)$. 

**Tip**

You can use `new StringBuilder(initialCapacity)` to create a **StringBuilder** with a specified initial capacity. By carefully choosing the initial capacity, you can make your program more efficient. If the capacity is always larger than the actual length of the builder, the JVM will never need to reallocate memory for the builder. On the other hand, if the capacity is too large, you will waste memory space. You can use the `trimToSize()` method to reduce the capacity to the actual size.
10.11.3 Case Study: Ignoring Nonalphanumeric Characters When Checking Palindromes

Listing 5.14, Palindrome.java, considered all the characters in a string to check whether it is a palindrome. Write a new program that ignores nonalphanumeric characters in checking whether a string is a palindrome.

Here are the steps to solve the problem:

1. Filter the string by removing the nonalphanumeric characters. This can be done by creating an empty string builder, adding each alphanumeric character in the string to a string builder, and returning the string from the string builder. You can use the `isLetterOrDigit(ch)` method in the `Character` class to check whether character `ch` is a letter or a digit.

2. Obtain a new string that is the reversal of the filtered string. Compare the reversed string with the filtered string using the `equals` method.

The complete program is shown in Listing 10.10.

**LISTING 10.10 PalindromeIgnoreNonAlphanumeric.java**

```java
import java.util.Scanner;

public class PalindromeIgnoreNonAlphanumeric {
    /** Main method */
    public static void main(String[] args) {
        // Create a Scanner
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter a string
        System.out.print("Enter a string: ");
        String s = input.nextLine();

        // Display result
        System.out.println("Ignoring nonalphanumeric characters, \nis " + s + " a palindrome? " + isPalindrome(s));
    }

    /** Return true if a string is a palindrome */
    public static boolean isPalindrome(String s) {
        // Create a new string by eliminating nonalphanumeric chars
        String s1 = filter(s);

        // Create a new string that is the reversal of s1
        String s2 = reverse(s1);

        // Check if the reversal is the same as the original string
        return s2.equals(s1);
    }

    /** Create a new string by eliminating nonalphanumeric chars */
    public static String filter(String s) {
        // Create a string builder
        StringBuilder stringBuilder = new StringBuilder(); 

        // Examine each char in the string to skip alphanumeric char
        for (int i = 0; i < s.length(); i++) {
            if (Character.isLetterOrDigit(s.charAt(i))) {
                stringBuilder.append(s.charAt(i));
            }
        }
        return stringBuilder.toString();
    }
}
```
// Return a new filtered string
        return stringBuilder.toString();
      }
      
      /** Create a new string by reversing a specified string */
      public static String reverse(String s) {
        StringBuilder stringBuilder = new StringBuilder(s);
        stringBuilder.reverse(); // Invoke reverse in StringBuilder
        return stringBuilder.toString();
      }
    }
  }

Enter a string: ab<c>cb?a
Ignoring nonalphanumeric characters,
is ab<c>cb?a a palindrome? true

Enter a string: abcc><?cab
Ignoring nonalphanumeric characters,
is abcc><?cab a palindrome? false

The filter(String s) method (lines 31–44) examines each character in string s and copies it to a string builder if the character is a letter or a numeric character. The filter method returns the string in the builder. The reverse(String s) method (lines 47–51) creates a new string that reverses the specified string s. The filter and reverse methods both return a new string. The original string is not changed.

The program in Listing 5.14 checks whether a string is a palindrome by comparing pairs of characters from both ends of the string. Listing 10.10 uses the reverse method in the StringBuilder class to reverse the string, then compares whether the two strings are equal to determine whether the original string is a palindrome.

10.26 What is the difference between StringBuilder and StringBuffer?
10.27 How do you create a string builder from a string? How do you return a string from a string builder?
10.28 Write three statements to reverse a string s using the reverse method in the StringBuilder class.
10.29 Write three statements to delete a substring from a string s of 20 characters, starting at index 4 and ending with index 10. Use the delete method in the StringBuilder class.
10.30 What is the internal storage for characters in a string and a string builder?
10.31 Suppose that s1 and s2 are given as follows:

StringBuilder s1 = new StringBuilder("Java");
StringBuilder s2 = new StringBuilder("HTML");

Show the value of s1 after each of the following statements. Assume that the statements are independent.

a. s1.append(" is fun");
b. s1.append(s2);
c. `s1.insert(2, "is fun");`
d. `s1.insert(1, s2);`
e. `s1.charAt(2);`
f. `s1.length();`
g. `s1.deleteCharAt(3);`
h. `s1.delete(1, 3);`
i. `s1.reverse();`
j. `s1.replace(1, 3, "Computer");`
k. `s1.substring(1, 3);`
l. `s1.substring(2);`

10.32 Show the output of the following program:

```java
public class Test {
    public static void main(String[] args) {
        String s = "Java";
        StringBuilder builder = new StringBuilder(s);
        change(s, builder);

        System.out.println(s);
        System.out.println(builder);
    }

    private static void change(String s, StringBuilder builder) {
        s = s + " and HTML";
        builder.append(" and HTML");
    }
}
```

**Key Terms**

- abstract data type (ADT) 366
- aggregation 374
- boxing 383
- class abstraction 366
- class encapsulation 366
- class’s contract 366
- composition 374
- has-a relationship 374
- multiplicity 373
- stack 378
- unboxing 383

**Chapter Summary**

1. The procedural paradigm focuses on designing methods. The object-oriented paradigm couples data and methods together into objects. Software design using the object-oriented paradigm focuses on objects and operations on objects. The object-oriented approach combines the power of the procedural paradigm with an added dimension that integrates data with operations into objects.

2. Many Java methods require the use of objects as arguments. Java offers a convenient way to incorporate, or wrap, a primitive data type into an object (e.g., wrapping `int` into the `Integer` class, and wrapping `double` into the `Double` class).
3. Java can automatically convert a primitive type value to its corresponding wrapper object in the context and vice versa.

4. The `BigInteger` class is useful for computing and processing integers of any size. The `BigDecimal` class can be used to compute and process floating-point numbers with any arbitrary precision.

5. A `String` object is immutable; its contents cannot be changed. To improve efficiency and save memory, the JVM stores two literal strings that have the same character sequence in a unique object. This unique object is called an interned string object.

6. A regular expression (abbreviated regex) is a string that describes a pattern for matching a set of strings. You can match, replace, or split a string by specifying a pattern.

7. The `StringBuilder` and `StringBuffer` classes can be used to replace the `String` class. The `String` object is immutable, but you can add, insert, or append new contents into `StringBuilder` and `StringBuffer` objects. Use `String` if the string contents do not require any change, and use `StringBuilder` or `StringBuffer` if they might change.

**Quiz**

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

**Programming Exercises**

Sections 10.2–10.3

*10.1* (The `Time` class) Design a class named `Time`. The class contains:

- The data fields `hour`, `minute`, and `second` that represent a time.
- A no-arg constructor that creates a `Time` object for the current time. (The values of the data fields will represent the current time.)
- A constructor that constructs a `Time` object with a specified elapsed time since midnight, January 1, 1970, in milliseconds. (The values of the data fields will represent this time.)
- A constructor that constructs a `Time` object with the specified hour, minute, and second.
- Three getter methods for the data fields `hour`, `minute`, and `second`, respectively.
- A method named `setTime(long elapsedTime)` that sets a new time for the object using the elapsed time. For example, if the elapsed time is 555550000 milliseconds, the hour is 10, the minute is 19, and the second is 10.

Draw the UML diagram for the class and then implement the class. Write a test program that creates two `Time` objects (using `new Time()` and `new Time(555550000)`) and displays their hour, minute, and second in the format `hour:minute:second`. 

*(Hint: The first two constructors will extract the hour, minute, and second from the elapsed time. For the no-arg constructor, the current time can be obtained using `System.currentTimeMillis()`, as shown in Listing 2.7, ShowCurrentTime.java.)*
10.2 \((\text{The BMI class})\) Add the following new constructor in the \textbf{BMI} class:

```java
/** Construct a BMI with the specified name, age, weight, * feet, and inches */
public BMI(String name, int age, double weight, double feet, double inches)
```

10.3 \((\text{The MyInteger class})\) Design a class named \textbf{MyInteger}. The class contains:

- An \texttt{int} data field named \texttt{value} that stores the \texttt{int} value represented by this object.
- A constructor that creates a \texttt{MyInteger} object for the specified \texttt{int} value.
- A getter method that returns the \texttt{int} value.
- The methods \texttt{isEven()}, \texttt{isOdd()}, and \texttt{isPrime()} that return \texttt{true} if the value in this object is even, odd, or prime, respectively.
- The static methods \texttt{isEven(int)}, \texttt{isOdd(int)}, and \texttt{isPrime(int)} that return \texttt{true} if the specified value is even, odd, or prime, respectively.
- The static methods \texttt{isEven(MyInteger)}, \texttt{isOdd(MyInteger)}, and \texttt{isPrime(MyInteger)} that return \texttt{true} if the specified value is even, odd, or prime, respectively.
- The methods \texttt{equals(int)} and \texttt{equals(MyInteger)} that return \texttt{true} if the value in this object is equal to the specified value.
- A static method \texttt{parseInt(char[])} that converts an array of numeric characters to an \texttt{int} value.
- A static method \texttt{parseInt(String)} that converts a string into an \texttt{int} value.

Draw the UML diagram for the class and then implement the class. Write a client program that tests all methods in the class.

10.4 \((\text{The MyPoint class})\) Design a class named \textbf{MyPoint} to represent a point with \(x\)- and \(y\)-coordinates. The class contains:

- The data fields \(x\) and \(y\) that represent the coordinates with getter methods.
- A no-arg constructor that creates a point \((0, 0)\).
- A constructor that constructs a point with specified coordinates.
- A method named \texttt{distance} that returns the distance from this point to a specified point of the \texttt{MyPoint} type.
- A method named \texttt{distance} that returns the distance from this point to another point with specified \(x\)- and \(y\)-coordinates.

Draw the UML diagram for the class and then implement the class. Write a test program that creates the two points \((0, 0)\) and \((10, 30.5)\) and displays the distance between them.

Sections 10.4–10.8

*10.5 \((\text{Displaying the prime factors})\) Write a program that prompts the user to enter a positive integer and displays all its smallest factors in decreasing order. For example, if the integer is 120, the smallest factors are displayed as 5, 3, 2, 2, 2. Use the \texttt{StackOfIntegers} class to store the factors (e.g., 2, 2, 2, 3, 5) and retrieve and display them in reverse order.

*10.6 \((\text{Displaying the prime numbers})\) Write a program that displays all the prime numbers less than 120 in decreasing order. Use the \texttt{StackOfIntegers} class to store the prime numbers (e.g., 2, 3, 5, \ldots) and retrieve and display them in reverse order.
**10.7 (Game: ATM machine)** Use the **Account** class created in Programming Exercise 9.7 to simulate an ATM machine. Create ten accounts in an array with id 0, 1, ..., 9, and initial balance $100. The system prompts the user to enter an id. If the id is entered incorrectly, ask the user to enter a correct id. Once an id is accepted, the main menu is displayed as shown in the sample run. You can enter a choice 1 for viewing the current balance, 2 for withdrawing money, 3 for depositing money, and 4 for exiting the main menu. Once you exit, the system will prompt for an id again. Thus, once the system starts, it will not stop.

```
Enter an id: 4
Main menu
1: check balance
2: withdraw
3: deposit
4: exit
Enter a choice: 1
The balance is 100.0

Main menu
1: check balance
2: withdraw
3: deposit
4: exit
Enter a choice: 2
Enter an amount to withdraw: 3
Main menu
1: check balance
2: withdraw
3: deposit
4: exit
Enter a choice: 1
The balance is 97.0

Main menu
1: check balance
2: withdraw
3: deposit
4: exit
Enter a choice: 3
Enter an amount to deposit: 10
Main menu
1: check balance
2: withdraw
3: deposit
4: exit
Enter a choice: 1
The balance is 107.0

Main menu
1: check balance
2: withdraw
3: deposit
4: exit
Enter a choice: 4
Enter an id:
```
Financial: the Tax class) Programming Exercise 8.12 writes a program for computing taxes using arrays. Design a class named Tax to contain the following instance data fields:

- **int filingStatus**: One of the four tax-filing statuses: 0—single filer, 1—married filing jointly or qualifying widow(er), 2—married filing separately, and 3—head of household. Use the public static constants `SINGLE_FILER` (0), `MARRIED_JOINTLY_OR_QUALIFYING_WIDOW(ER)` (1), `MARRIED_SEPARATELY` (2), `HEAD_OF_HOUSEHOLD` (3) to represent the statuses.
- **int[][] brackets**: Stores the tax brackets for each filing status.
- **double[] rates**: Stores the tax rates for each bracket.
- **double taxableIncome**: Stores the taxable income.

Provide the getter and setter methods for each data field and the `getTax()` method that returns the tax. Also provide a no-arg constructor and the constructor `Tax(filingStatus, brackets, rates, taxableIncome)`.

Draw the UML diagram for the class and then implement the class. Write a test program that uses the `Tax` class to print the 2001 and 2009 tax tables for taxable income from $50,000 to $60,000 with intervals of $1,000 for all four statuses. The tax rates for the year 2009 were given in Table 3.2. The tax rates for 2001 are shown in Table 10.1.

**10.9 (The Course class)** Revise the `Course` class as follows:

- The array size is fixed in Listing 10.6. Improve it to automatically increase the array size by creating a new larger array and copying the contents of the current array to it.
- Implement the `dropStudent` method.
- Add a new method named `clear()` that removes all students from the course.

Write a test program that creates a course, adds three students, removes one, and displays the students in the course.

**10.10 (The Queue class)** Section 10.6 gives a class for Stack. Design a class named `Queue` for storing integers. Like a stack, a queue holds elements. In a stack, the elements are retrieved in a last-in first-out fashion. In a queue, the elements are retrieved in a first-in first-out fashion. The class contains:

- An `int[][]` data field named `elements` that stores the `int` values in the queue.
- A data field named `size` that stores the number of elements in the queue.
- A constructor that creates a `Queue` object with default capacity 8.
- The method `enqueue(int v)` that adds `v` into the queue.

Table 10.1

<table>
<thead>
<tr>
<th>Tax rate</th>
<th>Single filers</th>
<th>Married filing jointly or qualifying widow(er)</th>
<th>Married filing separately</th>
<th>Head of household</th>
</tr>
</thead>
<tbody>
<tr>
<td>15%</td>
<td>Up to $27,050</td>
<td>Up to $45,200</td>
<td>Up to $22,600</td>
<td>Up to $36,250</td>
</tr>
<tr>
<td>27.5%</td>
<td>$27,051–$65,550</td>
<td>$45,201–$109,250</td>
<td>$22,601–$54,625</td>
<td>$36,251–$93,650</td>
</tr>
<tr>
<td>30.5%</td>
<td>$65,551–$136,750</td>
<td>$109,251–$166,500</td>
<td>$54,626–$83,250</td>
<td>$93,651–$151,650</td>
</tr>
<tr>
<td>39.1%</td>
<td>$297,351 or more</td>
<td>$297,351 or more</td>
<td>$148,676 or more</td>
<td>$297,351 or more</td>
</tr>
</tbody>
</table>
The method `dequeue()` that removes and returns the element from the queue.

The method `empty()` that returns true if the queue is empty.

The method `getSize()` that returns the size of the queue.

Draw an UML diagram for the class. Implement the class with the initial array size set to 8. The array size will be doubled once the number of the elements exceeds the size. After an element is removed from the beginning of the array, you need to shift all elements in the array one position the left. Write a test program that adds 20 numbers from 1 to 20 into the queue and removes these numbers and displays them.

*10.11* (Geometry: the `Circle2D` class) Define the `Circle2D` class that contains:

- Two `double` data fields named `x` and `y` that specify the center of the circle with getter methods.
- A data field `radius` with a getter method.
- A no-arg constructor that creates a default circle with `(0, 0)` for `(x, y)` and `1` for `radius`.
- A constructor that creates a circle with the specified `x, y`, and `radius`.
- A method `getArea()` that returns the area of the circle.
- A method `getPerimeter()` that returns the perimeter of the circle.
- A method `contains(double x, double y)` that returns `true` if the specified point `(x, y)` is inside this circle (see Figure 10.21a).
- A method `contains(Circle2D circle)` that returns `true` if the specified circle is inside this circle (see Figure 10.21b).
- A method `overlaps(Circle2D circle)` that returns `true` if the specified circle overlaps with this circle (see Figure 10.21c).

![Figure 10.21](a) A point is inside the circle. (b) A circle is inside another circle. (c) A circle overlaps another circle.

Draw the UML diagram for the class and then implement the class. Write a test program that creates a `Circle2D` object `c1 (new Circle2D(2, 2, 5.5))`, displays its area and perimeter, and displays the result of `c1.contains(3, 3)`, `c1.contains(new Circle2D(4, 5, 10.5))`, and `c1.overlaps(new Circle2D(3, 5, 2.3))`.

***10.12* (Geometry: the `Triangle2D` class) Define the `Triangle2D` class that contains:

- Three points named `p1`, `p2`, and `p3` of the type `MyPoint` with getter and setter methods. `MyPoint` is defined in Programming Exercise 10.4.
- A no-arg constructor that creates a default triangle with the points `(0, 0), (1, 1), and (2, 5)`.
- A constructor that creates a triangle with the specified points.
- A method `getArea()` that returns the area of the triangle.
- A method `getPerimeter()` that returns the perimeter of the triangle.
- A method `contains(MyPoint p)` that returns `true` if the specified point `p` is inside this triangle (see Figure 10.22a).
A method `contains(Triangle2D t)` that returns `true` if the specified triangle is inside this triangle (see Figure 10.22b).

A method `overlaps(Triangle2D t)` that returns `true` if the specified triangle overlaps with this triangle (see Figure 10.22c).

---

**Figure 10.22**  
(a) A point is inside the triangle. (b) A triangle is inside another triangle. (c) A triangle overlaps another triangle.

---

Draw the UML diagram for the class and then implement the class. Write a test program that creates a `Triangle2D` objects `t1` using the constructor `new Triangle2D(new MyPoint(2.5, 2), new MyPoint(4.2, 3), new MyPoint(5, 3.5))`, displays its area and perimeter, and displays the result of `t1.contains(3, 3)`, `r1.contains(new Triangle2D(new MyPoint(2.9, 2), new MyPoint(4, 1), MyPoint(1, 3.4))`, and `t1.overlaps(new Triangle2D(new MyPoint(2, 5.5), new MyPoint(4, -3), MyPoint(2, 6.5)))`.

*(Hint: For the formula to compute the area of a triangle, see Programming Exercise 2.19. To detect whether a point is inside a triangle, draw three dashed lines, as shown in Figure 10.23. If the point is inside a triangle, each dashed line should intersect a side only once. If a dashed line intersects a side twice, then the point must be outside the triangle. For the algorithm of finding the intersecting point of two lines, see Programming Exercise 3.25.)*

---

**Figure 10.23**  
(a) A point is inside the triangle. (b) A point is outside the triangle.

---

*10.13 (Geometry: the MyRectangle2D class)* Define the `MyRectangle2D` class that contains:

- Two `double` data fields named `x` and `y` that specify the center of the rectangle with getter and setter methods. (Assume that the rectangle sides are parallel to x- or y- axes.)
- The data fields `width` and `height` with getter and setter methods.
- A no-arg constructor that creates a default rectangle with `(0, 0)` for `(x, y)` and `1` for both `width` and `height`.
- A constructor that creates a rectangle with the specified `x`, `y`, `width`, and `height`.  

A method `getArea()` that returns the area of the rectangle.

A method `getPerimeter()` that returns the perimeter of the rectangle.

A method `contains(double x, double y)` that returns `true` if the specified point `(x, y)` is inside this rectangle (see Figure 10.24a).

A method `contains(MyRectangle2D r)` that returns `true` if the specified rectangle is inside this rectangle (see Figure 10.24b).

A method `overlaps(MyRectangle2D r)` that returns `true` if the specified rectangle overlaps with this rectangle (see Figure 10.24c).

**Figure 10.24** A point is inside the rectangle. (b) A rectangle is inside another rectangle. (c) A rectangle overlaps another rectangle. (d) Points are enclosed inside a rectangle.

Draw the UML diagram for the class and then implement the class. Write a test program that creates a `MyRectangle2D` object `r1` (new `MyRectangle2D(2, 2, 5.5, 4.9)`), displays its area and perimeter, and displays the result of `r1.contains(3, 3), r1.contains(new MyRectangle2D(4, 5, 10.5, 3.2)),` and `r1.overlaps(new MyRectangle2D(3, 5, 2.3, 5.4)).`

**10.14** (The MyDate class) Design a class named `MyDate`. The class contains:

- The data fields `year`, `month`, and `day` that represent a date. `month` is 0-based, i.e., 0 is for January.
- A no-arg constructor that creates a `MyDate` object for the current date.
- A constructor that constructs a `MyDate` object with a specified elapsed time since midnight, January 1, 1970, in milliseconds.
- A constructor that constructs a `MyDate` object with the specified year, month, and day.
- Three getter methods for the data fields `year`, `month`, and `day`, respectively.
- A method named `setDate(long elapsedTime)` that sets a new date for the object using the elapsed time.

Draw the UML diagram for the class and then implement the class. Write a test program that creates two `MyDate` objects (using `new MyDate()` and `new MyDate(34355555133101L)`) and displays their year, month, and day.

(Hint: The first two constructors will extract the year, month, and day from the elapsed time. For example, if the elapsed time is 56155550000 milliseconds, the year is 1987, the month is 9, and the day is 18. You may use the `GregorianCalendar` class discussed in Programming Exercise 9.5 to simplify coding.)

**10.15** (Geometry: the bounding rectangle) A bounding rectangle is the minimum rectangle that encloses a set of points in a two-dimensional plane, as shown in Figure 10.24d. Write a method that returns a bounding rectangle for a set of points in a two-dimensional plane, as follows:

```java
public static MyRectangle2D getRectangle(double[][] points)
```
The `Rectangle2D` class is defined in Programming Exercise 10.13. Write a test program that prompts the user to enter five points and displays the bounding rectangle’s center, width, and height. Here is a sample run:

```
Enter five points: 1.0 2.5 3 4 5 6 7 8 9 10
The bounding rectangle's center (5.0, 6.25), width 8.0, height 7.5
```

**Section 10.9**

*10.16 (Divisible by 2 or 3) Find the first ten numbers with 50 decimal digits that are divisible by 2 or 3.

*10.17 (Square numbers) Find the first ten square numbers that are greater than `Long.MAX_VALUE`. A square number is a number in the form of \( n^2 \). For example, 4, 9, and 16 are square numbers. Find an efficient approach to run your program fast.

*10.18 (Large prime numbers) Write a program that finds five prime numbers larger than `Long.MAX_VALUE`.

*10.19 (Mersenne prime) A prime number is called a Mersenne prime if it can be written in the form \( 2^p - 1 \) for some positive integer \( p \). Write a program that finds all Mersenne primes with \( p \leq 100 \) and displays the output as shown below. (Hint: You have to use `BigInteger` to store the number, because it is too big to be stored in `long`. Your program may take several hours to run.)

<table>
<thead>
<tr>
<th>( p )</th>
<th>( 2^p - 1 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>3</td>
<td>7</td>
</tr>
<tr>
<td>5</td>
<td>31</td>
</tr>
<tr>
<td>...</td>
<td></td>
</tr>
</tbody>
</table>

*10.20 (Approximate e) Programming Exercise 5.26 approximates \( e \) using the following series:

\[
e = 1 + \frac{1}{1!} + \frac{1}{2!} + \frac{1}{3!} + \frac{1}{4!} + \ldots + \frac{1}{i!}
\]

In order to get better precision, use `BigDecimal` with 25 digits of precision in the computation. Write a program that displays the \( e \) value for \( i = 100, 200, \ldots, 1000 \).

*10.21 (Divisible by 5 or 6) Find the first ten numbers greater than `Long.MAX_VALUE` that are divisible by 5 or 6.

**Sections 10.10–10.11**

**10.22 (Implement the String class)** The `String` class is provided in the Java library. Provide your own implementation for the following methods (name the new class `MyString1`):

```java
public MyString1(char[] chars);
public char charAt(int index);
public int length();
public MyString1 substring(int begin, int end);
public MyString1 toLowerCase();
public boolean equals(MyString1 s);
public static MyString1 valueOf(int i);
```
**10.23** (Implement the `String` class) The `String` class is provided in the Java library. Provide your own implementation for the following methods (name the new class `MyString2`):

```java
public MyString2(String s);
public int compare(String s);
public MyString2 substring(int begin);
public MyString2 toUpperCase();
public char[] toChars();
public static MyString2 valueOf(boolean b);
```

**10.24** (Implement the `Character` class) The `Character` class is provided in the Java library. Provide your own implementation for this class. Name the new class `MyCharacter`.

**10.25** (New string `split` method) The `split` method in the `String` class returns an array of strings consisting of the substrings split by the delimiters. However, the delimiters are not returned. Implement the following new method that returns an array of strings consisting of the substrings split by the matching delimiters, including the matching delimiters.

```java
public static String[] split(String s, String regex)
```

For example, `split("ab#12#453", ",#\")` returns `ab`, `#`, `12`, `#`, `453` in an array of `String`, and `split("a?b?gf#e", ",[?#]\")` returns `a`, `b`, `?`, `b`, `gf`, `#`, and `e` in an array of `String`.

**10.26** (Calculator) Revise Listing 7.9, `Calculator.java`, to accept an expression as a string in which the operands and operator are separated by zero or more spaces. For example, `3+4` and `3 + 4` are acceptable expressions. Here is a sample run:

![Image of Command Prompt with Java program output]

**10.27** (Implement the `StringBuilder` class) The `StringBuilder` class is provided in the Java library. Provide your own implementation for the following methods (name the new class `MyStringBuilder1`):

```java
public MyStringBuilder1(String s);
public MyStringBuilder1 append(MyStringBuilder1 s);
public MyStringBuilder1 append(int i);
public int length();
public char charAt(int index);
public MyStringBuilder1 toLowerCase();
public MyStringBuilder1 toLowerCase();
public MyStringBuilder1 substring(int begin, int end);
public String toString();
```
**10.28** (Implement the `StringBuilder` class) The `StringBuilder` class is provided in the Java library. Provide your own implementation for the following methods (name the new class `MyStringBuilder2`):

```java
public MyStringBuilder2();
public MyStringBuilder2(char[] chars);
public MyStringBuilder2(String s);
public MyStringBuilder2 insert(int offset, MyStringBuilder2 s);
public MyStringBuilder2 reverse();
public MyStringBuilder2 substring(int begin);
public MyStringBuilder2 toUpperCase();
```
INHERITANCE AND POLYMORPHISM

Objectives

■ To define a subclass from a superclass through inheritance (§11.2).
■ To invoke the superclass’s constructors and methods using the super keyword (§11.3).
■ To override instance methods in the subclass (§11.4).
■ To distinguish differences between overriding and overloading (§11.5).
■ To explore the toString() method in the Object class (§11.6).
■ To discover polymorphism and dynamic binding (§§11.7–11.8).
■ To describe casting and explain why explicit downcasting is necessary (§11.9).
■ To explore the equals method in the Object class (§11.10).
■ To store, retrieve, and manipulate objects in an ArrayList (§11.11).
■ To construct an array list from an array, to sort and shuffle a list, and to obtain max and min element from a list (§11.12).
■ To implement a Stack class using ArrayList (§11.13).
■ To enable data and methods in a superclass accessible from subclasses using the protected visibility modifier (§11.14).
■ To prevent class extending and method overriding using the final modifier (§11.15).
11.1 Introduction

Object-oriented programming allows you to define new classes from existing classes. This is called inheritance.

As discussed earlier in the book, the procedural paradigm focuses on designing methods and the object-oriented paradigm couples data and methods together into objects. Software design using the object-oriented paradigm focuses on objects and operations on objects. The object-oriented approach combines the power of the procedural paradigm with an added dimension that integrates data with operations into objects.

Inheritance is an important and powerful feature for reusing software. Suppose you need to define classes to model circles, rectangles, and triangles. These classes have many common features. What is the best way to design these classes so as to avoid redundancy and make the system easy to comprehend and easy to maintain? The answer is to use inheritance.

11.2 Superclasses and Subclasses

Inheritance enables you to define a general class (i.e., a superclass) and later extend it to more specialized classes (i.e., subclasses).

You use a class to model objects of the same type. Different classes may have some common properties and behaviors, which can be generalized in a class that can be shared by other classes. You can define a specialized class that extends the generalized class. The specialized classes inherit the properties and methods from the general class.

Consider geometric objects. Suppose you want to design the classes to model geometric objects such as circles and rectangles. Geometric objects have many common properties and behaviors. They can be drawn in a certain color and be filled or unfilled. Thus a general class GeometricObject can be used to model all geometric objects. This class contains the properties color and filled and their appropriate getter and setter methods. Assume that this class also contains the dateCreated property and the getDateCreated() and toString() methods. The toString() method returns a string representation of the object. Since a circle is a special type of geometric object, it shares common properties and methods with other geometric objects. Thus it makes sense to define the Circle class that extends the GeometricObject class. Likewise, Rectangle can also be defined as a subclass of GeometricObject. Figure 11.1 shows the relationship among these classes. A triangular arrow pointing to the superclass is used to denote the inheritance relationship between the two classes involved.

In Java terminology, a class C1 extended from another class C2 is called a subclass, and C2 is called a superclass. A subclass is also referred to as a parent class or a base class, and a subclass as a child class, an extended class, or a derived class. A subclass inherits accessible data fields and methods from its superclass and may also add new data fields and methods.

The Circle class inherits all accessible data fields and methods from the GeometricObject class. In addition, it has a new data field, radius, and its associated getter and setter methods. The Circle class also contains the getArea(), getPerimeter(), and getDiameter() methods for returning the area, perimeter, and diameter of the circle.

The Rectangle class inherits all accessible data fields and methods from the GeometricObject class. In addition, it has the data fields width and height and their associated getter and setter methods. It also contains the getArea() and getPerimeter() methods for returning the area and perimeter of the rectangle.

The GeometricObject, Circle, and Rectangle classes are shown in Listings 11.1, 11.2, and 11.3.

Note
To avoid a naming conflict with the improved GeometricObject, Circle, and Rectangle classes introduced in Chapter 13, we'll name these classes.
11.2 Superclasses and Subclasses

SimpleGeometricObject, CircleFromSimpleGeometricObject, and RectangleFromSimpleGeometricObject in this chapter. For simplicity, we will still refer to them in the text as GeometricObject, Circle, and Rectangle classes. The best way to avoid naming conflicts is to place these classes in different packages. However, for simplicity and consistency, all classes in this book are placed in the default package.

Listing 11.1  SimpleGeometricObject.java

```java
public class SimpleGeometricObject {
    private String color = "white";
    private boolean filled;
    private java.util.Date dateCreated;

    /** Construct a default geometric object */
    public SimpleGeometricObject() {
        dateCreated = new java.util.Date();
    }
}
```
/** Construct a geometric object with the specified color and filled value */
public SimpleGeometricObject(String color, boolean filled) {
    dateCreated = new java.util.Date();
    this.color = color;
    this.filled = filled;
}

/** Return color */
public String getColor() {
    return color;
}

/** Set a new color */
public void setColor(String color) {
    this.color = color;
}

/** Return filled. Since filled is boolean, its getter method is named isFilled */
public boolean isFilled() {
    return filled;
}

/** Set a new filled */
public void setFilled(boolean filled) {
    this.filled = filled;
}

/** Get dateCreated */
public java.util.Date getDateCreated() {
    return dateCreated;
}

/** Return a string representation of this object */
public String toString() {
    return "created on " + dateCreated + "color: " + color + " and filled: " + filled;
}

public class CircleFromSimpleGeometricObject extends SimpleGeometricObject {
    private double radius;

    public CircleFromSimpleGeometricObject() {
    }

    public CircleFromSimpleGeometricObject(double radius) {
        this.radius = radius;
    }

    public CircleFromSimpleGeometricObject(double radius, String color, boolean filled) {
        this.radius = radius;
        setColor(color);
        setFilled(filled);
    }
The `Circle` class (Listing 11.2) extends the `GeometricObject` class (Listing 11.1) using the following syntax:

```
public class Circle extends GeometricObject
```

The keyword `extends` (lines 1–2) tells the compiler that the `Circle` class extends the `GeometricObject` class, thus inheriting the methods `getColor`, `setColor`, `isFilled`, `setFilled`, and `toString`.

The overloaded constructor `Circle(double radius, String color, boolean filled)` is implemented by invoking the `setColor` and `setFilled` methods to set the `color` and `filled` properties (lines 12–17). These two public methods are defined in the superclass `GeometricObject` and are inherited in `Circle`, so they can be used in the `Circle` class.

You might attempt to use the data fields `color` and `filled` directly in the constructor as follows:

```
public CircleFromSimpleGeometricObject(
    double radius, String color, boolean filled) {
    this.radius = radius;
    this.color = color; // Illegal
    this.filled = filled; // Illegal
}
```
This is wrong, because the private data fields \texttt{color} and \texttt{filled} in the \texttt{GeometricObject} class cannot be accessed in any class other than in the \texttt{GeometricObject} class itself. The only way to read and modify \texttt{color} and \texttt{filled} is through their getter and setter methods.

The \texttt{Rectangle} class (Listing 11.3) extends the \texttt{GeometricObject} class (Listing 11.1) using the following syntax:

```
public class Rectangle extends GeometricObject
```

The keyword \texttt{extends} (lines 1–2) tells the compiler that the \texttt{Rectangle} class extends the \texttt{GeometricObject} class, thus inheriting the methods \texttt{getColor}, \texttt{setColor}, \texttt{isFilled}, \texttt{setFilled}, and \texttt{toString}.

**LISTING 11.3 RectangleFromSimpleGeometricObject.java**

```
1 public class RectangleFromSimpleGeometricObject
2     extends SimpleGeometricObject {
3     private double width;
4     private double height;
5
6     public RectangleFromSimpleGeometricObject() {
7         }
8
9     public RectangleFromSimpleGeometricObject(
10        double width, double height) {
11         this.width = width;
12         this.height = height;
13     }
14
15     public RectangleFromSimpleGeometricObject(
16        double width, double height, String color, boolean filled) {
17         this.width = width;
18         this.height = height;
19         setColor(color);
20         setFilled(filled);
21     }
22
23     /** Return width */
24     public double getWidth() {
25         return width;
26     }
27
28     /** Set a new width */
29     public void setWidth(double width) {
30         this.width = width;
31     }
32
33     /** Return height */
34     public double getHeight() {
35         return height;
36     }
37
38     /** Set a new height */
39     public void setHeight(double height) {
40         this.height = height;
41     }
```
/** Return area */
public double getArea() {
    return width * height;
}

/** Return perimeter */
public double getPerimeter() {
    return 2 * (width + height);
}

The code in Listing 11.4 creates objects of Circle and Rectangle and invokes the methods on these objects. The toString() method is inherited from the GeometricObject class and is invoked from a Circle object (line 5) and a Rectangle object (line 13).

LISTING 11.4 TestCircleRectangle.java

A circle created on Thu Feb 10 19:54:25 EST 2011
color: white and filled: false
The color is white
The radius is 1.0
The area is 3.141592653589793
The diameter is 2.0

A rectangle created on Thu Feb 10 19:54:25 EST 2011
color: white and filled: false
The area is 8.0
The perimeter is 12.0

Note the following points regarding inheritance:

- Contrary to the conventional interpretation, a subclass is not a subset of its superclass. In fact, a subclass usually contains more information and methods than its superclass.
- Private data fields in a superclass are not accessible outside the class. Therefore, they cannot be used directly in a subclass. They can, however, be accessed/mutated through public accessors/mutators if defined in the superclass.
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Not all is-a relationships should be modeled using inheritance. For example, a square is a rectangle, but you should not extend a Square class from a Rectangle class, because the width and height properties are not appropriate for a square. Instead, you should define a Square class to extend the GeometricObject class and define the side property for the side of a square.

Inheritance is used to model the is-a relationship. Do not blindly extend a class just for the sake of reusing methods. For example, it makes no sense for a Tree class to extend a Person class, even though they share common properties such as height and weight. A subclass and its superclass must have the is-a relationship.

Some programming languages allow you to derive a subclass from several classes. This capability is known as multiple inheritance. Java, however, does not allow multiple inheritance. A Java class may inherit directly from only one superclass. This restriction is known as single inheritance. If you use the extends keyword to define a subclass, it allows only one parent class. Nevertheless, multiple inheritance can be achieved through interfaces, which will be introduced in Section 13.4.

11.1 True or false? A subclass is a subset of a superclass.
11.2 What keyword do you use to define a subclass?
11.3 What is single inheritance? What is multiple inheritance? Does Java support multiple inheritance?

11.3 Using the super Keyword

The keyword super refers to the superclass and can be used to invoke the superclass’s methods and constructors.

A subclass inherits accessible data fields and methods from its superclass. Does it inherit constructors? Can the superclass’s constructors be invoked from a subclass? This section addresses these questions and their ramifications.

Section 9.14, The this Reference, introduced the use of the keyword this to reference the calling object. The keyword super refers to the superclass of the class in which super appears. It can be used in two ways:

To call a superclass constructor.
To call a superclass method.

11.3.1 Calling Superclass Constructors

A constructor is used to construct an instance of a class. Unlike properties and methods, the constructors of a superclass are not inherited by a subclass. They can only be invoked from the constructors of the subclasses using the keyword super.

The syntax to call a superclass’s constructor is:
super(), or super(parameters);

The statement super() invokes the no-arg constructor of its superclass, and the statement super(arguments) invokes the superclass constructor that matches the arguments. The statement super() or super(arguments) must be the first statement of the subclass’s constructor; this is the only way to explicitly invoke a superclass constructor. For example, the constructor in lines 12–17 in Listing 11.2 can be replaced by the following code:

```java
public CircleFromSimpleGeometricObject(
    double radius, String color, boolean filled) {
```
11.3 Using the `super` Keyword

```java
super(color, filled);
this.radius = radius;
```

**Caution**

You must use the keyword `super` to call the superclass constructor, and the call must be the first statement in the constructor. Invoking a superclass constructor's name in a subclass causes a syntax error.

### 11.3.2 Constructor Chaining

A constructor may invoke an overloaded constructor or its superclass constructor. If neither is invoked explicitly, the compiler automatically puts `super()` as the first statement in the constructor. For example:

```java
public ClassName() {
    // some statements
}                  // some statements
public ClassName() {
    super();
    // some statements
}
public ClassName(double d) {
    // some statements
}              // some statements
public ClassName(double d) {
    super();
    // some statements
}
```

In any case, constructing an instance of a class invokes the constructors of all the superclasses along the inheritance chain. When constructing an object of a subclass, the subclass constructor first invokes its superclass constructor before performing its own tasks. If the superclass is derived from another class, the superclass constructor invokes its parent-class constructor before performing its own tasks. This process continues until the last constructor along the inheritance hierarchy is called. This is called **constructor chaining**.

Consider the following code:

```java
1 public class Faculty extends Employee {
2     public static void main(String[] args) {
3         new Faculty();
4     }
5     
6     public Faculty() {
7         System.out.println("(4) Performs Faculty's tasks");
8     }
9 }
10 
11 class Employee extends Person {
12     public Employee() {
13         this("(2) Invoke Employee's overloaded constructor");
14         System.out.println("(3) Performs Employee's tasks ");
15     }
16     
17     public Employee(String s) {
18         System.out.println(s);
19     }
20 }
21 
22 class Person {
```
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```java
public Person() {
    System.out.println("(1) Performs Person's tasks");
}
```

The program produces the preceding output. Why? Let us discuss the reason. In line 3, `new Faculty()` invokes `Faculty`'s no-arg constructor. Since `Faculty` is a subclass of `Employee`, `Employee`'s no-arg constructor is invoked before any statements in `Faculty`'s constructor are executed. `Employee`'s no-arg constructor invokes `Employee`'s second constructor (line 13). Since `Employee` is a subclass of `Person`, `Person`'s no-arg constructor is invoked before any statements in `Employee`'s second constructor are executed. This process is illustrated in the following figure.

Caution

If a class is designed to be extended, it is better to provide a no-arg constructor to avoid programming errors. Consider the following code:

```java
public class Apple extends Fruit {
    
    class Fruit {
        public Fruit(String name) {
            System.out.println("Fruit's constructor is invoked");
        }
    }
}
```

Since no constructor is explicitly defined in `Apple`, `Apple`'s default no-arg constructor is defined implicitly. Since `Apple` is a subclass of `Fruit`, `Apple`'s default constructor automatically invokes `Fruit`'s no-arg constructor. However, `Fruit` does not have a no-arg constructor, because `Fruit` has an explicit constructor defined. Therefore, the program cannot be compiled.

Design Guide

If possible, you should provide a no-arg constructor for every class to make the class easy to extend and to avoid errors.

### 11.3.3 Calling Superclass Methods

The keyword `super` can also be used to reference a method other than the constructor in the superclass. The syntax is:

```java
super.method(parameters);
```
You could rewrite the `printCircle()` method in the `Circle` class as follows:

```java
class Circle {
    public void printCircle() {
        System.out.println("The circle is created "+
                           super.getDateCreated() + " and the radius is "+ radius);
    }
}
```

It is not necessary to put `super` before `getDateCreated()` in this case, however, because `getDateCreated()` is a method in the `GeometricObject` class and is inherited by the `Circle` class. Nevertheless, in some cases, as shown in the next section, the keyword `super` is needed.

### 11.4 What is the output of running the class C in (a)? What problem arises in compiling the program in (b)?

```java
11.5 How does a subclass invoke its superclass’s constructor?

11.6 True or false? When invoking a constructor from a subclass, its superclass’s no-arg constructor is always invoked.

### 11.4 Overriding Methods

*To override a method, the method must be defined in the subclass using the same signature and the same return type as in its superclass.*

A subclass inherits methods from a superclass. Sometimes it is necessary for the subclass to modify the implementation of a method defined in the superclass. This is referred to as **method overriding**.

The `toString` method in the `GeometricObject` class (lines 46–49 in Listing 11.1) returns the string representation of a geometric object. This method can be overridden to return the string representation of a circle. To override it, add the following new method in the `Circle` class in Listing 11.2.

```java
12.01 public class CircleFromSimpleGeometricObject
12.02     extends SimpleGeometricObject {
12.03     // Other methods are omitted
12.04
12.05     // Override the toString method defined in the superclass
12.06     public String toString() {
12.07         return super.toString() + "\nradius is "+ radius;
12.08     }
12.09 }
```
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The **toString()** method is defined in the **GeometricObject** class and modified in the **Circle** class. Both methods can be used in the **Circle** class. To invoke the **toString** method defined in the **GeometricObject** class from the **Circle** class, use `super.toString()` (line 7).

Can a subclass of **Circle** access the **toString** method defined in the **GeometricObject** class using syntax such as `super.super.toString()`? No. This is a syntax error.

Several points are worth noting:

- **An instance method can be overridden only if it is accessible.** Thus a private method cannot be overridden, because it is not accessible outside its own class. If a method defined in a subclass is private in its superclass, the two methods are completely unrelated.

- **Like an instance method, a static method can be inherited.** However, a static method cannot be overridden. If a static method defined in the superclass is redefined in a subclass, the method defined in the superclass is hidden. The hidden static methods can be invoked using the syntax `SuperClassName.staticMethodName`.

### Check Point

11.7 True or false? You can override a private method defined in a superclass.

11.8 True or false? You can override a static method defined in a superclass.

11.9 How do you explicitly invoke a superclass’s constructor from a subclass?

11.10 How do you invoke an overridden superclass method from a subclass?

### 11.5 Overriding vs. Overloading

**Overloading means to define multiple methods with the same name but different signatures. Overriding means to provide a new implementation for a method in the subclass.**

You learned about overloading methods in Section 6.8. To override a method, the method must be defined in the subclass using the same signature and the same return type.

Let us use an example to show the differences between overriding and overloading. In (a) below, the method `p(double i)` in class A overrides the same method defined in class B. In (b), however, the class A has two overloaded methods: `p(double i)` and `p(int i)`. The method `p(double i)` is inherited from B.

```java
public class Test {
    public static void main(String[] args) {
        A a = new A();
        a.p(10);
        a.p(10.0);
    }
}
class B {
    public void p(double i) {
        System.out.println(i * 2);
    }
}
class A extends B {
    // This method overrides the method in B
    public void p(double i) {
        System.out.println(i);
    }
}
```

(a)

```java
public class Test {
    public static void main(String[] args) {
        A a = new A();
        a.p(10);
        a.p(10.0);
    }
}
class B {
    public void p(double i) {
        System.out.println(i * 2);
    }
}
class A extends B {
    // This method overloads the method in B
    public void p(double i) {
        System.out.println(i);
    }
    public void p(int i) {
        System.out.println(i);
    }
}
```

(b)
When you run the `Test` class in (a), both `a.p(10)` and `a.p(10.0)` invoke the `p(double i)` method defined in class `A` to display `10.0`. When you run the `Test` class in (b), `a.p(10)` invokes the `p(int i)` method defined in class `A` to display `10`, and `a.p(10.0)` invokes the `p(double i)` method defined in class `B` to display `20.0`.

Note the following:

- Overridden methods are in different classes related by inheritance; overloaded methods can be either in the same class or different classes related by inheritance.
- Overridden methods have the same signature and return type; overloaded methods have the same name but a different parameter list.

To avoid mistakes, you can use a special Java syntax, called *override annotation*, to place `@Override` before the method in the subclass. For example:

```java
public class CircleFromSimpleGeometricObject extends SimpleGeometricObject {
    // Other methods are omitted

    @Override
    public String toString() {
        return super.toString() + "\nradius is " + radius;
    }
}
```

This annotation denotes that the annotated method is required to override a method in the superclass. If a method with this annotation does not override its superclass's method, the compiler will report an error. For example, if `toString` is mistyped as `tostring`, a compile error is reported. If the override annotation isn’t used, the compile won’t report an error. Using annotation avoids mistakes.

### 11.11 Identify the problems in the following code:

```java
public class Circle {
    private double radius;

    public Circle(double radius) {
        radius = radius;
    }

    public double getRadius() {
        return radius;
    }

    public double getArea() {
        return radius * radius * Math.PI;
    }
}

class B extends Circle {
    private double length;

    B(double radius, double length) {
        Circle(radius);
        length = length;
    }

    @Override
}
```
public double getArea() {
    return getArea() * length;
}

11.12 Explain the difference between method overloading and method overriding.

11.13 If a method in a subclass has the same signature as a method in its superclass with the same return type, is the method overridden or overloaded?

11.14 If a method in a subclass has the same signature as a method in its superclass with a different return type, will this be a problem?

11.15 If a method in a subclass has the same name as a method in its superclass with different parameter types, is the method overridden or overloaded?

11.16 What is the benefit of using the @Override annotation?

### 11.6 The Object Class and Its toString() Method

Every class in Java is descended from the java.lang.Object class.

If no inheritance is specified when a class is defined, the superclass of the class is Object by default. For example, the following two class definitions are the same:

| public class ClassName { | Equivalent | public class ClassName extends Object { |
| ... | ... |

Classes such as String, StringBuilder, Loan, and GeometricObject are implicitly subclasses of Object (as are all the main classes you have seen in this book so far). It is important to be familiar with the methods provided by the Object class so that you can use them in your classes. This section introduces the toString method in the Object class.

The signature of the toString() method is:

```java
public String toString()
```

Invoking toString() on an object returns a string that describes the object. By default, it returns a string consisting of a class name of which the object is an instance, an at sign (@), and the object’s memory address in hexadecimal. For example, consider the following code for the Loan class defined in Listing 10.2:

```java
Loan loan = new Loan();
System.out.println(loan.toString());
```

The output for this code displays something like Loan@15037e5. This message is not very helpful or informative. Usually you should override the toString method so that it returns a descriptive string representation of the object. For example, the toString method in the Object class was overridden in the GeometricObject class in lines 46–49 in Listing 11.1 as follows:

```java
public String toString() {
    return "created on " + dateCreated + "\ncolor: " + color + " and filled: " + filled;
}
```
11.7 Polymorphism

Polymorphism means that a variable of a supertype can refer to a subtype object.

The three pillars of object-oriented programming are encapsulation, inheritance, and polymorphism. You have already learned the first two. This section introduces polymorphism.

First, let us define two useful terms: subtype and supertype. A class defines a type. A type defined by a subclass is called a subtype, and a type defined by its superclass is called a supertype. Therefore, you can say that Circle is a subtype of GeometricObject and GeometricObject is a supertype for Circle.

The inheritance relationship enables a subclass to inherit features from its superclass with additional new features. A subclass is a specialization of its superclass; every instance of a subclass is also an instance of its superclass, but not vice versa. For example, every circle is a geometric object, but not every geometric object is a circle. Therefore, you can always pass an instance of a subclass to a parameter of its superclass type. Consider the code in Listing 11.5.

Listing 11.5 PolymorphismDemo.java

```java
public class PolymorphismDemo {
  /** Main method */
  public static void main(String[] args) {
    // Display circle and rectangle properties
    displayObject(new CircleFromSimpleGeometricObject(1, "red", false));
    displayObject(new RectangleFromSimpleGeometricObject(1, 1, "black", true));
  }
  /** Display geometric object properties */
  public static void displayObject(SimpleGeometricObject object) {
    System.out.println("Created on "+ object.getDateCreated() + ". Color is " + object.getColor());
  }
}
```

Created on Mon Mar 09 19:25:20 EDT 2011. Color is red
Created on Mon Mar 09 19:25:20 EDT 2011. Color is black

The method displayObject (line 12) takes a parameter of the GeometricObject type. You can invoke displayObject by passing any instance of GeometricObject (e.g., new CircleFromSimpleGeometricObject(1, "red", false) and new RectangleFromSimpleGeometricObject(1, 1, "black", false) in lines 5–8). An object of a subclass can be used wherever its superclass object is used. This is commonly known as polymorphism (from a Greek word meaning “many forms”). In simple terms, polymorphism means that a variable of a supertype can refer to a subtype object.
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11.8 Dynamic Binding

A method can be implemented in several classes along the inheritance chain. The JVM decides which method is invoked at runtime.

A method can be defined in a superclass and overridden in its subclass. For example, the `toString()` method is defined in the `Object` class and overridden in `GeometricObject`.

Consider the following code:

```java
Object o = new GeometricObject();
System.out.println(o.toString());
```

Which `toString()` method is invoked by `o`? To answer this question, we first introduce two terms: declared type and actual type. A variable must be declared a type. The type that declares a variable is called the variable’s declared type. Here `o`’s declared type is `Object`. A variable of a reference type can hold a `null` value or a reference to an instance of the declared type. The instance may be created using the constructor of the declared type or its subtype. The actual type of the variable is the actual class for the object referenced by the variable. Here `o`’s actual type is `GeometricObject`, because `o` references an object created using `new GeometricObject()`. Which `toString()` method is invoked by `o` is determined by `o`’s actual type. This is known as dynamic binding.

Dynamic binding works as follows: Suppose an object `o` is an instance of classes `C1`, `C2`, …, `Cn-1`, and `Cn`, where `C1` is a subclass of `C2`, `C2` is a subclass of `C3`, …, and `Cn-1` is a subclass of `Cn`, as shown in Figure 11.2. That is, `Cn` is the most general class, and `C1` is the most specific class. In Java, `Cn` is the `Object` class. If `o` invokes a method `p`, the JVM searches for the implementation of the method `p` in `C1`, `C2`, …, `Cn-1`, and `Cn`, in this order, until it is found. Once an implementation is found, the search stops and the first-found implementation is invoked.

Listing 11.6 gives an example to demonstrate dynamic binding.

### Listing 11.6 DynamicBindingDemo.java

```java
public class DynamicBindingDemo {
    public static void main(String[] args) {
        m(new GraduateStudent());
        m(new Student());
        m(new Person());
        m(new Object());
    }

    public static void m(Object x) {
        System.out.println(x.toString());
    }

    public static void m(Object x) {
        // Implementation
    }
}

class GraduateStudent extends Student {
}

class Student extends Person {
    @Override
    public String toString() {
        // Implementation
    }
}
```

**FIGURE 11.2** The method to be invoked is dynamically bound at runtime.
Method \texttt{m} (line 9) takes a parameter of the \texttt{Object} type. You can invoke \texttt{m} with any object (e.g., \texttt{new GraduateStudent()}, \texttt{new Student()}, \texttt{new Person()}, and \texttt{new Object()}) in lines 3–6).

When the method \texttt{m(Object x)} is executed, the argument \texttt{x}'s \texttt{toString} method is invoked. \texttt{x} may be an instance of \texttt{GraduateStudent}, \texttt{Student}, \texttt{Person}, or \texttt{Object}. The classes \texttt{GraduateStudent}, \texttt{Student}, \texttt{Person}, and \texttt{Object} have their own implementations of the \texttt{toString} method. Which implementation is used will be determined by \texttt{x}'s actual type at runtime. Invoking \texttt{m(new GraduateStudent())} (line 3) causes the \texttt{toString} method defined in the \texttt{Student} class to be invoked.

Invoking \texttt{m(new Student())} (line 4) causes the \texttt{toString} method defined in the \texttt{Student} class to be invoked; invoking \texttt{m(new Person())} (line 5) causes the \texttt{toString} method defined in the \texttt{Person} class to be invoked; and invoking \texttt{m(new Object())} (line 6) causes the \texttt{toString} method defined in the \texttt{Object} class to be invoked.

Matching a method signature and binding a method implementation are two separate issues. The \textit{declared type} of the reference variable decides which method to match at compile time. The compiler finds a matching method according to the parameter type, number of parameters, and order of the parameters at compile time. A method may be implemented in several classes along the inheritance chain. The JVM dynamically binds the implementation of the method at runtime, decided by the actual type of the variable.

11.17 What is polymorphism? What is dynamic binding?

11.18 Describe the difference between method matching and method binding.

11.19 Can you assign \texttt{new int[50]}, \texttt{new Integer[50]}, \texttt{new String[50]}, or \texttt{new Object[50]}, into a variable of \texttt{Object[]} type?

11.20 What is wrong in the following code?

```java
public class Test {
    public static void main(String[] args) {
        Integer[] list1 = {12, 24, 55, 1};
        Double[] list2 = {12.4, 24.0, 55.2, 1.0};
        int[] list3 = {1, 2, 3};
        printArray(list1);
        printArray(list2);
        printArray(list3);
    }

    public static void printArray(Object[] list) {
        for (Object o: list)
            System.out.println(o);
    }
}
```
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11.21 Show the output of the following code:

```
public class Test {
    public static void main(String[] args) {
        new Person().printPerson();
        new Student().printPerson();
    }
}

class Student extends Person {
    @Override
    public String getInfo() {
        return "Student";
    }
}

class Person {
    public String getInfo() {
        return "Person";
    }

    public void printPerson() {
        System.out.println(getInfo());
    }
}
```

(b)

```
public class Test {
    public static void main(String[] args) {
        new Person().printPerson();
        new Student().printPerson();
    }
}

class Student extends Person {
    private String getInfo() {
        return "Student";
    }
}

class Person {
    private String getInfo() {
        return "Person";
    }

    public void printPerson() {
        System.out.println(getInfo());
    }
}
```

(a)

11.22 Show the output of following program:

```
public class Test {
    public static void main(String[] args) {
        A a = new A(3);
    }
}

class A extends B {
    public A(int t) {
        System.out.println("A's constructor is invoked");
    }
}

class B {
    public B() {
        System.out.println("B's constructor is invoked");
    }
}
```

Is the no-arg constructor of Object invoked when new A(3) is invoked?

11.23 Show the output of following program:

```
public class Test {
    public static void main(String[] args) {
        new A();
        new B();
    }
}
```
```java
class A {
   int i = 7;

   public A()
   {
      setI(20);
      System.out.println("i from A is " + i);
   }

   public void setI(int i) {
      this.i = 2 * i;
   }
}
class B extends A {
   public B()
   {
      System.out.println("i from B is " + i);
   }

   public void setI(int i) {
      this.i = 3 * i;
   }
}
```

11.9 Casting Objects and the \texttt{instanceof} Operator

One object reference can be typecast into another object reference. This is called casting object.

In the preceding section, the statement

\begin{verbatim}
m(new Student());
\end{verbatim}

assigns the object \texttt{new Student()} to a parameter of the \texttt{Object} type. This statement is equivalent to

\begin{verbatim}
Object o = new Student(); // Implicit casting
m(o);
\end{verbatim}

The statement \texttt{Object o = new Student()}, known as \textit{implicit casting}, is legal because an instance of \texttt{Student} is an instance of \texttt{Object}.

Suppose you want to assign the object reference \texttt{o} to a variable of the \texttt{Student} type using the following statement:

\begin{verbatim}
Student b = o;
\end{verbatim}

In this case a compile error would occur. Why does the statement \texttt{Object o = new Student()} work but \texttt{Student b = o} doesn’t? The reason is that a \texttt{Student} object is always an instance of \texttt{Object}, but an \texttt{Object} is not necessarily an instance of \texttt{Student}. Even though you can see that \texttt{o} is really a \texttt{Student} object, the compiler is not clever enough to know it. To tell the compiler that \texttt{o} is a \texttt{Student} object, use \textit{explicit casting}. The syntax is similar to the one used for casting among primitive data types. Enclose the target object type in parentheses and place it before the object to be cast, as follows:

\begin{verbatim}
Student b = (Student)o; // Explicit casting
\end{verbatim}

It is always possible to cast an instance of a subclass to a variable of a superclass (known as \textit{upcasting}), because an instance of a subclass is always an instance of its superclass. When casting an instance of a superclass to a variable of its subclass (known as \textit{downcasting}), explicit
casting must be used to confirm your intention to the compiler with the \texttt{(SubclassName)} cast notation. For the casting to be successful, you must make sure that the object to be cast is an instance of the subclass. If the superclass object is not an instance of the subclass, a runtime \texttt{ClassCastException} occurs. For example, if an object is not an instance of \texttt{Student}, it cannot be cast into a variable of \texttt{Student}. It is a good practice, therefore, to ensure that the object is an instance of another object before attempting a casting. This can be accomplished by using the \texttt{instanceof} operator. Consider the following code:

\begin{verbatim}
Object myObject = new Circle();
... // Some lines of code
/** Perform casting if myObject is an instance of Circle */
if (myObject instanceof Circle) {
    System.out.println("The circle diameter is " +
                        ((Circle)myObject).getDiameter());
... }
\end{verbatim}

You may be wondering why casting is necessary. The variable \texttt{myObject} is declared \texttt{Object}. The \texttt{declared type} decides which method to match at compile time. Using \texttt{myObject.getDiameter()} would cause a compile error, because the \texttt{Object} class does not have the \texttt{getDiameter} method. The compiler cannot find a match for \texttt{myObject.getDiameter()}. Therefore, it is necessary to cast \texttt{myObject} into the \texttt{Circle} type to tell the compiler that \texttt{myObject} is also an instance of \texttt{Circle}.

Why not define \texttt{myObject} as a \texttt{Circle} type in the first place? To enable generic programming, it is a good practice to define a variable with a supertype, which can accept an object of any subtype.

\textbf{Note}\texttt{ instanceof} is a Java keyword. Every letter in a Java keyword is in lowercase.

\textbf{Tip} To help understand casting, you may also consider the analogy of fruit, apple, and orange, with the \texttt{Fruit} class as the superclass for \texttt{Apple} and \texttt{Orange}. An apple is a fruit, so you can always safely assign an instance of \texttt{Apple} to a variable for \texttt{Fruit}. However, a fruit is not necessarily an apple, so you have to use explicit casting to assign an instance of \texttt{Fruit} to a variable of \texttt{Apple}.

Listing 11.7 demonstrates polymorphism and casting. The program creates two objects (lines 5–6), a circle and a rectangle, and invokes the \texttt{displayObject} method to display them (lines 9–10). The \texttt{displayObject} method displays the area and diameter if the object is a circle (line 15), and the area if the object is a rectangle (lines 21–22).

\textbf{Listing 11.7} \texttt{CastingDemo.java}

\begin{verbatim}
1 public class CastingDemo {
2     /** Main method */
3     public static void main(String[] args) {
4         // Create and initialize two objects
5         Object object1 = new CircleFromSimpleGeometricObject(1);
6         Object object2 = new RectangleFromSimpleGeometricObject(1, 1);
7         // Display circle and rectangle
8         displayObject(object1);
9         displayObject(object2);
10     }
11 }
\end{verbatim}
The `displayObject(Object object)` method is an example of generic programming. It can be invoked by passing any instance of `Object`. The program uses implicit casting to assign a `Circle` object to `object1` and a `Rectangle` object to `object2` (lines 5–6), then invokes the `displayObject` method to display the information on these objects (lines 9–10).

In the `displayObject` method (lines 14–26), explicit casting is used to cast the object to `Circle` if the object is an instance of `Circle`, and the methods `getArea` and `getDiameter` are used to display the area and diameter of the circle.

Casting can be done only when the source object is an instance of the target class. The program uses the `instanceof` operator to ensure that the source object is an instance of the target class before performing a casting (line 15).

Explicit casting to `Circle` (lines 17, 19) and to `Rectangle` (line 24) is necessary because the `getArea` and `getDiameter` methods are not available in the `Object` class.

**Caution**

The object member access operator (.) precedes the casting operator. Use parentheses to ensure that casting is done before the . operator, as in

```java
((Circle)object).getArea();
```

Casting a primitive type value is different from casting an object reference. Casting a primitive type value returns a new value. For example:

```java
int age = 45;
byte newAge = (byte)age;  // A new value is assigned to newAge
```

However, casting an object reference does not create a new object. For example:

```java
Object o = new Circle();
Circle c = (Circle)o;  // No new object is created
```

Now reference variables `o` and `c` point to the same object.
11.24 Indicate true or false for the following statements:

- You can always successfully cast an instance of a subclass to a superclass.
- You can always successfully cast an instance of a superclass to a subclass.

11.25 For the GeometricObject and Circle classes in Listings 11.1 and 11.2, answer the following questions:

a. Assume are circle and object created as follows:
   Circle circle = new Circle(1);
   GeometricObject object = new GeometricObject();

   Are the following Boolean expressions true or false?
   (circle instanceof GeometricObject)
   (object instanceof GeometricObject)
   (circle instanceof Circle)
   (object instanceof Circle)

b. Can the following statements be compiled?
   Circle circle = new Circle(5);
   GeometricObject object = circle;

c. Can the following statements be compiled?
   GeometricObject object = new GeometricObject();
   Circle circle = (Circle)object;

11.26 Suppose that Fruit, Apple, Orange, GoldenDelicious, and McIntosh are defined in the following inheritance hierarchy:

```
Fruit
   Apple
   Orange
   GoldenDelicious
   McIntosh
```

Assume that the following code is given:

Fruit fruit = new GoldenDelicious();
Orange orange = new Orange();

Answer the following questions:

a. Is fruit instanceof Fruit?
b. Is fruit instanceof Orange?
c. Is fruit instanceof Apple?
d. Is fruit instanceof GoldenDelicious?
e. Is fruit instanceof McIntosh?
f. Is orange instanceof Orange?
g. Is `orange` instanceof `Fruit`?

h. Is `orange` instanceof `Apple`?

i. Suppose the method `makeAppleCider` is defined in the `Apple` class. Can `fruit` invoke this method? Can `orange` invoke this method?

j. Suppose the method `makeOrangeJuice` is defined in the `Orange` class. Can `orange` invoke this method? Can `fruit` invoke this method?

k. Is the statement `Orange p = new Apple()` legal?

l. Is the statement `McIntosh p = new Apple()` legal?

m. Is the statement `Apple p = new McIntosh()` legal?

11.27 What is wrong in the following code?

```java
public class Test {
    public static void main(String[] args) {
        Object fruit = new Fruit();
        Object apple = (Apple)fruit;
    }
}

class Apple extends Fruit {
}
class Fruit {
}
```

11.10 The `Object`'s `equals` Method

Like the `toString()` method, the `equals(Object)` method is another useful method defined in the `Object` class.

Another method defined in the `Object` class that is often used is the `equals` method. Its signature is:

```java
public boolean equals(Object o)
```

This method tests whether two objects are equal. The syntax for invoking it is:

```java
object1.equals(object2);
```

The default implementation of the `equals` method in the `Object` class is:

```java
public boolean equals(Object obj) {
    return (this == obj);
}
```

This implementation checks whether two reference variables point to the same object using the `==` operator. You should override this method in your custom class to test whether two distinct objects have the same content.

The `equals` method is overridden in many classes in the Java API, such as `java.lang.String` and `java.util.Date`, to compare whether the contents of two objects are equal. You have already used the `equals` method to compare two strings in Section 4.4.7, The `String` Class. The `equals` method in the `String` class is inherited from the `Object` class and is overridden in the `String` class to test whether two strings are identical in content.
You can override the `equals` method in the `Circle` class to compare whether two circles are equal based on their radius as follows:

```java
public boolean equals(Object o) {
    if (o instanceof Circle)
        return radius == ((Circle)o).radius;
    else
        return this == o;
}
```

**Note**
The `==` comparison operator is used for comparing two primitive data type values or for determining whether two objects have the same references. The `equals` method is intended to test whether two objects have the same contents, provided that the method is overridden in the defining class of the objects. The `==` operator is stronger than the `equals` method, in that the `==` operator checks whether the two reference variables refer to the same object.

**Caution**
Using the signature `equals(SomeClassName obj)` (e.g., `equals(Circle c)`) to override the `equals` method in a subclass is a common mistake. You should use `equals(Object obj)`. See CheckPoint Question 11.29.

11.28 Does every object have a `toString` method and an `equals` method? Where do they come from? How are they used? Is it appropriate to override these methods?

11.29 When overriding the `equals` method, a common mistake is mistyping its signature in the subclass. For example, the `equals` method is incorrectly written as `equals(Circle circle)`, as shown in (a) in following the code; instead, it should be `equals(Object circle)`, as shown in (b). Show the output of running class `Test` with the `Circle` class in (a) and in (b), respectively.

```java
public class Test {
    public static void main(String[] args) {
        Object circle1 = new Circle();
        Object circle2 = new Circle();
        System.out.println(circle1.equals(circle2));
    }
}
```

```java
class Circle {
    double radius;

    public boolean equals(Circle circle) {
        return this.radius == circle.radius;
    }
}
```

(a)

```java
class Circle {
    double radius;

    public boolean equals(Object circle) {
        return this.radius == ((Circle)circle).radius;
    }
}
```

(b)

If `Object` is replaced by `Circle` in the `Test` class, what would be the output to run `Test` using the `Circle` class in (a) and (b), respectively?

### 11.11 The ArrayList Class

An `ArrayList` object can be used to store a list of objects.

Now we are ready to introduce a very useful class for storing objects. You can create an array to store objects. But, once the array is created, its size is fixed. Java provides the `ArrayList`
class, which can be used to store an unlimited number of objects. Figure 11.3 shows some methods in ArrayList.

<table>
<thead>
<tr>
<th>java.util.ArrayList&lt;E&gt;</th>
<th>Creates an empty list.</th>
</tr>
</thead>
<tbody>
<tr>
<td>+Arraylist()</td>
<td>Appends a new element o at the end of this list.</td>
</tr>
<tr>
<td>+add(o: E): void</td>
<td>Adds a new element o at the specified index in this list.</td>
</tr>
<tr>
<td>+add(index: int, o: E): void</td>
<td>Removes all the elements from this list.</td>
</tr>
<tr>
<td>+clear(): void</td>
<td>Returns true if this list contains the element o.</td>
</tr>
<tr>
<td>+contains(o: Object): boolean</td>
<td>Returns the element from this list at the specified index.</td>
</tr>
<tr>
<td>+get(index: int): E</td>
<td>Returns the index of the first matching element in this list.</td>
</tr>
<tr>
<td>+isEmpty(): boolean</td>
<td>Returns true if this list contains no elements.</td>
</tr>
<tr>
<td>+indexOf(o: Object): int</td>
<td>Returns the index of the last matching element in this list.</td>
</tr>
<tr>
<td>+lastIndexOf(o: Object): int</td>
<td>Removes the first element o from this list. Returns true if an element is removed.</td>
</tr>
<tr>
<td>+remove(o: Object): boolean</td>
<td>Removes the number of elements in this list.</td>
</tr>
<tr>
<td>+remove(index: int): boolean</td>
<td>Removes the element at the specified index. Returns true if an element is removed.</td>
</tr>
<tr>
<td>+set(index: int, o: E): E</td>
<td>Sets the element at the specified index.</td>
</tr>
</tbody>
</table>

**Figure 11.3** An ArrayList stores an unlimited number of objects.

ArrayList is known as a generic class with a generic type E. You can specify a concrete type to replace E when creating an ArrayList. For example, the following statement creates an ArrayList and assigns its reference to variable cities. This ArrayList object can be used to store strings.

```java
ArrayList<String> cities = new ArrayList<String>();
```

The following statement creates an ArrayList and assigns its reference to variable dates. This ArrayList object can be used to store dates.

```java
ArrayList<java.util.Date> dates = new ArrayList<java.util.Date>();
```

**Note**
Since JDK 7, the statement

```java
ArrayList<AConcreteType> list = new ArrayList<AConcreteType>();
```

can be simplified by

```java
ArrayList<AConcreteType> list = new ArrayList<>();
```

The concrete type is no longer required in the constructor thanks to a feature called type inference. The compiler is able to infer the type from the variable declaration. More discussions on generics including how to define custom generic classes and methods will be introduced in Chapter 19, Generics.

Listing 11.8 gives an example of using ArrayList to store objects.

**Listing 11.8** TestArrayList.java

```java
import java.util.ArrayList;

import ArrayList;
```
public class TestArrayList {
    public static void main(String[] args) {
        // Create a list to store cities
        ArrayList<String> cityList = new ArrayList<>();

        // Add some cities in the list
        cityList.add("London");
        // cityList now contains [London]
        cityList.add("Denver");
        // cityList now contains [London, Denver]
        cityList.add("Paris");
        // cityList now contains [London, Denver, Paris]
        cityList.add("Miami");
        // cityList now contains [London, Denver, Paris, Miami]
        cityList.add("Seoul");
        // Contains [London, Denver, Paris, Miami, Seoul]
        cityList.add("Tokyo");

        System.out.println("List size? "+ cityList.size());
        System.out.println("Is Miami in the list? "+
                cityList.contains("Miami"));
        System.out.println("The location of Denver in the list? "+
                cityList.indexOf("Denver"));
        System.out.println("Is the list empty? "+
                cityList.isEmpty()); // Print false

        // Insert a new city at index 2
        cityList.add(2, "Xian");

        // Remove a city from the list
        cityList.remove("Miami");

        // Remove a city at index 1
        cityList.remove(1);

        // Display the contents in the list
        System.out.println(cityList.toString());

        // Display the contents in the list in reverse order
        for (int i = cityList.size() - 1; i >= 0; i--)
            System.out.println(cityList.get(i) + " ");

        // Create a list to store two circles
        ArrayList<CircleFromSimpleGeometricObject> list
                = new ArrayList<>();

        // Add two circles
        list.add(new CircleFromSimpleGeometricObject(2));
        list.add(new CircleFromSimpleGeometricObject(3));

        // Display the area of the first circle in the list
        System.out.println("The area of the circle? "+
                list.get(0).getArea());
    }
}
Since the `ArrayList` is in the `java.util` package, it is imported in line 1. The program creates an `ArrayList` of strings using its no-arg constructor and assigns the reference to `cityList` (line 6). The `add` method (lines 9–19) adds strings to the end of list. So, after `cityList.add("London")` (line 9), the list contains

```
[London]
```

After `cityList.add("Denver")` (line 11), the list contains

```
[London, Denver]
```

After adding `Paris, Miami, Seoul, and Tokyo` (lines 13–19), the list contains

```
```

Invoking `size()` (line 22) returns the size of the list, which is currently 6. Invoking `contains("Miami")` (line 24) checks whether the object is in the list. In this case, it returns `true`, since `Miami` is in the list. Invoking `indexOf("Denver")` (line 26) returns the index of `Denver` in the list, which is 1. If `Denver` were not in the list, it would return -1. The `isEmpty()` method (line 28) checks whether the list is empty. It returns `false`, since the list is not empty.

The statement `cityList.add(2, "Xian")` (line 31) inserts an object into the list at the specified index. After this statement, the list becomes

```
[London, Denver, Xian, Paris, Miami, Seoul, Tokyo]
```

The statement `cityList.remove("Miami")` (line 35) removes the object from the list. After this statement, the list becomes

```
```

The statement `cityList.remove(1)` (line 39) removes the object at the specified index from the list. After this statement, the list becomes

```
[London, Xian, Paris, Seoul, Tokyo]
```

The statement in line 43 is same as

```
System.out.println(cityList);
```

The `toString()` method returns a string representation of the list in the form of `[e0.toString(), e1.toString(), ..., ek.toString()]`, where `e0, e1, ..., and ek` are the elements in the list.

The `get(index)` method (line 47) returns the object at the specified index.

`ArrayList` objects can be used like arrays, but there are many differences. Table 11.1 lists their similarities and differences.

Once an array is created, its size is fixed. You can access an array element using the square-bracket notation (e.g., `a[index]`). When an `ArrayList` is created, its size is 0.
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You cannot use the `get(index)` and `set(index, element)` methods if the element is not in the list. It is easy to add, insert, and remove elements in a list, but it is rather complex to add, insert, and remove elements in an array. You have to write code to manipulate the array in order to perform these operations. Note that you can sort an array using the `java.util.Arrays.sort(array)` method. To sort an array list, use the `java.util.Collections.sort(arraylist)` method.

Suppose you want to create an `ArrayList` for storing integers. Can you use the following code to create a list?

```java
ArrayList<int> list = new ArrayList<>();
```

No. This will not work because the elements stored in an `ArrayList` must be of an object type. You cannot use a primitive data type such as `int` to replace a generic type. However, you can create an `ArrayList` for storing `Integer` objects as follows:

```java
ArrayList<Integer> list = new ArrayList<>();
```

Listing 11.9 gives a program that prompts the user to enter a sequence of numbers and displays the distinct numbers in the sequence. Assume that the input ends with 0 and 0 is not counted as a number in the sequence.

**LISTING 11.9  DistinctNumbers.java**

```java
import java.util.ArrayList;
import java.util.Scanner;

public class DistinctNumbers {
    public static void main(String[] args) {
        ArrayList<Integer> list = new ArrayList<>();
        Scanner input = new Scanner(System.in);
        System.out.print("Enter integers (input ends with 0): ");
        int value;
        do {
            value = input.nextInt(); // Read a value from the input
            if (!list.contains(value) && value != 0) {
                list.add(value); // Add the value if it is not in the list
            }
        } while (value != 0);
    }
}
```
// Display the distinct numbers
for (int i = 0; i < list.size(); i++)
    System.out.print(list.get(i) + " ");
}
}

Enter numbers (input ends with 0): 1 2 3 2 1 6 3 4 5 4 5 1 2 3 0
The distinct numbers are: 1 2 3 6 4 5

The program creates an ArrayList for Integer objects (line 6) and repeatedly reads a value in the loop (lines 12–17). For each value, if it is not in the list (line 15), add it to the list (line 16). You can rewrite this program using an array to store the elements rather than using an ArrayList. However, it is simpler to implement this program using an ArrayList for two reasons.

■ First, the size of an ArrayList is flexible so you don’t have to specify its size in advance. When creating an array, its size must be specified.

■ Second, ArrayList contains many useful methods. For example, you can test whether an element is in the list using the contains method. If you use an array, you have to write additional code to implement this method.

You can traverse the elements in an array using a foreach loop. The elements in an array list can also be traversed using a foreach loop using the following syntax:

for (elementType element: arrayList) {
    // Process the element
}

For example, you can replace the code in lines 20-21 using the following code:

for (int number: list)
    System.out.print(number + " ");

11.30 How do you do the following?

a. Create an ArrayList for storing double values?
b. Append an object to a list?
c. Insert an object at the beginning of a list?
d. Find the number of objects in a list?
e. Remove a given object from a list?
f. Remove the last object from the list?
g. Check whether a given object is in a list?
h. Retrieve an object at a specified index from a list?

11.31 Identify the errors in the following code.

```java
ArrayList<String> list = new ArrayList<>();
list.add("Denver");
list.add("Austin");
list.add(new java.util.Date());
String city = list.get(0);
list.set(3, "Dallas");
System.out.println(list.get(3));
```
11.32 Suppose the `ArrayList list` contains `{"Dallas", "Dallas", "Houston", "Dallas"}`. What is the list after invoking `list.remove("Dallas")` one time? Does the following code correctly remove all elements with value "Dallas" from the list? If not, correct the code.

```java
for (int i = 0; i < list.size(); i++)
    list.remove("Dallas");
```

11.33 Explain why the following code displays `[1, 3]` rather than `[2, 3]`.

```java
ArrayList<Integer> list = new ArrayList<>();
list.add(1);
list.add(2);
list.add(3);
list.remove(1);
System.out.println(list);
```

11.34 Explain why the following code is wrong.

```java
ArrayList<Double> list = new ArrayList<>();
list.add(1);
```

11.12 Useful Methods for Lists

Java provides the methods for creating a list from an array, for sorting a list, and finding maximum and minimum element in a list, and for shuffling a list.

**array to array list**

Often you need to create an array list from an array of objects or vice versa. You can write the code using a loop to accomplish this, but an easy way is to use the methods in the Java API. Here is an example to create an array list from an array:

```java
String[] array = {"red", "green", "blue"};
ArrayList<String> list = new ArrayList<>(Arrays.asList(array));
```

**array list to array**

The static method `asList` in the `Arrays` class returns a list that is passed to the `ArrayList` constructor for creating an `ArrayList`. Conversely, you can use the following code to create an array of objects from an array list.

```java
String[] array1 = new String[list.size()];
list.toArray(array1);
```

Invoking `list.toArray(array1)` copies the contents from `list` to `array1`.

**sort a list**

If the elements in a list are comparable such as integers, double, or strings, you can use the static `sort` method in the `java.util.Collections` class to sort the elements. Here are examples:

```java
Integer[] array = {3, 5, 95, 4, 15, 34, 3, 6, 5};
ArrayList<Integer> list = new ArrayList<>(Arrays.asList(array));
java.util.Collections.sort(list);
System.out.println(list);
```

**max and min methods**

You can use the static `max` and `min` in the `java.util.Collections` class to return the maximum and minimal element in a list. Here are examples:

```java
Integer[] array = {3, 5, 95, 4, 15, 34, 3, 6, 5};
ArrayList<Integer> list = new ArrayList<>(Arrays.asList(array));
System.out.println(java.util.Collections.max(list));
System.out.println(java.util.Collections.min(list));
```
You can use the static `shuffle` method in the `java.util.Collections` class to perform a random shuffle for the elements in a list. Here are examples:

```java
Integer[] array = {3, 5, 95, 4, 15, 34, 3, 6, 5};
ArrayList<Integer> list = new ArrayList<>(Arrays.asList(array));
java.util.Collections.shuffle(list);
System.out.println(list);
```

11.35 Correct errors in the following statements:

```java
int[] array = {3, 5, 95, 4, 15, 34, 3, 6, 5};
ArrayList<Integer> list = new ArrayList<>(Arrays.asList(array));
```

11.36 Correct errors in the following statements:

```java
int[] array = {3, 5, 95, 4, 15, 34, 3, 6, 5};
System.out.println(java.util.Collections.max(array));
```

### 11.13 Case Study: A Custom Stack Class

This section designs a stack class for holding objects.

Section 10.6 presented a stack class for storing `int` values. This section introduces a stack class to store objects. You can use an `ArrayList` to implement `Stack`, as shown in Listing 11.10. The UML diagram for the class is shown in Figure 11.4.

<table>
<thead>
<tr>
<th>MyStack</th>
</tr>
</thead>
<tbody>
<tr>
<td>- <code>list</code>: ArrayList&lt;Object&gt;</td>
</tr>
<tr>
<td>+ <code>isEmpty()</code>: boolean</td>
</tr>
<tr>
<td>+ <code>getSize()</code>: int</td>
</tr>
<tr>
<td>+ <code>peek()</code>: Object</td>
</tr>
<tr>
<td>+ <code>pop()</code>: Object</td>
</tr>
<tr>
<td>+ <code>push(o: Object): void</code></td>
</tr>
</tbody>
</table>

**Figure 11.4** The `MyStack` class encapsulates the stack storage and provides the operations for manipulating the stack.

**Listing 11.10** `MyStack.java`

```java
import java.util.ArrayList;

public class MyStack {
    private ArrayList<Object> list = new ArrayList<>();

    public boolean isEmpty() {
        return list.isEmpty();
    }

    public int getSize() {
        return list.size();
    }

    public Object peek() {
        return list.get(getSize() - 1);
    }

    public Object pop() {
        return list.get(getSize() - 1);
    }

    public void push(o: Object) {
        list.add(o);
    }
}
```
public Object pop() {
    Object o = list.get(getSize() - 1);
    list.remove(getSize() - 1);
    return o;
}

public void push(Object o) {
    list.add(o);
}

@Override
public String toString() {
    return "stack: " + list.toString();
}

An array list is created to store the elements in the stack (line 4). The isEmpty() method (lines 6–8) returns list.isEmpty(). The getSize() method (lines 10–12) returns list.size(). The peek() method (lines 14–16) retrieves the element at the top of the stack without removing it. The end of the list is the top of the stack. The pop() method (lines 18–22) removes the top element from the stack and returns it. The push(Object element) method (lines 24–26) adds the specified element to the stack. The toString() method (lines 28–31) defined in the Object class is overridden to display the contents of the stack by invoking list.toString(). The toString() method implemented in ArrayList returns a string representation of all the elements in an array list.

Design Guide

In Listing 11.10, MyStack contains ArrayList. The relationship between MyStack and ArrayList is composition. While inheritance models an is-a relationship, composition models a has-a relationship. You could also implement MyStack as a subclass of ArrayList (see Programming Exercise 11.10). Using composition is better, however, because it enables you to define a completely new stack class without inheriting the unnecessary and inappropriate methods from ArrayList.

11.14 The protected Data and Methods

A protected member of a class can be accessed from a subclass.

So far you have used the private and public keywords to specify whether data fields and methods can be accessed from outside of the class. Private members can be accessed only from inside of the class, and public members can be accessed from any other classes.

Often it is desirable to allow subclasses to access data fields or methods defined in the superclass, but not to allow nonsubclasses to access these data fields and methods. To accomplish this, you can use the protected keyword. This way you can access protected data fields or methods in a superclass from its subclasses.

The modifiers private, protected, and public are known as visibility or accessibility modifiers because they specify how classes and class members are accessed. The visibility of these modifiers increases in this order:

Visibility increases

private, default (no modifier), protected, public

Table 11.2 summarizes the accessibility of the members in a class. Figure 11.5 illustrates how a public, protected, default, and private datum or method in class C1 can be accessed from a class C2 in the same package, from a subclass C3 in the same package, from a subclass C4 in a different package, and from a class C5 in a different package.
Use the `private` modifier to hide the members of the class completely so that they cannot be accessed directly from outside the class. Use no modifiers (the default) in order to allow the members of the class to be accessed directly from any class within the same package but not from other packages. Use the `protected` modifier to enable the members of the class to be accessed by the subclasses in any package or classes in the same package. Use the `public` modifier to enable the members of the class to be accessed by any class.

### Table 11.2: Data and Methods Visibility

<table>
<thead>
<tr>
<th>Modifier on members in a class</th>
<th>Accessed from the same class</th>
<th>Accessed from the same package</th>
<th>Accessed from a subclass in a different package</th>
<th>Accessed from a different package</th>
</tr>
</thead>
<tbody>
<tr>
<td>public</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
</tr>
<tr>
<td>protected</td>
<td>✓</td>
<td>✓</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>default (no modifier)</td>
<td>✓</td>
<td>✓</td>
<td>–</td>
<td>–</td>
</tr>
<tr>
<td>private</td>
<td>✓</td>
<td>–</td>
<td>–</td>
<td>–</td>
</tr>
</tbody>
</table>

**Figure 11.5** Visibility modifiers are used to control how data and methods are accessed.

Your class can be used in two ways: (1) for creating instances of the class and (2) for defining subclasses by extending the class. Make the members `private` if they are not intended for use from outside the class. Make the members `public` if they are intended for the users of the class. Make the fields or methods `protected` if they are intended for the extenders of the class but not for the users of the class.

The `private` and `protected` modifiers can be used only for members of the class. The `public` modifier and the default modifier (i.e., no modifier) can be used on members of the class as well as on the class. A class with no modifier (i.e., not a public class) is not accessible by classes from other packages.
Note
A subclass may override a protected method defined in its superclass and change its visibility to public. However, a subclass cannot weaken the accessibility of a method defined in the superclass. For example, if a method is defined as public in the superclass, it must be defined as public in the subclass.

11.37 What modifier should you use on a class so that a class in the same package can access it, but a class in a different package cannot access it?

11.38 What modifier should you use so that a class in a different package cannot access the class, but its subclasses in any package can access it?

11.39 In the following code, the classes A and B are in the same package. If the question marks in (a) are replaced by blanks, can class B be compiled? If the question marks are replaced by private, can class B be compiled? If the question marks are replaced by protected, can class B be compiled?

11.40 In the following code, the classes A and B are in different packages. If the question marks in (a) are replaced by blanks, can class B be compiled? If the question marks are replaced by private, can class B be compiled? If the question marks are replaced by protected, can class B be compiled?

11.15 Preventing Extending and Overriding
Neither a final class nor a final method can be extended. A final data field is a constant.

You may occasionally want to prevent classes from being extended. In such cases, use the final modifier to indicate that a class is final and cannot be a parent class. The Math class is a final class. The String, StringBuilder, and StringBuffer classes are also final classes. For example, the following class A is final and cannot be extended:

```java
public final class A {
    // Data fields, constructors, and methods omitted
}
```
You also can define a method to be final; a final method cannot be overridden by its subclasses.

For example, the following method `m` is final and cannot be overridden:

```java
public class Test {
    // Data fields, constructors, and methods omitted

    public final void m() {
        // Do something
    }
}
```

**Note**
The modifiers `public`, `protected`, `private`, `static`, `abstract`, and `final` are used on classes and class members (data and methods), except that the `final` modifier can also be used on local variables in a method. A `final` local variable is a constant inside a method.

11.41 How do you prevent a class from being extended? How do you prevent a method from being overridden?

11.42 Indicate true or false for the following statements:

   a. A protected datum or method can be accessed by any class in the same package.
   b. A protected datum or method can be accessed by any class in different packages.
   c. A protected datum or method can be accessed by its subclasses in any package.
   d. A final class can have instances.
   e. A final class can be extended.
   f. A final method can be overridden.

**Key Terms**

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**Chapter Summary**

1. You can define a new class from an existing class. This is known as class inheritance. The new class is called a subclass, child class, or extended class. The existing class is called a superclass, parent class, or base class.

2. A constructor is used to construct an instance of a class. Unlike properties and methods, the constructors of a superclass are not inherited in the subclass. They can be invoked only from the constructors of the subclasses, using the keyword `super`. 
3. A constructor may invoke an overloaded constructor or its superclass’s constructor. The call must be the first statement in the constructor. If none of them is invoked explicitly, the compiler puts `super()` as the first statement in the constructor, which invokes the superclass’s no-arg constructor.

4. To override a method, the method must be defined in the subclass using the same signature and the same return type as in its superclass.

5. An instance method can be overridden only if it is accessible. Thus, a private method cannot be overridden because it is not accessible outside its own class. If a method defined in a subclass is private in its superclass, the two methods are completely unrelated.

6. Like an instance method, a static method can be inherited. However, a static method cannot be overridden. If a static method defined in the superclass is redefined in a subclass, the method defined in the superclass is hidden.

7. Every class in Java is descended from the `java.lang.Object` class. If no superclass is specified when a class is defined, its superclass is `Object`.

8. If a method’s parameter type is a superclass (e.g., `Object`), you may pass an object to this method of any of the parameter’s subclasses (e.g., `Circle` or `String`). This is known as polymorphism.

9. It is always possible to cast an instance of a subclass to a variable of a superclass, because an instance of a subclass is always an instance of its superclass. When casting an instance of a superclass to a variable of its subclass, explicit casting must be used to confirm your intention to the compiler with the `(SubclassName)` cast notation.

10. A class defines a type. A type defined by a subclass is called a *subtype* and a type defined by its superclass is called a *supertype*.

11. When invoking an instance method from a reference variable, the actual type of the variable decides which implementation of the method is used at runtime. This is known as dynamic binding.

12. You can use `obj instanceof AClass` to test whether an object is an instance of a class.

13. You can use the `ArrayList` class to create an object to store a list of objects.

14. You can use the `protected` modifier to prevent the data and methods from being accessed by nonsubclasses from a different package.

15. You can use the `final` modifier to indicate that a class is final and cannot be extended and to indicate that a method is final and cannot be overridden.

---

**Quiz**

Answer the quiz for this chapter online at [www.cs.armstrong.edu/liang/intro10e/quiz.html](http://www.cs.armstrong.edu/liang/intro10e/quiz.html).
**Programming Exercises**

**Sections 11.2–11.4**

11.1 *(The Triangle class)* Design a class named *Triangle* that extends *GeometricObject*. The class contains:

- Three *double* data fields named *side1*, *side2*, and *side3* with default values 1.0 to denote three sides of the triangle.
- A no-arg constructor that creates a default triangle.
- A constructor that creates a triangle with the specified *side1*, *side2*, and *side3*.
- The accessor methods for all three data fields.
- A method named *getArea()* that returns the area of this triangle.
- A method named *getPerimeter()* that returns the perimeter of this triangle.
- A method named *toString()* that returns a string description for the triangle.

For the formula to compute the area of a triangle, see Programming Exercise 2.19. The *toString()* method is implemented as follows:

```
return "Triangle: side1 = " + side1 + " side2 = " + side2 + " side3 = " + side3;
```

Draw the UML diagrams for the classes *Triangle* and *GeometricObject* and implement the classes. Write a test program that prompts the user to enter three sides of the triangle, a color, and a Boolean value to indicate whether the triangle is filled. The program should create a *Triangle* object with these sides and set the *color* and *filled* properties using the input. The program should display the area, perimeter, color, and true or false to indicate whether it is filled or not.

**Sections 11.5–11.14**

11.2 *(The Person, Student, Employee, Faculty, and Staff classes)* Design a class named *Person* and its two subclasses named *Student* and *Employee*. Make *Faculty* and *Staff* subclasses of *Employee*. A person has a name, address, phone number, and email address. A student has a class status (freshman, sophomore, junior, or senior). Define the status as a constant. An employee has an office, salary, and date hired. Use the *MyDate* class defined in Programming Exercise 10.14 to create an object for date hired. A faculty member has office hours and a rank. A staff member has a title. Override the *toString()* method in each class to display the class name and the person’s name.

Draw the UML diagram for the classes and implement them. Write a test program that creates a *Person*, *Student*, *Employee*, *Faculty*, and *Staff*, and invokes their *toString()* methods.

11.3 *(Subclasses of Account)* In Programming Exercise 9.7, the *Account* class was defined to model a bank account. An account has the properties account number, balance, annual interest rate, and date created, and methods to deposit and withdraw funds. Create two subclasses for checking and saving accounts. A checking account has an overdraft limit, but a savings account cannot be overdrawn.

Draw the UML diagram for the classes and then implement them. Write a test program that creates objects of *Account*, *SavingsAccount*, and *CheckingAccount* and invokes their *toString()* methods.

11.4 *(Maximum element in ArrayList)* Write the following method that returns the maximum value in an *ArrayList* of integers. The method returns *null* if the list is *null* or the list size is 0.

```
public static Integer max(ArrayList<Integer> list)
```
Write a test program that prompts the user to enter a sequence of numbers ending with 0, and invokes this method to return the largest number in the input.

11.5 *(The Course class)* Rewrite the Course class in Listing 10.6. Use an ArrayList to replace an array to store students. Draw the new UML diagram for the class. You should not change the original contract of the Course class (i.e., the definition of the constructors and methods should not be changed, but the private members may be changed.)

11.6 *(Use ArrayList)* Write a program that creates an ArrayList and adds a Loan object, a Date object, a string, and a Circle object to the list, and use a loop to display all the elements in the list by invoking the object’s toString() method.

11.7 *(Shuffle ArrayList)* Write the following method that shuffles the elements in an ArrayList of integers.

```
public static void shuffle(ArrayList<Integer> list)
```

**11.8 *(New Account class)* An Account class was specified in Programming Exercise 9.7. Design a new Account class as follows:

- Add a new data field name of the String type to store the name of the customer.
- Add a new constructor that constructs an account with the specified name, id, and balance.
- Add a new data field named transactions whose type is ArrayList that stores the transaction for the accounts. Each transaction is an instance of the Transaction class. The Transaction class is defined as shown in Figure 11.6.

```
public class Account {
    private String name;
    private int id;
    private double balance;
    private ArrayList<Transaction> transactions;

    // Constructor, getters, and setters...
}
```

```
public class Transaction {
    private java.util.Date date;
    private char type;
    private double amount;
    private double balance;
    private String description;

    public Transaction(char type, double amount, double balance, String description) {
        this.type = type;
        this.amount = amount;
        this.balance = balance;
        this.description = description;
    }

    // Getters and setters...
}
```

**Figure 11.6** The Transaction class describes a transaction for a bank account.

- Modify the withdraw and deposit methods to add a transaction to the transactions array list.
- All other properties and methods are the same as in Programming Exercise 9.7.

Write a test program that creates an Account with annual interest rate 1.5%, balance 1000, id 1122, and name George. Deposit $30, $40, and $50 to the account and withdraw $5, $4, and $2 from the account. Print an account summary that shows account holder name, interest rate, balance, and all transactions.
11.9 (Largest rows and columns) Write a program that randomly fills in 0s and 1s into an n-by-n matrix, prints the matrix, and finds the rows and columns with the most 1s. (Hint: Use two ArrayLists to store the row and column indices with the most 1s.) Here is a sample run of the program:

Enter the array size n: 4
The random array is
0011
0011
1101
1010
The largest row index: 2
The largest column index: 2, 3

11.10 (Implement MyStack using inheritance) In Listing 11.10, MyStack is implemented using composition. Define a new stack class that extends ArrayList. Draw the UML diagram for the classes and then implement MyStack. Write a test program that prompts the user to enter five strings and displays them in reverse order.

11.11 (Sort ArrayList) Write the following method that sorts an ArrayList of numbers:

```java
public static void sort(ArrayList<Integer> list)
```
Write a test program that prompts the user to enter 5 numbers, stores them in an array list, and displays them in increasing order.

11.12 (Sum ArrayList) Write the following method that returns the sum of all numbers in an ArrayList:

```java
public static double sum(ArrayList<Double> list)
```
Write a test program that prompts the user to enter 5 numbers, stores them in an array list, and displays their sum.

11.13 (Remove duplicates) Write a method that removes the duplicate elements from an array list of integers using the following header:

```java
public static void removeDuplicate(ArrayList<Integer> list)
```
Write a test program that prompts the user to enter 10 integers to a list and displays the distinct integers separated by exactly one space. Here is a sample run:

Enter ten integers: 34 5 3 5 6 4 33 2 2 4
The distinct integers are 34 5 3 6 4 33 2

11.14 (Combine two lists) Write a method that returns the union of two array lists of integers using the following header:

```java
public static ArrayList<Integer> union(
   ArrayList<Integer> list1, ArrayList<Integer> list2)
```
For example, the union of two array lists \{2, 3, 1, 5\} and \{3, 4, 6\} is \{2, 3, 1, 5, 3, 4, 6\}. Write a test program that prompts the user to enter two lists, each with five integers, and displays their union. The numbers are separated by exactly one space in the output. Here is a sample run:

```
Enter five integers for list1: 3 5 45 4 3
Enter five integers for list2: 33 51 5 4 13
The combined list is 3 5 45 4 3 33 51 5 4 13
```

**11.15 (Area of a convex polygon)** A polygon is convex if it contains any line segments that connect two points of the polygon. Write a program that prompts the user to enter the number of points in a convex polygon, then enter the points clockwise, and display the area of the polygon. Here is a sample run of the program:

```
Enter the number of the points: 7
Enter the coordinates of the points:
-12 0 -8.5 10 0 11.4 5.5 7.8 6 -5.5 0 -7 -3.5 -3.5
The total area is 250.075
```

**11.16 (Addition quiz)** Rewrite Listing 5.1 RepeatAdditionQuiz.java to alert the user if an answer is entered again. *Hint: use an array list to store answers.* Here is a sample run:

```
What is 5 + 9? 12
Wrong answer. Try again. What is 5 + 9? 34
Wrong answer. Try again. What is 5 + 9? 12
You already entered 12
Wrong answer. Try again. What is 5 + 9? 14
You got it!
```

**11.17 (Algebra: perfect square)** Write a program that prompts the user to enter an integer \(m\) and find the smallest integer \(n\) such that \(m \times n\) is a perfect square. (*Hint:* Store all smallest factors of \(m\) into an array list, \(n\) is the product of the factors that appear an odd number of times in the array list. For example, consider \(m = 90\), store the factors 2, 3, 3, 5 in an array list. 2 and 5 appear an odd number of times in the array list. So, \(n\) is 10.) Here are sample runs:

```
Enter an integer m: 1500
The smallest number n for m \times n to be a perfect square is 15
m \times n is 22500
```

```
Enter an integer m: 63
The smallest number n for m \times n to be a perfect square is 7
m \times n is 441
```
Objectives

- To get an overview of exceptions and exception handling (§12.2).
- To explore the advantages of using exception handling (§12.2).
- To distinguish exception types: **Error** (fatal) vs. **Exception** (nonfatal) and checked vs. unchecked (§12.3).
- To declare exceptions in a method header (§12.4.1).
- To throw exceptions in a method (§12.4.2).
- To write a **try-catch** block to handle exceptions (§12.4.3).
- To explain how an exception is propagated (§12.4.3).
- To obtain information from an exception object (§12.4.4).
- To develop applications with exception handling (§12.4.5).
- To use the **finally** clause in a **try-catch** block (§12.5).
- To use exceptions only for unexpected errors (§12.6).
- To rethrow exceptions in a **catch** block (§12.7).
- To create chained exceptions (§12.8).
- To define custom exception classes (§12.9).
- To discover file/directory properties, to delete and rename files/directories, and to create directories using the **File** class (§12.10).
- To write data to a file using the **PrintWriter** class (§12.11.1).
- To use try-with-resources to ensure that the resources are closed automatically (§12.11.2).
- To read data from a file using the **Scanner** class (§12.11.3).
- To understand how data is read using a **Scanner** (§12.11.4).
- To develop a program that replaces text in a file (§12.11.5).
- To read data from the Web (§12.12).
- To develop a Web crawler (§12.13).
12.1 Introduction

Exception handling enables a program to deal with exceptional situations and continue its normal execution.

Runtime errors occur while a program is running if the JVM detects an operation that is impossible to carry out. For example, if you access an array using an index that is out of bounds, you will get a runtime error with an `ArrayIndexOutOfBoundsException`. If you enter a `double` value when your program expects an integer, you will get a runtime error with an `InputMismatchException`.

In Java, runtime errors are thrown as exceptions. An exception is an object that represents an error or a condition that prevents execution from proceeding normally. If the exception is not handled, the program will terminate abnormally. How can you handle the exception so that the program can continue to run or else terminate gracefully? This chapter introduces this subject and text input and output.

12.2 Exception-Handling Overview

Exceptions are thrown from a method. The caller of the method can catch and handle the exception.

To demonstrate exception handling, including how an exception object is created and thrown, let’s begin with the example in Listing 12.1, which reads in two integers and displays their quotient.

**Listing 12.1 Quotient.java**

```java
1 import java.util.Scanner;
2
3 public class Quotient {
4   public static void main(String[] args) {
5     Scanner input = new Scanner(System.in);
6     // Prompt the user to enter two integers
7     System.out.print("Enter two integers: ");
8     int number1 = input.nextInt();
9     int number2 = input.nextInt();
10    System.out.println(number1 + " / " + number2 + " is " +
11                         (number1 / number2));
12   }
13 }
```

<table>
<thead>
<tr>
<th>Enter two integers: 5 2</th>
<th>Enter</th>
</tr>
</thead>
<tbody>
<tr>
<td>5 / 2 is 2</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Enter two integers: 3 0</th>
<th>Enter</th>
</tr>
</thead>
<tbody>
<tr>
<td>Exception in thread &quot;main&quot; java.lang.ArithmeticException: / by zero at Quotient.main(Quotient.java:11)</td>
<td></td>
</tr>
</tbody>
</table>

If you entered 0 for the second number, a runtime error would occur, because you cannot divide an integer by 0. *(Note that a floating-point number divided by 0 does not raise an exception.)* A simple way to fix this error is to add an `if` statement to test the second number, as shown in Listing 12.2.
LISTING 12.2  QuotientWithIf.java

```java
import java.util.Scanner;

public class QuotientWithIf {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter two integers
        System.out.print("Enter two integers: ");
        int number1 = input.nextInt();
        int number2 = input.nextInt();

        if (number2 != 0) {
            System.out.println(number1 + " / " + number2 + " is " + (number1 / number2));
        } else {
            System.out.println("Divisor cannot be zero ");
        }
    }
}
```

Enter two integers: 5 0
Divisor cannot be zero

Before introducing exception handling, let us rewrite Listing 12.2 to compute a quotient using a method, as shown in Listing 12.3.

LISTING 12.3  QuotientWithMethod.java

```java
import java.util.Scanner;

public class QuotientWithMethod {
    public static int quotient(int number1, int number2) {
        if (number2 == 0) {
            System.out.println("Divisor cannot be zero");
            System.exit(1);
        }
        return number1 / number2;
    }

    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter two integers
        System.out.print("Enter two integers: ");
        int number1 = input.nextInt();
        int number2 = input.nextInt();

        int result = quotient(number1, number2);
        System.out.println(number1 + " / " + number2 + " is " + result);
    }
}
```

quotient method
terminate the program
invoke method
The method `quotient` (lines 4–11) returns the quotient of two integers. If `number2` is 0, it cannot return a value, so the program is terminated in line 7. This is clearly a problem. You should not let the method terminate the program—the caller should decide whether to terminate the program.

How can a method notify its caller an exception has occurred? Java enables a method to throw an exception that can be caught and handled by the caller. Listing 12.3 can be rewritten, as shown in Listing 12.4.

**Listing 12.4 QuotientWithException.java**

```java
import java.util.Scanner;

public class QuotientWithException {
    public static int quotient(int number1, int number2) {
        if (number2 == 0)
            throw new ArithmeticException("Divisor cannot be zero");
        return number1 / number2;
    }

    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);

        // Prompt the user to enter two integers
        System.out.print("Enter two integers: ");
        int number1 = input.nextInt();
        int number2 = input.nextInt();

        try {
            int result = quotient(number1, number2);
            System.out.println(number1 + " / " + number2 + " is " + result);
        } catch (ArithmeticException ex) {
            System.out.println("Exception: an integer " +
                               "cannot be divided by zero ");
        }
        System.out.println("Execution continues ...");
    }
}
```

Enter two integers: 5 3
5 / 3 is 1

Enter two integers: 5 0
Divisor cannot be zero

Enter two integers: 5 3
Enter two integers: 5 0
Enter two integers: 5 0
Divisor cannot be zero
If \texttt{number2} is 0, the method throws an exception (line 6) by executing

\begin{verbatim}
    throw new ArithmeticException("Divisor cannot be zero");
\end{verbatim}

The value thrown, in this case \texttt{new ArithmeticException("Divisor cannot be zero")}, is called an \textit{exception}. The execution of a \texttt{throw} statement is called \textit{throwing an exception}. The exception is an object created from an exception class. In this case, the exception class is \texttt{java.lang.ArithmeticException}. The constructor \texttt{ArithmeticException(str)} is invoked to construct an exception object, where \texttt{str} is a message that describes the exception.

When an exception is thrown, the normal execution flow is interrupted. As the name suggests, to “throw an exception” is to pass the exception from one place to another. The statement for invoking the method is contained in a \texttt{try} block and a \texttt{catch} block. The \texttt{try} block (lines 19–23) contains the code that is executed in normal circumstances. The exception is caught by the \texttt{catch} block. The code in the \texttt{catch} block is executed to \textit{handle the exception}. Afterward, the statement (line 29) after the \texttt{catch} block is executed.

The \texttt{throw} statement is analogous to a method call, but instead of calling a method, it calls a \texttt{catch} block. In this sense, a \texttt{catch} block is like a method definition with a parameter that matches the type of the value being thrown. Unlike a method, however, after the \texttt{catch} block is executed, the program control does not return to the \texttt{throw} statement; instead, it executes the next statement after the \texttt{catch} block.

The identifier \texttt{ex} in the \texttt{catch–block header}

\begin{verbatim}
    catch (ArithmeticException ex)
\end{verbatim}

acts very much like a parameter in a method. Thus, this parameter is referred to as a \texttt{catch–block parameter}. The type (e.g., \texttt{ArithmeticException}) preceding \texttt{ex} specifies what kind of exception the \texttt{catch} block can catch. Once the exception is caught, you can access the thrown value from this parameter in the body of a \texttt{catch} block.

In summary, a template for a \texttt{try-throw-catch} block may look like this:

\begin{verbatim}
try {
    Code to run;
    A statement or a method that may throw an exception;
    More code to run;
}
catch (type ex) {
    Code to process the exception;
}
\end{verbatim}

An exception may be thrown directly by using a \texttt{throw} statement in a \texttt{try} block, or by invoking a method that may throw an exception.

The main method invokes \texttt{quotient} (line 20). If the quotient method executes normally, it returns a value to the caller. If the \texttt{quotient} method encounters an exception, it throws the exception back to its caller. The caller’s \texttt{catch} block handles the exception.

Now you can see the \textit{advantage} of using exception handling: It enables a method to throw an exception to its caller, enabling the caller to handle the exception. Without this capability, the called method itself must handle the exception or terminate the program. Often the called method does not know what to do in case of error. This is typically the case for the library methods. The library method can detect the error, but only the caller knows what needs to be
done when an error occurs. The key benefit of exception handling is separating the detection of an error (done in a called method) from the handling of an error (done in the calling method).

Many library methods throw exceptions. Listing 12.5 gives an example that handles an InputMismatchException when reading an input.

**LISTING 12.5 InputMismatchExceptionDemo.java**

```java
import java.util.*;

public class InputMismatchExceptionDemo {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        boolean continueInput = true;

        do {
            try {
                System.out.print("Enter an integer: ");
                int number = input.nextInt();
                // Display the result
                System.out.println("The number entered is " + number);
                continueInput = false;
            } catch (InputMismatchException ex) {
                System.out.println("Try again. (Incorrect input: an integer is required) (" +
                                  "Incorrect input: an integer is required)" +
                                  "Incorrect input: an integer is required) ");
                input.nextLine(); // Discard input
            }
        } while (continueInput);
    }
}
```

When executing `input.nextInt()` (line 11), an InputMismatchException occurs if the input entered is not an integer. Suppose 3.5 is entered. An InputMismatchException occurs and the control is transferred to the catch block. The statements in the catch block are now executed. The statement `input.nextLine()` in line 22 discards the current input line so that the user can enter a new line of input. The variable `continueInput` controls the loop. Its initial value is `true` (line 6), and it is changed to `false` (line 17) when a valid input is received. Once a valid input is received, there is no need to continue the input.

**Check Point**

12.1 What is the advantage of using exception handling?

12.2 Which of the following statements will throw an exception?

```java
System.out.println(1 / 0);
System.out.println(1.0 / 0);
```
12.3 Exception Types

Exceptions are objects, and objects are defined using classes. The root class for exceptions is `java.lang.Throwable`.

The preceding section used the classes `ArithmeticException` and `InputMismatchException`. Are there any other types of exceptions you can use? Can you define your own exception classes? Yes. There are many predefined exception classes in the Java API. Figure 12.1 shows some of them, and in Section 12.9 you will learn how to define your own exception classes.
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Note
The class names Error, Exception, and RuntimeException are somewhat confusing. All three of these classes are exceptions, and all of the errors occur at runtime.

The Throwable class is the root of exception classes. All Java exception classes inherit directly or indirectly from Throwable. You can create your own exception classes by extending Exception or a subclass of Exception.

The exception classes can be classified into three major types: system errors, exceptions, and runtime exceptions.

- **System errors** are thrown by the JVM and are represented in the Error class. The Error class describes internal system errors, though such errors rarely occur. If one does, there is little you can do beyond notifying the user and trying to terminate the program gracefully. Examples of subclasses of Error are listed in Table 12.1.

<table>
<thead>
<tr>
<th>Class</th>
<th>Reasons for Exception</th>
</tr>
</thead>
<tbody>
<tr>
<td>LinkageError</td>
<td>A class has some dependency on another class, but the latter class has changed incompatibly after the compilation of the former class.</td>
</tr>
<tr>
<td>VirtualMachineError</td>
<td>The JVM is broken or has run out of the resources it needs in order to continue operating.</td>
</tr>
</tbody>
</table>

- **Exceptions** are represented in the Exception class, which describes errors caused by your program and by external circumstances. These errors can be caught and handled by your program. Examples of subclasses of Exception are listed in Table 12.2.

<table>
<thead>
<tr>
<th>Class</th>
<th>Reasons for Exception</th>
</tr>
</thead>
<tbody>
<tr>
<td>ClassNotFoundException</td>
<td>Attempt to use a class that does not exist. This exception would occur, for example, if you tried to run a nonexistent class using the java command, or if your program were composed of, say, three class files, only two of which could be found.</td>
</tr>
<tr>
<td>IOException</td>
<td>Related to input/output operations, such as invalid input, reading past the end of a file, and opening a nonexistent file. Examples of subclasses of IOException are InterruptedIOException, EOFException (EOF is short for End of File), and FileNotFoundException.</td>
</tr>
</tbody>
</table>
Runtime exceptions are represented in the RuntimeException class, which describes programming errors, such as bad casting, accessing an out-of-bounds array, and numeric errors. Runtime exceptions are generally thrown by the JVM. Examples of subclasses are listed in Table 12.3.

**Table 12.3** Examples of Subclasses of RuntimeException

<table>
<thead>
<tr>
<th>Class</th>
<th>Reasons for Exception</th>
</tr>
</thead>
<tbody>
<tr>
<td>ArithmeticException</td>
<td>Dividing an integer by zero. Note that floating-point arithmetic does not throw exceptions (see Appendix E, Special Floating-Point Values).</td>
</tr>
<tr>
<td>NullPointerException</td>
<td>Attempt to access an object through a null reference variable.</td>
</tr>
<tr>
<td>IndexOutOfBoundsException</td>
<td>Index to an array is out of range.</td>
</tr>
<tr>
<td>IllegalArgumentException</td>
<td>A method is passed an argument that is illegal or inappropriate.</td>
</tr>
</tbody>
</table>

RuntimeException, Error, and their subclasses are known as unchecked exceptions. All other exceptions are known as checked exceptions, meaning that the compiler forces the programmer to check and deal with them in a try-catch block or declare it in the method header. Declaring an exception in the method header will be covered in Section 12.4.

In most cases, unchecked exceptions reflect programming logic errors that are unrecoverable. For example, a NullPointerException is thrown if you access an object through a reference variable before an object is assigned to it; an IndexOutOfBoundsException is thrown if you access an element in an array outside the bounds of the array. These are logic errors that should be corrected in the program. Unchecked exceptions can occur anywhere in a program. To avoid cumbersome overuse of try-catch blocks, Java does not mandate that you write code to catch or declare unchecked exceptions.

12.7 Describe the Java Throwable class, its subclasses, and the types of exceptions.
12.8 What RuntimeException will the following programs throw, if any?

(a)```java
public class Test {
    public static void main(String[] args) {
        System.out.println(1 / 0);
    }
}
```

(b)```java
public class Test {
    public static void main(String[] args) {
        int[] list = new int[5];
        System.out.println(list[5]);
    }
}
```

(c)```java
public class Test {
    public static void main(String[] args) {
        String s = "abc";
        System.out.println(s.charAt(3));
    }
}
```

(d)```java
public class Test {
    public static void main(String[] args) {
        Object o = new Object();
        String d = (String)o;
    }
}
```

(e)```java
public class Test {
    public static void main(String[] args) {
        Object o = null;
        System.out.println(o.toString());
    }
}
```

(f)```java
public class Test {
    public static void main(String[] args) {
        System.out.println(1.0 / 0);
    }
}
```
12.4 More on Exception Handling

A handler for an exception is found by propagating the exception backward through a chain of method calls, starting from the current method.

The preceding sections gave you an overview of exception handling and introduced several predefined exception types. This section provides an in-depth discussion of exception handling.

Java’s exception-handling model is based on three operations: declaring an exception, throwing an exception, and catching an exception, as shown in Figure 12.2.

12.4.1 Declaring Exceptions

In Java, the statement currently being executed belongs to a method. The Java interpreter invokes the main method to start executing a program. Every method must state the types of checked exceptions it might throw. This is known as declaring exceptions. Because system errors and runtime errors can happen to any code, Java does not require that you declare Error and RuntimeException (unchecked exceptions) explicitly in the method. However, all other exceptions thrown by the method must be explicitly declared in the method header so that the caller of the method is informed of the exception.

To declare an exception in a method, use the throws keyword in the method header, as in this example:

```java
public void myMethod() throws IOException
```

The throws keyword indicates that myMethod might throw an IOException. If the method might throw multiple exceptions, add a list of the exceptions, separated by commas, after throws:

```java
public void myMethod()
    throws Exception1, Exception2, ..., ExceptionN
```

Note

If a method does not declare exceptions in the superclass, you cannot override it to declare exceptions in the subclass.

12.4.2 Throwing Exceptions

A program that detects an error can create an instance of an appropriate exception type and throw it. This is known as throwing an exception. Here is an example: Suppose the program detects that an argument passed to the method violates the method contract (e.g., the argument...
must be nonnegative, but a negative argument is passed); the program can create an instance of `IllegalArgumentException` and throw it, as follows:

```java
IllegalArgumentException ex =
    new IllegalArgumentException("Wrong Argument");
throw ex;
```

Or, if you prefer, you can use the following:

```java
throw new IllegalArgumentException("Wrong Argument");
```

**Note**

`IllegalArgumentException` is an exception class in the Java API. In general, each exception class in the Java API has at least two constructors: a no-arg constructor, and a constructor with a `String` argument that describes the exception. This argument is called the *exception message*, which can be obtained using `getMessage()`.

**Tip**

The keyword to declare an exception is *throws*, and the keyword to throw an exception is *throw*.

### 12.4.3 Catching Exceptions

You now know how to declare an exception and how to throw an exception. When an exception is thrown, it can be caught and handled in a `try-catch` block, as follows:

```java
try {
    statements; // Statements that may throw exceptions
} catch (Exception1 exVar1) {
    handler for exception1;
} catch (Exception2 exVar2) {
    handler for exception2;
}...
catch (ExceptionN exVarN) {
    handler for exceptionN;
}
```

If no exceptions arise during the execution of the `try` block, the `catch` blocks are skipped. If one of the statements inside the `try` block throws an exception, Java skips the remaining statements in the `try` block and starts the process of finding the code to handle the exception. The code that handles the exception is called the *exception handler*; it is found by *propagating the exception* backward through a chain of method calls, starting from the current method. Each `catch` block is examined in turn, from first to last, to see whether the type of the exception object is an instance of the exception class in the `catch` block. If so, the exception object is assigned to the variable declared, and the code in the `catch` block is executed. If no handler is found, Java exits this method, passes the exception to the method that invoked the method, and continues the same process to find a handler. If no handler is found in the chain of methods being invoked, the program terminates and prints an error message on the console. The process of finding a handler is called *catching an exception*. 
Suppose the `main` method invokes `method1`, `method1` invokes `method2`, `method2` invokes `method3`, and `method3` throws an exception, as shown in Figure 12.3. Consider the following scenario:

- If the exception type is `Exception3`, it is caught by the `catch` block for handling exception `ex3` in `method2`. `statement5` is skipped, and `statement6` is executed.
- If the exception type is `Exception2`, `method2` is aborted, the control is returned to `method1`, and the exception is caught by the `catch` block for handling exception `ex2` in `method1`. `statement3` is skipped, and `statement4` is executed.
- If the exception type is `Exception1`, `method1` is aborted, the control is returned to the `main` method, and the exception is caught by the `catch` block for handling exception `ex1` in the `main` method. `statement1` is skipped, and `statement2` is executed.
- If the exception type is not caught in `method2`, `method1`, or `main`, the program terminates, and `statement1` and `statement2` are not executed.

![Call stack](image)

**Figure 12.3** If an exception is not caught in the current method, it is passed to its caller. The process is repeated until the exception is caught or passed to the `main` method.

**Note**
Various exception classes can be derived from a common superclass. If a `catch` block catches exception objects of a superclass, it can catch all the exception objects of the subclasses of that superclass.

**Note**
The order in which exceptions are specified in `catch` blocks is important. A compile error will result if a catch block for a superclass type appears before a catch block for a subclass type. For example, the ordering in (a) on the next page is erroneous, because `RuntimeException` is a subclass of `Exception`. The correct ordering should be as shown in (b).
12.4 More on Exception Handling

Note
Java forces you to deal with checked exceptions. If a method declares a checked exception (i.e., an exception other than `Error` or `RuntimeException`), you must invoke it in a `try-catch` block or declare to throw the exception in the calling method. For example, suppose that method `p1` invokes method `p2`, and `p2` may throw a checked exception (e.g., `IOException`); you have to write the code as shown in (a) or (b) below.

```java
void p1() {
    try {
        p2();
    } catch (IOException ex) {
        // Code to handle IOException
    }
}
```

(a) Wrong order

```java
void p1() throws IOException {
    p2();
}
```

(b) Correct order

catch or declare checked exceptions

Note
You can use the new JDK 7 multi-catch feature to simplify coding for the exceptions with the same handling code. The syntax is:

```java
catch (Exception1 | Exception2 | ... | Exceptionk ex) {
    // Same code for handling these exceptions
}
```

Each exception type is separated from the next with a vertical bar (`|`). If one of the exceptions is caught, the handling code is executed.

12.4.4 Getting Information from Exceptions
An exception object contains valuable information about the exception. You may use the following instance methods in the `java.lang.Throwable` class to get information regarding the exception, as shown in Figure 12.4. The `printStackTrace()` method prints stack trace methods in `Throwable`.

```java
java.lang.Throwable
+getMessage(): String
+toString(): String
+printStackTrace(): void
+getStackTrace(): StackTraceElement[]
```

Returns the message that describes this exception object.
Returns the concatenation of three strings: (1) the full name of the exception class; (2) "": (a colon and a space); (3) the `getMessage()` method.
Downloads the `Throwable` object and its call stack trace information on the console.
Returns an array of stack trace elements representing the stack trace pertaining to this exception object.

Figure 12.4 `Throwable` is the root class for all exception objects.
information on the console. The `getStackTrace()` method provides programmatic access to the stack trace information printed by `printStackTrace()`.

Listing 12.6 gives an example that uses the methods in `Throwables` to display exception information. Line 4 invokes the `sum` method to return the sum of all the elements in the array. There is an error in line 23 that causes the `ArrayIndexOutOfBoundsException`, a subclass of `IndexOutOfBoundsException`. This exception is caught in the `try-catch` block. Lines 7, 8, and 9 display the stack trace, exception message, and exception object and message using the `printStackTrace()`, `getMessage()`, and `toString()` methods, as shown in Figure 12.5. Line 12 brings stack trace elements into an array. Each element represents a method call. You can obtain the method (line 14), class name (line 15), and exception line number (line 16) for each element.

![Figure 12.5](image)

**Figure 12.5** You can use the `printStackTrace()`, `getMessage()`, `toString()`, and `getStackTrace()` methods to obtain information from exception objects.

### Listing 12.6 TestException.java

```java
public class TestException {
    public static void main(String[] args) {
        try {
            System.out.println(sum(new int[] {1, 2, 3, 4, 5}));
        }
    }
}
```

```java
public static int sum(int[] list) {
    int result = 0;
    for (int i = 0; i < list.length; i++) {
        System.out.println(list[i] + 1);
        result = result + list[i];
    }
    return result;
}
```

```java
private static int sum(int[] list) {
    int result = 0;
    for (int i = 0; i < list.length; i++) {
        System.out.println(list[i] + 1);
        result = result + list[i];
    }
    return result;
}
```

cause an exception

```java
private static int sum(int[] list) {
    int result = 0;
    for (int i = 0; i < list.length; i++) {
        System.out.println(list[i] + 1);
        result = result + list[i];
    }
    return result;
}
```
12.4 More on Exception Handling

result += list[i];
return result;

12.4.5 Example: Declaring, Throwing, and Catching Exceptions

This example demonstrates declaring, throwing, and catching exceptions by modifying the `setRadius` method in the `Circle` class in Listing 9.8, `CircleWithPrivateDataFields.java`. The new `setRadius` method throws an exception if the radius is negative.

Listing 12.7 defines a new circle class named `CircleWithException`, which is the same as `CircleWithPrivateDataFields` except that the `setRadius(double newRadius)` method throws an `IllegalArgumentException` if the argument `newRadius` is negative.

**LISTING 12.7 CircleWithException.java**

```java
public class CircleWithException {
    /** The radius of the circle */
    private double radius;

    /** The number of the objects created */
    private static int numberOfObjects = 0;

    /** Construct a circle with radius 1 */
    public CircleWithException() {
        this(1.0);
    }

    /** Construct a circle with a specified radius */
    public CircleWithException(double newRadius) {
        setRadius(newRadius);
        numberOfObjects++;
    }

    /** Return radius */
    public double getRadius() {
        return radius;
    }

    /** Set a new radius */
    public void setRadius(double newRadius)
        throws IllegalArgumentException {
        if (newRadius >= 0)
            radius = newRadius;
        else
            throw new IllegalArgumentException("Radius cannot be negative");
    }

    /** Return numberOfObjects */
    public static int getNumberOfObjects() {
        return numberOfObjects;
    }

    /** Return the area of this circle */
    public double findArea() {
        return radius * radius * 3.14159;
    }
}
```
A test program that uses the new `Circle` class is given in Listing 12.8.

**Listing 12.8  TestCircleWithException.java**

```java
public class TestCircleWithException {
  public static void main(String[] args) {
    try {
      CircleWithException c1 = new CircleWithException(5);
      CircleWithException c2 = new CircleWithException(-5);
      CircleWithException c3 = new CircleWithException(0);
    }
    catch (IllegalArgumentException ex) {
      System.out.println(ex);
    }
    System.out.println("Number of objects created: " +
      CircleWithException.getNumberOfObjects());
  }
}
```

The original `Circle` class remains intact except that the class name is changed to `CircleWithException`, a new constructor `CircleWithException(newRadius)` is added, and the `setRadius` method now declares an exception and throws it if the radius is negative.

The `setRadius` method declares to throw `IllegalArgumentException` in the method header (lines 25–32 in `CircleWithException.java`). The `CircleWithException` class would still compile if the `throws IllegalArgumentException` clause (line 26) were removed from the method declaration, since it is a subclass of `RuntimeException` and every method can throw `RuntimeException` (an unchecked exception) regardless of whether it is declared in the method header.

The test program creates three `CircleWithException` objects—`c1`, `c2`, and `c3`—to test how to handle exceptions. Invoking `new CircleWithException(-5)` (line 5 in Listing 12.8) causes the `setRadius` method to be invoked, which throws an `IllegalArgumentException`, because the radius is negative. In the `catch` block, the type of the object `ex` is `IllegalArgumentException`, which matches the exception object thrown by the `setRadius` method, so this exception is caught by the `catch` block.

The exception handler prints a short message, `ex.toString()` (line 9 in Listing 12.8), about the exception, using `System.out.println(ex).

Note that the execution continues in the event of the exception. If the handlers had not caught the exception, the program would have abruptly terminated.

The test program would still compile if the `try` statement were not used, because the method throws an instance of `IllegalArgumentException`, a subclass of `RuntimeException` (an unchecked exception). If a method throws an exception other than `RuntimeException` or `Error`, the method must be invoked within a `try-catch` block.

12.9 What is the purpose of declaring exceptions? How do you declare an exception, and where? Can you declare multiple exceptions in a method header?

12.10 What is a checked exception, and what is an unchecked exception?

12.11 How do you throw an exception? Can you throw multiple exceptions in one `throw` statement?

12.12 What is the keyword `throw` used for? What is the keyword `throws` used for?
12.13 Suppose that `statement2` causes an exception in the following `try-catch` block:

```java
try {
    statement1;
    statement2;
    statement3;
} catch (Exception1 ex1) {} catch (Exception2 ex2) {
    statement4;
}
```

Answer the following questions:
- Will `statement3` be executed?
- If the exception is not caught, will `statement4` be executed?
- If the exception is caught in the `catch` block, will `statement4` be executed?

12.14 What is displayed when the following program is run?

```java
public class Test {
    public static void main(String[] args) {
        try {
            int[] list = new int[10];
            System.out.println("list[10] is " + list[10]);
        } catch (ArithmeticException ex) {
            System.out.println("ArithmeticException");
        } catch (RuntimeException ex) {
            System.out.println("RuntimeException");
        } catch (Exception e) {
            System.out.println("Exception");
        }
    }
}
```

12.15 What is displayed when the following program is run?

```java
public class Test {
    public static void main(String[] args) {
        try {
            method();
            System.out.println("After the method call");
        } catch (ArithmeticException ex) {
            System.out.println("ArithmeticException");
        } catch (RuntimeException ex) {
            System.out.println("RuntimeException");
        } catch (Exception e) {
            System.out.println("Exception");
        }
    }

    static void method() throws Exception {
```
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12.16 What is displayed when the following program is run?

```java
public class Test {
    public static void main(String[] args) {
        try {
            method();
            System.out.println("After the method call");
        } catch (RuntimeException ex) {
            System.out.println("RuntimeException in main");
        } catch (Exception ex) {
            System.out.println("Exception in main");
        }
    }

    static void method() throws Exception {
        try {
            String s = "abc";
            System.out.println(s.charAt(3));
        } catch (RuntimeException ex) {
            System.out.println("RuntimeException in method()");
        } catch (Exception ex) {
            System.out.println("Exception in method()");
        }
    }
}
```

12.17 What does the method `getMessage()` do?

12.18 What does the method `printStackTrace()` do?

12.19 Does the presence of a `try-catch` block impose overhead when no exception occurs?

12.20 Correct a compile error in the following code:

```java
public void m(int value) {
    if (value < 40)
        throw new Exception("value is too small");
}
```

12.5 The finally Clause

The **finally** clause is always executed regardless whether an exception occurred or not.

Occasionally, you may want some code to be executed regardless of whether an exception occurs or is caught. Java has a **finally** clause that can be used to accomplish this objective. The syntax for the `finally` clause might look like this:

```java
try {
    statements;
} catch (TheException ex) {
    handling ex;
}
```
Finally block

```java
finally {
    finalStatements;
}
```

The code in the `finally` block is executed under all circumstances, regardless of whether an exception occurs in the `try` block or is caught. Consider three possible cases:

- If no exception arises in the `try` block, `finalStatements` is executed, and the next statement after the `try` statement is executed.
- If a statement causes an exception in the `try` block that is caught in a `catch` block, the rest of the statements in the `try` block are skipped, the `catch` block is executed, and the `finally` clause is executed. The next statement after the `try` statement is executed.
- If one of the statements causes an exception that is not caught in any `catch` block, the other statements in the `try` block are skipped, the `finally` clause is executed, and the exception is passed to the caller of this method.

The `finally` block executes even if there is a `return` statement prior to reaching the `finally` block.

**Note**
The `catch` block may be omitted when the `finally` clause is used.

### 12.2.1

Suppose that `statement2` causes an exception in the following statement:

```java
try {
    statement1;
    statement2;
    statement3;
}
catch (Exception1 ex1) {
}
finally {
    statement4;
}
statement5;
```

Answer the following questions:

- If no exception occurs, will `statement4` be executed, and will `statement5` be executed?
- If the exception is of type `Exception1`, will `statement4` be executed, and will `statement5` be executed?
- If the exception is not of type `Exception1`, will `statement4` be executed, and will `statement5` be executed?

### 12.6 When to Use Exceptions

*A method should throw an exception if the error needs to be handled by its caller.*

The `try` block contains the code that is executed in normal circumstances. The `catch` block contains the code that is executed in exceptional circumstances. Exception handling separates error-handling code from normal programming tasks, thus making programs easier to read and to modify. Be aware, however, that exception handling usually requires more time and resources, because it requires instantiating a new exception object, rolling back the call stack, and propagating the exception through the chain of methods invoked to search for the handler.
An exception occurs in a method. If you want the exception to be processed by its caller, you should create an exception object and throw it. If you can handle the exception in the method where it occurs, there is no need to throw or use exceptions.

In general, common exceptions that may occur in multiple classes in a project are candidates for exception classes. Simple errors that may occur in individual methods are best handled without throwing exceptions. This can be done by using if statements to check for errors.

When should you use a try-catch block in the code? Use it when you have to deal with unexpected error conditions. Do not use a try-catch block to deal with simple, expected situations. For example, the following code

```java
try {
    System.out.println(refVar.toString());
} catch (NullPointerException ex) {
    System.out.println("refVar is null");
}
```

is better replaced by

```java
if (refVar != null)
    System.out.println(refVar.toString());
else
    System.out.println("refVar is null");
```

Which situations are exceptional and which are expected is sometimes difficult to decide. The point is not to abuse exception handling as a way to deal with a simple logic test.

The following method checks whether a string is a numeric string:

```java
public static boolean isNumeric(String token) {
    try {
        Double.parseDouble(token);
        return true;
    } catch (java.lang.NumberFormatException ex) {
        return false;
    }
}
```

Is it correct? Rewrite it without using exceptions.

### 12.7 Rethrowing Exceptions

Java allows an exception handler to rethrow the exception if the handler cannot process the exception or simply wants to let its caller be notified of the exception.

The syntax for rethrowing an exception may look like this:

```java
try {
    statements;
} catch (TheException ex) {
    perform operations before exits;
    throw ex;
}
```

The statement throw ex rethrows the exception to the caller so that other handlers in the caller get a chance to process the exception ex.
12.23 Suppose that \texttt{statement2} causes an exception in the following statement:

\begin{verbatim}
try {
    statement1;
    statement2;
    statement3;
} catch (Exception1 ex1) {
} catch (Exception2 ex2) {
    throw ex2;
} finally {
    statement4;
} statement5;
\end{verbatim}

Answer the following questions:

- If no exception occurs, will \texttt{statement4} be executed, and will \texttt{statement5} be executed?
- If the exception is of type \texttt{Exception1}, will \texttt{statement4} be executed, and will \texttt{statement5} be executed?
- If the exception is of type \texttt{Exception2}, will \texttt{statement4} be executed, and will \texttt{statement5} be executed?
- If the exception is not \texttt{Exception1} nor \texttt{Exception2}, will \texttt{statement4} be executed, and will \texttt{statement5} be executed?

12.8 Chained Exceptions

\textit{Throwing an exception along with another exception forms a chained exception.}

In the preceding section, the \texttt{catch} block rethrows the original exception. Sometimes, you may need to throw a new exception (with additional information) along with the original exception. This is called \textit{chained exceptions}. Listing 12.9 illustrates how to create and throw chained exceptions.

\begin{verbatim}
LISTING 12.9 ChainedExceptionDemo.java
public class ChainedExceptionDemo {
    public static void main(String[] args) {
        try {
            method1();
        } catch (Exception ex) {
            ex.printStackTrace();
        }
    }

    public static void method1() throws Exception {
        try {
            method2();
        } catch (Exception ex) {
            throw new Exception("New info from method1", ex);
        }
    }
}
\end{verbatim}
Chapter 12  Exception Handling and Text I/O

public static void method2() throws Exception {
    throw new Exception("New info from method2");
}

java.lang.Exception: New info from method1
    at ChainedExceptionDemo.method1(ChainedExceptionDemo.java:16)
    at ChainedExceptionDemo.main(ChainedExceptionDemo.java:4)
Caused by: java.lang.Exception: New info from method2
    at ChainedExceptionDemo.method2(ChainedExceptionDemo.java:21)
    at ChainedExceptionDemo.method1(ChainedExceptionDemo.java:13)
    ... 1 more

The main method invokes method1 (line 4), method1 invokes method2 (line 13), and method2 throws an exception (line 21). This exception is caught in the catch block in method1 and is wrapped in a new exception in line 16. The new exception is thrown and caught in the catch block in the main method in line 6. The sample output shows the output from the printStackTrace() method in line 7. The new exception thrown from method1 is displayed first, followed by the original exception thrown from method2.

12.24 What would be the output if line 16 is replaced by the following line?

    throw new Exception("New info from method1");

12.9 Defining Custom Exception Classes

You can define a custom exception class by extending the java.lang.Exception class.

Java provides quite a few exception classes. Use them whenever possible instead of defining your own exception classes. However, if you run into a problem that cannot be adequately described by the predefined exception classes, you can create your own exception class, derived from Exception or from a subclass of Exception, such as IOException.

In Listing 12.7, CircleWithException.java, the setRadius method throws an exception if the radius is negative. Suppose you wish to pass the radius to the handler. In that case, you can define a custom exception class, as shown in Listing 12.10.

LISTING 12.10  InvalidRadiusException.java

1  public class InvalidRadiusException extends Exception {
2      private double radius;
3  
4     /** Construct an exception */
5     public InvalidRadiusException(double radius) {
6         super("Invalid radius "+radius);
7         this.radius = radius;
8     }
9  
10    /** Return the radius */
11     public double getRadius() {
12         return radius;
13     }
14  }

This custom exception class extends java.lang.Exception (line 1). The Exception class extends java.lang.Throwable. All the methods (e.g., getMessage(), toString(), and
Defining Custom Exception Classes

printStackTrace() in Exception are inherited from Throwable. The Exception class contains four constructors. Among them, the following two constructors are often used:

<table>
<thead>
<tr>
<th>java.lang.Exception</th>
</tr>
</thead>
<tbody>
<tr>
<td>+Exception()</td>
</tr>
<tr>
<td>+Exception(message: String)</td>
</tr>
</tbody>
</table>

Constructs an exception with no message. Constructs an exception with the specified message.

Line 6 invokes the superclass’s constructor with a message. This message will be set in the exception object and can be obtained by invoking getMessage() on the object.

Tip
Most exception classes in the Java API contain two constructors: a no-arg constructor and a constructor with a message parameter.
To create an InvalidRadiusException, you have to pass a radius. Therefore, the setRadius method in Listing 12.7 can be modified as shown in Listing 12.11.

LISTING 12.11  TestCircleWithCustomException.java

```java
1 public class TestCircleWithCustomException {
2   public static void main(String[] args) {
3     try {
4       new CircleWithCustomException(5);
5       new CircleWithCustomException(-5);
6       new CircleWithCustomException(0);
7     } 
8       catch (InvalidRadiusException ex) {
9         System.out.println(ex);
10     }
11     System.out.println("Number of objects created: " +
12       CircleWithCustomException.getNumberOfObjects());
13   }
14 }
15
16 class CircleWithCustomException {
17   /** The radius of the circle */
18   private double radius;
19
20   /** The number of objects created */
21   private static int numberOfObjects = 0;
22
23   /** Construct a circle with radius 1 */
24   public CircleWithCustomException() throws InvalidRadiusException { declare exception
25     this(1.0);
26   }
27
28   /** Construct a circle with a specified radius */
29   public CircleWithCustomException(double newRadius) throws InvalidRadiusException {
30     setRadius(newRadius);
31     numberOfObjects++;
32   }
33
34   /** Return radius */
35   public double getRadius() {
36     return radius;
37   }
38 }
```
The `setRadius` method in `CircleWithCustomException` throws an `InvalidRadiusException` when radius is negative (line 47). Since `InvalidRadiusException` is a checked exception, the `setRadius` method must declare it in the method header (line 43). Since the constructors for `CircleWithCustomException` invoke the `setRadius` method to set a new radius and it may throw an `InvalidRadiusException`, the constructors are declared to throw `InvalidRadiusException` (lines 25, 31).

Invoking `new CircleWithCustomException(-5)` (line 5) throws an `InvalidRadiusException`, which is caught by the handler. The handler displays the radius in the exception object `ex`.

**Tip**

Can you define a custom exception class by extending `RuntimeException`? Yes, but it is not a good way to go, because it makes your custom exception unchecked. It is better to make a custom exception checked, so that the compiler can force these exceptions to be caught in your program.

**Check Point**

12.25 How do you define a custom exception class?

12.26 Suppose the `setRadius` method throws the `InvalidRadiusException` defined in Listing 12.10. What is displayed when the following program is run?

```java
public class Test {
    public static void main(String[] args) {
        try {
            method();
            System.out.println("After the method call");
        }
        catch (RuntimeException ex) {
            System.out.println("RuntimeException in main");
        }
    }
}
```
catch (Exception ex) {
    System.out.println("Exception in main");
}

static void method() throws Exception {
    try {
        Circle c1 = new Circle(1);
        c1.setRadius(-1);
        System.out.println(c1.getRadius());
    } catch (RuntimeException ex) {
        System.out.println("RuntimeException in method()");
    } catch (Exception ex) {
        System.out.println("Exception in method()");
        throw ex;
    }
}

12.10 The File Class

The File class contains the methods for obtaining the properties of a file/directory and for renaming and deleting a file/directory.

Having learned exception handling, you are ready to step into file processing. Data stored in the program are temporary; they are lost when the program terminates. To permanently store the data created in a program, you need to save them in a file on a disk or other permanent storage device. The file can then be transported and read later by other programs. Since data are stored in files, this section introduces how to use the File class to obtain file/directory properties, to delete and rename files/directories, and to create directories. The next section introduces how to read/write data from/to text files.

Every file is placed in a directory in the file system. An absolute file name (or full name) contains a file name with its complete path and drive letter. For example, c:\book\Welcome.java is the absolute file name for the file Welcome.java on the Windows operating system. Here c:\book is referred to as the directory path for the file. Absolute file names are machine dependent. On the UNIX platform, the absolute file name may be /home/liang/book/Welcome.java, where /home/liang/book is the directory path for the file Welcome.java.

A relative file name is in relation to the current working directory. The complete directory path for a relative file name is omitted. For example, Welcome.java is a relative file name. If the current working directory is c:\book, the absolute file name would be c:\book\Welcome.java.

The File class is intended to provide an abstraction that deals with most of the machine-dependent complexities of files and path names in a machine-independent fashion. The File class contains the methods for obtaining file and directory properties and for renaming and deleting files and directories, as shown in Figure 12.6. However, the File class does not contain the methods for reading and writing file contents.

The file name is a string. The File class is a wrapper class for the file name and its directory path. For example, new File("c:\book") creates a File object for the directory c:\book, and new File("c:\book\test.dat") creates a File object for the file c:\book\test.dat, both on Windows. You can use the File class’s isDirectory() method to check whether the object represents a directory, and the isFile() method to check whether the object represents a file.
Caution

The directory separator for Windows is a backslash (`\`). The backslash is a special character in Java and should be written as `\` in a string literal (see Table 4.5).

Note

Constructing a `File` instance does not create a file on the machine. You can create a `File` instance for any file name regardless whether it exists or not. You can invoke the `exists()` method on a `File` instance to check whether the file exists.

Do not use absolute file names in your program. If you use a file name such as `c:\\book\\Welcome.java`, it will work on Windows but not on other platforms. You should use a file name relative to the current directory. For example, you may create a `File` object using `new File("Welcome.java")` for the file `Welcome.java` in the current directory. You may create a `File` object using `new File("image/us.gif")` for the file `us.gif` under the `image` directory in the current directory. The forward slash (`/`) is the Java directory separator, which
is the same as on UNIX. The statement `new File("image/us.gif")` works on Windows, UNIX, and any other platform.

Listing 12.12 demonstrates how to create a `File` object and use the methods in the `File` class to obtain its properties. The program creates a `File` object for the file `us.gif`. This file is stored under the `image` directory in the current directory.

### Listing 12.12 TestFileClass.java

```java
public class TestFileClass {
  public static void main(String[] args) {
    java.io.File file = new java.io.File("image/us.gif");
    System.out.println("Does it exist? "+ file.exists());
    System.out.println("The file has "+ file.length() + " bytes");
    System.out.println("Can it be read? "+ file.canRead());
    System.out.println("Can it be written? "+ file.canWrite());
    System.out.println("Is it a directory? "+ file.isDirectory());
    System.out.println("Is it a file? "+ file.isFile());
    System.out.println("Is it absolute? "+ file.isAbsolute());
    System.out.println("Is it hidden? "+ file.isHidden());
    System.out.println("Absolute path is "+ file.getAbsolutePath());
    System.out.println("Last modified on "+
      new java.util.Date(file.lastModified()));
  }
}
```

The `lastModified()` method returns the date and time when the file was last modified, measured in milliseconds since the beginning of UNIX time (00:00:00 GMT, January 1, 1970). The `Date` class is used to display it in a readable format in lines 14–15.

Figure 12.7a shows a sample run of the program on Windows, and Figure 12.7b, a sample run on UNIX. As shown in the figures, the path-naming conventions on Windows are different from those on UNIX.

![Sample Run on Windows](image1.png)

![Sample Run on UNIX](image2.png)

(Figure 12.7) The program creates a `File` object and displays file properties.

### 12.27 What is wrong about creating a `File` object using the following statement?

```java
new File("c:\book\test.dat");
```

### 12.28 How do you check whether a file already exists? How do you delete a file? How do you rename a file? Can you find the file size (the number of bytes) using the `File` class? How do you create a directory?

### 12.29 Can you use the `File` class for I/O? Does creating a `File` object create a file on the disk?
12.11 File Input and Output

Use the Scanner class for reading text data from a file and the PrintWriter class for writing text data to a file.

A File object encapsulates the properties of a file or a path, but it does not contain the methods for creating a file or for reading/writing data to/from a file (referred to as data input and output, or I/O for short). In order to perform I/O, you need to create objects using appropriate Java I/O classes. The objects contain the methods for reading/writing data from/to a file. There are two types of files: text and binary. This section introduces how to read/write strings and numeric values from/to a text file using the Scanner and PrintWriter classes. Binary files will be introduced in Chapter 17.

12.11.1 Writing Data Using PrintWriter

The java.io.PrintWriter class can be used to create a file and write data to a text file. First, you have to create a PrintWriter object for a text file as follows:

```java
PrintWriter output = new PrintWriter(filename);
```

Then, you can invoke the print, println, and printf methods on the PrintWriter object to write data to a file. Figure 12.8 summarizes frequently used methods in PrintWriter.

![Figure 12.8](image-url)

**Figure 12.8** The PrintWriter class contains the methods for writing data to a text file.

Listing 12.13 gives an example that creates an instance of PrintWriter and writes two lines to the file scores.txt. Each line consists of a first name (a string), a middle-name initial (a character), a last name (a string), and a score (an integer).

### Listing 12.13 WriteData.java

```java
public class WriteData {
    public static void main(String[] args) throws IOException {
        java.io.File file = new java.io.File("scores.txt");
        if (file.exists()) {
            System.out.println("File already exists");
            System.exit(1);
        }
    }
}
```

throws an exception
create File object
file exist?
Lines 4–7 check whether the file scores.txt exists. If so, exit the program (line 6).

Invoking the constructor of `PrintWriter` will create a new file if the file does not exist. If the file already exists, the current content in the file will be discarded without verifying with the user.

Invoking the constructor of `PrintWriter` may throw an I/O exception. Java forces you to write the code to deal with this type of exception. For simplicity, we declare `throws IOException` in the main method header (line 2).

You have used the `System.out.print`, `System.out.println`, and `System.out.printf` methods to write text to the console. `System.out` is a standard Java object for the console output. You can create `PrintWriter` objects for writing text to any file using `print`, `println`, and `printf` (lines 13–16).

The `close()` method must be used to close the file (line 19). If this method is not invoked, the data may not be saved properly in the file.

### 12.11.2 Closing Resources Automatically Using try-with-resources

Programmers often forget to close the file. JDK 7 provides the followings new try-with-resources syntax that automatically closes the files.

```java
try (declare and create resources) {
    Use the resource to process the file;
}
```

Using the try-with-resources syntax, we rewrite the code in Listing 12.13 in Listing 12.14.

**LISTING 12.14 WriteDataWithAutoClose.java**

```java
public class WriteDataWithAutoClose {
    public static void main(String[] args) throws Exception {
        java.io.File file = new java.io.File("scores.txt");
        if (file.exists()) {
            System.out.println("File already exists");
            System.exit(0);
        }

        try {
            // Create a file
            java.io.PrintWriter output = new java.io.PrintWriter(file);
            // Write formatted output to the file
            output.print("John T Smith ");
            output.println(90);
            output.print("Eric K Jones ");
            output.println(85);
        }
    }
}
```
A resource is declared and created followed by the keyword `try`. Note that the resources are enclosed in the parentheses (lines 9–12). The resources must be a subtype of `AutoCloseable` such as a `PrintWriter` that has the `close()` method. A resource must be declared and created in the same statement and multiple resources can be declared and created inside the parentheses. The statements in the block (lines 12–18) immediately following the resource declaration use the resource. After the block is finished, the resource’s `close()` method is automatically invoked to close the resource. Using try-with-resources can not only avoid errors but also make the code simpler.

### 12.11.3 Reading Data Using `Scanner`

The `java.util.Scanner` class was used to read strings and primitive values from the console in Section 2.3, Reading Input from the Console. A `Scanner` breaks its input into tokens delimited by whitespace characters. To read from the keyboard, you create a `Scanner` for `System.in`, as follows:

```java
Scanner input = new Scanner(System.in);
```

To read from a file, create a `Scanner` for a file, as follows:

```java
Scanner input = new Scanner(new File(filename));
```

Figure 12.9 summarizes frequently used methods in `Scanner`.

<table>
<thead>
<tr>
<th>java.util.Scanner</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>+Scanner(source: File)</td>
<td>Creates a <code>Scanner</code> that scans tokens from the specified file.</td>
</tr>
<tr>
<td>+Scanner(source: String)</td>
<td>Creates a <code>Scanner</code> that scans tokens from the specified string.</td>
</tr>
<tr>
<td>+close()</td>
<td>Closes this scanner.</td>
</tr>
<tr>
<td>+hasNext(): boolean</td>
<td>Returns true if this scanner has more data to be read.</td>
</tr>
<tr>
<td>+next(): String</td>
<td>Returns next token as a string from this scanner.</td>
</tr>
<tr>
<td>+nextLine(): String</td>
<td>Returns a line ending with the line separator from this scanner.</td>
</tr>
<tr>
<td>+nextByte(): byte</td>
<td>Returns next token as a byte from this scanner.</td>
</tr>
<tr>
<td>+nextShort(): short</td>
<td>Returns next token as a short from this scanner.</td>
</tr>
<tr>
<td>+nextInt(): int</td>
<td>Returns next token as an <code>int</code> from this scanner.</td>
</tr>
<tr>
<td>+nextLong(): long</td>
<td>Returns next token as a <code>long</code> from this scanner.</td>
</tr>
<tr>
<td>+nextFloat(): float</td>
<td>Returns next token as a <code>float</code> from this scanner.</td>
</tr>
<tr>
<td>+nextDouble(): double</td>
<td>Returns next token as a <code>double</code> from this scanner.</td>
</tr>
<tr>
<td>+useDelimiter(pattern: String): Scanner</td>
<td>Sets this scanner’s delimiting pattern and returns this scanner.</td>
</tr>
</tbody>
</table>

**Figure 12.9** The `Scanner` class contains the methods for scanning data.

Listing 12.15 gives an example that creates an instance of `Scanner` and reads data from the file `scores.txt`.

**Listing 12.15** `ReadData.java`

```java
1 import java.util.Scanner;
2 3 public class ReadData {
4     public static void main(String[] args) throws Exception {
5         // Create a File instance
6         java.io.File file = new java.io.File("scores.txt");
7 8         // Create a Scanner for the file
9         Scanner input = new Scanner(file);
```
12.11 File Input and Output

Note that `new Scanner(String)` creates a `Scanner` for a given string. To create a `Scanner` to read data from a file, you have to use the `java.io.File` class to create an instance of the `File` using the constructor `new File(filename)` (line 6), and use `new Scanner(File)` (line 9) to create a `Scanner` for the file.

Invoking the constructor `new Scanner(File)` may throw an I/O exception, so the `main` method declares `throws Exception` in line 4.

Each iteration in the `while` loop reads the first name, middle initial, last name, and score from the text file (lines 12–19). The file is closed in line 22.

It is not necessary to close the input file (line 22), but it is a good practice to do so to release the resources occupied by the file. You can rewrite this program using the try-with-resources syntax. See www.cs.armstrong.edu/liang/intro10e/html/ReadDataWithAutoClose.html.

12.11.4 How Does `Scanner` Work?

The `nextByte()`, `nextShort()`, `nextInt()`, `nextLong()`, `nextFloat()`, `nextDouble()`, and `next()` methods are known as token-reading methods, because they read tokens separated by delimiters. By default, the delimiters are whitespace characters. You can use the `useDelimiter(String regex)` method to set a new pattern for delimiters.

How does an input method work? A token-reading method first skips any delimiters (whitespace characters by default), then reads a token ending at a delimiter. The token is then automatically converted into a value of the `byte`, `short`, `int`, `long`, `float`, or `double` type for `nextByte()`, `nextShort()`, `nextInt()`, `nextLong()`, `nextFloat()`, and `nextDouble()`, respectively. For the `next()` method, no conversion is performed. If the token does not match the expected type, a runtime exception `java.util.InputMismatchException` will be thrown.

Both methods `next()` and `nextLine()` read a string. The `next()` method reads a string delimited by delimiters, and `nextLine()` reads a line ending with a line separator.

**Note**
The line-separator string is defined by the system. It is `\r\n` on Windows and `\n` on UNIX. To get the line separator on a particular platform, use

```java
String lineSeparator = System.getProperty("line.separator");
```

If you enter input from a keyboard, a line ends with the `Enter` key, which corresponds to the `\n` character.

The token-reading method does not read the delimiter after the token. If the `nextLine()` method is invoked after a token-reading method, this method reads characters that start from this delimiter and end with the line separator. The line separator is read, but it is not part of the string returned by `nextLine()`.

```java
// Read data from a file
while (input.hasNext()) {
    String firstName = input.next();
    String mi = input.next();
    String lastName = input.next();
    int score = input.nextInt();
    System.out.println(firstName + mi + lastName + score);
}
// Close the file
input.close();
```
Suppose a text file named test.txt contains a line

34 567

After the following code is executed:

```java
Scanner input = new Scanner(new File("test.txt"));
int intValue = input.nextInt();
String line = input.nextLine();
```

intValue contains 34 and line contains the characters ' ', 5, 6, and 7.

What happens if the input is entered from the keyboard? Suppose you enter 34, press the Enter key, then enter 567 and press the Enter key for the following code:

```java
Scanner input = new Scanner(System.in);
int intValue = input.nextInt();
String line = input.nextLine();
```

You will get 34 in intValue and an empty string in line. Why? Here is the reason. The token-reading method `nextInt()` reads in 34 and stops at the delimiter, which in this case is a line separator (the Enter key). The `nextLine()` method ends after reading the line separator and returns the string read before the line separator. Since there are no characters before the line separator, line is empty.

You can read data from a file or from the keyboard using the `Scanner` class. You can also scan data from a string using the `Scanner` class. For example, the following code

```java
Scanner input = new Scanner("13 14");
int sum = input.nextInt() + input.nextInt();
System.out.println("Sum is " + sum);
```

displays

The sum is 27

### 12.11.5 Case Study: Replacing Text

Suppose you are to write a program named ReplaceText that replaces all occurrences of a string in a text file with a new string. The file name and strings are passed as command-line arguments as follows:

```java
java ReplaceText sourceFile targetFile oldString newString
```

For example, invoking

```java
java ReplaceText FormatString.java t.txt StringBuilder StringBuffer
```

replaces all the occurrences of `StringBuilder` by `StringBuffer` in the file `FormatString.java` and saves the new file in `t.txt`.

Listing 12.16 gives the program. The program checks the number of arguments passed to the `main` method (lines 7–11), checks whether the source and target files exist (lines 14–25), creates a `Scanner` for the source file (line 29), creates a `PrintWriter` for the target file (line 30), and repeatedly reads a line from the source file (line 33), replaces the text (line 34), and writes a new line to the target file (line 35).

**Listing 12.16 ReplaceText.java**

```java
1 import java.io.*;
2 import java.util.*;
3
```
public class ReplaceText {
    public static void main(String[] args) throws Exception {
        // Check command line parameter usage
        if (args.length != 4) {
            System.out.println("Usage: java ReplaceText sourceFile targetFile oldStr newStr");
            System.exit(1);
        }
        // Check if source file exists
        File sourceFile = new File(args[0]);
        if (!sourceFile.exists()) {
            System.out.println("Source file " + args[0] + " does not exist");
            System.exit(2);
        }
        // Check if target file exists
        File targetFile = new File(args[1]);
        if (targetFile.exists()) {
            System.out.println("Target file " + args[1] + " already exists");
            System.exit(3);
        }
        try {
            // Create input and output files
            Scanner input = new Scanner(sourceFile);
            PrintWriter output = new PrintWriter(targetFile);
            while (input.hasNext()) {
                String s1 = input.nextLine();
                String s2 = s1.replaceAll(args[2], args[3]);
                output.println(s2);
            }
        } finally {
            // Close files
            output.close();
        }
    }
}

In a normal situation, the program is terminated after a file is copied. The program is
terminated abnormally if the command-line arguments are not used properly (lines 7–11),
if the source file does not exist (lines 14–18), or if the target file already exists (lines
22–25). The exit status code 1, 2, and 3 are used to indicate these abnormal terminations
(lines 10, 17, 24).

12.30 How do you create a PrintWriter to write data to a file? What is the reason to
declare throws Exception in the main method in Listing 12.13, WriteData.java?
What would happen if the close() method were not invoked in Listing 12.13?

12.31 Show the contents of the file temp.txt after the following program is executed.

public class Test {
    public static void main(String[] args) throws Exception {
        java.io.PrintWriter output = new java.io.PrintWriter("temp.txt");
        output.printf("amount is %f %e \n", 32.32, 32.32);
        output.printf("amount is %5.4f %5.4e \n", 32.32, 32.32);
        output.printf("%6b\n", (1 > 2));
        output.printf("%6s\n", "Java");
        output.close();
    }
}
12.32 Rewrite the code in the preceding question using a try-with-resources syntax.

12.33 How do you create a `Scanner` to read data from a file? What is the reason to define `throws Exception` in the main method in Listing 12.15, ReadData.java? What would happen if the `close()` method were not invoked in Listing 12.15?

12.34 What will happen if you attempt to create a `Scanner` for a nonexistent file? What will happen if you attempt to create a `PrintWriter` for an existing file?

12.35 Is the line separator the same on all platforms? What is the line separator on Windows?

12.36 Suppose you enter 45 57.8 789, then press the `Enter` key. Show the contents of the variables after the following code is executed.

```java
Scanner input = new Scanner(System.in);
int intValue = input.nextInt();
double doubleValue = input.nextDouble();
String line = input.nextLine();
```

12.37 Suppose you enter 45, press the `Enter` key, 57.8, press the `Enter` key, 789, and press the `Enter` key. Show the contents of the variables after the following code is executed.

```java
Scanner input = new Scanner(System.in);
int intValue = input.nextInt();
double doubleValue = input.nextDouble();
String line = input.nextLine();
```

12.12 Reading Data from the Web

*Key Point*

Just like you can read data from a file on your computer, you can read data from a file on the Web.

In addition to reading data from a local file on a computer or file server, you can also access data from a file that is on the Web if you know the file’s URL (Uniform Resource Locator—the unique address for a file on the Web). For example, `www.google.com/index.html` is the URL for the file `index.html` located on the Google Web server. When you enter the URL in a Web browser, the Web server sends the data to your browser, which renders the data graphically. Figure 12.10 illustrates how this process works.

![Figure 12.10](image)

**Figure 12.10** The client retrieves files from a Web server.

For an application program to read data from a URL, you first need to create a `URL` object using the `java.net.URL` class with this constructor:

```java
public URL(String spec) throws MalformedURLException
```

For example, the following statement creates a URL object for `http://www.google.com/index.html`.

```java
try {
    URL url = new URL("http://www.google.com/index.html");
} 
```
A `MalformedURLException` is thrown if the URL string has a syntax error. For example, the URL string “http://www.google.com/index.html” would cause a `MalformedURLException` runtime error because two slashes (//) are required after the colon (:). Note that the http:// prefix is required for the `URL` class to recognize a valid URL. It would be wrong if you replace line 2 with the following code:

```java
URL url = new URL("www.google.com/index.html");
```

After a `URL` object is created, you can use the `openStream()` method defined in the `URL` class to open an input stream and use this stream to create a `Scanner` object as follows:

```java
Scanner input = new Scanner(url.openStream());
```

Now you can read the data from the input stream just like from a local file. The example in Listing 12.17 prompts the user to enter a URL and displays the size of the file.

**LISTING 12.17  ReadFileFromURL.java**

```java
import java.util.Scanner;

public class ReadFileFromURL {
    public static void main(String[] args) {
        System.out.print("Enter a URL: ");
        String URLString = new Scanner(System.in).next();

        try {
            java.net.URL url = new java.net.URL(URLString);
            int count = 0;
            Scanner input = new Scanner(url.openStream());
            while (input.hasNext()) {
                String line = input.nextLine();
                count += line.length();
            }
            System.out.println("The file size is "+ count + " characters");
        }
        catch (java.net.MalformedURLException ex) {
            System.out.println("Invalid URL");
        }
        catch (java.io.IOException ex) {
            System.out.println("I/O Errors: no such file");
        }
    }
}
```

Enter a URL: http://cs.armstrong.edu/liang/data/Lincoln.txt
The file size is 1469 characters

Enter a URL: http://www.yahoo.com
The file size is 190006 characters
The program prompts the user to enter a URL string (line 6) and creates a URL object (line 9). The constructor will throw a java.net.MalformedURLException (line 19) if the URL isn’t formed correctly.

The program creates a Scanner object from the input stream for the URL (line 11). If the URL is formed correctly but does not exist, an IOException will be thrown (line 22). For example, http://google.com/index1.html uses the appropriate form, but the URL itself does not exist. An IOException would be thrown if this URL was used for this program.

**Check Point**

12.38 How do you create a Scanner object for reading text from a URL?

**12.13 Case Study: Web Crawler**

This case study develops a program that travels the Web by following hyperlinks.

The World Wide Web, abbreviated as WWW, W3, or Web, is a system of interlinked hypertext documents on the Internet. With a Web browser, you can view a document and follow the hyperlinks to view other documents. In this case study, we will develop a program that automatically traverses the documents on the Web by following the hyperlinks. This type of program is commonly known as a Web crawler. For simplicity, our program follows for the hyperlink that starts with http://. Figure 12.11 shows an example of traversing the Web. We start from a Web page that contains three URLs named URL1, URL2, and URL3. Following URL1 leads to the page that contains three URLs named URL11, URL12, and URL13. Following URL2 leads to the page that contains two URLs named URL21 and URL22. Following URL3 leads to the page that contains four URLs named URL31, URL32, URL33, and URL34. Continue to traverse the Web following the new hyperlinks. As you see, this process may continue forever, but we will exit the program once we have traversed 100 pages.

![Figure 12.11](Image)

The program follows the URLs to traverse the Web. To ensure that each URL is traversed only once, the program maintains two lists of URLs. One list stores the URLs pending for traversing and the other stores the URLs that have already been traversed. The algorithm for this program can be described as follows:

Add the starting URL to a list named listOfPendingURLs; while listOfPendingURLs is not empty and size of listOfTraversedURLs <= 100 {

...
Listing 12.18 gives the program that implements this algorithm.

**LISTING 12.18  WebCrawler.java**

```java
import java.util.Scanner;
import java.util.ArrayList;

public class WebCrawler {
    public static void main(String[] args) {
        java.util.Scanner input = new java.util.Scanner(System.in);
        System.out.print("Enter a URL: ");
        String url = input.nextLine();
        crawler(url); // Traverse the Web from the a starting url
    }

    public static void crawler(String startingURL) {
        ArrayList<String> listOfPendingURLs = new ArrayList<>();
        ArrayList<String> listOfTraversedURLs = new ArrayList<>();
        listOfPendingURLs.add(startingURL);

        while (!listOfPendingURLs.isEmpty() &&
            listOfTraversedURLs.size() <= 100) {
            String urlString = listOfPendingURLs.remove(0);
            if (!listOfTraversedURLs.contains(urlString)) {
                listOfTraversedURLs.add(urlString);
                System.out.println("Craw "+ urlString);
                for (String s: getSubURLs(urlString)) {
                    if (!listOfTraversedURLs.contains(s)) {
                        listOfPendingURLs.add(s);
                    }
                }
            }
        }
    }

    public static ArrayList<String> getSubURLs(String urlString) {
        ArrayList<String> list = new ArrayList<>();
        try {
            java.net.URL url = new java.net.URL(urlString);
            Scanner input = new Scanner(url.openStream());
            int current = 0;
            while (input.hasNext()) {
                String line = input.nextLine();
                current = line.indexOf("http:", current);
                while (current > 0) {
                    int endIndex = line.indexOf("\", current);
                    if (endIndex > 0) { // Ensure that a correct URL is found
                        list.add(line.substring(current, endIndex));
                        current = line.indexOf("http:", endIndex);
                    }
                }
            }
        } catch (Exception e) {
            e.printStackTrace();
        }
        return list;
```
The program prompts the user to enter a starting URL (lines 7–8) and invokes the `crawler(url)` method to traverse the web (line 9).

The `crawler(url)` method adds the starting url to `listOfPendingURLs` (line 16) and repeatedly processes each URL in `listOfPendingURLs` in a while loop (lines 17–29). It removes the first URL in the list (line 19) and processes the URL if it has not been processed (lines 20–28). To process each URL, the program first adds the URL to `listOfTraversedURLs` (line 21). This list stores all the URLs that have been processed. The `getSubURLs(url)` method returns a list of URLs in the Web page for the specified URL (line 24). The program uses a foreach loop to add each URL in the page into `listOfPendingURLs` if it is not in `listOfTraversedURLs` (lines 24–26).

The `getSubURLs(url)` method reads each line from the Web page (line 40) and searches for the URLs in the line (line 41). Note that a correct URL cannot contain line break characters. So it is sufficient to limit the search for a URL in one line of the text in a Web page. For simplicity, we assume that a URL ends with a quotation mark " (line 43). The method obtains a URL and adds it to a list (line 45). A line may contain multiple URLs. The method continues to search for the next URL (line 46). If no URL is found in the line, `current` is set to -1 (line 49). The URLs contained in the page are returned in the form of a list (line 57).

The program terminates when the number of traversed URLs reaches to 100 (line 18). This is a simple program to traverse the Web. Later you will learn the techniques to make the program more efficient and robust.

**Check Point**

12.39 Before a URL is added to `listOfPendingURLs`, line 25 checks whether it has been traversed. Is it possible that `listOfPendingURLs` contains duplicate URLs? If so, give an example.

### Key Terms

- absolute file name 473
- chained exception 469
- checked exception 457
- declare exception 458
- directory path 473
- exception 450
- exception propagation 459
- relative file name 473
- throw exception 452
- unchecked exception 457
**Chapter Summary**

1. Exception handling enables a method to throw an exception to its caller.

2. A Java *exception* is an instance of a class derived from `java.lang.Throwable`. Java provides a number of predefined exception classes, such as `Error`, `Exception`, `RuntimeException`, `ClassNotFoundException`, `NullPointerException`, and `ArithmeticException`. You can also define your own exception class by extending `Exception`.

3. Exceptions occur during the execution of a method. `RuntimeException` and `Error` are *unchecked exceptions*; all other exceptions are *checked*.

4. When declaring a method, you have to declare a checked exception if the method might throw it, thus telling the compiler what can go wrong.

5. The keyword for declaring an exception is `throws`, and the keyword for throwing an exception is `throw`.

6. To invoke the method that declares checked exceptions, enclose it in a `try` statement. When an exception occurs during the execution of the method, the `catch` block catches and handles the exception.

7. If an exception is not caught in the current method, it is passed to its caller. The process is repeated until the exception is caught or passed to the `main` method.

8. Various exception classes can be derived from a common superclass. If a `catch` block catches the exception objects of a superclass, it can also catch all the exception objects of the subclasses of that superclass.

9. The order in which exceptions are specified in a `catch` block is important. A compile error will result if you specify an exception object of a class after an exception object of the superclass of that class.

10. When an exception occurs in a method, the method exits immediately if it does not catch the exception. If the method is required to perform some task before exiting, you can catch the exception in the method and then rethrow it to its caller.

11. The code in the `finally` block is executed under all circumstances, regardless of whether an exception occurs in the `try` block or whether an exception is caught if it occurs.

12. Exception handling separates error-handling code from normal programming tasks, thus making programs easier to read and to modify.

13. Exception handling should not be used to replace simple tests. You should perform simple test using `if` statements whenever possible, and reserve exception handling for dealing with situations that cannot be handled with `if` statements.

14. The `File` class is used to obtain file properties and manipulate files. It does not contain the methods for creating a file or for reading/writing data from/to a file.

15. You can use `Scanner` to read string and primitive data values from a text file and use `PrintWriter` to create a file and write data to a text file.

16. You can read from a file on the Web using the `URL` class.
Quiz

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

Programming Exercises

Sections 12.2–12.9

*12.1 (NumberFormatException) Listing 7.9, Calculator.java, is a simple command-line calculator. Note that the program terminates if any operand is nonnumeric. Write a program with an exception handler that deals with nonnumeric operands; then write another program without using an exception handler to achieve the same objective. Your program should display a message that informs the user of the wrong operand type before exiting (see Figure 12.12).

*12.2 (InputMismatchException) Write a program that prompts the user to read two integers and displays their sum. Your program should prompt the user to read the number again if the input is incorrect.

*12.3 (ArrayIndexOutOfBoundsException) Write a program that meets the following requirements:

- Creates an array with 100 randomly chosen integers.
- Prompts the user to enter the index of the array, then displays the corresponding element value. If the specified index is out of bounds, display the message Out of Bounds.

*12.4 (IllegalArgumentException) Modify the Loan class in Listing 10.2 to throw IllegalArgumentException if the loan amount, interest rate, or number of years is less than or equal to zero.

*12.5 (IllegalTriangleException) Programming Exercise 11.1 defined the Triangle class with three sides. In a triangle, the sum of any two sides is greater than the other side. The Triangle class must adhere to this rule. Create the IllegalTriangleException class, and modify the constructor of the Triangle class to throw an IllegalTriangleException object if a triangle is created with sides that violate the rule, as follows:

```java
/** Construct a triangle with the specified sides */
public Triangle(double side1, double side2, double side3) throws IllegalTriangleException {
    // Implement it
}
```
*12.6 *(NumberFormatException) Listing 6.8 implements the `hex2Dec(String hexString)` method, which converts a hex string into a decimal number. Implement the `hex2Dec` method to throw a `NumberFormatException` if the string is not a hex string.

*12.7 *(NumberFormatException) Write the `bin2Dec(String binaryString)` method to convert a binary string into a decimal number. Implement the `bin2Dec` method to throw a `NumberFormatException` if the string is not a binary string.

*12.8 *(HexFormatException) Exercise 12.6 implements the `hex2Dec` method to throw a `NumberFormatException` if the string is not a hex string. Define a custom exception called `HexFormatException`. Implement the `hex2Dec` method to throw a `HexFormatException` if the string is not a hex string.

*12.9 *(BinaryFormatException) Exercise 12.7 implements the `bin2Dec` method to throw a `BinaryFormatException` if the string is not a binary string. Define a custom exception called `BinaryFormatException`. Implement the `bin2Dec` method to throw a `BinaryFormatException` if the string is not a binary string.

*12.10 *(OutOfMemoryError) Write a program that causes the JVM to throw an `OutOfMemoryError` and catches and handles this error.

Sections 12.10–12.12

**12.11 *(Remove text) Write a program that removes all the occurrences of a specified string from a text file. For example, invoking

```
java Exercise12_11 John filename
```

removes the string `John` from the specified file. Your program should get the arguments from the command line.

**12.12 *(Reformat Java source code) Write a program that converts the Java source code from the next-line brace style to the end-of-line brace style. For example, the following Java source in (a) uses the next-line brace style. Your program converts it to the end-of-line brace style in (b).

(a) Next-line brace style

```
public class Test {
    public static void main(String[] args) {
        // Some statements
    }
}
```

(b) End-of-line brace style

```
public class Test {
    public static void main(String[] args) {
        // Some statements
    }
}
```

Your program can be invoked from the command line with the Java source-code file as the argument. It converts the Java source code to a new format. For example, the following command converts the Java source-code file `Test.java` to the end-of-line brace style.

```
java Exercise12_12 Test.java
```

*12.13 *(Count characters, words, and lines in a file) Write a program that will count the number of characters, words, and lines in a file. Words are separated by whitespace characters. The file name should be passed as a command-line argument, as shown in Figure 12.13.
12.14 (Process scores in a text file) Suppose that a text file contains an unspecified number of scores separated by blanks. Write a program that prompts the user to enter the file, reads the scores from the file, and displays their total and average.

12.15 (Write/read data) Write a program to create a file named Exercise12_15.txt if it does not exist. Write 100 integers created randomly into the file using text I/O. Integers are separated by spaces in the file. Read the data back from the file and display the data in increasing order.

12.16 (Replace text) Listing 12.16, ReplaceText.java, gives a program that replaces text in a source file and saves the change into a new file. Revise the program to save the change into the original file. For example, invoking

```
java Exercise12_16 file oldString newString
```

replaces oldString in the source file with newString.

12.17 (Game: hangman) Rewrite Programming Exercise 7.35. The program reads the words stored in a text file named hangman.txt. Words are delimited by spaces.

12.18 (Add package statement) Suppose you have Java source files under the directories chapter1, chapter2,..., chapter34. Write a program to insert the statement `package chapteri;` as the first line for each Java source file under the directory chapteri. Suppose chapter1, chapter2,..., chapter34 are under the root directory srcRootDirectory. The root directory and chapteri directory may contain other folders and files. Use the following command to run the program:

```
java Exercise12_18 srcRootDirectory
```

12.19 (Count words) Write a program that counts the number of words in President Abraham Lincoln’s Gettysburg address from http://cs.armstrong.edu/liang/data/Lincoln.txt.

12.20 (Remove package statement) Suppose you have Java source files under the directories chapter1, chapter2,..., chapter34. Write a program to remove the statement `package chapteri;` in the first line for each Java source file under the directory chapteri. Suppose chapter1, chapter2,..., chapter34 are under the root directory srcRootDirectory. The root directory and chapteri directory may contain other folders and files. Use the following command to run the program:

```
java Exercise12_20 srcRootDirectory
```

12.21 (Data sorted?) Write a program that reads the strings from file SortedStrings.txt and reports whether the strings in the files are stored in increasing order.
**12.22 ***(Replace text)*** Revise Programming Exercise 12.16 to replace a string in a file with a new string for all files in the specified directory using the command:

```
java Exercise12_22 dir oldString newString
```

**12.23 ***(Process scores in a text file on the Web)*** Suppose that the text file on the Web [http://cs.armstrong.edu/liang/data/Scores.txt](http://cs.armstrong.edu/liang/data/Scores.txt) contains an unspecified number of scores. Write a program that reads the scores from the file and displays their total and average. Scores are separated by blanks.

**12.24 ***(Create large dataset)*** Create a data file with 1,000 lines. Each line in the file consists of a faculty member’s first name, last name, rank, and salary. The faculty member’s first name and last name for the i-th line are FirstName \(_i\) and LastName \(_i\). The rank is randomly generated as assistant, associate, and full. The salary is randomly generated as a number with two digits after the decimal point. The salary for an assistant professor should be in the range from 50,000 to 80,000, for associate professor from 60,000 to 110,000, and for full professor from 75,000 to 130,000. Save the file in Salary.txt. Here are some sample data:

FirstName1 LastName1 assistant 60055.95
FirstName2 LastName2 associate 81112.45

... 
FirstName1000 LastName1000 full 92255.21

**12.25 ***(Process large dataset)*** A university posts its employees’ salaries at [http://cs.armstrong.edu/liang/data/Salary.txt](http://cs.armstrong.edu/liang/data/Salary.txt). Each line in the file consists of a faculty member’s first name, last name, rank, and salary (see Programming Exercise 12.24). Write a program to display the total salary for assistant professors, associate professors, full professors, and all faculty, respectively, and display the average salary for assistant professors, associate professors, full professors, and all faculty, respectively.

**12.26 ***(Create a directory)*** Write a program that prompts the user to enter a directory name and creates a directory using the File's `mkdirs` method. The program displays the message “Directory created successfully” if a directory is created or “Directory already exists” if the directory already exists.

**12.27 ***(Replace words)*** Suppose you have a lot of files in a directory that contain words `Exercise_i_j`, where i and j are digits. Write a program that pads a 0 before i if i is a single digit and 0 before j if j is a single digit. For example, the word `Exercise2_1` in a file will be replaced by `Exercise02_01`. In Java, when you pass the symbol * from the command line, it refers to all files in the directory (see Supplement III.V). Use the following command to run your program.

```
java Exercise12_27 *
```

**12.28 ***(Rename files)*** Suppose you have a lot of files in a directory named `Exercise_i_j`, where i and j are digits. Write a program that pads a 0 before i if i is a single digit. For example, a file named `Exercise2_1` in a directory will be renamed to `Exercise02_1`. In Java, when you pass the symbol * from the command line, it refers to all files in the directory (see Supplement III.V). Use the following command to run your program.

```
java Exercise12_28 *
```
12.29 (Rename files) Suppose you have a lot of files in a directory named Exercise\textsubscript{i} \_\textsubscript{j}, where \(i\) and \(j\) are digits. Write a program that pads a 0 before \(j\) if \(j\) is a single digit. For example, a file named Exercise\textsubscript{2} \_\textsubscript{1} in a directory will be renamed to Exercise\textsubscript{2} \_\textsubscript{01}. In Java, when you pass the symbol * from the command line, it refers to all files in the directory (see Supplement III.V). Use the following command to run your program.

```
java Exercise12_29 *
```

12.30 (Occurrences of each letter) Write a program that prompts the user to enter a file name and displays the occurrences of each letter in the file. Letters are case-insensitive. Here is a sample run:

```
Enter a filename: Lincoln.txt
Number of A's: 56
Number of B's: 134
...  
Number of Z's: 9
```

12.31 (Baby name popularity ranking) The popularity ranking of baby names from years 2001 to 2010 is downloaded from www.ssa.gov/oact/babynames and stored in files named babynameranking2001.txt, babynameranking2002.txt, . . . , babynameranking2010.txt. Each file contains one thousand lines. Each line contains a ranking, a boy’s name, number for the boy’s name, a girl’s name, and number for the girl’s name. For example, the first two lines in the file babynameranking2010.txt are as follows:

```
1    Jacob  21,875    Isabella  22,731
2    Ethan  17,866   Sophia    20,477
```

So, the boy’s name Jacob and girl’s name Isabella are ranked #1 and the boy’s name Ethan and girl’s name Sophia are ranked #2. 21,875 boys are named Jacob and 22,731 girls are named Isabella. Write a program that prompts the user to enter the year, gender, and followed by a name, and displays the ranking of the name for the year. Here is a sample run:

```
Enter the year: 2010
Enter the gender: M
Enter the name: Javier
Javier is ranked #190 in year 2010
```

```
Enter the year: 2010
Enter the gender: F
Enter the name: ABC
The name ABC is not ranked in year 2010
```
*12.32  (*Ranking summary*) Write a program that uses the files described in Programming Exercise 12.31 and displays a ranking summary table for the first five girl’s and boy’s names as follows:

<table>
<thead>
<tr>
<th>Year</th>
<th>Rank 1</th>
<th>Rank 2</th>
<th>Rank 3</th>
<th>Rank 4</th>
<th>Rank 5</th>
<th>Rank 1</th>
<th>Rank 2</th>
<th>Rank 3</th>
<th>Rank 4</th>
<th>Rank 5</th>
</tr>
</thead>
<tbody>
<tr>
<td>2010</td>
<td>Isabella</td>
<td>Sophia</td>
<td>Emma</td>
<td>Olivia</td>
<td>Ava</td>
<td>Jacob</td>
<td>Ethan</td>
<td>Michael</td>
<td>Jayden</td>
<td>William</td>
</tr>
<tr>
<td>2009</td>
<td>Isabella</td>
<td>Emma</td>
<td>Olivia</td>
<td>Sophia</td>
<td>Ava</td>
<td>Jacob</td>
<td>Ethan</td>
<td>Michael</td>
<td>Alexander</td>
<td>William</td>
</tr>
<tr>
<td>...</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>2001</td>
<td>Emily</td>
<td>Madison</td>
<td>Hannah</td>
<td>Ashley</td>
<td>Alexis</td>
<td>Jacob</td>
<td>Michael</td>
<td>Matthew</td>
<td>Joshua</td>
<td>Christopher</td>
</tr>
</tbody>
</table>

**12.33  (*Search Web*) Modify Listing 12.18 WebCrawler.java to search for the word *Computer Programming* starting from the URL http://cs.armstrong.edu/liang. Your program terminates once the word is found. Display the URL for the page that contains the word.
Abstract Classes and Interfaces

Objectives

- To design and use abstract classes (§13.2).
- To generalize numeric wrapper classes, `BigInteger`, and `BigDecimal` using the abstract `Number` class (§13.3).
- To process a calendar using the `Calendar` and `GregorianCalendar` classes (§13.4).
- To specify common behavior for objects using interfaces (§13.5).
- To define interfaces and define classes that implement interfaces (§13.5).
- To define a natural order using the `Comparable` interface (§13.6).
- To make objects cloneable using the `Cloneable` interface (§13.7).
- To explore the similarities and differences among concrete classes, abstract classes, and interfaces (§13.8).
- To design the `Rational` class for processing rational numbers (§13.9).
- To design classes that follow the class-design guidelines (§13.10).
13.1 Introduction

A superclass defines common behavior for related subclasses. An interface can be used to define common behavior for classes (including unrelated classes).

You can use the java.util.Arrays.sort method to sort an array of numbers or strings. Can you apply the same sort method to sort an array of geometric objects? In order to write such code, you have to know about interfaces. An interface is for defining common behavior for classes (including unrelated classes). Before discussing interfaces, we introduce a closely related subject: abstract classes.

13.2 Abstract Classes

An abstract class cannot be used to create objects. An abstract class can contain abstract methods, which are implemented in concrete subclasses.

In the inheritance hierarchy, classes become more specific and concrete with each new subclass. If you move from a subclass back up to a superclass, the classes become more general and less specific. Class design should ensure that a superclass contains common features of its subclasses. Sometimes a superclass is so abstract that it cannot be used to create any specific instances. Such a class is referred to as an abstract class.

In Chapter 11, GeometricObject was defined as the superclass for Circle and Rectangle. GeometricObject models common features of geometric objects. Both Circle and Rectangle contain the getArea() and getPerimeter() methods for computing the area and perimeter of a circle and a rectangle. Since you can compute areas and perimeters for all geometric objects, it is better to define the getArea() and getPerimeter() methods in the GeometricObject class. However, these methods cannot be implemented in the GeometricObject class, because their implementation depends on the specific type of geometric object. Such methods are referred to as abstract methods and are denoted using the abstract modifier in the method header. After you define the methods in GeometricObject, it becomes an abstract class. Abstract classes are denoted using the abstract modifier in the class header. In UML graphic notation, the names of abstract classes and their abstract methods are italicized, as shown in Figure 13.1. Listing 13.1 gives the source code for the new GeometricObject class.

**LISTING 13.1 GeometricObject.java**

```java
public abstract class GeometricObject {
  private String color = "white";
  private boolean filled;
  private java.util.Date dateCreated;

  /** Construct a default geometric object */
  protected GeometricObject() {
    dateCreated = new java.util.Date();
  }

  /** Construct a geometric object with color and filled value */
  protected GeometricObject(String color, boolean filled) {
    dateCreated = new java.util.Date();
    this.color = color;
    this.filled = filled;
  }

  /** Return color */
  public String getColor() {
    return color;
  }
```


Abstract class name is italicized

The # sign indicates protected modifier

Abstract methods are italicized

Methods `getArea` and `getPerimeter` are overridden in `Circle` and `Rectangle`. Superclass methods are generally omitted in the UML diagram for subclasses.

---

**Figure 13.1** The new `GeometricObject` class contains abstract methods.

```java
21 } 22 23 /** Set a new color */ 24 public void setColor(String color) { 25 this.color = color; 26 } 27 28 /** Return filled. Since filled is boolean, 29 * the get method is named isFilled */ 30 public boolean isFilled() { 31 return filled; 32 } 33 34 /** Set a new filled */ 35 public void setFilled(boolean filled) { 36 this.filled = filled; 37 } 38 39 /** Get dateCreated */ 40 public java.util.Date getDateCreated() { 41 return dateCreated; 42 }
```
13.2 Why Abstract Methods?

You may be wondering what advantage is gained by defining the methods `getArea()` and `getPerimeter()` as abstract in the `GeometricObject` class. The example in Listing 13.4 shows the benefits of defining them in the `GeometricObject` class. The program creates two geometric objects, a circle and a rectangle, invokes the `equalArea` method to check whether they have equal areas, and invokes the `displayGeometricObject` method to display them.

**LISTING 13.4 TestGeometricObject.java**

```java
1 public class TestGeometricObject {
2     /** Main method */
3     public static void main(String[] args) {
4         // Create two geometric objects
5         GeometricObject geoObject1 = new Circle(5);
6         GeometricObject geoObject2 = new Rectangle(5, 3);
7     }
8 }
```
13.2 Abstract Classes

7 System.out.println("The two objects have the same area? "+
8 equalArea(geoObject1, geoObject2));
9
10 // Display circle
11 displayGeometricObject(geoObject1);
12
13 // Display rectangle
14 displayGeometricObject(geoObject2);
15 }
16
17 /** A method for comparing the areas of two geometric objects */
18 public static boolean equalArea(GeometricObject object1,
19 GeometricObject object2) {
20 return object1.getArea() == object2.getArea();
21 }
22
23 /** A method for displaying a geometric object */
24 public static void displayGeometricObject(GeometricObject object) {
25 System.out.println();
26 System.out.println("The area is " + object.getArea());
27 System.out.println("The perimeter is " + object.getPerimeter());
28 }
29 }
30 }

The two objects have the same area? false

The area is 78.53981633974483
The perimeter is 31.41592653589793

The area is 13.0
The perimeter is 16.0

The methods getArea() and getPerimeter() defined in the GeometricObject class are overridden in the Circle class and the Rectangle class. The statements (lines 5–6)

    GeometricObject geoObject1 = new Circle(5);
    GeometricObject geoObject2 = new Rectangle(5, 3);

create a new circle and rectangle and assign them to the variables geoObject1 and geoObject2. These two variables are of the GeometricObject type. When invoking equalArea(geoObject1, geoObject2) (line 9), the getArea() method defined in the Circle class is used for object1.getArea(), since geoObject1 is a circle, and the getArea() method defined in the Rectangle class is used for object2.getArea(), since geoObject2 is a rectangle.

Similarly, when invoking displayGeometricObject(geoObject1) (line 12), the methods getArea() and getPerimeter() defined in the Circle class are used, and when invoking displayGeometricObject(geoObject2) (line 15), the methods getArea and getPerimeter defined in the Rectangle class are used. The JVM dynamically determines which of these methods to invoke at runtime, depending on the actual object that invokes the method.

Note that you could not define the equalArea method for comparing whether two geometric objects have the same area if the getArea method were not defined in GeometricObject. Now you have seen the benefits of defining the abstract methods in GeometricObject. why abstract methods?
13.2.2 Interesting Points about Abstract Classes

The following points about abstract classes are worth noting:

- An abstract method cannot be contained in a nonabstract class. If a subclass of an abstract superclass does not implement all the abstract methods, the subclass must be defined as abstract. In other words, in a nonabstract subclass extended from an abstract class, all the abstract methods must be implemented. Also note that abstract methods are nonstatic.

- An abstract class cannot be instantiated using the `new` operator, but you can still define its constructors, which are invoked in the constructors of its subclasses. For instance, the constructors of `GeometricObject` are invoked in the `Circle` class and the `Rectangle` class.

- A class that contains abstract methods must be abstract. However, it is possible to define an abstract class that doesn’t contain any abstract methods. In this case, you cannot create instances of the class using the `new` operator. This class is used as a base class for defining subclasses.

- A subclass can override a method from its superclass to define it as abstract. This is very unusual, but it is useful when the implementation of the method in the superclass becomes invalid in the subclass. In this case, the subclass must be defined as abstract.

- A subclass can be abstract even if its superclass is concrete. For example, the `Object` class is concrete, but its subclasses, such as `GeometricObject`, may be abstract.

- You cannot create an instance from an abstract class using the `new` operator, but an abstract class can be used as a data type. Therefore, the following statement, which creates an array whose elements are of the `GeometricObject` type, is correct.

```java
GeometricObject[] objects = new GeometricObject[10];
```

You can then create an instance of `GeometricObject` and assign its reference to the array like this:

```java
objects[0] = new Circle();
```

13.1 Which of the following classes defines a legal abstract class?

- (a) `public class abstract A { abstract void unfinished(); }
- (b) `class A { abstract void unfinished() { }
- (c) `class A { abstract void unfinished();
- (d) `abstract class A { protected void unfinished();
- (e) `abstract class A { abstract void unfinished();
- (f) `abstract class A { abstract int unfinished();`
13.2 The `getArea()` and `getPerimeter()` methods may be removed from the `GeometricObject` class. What are the benefits of defining `getArea()` and `getPerimeter()` as abstract methods in the `GeometricObject` class?

13.3 True or false?

a. An abstract class can be used just like a nonabstract class except that you cannot use the `new` operator to create an instance from the abstract class.
b. An abstract class can be extended.
c. A subclass of a nonabstract superclass cannot be abstract.
d. A subclass cannot override a concrete method in a superclass to define it as abstract.
e. An abstract method must be nonstatic.

13.3 Case Study: the Abstract `Number` Class

`Number` is an abstract superclass for numeric wrapper classes, `BigInteger`, and `BigDecimal`.

Section 10.7 introduced numeric wrapper classes and Section 10.9 introduced the `BigInteger` and `BigDecimal` classes. These classes have common methods `byteValue()`, `shortValue()`, `intValue()`, `longValue()`, `floatValue()`, and `doubleValue()` for returning a `byte`, `short`, `int`, `long`, `float`, and `double` value from an object of these classes. These common methods are actually defined in the `Number` class, which is a superclass for the numeric wrapper classes, `BigInteger`, and `BigDecimal`, as shown in Figure 13.2.

![Diagram of the hierarchy of numeric classes](https://example.com/diagram)

**FIGURE 13.2** The `Number` class is an abstract superclass for `Double`, `Float`, `Long`, `Integer`, `Short`, `Byte`, `BigInteger`, and `BigDecimal`.

Since the `intValue()`, `longValue()`, `floatValue()`, and `doubleValue()` methods cannot be implemented in the `Number` class, they are defined as abstract methods in the `Number` class. The `Number` class is therefore an abstract class. The `byteValue()` and `shortValue()` method are implemented from the `intValue()` method as follows:

```java
public byte byteValue() {
    return (byte)intValue();
}

public short shortValue() {
    return (short)intValue();
}
```
With `Number` defined as the superclass for the numeric classes, we can define methods to perform common operations for numbers. Listing 13.5 gives a program that finds the largest number in a list of `Number` objects.

**Listing 13.5  LargestNumbers.java**

```java
import java.util.ArrayList;
import java.math.*;

public class LargestNumbers {
    public static void main(String[] args) {
        ArrayList<Number> list = new ArrayList<>();
        list.add(45); // Add an integer
        list.add(3445.53); // Add a double
        list.add(new BigInteger("3432323234344343101"); // Add a BigInteger
        list.add(new BigDecimal("2.0909090989091343433344343");
        System.out.println("The largest number is " + getLargestNumber(list));
    }

    public static Number getLargestNumber(ArrayList<Number> list) {
        if (list == null || list.size() == 0)
            return null;
        Number number = list.get(0);
        for (int i = 1; i < list.size(); i++)
            if (number.doubleValue() < list.get(i).doubleValue())
                number = list.get(i);
        return number;
    }
}
```

The program creates an `ArrayList` of `Number` objects (line 6). It adds an `Integer` object, a `Double` object, a `BigInteger` object, and a `BigDecimal` object to the list (lines 7–12). Note that `45` is automatically converted into an `Integer` object and added to the list in line 7 and that `3445.53` is automatically converted into a `Double` object and added to the list in line 8 using autoboxing.

Invoking the `getLargestNumber` method returns the largest number in the list (line 15). The `getLargestNumber` method returns `null` if the list is `null` or the list size is `0` (lines 19–20). To find the largest number in the list, the numbers are compared by invoking their `doubleValue()` method (line 24). The `doubleValue()` method is defined in the `Number` class and implemented in the concrete subclass of `Number`. If a number is an `Integer` object, the `Integer's doubleValue()` is invoked. If a number is a `BigDecimal` object, the `BigDecimal's doubleValue()` is invoked.

If the `doubleValue()` method were not defined in the `Number` class, you will not be able to find the largest number among different types of numbers using the `Number` class.

**Check Point**

13.4 Why do the following two lines of code compile but cause a runtime error?

```java
Number numberRef = new Integer(0);
Double doubleRef = (Double)numberRef;
```
13.4 Case Study: Calendar and GregorianCalendar

GregorianCalendar is a concrete subclass of the abstract class Calendar.

An instance of java.util.Date represents a specific instant in time with millisecond precision. java.util.Calendar is an abstract base class for extracting detailed calendar information, such as the year, month, date, hour, minute, and second. Subclasses of Calendar can implement specific calendar systems, such as the Gregorian calendar, the lunar calendar, and the Jewish calendar. Currently, java.util.GregorianCalendar for the Gregorian calendar is supported in Java, as shown in Figure 13.3. The add method is abstract in the Calendar class, because its implementation is dependent on a concrete calendar system.

You can use new GregorianCalendar() to construct a default GregorianCalendar with the current time and new GregorianCalendar(year, month, date) to construct a GregorianCalendar with the specified year, month, and date. The month parameter is 0 based—that is, 0 is for January.

The get(int field) method defined in the Calendar class is useful for extracting the date and time information from a Calendar object. The fields are defined as constants, as shown in Table 13.1.

Listing 13.6 gives an example that displays the date and time information for the current time.
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FIGURE 13.3  The abstract Calendar class defines common features of various calendars.

```
java.util.Calendar

#Calendar()
+get(field: int): int
+set(field: int, value: int): void
+set(year: int, month: int, dayOfMonth: int): void
+getActualMaximum(field: int): int
+add(field: int, amount: int): void
+getTime(): java.util.Date
+setTime(date: java.util.Date): void

java.util.GregorianCalendar

+GregorianCalendar()
+GregorianCalendar(year: int, month: int, dayOfMonth: int)
+GregorianCalendar(year: int, month: int, dayOfMonth: int, hour:int, minute: int, second: int)

Constructs a default calendar.
Returns the value of the given calendar field.
Sets the given calendar to the specified value.
Sets the calendar with the specified year, month, and date. The month parameter is 0-based; that is, 0 is for January.
Returns the maximum value that the specified calendar field could have.
Adds or subtracts the specified amount of time to the given calendar field.
Returns a Date object representing this calendar’s time value (million second offset from the UNIX epoch).
Sets this calendar’s time with the given Date object.

Constructs a GregorianCalendar for the current time.
Constructs a GregorianCalendar for the specified year, month, and date.
Constructs a GregorianCalendar for the specified year, month, date, hour, minute, and second. The month parameter is 0-based, that is, 0 is for January.
```

#Calendar()
+get(field: int): int
+set(field: int, value: int): void
+set(year: int, month: int, dayOfMonth: int): void
+getActualMaximum(field: int): int
+add(field: int, amount: int): void
+getTime(): java.util.Date
+setTime(date: java.util.Date): void

Constructs a default calendar.
Returns the value of the given calendar field.
Sets the given calendar to the specified value.
Sets the calendar with the specified year, month, and date. The month parameter is 0-based; that is, 0 is for January.
Returns the maximum value that the specified calendar field could have.
Adds or subtracts the specified amount of time to the given calendar field.
Returns a Date object representing this calendar’s time value (million second offset from the UNIX epoch).
Sets this calendar’s time with the given Date object.

```
java.util.GregorianCalendar

+GregorianCalendar()
+GregorianCalendar(year: int, month: int, dayOfMonth: int)
+GregorianCalendar(year: int, month: int, dayOfMonth: int, hour:int, minute: int, second: int)

Constructs a GregorianCalendar for the current time.
Constructs a GregorianCalendar for the specified year, month, and date.
Constructs a GregorianCalendar for the specified year, month, date, hour, minute, and second. The month parameter is 0-based, that is, 0 is for January.
```

TABLE 13.1  Field Constants in the Calendar Class

<table>
<thead>
<tr>
<th>Constant</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>YEAR</td>
<td>The year of the calendar.</td>
</tr>
<tr>
<td>MONTH</td>
<td>The month of the calendar, with 0 for January.</td>
</tr>
<tr>
<td>DATE</td>
<td>The day of the calendar.</td>
</tr>
<tr>
<td>HOUR</td>
<td>The hour of the calendar (12-hour notation).</td>
</tr>
<tr>
<td>HOUR_OF_DAY</td>
<td>The hour of the calendar (24-hour notation).</td>
</tr>
<tr>
<td>MINUTE</td>
<td>The minute of the calendar.</td>
</tr>
<tr>
<td>SECOND</td>
<td>The second of the calendar.</td>
</tr>
<tr>
<td>DAY_OF_WEEK</td>
<td>The day number within the week, with 1 for Sunday.</td>
</tr>
<tr>
<td>DAY_OF_MONTH</td>
<td>Same as DATE.</td>
</tr>
<tr>
<td>DAY_OF_YEAR</td>
<td>The day number in the year, with 1 for the first day of the year.</td>
</tr>
<tr>
<td>WEEK_OF_MONTH</td>
<td>The week number within the month, with 1 for the first week.</td>
</tr>
<tr>
<td>WEEK_OF_YEAR</td>
<td>The week number within the year, with 1 for the first week.</td>
</tr>
<tr>
<td>AM_PM</td>
<td>Indicator for AM or PM (0 for AM and 1 for PM).</td>
</tr>
</tbody>
</table>

LISTING 13.6  TestCalendar.java

```
1 \* import java.util.*;
2
3 public class TestCalendar {
4    public static void main(String[] args) {
5        // Construct a Gregorian calendar for the current date and time
6        Calendar calendar = new GregorianCalendar();
7        System.out.println("Current time is "+ new Date());
8        System.out.println("YEAR: "+ calendar.get(Calendar.YEAR));
```
System.out.println("MONTH: "+calendar.get(Calendar.MONTH));
System.out.println("DATE: "+calendar.get(Calendar.DATE));
System.out.println("HOUR: "+calendar.get(Calendar.HOUR));
System.out.println("HOUR_OF_DAY: " +
    calendar.get(Calendar.HOUR_OF_DAY));
System.out.println("MINUTE: "+calendar.get(Calendar.MINUTE));
System.out.println("SECOND: "+calendar.get(Calendar.SECOND));
System.out.println("DAY_OF_WEEK: " +
    calendar.get(Calendar.DAY_OF_WEEK));
System.out.println("DAY_OF_MONTH: " +
    calendar.get(Calendar.DAY_OF_MONTH));
System.out.println("DAY_OF_YEAR: " +
    calendar.get(Calendar.DAY_OF_YEAR));
System.out.println("WEEK_OF_MONTH: " +
    calendar.get(Calendar.WEEK_OF_MONTH));
System.out.println("WEEK_OF_YEAR: " +
    calendar.get(Calendar.WEEK_OF_YEAR));
System.out.println("AM_PM: " +calendar.get(Calendar.AM_PM));

// Construct a calendar for September 11, 2001
Calendar calendar1 = new GregorianCalendar(2001, 8, 11);
String[] dayNameOfWeek = {
    "Sunday", "Monday", "Tuesday", "Wednesday",
    "Thursday", "Friday", "Saturday"};
System.out.println("September 11, 2001 is a " +
    dayNameOfWeek[calendar1.get(Calendar.DAY_OF_WEEK) - 1]);
}

The set(int field, value) method defined in the Calendar class can be used to set a field. For example, you can use calendar.set(Calendar.DAY_OF_MONTH, 1) to set the calendar to the first day of the month.

The add(field, value) method adds the specified amount to a given field. For example, add(Calendar.DAY_OF_MONTH, 5) adds five days to the current time of the calendar. add(Calendar.DAY_OF_MONTH, -5) subtracts five days from the current time of the calendar.

To obtain the number of days in a month, use calendar.getActualMaximum(Calendar.DAY_OF_MONTH). For example, if the calendar were for March, this method would return 31.
You can set a time represented in a Date object for the calendar by invoking 
\texttt{calendar.setTime(date)} and retrieve the time by invoking 
\texttt{calendar.getTime()}.

\begin{enumerate}
\item[13.9] Can you create a Calendar object using the Calendar class?
\item[13.10] Which method in the Calendar class is abstract?
\item[13.11] How do you create a Calendar object for the current time?
\item[13.12] For a Calendar object \texttt{c}, how do you get its year, month, date, hour, minute, and second?
\end{enumerate}

\section*{13.5 Interfaces}

\textit{An interface is a class-like construct that contains only constants and abstract methods.}

In many ways an interface is similar to an abstract class, but its intent is to specify common 
behavior for objects of related classes or unrelated classes. For example, using appropriate 
interfaces, you can specify that the objects are comparable, edible, and/or cloneable.

To distinguish an interface from a class, Java uses the following syntax to define an interface:

\begin{verbatim}
 modifier interface InterfaceName {
 /** Constant declarations */
 /** Abstract method signatures */
 }
\end{verbatim}

Here is an example of an interface:

\begin{verbatim}
 public interface Edible {
 /** Describe how to eat */
 public abstract String howToEat();
 }
\end{verbatim}

An interface is treated like a special class in Java. Each interface is compiled into a separate 
bytecode file, just like a regular class. You can use an interface more or less the same way 
you use an abstract class. For example, you can use an interface as a data type for a reference 
variable, as the result of casting, and so on. As with an abstract class, you cannot create an 
instance from an interface using the new operator.

You can use the Edible interface to specify whether an object is edible. This is accompl-
ished by letting the class for the object implement this interface using the implements 
keyword. For example, the classes Chicken and Fruit in Listing 13.7 (lines 20, 39) imple-
ment the Edible interface. The relationship between the class and the interface is known as 
interface inheritance. Since interface inheritance and class inheritance are essentially the 
same, we will simply refer to both as \textit{inheritance}.

\begin{verbatim}
Listing 13.7 TestEdible.java
\end{verbatim}

\begin{verbatim}
 public class TestEdible {
 public static void main(String[] args) {
   Object[] objects = \{ \texttt{new} Tiger(), \texttt{new} Chicken(), \texttt{new} Apple()\};
   for (int i = 0; i < objects.length; i++) {
     if (objects[i] instanceof Edible)
       System.out.println(((Edible)objects[i]).howToEat());
     if (objects[i] instanceof Animal)
       System.out.println(((Animal)objects[i]).sound());
   }
 }
\end{verbatim}
abstract class Animal {
    /** Return animal sound */
    public abstract String sound();
}

class Chicken extends Animal implements Edible {
    @Override
    public String howToEat() {
        return "Chicken: Fry it";
    }
    @Override
    public String sound() {
        return "Chicken: cock-a-doodle-doo";
    }
}
class Tiger extends Animal {
    @Override
    public String sound() {
        return "Tiger: RROOAARR";
    }
}

abstract class Fruit implements Edible {
    // Data fields, constructors, and methods omitted here
}
class Apple extends Fruit {
    @Override
    public String howToEat() {
        return "Apple: Make apple cider";
    }
}
class Orange extends Fruit {
    @Override
    public String howToEat() {
        return "Orange: Make orange juice";
    }
}

This example uses several classes and interfaces. Their inheritance relationship is shown in Figure 13.4.

The Animal class defines the sound method (line 17). It is an abstract method and will be implemented by a concrete animal class.

The Chicken class implements Edible to specify that chickens are edible. When a class implements an interface, it implements all the methods defined in the interface with the exact signature and return type. The Chicken class implements the howToEat method (lines 22–24). Chicken also extends Animal to implement the sound method (lines 27–29).
Chapter 13  Abstract Classes and Interfaces

The *Fruit* class implements *Edible*. Since it does not implement the *howToEat* method, *Fruit* must be denoted as *abstract* (line 39). The concrete subclasses of *Fruit* must implement the *howToEat* method. The *Apple* and *Orange* classes implement the *howToEat* method (lines 45, 52).

The *main* method creates an array with three objects for *Tiger*, *Chicken*, and *Apple* (line 3), and invokes the *howToEat* method if the element is edible (line 6) and the *sound* method if the element is an animal (line 9).

In essence, the *Edible* interface defines common behavior for edible objects. All edible objects have the *howToEat* method.

*Note* Since all data fields are *public static final* and all methods are *public abstract* in an interface, Java allows these modifiers to be omitted. Therefore the following interface definitions are equivalent:

```java
public interface T {
    public static final int K = 1;
    public abstract void p();
}
```

Equivalent

```java
public interface T {
    int K = 1;
    void p();
}
```

13.13 Suppose *A* is an interface. Can you create an instance using `new A()`?

13.14 Suppose *A* is an interface. Can you declare a reference variable *x* with type *A* like this?

```java
A x;
```

13.15 Which of the following is a correct interface?

```java
interface A {
    void print() { }
}
```

(a)

```java
abstract interface A extends I1, I2 {
    abstract void print() { }
}
```

(b)

```java
abstract interface A {
    print();
}
```

(c)

```java
interface A {
    void print();
}
```

(d)
13.6 The **Comparable** Interface

*The Comparable interface defines the compareTo method for comparing objects.*

Suppose you want to design a generic method to find the larger of two objects of the same type, such as two students, two dates, two circles, two rectangles, or two squares. In order to accomplish this, the two objects must be comparable, so the common behavior for the objects must be comparable. Java provides the **Comparable** interface for this purpose. The interface is defined as follows:

```java
// Interface for comparing objects, defined in java.lang
package java.lang;

public interface Comparable<E> {
    public int compareTo(E o);
}
```

The `compareTo` method determines the order of this object with the specified object `o` and returns a negative integer, zero, or a positive integer if this object is less than, equal to, or greater than `o`.

The **Comparable** interface is a generic interface. The generic type `E` is replaced by a concrete type when implementing this interface. Many classes in the Java library implement **Comparable** to define a natural order for objects. The classes `Byte`, `Short`, `Integer`, `Long`, `Float`, `Double`, `Character`, `BigInteger`, `BigDecimal`, `Calendar`, `String`, and `Date` all implement the **Comparable** interface. For example, the `Integer`, `BigInteger`, `String`, and `Date` classes are defined as follows in the Java API:

```java
public class Integer extends Number implements Comparable<Integer> {
    // class body omitted
    @Override
    public int compareTo(Integer o) {
        // Implementation omitted
    }
}

public class BigInteger extends Number implements Comparable<BigInteger> {
    // class body omitted
    @Override
    public int compareTo(BigInteger o) {
        // Implementation omitted
    }
}

public class String extends Object implements Comparable<String> {
    // class body omitted
    @Override
    public int compareTo(String o) {
        // Implementation omitted
    }
}

public class Date extends Object implements Comparable<Date> {
    // class body omitted
    @Override
    public int compareTo(Date o) {
        // Implementation omitted
    }
}
```
Thus, numbers are comparable, strings are comparable, and so are dates. You can use the
`compareTo` method to compare two numbers, two strings, and two dates. For example, the
following code

```java
1 System.out.println(new Integer(3).compareTo(new Integer(5)));
2 System.out.println("ABC".compareTo("ABE"));
3 java.util.Date date1 = new java.util.Date(2013, 1, 1);
4 java.util.Date date2 = new java.util.Date(2012, 1, 1);
5 System.out.println(date1.compareTo(date2));
```
displays

```
-1
-2
1
```

Line 1 displays a negative value since 3 is less than 5. Line 2 displays a negative value
since ABC is less than ABE. Line 5 displays a positive value since `date1` is greater than `date2`.

Let `n` be an `Integer` object, `s` be a `String` object, and `d` be a `Date` object. All the follow-
ing expressions are `true`.

<table>
<thead>
<tr>
<th>n instanceof Integer</th>
<th>s instanceof String</th>
<th>d instanceof java.util.Date</th>
</tr>
</thead>
<tbody>
<tr>
<td>n instanceof Object</td>
<td>s instanceof Object</td>
<td>d instanceof Object</td>
</tr>
<tr>
<td>n instanceof Comparable</td>
<td>s instanceof Comparable</td>
<td>d instanceof Comparable</td>
</tr>
</tbody>
</table>

Since all `Comparable` objects have the `compareTo` method, the `java.util.Arrays.sort(Object[])` method in the Java API uses the `compareTo` method to compare and sorts the objects in an array, provided that the objects are instances of the `Comparable` inter-
face. Listing 13.8 gives an example of sorting an array of strings and an array of `BigInteger` objects.

**Listing 13.8  SortComparableObjects.java**

```java
1 import java.math.*;
2 public class SortComparableObjects {
3     public static void main(String[] args) {
4         String[] cities = {"Savannah", "Boston", "Atlanta", "Tampa"};
5         java.util.Arrays.sort(cities);
6         for (String city: cities)
7             System.out.print(city + " ");
8         System.out.println();
9     }
10 }
11 BigInteger[] hugeNumbers = {
12     new BigInteger("2323231092923992"),
13     new BigInteger("4322323239292"),
14     new BigInteger("54623239292")};
15 java.util.Arrays.sort(hugeNumbers);
16 for (BigInteger number: hugeNumbers)
17     System.out.print(number + " ");
18 }
```
The program creates an array of strings (line 5) and invokes the sort method to sort the strings (line 6). The program creates an array of BigInteger objects (lines 11–13) and invokes the sort method to sort the BigInteger objects (line 14).

You cannot use the sort method to sort an array of Rectangle objects, because Rectangle does not implement Comparable. However, you can define a new rectangle class that implements Comparable. The instances of this new class are comparable. Let this new class be named ComparableRectangle, as shown in Listing 13.9.

```
LISTING 13.9 ComparableRectangle.java
1 public class ComparableRectangle extends Rectangle
2     implements Comparable<ComparableRectangle> {
3     /** Construct a ComparableRectangle with specified properties */
4     public ComparableRectangle(double width, double height) {
5         super(width, height);
6     }
7     @Override // Implement the compareTo method defined in Comparable
8     public int compareTo(ComparableRectangle o) {
9         if (getArea() > o.getArea())
10            return 1;
11         else if (getArea() < o.getArea())
12            return -1;
13         else
14            return 0;
15     }
16     @Override // Implement the toString method in GeometricObject
17     public String toString() {
18         return super.toString() + " Area: " + getArea();
19     }
20 }
```

ComparableRectangle extends Rectangle and implements Comparable, as shown in Figure 13.5. The keyword implements indicates that ComparableRectangle inherits all the constants from the Comparable interface and implements the methods in the interface. The compareTo method compares the areas of two rectangles. An instance of ComparableRectangle is also an instance of Rectangle, GeometricObject, Object, and Comparable.
You can now use the sort method to sort an array of ComparableRectangle objects, as in Listing 13.10.

**Listing 13.10  SortRectangles.java**

```java
public class SortRectangles {
    public static void main(String[] args) {
        ComparableRectangle[] rectangles = {
            new ComparableRectangle(3.4, 5.4),
            new ComparableRectangle(13.24, 55.4),
            new ComparableRectangle(7.4, 35.4),
            new ComparableRectangle(1.4, 25.4)};
        java.util.Arrays.sort(rectangles);
        for (Rectangle rectangle: rectangles) {
            System.out.print(rectangle + " ");
            System.out.println();
        }
    }
}
```

An interface provides another form of generic programming. It would be difficult to use a generic sort method to sort the objects without using an interface in this example, because multiple inheritance would be necessary to inherit Comparable and another class, such as Rectangle, at the same time.

The Object class contains the equals method, which is intended for the subclasses of the Object class to override in order to compare whether the contents of the objects are the same. Suppose that the Object class contains the compareTo method, as defined in the Comparable interface; the sort method can be used to compare a list of any objects. Whether a compareTo method should be included in the Object class is debatable. Since the compareTo method is not defined in the Object class, the Comparable interface is defined in Java to enable objects to be compared if they are instances of the Comparable interface. It is strongly recommended (though not required) that compareTo should be consistent with equals. That is, for two objects o1 and o2, o1.compareTo(o2) == 0 if and only if o1.equals(o2) is true.

**13.17** True or false? If a class implements Comparable, the object of the class can invoke the compareTo method.

**13.18** Which of the following is the correct method header for the compareTo method in the String class?

- `public int compareTo(String o)`
- `public int compareTo(Object o)`

**13.19** Can the following code be compiled? Why?

```java
Integer n1 = new Integer(3);
Object n2 = new Integer(4);
System.out.println(n1.compareTo(n2));
```
13.20 You can define the compareTo method in a class without implementing the Comparable interface. What are the benefits of implementing the Comparable interface?

13.21 What is wrong in the following code?

```java
public class Test {
    public static void main(String[] args) {
        Person[] persons = {new Person(3), new Person(4), new Person(1)};
        java.util.Arrays.sort(persons);
    }
}

class Person {
    private int id;
    Person(int id) {
        this.id = id;
    }
}
```

13.7 The Cloneable Interface

The Cloneable interface specifies that an object can be cloned.

Often it is desirable to create a copy of an object. To do this, you need to use the clone method and understand the Cloneable interface.

An interface contains constants and abstract methods, but the Cloneable interface is a special case. The Cloneable interface in the java.lang package is defined as follows:

```java
package java.lang;

public interface Cloneable {
}
```

This interface is empty. An interface with an empty body is referred to as a marker interface. A marker interface does not contain constants or methods. It is used to denote that a class possesses certain desirable properties. A class that implements the Cloneable interface is marked cloneable, and its objects can be cloned using the clone() method defined in the Object class.

Many classes in the Java library (e.g., Date, Calendar, and ArrayList) implement Cloneable. Thus, the instances of these classes can be cloned. For example, the following code

```java
Calendar calendar = new GregorianCalendar(2013, 2, 1);
Calendar calendar1 = calendar;
Calendar calendar2 = (Calendar)calendar.clone();
System.out.println("calendar == calendar1 is " +
    (calendar == calendar1));
System.out.println("calendar == calendar2 is " +
    (calendar == calendar2));
System.out.println("calendar.equals(calendar2) is " +
    calendar.equals(calendar2));
```

displays

```
calendar == calendar1 is true
calendar == calendar2 is false
calendar.equals(calendar2) is true
```
In the preceding code, line 2 copies the reference of `calendar` to `calendar1`, so `calendar` and `calendar1` point to the same `Calendar` object. Line 3 creates a new object that is the clone of `calendar` and assigns the new object’s reference to `calendar2`. `calendar2` and `calendar` are different objects with the same contents.

The following code displays:

```
list1 is [2.5, 3.5]
list2 is [1.5, 2.5, 3.5, 4.5]
list3 is [2.5, 3.5]
```

In the preceding code, line 5 creates a new object that is the clone of `list1` and assigns the new object’s reference to `list2`. `list2` and `list1` are different objects with the same contents. Line 6 copies the reference of `list1` to `list3`, so `list1` and `list3` point to the same `ArrayList` object. Line 7 adds 4.5 into `list2`. Line 8 removes 1.5 from `list3`. Since `list1` and `list3` point to the same `ArrayList`, line 9 and 11 display the same content.

You can clone an array using the `clone` method. For example, the following code displays:

```
list1 is 7, 2
list2 is 1, 8
```

To define a custom class that implements the `Cloneable` interface, the class must override the `clone()` method in the `Object` class. Listing 13.11 defines a class named `House` that implements `Cloneable` and `Comparable`.

**Listing 13.11  House.java**

```
public class House implements Cloneable, Comparable<House> {
    private int id;
    private double area;
    private java.util.Date whenBuilt;

    public House(int id, double area) {
        this.id = id;
        this.area = area;
        whenBuilt = new java.util.Date();
    }
}
```
11  public int getId() {
12    return id;
13  }
14
15  public double getArea() {
16    return area;
17  }
18
19  public java.util.Date getWhenBuilt() {
20    return whenBuilt;
21  }
22
23  @Override /** Override the protected clone method defined in
24     the Object class, and strengthen its accessibility */
25  public Object clone() throws CloneNotSupportedException {
26    return super.clone();
27  }
28
29  @Override // Implement the compareTo method defined in Comparable
30  public int compareTo(House o) {
31    if (area > o.area)
32      return 1;
33    else if (area < o.area)
34      return -1;
35    else
36      return 0;
37  }
38  }

The House class implements the clone method (lines 26–28) defined in the Object class. The header is:

protected native Object clone() throws CloneNotSupportedException;

The keyword native indicates that this method is not written in Java but is implemented in the JVM for the native platform. The keyword protected restricts the method to be accessed in the same package or in a subclass. For this reason, the House class must override the method and change the visibility modifier to public so that the method can be used in any package. Since the clone method implemented for the native platform in the Object class performs the task of cloning objects, the clone method in the House class simply invokes super.clone(). The clone method defined in the Object class may throw CloneNotSupportedException.

The House class implements the compareTo method (lines 31–38) defined in the Comparable interface. The method compares the areas of two houses.

You can now create an object of the House class and create an identical copy from it, as follows:

House house1 = new House(1, 1750.50);
House house2 = (House)house1.clone();

house1 and house2 are two different objects with identical contents. The clone method in the Object class copies each field from the original object to the target object. If the field is of a primitive type, its value is copied. For example, the value of area (double type) is copied from house1 to house2. If the field is of an object, the reference of the field is copied. For example, the field whenBuilt is of the Date class, so its reference is copied into house2, as shown in Figure 13.6. Therefore, house1.whenBuilt == house2.whenBuilt is true, although house1 == house2 is false. This is referred to as a shallow copy rather than a
deep copy

...meaning that if the field is of an object type, the object’s reference is copied rather than its contents.

To perform a deep copy for a `House` object, replace the `clone()` method in lines 26–28 with the following code:

```java
public Object clone() throws CloneNotSupportedException {
    // Perform a shallow copy
    House houseClone = (House) super.clone();
    // Deep copy on whenBuilt
    houseClone.whenBuilt = (java.util.Date)(whenBuilt.clone());
    return houseClone;
}
```

or

```java
public Object clone() {
    try {
        // Perform a shallow copy
        House houseClone = (House) super.clone();
        // Deep copy on whenBuilt
        houseClone.whenBuilt = (java.util.Date)(whenBuilt.clone());
        return houseClone;
    }
    catch (CloneNotSupportedException ex) {
        return null;
    }
}
```

Now if you clone a `House` object in the following code:

```java
House house1 = new House(1, 1750.50);
House house2 = (House)house1.clone();
```

`house1.whenBuilt == house2.whenBuilt` will be `false`. `house1` and `house2` contain two different `Date` objects, as shown in Figure 13.6b.
13.22 Can you invoke the `clone()` method to clone an object if the class for the object does not implement the `java.lang.Cloneable`? Does the `Date` class implement `Cloneable`?

13.23 What would happen if the `House` class (defined in Listing 13.11) did not override the `clone()` method or if `House` did not implement `java.lang.Cloneable`?

13.24 Show the output of the following code:

```java
java.util.Date date = new java.util.Date();
java.util.Date date1 = date;
java.util.Date date2 = (java.util.Date)(date.clone());
System.out.println(date == date1);
System.out.println(date == date2);
System.out.println(date.equals(date2));
```

13.25 Show the output of the following code:

```java
ArrayList<String> list = new ArrayList<>();
list.add("New York");
ArrayList<String> list1 = list;
ArrayList<String> list2 = (ArrayList<String>)(list.clone());
list.add("Atlanta");
System.out.println(list == list1);
System.out.println(list == list2);
System.out.println("list is " + list);
System.out.println("list1 is " + list1);
System.out.println("list2.get(0) is " + list2.get(0));
System.out.println("list2.size() is " + list2.size());
```

13.26 What is wrong in the following code?

```java
public class Test {
    public static void main(String[] args) {
        GeometricObject x = new Circle(3);
        GeometricObject y = x.clone();
        System.out.println(x == y);
    }
}
```

13.8 Interfaces vs. Abstract Classes

A class can implement multiple interfaces, but it can only extend one superclass.

An interface can be used more or less the same way as an abstract class, but defining an interface is different from defining an abstract class. Table 13.2 summarizes the differences.

<table>
<thead>
<tr>
<th>Variables</th>
<th>Constructors</th>
<th>Methods</th>
</tr>
</thead>
<tbody>
<tr>
<td>Abstract class</td>
<td>No restrictions.</td>
<td>Constructors are invoked by subclasses through constructor chaining. An abstract class cannot be instantiated using the new operator.</td>
</tr>
<tr>
<td>Interface</td>
<td>All variables must be <code>public static final</code></td>
<td>No constructors. An interface cannot be instantiated using the new operator.</td>
</tr>
</tbody>
</table>

**Table 13.2** Interfaces vs. Abstract Classes
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Java allows only single inheritance for class extension but allows multiple extensions for interfaces. For example,

```java
public class NewClass extends BaseClass
    implements Interface1, ..., InterfaceN {
    ...
}
```

An interface can inherit other interfaces using the `extends` keyword. Such an interface is called a subinterface. For example, `NewInterface` in the following code is a subinterface of `Interface1,..., and InterfaceN`.

```java
public interface NewInterface extends Interface1, ..., InterfaceN {
    // constants and abstract methods
}
```

A class implementing `NewInterface` must implement the abstract methods defined in `NewInterface, Interface1,..., and InterfaceN`. An interface can extend other interfaces but not classes. A class can extend its superclass and implement multiple interfaces.

All classes share a single root, the `Object` class, but there is no single root for interfaces. Like a class, an interface also defines a type. A variable of an interface type can reference any instance of the class that implements the interface. If a class implements an interface, the interface is like a superclass for the class. You can use an interface as a data type and cast a variable of an interface type to its subclass, and vice versa. For example, suppose that `c` is an instance of `Class2` in Figure 13.7. `c` is also an instance of `Object, Class1, Interface1, Interface1_1, Interface1_2, Interface2_1, and Interface2_2`.

![Diagram](image_url)

**Figure 13.7** Class1 implements `Interface1; Interface1` extends `Interface1_1` and `Interface1_2`. Class2 extends Class1 and implements `Interface2_1` and `Interface2_2`.

Class names are nouns. Interface names may be adjectives or nouns.

**Design Guide**

Abstract classes and interfaces can both be used to specify common behavior of objects. How do you decide whether to use an interface or a class? In general, a strong is-a relationship that clearly describes a parent-child relationship should be modeled using classes. For example, Gregorian calendar is a calendar, so the relationship between the class `java.util.GregorianCalendar` and `java.util.Calendar` is modeled using class inheritance. A weak is-a relationship, also known as an is-kind-of relationship, indicates that an object possesses a certain property. A weak is-a relationship can be modeled using interfaces. For example, all strings are comparable, so the `String` class implements the `Comparable` interface.
In general, interfaces are preferred over abstract classes because an interface can define a common supertype for unrelated classes. Interfaces are more flexible than classes. Consider the Animal class. Suppose the howToEat method is defined in the Animal class, as follows:

```java
abstract class Animal {
    public abstract String howToEat();
}
```

Two subclasses of Animal are defined as follows:

```java
class Chicken extends Animal {
    @Override
    public String howToEat() {
        return "Fry it";
    }
}
class Duck extends Animal {
    @Override
    public String howToEat() {
        return "Roast it";
    }
}
```

Given this inheritance hierarchy, polymorphism enables you to hold a reference to a Chicken object or a Duck object in a variable of type Animal, as in the following code:

```java
public static void main(String[] args) {
    Animal animal = new Chicken();
eat(animal);
    animal = new Duck();
eat(animal);
}
```

The JVM dynamically decides which howToEat method to invoke based on the actual object that invokes the method.

You can define a subclass of Animal. However, there is a restriction: The subclass must be for another animal (e.g., Turkey).

Interfaces don’t have this restriction. Interfaces give you more flexibility than classes, because you don’t have to make everything fit into one type of class. You may define the howToEat() method in an interface and let it serve as a common supertype for other classes. For example,

```java
public static void main(String[] args) {
    Edible stuff = new Chicken();
eat(stuff);
    stuff = new Duck();
eat(stuff);
    stuff = new Broccoli();
eat(stuff);
}
```
public static void eat(Edible stuff) {
    stuff.howToEat();
}

interface Edible {
    public String howToEat();
}

class Chicken implements Edible {
    @Override
    public String howToEat() {
        return "Fry it";
    }
}

class Duck implements Edible {
    @Override
    public String howToEat() {
        return "Roast it";
    }
}

class Broccoli implements Edible {
    @Override
    public String howToEat() {
        return "Stir-fry it";
    }
}

To define a class that represents edible objects, simply let the class implement the Edible interface. The class is now a subtype of the Edible type, and any Edible object can be passed to invoke the howToEat method.

13.27 Give an example to show why interfaces are preferred over abstract classes.

13.28 Define the terms abstract classes and interfaces. What are the similarities and differences between abstract classes and interfaces?

13.29 True or false?
   a. An interface is compiled into a separate bytecode file.
   b. An interface can have static methods.
   c. An interface can extend one or more interfaces.
   d. An interface can extend an abstract class.
   e. An abstract class can extend an interface.

13.9 Case Study: The Rational Class

This section shows how to design the Rational class for representing and processing rational numbers.

A rational number has a numerator and a denominator in the form \( \frac{a}{b} \), where \( a \) is the numerator and \( b \) the denominator. For example, \( \frac{1}{3}, \frac{3}{4}, \) and \( \frac{10}{4} \) are rational numbers.

A rational number cannot have a denominator of 0, but a numerator of 0 is fine. Every integer \( i \) is equivalent to a rational number \( \frac{i}{1} \). Rational numbers are used in exact computations involving fractions—for example, \( \frac{1}{3} = 0.33333... \). This number cannot be precisely represented in floating-point format using either the data type double or float. To obtain the exact result, we must use rational numbers.
Java provides data types for integers and floating-point numbers, but not for rational numbers. This section shows how to design a class to represent rational numbers.

Since rational numbers share many common features with integers and floating-point numbers, and \texttt{Number} is the root class for numeric wrapper classes, it is appropriate to define \texttt{Rational} as a subclass of \texttt{Number}. Since rational numbers are comparable, the \texttt{Rational} class should also implement the \texttt{Comparable} interface. Figure 13.8 illustrates the \texttt{Rational} class and its relationship to the \texttt{Number} class and the \texttt{Comparable} interface.

![Diagram of Rational class](image)

**Figure 13.8** The properties, constructors, and methods of the \texttt{Rational} class are illustrated in UML.

A rational number consists of a numerator and a denominator. There are many equivalent rational numbers—for example, $1/3 = 2/6 = 3/9 = 4/12$. The numerator and the denominator of $1/3$ have no common divisor except 1, so $1/3$ is said to be in lowest terms.

To reduce a rational number to its lowest terms, you need to find the greatest common divisor (GCD) of the absolute values of its numerator and denominator, then divide both the numerator and denominator by this value. You can use the method for computing the GCD of two integers \texttt{n} and \texttt{d}, as suggested in Listing 5.9, GreatestCommonDivisor.java. The numerator and denominator in a \texttt{Rational} object are reduced to their lowest terms.

As usual, let us first write a test program to create two \texttt{Rational} objects and test its methods. Listing 13.12 is a test program.

**Listing 13.12** TestRationalClass.java

```java
public class TestRationalClass {
    /** Main method */
    public static void main(String[] args) {
        // Create and initialize two rational numbers r1 and r2
        Rational r1 = new Rational(4, 2);  // create a Rational
        Rational r2 = new Rational(2, 3);  // create a Rational

        // Display results
    }
}
```

The numerator of this rational number.

The denominator of this rational number.

Creates a rational number with numerator 0 and denominator 1.

Creates a rational number with a specified numerator and denominator.

Returns the numerator of this rational number.

Returns the denominator of this rational number.

Returns the addition of this rational number with another.

Returns the subtraction of this rational number with another.

Returns the multiplication of this rational number with another.

Returns the division of this rational number with another.

Returns a string in the form “numerator/denominator.” Returns the numerator if denominator is 1.

Returns the greatest common divisor of \texttt{n} and \texttt{d}.
add
System.out.println(r1 + " + " + r2 + " = " + r1.add(r2));
System.out.println(r1 + " - " + r2 + " = " + r1.subtract(r2));
System.out.println(r1 + " * " + r2 + " = " + r1.multiply(r2));
System.out.println(r1 + " / " + r2 + " = " + r1.divide(r2));
System.out.println(r2 + " is " + r2.doubleValue());
}
}

2 + 2/3 = 8/3
2 - 2/3 = 4/3
2 * 2/3 = 4/3
2 / 2/3 = 3
2/3 is 0.6666666666666666

The main method creates two rational numbers, r1 and r2 (lines 5–6), and displays the results of r1 + r2, r1 - r2, r1 x r2, and r1 / r2 (lines 9–12). To perform r1 + r2, invoke r1.add(r2) to return a new Rational object. Similarly, invoke r1.subtract(r2) for r1 - r2, r1.multiply(r2) for r1 x r2, and r1.divide(r2) for r1 / r2.

The doubleValue() method displays the double value of r2 (line 13). The doubleValue() method is defined in java.lang.Number and overridden in Rational.

Note that when a string is concatenated with an object using the plus sign (+), the object’s string representation from the toString() method is used to concatenate with the string. So r1 + " + " + r2 + " = " + r1.add(r2) is equivalent to r1.toString() + " + " + r2.toString() + " = " + r1.add(r2).toString().

The Rational class is implemented in Listing 13.13.

**LISTING 13.13  Rational.java**

```java
public class Rational extends Number implements Comparable<Rational> {
    // Data fields for numerator and denominator
    private long numerator = 0;
    private long denominator = 1;

    /** Construct a rational with default properties */
    public Rational() {
        this(0, 1);
    }

    /** Construct a rational with specified numerator and denominator */
    public Rational(long numerator, long denominator) {
        long gcd = gcd(numerator, denominator);
        this.numerator = ((denominator > 0) ? 1 : -1) * numerator / gcd;
        this.denominator = Math.abs(denominator) / gcd;
    }

    /** Find GCD of two numbers */
    private static long gcd(long n, long d) {
        long n1 = Math.abs(n);
        long n2 = Math.abs(d);
        int gcd = 1;
        for (int k = 1; k <= n1 && k <= n2; k++) {
            if (n1 % k == 0 && n2 % k == 0)
                gcd = k;
        }
        return gcd;
    }
}
```
/** Return numerator */
public long getNumerator() {
    return numerator;
}
/** Return denominator */
public long getDenominator() {
    return denominator;
}
/** Add a rational number to this rational */
public Rational add(Rational secondRational) {
    long n = numerator * secondRational.getDenominator() +
            denominator * secondRational.getNumerator();
    long d = denominator * secondRational.getDenominator();
    return new Rational(n, d);
}
/** Subtract a rational number from this rational */
public Rational subtract(Rational secondRational) {
    long n = numerator * secondRational.getDenominator()
            - denominator * secondRational.getNumerator();
    long d = denominator * secondRational.getDenominator();
    return new Rational(n, d);
}
/** Multiply a rational number by this rational */
public Rational multiply(Rational secondRational) {
    long n = numerator * secondRational.getNumerator();
    long d = denominator * secondRational.getDenominator();
    return new Rational(n, d);
}
/** Divide a rational number by this rational */
public Rational divide(Rational secondRational) {
    long n = numerator * secondRational.getDenominator();
    long d = denominator * secondRational.numerator;
    return new Rational(n, d);
}

@Override
public String toString() {
    if (denominator == 1)
        return numerator + "";
    else
        return numerator + "/" + denominator;
}
@Override // Override the equals method in the Object class
public boolean equals(Object other) {
    if (((Rational)(other)).getNumerator() == 0)
        return true;
    else
        return false;
}
@Override // Implement the abstract intValue method in Number
public int intValue() {

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90  return (int)doubleValue();
91  }
92
93  @Override // Implement the abstract floatValue method in Number
94  public float floatValue() {
95    return (float)doubleValue();
96  }
97
98  @Override // Implement the doubleValue method in Number
99  public double doubleValue() {
100    return numerator * 1.0 / denominator;
101  }
102
103  @Override // Implement the abstract longValue method in Number
104  public long longValue() {
105    return (long)doubleValue();
106  }
107
108  @Override // Implement the compareTo method in Comparable
109  public int compareTo(Rational o) {
110    if (this.subtract(o).getNumerator() > 0)
111      return 1;
112    else if (this.subtract(o).getNumerator() < 0)
113      return -1;
114    else
115      return 0;
116  }
117  }

The rational number is encapsulated in a Rational object. Internally, a rational number is represented in its lowest terms (line 13), and the numerator determines its sign (line 14). The denominator is always positive (line 15).

The gcd method (lines 19–30 in the Rational class) is private; it is not intended for use by clients. The gcd method is only for internal use by the Rational class. The gcd method is also static, since it is not dependent on any particular Rational object.

The abs(x) method (lines 20–21 in the Rational class) is defined in the Math class and returns the absolute value of x.

Two Rational objects can interact with each other to perform add, subtract, multiply, and divide operations. These methods return a new Rational object (lines 43–70).

The methods toString and equals in the Object class are overridden in the Rational class (lines 72–86). The toString() method returns a string representation of a Rational object in the form numerator/denominator, or simply numerator if denominator is 1. The equals(Object other) method returns true if this rational number is equal to the other rational number.

The abstract methods intValue, longValue, floatValue, and doubleValue in the Number class are implemented in the Rational class (lines 88–106). These methods return the int, long, float, and double value for this rational number.

The compareTo(Rational other) method in the Comparable interface is implemented in the Rational class (lines 108–116) to compare this rational number to the other rational number.

Tip
The getter methods for the properties numerator and denominator are provided in the Rational class, but the setter methods are not provided, so, once a Rational object is created, its contents cannot be changed. The Rational class is immutable. The String class and the wrapper classes for primitive type values are also immutable.
Tip
The numerator and denominator are represented using two variables. It is possible to use an array of two integers to represent the numerator and denominator (see Programming Exercise 13.14). The signatures of the public methods in the Rational class are not changed, although the internal representation of a rational number is changed. This is a good example to illustrate the idea that the data fields of a class should be kept private so as to encapsulate the implementation of the class from the use of the class.

The Rational class has serious limitations and can easily overflow. For example, the following code will display an incorrect result, because the denominator is too large.

```java
class Test {
    public static void main(String[] args) {
        Rational r1 = new Rational(1, 123456789);
        Rational r2 = new Rational(1, 123456789);
        Rational r3 = new Rational(1, 123456789);
        System.out.println("r1 * r2 * r3 is " + r1.multiply(r2.multiply(r3)));
    }
}
```

To fix it, you can implement the Rational class using the BigInteger for numerator and denominator (see Programming Exercise 13.15).

13.30 Show the output of the following code?

```java
Rational r1 = new Rational(-2, 6);
System.out.println(r1.getNumerator());
System.out.println(r1.getDenominator());
System.out.println(r1.intValue());
System.out.println(r1.doubleValue());
```

13.31 Why is the following code wrong?

```java
Rational r1 = new Rational(-2, 6);
Object r2 = new Rational(1, 45);
System.out.println(r2.compareTo(r1));
```

13.32 Why is the following code wrong?

```java
Object r1 = new Rational(-2, 6);
Rational r2 = new Rational(1, 45);
System.out.println(r2.compareTo(r1));
```

13.33 How do you simplify the code in lines 82–85 in Listing 13.13 Rational.java using one line of code without using the if statement?

13.34 Trace the program carefully and show the output of the following code.

```java
Rational r1 = new Rational(1, 2);
Rational r2 = new Rational(1, -2);
System.out.println(r1.add(r2));
```

13.10 Class Design Guidelines

Class design guidelines are helpful for designing sound classes.

You have learned how to design classes from the preceding two examples and from many other examples in the preceding chapters. This section summarizes some of the guidelines.
13.10.1 Cohesion

A class should describe a single entity, and all the class operations should logically fit together to support a coherent purpose. You can use a class for students, for example, but you should not combine students and staff in the same class, because students and staff are different entities.

A single entity with many responsibilities can be broken into several classes to separate the responsibilities. The classes String, StringBuilder, and StringBuffer all deal with strings, for example, but have different responsibilities. The String class deals with immutable strings, the StringBuilder class is for creating mutable strings, and the StringBuffer class is similar to StringBuilder except that StringBuffer contains synchronized methods for updating strings.

13.10.2 Consistency

Follow standard Java programming style and naming conventions. Choose informative names for classes, data fields, and methods. A popular style is to place the data declaration before the constructor and place constructors before methods.

Make the names consistent. It is not a good practice to choose different names for similar operations. For example, the length() method returns the size of a String, a StringBuilder, and a StringBuffer. It would be inconsistent if different names were used for this method in these classes.

In general, you should consistently provide a public no-arg constructor for constructing a default instance. If a class does not support a no-arg constructor, document the reason. If no constructors are defined explicitly, a public default no-arg constructor with an empty body is assumed.

If you want to prevent users from creating an object for a class, you can declare a private constructor in the class, as is the case for the Math class.

13.10.3 Encapsulation

A class should use the private modifier to hide its data from direct access by clients. This makes the class easy to maintain.

Provide a getter method only if you want the data field to be readable, and provide a setter method only if you want the data field to be updateable. For example, the Rational class provides a getter method for numerator and denominator, but no setter method, because a Rational object is immutable.

13.10.4 Clarity

Cohesion, consistency, and encapsulation are good guidelines for achieving design clarity. Additionally, a class should have a clear contract that is easy to explain and easy to understand.

Users can incorporate classes in many different combinations, orders, and environments. Therefore, you should design a class that imposes no restrictions on how or when the user can use it, design the properties in a way that lets the user set them in any order and with any combination of values, and design methods that function independently of their order of occurrence. For example, the Loan class contains the properties loanAmount, numberOfYears, and annualInterestRate. The values of these properties can be set in any order.

Methods should be defined intuitively without causing confusion. For example, the substring(int beginIndex, int endIndex) method in the String class is somewhat confusing. The method returns a substring from beginIndex to endIndex - 1, rather than to endIndex. It would be more intuitive to return a substring from beginIndex to endIndex.

You should not declare a data field that can be derived from other data fields. For example, the following Person class has two data fields: birthDate and age. Since age can be derived from birthDate, age should not be declared as a data field.

```java
public class Person {
    private java.util.Date birthDate;
```
13.10.5 Completeness

Classes are designed for use by many different customers. In order to be useful in a wide range of applications, a class should provide a variety of ways for customization through properties and methods. For example, the `String` class contains more than 40 methods that are useful for a variety of applications.

13.10.6 Instance vs. Static

A variable or method that is dependent on a specific instance of the class must be an instance variable or method. A variable that is shared by all the instances of a class should be declared static. For example, the variable `numberOfObjects` in `CircleWithPrivateDataFields` in Listing 9.8 is shared by all the objects of the `CircleWithPrivateDataFields` class and therefore is declared static. A method that is not dependent on a specific instance should be defined as a static method. For instance, the `getNumberOfObjects()` method in `CircleWithPrivateDataFields` is not tied to any specific instance and therefore is defined as a static method.

Always reference static variables and methods from a class name (rather than a reference variable) to improve readability and avoid errors.

Do not pass a parameter from a constructor to initialize a static data field. It is better to use a setter method to change the static data field. Thus, the following class in (a) is better replaced by (b).

```java
public class SomeThing {
    private int tl;
    private static int t2;

    public SomeThing(int tl, int t2) {
        ...
    }
}
```

```java
public class SomeThing {
    private int tl;
    private static int t2;

    public SomeThing(int tl) {
        ...
    }

    public static void setT2(int t2) {
        SomeThing.t2 = t2;
    }
}
```

(a)  

(b)  

Instance and static are integral parts of object-oriented programming. A data field or method is either instance or static. Do not mistakenly overlook static data fields or methods. It is a common design error to define an instance method that should have been static. For example, the `factorial(int n)` method for computing the factorial of `n` should be defined static, because it is independent of any specific instance.

A constructor is always instance, because it is used to create a specific instance. A static variable or method can be invoked from an instance method, but an instance variable or method cannot be invoked from a static method.

13.10.7 Inheritance vs. Aggregation

The difference between inheritance and aggregation is the difference between an is-a and a has-a relationship. For example, an apple is a fruit; thus, you would use inheritance to model the relationship between the classes `Apple` and `Fruit`. A person has a name; thus, you would use aggregation to model the relationship between the classes `Person` and `Name`. 
13.10.8 Interfaces vs. Abstract Classes

Both interfaces and abstract classes can be used to specify common behavior for objects. How do you decide whether to use an interface or a class? In general, a strong is-a relationship that clearly describes a parent–child relationship should be modeled using classes. For example, since an orange is a fruit, their relationship should be modeled using class inheritance. A weak is-a relationship, also known as an is-kind-of relationship, indicates that an object possesses a certain property. A weak is-a relationship can be modeled using interfaces. For example, all strings are comparable, so the `String` class implements the `Comparable` interface. A circle or a rectangle is a geometric object, so `Circle` can be designed as a subclass of `GeometricObject`. Circles are different and comparable based on their radii, so `Circle` can implement the `Comparable` interface.

Interfaces are more flexible than abstract classes, because a subclass can extend only one superclass but can implement any number of interfaces. However, interfaces cannot contain concrete methods. The virtues of interfaces and abstract classes can be combined by creating an interface with an abstract class that implements it. Then you can use the interface or the abstract class, whichever is convenient. We will give examples of this type of design in Chapter 20, Lists, Stacks, Queues, and Priority Queues.

**Check Point**

Describe class design guidelines.

**Key Terms**

| abstract class | 496 | marker interface | 513 |
| abstract method | 496 | shallow copy | 515 |
| deep copy | 516 | subinterface | 518 |
| interface | 496 |

**Chapter Summary**

1. *Abstract classes* are like regular classes with data and methods, but you cannot create instances of abstract classes using the `new` operator.

2. An *abstract method* cannot be contained in a nonabstract class. If a subclass of an abstract superclass does not implement all the inherited abstract methods of the superclass, the subclass must be defined as abstract.

3. A class that contains abstract methods must be abstract. However, it is possible to define an abstract class that doesn’t contain any abstract methods.

4. A subclass can be abstract even if its superclass is concrete.

5. An *interface* is a class-like construct that contains only constants and abstract methods. In many ways, an interface is similar to an abstract class, but an abstract class can contain constants and abstract methods as well as variables and concrete methods.

6. An interface is treated like a special class in Java. Each interface is compiled into a separate bytecode file, just like a regular class.

7. The `java.lang.Comparable` interface defines the `compareTo` method. Many classes in the Java library implement `Comparable`. 
8. The `java.lang.Cloneable` interface is a *marker interface*. An object of the class that implements the `Cloneable` interface is cloneable.

9. A class can extend only one superclass but can implement one or more interfaces.

10. An interface can extend one or more interfaces.

**Quiz**

Answer the quiz for this chapter online at [www.cs.armstrong.edu/liang/intro10e/quiz.html](http://www.cs.armstrong.edu/liang/intro10e/quiz.html).

**PROGRAMMING EXERCISES**

Sections 13.2–13.3

**13.1 (Triangle class)** Design a new `Triangle` class that extends the abstract `GeometricObject` class. Draw the UML diagram for the classes `Triangle` and `GeometricObject` and then implement the `Triangle` class. Write a test program that prompts the user to enter three sides of the triangle, a color, and a Boolean value to indicate whether the triangle is filled. The program should create a `Triangle` object with these sides and set the color and filled properties using the input. The program should display the area, perimeter, color, and true or false to indicate whether it is filled or not.

**13.2 (Shuffle ArrayList)** Write the following method that shuffles an `ArrayList` of numbers:

```java
public static void shuffle(ArrayList<Number> list)
```

**13.3 (Sort ArrayList)** Write the following method that sorts an `ArrayList` of numbers.

```java
public static void sort(ArrayList<Number> list)
```

**13.4 (Display calendars)** Rewrite the `PrintCalendar` class in Listing 6.12 to display a calendar for a specified month using the `Calendar` and `GregorianCalendar` classes. Your program receives the month and year from the command line. For example:

```java
java Exercise13_04 5 2016
```

This displays the calendar shown in Figure 13.9.

![Calendar Display](image)
You also can run the program without the year. In this case, the year is the current year. If you run the program without specifying a month and a year, the month is the current month.

Sections 13.4–13.8

*13.5 (Enable GeometricObject comparable) Modify the GeometricObject class to implement the Comparable interface, and define a static max method in the GeometricObject class for finding the larger of two GeometricObject objects. Draw the UML diagram and implement the new GeometricObject class. Write a test program that uses the max method to find the larger of two circles and the larger of two rectangles.

*13.6 (The ComparableCircle class) Define a class named ComparableCircle that extends Circle and implements Comparable. Draw the UML diagram and implement the compareTo method to compare the circles on the basis of area. Write a test class to find the larger of two instances of ComparableCircle objects.

*13.7 (The Colorable interface) Design an interface named Colorable with a void method named howToColor(). Every class of a colorable object must implement the Colorable interface. Design a class named Square that extends GeometricObject and implements Colorable. Implement howToColor to display the message Color all four sides. Draw a UML diagram that involves Colorable, Square, and GeometricObject. Write a test program that creates an array of five GeometricObject objects. For each object in the array, display its area and invoke its howToColor method if it is colorable.

*13.8 (Revise the MyStack class) Rewrite the MyStack class in Listing 11.10 to perform a deep copy of the list field.

*13.9 (Enable Circle comparable) Rewrite the Circle class in Listing 13.2 to extend GeometricObject and implement the Comparable interface. Override the equals method in the Object class. Two Circle objects are equal if their radii are the same. Draw the UML diagram that involves Circle, GeometricObject, and Comparable.

*13.10 (Enable Rectangle comparable) Rewrite the Rectangle class in Listing 13.3 to extend GeometricObject and implement the Comparable interface. Override the equals method in the Object class. Two Rectangle objects are equal if their areas are the same. Draw the UML diagram that involves Rectangle, GeometricObject, and Comparable.

*13.11 (The Octagon class) Write a class named Octagon that extends GeometricObject and implements the Comparable and Cloneable interfaces. Assume that all eight sides of the octagon are of equal length. The area can be computed using the following formula:

\[
\text{area} = (2 + 4/\sqrt{2}) \times \text{side} \times \text{side}
\]

Draw the UML diagram that involves Octagon, GeometricObject, Comparable, and Cloneable. Write a test program that creates an Octagon object with side value 5 and displays its area and perimeter. Create a new object using the clone method and compare the two objects using the compareTo method.

*13.12 (Sum the areas of geometric objects) Write a method that sums the areas of all the geometric objects in an array. The method signature is:

```java
public static double sumArea(GeometricObject[] a)
```
Write a test program that creates an array of four objects (two circles and two rectangles) and computes their total area using the `sumArea` method.

*13.13 (Enable the Course class cloneable) Rewrite the Course class in Listing 10.6 to add a `clone` method to perform a deep copy on the students field.

Section 13.9

*13.14 (Demonstrate the benefits of encapsulation) Rewrite the Rational class in Listing 13.13 using a new internal representation for the numerator and denominator. Create an array of two integers as follows:

```java
private long[] r = new long[2];
```

Use `r[0]` to represent the numerator and `r[1]` to represent the denominator. The signatures of the methods in the Rational class are not changed, so a client application that uses the previous Rational class can continue to use this new Rational class without being recompiled.

*13.15 (Use BigInteger for the Rational class) Redesign and implement the Rational class in Listing 13.13 using BigInteger for the numerator and denominator.

*13.16 (Create a rational-number calculator) Write a program similar to Listing 7.9, Calculator.java. Instead of using integers, use rationals, as shown in Figure 13.10a. You will need to use the `split` method in the String class, introduced in Section 10.10.3, Replacing and Splitting Strings, to retrieve the numerator string and denominator string, and convert strings into integers using the `Integer.parseInt` method.

*13.17 (Math: The Complex class) A complex number is a number in the form `a + bi`, where `a` and `b` are real numbers and `i` is \(\sqrt{-1}\). The numbers `a` and `b` are known as the real part and imaginary part of the complex number, respectively. You can perform addition, subtraction, multiplication, and division for complex numbers using the following formulas:

\[
a + bi + c + di = (a + c) + (b + d)i \\
a + bi - (c + di) = (a - c) + (b - d)i \\
(a + bi)^*(c + di) = (ac - bd) + (bc + ad)i \\
(a + bi) / (c + di) = (ac + bd)(c^2 + d^2) + (bc - ad)i(c^2 + d^2)
\]
You can also obtain the absolute value for a complex number using the following formula:

$$|a + bi| = \sqrt{a^2 + b^2}$$

(A complex number can be interpreted as a point on a plane by identifying the \((a, b)\) values as the coordinates of the point. The absolute value of the complex number corresponds to the distance of the point to the origin, as shown in Figure 13.10b.)

Design a class named `Complex` for representing complex numbers and the methods `add`, `subtract`, `multiply`, `divide`, and `abs` for performing complex-number operations, and override `toString` method for returning a string representation for a complex number. The `toString` method returns \((a + bi)\) as a string. If \(b\) is 0, it simply returns \(a\). Your `Complex` class should also implement the `Cloneable` interface.

Provide three constructors `Complex(a, b)`, `Complex(a)`, and `Complex()`. `Complex()` creates a `Complex` object for number 0 and `Complex(a)` creates a `Complex` object with 0 for \(b\). Also provide the `getRealPart()` and `getImaginaryPart()` methods for returning the real and imaginary part of the complex number, respectively.

Write a test program that prompts the user to enter two complex numbers and displays the result of their addition, subtraction, multiplication, division, and absolute value. Here is a sample run:

```
Enter the first complex number: 3.5 5.5
Enter the second complex number: -3.5 1
(3.5 + 5.5i) + (-3.5 + 1.0i) = 0.0 + 6.5i
(3.5 + 5.5i) - (-3.5 + 1.0i) = 7.0 + 4.5i
(3.5 + 5.5i) * (-3.5 + 1.0i) = -17.75 + -13.75i
(3.5 + 5.5i) / (-3.5 + 1.0i) = -0.5094 + -1.7i
| (3.5 + 5.5i) | = 6.519202405202649
```

13.18 (*Use the `Rational` class*) Write a program that computes the following summation series using the `Rational` class:

$$\frac{1}{2} + \frac{2}{3} + \frac{3}{4} + \ldots + \frac{98}{99} + \frac{99}{100}$$

You will discover that the output is incorrect because of integer overflow (too large). To fix this problem, see Programming Exercise 13.15.

13.19 (*Convert decimals to fractions*) Write a program that prompts the user to enter a decimal number and displays the number in a fraction. Hint: read the decimal number as a string, extract the integer part and fractional part from the string, and use the `BigInteger` implementation of the `Rational` class in Programming Exercise 13.15 to obtain a rational number for the decimal number. Here are some sample runs:

```
Enter a decimal number: 3.25
The fraction number is 13/4
```
13.20  (Algebra: solve quadratic equations) Rewrite Programming Exercise 3.1 to obtain imaginary roots if the determinant is less than 0 using the Complex class in Programming Exercise 13.17. Here are some sample runs.

```
Enter a, b, c: 1 3 1
The roots are -0.381966 and -2.61803
```

```
Enter a, b, c: 1 2 1
The root is -1
```

```
Enter a, b, c: 1 2 3
The roots are -1.0 + 1.4142i and -1.0 + -1.4142i
```

13.21  (Algebra: vertex form equations) The equation of a parabola can be expressed in either standard form \((y = ax^2 + bx + c)\) or vertex form \((y = a(x - h)^2 + k)\). Write a program that prompts the user to enter \(a\), \(b\), and \(c\) as integers in standard form and displays \(h\) and \(k\) in the vertex form. Here are some sample runs.

```
Enter a, b, c: 1 3 1
h is -3/2 k is -5/4
```

```
Enter a, b, c: 2 3 4
h is -3/4 k is 23/8
```
JAVAFX BASICS

Objectives

■ To distinguish between JavaFX, Swing, and AWT (§14.2).
■ To write a simple JavaFX program and understand the relationship among stages, scenes, and nodes (§14.3).
■ To create user interfaces using panes, UI controls, and shapes (§14.4).
■ To update property values automatically through property binding (§14.5).
■ To use the common properties style and rotate for nodes (§14.6).
■ To create colors using the Color class (§14.7).
■ To create fonts using the Font class (§14.8).
■ To create images using the Image class and to create image views using the ImageView class (§14.9).
■ To layout nodes using Pane, StackPane, FlowPane, GridPane, BorderPane, HBox, and VBox (§14.10).
■ To display text using the Text class and create shapes using Line, Circle, Rectangle, Ellipse, Arc, Polygon, and Polyline (§14.11).
■ To develop the reusable GUI component ClockPane for displaying an analog clock (§14.12).
14.1 Introduction

JavaFX is a new framework for developing Java GUI programs. The JavaFX API is an excellent example of how the object-oriented principles are applied. This chapter serves two purposes. First, it presents the basics of JavaFX programming. Second, it uses JavaFX to demonstrate object-oriented design and programming. Specifically, this chapter introduces the framework of JavaFX and discusses JavaFX GUI components and their relationships. You will learn how to develop simple GUI programs using layout panes, buttons, labels, text fields, colors, fonts, images, image views, and shapes.

14.2 JavaFX vs Swing and AWT

Swing and AWT are replaced by the JavaFX platform for developing rich Internet applications.

When Java was introduced, the GUI classes were bundled in a library known as the Abstract Windows Toolkit (AWT). AWT is fine for developing simple graphical user interfaces, but not for developing comprehensive GUI projects. In addition, AWT is prone to platform-specific bugs. The AWT user-interface components were replaced by a more robust, versatile, and flexible library known as Swing components. Swing components are painted directly on canvases using Java code. Swing components depend less on the target platform and use less of the native GUI resources. Swing is designed for developing desktop GUI applications. It is now replaced by a completely new GUI platform known as JavaFX. JavaFX incorporates modern GUI technologies to enable you to develop rich Internet applications. A rich Internet application (RIA) is a Web application designed to deliver the same features and functions normally associated with desktop applications. A JavaFX application can run seamlessly on a desktop and from a Web browser. Additionally, JavaFX provides a multi-touch support for touch-enabled devices such as tablets and smart phones. JavaFX has a built-in 2D, 3D, animation support, video and audio playback, and runs as a stand-alone application or from a browser.

This book teaches Java GUI programming using JavaFX for two reasons. First, JavaFX is much simpler to learn and use for new Java programmers. Second, Swing is essentially dead, because it will not receive any further enhancement. JavaFX is the new GUI tool for developing cross-platform-rich Internet applications on desktop computers, on hand-held devices, and on the Web.

14.1 Explain the evolution of Java GUI technologies.

14.2 Explain why this book teaches Java GUI using JavaFX.

14.3 The Basic Structure of a JavaFX Program

The abstract javafx.application.Application class defines the essential framework for writing JavaFX programs.

We begin by writing a simple JavaFX program that illustrates the basic structure of a JavaFX program. Every JavaFX program is defined in a class that extends javafx.application.Application, as shown in Listing 14.1:

Listing 14.1 MyJavaFX.java

```
1 import javafx.application.Application;
2 import javafx.scene.Scene;
3 import javafx.scene.control.Button;
4 import javafx.stage.Stage;
```
14.3 The Basic Structure of a JavaFX Program

```java
public class MyJavaFX extends Application {

    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a scene and place a button in the scene
        Button btOK = new Button("OK");
        Scene scene = new Scene(btOK, 200, 250);
        primaryStage.setTitle("MyJavaFX"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }

    /**
     * The main method is only needed for the IDE with limited
     * JavaFX support. Not needed for running from the command line.
     */
    public static void main(String[] args) {
        Application.launch(args);
    }
}
```

You can test and run your program from a command window or from an IDE such as NetBeans or Eclipse. A sample run of the program is shown in Figure 14.1. Supplements II.F–H give the tips for running JavaFX programs from a command window, NetBeans, and Eclipse. A JavaFX program can run stand-alone or from a Web browser. For running a JavaFX program from a Web browser, see Supplement II.I.

![Figure 14.1](image)

A simple JavaFX displays a button in the window.

The `launch` method (line 22) is a static method defined in the `Application` class for launching a stand-alone JavaFX application. The `main` method (lines 21–23) is not needed if you run the program from the command line. It may be needed to launch a JavaFX program from an IDE with a limited JavaFX support. When you run a JavaFX application without a main method, JVM automatically invokes the `launch` method to run the application.

The main class overrides the `start` method defined in `javafx.application.Application` (line 8). After a JavaFX application is launched, the JVM constructs an instance of the class using its `no-arg` constructor and invokes its `start` method. The `start` method normally places UI controls in a scene and displays the scene in a stage, as shown in Figure 14.2a.

Line 10 creates a `Button` object and places it in a `Scene` object (line 11). A `Scene` object can be created using the constructor `Scene(node, width, height)`. This constructor specifies the width and height of the scene and places the node in the scene.

A `Stage` object is a window. A `Stage` object called `primary stage` is automatically created by the JVM when the application is launched. Line 13 sets the scene to the primary stage and line 14 displays the primary stage. JavaFX names the `Stage` and `Scene` classes using the analogy from the theater. You may think stage as the platform to support scenes and nodes as actors to perform in the scenes.

You can create additional stages if needed. The JavaFX program in Listing 14.2 displays two stages, as shown in Figure 14.2b.
Chapter 14  JavaFX Basics

Listing 14.2  MultipleStageDemo.java

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.stage.Stage;

public class MultipleStageDemo extends Application {

    @Override
    public void start(Stage primaryStage) {
        Scene scene = new Scene(new Button("OK"), 200, 250);
        primaryStage.setTitle("MyJavaFX");
        primaryStage.setScene(scene);
        primaryStage.show();

        Stage stage = new Stage();
        stage.setTitle("Second Stage");
        stage.setScene(new Scene(new Button("New Stage"), 100, 100));
        stage.show();
    }
}
```

Note that the main method is omitted in the listing since it is identical for every JavaFX application. From now on, we will not list the main method in our JavaFX source code for brevity.

By default, the user can resize the stage. To prevent the user from resizing the stage, invoke `stage.setResizable(false)`.

Check Point

14.3 How do you define a JavaFX main class? What is the signature of the start method? What is a stage? What is a primary stage? Is a primary stage automatically created? How do you display a stage? Can you prevent the user from resizing the stage? Can you replace `Application.launch(args)` by `launch(args)` in line 22 in Listing 14.1?

14.4 Show the output of the following JavaFX program.

```java
import javafx.application.Application;
import javafx.stage.Stage;

public class Test extends Application {
    public Test() {
        System.out.println("Test constructor is invoked");
    }
}
```
@Override // Override the start method in the Application class
public void start(Stage primaryStage) {
    System.out.println("start method is invoked");
}

public static void main(String[] args) {
    System.out.println("launch application");
    Application.launch(args);
}

14.4 Panes, UI Controls, and Shapes

Panes, UI controls, and shapes are subtypes of Node.

When you run MyJavaFX in Listing 14.1, the window is displayed as shown in Figure 14.1. The button is always centered in the scene and occupies the entire window no matter how you resize it. You can fix the problem by setting the position and size properties of a button. However, a better approach is to use container classes, called panes, for automatically laying out the nodes in a desired location and size. You place nodes inside a pane and then place the pane into a scene. A node is a visual component such as a shape, an image view, a UI control, or a pane. A shape refers to a text, line, circle, ellipse, rectangle, arc, polygon, polyline, etc. A UI control refers to a label, button, check box, radio button, text field, text area, etc. A scene can be displayed in a stage, as shown in Figure 14.3a. The relationship among Stage, Scene, Node, Control, and Pane is illustrated in the UML diagram, as shown in Figure 14.3b. Note that a Scene can contain a Control or a Pane, but not a Shape or an ImageView. A Pane can contain any subtype of Node. You can create a Scene using the constructor Scene(Parent, width, height) or Scene(Parent). The dimension of the scene is automatically decided in the latter constructor. Every subclass of Node has a no-arg constructor for creating a default node.

Listing 14.3 gives a program that places a button in a pane, as shown in Figure 14.4.

Figure 14.3  (a) Panes are used to hold nodes. (b) Nodes can be shapes, image views, UI controls, and panes.
Listing 14.3  ButtonInPane.java

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.stage.Stage;
import javafx.scene.layout.StackPane;

public class ButtonInPane extends Application {
    @Override
    public void start(Stage primaryStage) {
        StackPane pane = new StackPane();
        pane.getChildren().add(new Button("OK"));
        Scene scene = new Scene(pane, 200, 50);
        primaryStage.setTitle("Button in a pane");
        primaryStage.setScene(scene);
        primaryStage.show();
    }
}
```

Figure 14.4  A button is placed in the center of the pane.

The program creates a StackPane (line 11) and adds a button as a child of the pane (line 12). The getChildren() method returns an instance of javafx.collections.ObservableList. ObservableList behaves very much like an ArrayList for storing a collection of elements. Invoking add(e) adds an element to the list. The StackPane places the nodes in the center of the pane on top of each other. Here, there is only one node in the pane. The StackPane respects a node’s preferred size. So you see the button displayed in its preferred size.

Listing 14.4 gives an example that displays a circle in the center of the pane, as shown in Figure 14.5a.

Listing 14.4  ShowCircle.java

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Circle;
import javafx.stage.Stage;

public class ShowCircle extends Application {
    @Override
    public void start(Stage primaryStage) {
        Circle circle = new Circle();
        circle.setCenterX(100);
        circle.setCenterY(100);
        circle.setRadius(50);
        circle.setStroke(Color.BLACK);
        circle.setFill(Color.WHITE);

        Pane pane = new Pane();
    }
}
```
```java
21     pane.getChildren().add(circle);
22     // Create a scene and place it in the stage
23     Scene scene = new Scene(pane, 200, 200);
24     primaryStage.setTitle("ShowCircle"); // Set the stage title
25     primaryStage.setScene(scene); // Place the scene in the stage
26     primaryStage.show(); // Display the stage
27     }
28     }
```

Figures 14.5 (a) A circle is displayed in the center of the scene. (b) The circle is not centered after the window is resized.

The program creates a Circle (line 12) and sets its center at (100, 100) (lines 13–14), which is also the center for the scene, since the scene is created with the width and height of 200 (line 24). The radius of the circle is set to 50 (line 15). Note that the measurement units for graphics in Java are all in pixels.

The stroke color (i.e., the color to draw the circle) is set to black (line 16). The fill color (i.e., the color to fill the circle) is set to white (line 17). You may set the color to null to specify that no color is set.

The program creates a Pane (line 20) and places the circle in the pane (line 21). Note that the coordinates of the upper left corner of the pane is (0, 0) in the Java coordinate system, as shown in Figure 14.6a, as opposed to the conventional coordinate system where (0, 0) is at the center of the window, as shown in Figure 14.6b. The x-coordinate increases from left to right and the y-coordinate increases downward in the Java coordinate system.

The pane is placed in the scene (line 24) and the scene is set in the stage (line 26). The circle is displayed in the center of the stage, as shown in Figure 14.5a. However, if you resize the window, the circle is not centered, as shown in Figure 14.5b. In order to display the circle centered as the window resizes, the x- and y-coordinates of the circle center need to be reset to the center of the pane. This can be done by using property binding, introduced in the next section.

Figure 14.6 The Java coordinate system is measured in pixels, with (0, 0) at its upper-left corner.
14.5 How do you create a Scene object? How do you set a scene in a stage? How do you place a circle into a scene?

14.6 What is a pane? What is a node? How do you place a node in a pane? Can you directly place a Shape or an ImageView into a Scene? Can you directly place a Control or a Pane into a Scene?

14.7 How do you create a Circle? How do you set its center location and radius? How do you set its stroke color and fill color?

### 14.5 Property Binding

You can bind a target object to a source object. A change in the source object will be automatically reflected in the target object.

JavaFX introduces a new concept called property binding that enables a target object to be bound to a source object. If the value in the source object changes, the target object is also changed automatically. The target object is called a binding object or a binding property and the source object is called a bindable object or observable object. As discussed in the preceding listing, the circle is not centered after the window is resized. In order to display the circle centered as the window resizes, the x- and y-coordinates of the circle center need to be reset to the center of the pane. This can be done by binding the centerX with pane’s width/2 and centerY with pane’s height/2, as shown in Listing 14.5.

#### Listing 14.5 ShowCircleCentered.java

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Circle;
import javafx.stage.Stage;

public class ShowCircleCentered extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a pane to hold the circle
        Pane pane = new Pane();

        // Create a circle and set its properties
        Circle circle = new Circle();
        circle.centerXProperty().bind(pane.widthProperty().divide(2));
        circle.centerYProperty().bind(pane.heightProperty().divide(2));
        circle.setStroke(Color.BLACK);
        circle.setFill(Color.WHITE);
        pane.getChildren().add(circle); // Add circle to the pane

        // Create a scene and place it in the stage
        Scene scene = new Scene(pane, 200, 200);
        primaryStage.setTitle("ShowCircleCentered"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }
}
```

The Circle class has the centerX property for representing the x-coordinate of the circle center. This property like many properties in JavaFX classes can be used both as target and source in a property binding. A target listens to the changes in the source and automatically
updates itself once a change is made in the source. A target binds with a source using the `bind` method as follows:

```
    target.bind(source);
```

The `bind` method is defined in the `javafx.beans.property.Property` interface. A binding property is an instance of `javafx.beans.property.Property`. A source object is an instance of the `javafx.beans.value.ObservableValue` interface. An `ObservableValue` is an entity that wraps a value and allows to observe the value for changes.

JavaFX defines binding properties for primitive types and strings. For a `double/float/long/int/boolean` value, its binding property type is `DoubleProperty/FloatProperty/LongProperty/IntegerProperty/BooleanProperty`. For a string, its binding property type is `StringProperty`. These properties are also subtypes of `ObservableValue`. So they can also be used as source objects for binding properties.

By convention, each binding property (e.g., `centerX`) in a JavaFX class (e.g., `Circle`) has a getter (e.g., `getCenterX()`) and setter (e.g., `setCenterX(double)`) method for returning and setting the property’s value. It also has a method for returning the property itself. The naming convention for this method is the property name followed by the word `Property`. For example, the property getter method for `centerX` is `centerXProperty()`. We call the `getCenterX()` method as the `value getter method`, the `setCenterX(double)` method as the `value setter method`, and `centerXProperty()` as the `property getter method`. Note that `getCenterX()` returns a `double` value and `centerXProperty()` returns an object of the `DoubleProperty` type.

Figure 14.7a shows the convention for defining a binding property in a class and Figure 14.7b shows a concrete example in which `centerX` is a binding property of the type `DoubleProperty`.

```
public class SomeClassName {
    private PropertyType x;
    /** Value getter method */
    public propertyValueType getX() { ... }
    /** Value setter method */
    public void setX(propertyValueType value) { ... }
    /** Property getter method */
    public PropertyType xProperty() { ... }
}
```

```
public class Circle {
    private DoubleProperty centerX;
    /** Value getter method */
    public double getCenterX() { ... }
    /** Value setter method */
    public void setCenterX(double value) { ... }
    /** Property getter method */
    public DoubleProperty centerXProperty() { ... }
}
```

(a) `x` is a binding property  (b) `centerX` is binding property

**Figure 14.7** A binding property has a value getter method, setter method, and property getter method.

The program in Listing 14.5 is the same as in Listing 14.4 except that it binds `circle's centerX` and `centerY` properties to half of `pane’s` width and height (lines 16–17). Note that `circle.centerXProperty()` returns `centerX` and `pane.widthProperty()` returns `width`. Both `centerX` and `width` are binding properties of the `DoubleProperty` type. The numeric binding property classes such as `DoubleProperty` and `IntegerProperty` contain the `add`, `subtract`, `multiply`, and `divide` methods for adding, subtracting, multiplying, and dividing a value in a binding property and returning a new observable property. So, `pane.widthProperty().divide(2)` returns a new observable property that represents half of the `pane’s` width. The statement

```
circle.centerXProperty().bind(pane.widthProperty().divide(2));
```

is same as

```
centerX.bind(width.divide(2));
```
Since centerX is bound to width.divide(2), when pane’s width is changed, centerX automatically updates itself to match pane’s width / 2.

Listing 14.6 gives another example that demonstrates bindings.

**Listing 14.6 BindingDemo.java**

```java
class BindingDemo {  
    public static void main(String[] args) {  
        DoubleProperty d1 = new SimpleDoubleProperty(1);  
        DoubleProperty d2 = new SimpleDoubleProperty(2);  
        d1.bind(d2);  
        System.out.println("d1 is " + d1.getValue()  
            + " and d2 is " + d2.getValue());  
        d2.setValue(70.2);  
        System.out.println("d1 is " + d1.getValue()  
            + " and d2 is " + d2.getValue());  
    }  
}
```

The program creates an instance of DoubleProperty using SimpleDoubleProperty(1) (line 6). Note that DoubleProperty, FloatProperty, LongProperty, IntegerProperty, and BooleanProperty are abstract classes. Their concrete subclasses SimpleDoubleProperty, SimpleFloatProperty, SimpleLongProperty, SimpleIntegerProperty, and SimpleBooleanProperty are used to create instances of these properties. These classes are very much like wrapper classes Double, Float, Long, Integer, and Boolean with additional features for binding to a source object.

The program binds d1 with d2 (line 8). Now the values in d1 and d2 are the same. After setting d2 to 70.2 (line 11), d1 also becomes 70.2 (line 13).

The binding demonstrated in this example is known as *unidirectional binding*. Occasionally, it is useful to synchronize two properties so that a change in one property is reflected in another object, and vice versa. This is called a *bidirectional binding*. If the target and source are both binding properties and observable properties, they can be bound bidirectionally using the bindBidirectional method.

14.8 What is a binding property? What interface defines a binding property? What interface defines a source object? What are the binding object types for int, long, float, double, and boolean? Are Integer and Double binding properties? Can Integer and Double be used as source objects in a binding?

14.9 Following the JavaFX binding property naming convention, for a binding property named age of the IntegerProperty type, what is its value getter method, value setter method, and property getter method?

14.10 Can you create an object of IntegerProperty using new IntegerProperty(3)? If not, what is the correct way to create it? What will the output if line 8 is replaced by d1.bind(d2.multiply(2)) in Listing 14.6? What will the output if line 8 is replaced by d1.bind(d2.add(2)) in Listing 14.6?

14.11 What is a unidirectional binding and what is bidirectional binding? Are all binding properties capable of bidirectional binding? Write a statement to bind property d1 with property d2 bidirectionally.
14.6 Common Properties and Methods for Nodes

The abstract Node class defines many properties and methods that are common to all nodes.

Nodes share many common properties. This section introduces two such properties style and rotate.

JavaFX style properties are similar to cascading style sheets (CSS) used to specify the styles for HTML elements in a Web page. So, the style properties in JavaFX are called JavaFX CSS. In JavaFX, a style property is defined with a prefix -fx-. Each node has its own style properties. You can find these properties from http://docs.oracle.com/javafx/2/api/javafx/scene/doc-files/cssref.html. For information on HTML and CSS, see Supplements V.A and V.B. If you are not familiar with HTML and CSS, you can still use JavaFX CSS.

The syntax for setting a style is styleName:value. Multiple style properties for a node can be set together separated by semicolon (;). For example, the following statement

circle.setStyle("-fx-stroke: black; -fx-fill: red;");

sets two JavaFX CSS properties for a circle. This statement is equivalent to the following two statements.

circle.setStroke(Color.BLACK);
circle.setFill(Color.RED);

If an incorrect JavaFX CSS is used, your program will still compile and run, but the style is ignored.

The rotate property enables you to specify an angle in degrees for rotating the node from its center. If the degree is positive, the rotation is performed clockwise; otherwise, it is performed counterclockwise. For example, the following code rotates a button 80 degrees.

button.setRotate(80);

Listing 14.7 gives an example that creates a button, sets its style, and adds it to a pane. It then rotates the pane 45 degrees and set its style with border color red and background color light gray, as shown in Figure 14.8.

LISTING 14.7 NodeStyleRotateDemo.java

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.stage.Stage;
import javafx.scene.layout.StackPane;

public class NodeStyleRotateDemo extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a scene and place a button in the scene
        StackPane pane = new StackPane();
        Button btOK = new Button("OK");
        btOK.setStyle("-fx-border-color: blue;");
        pane.getChildren().add(btOK);

        pane.setRotate(45);
        pane.setStyle("-fx-border-color: red; -fx-background-color: lightgray;");;

        Scene scene = new Scene(pane, 200, 250);
        primaryStage.setTitle("NodeStyleRotateDemo"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
    }
}
```
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```java
23    primaryStage.show(); // Display the stage
24  }
25  }
```

![Image of JavaFX demo](image)

**Figure 14.8** A pane’s style is set and it is rotated 45 degrees.

As seen in Figure 14.8, the rotate on a pane causes all its containing nodes rotated too.

The `Node` class contains many useful methods that can be applied to all nodes. For example, you can use the `contains(double x, double y)` method to test where a point \((x, y)\) is inside the boundary of a node.

14.12 How do you set a style of a node with border color red? Modify the code to set the text color for the button to red.

14.13 Can you rotate a pane, a text, or a button? Modify the code to rotate the button 15 degrees counterclockwise?

14.7 The **Color** Class

*The Color class can be used to create colors.*

JavaFX defines the abstract `Paint` class for painting a node. The `javafx.scene.paint.Color` is a concrete subclass of `Paint`, which is used to encapsulate colors, as shown in Figure 14.9.

![UML diagram of Color class](image)

**Figure 14.9** `Color` encapsulates information about colors.
A color instance can be constructed using the following constructor:

```java
public Color(double r, double g, double b, double opacity);
```

in which `r`, `g`, and `b` specify a color by its red, green, and blue components with values in the range from 0.0 (darkest shade) to 1.0 (lightest shade). The `opacity` value defines the transparency of a color within the range from 0.0 (completely transparent) to 1.0 (completely opaque). This is known as the RGBA model, where RGBA stands for red, green, blue, and alpha. The alpha value indicates the opacity. For example,

```java
Color color = new Color(0.25, 0.14, 0.333, 0.51);
```

The `Color` class is immutable. Once a `Color` object is created, its properties cannot be changed. The `brighter()` method returns a new `Color` with a larger red, green, and blue values and the `darker()` method returns a new `Color` with a smaller red, green, and blue values. The `opacity` value is the same as in the original `Color` object.

You can also create a `Color` object using the static methods `color(r, g, b), color(r, g, b, opacity), rgb(r, g, b), and rgb(r, g, b, opacity).` Alternatively, you can use one of the many standard colors such as `BEIGE, BLACK, BLUE, BROWN, CYAN, DARKGRAY, GOLD, GRAY, GREEN, LIGHTGRAY, MAGENTA, NAVY, ORANGE, PINK, RED, SILVER, WHITE,` and `YELLOW` defined as constants in the `Color` class. The following code, for instance, sets the fill color of a circle to red:

```java
circle.setFill(Color.RED);
```

### 14.14 How do you create a color? What is wrong about creating a `Color` using `new Color(1.2, 2.3, 3.5, 4)`? Which of two colors is darker, `new Color(0, 0, 0, 1)` or `new Color(1, 1, 1, 1)`? Does invoking `c.darker()` change the color value in `c`?

### 14.15 How do you create a `Color` object with a random color?

### 14.16 How do you set a circle object `c` with blue fill color using the `setFill` method and using the `setStyle` method?

### 14.8 The `Font` Class

A `Font` describes font name, weight, and size.

You can set fonts for rendering the text. The `javafx.scene.text.Font` class is used to create fonts, as shown in Figure 14.10.

A `Font` instance can be constructed using its constructors or using its static methods. A `Font` is defined by its name, weight, posture, and size. Times, Courier, and Arial are the examples of the font names. You can obtain a list of available font family names by invoking the static `getFamilies()` method. `List` is an interface that defines common methods for a list. `ArrayList` is a concrete implementation of `List`. The font postures are two constants: `FontPosture.ITALIC` and `FontPosture.REGULAR`. For example, the following statements create two fonts.

```java
Font font1 = new Font("SansSerif", 16);
Font font2 = Font.font("Times New Roman", FontWeight.BOLD, FontPosture.ITALIC, 12);
```

Listing 14.8 gives a program that displays a label using the font (Times New Roman, bold, italic, and size 20), as shown in Figure 14.11.
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LISTING 14.8  FontDemo.java

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.layout.*;
import javafx.scene.paint.Color;
import javafx.scene.shape.Circle;
import javafx.scene.text.*;
import javafx.scene.control.*;
import javafx.stage.Stage;

public class FontDemo extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a pane to hold the circle
        Pane pane = new StackPane();

        // Create a circle and set its properties
        Circle circle = new Circle();
        circle.setRadius(50);
        circle.setStroke(Color.BLACK);
        circle.setFill(new Color(0.5, 0.5, 0.5, 0.1));
        pane.getChildren().add(circle); // Add circle to the pane

        // Create a label and set its properties
        Label label = new Label("JavaFX");
        pane.getChildren().add(label); // Add label to the pane

        // Create a scene and place it in the stage
        Scene scene = new Scene(pane);
        primaryStage.setTitle("FontDemo"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
    }
}
```

**FIGURE 14.10**  Font encapsulates information about fonts.

```java
javafx.scene.text.Font
- size: double
- name: String
- family: String

+ Font(size: double)
+ Font(name: String, size: double)
+ font(name: String, size: double)
+ font(name: String, w: FontWeight, size: double)
+ font(name: String, w: FontWeight, p: FontPosture, size: double)
+ getFamilies(): List<String>
+ getFontNames(): List<String>
```

The size of this font.
The name of this font.
The family of this font.

Creates a Font with the specified size.
Creates a Font with the specified full font name and size.
Creates a Font with the specified name and size.
Creates a Font with the specified name, weight, and size.
Creates a Font with the specified name, weight, posture, and size.
Returns a list of font family names.
Returns a list of full font names including family and weight.
The program creates a StackPane (line 14) and adds a circle and a label to it (lines 21, 27). These two statements can be combined using the following one statement:

```java
pane.getChildren().addAll(circle, label);
```

A StackPane places the nodes in the center and nodes are placed on top of each other. A custom color is created and set as a fill color for the circle (line 20). The program creates a label and sets a font (line 25) so the text in the label is displayed in Times New Roman, bold, italic, and 20 pixels.

As you resize the window, the circle and label are displayed in the center of the window, because the circle and label are placed in the stack pane. Stack pane automatically places nodes in the center of the pane.

A Font object is immutable. Once a Font object is created, its properties cannot be changed.

**14.17** How do you create a Font object with font name Courier, size 20, and weight bold?

**14.18** How do you find all available fonts on your system?

### 14.9 The Image and ImageView Classes

The Image class represents a graphical image and the ImageView class can be used to display an image.

The javafx.scene.image.Image class represents a graphical image and is used for loading an image from a specified filename or a URL. For example, `new Image("image/us.gif")` creates an Image object for the image file `us.gif` under the directory `image` in the Java class directory and `new Image("http://www.cs.armstrong.edu/liang/image/us.gif")` creates an Image object for the image file in the URL on the Web.

The javafx.scene.image.ImageView is a node for displaying an image. An ImageView can be created from an Image object. For example, the following code creates an ImageView from an image file:

```java
Image image = new Image("image/us.gif");
ImageView imageView = new ImageView(image);
```

Alternatively, you can create an ImageView directly from a file or a URL as follows:

```java
ImageView imageView = new ImageView("image/us.gif");
```

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Listing 14.9 displays an image in three image views, as shown in Figure 14.14.

Listing 14.9  ShowImage.java

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.layout.HBox;
import javafx.scene.layout.Pane;
import javafx.geometry.Insets;
import javafx.stage.Stage;
import javafx.scene.image.Image;
import javafx.scene.image.ImageView;

public class ShowImage extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        Pane pane = new HBox(10);
        pane.setPadding(new Insets(5, 5, 5, 5));
        Image image = new Image("image/us.gif");
        pane.getChildren().add(new ImageView(image));

        ImageView imageView2 = new ImageView(image);
        imageView2.setFitHeight(100);
        imageView2.setFitWidth(100);
    }
}
```

Figure 14.12  Image encapsulates information about images.

Figure 14.13  ImageView is a node for displaying an image.

Listing 14.9 displays an image in three image views, as shown in Figure 14.14.
22    pane.getChildren().add(imageView2);
23    
24    ImageView imageView3 = new ImageView(image);
25    imageView3.setRotate(90);
26    pane.getChildren().add(imageView3);
27    
28    // Create a scene and place it in the stage
29    Scene scene = new Scene(pane);
30    primaryStage.setTitle("ShowImage"); // Set the stage title
31    primaryStage.setScene(scene); // Place the scene in the stage
32    primaryStage.show(); // Display the stage
33    }
34  }

The program creates an HBox (line 14). An HBox is a pane that places all nodes horizontally in one row. The program creates an ImageView, and then an ImageView for displaying the image, and places the ImageView in the HBox (line 17).

The program creates the second ImageView (line 19), sets its fitHeight and fitWidth properties (lines 20–21) and places the ImageView into the HBox (line 22). The program creates the third ImageView (line 24), rotates it 90 degrees (line 25), and places it into the HBox (line 26). The setRotate method is defined in the Node class and can be used for any node. Note that an Image object can be shared by multiple nodes. In this case, it is shared by three ImageView. However, a node such as ImageView cannot be shared. You cannot place an ImageView multiple times into a pane or scene.

Note that you must place the image file in the same directory as the class file, as shown in the following figure.

Figure 14.14 An image is displayed in three image views placed in a pane.

If you use the URL to locate the image file, the URL protocol http:// must be present. So the following code is wrong.

    new Image("www.cs.armstrong.edu/liang/image/us.gif");

It must be replaced by

    new Image("http://www.cs.armstrong.edu/liang/image/us.gif");
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14.19 How do you create an Image from a URL or a filename?
14.20 How do you create an ImageView from an Image, or directly from a file or a URL?
14.21 Can you set an Image to multiple ImageView? Can you display the same ImageView multiple times?

14.10 Layout Panes

JavaFX provides many types of panes for automatically laying out nodes in a desired location and size.

JavaFX provides many types of panes for organizing nodes in a container, as shown in Table 14.1. You have used the layout panes Pane, StackPane, and HBox in the preceding sections for containing nodes. This section introduces the panes in more details.

<table>
<thead>
<tr>
<th>Class</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pane</td>
<td>Base class for layout panes. It contains the getChildren() method for returning a list of nodes in the pane.</td>
</tr>
<tr>
<td>StackPane</td>
<td>Places the nodes on top of each other in the center of the pane.</td>
</tr>
<tr>
<td>FlowPane</td>
<td>Places the nodes row-by-row horizontally or column-by-column vertically.</td>
</tr>
<tr>
<td>GridPane</td>
<td>Places the nodes in the cells in a two-dimensional grid.</td>
</tr>
<tr>
<td>BorderPane</td>
<td>Places the nodes in the top, right, bottom, left, and center regions.</td>
</tr>
<tr>
<td>HBox</td>
<td>Places the nodes in a single row.</td>
</tr>
<tr>
<td>VBox</td>
<td>Places the nodes in a single column.</td>
</tr>
</tbody>
</table>

You have used the Pane in Listing 14.4, ShowCircle.java. A Pane is usually used as a canvas for displaying shapes. Pane is the base class for all specialized panes. You have used a specialized pane StackPane in Listing 14.3, ButtonInPane.java. Nodes are placed in the center of a StackPane. Each pane contains a list for holding nodes in the pane. This list is an instance of ObservableList, which can be obtained using pane’s getChildren() method. You can use the add(node) method to add an element to the list, use addAll(node1, node2, ...) to add a variable number of nodes to the pane.

14.10.1 FlowPane

FlowPane arranges the nodes in the pane horizontally from left to right or vertically from top to bottom in the order in which they were added. When one row or one column is filled, a new row or column is started. You can specify the way the nodes are placed horizontally or vertically using one of two constants: Orientation.HORIZONTAL or Orientation.VERTICAL. You can also specify the gap between the nodes in pixels. The class diagram for FlowPane is shown in Figure 14.15.

Data fields alignment, orientation, hgap, and vgap are binding properties. Each binding property in JavaFX has a getter method (e.g., getHgap()) that returns its value, a setter method (e.g., sethGap(double)) for setting a value, and a getter method that returns the property itself (e.g., hGapProperty()). For a data field of ObjectProperty type, the value getter method returns a value of type T and the property getter method returns a property value of type ObjectProperty<T>.
Listing 14.10 gives a program that demonstrates FlowPane. The program adds labels and text fields to a FlowPane, as shown in Figure 14.16.

LISTING 14.10  ShowFlowPane.java

```java
import javafx.application.Application;
import javafx.geometry.Insets;
import javafx.scene.Scene;
import javafx.scene.control.Label;
import javafx.scene.control.TextField;
import javafx.scene.layout.FlowPane;
import javafx.stage.Stage;

public class ShowFlowPane extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a pane and set its properties
        FlowPane pane = new FlowPane();
        pane.setPadding(new Insets(11, 12, 13, 14));
        pane.setHgap(5);
        pane.setVgap(5);

        // Place nodes in the pane
        pane.getChildren().addAll(new Label("First Name:"),
                                  new TextField(),
                                  new Label("MI:"),
                                  new TextField());

        // Create a scene and place it in the stage
        Scene scene = new Scene(pane, 200, 250);
        primaryStage.setTitle("ShowFlowPane"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }
}
```

Figure 14.15  FlowPane lays out nodes row by row horizontally or column by column vertically.
The program creates a `FlowPane` (line 13) and sets its `padding` property with an `Insets` object (line 14). An `Insets` object specifies the size of the border of a pane. The constructor `Insets(11, 12, 13, 14)` creates an `Insets` with the border sizes for top (11), right (12), bottom (13), and left (14) in pixels, as shown in Figure 14.17. You can also use the constructor `Insets(value)` to create an `Insets` with the same value for all four sides. The `hGap` and `vGap` properties are in lines 15–16 to specify the horizontal gap and vertical gap between two nodes in the pane, as shown in Figure 14.17.

![Figure 14.16](image1.png)

**Figure 14.16** The nodes fill in the rows in the `FlowPane` one after another.

![Figure 14.17](image2.png)

**Figure 14.17** You can specify `hGap` and `vGap` between the nodes in a `FlowPane`.

Each `FlowPane` contains an object of `ObservableList` for holding the nodes. This list can be obtained using the `getChildren()` method (line 19). To add a node into a `FlowPane` is to add it to this list using the `add(node)` or `addAll(node1, node2, ...)` method. You can also remove a node from the list using the `remove(node)` method or use the `removeAll()` method to remove all nodes from the pane. The program adds the labels and text fields into the pane (lines 19–24). Invoking `tfMi.setPrefColumnCount(1)` sets the preferred column count to 1 for the MI text field (line 22). The program declares an explicit reference `tfMi` for a `TextField` object for MI. The explicit reference is necessary, because we need to reference the object directly to set its `prefColumnCount` property.

The program adds the pane to the scene (line 27), sets the scene in the stage (line 29), and displays the stage (line 30). Note that if you resize the window, the nodes are automatically rearranged to fit in the pane. In Figure 14.16a, the first row has three nodes, but in Figure 14.16b, the first row has four nodes, because the width has been increased.

Suppose you wish to add the object `tfMi` to a pane ten times; will ten text fields appear in the pane? No, a node such as a text field can be added to only one pane and once. Adding a node to a pane multiple times or to different panes will cause a runtime error.

**Note**
A node can be placed only in one pane. Therefore, the relationship between a pane and a node is the composition denoted by a filled diamond, as shown in Figure 14.3b.
14.10.2 GridPane

A GridPane arranges nodes in a grid (matrix) formation. The nodes are placed in the specified column and row indices. The class diagram for GridPane is shown in Figure 14.18.

**Figure 14.18** GridPane lays out nodes in the specified cell in a grid.

Listing 14.11 gives a program that demonstrates GridPane. The program is similar to the one in Listing 14.10, except that it adds three labels and three text fields, and a button to the specified location in a grid, as shown in Figure 14.19.

**Figure 14.19** The GridPane places the nodes in a grid with a specified column and row indices.

**Listing 14.11** ShowGridPane.java

```java
import javafx.application.Application;
import javafx.geometry.HPos;
import javafx.geometry.Insets;
```
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.scene.control.Label;
import javafx.scene.control.TextField;
import javafx.scene.layout.GridPane;
import javafx.stage.Stage;

public class ShowGridPane extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        GridPane pane = new GridPane();
        pane.setAlignment(Pos.CENTER);
        pane.setPadding(new Insets(11.5, 12.5, 13.5, 14.5));
        pane.setHgap(5.5);
        pane.setVgap(5.5);

        pane.add(new Label("First Name:"), 0, 0);
        pane.add(new TextField(), 1, 0);
        pane.add(new Label("MI:"), 0, 1);
        pane.add(new TextField(), 1, 1);
        pane.add(new Label("Last Name:"), 0, 2);
        pane.add(new TextField(), 1, 2);
        Button btAdd = new Button("Add Name");
        pane.add(btAdd, 1, 3);
        pane.setHalignment(btAdd, HPos.RIGHT);

        Scene scene = new Scene(pane);
        primaryStage.setTitle("ShowGridPane"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }
}

The program creates a GridPane (line 16) and sets its properties (line 17–20). The alignment is set to the center position (line 17), which causes the nodes to be placed in the center of the grid pane. If you resize the window, you will see the nodes remain in the center of the grid pane.

The program adds the label in column 0 and row 0 (line 23). The column and row index starts from 0. The add method places a node in the specified column and row. Not every cell in the grid needs to be filled. A button is placed in column 1 and row 3 (line 30), but there are no nodes placed in column 0 and row 3. To remove a node from a GridPane, use pane.getChildren().remove(node). To remove all nodes, use pane.getChildren().removeAll().

The program invokes the static setHalignment method to align the button right in the cell (line 31).

Note that the scene size is not set (line 34). In this case, the scene size is automatically computed according to the sizes of the nodes placed inside the scene.

14.10.3 BorderPane
A BorderPane can place nodes in five regions: top, bottom, left, right, and center, using the setTop(node), setBottom(node), setLeft(node), setRight(node), and setCenter(node) methods. The class diagram for GridPane is shown in Figure 14.20.
The getter and setter methods for property values and a getter for property itself are provided in the class, but omitted in the UML diagram for brevity.

**FIGURE 14.20** BorderPane places the nodes in top, bottom, left, right, and center regions.

Listing 14.12 gives a program that demonstrates BorderPane. The program places five buttons in the five regions of the pane, as shown in Figure 14.21.

**LISTING 14.12** ShowBorderPane.java

```java
import javafx.application.Application;
import javafx.geometry.Insets;
import javafx.scene.Scene;
import javafx.scene.control.Label;
import javafx.scene.layout.BorderPane;
import javafx.scene.layout.StackPane;
import javafx.stage.Stage;

public class ShowBorderPane extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a border pane
        BorderPane pane = new BorderPane();

        // Place nodes in the pane
        pane.setTop(new CustomPane("Top")); // add to top
        pane.setRight(new CustomPane("Right")); // add to right
        pane.setBottom(new CustomPane("Bottom")); // add to bottom
        pane.setLeft(new CustomPane("Left")); // add to left
        pane.setCenter(new CustomPane("Center")); // add to center

        // Create a scene and place it in the stage
        Scene scene = new Scene(pane); // create a scene
        primaryStage.setTitle("ShowBorderPane"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }

    // Define a custom pane to hold a label in the center of the pane
    class CustomPane extends StackPane {
        public CustomPane(String title) {
            getChildren().add(new Label(title));
            setStyle("-fx-border-color: red");
            setPadding(new Insets(11.5, 12.5, 13.5, 14.5));
        }
    }
}
```

create a border pane
add to top
add to right
add to bottom
add to left
add to center
define a custom pane
add a label to pane
set style
set padding
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The program defines **CustomPane** that extends **StackPane** (line 31). The constructor of **CustomPane** adds a label with the specified title (line 33), sets a style for the border color, and sets a padding using insets (line 35).

The program creates a **BorderPane** (line 13) and places five instances of **CustomPane** into five regions of the border pane (lines 16–20). Note that a pane is a node. So a pane can be added into another pane. To remove a node from the top region, invoke `setTop(null)`. If a region is not occupied, no space will be allocated for this region.

### 14.10.4 HBox and VBox

An **HBox** lays out its children in a single horizontal row. A **VBox** lays out its children in a single vertical column. Recall that a **FlowPane** can lay out its children in multiple rows or multiple columns, but an **HBox** or a **VBox** can lay out children only in one row or one column. The class diagrams for **HBox** and **VBox** are shown in Figures 14.22 and 14.23.

![Figure 14.21](image.png)

**Figure 14.21** The **BorderPane** places the nodes in five regions of the pane.

![Figure 14.22](image.png)

**Figure 14.22** **HBox** places the nodes in one row.

![Figure 14.23](image.png)

**Figure 14.23** **VBox** places the nodes in one column.
Listing 14.12 gives a program that demonstrates **HBox** and **VBox**. The program places two buttons in an **HBox** and five labels in a **VBox**, as shown in Figure 14.24.

**LISTING 14.13**  ShowHBoxVBox.java

```java
1 import javafx.application.Application;
2 import javafx.geometry.Insets;
3 import javafx.scene.Scene;
4 import javafx.scene.control.Button;
5 import javafx.scene.control.Label;
6 import javafx.scene.layout.BorderPane;
7 import javafx.scene.layout.HBox;
8 import javafx.scene.layout.VBox;
9 import javafx.stage.Stage;
10 import javafx.scene.image.Image;
11 import javafx.scene.image.ImageView;
12
13 public class ShowHBoxVBox extends Application {
14    @Override // Override the start method in the Application class
15    public void start(Stage primaryStage) {
16        // Create a border pane
17        BorderPane pane = new BorderPane();
18
19        // Place nodes in the pane
20        pane.setTop(getHBox());
21        pane.setLeft(getVBox());
22
23        // Create a scene and place it in the stage
24        Scene scene = new Scene(pane); // Create a scene
25        primaryStage.setTitle("ShowHBoxVBox"); // Set the stage title
26        primaryStage.setScene(scene); // Place the scene in the stage
27        primaryStage.show(); // Display the stage
28    }
29
30    private HBox getHBox() {
31        HBox hBox = new HBox();
32        hBox.setPadding(new Insets(15, 15, 15, 15));
33        hBox.setStyle("-fx-background-color: gold");
34        hBox.getChildren().add(new Button("Computer Science"));
35        hBox.getChildren().add(new Button("Chemistry"));
36        Image imageView = new Image("image/us.gif");
37        hBox.getChildren().add(imageView);
38        return hBox;
39    }
40
41    private VBox getVBox() {
42        VBox vBox = new VBox();
43        vBox.setPadding(new Insets(15, 5, 5, 5));
44        Label[] courses = {new Label("CSCI 1301"), new Label("CSCI 1302"),
45                             new Label("CSCI 2410"), new Label("CSCI 3720")};
46        for (Label course: courses) {
47            VBox.setMargin(course, new Insets(0, 0, 0, 15));
48            vBox.getChildren().add(course);
49        }
50        return vBox;
51    }
52
53    } // end class ShowHBoxVBox
```
The program defines the `getHBox()` method. This method returns an `HBox` that contains two buttons and an image view (lines 30–39). The background color of the `HBox` is set to gold using Java CSS (line 33). The program defines the `getVBox()` method. This method returns a `VBox` that contains five labels (lines 41–55). The first label is added to the `VBox` in line 44 and the other four are added in line 51. The `setMargin` method is used to set a node’s margin when placed inside the `VBox` (line 50).

### 14.22 How do you add a node to a `Pane`, `StackPane`, `FlowPane`, `GridPane`, `BorderPane`, `HBox`, and `VBox`? How do you remove a node from these panes?

### 14.23 How do you set the alignment to right for nodes in a `FlowPane`, `GridPane`, `HBox`, and `VBox`?

### 14.24 How do you set the horizontal gap and vertical gap between nodes in 8 pixels in a `FlowPane` and `GridPane` and set spacing in 8 pixels in an `HBox` and `VBox`?

### 14.25 How do you get the column and row index of a node in a `GridPane`? How do you reposition a node in a `GridPane`?

### 14.26 What are the differences between a `FlowPane` and an `HBox` or a `VBox`?

## 14.11 Shapes

*JavaFX provides many shape classes for drawing texts, lines, circles, rectangles, ellipses, arcs, polygons, and polylines.*

The `Shape` class is the abstract base class that defines the common properties for all shapes. Among them are the `fill`, `stroke`, and `strokeWidth` properties. The `fill` property specifies a color that fills the interior of a shape. The `stroke` property specifies a color that is used to draw the outline of a shape. The `strokeWidth` property specifies the width of the outline of a shape. This section introduces the classes `Text`, `Line`, `Rectangle`, `Circle`, `Ellipse`, `Arc`, `Polygon`, and `Polyline` for drawing texts and simple shapes. All these are subclasses of `Shape`, as shown in Figure 14.25.

### 14.11.1 Text

The `Text` class defines a node that displays a string at a starting point \((x, y)\), as shown in Figure 14.27a. A `Text` object is usually placed in a pane. The pane’s upper-left corner point is \((0, 0)\) and the bottom-right point is \((\text{pane.getWidth()}, \text{pane.getHeight()})\). A string may be displayed in multiple lines separated by \(\backslash n\). The UML diagram for the `Text` class is shown in Figure 14.26. Listing 14.13 gives an example that demonstrates text, as shown in Figure 14.27b.
14.11 Shapes

**FIGURE 14.25** A shape is a node. The **Shape** class is the root of all shape classes.

**FIGURE 14.26** **Text** defines a node for displaying a text.

**FIGURE 14.27** A **Text** object is created to display a text.

**LISTING 14.14** **ShowText.java**

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.geometry.Insets;
```

```java
import javafx.scene.text.Text;
```

`javafx.scene.text.Text`

- **text**: StringProperty
- **x**: DoubleProperty
- **y**: DoubleProperty
- **underline**: BooleanProperty
- **strikethrough**: BooleanProperty
- **font**: ObjectProperty<Font>

**+Text()**

**+Text(text: String)**

**+Text(x: double, y: double, text: String)**

The getter and setter methods for property values and a getter for property itself are provided in the class, but omitted in the UML diagram for brevity.

**FIGURE 14.28** The **Text** object is created to display a text.

(a) **Text(x, y, text)**

(b) **Three Text objects are displayed**
import javafx.stage.Stage;
import javafx.scene.text.Text;
import javafx.scene.text.Font;
import javafx.scene.text.FontWeight;
import javafx.scene.text.FontPosture;

public class ShowText extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a pane to hold the texts
        Pane pane = new Pane();
        pane.setPadding(new Insets(5, 5, 5, 5));

        Text text1 = new Text(20, 20, "Programming is fun");
        text1.setFont(Font.font("Courier", FontWeight.BOLD, FontPosture.ITALIC, 15));
        pane.getChildren().add(text1);

        Text text2 = new Text(60, 60, "Programming is fun\nDisplay text");
        pane.getChildren().add(text2);

        Text text3 = new Text(10, 100, "Programming is fun\nDisplay text");
        text3.setFill(Color.RED);
        text3.setUnderline(true);
        text3.setStrikethrough(true);
        pane.getChildren().add(text3);

        // Create a scene and place it in the stage
        Scene scene = new Scene(pane);
        primaryStage.setTitle("ShowText"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }
}

The program creates a Text (line 18), sets its font (line 19), and places it to the pane (line 21). The program creates another Text with multiple lines (line 23) and places it to the pane (line 24). The program creates the third Text (line 26), sets its color (line 27), sets an underline and a strike through line (lines 28–29), and places it to the pane (line 30).

14.11.2 Line
A line connects two points with four parameters startx, starty, endx, and endy, as shown in Figure 14.29a. The Line class defines a line. The UML diagram for the Line class is shown in Figure 14.28. Listing 14.15 gives an example that demonstrates text, as shown in Figure 14.29b.

Listing 14.15 ShowLine.java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.stage.Stage;
import javafx.scene.shape.Line;

public class ShowLine extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a scene and place it in the stage
        Scene scene = new Scene(pane);
        primaryStage.setTitle("ShowText"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }
}
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```java
12 Scene scene = new Scene(new LinePane(), 200, 200);  // create a pane in scene
13 primaryStage.setTitle("ShowLine"); // Set the stage title
14 primaryStage.setScene(scene); // Place the scene in the stage
15 primaryStage.show(); // Display the stage
16 }
17 }
18
19 class LinePane extends Pane {
20     public LinePane() {
21         Line line1 = new Line(10, 10, 10, 10);  // create a line
22         line1.endXProperty().bind(widthProperty().subtract(10));
23         line1.endYProperty().bind(heightProperty().subtract(10));
24         line1.setStrokeWidth(5);
25         line1.setStroke(Color.GREEN);
26         getChildren().add(line1);
27
28         Line line2 = new Line(10, 10, 10, 10);  // create a line
29         line2.startXProperty().bind(widthProperty().subtract(10));
30         line2.endYProperty().bind(heightProperty().subtract(10));
31         line2.setStrokeWidth(5);
32         line2.set Stroke(Color.GREEN);
33         getChildren().add(line2);
34     }
35 }
```

The program defines a custom pane class named `LinePane` (line 19). The custom pane class creates two lines and binds the starting and ending points of the line with the width and height of the pane (lines 22–23, 29–30) so that the two points of the lines are changed as the pane is resized.
14.11.3 Rectangle

A rectangle is defined by the parameters \(x, y, \text{width}, \text{height}, \text{arcWidth}, \) and \(\text{arcHeight},\) as shown in Figure 14.31a. The rectangle’s upper-left corner point is at \((x, y)\) and parameter \(aw\) (\(\text{arcWidth}\)) is the horizontal diameter of the arcs at the corner, and \(ah\) (\(\text{arcHeight}\)) is the vertical diameter of the arcs at the corner.

The Rectangle class defines a rectangle. The UML diagram for the Rectangle class is shown in Figure 14.30. Listing 14.15 gives an example that demonstrates rectangles, as shown in Figure 14.31b.

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.stage.Stage;
import javafx.scene.text.Text;
import javafx.scene.shape.Rectangle;

public class ShowRectangle extends Application {
    @Override
    public void start(Stage primaryStage) {
        // Create a pane
```
**14.11 Shapes**

```java
import javafx.scene.Scene;
import javafx.scene.shape.Pane;
import javafx.scene.shape.Rectangle;
import javafx.scene.shape.Text;
import javafx.stage.Stage;

Pane pane = new Pane();

// Create rectangles and add to pane
Rectangle r1 = new Rectangle(25, 10, 60, 30);
r1.setStroke(Color.BLACK);
r1.setFill(Color.WHITE);
pane.getChildren().add(new Text(10, 27, "r1"));
pane.getChildren().add(r1);

Rectangle r2 = new Rectangle(25, 50, 60, 30);
pane.getChildren().add(new Text(10, 67, "r2"));
pane.getChildren().add(r2);

Rectangle r3 = new Rectangle(25, 90, 60, 30);
r3.setArcWidth(15);
r3.setArcHeight(25);
pane.getChildren().add(new Text(10, 107, "r3"));
pane.getChildren().add(r3);

for (int i = 0; i < 4; i++) {
    Rectangle r = new Rectangle(100, 50, 100, 30);
r.setRotate(i * 360 / 8);
r.setStroke(Color.color(Math.random(), Math.random(),
               Math.random()));
r.setFill(Color.WHITE);
pane.getChildren().add(r);
}

// Create a scene and place it in the stage
Scene scene = new Scene(pane, 250, 150);
primaryStage.setTitle("ShowRectangle");
primaryStage.setScene(scene);
primaryStage.show();
```

The program creates multiple rectangles. By default, the fill color is black. So a rectangle is filled with black color. The stroke color is white by default. Line 17 sets stroke color of rectangle `r1` to black. The program creates rectangle `r3` (line 26) and sets its arc width and arc height (lines 27–28). So `r3` is displayed as a rounded rectangle.

The program repeatedly creates a rectangle (line 33), rotates it (line 34), sets a random stroke color (lines 35–36), its fill color to white (line 37), and adds the rectangle to the pane (line 38).

If line 37 is replaced by the following line

```java
r.setFill(null);
```

the rectangle is not filled with a color. So they are displayed as shown in Figure 14.31c.

### 14.11.4 Circle and Ellipse

You have used circles in several examples early in this chapter. A circle is defined by its parameters `centerX`, `centerY`, and `radius`. The Circle class defines a circle. The UML diagram for the Circle class is shown in Figure 14.32.

An ellipse is defined by its parameters `centerX`, `centerY`, `radiusX`, and `radiusY`, as shown in Figure 14.34a. The Ellipse class defines an ellipse. The UML diagram for the Ellipse class is shown in Figure 14.33. Listing 14.17 gives an example that demonstrates ellipses, as shown in Figure 14.34b.
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Listing 14.17  ShowEllipse.java

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.stage.Stage;
import javafx.scene.shape.Ellipse;

public class ShowEllipse extends Application {
    @Override
    public void start(Stage primaryStage) {
        // Code to show an ellipse
    }
}
```

The `Circle` class defines circles.

- centerX: DoubleProperty  
- centerY: DoubleProperty  
- radius: DoubleProperty

+Circle()  
+Circle(x: double, y: double)  
+Circle(x: double, y: double, radius: double)

The getter and setter methods for property values and a getter for property itself are provided in the class, but omitted in the UML diagram for brevity.

The x-coordinate of the center of the circle (default 0).  
The y-coordinate of the center of the circle (default 0).  
The radius of the circle (default: 0).

Creates an empty Circle.  
Creates a Circle with the specified center.  
Creates a Circle with the specified center and radius.

The `Ellipse` class defines ellipses.

- centerX: DoubleProperty  
- centerY: DoubleProperty  
- radiusX: DoubleProperty  
- radiusY: DoubleProperty

+Ellipse()  
+Ellipse(x: double, y: double)  
+Ellipse(x: double, y: double, radiusX: double, radiusY: double)

The getter and setter methods for property values and a getter for property itself are provided in the class, but omitted in the UML diagram for brevity.

The x-coordinate of the center of the ellipse (default 0).  
The y-coordinate of the center of the ellipse (default 0).  
The horizontal radius of the ellipse (default: 0).  
The vertical radius of the ellipse (default: 0).

Creates an empty Ellipse.  
Creates an Ellipse with the specified center.  
Creates an Ellipse with the specified center and radiuses.

An Ellipse object is created to display an ellipse.

(a) Ellipse(centerX, centerY, radiusX, radiusY)  
(b) Multiple ellipses are displayed.

Figure 14.34  An Ellipse object is created to display an ellipse.

Figure 14.32  The Circle class defines circles.

Figure 14.33  The Ellipse class defines ellipses.
public void start(Stage primaryStage) {
    // Create a pane
    Pane pane = new Pane();

    for (int i = 0; i < 16; i++) {
        // Create an ellipse and add it to pane
        Ellipse e1 = new Ellipse(150, 100, 100, 50);
        e1.setStroke(Color.color(Math.random(), Math.random(), Math.random()));
        e1.setFill(Color.WHITE);
        e1.setRotate(i * 180 / 16);
        pane.getChildren().add(e1);
    }

    // Create a scene and place it in the stage
    Scene scene = new Scene(pane, 300, 200);
    primaryStage.setTitle("ShowEllipse"); // Set the stage title
    primaryStage.setScene(scene); // Place the scene in the stage
    primaryStage.show(); // Display the stage
}

The program repeatedly creates an ellipse (line 16), sets a random stroke color (lines 17–18), sets its fill color to white (line 19), rotates it (line 20), and adds the rectangle to the pane (line 21).

14.11.5 Arc

An arc is conceived as part of an ellipse, defined by the parameters centerX, centerY, radiusX, radiusY, startAngle, length, and an arc type (ArcType.OPEN, ArcType.CHORD, or ArcType.ROUND). The parameter startAngle is the starting angle; and length is the spanning angle (i.e., the angle covered by the arc). Angles are measured in degrees and follow the usual mathematical conventions (i.e., 0 degrees is in the easterly direction, and positive angles indicate counterclockwise rotation from the easterly direction), as shown in Figure 14.36a.

The Arc class defines an arc. The UML diagram for the Arc class is shown in Figure 14.35. Listing 14.18 gives an example that demonstrates ellipses, as shown in Figure 14.36b.

```
javafx.scene.shape.Arc

- centerX: DoubleProperty
- centerY: DoubleProperty
- radiusX: DoubleProperty
- radiusY: DoubleProperty
- startAngle: DoubleProperty
- length: DoubleProperty
- type: ObjectProperty<ArcType>

+Arc()
+Arc(x: double, y: double, radiusX: double, radiusY: double, startAngle: double, length: double)

The getter and setter methods for property values and a getter for property itself are provided in the class, but omitted in the UML diagram for brevity.

The x-coordinate of the center of the ellipse (default 0).
The y-coordinate of the center of the ellipse (default 0).
The horizontal radius of the ellipse (default 0).
The vertical radius of the ellipse (default: 0).
The start angle of the arc in degrees.
The angular extent of the arc in degrees.
The closure type of the arc (ArcType.OPEN, ArcType.CHORD, ArcType.ROUND).

Creates an empty Arc.
Creates an Arc with the specified arguments.
```

FIGURE 14.35 The Arc class defines an arc.
Figure 14.36 An Arc object is created to display an arc.

Listing 14.18 ShowArc.java

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.stage.Stage;
import javafx.scene.shape.Arc;
import javafx.scene.shape.ArcType;
import javafx.scene.text.Text;

public class ShowArc extends Application {
    @Override
    public void start(Stage primaryStage) {
        Pane pane = new Pane();

        Arc arc1 = new Arc(150, 100, 80, 80, 30, 35); // Create an arc
        arc1.setFill(Color.RED); // Set fill color
        arc1.setType(ArcType.ROUND); // Set arc type
        pane.getChildren().add(new Text(210, 40, "arc1: round"));
        pane.getChildren().add(arc1); // Add arc to pane

        Arc arc2 = new Arc(150, 100, 80, 80, 30 + 90, 35);
        arc2.setFill(Color.WHITE);
        arc2.setType(ArcType.OPEN);
        arc2.setStroke(Color.BLACK);
        pane.getChildren().add(new Text(20, 40, "arc2: open"));
        pane.getChildren().add(arc2);

        Arc arc3 = new Arc(150, 100, 80, 80, 30 + 180, 35);
        arc3.setFill(Color.WHITE);
        arc3.setType(ArcType.CHORD);
        arc3.setStroke(Color.BLACK);
        pane.getChildren().add(new Text(20, 170, "arc3: chord"));
        pane.getChildren().add(arc3);

        Arc arc4 = new Arc(150, 100, 80, 80, 30 + 270, 35);
        arc4.setFill(Color.GREEN);
        arc4.setType(ArcType.CHORD);
    }
}
```
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```java
39      arc4.setStroke(Color.BLACK);
40      pane.getChildren().add(new Text(210, 170, "arc4: chord"));
41      pane.getChildren().add(arc4);
42
43      // Create a scene and place it in the stage
44      Scene scene = new Scene(pane, 300, 200);
45      primaryStage.setTitle("ShowArc"); // Set the stage title
46      primaryStage.setScene(scene); // Place the scene in the stage
47      primaryStage.show(); // Display the stage
48    }
49  }
```

The program creates an arc `arc1` centered at (150, 100) with `radiusX 80` and `radiusY 80`. The starting angle is 30 with `length 35` (line 15). Arc1’s arc type is set to `ArcType.ROUND` (line 18). Since `arc1`’s fill color is red, `arc1` is displayed filled with red round.

The program creates an arc `arc3` centered at (150, 100) with `radiusX 80` and `radiusY 80`. The starting angle is `30+180` with `length 35` (line 29). Arc3’s arc type is set to `ArcType.CHORD` (line 31). Since `arc3`’s fill color is white and stroke color is black, `arc3` is displayed with black outline as a chord.

Angles may be negative. A negative starting angle sweeps clockwise from the easterly direction, as shown in Figure 14.37. A negative spanning angle sweeps clockwise from the starting angle. The following two statements define the same arc:

```java
new Arc(x, y, radiusX, radiusY, -30, -20);
new Arc(x, y, radiusX, radiusY, -50, 20);
```

The first statement uses negative starting angle -30 and negative spanning angle -20, as shown in Figure 14.37a. The second statement uses negative starting angle -50 and positive spanning angle 20, as shown in Figure 14.37b.

![Figure 14.37](image)  
(a) Negative starting angle –30° and negative spanning angle –20°
(b) Negative starting angle –50° and positive spanning angle 20°

**Note that** the trigonometric methods in the `Math` class use the angles in radians, but the angles in the `Arc` class are in degrees.

### 14.11.6 Polygon and Polyline

The **Polygon** class defines a polygon that connects a sequence of points, as shown in Figure 14.38a. The **Polyline** class is similar to the **Polygon** class except that the **Polyline** class is not automatically closed, as shown in Figure 14.38b.
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The UML diagram for the Polygon class is shown in Figure 14.39. Listing 14.19 gives an example that creates a hexagon, as shown in Figure 14.40.

**Figure 14.38** Polygon is closed and Polyline is not closed.

The getter and setter methods for property values and a getter for property itself are provided in the class, but omitted in the UML diagram for brevity.

**Figure 14.39** Polygon defines a polygon.

**Figure 14.40** (a) A Polygon is displayed. (b) A Polyline is displayed.

**Listing 14.19** ShowPolygon.java

```java
import javafx.application.Application;
import javafx.collections.ObservableList;
import javafx.scene.Scene;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.stage.Stage;
import javafx.scene.shape.Polygon;
```
public class ShowPolygon extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a pane, a polygon, and place polygon to pane
        Pane pane = new Pane();
        Polygon polygon = new Polygon();
        pane.getChildren().add(polygon);
        polygon.setFill(Color.WHITE);
        polygon.setStroke(Color.BLACK);
        ObservableList<Double> list = polygon.getPoints();

        final double WIDTH = 200, HEIGHT = 200;
        double centerX = WIDTH / 2, centerY = HEIGHT / 2;
        double radius = Math.min(WIDTH, HEIGHT) * 0.4;

        // Add points to the polygon list
        for (int i = 0; i < 6; i++) {
            list.add(centerX + radius * Math.cos(2 * i * Math.PI / 6));
            list.add(centerY - radius * Math.sin(2 * i * Math.PI / 6));
        }

        // Create a scene and place it in the stage
        Scene scene = new Scene(pane, WIDTH, HEIGHT);
        primaryStage.setTitle("ShowPolygon"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }
}

The program creates a polygon (line 14) and adds it to a pane (line 15). The `polygon.getPoints()` method returns an `ObservableList<Double>` (line 18), which contains the `add` method for adding an element to the list (lines 26–27). Note that the value passed to `add(value)` must be a `double` value. If an `int` value is passed, the `int` value would be automatically boxed into an `Integer`. This would cause an error because the `ObservableList<Double>` consists of `Double` elements.

The loop adds six points to the polygon (lines 25–28). Each point is represented by its x- and y-coordinates. For each point, its x-coordinate is added to the polygon’s list (line 26) and then its y-coordinate is added to the list (line 27). The formula for computing the x- and y-coordinates for a point in the hexagon is illustrated in Figure 14.40a.

If you replace `Polygon` by `Polyline`, the program displays a polyline as shown in Figure 14.40b. The `Polyline` class is used in the same way as `Polygon` except that the starting and ending point are not connected in `Polyline`.

14.28 Write code fragments to display a string rotated 45 degrees in the center of the pane.
14.30 Write code fragments to fill red color in a rectangle of width 100 and height 50 with the upper-left corner at (10, 10).
14.31 Write code fragments to display a round-cornered rectangle with width 200, height 100 with the upper-left corner at (10, 10), corner horizontal diameter 40, and corner vertical diameter 20.
14.32 Write code fragments to display an ellipse with horizontal radius 50 and vertical radius 100.
14.33 Write code fragments to display the outline of the upper half of a circle with radius 50.
14.34 Write code fragments to display the lower half of a circle with radius 50 filled with the red color.

14.35 Write code fragments to display a polygon connecting the following points: (20, 40), (30, 50), (40, 90), (90, 10), (10, 30), and fill the polygon with green color.

14.36 Write code fragments to display a polyline connecting the following points: (20, 40), (30, 50), (40, 90), (90, 10), (10, 30).

14.12 Case Study: The ClockPane Class

This case study develops a class that displays a clock on a pane.

The contract of the ClockPane class is shown in Figure 14.41.

Assume ClockPane is available; we write a test program in Listing 14.20 to display an analog clock and use a label to display the hour, minute, and second, as shown in Figure 14.42.
**Listing 14.20**  DisplayClock.java

```java
import javafx.application.Application;
import javafx.geometry.Pos;
import javafx.stage.Stage;
import javafx.scene.Scene;
import javafx.scene.control.Label;
import javafx.scene.layout.BorderPane;

public class DisplayClock extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a clock and a label
        ClockPane clock = new ClockPane();
        String timeString = clock.getHour() + ":
        String timeString = clock.getMinute() + ":
        String timeString = clock.getSecond();
        Label lblCurrentTime = new Label(timeString);

        // Place clock and label in border pane
        BorderPane pane = new BorderPane();
        pane.setCenter(clock);
        pane.setBottom(lblCurrentTime);
        BorderPane.setAlignment(lblCurrentTime, Pos.TOP_CENTER);

        // Create a scene and place it in the stage
        Scene scene = new Scene(pane, 250, 250);
        primaryStage.setTitle("DisplayClock"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }
}
```

The rest of this section explains how to implement the `ClockPane` class. Since you can use the class without knowing how it is implemented, you may skip the implementation if you wish.

To draw a clock, you need to draw a circle and three hands for the second, minute, and hour. To draw a hand, you need to specify the two ends of the line. As shown in Figure 14.42b, one end is the center of the clock at \((centerX, centerY)\); the other end, at \((endX, endY)\), is determined by the following formula:

\[
\begin{align*}
endX &= centerX + \text{handLength} \times \sin(\theta) \\
endY &= centerY - \text{handLength} \times \cos(\theta)
\end{align*}
\]

Since there are 60 seconds in one minute, the angle for the second hand is

\[\text{second} \times \left(\frac{2\pi}{60}\right)\]

The position of the minute hand is determined by the minute and second. The exact minute value combined with seconds is \(\text{minute} + \text{second}/60\). For example, if the time is 3 minutes and 30 seconds, the total minutes are 3.5. Since there are 60 minutes in one hour, the angle for the minute hand is

\[(\text{minute} + \text{second}/60) \times \left(\frac{2\pi}{60}\right)\]

Since one circle is divided into 12 hours, the angle for the hour hand is

\[(\text{hour} + \text{minute}/60 + \text{second}/(60 \times 60)) \times \left(\frac{2\pi}{12}\right)\]
For simplicity in computing the angles of the minute hand and hour hand, you can omit the seconds, because they are negligibly small. Therefore, the endpoints for the second hand, minute hand, and hour hand can be computed as:

\[
\begin{align*}
\text{secondX} &= \text{centerX} + \text{secondHandLength} \times \sin(\text{second} \times (2\pi/60)) \\
\text{secondY} &= \text{centerY} - \text{secondHandLength} \times \cos(\text{second} \times (2\pi/60)) \\
\text{minuteX} &= \text{centerX} + \text{minuteHandLength} \times \sin(\text{minute} \times (2\pi/60)) \\
\text{minuteY} &= \text{centerY} - \text{minuteHandLength} \times \cos(\text{minute} \times (2\pi/60)) \\
\text{hourX} &= \text{centerX} + \text{hourHandLength} \times \sin((\text{hour} + \text{minute}/60) \times (2\pi/12)) \\
\text{hourY} &= \text{centerY} - \text{hourHandLength} \times \cos((\text{hour} + \text{minute}/60) \times (2\pi/12))
\end{align*}
\]

The `ClockPane` class is implemented in Listing 14.21.

**Listing 14.21 ClockPane.java**

```java
import java.util.Calendar;
import java.util.GregorianCalendar;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Circle;
import javafx.scene.shape.Line;
import javafx.scene.text.Text;

public class ClockPane extends Pane {
    private int hour;
    private int minute;
    private int second;

    // Clock pane's width and height
    private double w = 250, h = 250;

    /** Construct a default clock with the current time*/
    public ClockPane() {
        setCurrentTime();
    }

    /** Construct a clock with specified hour, minute, and second */
    public ClockPane(int hour, int minute, int second) {
        this.hour = hour;
        this.minute = minute;
        this.second = second;
        paintClock();
    }

    /** Return hour */
    public int getHour() {
        return hour;
    }

    /** Set a new hour */
    public void setHour(int hour) {
        this.hour = hour;
        paintClock();
    }

    /** Return minute */
    public int getMinute() {
        return minute;
    }

    /** Paint the clock */
    private void paintClock() {
        // Clock properties
        double radius = Math.min(w/2, h/2);

        // Second hand
        Circle secondHand = new Circle(radius);
        secondHand.setFill(Color.RED);
        double angle = Math.toDegrees(hour * 30 + minute/60) + Math.toDegrees(second/60) - 90;
        double secondX = centerX + secondHandLength * Math.sin(angle); 
        double secondY = centerY - secondHandLength * Math.cos(angle);
        circleX = secondX;
        circleY = secondY;

        // Minute hand
        Circle minuteHand = new Circle(radius/2);
        minuteHand.setFill(Color.BLACK);
        double minuteAngle = Math.toDegrees(hour * 30 + minute/60);
        double minuteX = centerX + minuteHandLength * Math.sin(minuteAngle);
        double minuteY = centerY - minuteHandLength * Math.cos(minuteAngle);
        circleX = minuteX;
        circleY = minuteY;

        // Hour hand
        Circle hourHand = new Circle(radius/4);
        hourHand.setFill(Color.BLUE);
        double hourAngle = Math.toDegrees(hour * 30 + minute/60);
        double hourX = centerX + hourHandLength * Math.sin(hourAngle);
        double hourY = centerY - hourHandLength * Math.cos(hourAngle);
        circleX = hourX;
        circleY = hourY;

        // Paint the clock face
        PaintClockFace();
    }

    /** Paint the clock face */
    private void PaintClockFace() {
        // Clock properties
        double radius = Math.min(w/2, h/2);

        // Outer circle
        Circle clockFace = new Circle(w/2);
        clockFace.setFill(Color.WHITE);
        clockFace.setStroke(Color.BLACK);
        double angle = Math.toDegrees(hour * 30 + minute/60) + Math.toDegrees(second/60) - 90;
        double x = centerX + radius * Math.cos(angle);
        double y = centerY - radius * Math.sin(angle);
        Circle clockCircle = new Circle(radius);
        clockCircle.setFill(Color.WHITE);
        clockCircle.setStroke(Color.BLACK);
        double hourAngle = Math.toDegrees(hour * 30 + minute/60);
        double minuteAngle = Math.toDegrees(hour * 30 + minute/60);
        double secondAngle = Math.toDegrees(hour * 30 + minute/60 + second/60);
        double hourX = centerX + hourHandLength * Math.sin(hourAngle);
        double hourY = centerY - hourHandLength * Math.cos(hourAngle);
        double minuteX = centerX + minuteHandLength * Math.sin(minuteAngle);
        double minuteY = centerY - minuteHandLength * Math.cos(minuteAngle);
        double secondX = centerX + secondHandLength * Math.sin(secondAngle);
        double secondY = centerY - secondHandLength * Math.cos(secondAngle);
        lineX = hourX;
        lineY = hourY;
        lineX2 = minuteX;
        lineY2 = minuteY;
        lineX3 = secondX;
        lineY3 = secondY;

        // Paint the hour markers
        for (int i = 0; i < 12; i++) {
            double angle = Math.toDegrees(i * 30);
            double x = centerX + radius * Math.cos(angle);
            double y = centerY - radius * Math.sin(angle);
            Circle hourMarker = new Circle(radius/10);
            hourMarker.setFill(Color.GRAY);
            hourMarker.setStroke(Color.GRAY);
            hourMarker.setCenterX(x);
            hourMarker.setCenterY(y);
            hourMarkers.add(hourMarker);
        }

        // Paint the minute markers
        for (int i = 0; i < 60; i++) {
            double angle = Math.toDegrees(i / 5);
            double x = centerX + radius * Math.cos(angle);
            double y = centerY - radius * Math.sin(angle);
            Circle minuteMarker = new Circle(radius/20);
            minuteMarker.setFill(Color.GRAY);
            minuteMarker.setStroke(Color.GRAY);
            minuteMarker.setCenterX(x);
            minuteMarker.setCenterY(y);
            minuteMarkers.add(minuteMarker);
        }

        // Paint the second markers
        for (int i = 0; i < 60; i++) {
            double angle = Math.toDegrees(i / 10);
            double x = centerX + radius * Math.cos(angle);
            double y = centerY - radius * Math.sin(angle);
            Circle secondMarker = new Circle(radius/30);
            secondMarker.setFill(Color.GRAY);
            secondMarker.setStroke(Color.GRAY);
            secondMarker.setCenterX(x);
            secondMarker.setCenterY(y);
            secondMarkers.add(secondMarker);
        }
    }

    /** Paint the clock marker */
    private void PaintClockMarker() {
        // Clock properties
        double radius = Math.min(w/2, h/2);

        // Outer circle
        Circle clockFace = new Circle(w/2);
        clockFace.setFill(Color.WHITE);
        clockFace.setStroke(Color.BLACK);
        double angle = Math.toDegrees(hour * 30 + minute/60) + Math.toDegrees(second/60) - 90;
        double x = centerX + radius * Math.cos(angle);
        double y = centerY - radius * Math.sin(angle);
        Circle clockCircle = new Circle(radius);
        clockCircle.setFill(Color.WHITE);
        clockCircle.setStroke(Color.BLACK);
        double hourAngle = Math.toDegrees(hour * 30 + minute/60);
        double minuteAngle = Math.toDegrees(hour * 30 + minute/60);
        double secondAngle = Math.toDegrees(hour * 30 + minute/60 + second/60);
        double hourX = centerX + hourHandLength * Math.sin(hourAngle);
        double hourY = centerY - hourHandLength * Math.cos(hourAngle);
        double minuteX = centerX + minuteHandLength * Math.sin(minuteAngle);
        double minuteY = centerY - minuteHandLength * Math.cos(minuteAngle);
        double secondX = centerX + secondHandLength * Math.sin(secondAngle);
        double secondY = centerY - secondHandLength * Math.cos(secondAngle);
        lineX = hourX;
        lineY = hourY;
        lineX2 = minuteX;
        lineY2 = minuteY;
        lineX3 = secondX;
        lineY3 = secondY;

        // Paint the hour markers
        for (int i = 0; i < 12; i++) {
            double angle = Math.toDegrees(i * 30);
            double x = centerX + radius * Math.cos(angle);
            double y = centerY - radius * Math.sin(angle);
            Circle hourMarker = new Circle(radius/10);
            hourMarker.setFill(Color.GRAY);
            hourMarker.setStroke(Color.GRAY);
            hourMarker.setCenterX(x);
            hourMarker.setCenterY(y);
            hourMarkers.add(hourMarker);
        }

        // Paint the minute markers
        for (int i = 0; i < 60; i++) {
            double angle = Math.toDegrees(i / 5);
            double x = centerX + radius * Math.cos(angle);
            double y = centerY - radius * Math.sin(angle);
            Circle minuteMarker = new Circle(radius/20);
            minuteMarker.setFill(Color.GRAY);
            minuteMarker.setStroke(Color.GRAY);
            minuteMarker.setCenterX(x);
            minuteMarker.setCenterY(y);
            minuteMarkers.add(minuteMarker);
        }

        // Paint the second markers
        for (int i = 0; i < 60; i++) {
            double angle = Math.toDegrees(i / 10);
            double x = centerX + radius * Math.cos(angle);
            double y = centerY - radius * Math.sin(angle);
            Circle secondMarker = new Circle(radius/30);
            secondMarker.setFill(Color.GRAY);
            secondMarker.setStroke(Color.GRAY);
            secondMarker.setCenterX(x);
            secondMarker.setCenterY(y);
            secondMarkers.add(secondMarker);
        }
    }
}
```
/** Set a new minute */
public void setMinute(int minute) {
    this.minute = minute;
paintClock();
}

/** Return second */
public int getSecond() {
    return second;
}

/** Set a new second */
public void setSecond(int second) {
    this.second = second;
paintClock();
}

/** Return clock pane's width */
public double getW() {
    return w;
}

/** Set clock pane's width */
public void setW(double w) {
    this.w = w;
paintClock();
}

/** Return clock pane's height */
public double getH() {
    return h;
}

/** Set clock pane's height */
public void setH(double h) {
    this.h = h;
paintClock();
}

/** Set the current time for the clock */
public void setCurrentTime() {
    Calendar calendar = new GregorianCalendar();
    this.hour = calendar.get(Calendar.HOUR_OF_DAY);
    this.minute = calendar.get(Calendar.MINUTE);
    this.second = calendar.get(Calendar.SECOND);
paintClock(); // Repaint the clock
}

/** Paint the clock */
protected void paintClock() {
    // Initialize clock parameters
    double clockRadius = Math.min(w, h) * 0.8 * 0.5;
double centerX = w / 2;
double centerY = h / 2;
    // Draw circle
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```java
Circle circle = new Circle(centerX, centerY, clockRadius);
circle.setFill(Color.WHITE);
circle.setStroke(Color.BLACK);

Text t1 = new Text(centerX - 5, centerY - clockRadius + 12, "12");
Text t2 = new Text(centerX - clockRadius + 3, centerY + 5, "9");
Text t3 = new Text(centerX + clockRadius - 10, centerY + 3, "3");
Text t4 = new Text(centerX - 3, centerY + clockRadius - 3, "6");

// Draw second hand
double sLength = clockRadius * 0.8;
double secondX = centerX + sLength * Math.sin(second * (2 * Math.PI / 60));
double secondY = centerY - sLength * Math.cos(second * (2 * Math.PI / 60));

// Draw minute hand
double mLength = clockRadius * 0.65;
double xMinute = centerX + mLength * Math.sin(minute * (2 * Math.PI / 60));
double minuteY = centerY - mLength * Math.cos(minute * (2 * Math.PI / 60));

// Draw hour hand
double hLength = clockRadius * 0.5;
double hourX = centerX + hLength * Math.sin((hour % 12 + minute / 60.0) * (2 * Math.PI / 12));
double hourY = centerY - hLength * Math.cos((hour % 12 + minute / 60.0) * (2 * Math.PI / 12));

getChildren().clear();
getChildren().addAll(circle, t1, t2, t3, t4, sLine, mLine, hLine);
```

The program displays a clock for the current time using the no-arg constructor (lines 18–20) and displays a clock for the specified hour, minute, and second using the other constructor (lines 23–28). The current hour, minute, and second is obtained by using the `GregorianCalendar` class (lines 86–96). The `GregorianCalendar` class in the Java API enables you to create a `Calendar` instance for the current time using its no-arg constructor. You can then use its methods `get(Calendar.HOUR)`, `get(Calendar.MINUTE)`, and `get(Calendar.SECOND)` to return the hour, minute, and second from a `Calendar` object.

The class defines the properties `hour`, `minute`, and `second` to store the time represented in the clock (lines 10–12) and uses the `w` and `h` properties to represent the width and height of the clock pane (line 15). The initial values of `w` and `h` are set to 250. The `w` and `h` values can be reset using the `setW` and `setH` methods (lines 69, 80). These values are used to draw a clock in the pane in the `paintClock()` method.

The `paintClock()` method paints the clock (lines 99–143). The clock radius is proportional to the width and height of the pane (line 101). A circle for the clock is created at the center of the pane (line 106). The text for showing the hours 12, 3, 6, 9 are created in lines 109–112.

The `paintClock()` method paints the clock (lines 99–143). The clock radius is proportional to the width and height of the pane (line 101). A circle for the clock is created at the center of the pane (line 106). The text for showing the hours 12, 3, 6, 9 are created in lines 109–112.
The second hand, minute hand, and hour hand are the lines created in lines 114–139. The `paintClock()` method places all these shapes in the pane using the `addAll` method in a list (line 142). Because the `paintClock()` method is invoked whenever a new property (`hour`, `minute`, `second`, `w`, and `h`) is set (lines 27, 38, 49, 60, 71, 82, 95), before adding new contents into the pane, the old contents are cleared from the pane (line 141).

**Key Terms**

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</tr>
<tr>
<td>primary stage</td>
<td>537</td>
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<td>shape</td>
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<td>Swing</td>
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<tr>
<td>value getter method</td>
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<tr>
<td>value setter method</td>
<td>543</td>
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<tr>
<td>UI control</td>
<td>539</td>
</tr>
<tr>
<td>unidirectional binding</td>
<td>544</td>
</tr>
</tbody>
</table>

**Chapter Summary**

1. JavaFX is the new framework for developing rich Internet applications. JavaFX completely replaces Swing and AWT.

2. A main JavaFX class must extend `javafx.application.Application` and implement the `start` method. The primary stage is automatically created by the JVM and passed to the `start` method.

3. A stage is a window for displaying a scene. You can add nodes to a scene. Panes, controls, and shapes are nodes. Panes can be used as the containers for nodes.

4. A binding property can be bound to an observable source object. A change in the source object will be automatically reflected in the binding property. A binding property has a value getter method, value setter method, and property getter method.

5. The `Node` class defines many properties that are common to all nodes. You can apply these properties to panes, controls, and shapes.

6. You can create a `Color` object with the specified red, green, blue components, and opacity value.

7. You can create a `Font` object and set its name, size, weight, and posture.

8. The `javafx.scene.image.Image` class can be used to load an image and this image can be displayed in an `ImageView` object.

9. JavaFX provides many types of panes for automatically laying out nodes in a desired location and size. The `Pane` is the base class for all panes. It contains the `getChildren()` method to return an `ObservableList`. You can use `ObservableList's add(node)` and `addAll(node1, node2, ...)` methods for adding nodes into a pane.
10. A **FlowPane** arranges the nodes in the pane horizontally from left to right or vertically from top to bottom in the order in which they were added. A **GridPane** arranges nodes in a grid (matrix) formation. The nodes are placed in the specified column and row indices. A **BorderPane** can place nodes in five regions: top, bottom, left, right, and center. An **HBox** lays out its children in a single horizontal row. A **VBox** lays out its children in a single vertical column.

11. JavaFX provides many shape classes for drawing texts, lines, circles, rectangles, ellipses, arcs, polygons, and polylines.

**Quiz**

Answer the quiz for this chapter online at [www.cs.armstrong.edu/liang/intro10e/quiz.html](http://www.cs.armstrong.edu/liang/intro10e/quiz.html).

**PROGRAMMING EXERCISES**

**Note**

The image files used in the exercises can be obtained from [www.cs.armstrong.edu/liang/intro10e/book.zip](http://www.cs.armstrong.edu/liang/intro10e/book.zip) under the image folder.

**Sections 14.2–14.9**

14.1 *(Display images)* Write a program that displays four images in a grid pane, as shown in Figure 14.43a.

![Exercise14_01](image) ![Exercise14_02](image) ![Exercise14_03](image)

**Figure 14.43** (a) Exercise 14.1 displays four images. (b) Exercise 14.2 displays a tic-tac-toe board with images. (c) Three cards are randomly selected.

*14.2 *(Tic-tac-toe board)* Write a program that displays a tic-tac-toe board, as shown in Figure 14.43b. A cell may be X, O, or empty. What to display at each cell is randomly decided. The X and O are images in the files *x.gif* and *o.gif*.

*14.3 *(Display three cards)* Write a program that displays three cards randomly selected from a deck of 52, as shown in Figure 14.43c. The card image files are named *1.png*, *2.png*, ..., *52.png* and stored in the *image/card* directory. All three cards are distinct and selected randomly. Hint: You can select random cards by storing the numbers 1–52 to an array list, perform a random shuffle introduced in Section 11.12, and use the first three numbers in the array list as the file names for the image.

14.4 *(Color and font)* Write a program that displays five texts vertically, as shown in Figure 14.44a. Set a random color and opacity for each text and set the font of each text to Times Roman, bold, italic, and 22 pixels.
14.5  *(Characters around circle)*  Write a program that displays a string Welcome to Java around the circle, as shown in Figure 14.44b. Hint: You need to display each character in the right location with appropriate rotation using a loop.

*14.6  *(Game: display a checkerboard)*  Write a program that displays a checkerboard in which each white and black cell is a Rectangle with a fill color black or white, as shown in Figure 14.44c.

Sections 14.10–14.11

*14.7  *(Display random 0 or 1)*  Write a program that displays a 10-by-10 square matrix, as shown in Figure 14.45a. Each element in the matrix is 0 or 1, randomly generated. Display each number centered in a text field. Use TextField’s setText method to set value 0 or 1 as a string.

14.8  *(Display 54 cards)*  Expand Exercise 14.3 to display all 54 cards (including two jokers), nine per row. The image files are jokers and are named 53.jpg and 54.jpg.

*14.9  *(Create four fans)*  Write a program that places four fans in a GridPane with two rows and two columns, as shown in Figure 14.45b.

*14.10  *(Display a cylinder)*  Write a program that draws a cylinder, as shown in Figure 14.45b. You can use the following method to set the dashed stroke for an arc:

```java
arc.setStrokeDashArray().addAll(6.0, 21.0);
```
**14.11** *(Paint a smiley face)* Write a program that paints a smiley face, as shown in Figure 14.46a.

![Smiley face](image)

**14.12** *(Display a bar chart)* Write a program that uses a bar chart to display the percentages of the overall grade represented by projects, quizzes, midterm exams, and the final exam, as shown in Figure 14.46b. Suppose that projects take 20 percent and are displayed in red, quizzes take 10 percent and are displayed in blue, midterm exams take 30 percent and are displayed in green, and the final exam takes 40 percent and is displayed in orange. Use the `Rectangle` class to display the bars. Interested readers may explore the JavaFX `BarChart` class for further study.

**14.13** *(Display a pie chart)* Write a program that uses a pie chart to display the percentages of the overall grade represented by projects, quizzes, midterm exams, and the final exam, as shown in Figure 14.46c. Suppose that projects take 20 percent and are displayed in red, quizzes take 10 percent and are displayed in blue, midterm exams take 30 percent and are displayed in green, and the final exam takes 40 percent and is displayed in orange. Use the `Arc` class to display the pies. Interested readers may explore the JavaFX `PieChart` class for further study.

**14.14** *(Display a rectanguloid)* Write a program that displays a rectanguloid, as shown in Figure 14.47a. The cube should grow and shrink as the window grows or shrinks.

![Rectanguloid](image)

**14.15** *(Display a STOP sign)* Write a program that displays a STOP sign, as shown in Figure 14.47b. The octagon is in red and the sign is in white. *(Hint: Place an octagon and a text in a stack pane.)*
*14.16 (Display a 3 × 3 grid) Write a program that displays a 3 × 3 grid, as shown in Figure 14.47c. Use red color for vertical lines and blue for horizontals. The lines are automatically resized when the window is resized.

14.17 (Game: hangman) Write a program that displays a drawing for the popular hangman game, as shown in Figure 14.48a.

![Images](a) Exercise 14.17 draws a sketch for the hangman game. (c) Exercise 14.18 plots the quadratic function. (c) Exercise 14.19 plots the sine/cosine functions.

*14.18 (Plot the square function) Write a program that draws a diagram for the function \( f(x) = x^2 \) (see Figure 14.48b).

Hint: Add points to a polyline using the following code:

```java
Polyline polyline = new Polyline();
ObservableList<Double> list = polyline.getPoints();
double scaleFactor = 0.0125;
for (int x = -100; x <= 100; x++) {
    list.add(x + 200.0);
    list.add(scaleFactor * x * x);
}
```

**14.19 (Plot the sine and cosine functions) Write a program that plots the sine function in red and cosine in blue, as shown in Figure 14.48c.

Hint: The Unicode for \( \pi \) is \u03c0. To display \(-2\pi\), use `Text(x, y, "-2\u03c0")`. For a trigonometric function like \( \sin(x) \), \( x \) is in radians. Use the following loop to add the points to a polyline:

```java
Polyline polyline = new Polyline();
ObservableList<Double> list = polyline.getPoints();
double scaleFactor = 50;
for (int x = -170; x <= 170; x++) {
    list.add(x + 200.0);
    list.add(100 - 50 * Math.sin((x / 100.0) * 2 * Math.PI));
}
```

**14.20 (Draw an arrow line) Write a static method that draws an arrow line from a starting point to an ending point in a pane using the following method header:

```java
public static void drawArrowLine(double startX, double startY, double endX, double endY, Pane pane)
```

Write a test program that randomly draws an arrow line, as shown in Figure 14.49a.
*14.21 (Two circles and their distance) Write a program that draws two filled circles with radius 15 pixels, centered at random locations, with a line connecting the two circles. The distance between the two centers is displayed on the line, as shown in Figure 14.49b.

*14.22 (Connect two circles) Write a program that draws two circles with radius 15 pixels, centered at random locations, with a line connecting the two circles. The line should not cross inside the circles, as shown in Figure 14.49c.

*14.23 (Geometry: two rectangles) Write a program that prompts the user to enter the center coordinates, width, and height of two rectangles from the command line. The program displays the rectangles and a text indicating whether the two are overlapping, whether one is contained in the other, or whether they don’t overlap, as shown in Figure 14.50. See Programming Exercise 10.13 for checking the relationship between two rectangles.

*14.24 (Geometry: Inside a polygon?) Write a program that prompts the user to enter the coordinates of five points from the command line. The first four points form a polygon, and the program displays the polygon and a text that indicates whether the fifth point is inside the polygon, as shown in Figure 14.51a. Hint: Use the Node’s contains method to test whether a point is inside a node.
*14.25  \((Random \ points \ on \ a \ circle)\) Modify Programming Exercise 4.6 to create five random points on a circle, form a polygon by connecting the points clockwise, and display the circle and the polygon, as shown in Figure 14.51b.

**Section 14.12**

14.26  \((Use \ the \ ClockPane \ class)\) Write a program that displays two clocks. The hour, minute, and second values are 4, 20, 45 for the first clock and 22, 46, 15 for the second clock, as shown in Figure 14.51c.

*14.27  \((Draw \ a \ detailed \ clock)\) Modify the ClockPane class in Section 14.12 to draw the clock with more details on the hours and minutes, as shown in Figure 14.52a.

*14.28  \((Random \ time)\) Modify the ClockPane class with three new Boolean properties—hourHandVisible, minuteHandVisible, and secondHandVisible—and their associated accessor and mutator methods. You can use the set methods to make a hand visible or invisible. Write a test program that displays only the hour and minute hands. The hour and minute values are randomly generated. The hour is between 0 and 11, and the minute is either 0 or 30, as shown in Figure 14.52b.

**14.29  \((Game: \ bean \ machine)\) Write a program that displays a bean machine introduced in Programming Exercise 7.21, as shown in Figure 14.52c.
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Event-Driven Programming and Animations

Objectives

- To get a taste of event-driven programming (§15.1).
- To describe events, event sources, and event classes (§15.2).
- To define handler classes, register handler objects with the source object, and write the code to handle events (§15.3).
- To define handler classes using inner classes (§15.4).
- To define handler classes using anonymous inner classes (§15.5).
- To simplify event handling using lambda expressions (§15.6).
- To develop a GUI application for a loan calculator (§15.7).
- To write programs to deal with MouseEvents (§15.8).
- To write programs to deal with KeyEvent (§15.9).
- To create listeners for processing a value change in an observable object (§15.10).
- To use the Animation, PathTransition, FadeTransition, and Timeline classes to develop animations (§15.11).
- To develop an animation for simulating a bouncing ball (§15.12).
15.1 Introduction

You can write code to process events such as a button click, mouse movement, and keystrokes.

Suppose you wish to write a GUI program that lets the user enter a loan amount, annual interest rate, and number of years and click the Calculate button to obtain the monthly payment and total payment, as shown in Figure 15.1. How do you accomplish the task? You have to use event-driven programming to write the code to respond to the button-clicking event.

Figure 15.1 The program computes loan payments.

Before delving into event-driven programming, it is helpful to get a taste using a simple example. The example displays two buttons in a pane, as shown in Figure 15.2.

Figure 15.2 (a) The program displays two buttons. (b) A message is displayed in the console when a button is clicked.

To respond to a button click, you need to write the code to process the button-clicking action. The button is an event source object—where the action originates. You need to create an object capable of handling the action event on a button. This object is called an event handler, as shown in Figure 15.3.

Figure 15.3 An event handler processes the event fired from the source object.

Not all objects can be handlers for an action event. To be a handler of an action event, two requirements must be met:

1. The object must be an instance of the EventHandler<T extends Event> interface. This interface defines the common behavior for all handlers. <T extends Event> denotes that T is a generic type that is a subtype of Event.

2. The EventHandler object handler must be registered with the event source object using the method source.setOnAction(handler).
The `EventHandler<ActionEvent>` interface contains the `handle(ActionEvent)` method for processing the action event. Your handler class must override this method to respond to the event. Listing 15.1 gives the code that processes the `ActionEvent` on the two buttons. When you click the `OK` button, the message “OK button clicked” is displayed. When you click the `Cancel` button, the message “Cancel button clicked” is displayed, as shown in Figure 15.2.

**Listing 15.1 HandleEvent.java**

```java
import javafx.application.Application;
import javafx.geometry.Pos;
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.scene.layout.HBox;
import javafx.stage.Stage;
import javafx.event.ActionEvent;
import javafx.event.EventHandler;

public class HandleEvent extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a pane and set its properties
        HBox pane = new HBox(10);
        pane.setAlignment(Pos.CENTER);
        Button btOK = new Button("OK");
        Button btCancel = new Button("Cancel");
        OKHandlerClass handler1 = new OKHandlerClass();
        btOK.setOnAction(handler1);
        CancelHandlerClass handler2 = new CancelHandlerClass();
        btCancel.setOnAction(handler2);
        pane.getChildren().addAll(btOK, btCancel);

        // Create a scene and place it in the stage
        Scene scene = new Scene(pane);
        primaryStage.setTitle("HandleEvent"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }
}

class OKHandlerClass implements EventHandler<ActionEvent> {
    @Override
    public void handle(ActionEvent e) {
        System.out.println("OK button clicked");
    }
}

class CancelHandlerClass implements EventHandler<ActionEvent> {
    @Override
    public void handle(ActionEvent e) {
        System.out.println("Cancel button clicked");
    }
}
```

Two handler classes are defined in lines 32–44. Each handler class implements `EventHandler<ActionEvent>` to process `ActionEvent`. The object `handler1` is an instance of `OKHandlerClass` (line 18), which is registered with the button `btOK` (line 19). When the `OK` button is clicked, the `handle(ActionEvent)` method (line 34) in
OKHandlerClass is invoked to process the event. The object handler2 is an instance of CancelHandlerClass (line 20), which is registered with the button btCancel in line 21. When the Cancel button is clicked, the handle(ActionEvent) method (line 41) in CancelHandlerClass is invoked to process the event.

You now have seen a glimpse of event-driven programming in JavaFX. You probably have many questions, such as why a handler class is defined to implement the EventHandler<ActionEvent>. The following sections will give you all the answers.

15.2 Events and Event Sources

An event is an object created from an event source. Firing an event means to create an event and delegate the handler to handle the event.

When you run a Java GUI program, the program interacts with the user, and the events drive its execution. This is called event-driven programming. An event can be defined as a signal to the program that something has happened. Events are triggered by external user actions, such as mouse movements, mouse clicks, and keystrokes. The program can choose to respond to or ignore an event. The example in the preceding section gave you a taste of event-driven programming.

The component that creates an event and fires it is called the event source object, or simply source object or source component. For example, a button is the source object for a button-clicking action event. An event is an instance of an event class. The root class of the Java event classes is java.util.EventObject. The root class of the JavaFX event classes is javafx.event.Event. The hierarchical relationships of some event classes are shown in Figure 15.4.

Figure 15.4 An event in JavaFX is an object of the javafx.event.Event class.

An event object contains whatever properties are pertinent to the event. You can identify the source object of an event using the getSource() instance method in the EventObject class. The subclasses of EventObject deal with specific types of events, such as action events, window events, mouse events, and key events. The first three columns in Table 15.1 list some external user actions, source objects, and event types fired. For example, when clicking a button, the button creates and fires an ActionEvent, as indicated in the first line of this table. Here, the button is an event source object, and an ActionEvent is the event object fired by the source object, as shown in Figure 15.3.

Note

If a component can fire an event, any subclass of the component can fire the same type of event. For example, every JavaFX shape, layout pane, and control can fire MouseEvent and KeyEvent since Node is the superclass for shapes, layout panes, and controls.
15.3 Registering Handlers and Handling Events

A handler is an object that must be registered with an event source object, and it must be an instance of an appropriate event-handling interface.

Java uses a delegation-based model for event handling: a source object fires an event, and an object interested in the event handles it. The latter object is called an event handler or an event listener. For an object to be a handler for an event on a source object, two things are needed, as shown in Figure 15.5.

1. The handler object must be an instance of the corresponding event-handler interface to ensure that the handler has the correct method for processing the event. JavaFX defines a unified handler interface `EventHandler<T extends Event>` for an event `T`. The handler interface contains the `handle(T e)` method for processing the event. For example, the handler interface for `ActionEvent` is `EventHandler<ActionEvent>`; each handler for `ActionEvent` should implement the `handle(ActionEvent e)` method for processing an `ActionEvent`.

2. The handler object must be registered by the source object. Registration methods depend on the event type. For `ActionEvent`, the method is `setOnAction`. For a mouse pressed event, the method is `setOnMousePressed`. For a key pressed event, the method is `setOnKeyPressed`.

Let’s revisit Listing 15.1, HandleEvent.java. Since a `Button` object fires `ActionEvent`, a handler object for `ActionEvent` must be an instance of `EventHandler<ActionEvent>`, so
the handler class implements `EventHandler<ActionEvent>` in line 34. The source object invokes `setOnAction(handler)` to register a handler, as follows:

```java
Button btOK = new Button("OK"); // Line 16 in Listing 15.1
OKHandlerClass handler1 = new OKHandlerClass(); // Line 18 in Listing 15.1
btOK.setOnAction(handler1); // Line 19 in Listing 15.1
```

When you click the button, the `Button` object fires an `ActionEvent` and passes it to invoke the handler’s `handle(ActionEvent)` method to handle the event. The event object contains information pertinent to the event, which can be obtained using the methods. For example, you can use `e.getSource()` to obtain the source object that fired the event.

We now write a program that uses two buttons to control the size of a circle, as shown in Figure 15.6. We will develop this program incrementally. First, we write the program in Listing 15.2 that displays the user interface with a circle in the center (lines 15-19) and two buttons on the bottom (lines 21-27).

```
import javafx.application.Application;
import javafx.geometry.Pos;
import javafx.scene.Scene;
import javafx.scene.control.Button;
```

**Figure 15.6** The user clicks the *Enlarge* and *Shrink* buttons to enlarge and shrink the size of the circle.

**Listing 15.2** ControlCircleWithoutEventHandling.java

1. import javafx.application.Application;
2. import javafx.geometry.Pos;
3. import javafx.scene.Scene;
4. import javafx.scene.control.Button;
15.3 Registering Handlers and Handling Events

```java
import javafx.scene.layout.StackPane;
import javafx.scene.layout.HBox;
import javafx.scene.layout.BorderPane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Circle;
import javafx.stage.Stage;

public class ControlCircleWithoutEventHandling extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        StackPane pane = new StackPane();
        Circle circle = new Circle(50);
        circle.setStroke(Color.BLACK);
        circle.setFill(Color.WHITE);
        pane.getChildren().add(circle);

        HBox hBox = new HBox();
        hBox.setSpacing(10);
        hBox.setAlignment(Pos.CENTER);
        Button btEnlarge = new Button("Enlarge");
        Button btShrink = new Button("Shrink");
        hBox.getChildren().add(btEnlarge);
        hBox.getChildren().add(btShrink);

        BorderPane borderPane = new BorderPane();
        borderPane.setCenter(pane);
        borderPane.setBottom(hBox);
        BorderPane.setAlignment(hBox, Pos.CENTER);

        // Create a scene and place it in the stage
        Scene scene = new Scene(borderPane, 200, 150);
        primaryStage.setTitle("ControlCircle"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }
}
```

How do you use the buttons to enlarge or shrink the circle? When the **Enlarge** button is clicked, you want the circle to be repainted with a larger radius. How can you accomplish this? You can expand and modify the program in Listing 15.2 into Listing 15.3 with the following features:

1. Define a new class named `CirclePane` for displaying the circle in a pane (lines 51–68). This new class displays a circle and provides the `enlarge` and `shrink` methods for increasing and decreasing the radius of the circle (lines 60–62, 64–67). It is a good strategy to design a class to model a circle pane with supporting methods so that these related methods along with the circle are coupled in one object.

2. Create a `CirclePane` object and declare `circlePane` as a data field to reference this object (line 15) in the `ControlCircle` class. The methods in the `ControlCircle` class can now access the `CirclePane` object through this data field.

3. Define a handler class named `EnlargeHandler` that implements `EventHandler<ActionEvent>` (lines 43–48). To make the reference variable `circlePane` accessible from the `handle` method, define `EnlargeHandler` as an inner class of the `ControlCircle` class. (**Inner classes** are defined inside another class. We use an inner class here and will introduce it fully in the next section.)

4. Register the handler for the **Enlarge** button (line 29) and implement the `handle` method in `EnlargeHandler` to invoke `circlePane.enlarge()` (line 46).
LISTING 15.3  ControlCircle.java

```java
import javafx.application.Application;
import javafx.event.ActionEvent;
import javafx.event.EventHandler;
import javafx.geometry.Pos;
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.scene.layout.StackPane;
import javafx.scene.layout.HBox;
import javafx.scene.layout.BorderPane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Circle;
import javafx.stage.Stage;

public class ControlCircle extends Application {
    private CirclePane circlePane = new CirclePane();

    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Hold two buttons in an HBox
        HBox hBox = new HBox();
        hBox.setSpacing(10);
        hBox.setAlignment(Pos.CENTER);
        Button btEnlarge = new Button("Enlarge");
        Button btShrink = new Button("Shrink");
        hBox.getChildren().add(btEnlarge);
        hBox.getChildren().add(btShrink);

        // Create and register the handler
        btEnlarge.setOnAction(new EnlargeHandler());

        BorderPane borderPane = new BorderPane();
        borderPane.setCenter(circlePane);
        borderPane.setBottom(hBox);
        BorderPane.setAlignment(hBox, Pos.CENTER);

        // Create a scene and place it in the stage
        Scene scene = new Scene(borderPane, 200, 150);
        primaryStage.setTitle("ControlCircle"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }

    class EnlargeHandler implements EventHandler<ActionEvent> {
        @Override // Override the handle method
        public void handle(ActionEvent e) {
            circlePane.enlarge();
        }
    }

    class CirclePane extends StackPane {
        private Circle circle = new Circle(50);

        public CirclePane() {
            getChildren().add(circle);
            circle.setStroke(Color.BLACK);
            circle.setFill(Color.WHITE);
        }
    }
```
public void enlarge() {
    circle.setRadius(circle.getRadius() + 2);
}

public void shrink() {
    circle.setRadius(circle.getRadius() > 2 ?
        circle.getRadius() - 2 : circle.getRadius());
}

As an exercise, add the code for handling the Shrink button to display a smaller circle when the Shrink button is clicked.

15.3 Why must a handler be an instance of an appropriate handler interface?
15.4 Explain how to register a handler object and how to implement a handler interface.
15.5 What is the handler method for the EventHandler<ActionEvent> interface?
15.6 What is the registration method for a button to register an ActionEvent handler?

15.4 Inner Classes

An inner class, or nested class, is a class defined within the scope of another class. Inner classes are useful for defining handler classes.

Inner classes are used in the preceding section. This section introduces inner classes in detail. First, let us see the code in Figure 15.7. The code in Figure 15.7a defines two separate classes, Test and A. The code in Figure 15.7b defines A as an inner class in Test.

As an exercise, add the code for handling the Shrink button to display a smaller circle when the Shrink button is clicked.

The class InnerClass defined inside OuterClass in Figure 15.7c is another example of an inner class. An inner class may be used just like a regular class. Normally, you define
Chapter 15  Event-Driven Programming and Animations

a class as an inner class if it is used only by its outer class. An inner class has the following features:

- An inner class is compiled into a class named `OuterClassName$InnerClassName.class`. For example, the inner class `A` in `Test` is compiled into `Test$A.class` in Figure 15.7b.

- An inner class can reference the data and the methods defined in the outer class in which it nests, so you need not pass the reference of an object of the outer class to the constructor of the inner class. For this reason, inner classes can make programs simple and concise. For example, `circlePane` is defined in `ControlCircle` in Listing 15.3 (line 15). It can be referenced in the inner class `EnlargeHandler` in line 46.

- An inner class can be defined with a visibility modifier subject to the same visibility rules applied to a member of the class.

- An inner class can be defined as `static`. A `static` inner class can be accessed using the outer class name. A `static` inner class cannot access nonstatic members of the outer class.

- Objects of an inner class are often created in the outer class. But you can also create an object of an inner class from another class. If the inner class is nonstatic, you must first create an instance of the outer class, then use the following syntax to create an object for the inner class:

  ```java
  OuterClass.InnerClass innerObject = outerObject.new InnerClass();
  ```

- If the inner class is static, use the following syntax to create an object for it:

  ```java
  OuterClass.InnerClass innerObject = new OuterClass.InnerClass();
  ```

A simple use of inner classes is to combine dependent classes into a primary class. This reduces the number of source files. It also makes class files easy to organize since they are all named with the primary class as the prefix. For example, rather than creating the two source files `Test.java` and `A.java` as shown in Figure 15.7a, you can merge class `A` into class `Test` and create just one source file, `Test.java` as shown in Figure 15.7b. The resulting class files are `Test.class` and `Test$A.class`.

Another practical use of inner classes is to avoid class-naming conflicts. Two versions of `CirclePane` are defined in Listings 15.2 and 15.3. You can define them as inner classes to avoid a conflict.

A handler class is designed specifically to create a handler object for a GUI component (e.g., a button). The handler class will not be shared by other applications and therefore is appropriate to be defined inside the main class as an inner class.

15.7 Can an inner class be used in a class other than the class in which it nests?

15.8 Can the modifiers `public`, `protected`, `private`, and `static` be used for inner classes?

### 15.5 Anonymous Inner Class Handlers

An anonymous inner class is an inner class without a name. It combines defining an inner class and creating an instance of the class into one step.

Inner-class handlers can be shortened using *anonymous inner classes*. The inner class in Listing 15.3 can be replaced by an anonymous inner class as shown below.

```java
    Point check = new Point();
    Point key = new Key();
```
The syntax for an anonymous inner class is shown below:

```java
new SuperClassName/InterfaceName() {
    // Implement or override methods in superclass or interface
    // Other methods if necessary
}
```

Since an anonymous inner class is a special kind of inner class, it is treated like an inner class with the following features:

- An anonymous inner class must always extend a superclass or implement an interface, but it cannot have an explicit `extends` or `implements` clause.
- An anonymous inner class must implement all the abstract methods in the superclass or in the interface.
- An anonymous inner class always uses the no-arg constructor from its superclass to create an instance. If an anonymous inner class implements an interface, the constructor is `Object()`.
- An anonymous inner class is compiled into a class named `OuterClassName$.class`. For example, if the outer class `Test` has two anonymous inner classes, they are compiled into `Test$1.class` and `Test$2.class`.

Listing 15.4 gives an example that handles the events from four buttons, as shown in Figure 15.8.

```java
import javafx.application.Application;
import javafx.event.ActionEvent;
import javafx.event.EventHandler;
import javafx.geometry.Pos;
import javafx.scene.Scene;

public class EnlargeListener implements EventHandler<ActionEvent> {
    public void handle(ActionEvent e) {
        circlePane.enlarge();
    }
}

Listing 15.4 AnonymousHandlerDemo.java
```

**Figure 15.8** The program handles the events from four buttons.

**Listing 15.4** AnonymousHandlerDemo.java
import javafx.scene.control.Button;
import javafx.scene.layout.HBox;
import javafx.stage.Stage;

public class AnonymousHandlerDemo extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Hold two buttons in an HBox
        HBox hBox = new HBox();
        hBox.setSpacing(10);
        hBox.setAlignment(Pos.CENTER);
        Button btNew = new Button("New");
        Button btOpen = new Button("Open");
        Button btSave = new Button("Save");
        Button btPrint = new Button("Print");
        hBox.getChildren().addAll(btNew, btOpen, btSave, btPrint);

        btNew.setOnAction(new EventHandler<ActionEvent>() { // Create and register the handler
            @Override // Override the handle method
            public void handle(ActionEvent e) {
                System.out.println("Process New");
            }
        });

        btOpen.setOnAction(new EventHandler<ActionEvent>() { // Override the handle method
            @Override // Override the handle method
            public void handle(ActionEvent e) {
                System.out.println("Process Open");
            }
        });

        btSave.setOnAction(new EventHandler<ActionEvent>() { // Override the handle method
            @Override // Override the handle method
            public void handle(ActionEvent e) {
                System.out.println("Process Save");
            }
        });

        btPrint.setOnAction(new EventHandler<ActionEvent>() { // Override the handle method
            @Override // Override the handle method
            public void handle(ActionEvent e) {
                System.out.println("Process Print");
            }
        });

        // Create a scene and place it in the stage
        Scene scene = new Scene(hBox, 300, 50);
        primaryStage.setTitle("AnonymousHandlerDemo"); // Set title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }
}

The program creates four handlers using anonymous inner classes (lines 24–50). Without using anonymous inner classes, you would have to create four separate classes. An anonymous handler works the same way as that of an inner class handler. The program is condensed using an anonymous inner class.
15.6 Simplifying Event Handling Using Lambda Expressions

Lambda expressions can be used to greatly simplify coding for event handling.

Lambda expression is a new feature in Java 8. Lambda expressions can be viewed as an anonymous class with a concise syntax. For example, the following code in (a) can be greatly simplified using a lambda expression in (b) in three lines.

(a) Anonymous inner class event handler
(b) Lambda expression event handler

The basic syntax for a lambda expression is either

(type1 param1, type2 param2, ...) -> expression

or

(type1 param1, type2 param2, ...) -> { statements; }
The data type for a parameter may be explicitly declared or implicitly inferred by the compiler. The parentheses can be omitted if there is only one parameter without an explicit data type. In the preceding example, the lambda expression is as follows:

```java
e -> {
    // Code for processing event e
}
```

The compiler treats a lambda expression as if it is an object created from an anonymous inner class. In this case, the compiler understands that the object must be an instance of `EventHandler<ActionEvent>`. Since the `EventHandler` interface defines the `handle` method with a parameter of the `ActionEvent` type, the compiler automatically recognizes that `e` is a parameter of the `ActionEvent` type, and the statements are for the body of the `handle` method. The `EventHandler` interface contains just one method. The statements in the lambda expression are all for that method. If it contains multiple methods, the compiler will not be able to compile the lambda expression. So, for the compiler to understand lambda expressions, the interface must contain exactly one abstract method. Such an interface is known as a functional interface or a Single Abstract Method (SAM) interface.

Listing 15.4 can be simplified using lambda expressions as shown in Listing 15.5.

### Listing 15.5  LambdaHandlerDemo.java

```java
import javafx.application.Application;
import javafx.event.ActionEvent;
import javafx.geometry.Pos;
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.scene.layout.HBox;
import javafx.stage.Stage;

public class LambdaHandlerDemo extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Hold two buttons in an HBox
        HBox hBox = new HBox();
        hBox.setSpacing(10);
        hBox.setAlignment(Pos.CENTER);

        Button btNew = new Button("New");
        Button btOpen = new Button("Open");
        Button btSave = new Button("Save");
        Button btPrint = new Button("Print");

        hBox.getChildren().addAll(btNew, btOpen, btSave, btPrint);

        // Create and register the handler
        btNew.setOnAction((ActionEvent e) -> {
            System.out.println("Process New");
        });

        btOpen.setOnAction((e) -> {
            System.out.println("Process Open");
        });

        btSave.setOnAction(e -> {
            System.out.println("Process Save");
        });

        btPrint.setOnAction(e -> System.out.println("Process Print"));
    }
}
```
15.6 Simplifying Event Handling Using Lambda Expressions

36  // Create a scene and place it in the stage
37  Scene scene = new Scene(hBox, 300, 50);
38  primaryStage.setTitle("LambdaHandlerDemo"); // Set title
39  primaryStage.setScene(scene); // Place the scene in the stage
40  primaryStage.show(); // Display the stage
41  }
42  }

The program creates four handlers using lambda expressions (lines 23–35). Using lambda expressions, the code is shorter and cleaner. As seen in this example, lambda expressions may have many variations. Line 23 uses a declared type. Line 27 uses an inferred type since the type can be determined by the compiler. Line 31 omits the parentheses for a single inferred type. Line 35 omits the braces for a single statement in the body.

You can handle events by defining handler classes using inner classes, anonymous inner classes, or lambda expressions. We recommend that you use lambda expressions because it produces a shorter, clearer, and cleaner code.

**Check Point**

15.11 What is a lambda expression? What is the benefit of using lambda expressions for event handling? What is the syntax of a lambda expression?

15.12 What is a functional interface? Why is a functional interface required for a lambda expression?

15.13 Show the output of the following code:

```java
public class Test {
    public static void main(String[] args) {
        Test test = new Test();
        test.setAction1(() -> System.out.print("Action 1! "));
        test.setAction2(e -> System.out.print(e + " "));
        System.out.println(test.setAction3(e -> e * 2));
    }

    public void setAction1(T1 t) {
        t.m();
    }

    public void setAction2(T2 t) {
        t.m(4.5);
    }

    public double setAction3(T3 t) {
        return t.m(5.5);
    }
}
```

```java
interface T1 {
    public void m();
}

interface T2 {
    public void m(Double d);
}

interface T3 {
    public double m(Double d);
}
```
15.7 Case Study: Loan Calculator

This case study develops a loan calculator using event-driven programming with GUI controls.

Now, we will write the program for the loan-calculator problem presented at the beginning of this chapter. Here are the major steps in the program:

1. Create the user interface, as shown in Figure 15.9.
   a. Create a GridPane. Add labels, text fields, and button to the pane.
   b. Set the alignment of the button to the right.

2. Process the event.

Create and register the handler for processing the button-clicking action event. The handler obtains the user input on the loan amount, interest rate, and number of years, computes the monthly and total payments, and displays the values in the text fields.

The complete program is given in Listing 15.6.

**Listing 15.6 LoanCalculator.java**

```java
import javafx.application.Application;
import javafx.geometry.Pos;
import javafx.geometry.HPos;
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.scene.control.Label;
import javafx.scene.control.TextField;
import javafx.scene.layout.GridPane;
import javafx.stage.Stage;

public class LoanCalculator extends Application {
    private TextField tfAnnualInterestRate = new TextField();
    private TextField tfNumberOfYears = new TextField();
    private TextField tfLoanAmount = new TextField();
    private TextField tfMonthlyPayment = new TextField();
    private TextField tfTotalPayment = new TextField();
    private Button btCalculate = new Button("Calculate");

    @Override
    public void start(Stage primaryStage) {
        // Create UI
        GridPane gridPane = new GridPane();
```

Figure 15.9 The program computes loan payments.
gridPane.setHgap(5);
gridPane.setVgap(5);
gridPane.add(new Label("Annual Interest Rate:"), 0, 0);
gridPane.add(tfAnnualInterestRate, 1, 0);
gridPane.add(new Label("Number of Years:"), 0, 1);
gridPane.add(tfNumberOfYears, 1, 1);
gridPane.add(new Label("Loan Amount:"), 0, 2);
gridPane.add(tfLoanAmount, 1, 2);
gridPane.add(new Label("Monthly Payment:"), 0, 3);
gridPane.add(tfMonthlyPayment, 1, 3);
gridPane.add(new Label("Total Payment:"), 0, 4);
gridPane.add(tfTotalPayment, 1, 4);
gridPane.add(btCalculate, 1, 5);

// Set properties for UI
gridPane.setAlignment(Pos.CENTER);
tfAnnualInterestRate.setAlignment(Pos.BOTTOM_RIGHT);
tfNumberOfYears.setAlignment(Pos.BOTTOM_RIGHT);
tfLoanAmount.setAlignment(Pos.BOTTOM_RIGHT);
tfMonthlyPayment.setAlignment(Pos.BOTTOM_RIGHT);
tfTotalPayment.setAlignment(Pos.BOTTOM_RIGHT);
tfMonthlyPayment.setEditable(false);
tfTotalPayment.setEditable(false);
GridPane.setHalignment(btCalculate, HPos.RIGHT);

// Process events
btCalculate.setOnAction(e -> calculateLoanPayment());

private void calculateLoanPayment() {
    // Get values from text fields
    double interest = Double.parseDouble(tfAnnualInterestRate.getText());
    int year = Integer.parseInt(tfNumberOfYears.getText());
    double loanAmount = Double.parseDouble(tfLoanAmount.getText());

    // Create a loan object. Loan defined in Listing 10.2
    Loan loan = new Loan(interest, year, loanAmount);

    // Display monthly payment and total payment
    tfMonthlyPayment.setText(String.format("%.2f", loan.getMonthlyPayment()));
    tfTotalPayment.setText(String.format("%.2f", loan.getTotalPayment()));
}

The user interface is created in the start method (lines 22–46). The button is the source of the event. A handler is created and registered with the button (line 49). The button handler invokes the calculateLoanPayment() method to get the interest rate (line 60), number of years (line 62), and loan amount (line 64). Invoking tfAnnualInterestRate.getText() returns the string text in the tfAnnualInterestRate text field. The Loan class is used for
computing the loan payments. This class was introduced in Listing 10.2, Loan.java. Invoking
\texttt{loan.getMonthlyPayment()} returns the monthly payment for the loan (line 71). The
\texttt{String.format} method, introduced in Section 10.10.7, is used to format a number into a
desirable format and returns it as a string (lines 70, 72). Invoking the \texttt{setText} method on a
text field sets a string value in the text field.

15.8 Mouse Events

A \texttt{MouseEvent} is fired whenever a mouse button is pressed, released, clicked, moved,
or dragged on a node or a scene.

The \texttt{MouseEvent} object captures the event, such as the number of clicks associated with it,
the location (the \texttt{x} - and \texttt{y}-coordinates) of the mouse, or which mouse button was pressed, as
shown in Figure 15.10.

<table>
<thead>
<tr>
<th>javafx.scene.input.MouseEvent</th>
</tr>
</thead>
<tbody>
<tr>
<td>\texttt{getButton()} : MouseButton</td>
</tr>
<tr>
<td>\texttt{getClickCount()} : int</td>
</tr>
<tr>
<td>\texttt{getX()} : double</td>
</tr>
<tr>
<td>\texttt{getY()} : double</td>
</tr>
<tr>
<td>\texttt{getSceneX()} : double</td>
</tr>
<tr>
<td>\texttt{getSceneY()} : double</td>
</tr>
<tr>
<td>\texttt{getScreenX()} : double</td>
</tr>
<tr>
<td>\texttt{getScreenY()} : double</td>
</tr>
<tr>
<td>\texttt{isAltDown()} : boolean</td>
</tr>
<tr>
<td>\texttt{isControlDown()} : boolean</td>
</tr>
<tr>
<td>\texttt{isMetaDown()} : boolean</td>
</tr>
<tr>
<td>\texttt{isShiftDown()} : boolean</td>
</tr>
</tbody>
</table>

Four constants—\texttt{PRIMARY}, \texttt{SECONDARY}, \texttt{MIDDLE}, and \texttt{NONE}—are defined in \texttt{MouseButton}
to indicate the left, right, middle, and none mouse buttons. You can use the \texttt{getButton()} method
to detect which button is pressed. For example, \texttt{getButton() == MouseButton.SECONDARY}
indicates that the right button was pressed.

The mouse events are listed in Table 15.1. To demonstrate using mouse events, we give
an example that displays a message in a pane and enables the message to be moved using a
mouse. The message moves as the mouse is dragged, and it is always displayed at the mouse
point. Listing 15.7 gives the program. A sample run of the program is shown in Figure 15.11.

![MouseEventDemo](image)

The \texttt{MouseEvent} class encapsulates information for mouse events.

Figure 15.10

Detect mouse buttons

### Listing 15.7 MouseEventDemo.java

```java
1 import javafx.application.Application;
2 import javafx.scene.Scene;
3 import javafx.scene.layout.Pane;
```

![VideoNote](image)

Move message using the mouse
15.9 Key Events

Each node or scene can fire mouse events. The program creates a `Text` (line 12) and registers a handler to handle move dragged event (line 14). Whenever a mouse is dragged, the text’s `x`- and `y`-coordinates are set to the mouse position (lines 15 and 16).

15.14 What method do you use to get the mouse-point position for a mouse event?

15.15 What methods do you use to register a handler for a mouse pressed, released, clicked, entered, exited, moved and dragged event?

15.9 Key Events

A KeyEvent is fired whenever a key is pressed, released, or typed on a node or a scene.

Key events enable the use of the keys to control and perform actions or get input from the keyboard. The `KeyEvent` object describes the nature of the event (namely, that a key has been pressed, released, or typed) and the value of the key, as shown in Figure 15.12.

```
import javafx.scene.text.Text;
import javafx.stage.Stage;

public class MouseEventDemo extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a pane and set its properties
        Pane pane = new Pane();
        Text text = new Text(20, 20, "Programming is fun");
        pane.getChildren().addAll(text);
        text.setOnMouseDragged(e -> {
            text.setX(e.getX());
            text.setY(e.getY());
        });

        // Create a scene and place it in the stage
        Scene scene = new Scene(pane, 300, 100);
        primaryStage.setTitle("MouseEventDemo"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }
}
```

Every key event has an associated code that is returned by the `getCode()` method in `KeyEvent`. The key codes are constants defined in `KeyCode`. Table 15.2 lists some constants. `KeyCode` is an `enum` type. For use of `enum` types, see Appendix I. For the key-pressed and...
key-released events, `getCode()` returns the value as defined in the table, `getText()` returns a string that describes the key code, and `getCharacter()` returns an empty string. For the key-typed event, `getCode()` returns `UNDEFINED` and `getCharacter()` returns the Unicode character or a sequence of characters associated with the key-typed event.

### Table 15.2 KeyCode Constants

<table>
<thead>
<tr>
<th>Constant</th>
<th>Description</th>
<th>Constant</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>HOME</td>
<td>The Home key</td>
<td>CONTROL</td>
<td>The Control key</td>
</tr>
<tr>
<td>END</td>
<td>The End key</td>
<td>SHIFT</td>
<td>The Shift key</td>
</tr>
<tr>
<td>PAGE_UP</td>
<td>The Page Up key</td>
<td>BACK_SPACE</td>
<td>The Backspace key</td>
</tr>
<tr>
<td>PAGE_DOWN</td>
<td>The Page Down key</td>
<td>CAPS</td>
<td>The Caps Lock key</td>
</tr>
<tr>
<td>UP</td>
<td>The up-arrow key</td>
<td>NUM_LOCK</td>
<td>The Num Lock key</td>
</tr>
<tr>
<td>DOWN</td>
<td>The down-arrow key</td>
<td>ENTER</td>
<td>The Enter key</td>
</tr>
<tr>
<td>LEFT</td>
<td>The left-arrow key</td>
<td>UNDEFINED</td>
<td>The <code>keyCode</code> unknown</td>
</tr>
<tr>
<td>RIGHT</td>
<td>The right-arrow key</td>
<td>F1 to F12</td>
<td>The function keys from F1 to F12</td>
</tr>
<tr>
<td>ESCAPE</td>
<td>The Esc key</td>
<td>0 to 9</td>
<td>The number keys from 0 to 9</td>
</tr>
<tr>
<td>TAB</td>
<td>The Tab key</td>
<td>A to Z</td>
<td>The letter keys from A to Z</td>
</tr>
</tbody>
</table>

The program in Listing 15.8 displays a user-input character. The user can move the character up, down, left, and right, using the up, down, left, and right arrow keys. Figure 15.13 contains a sample run of the program.

![Key event demo](image)

**Figure 15.13** The program responds to key events by displaying a character and moving it up, down, left, or right.

**Listing 15.8 KeyEventDemo.java**

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.layout.Pane;
import javafx.scene.text.Text;
import javafx.stage.Stage;

public class KeyEventDemo extends Application {
    @Override
    public void start(Stage primaryStage) {
        Pane pane = new Pane();
        Text text = new Text(20, 20, "A");
        pane.getChildren().add(text);
        text.setOnKeyPressed(e -> {
            switch (e.getCode()) {
                case DOWN: text.setY(text.getY() + 10); break;
                case UP: text.setY(text.getY() - 10); break;
                case LEFT: text.setX(text.getX() - 10); break;
                case RIGHT: text.setX(text.getX() + 10); break;
            }
            text.setTranslateX(text.getX());
            text.setTranslateY(text.getY());
        });
    }
}
```
15.9 Key Events 605

```java
15.9 Key Events 605

The program creates a pane (line 11), creates a text (line 12), and places the text into the pane (line 14). The text registers the handler for the key-pressed event in lines 15–25. When a key is pressed, the handler is invoked. The program uses `e.getCode()` (line 16) to obtain the key code and `e.getText()` (line 23) to get the character for the key. When a nonarrow key is pressed, the character is displayed (lines 22 and 23). When an arrow key is pressed, the character moves in the direction indicated by the arrow key (lines 17–20). Note that in a switch statement for an enum type value, the cases are for the enum constants (lines 16–24). The constants are unqualified. For example, using `KeyCode.DOWN` in the case clause would be wrong (see Appendix I).

Only a focused node can receive `KeyEvent`. Invoking `requestFocus()` on `text` enables `text` to receive key input (line 33). This method must be invoked after the stage is displayed.

We can now add more control for our `ControlCircle` example in Listing 15.3 to increase/decrease the circle radius by clicking the left/right mouse button or by pressing the U and D keys. The new program is given in Listing 15.9.

**LISTING 15.9 ControlCircleWithMouseAndKey.java**

```java
import javafx.application.Application;
import javafx.geometry.Pos;
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.scene.input.KeyCode;
import javafx.scene.input.MouseButton;
import javafx.scene.layout.HBox;
import javafx.scene.layout.BorderPane;
import javafx.stage.Stage;

public class ControlCircleWithMouseAndKey extends Application {
    private CirclePane circlePane = new CirclePane();

    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Hold two buttons in an HBox
        HBox hBox = new HBox();
        hBox.setSpacing(10);
        hBox.setAlignment(Pos.CENTER);
        Button btEnlarge = new Button("Enlarge");
        Button btShrink = new Button("Shrink");
        hBox.getChildren().add(btEnlarge);
        hBox.getChildren().add(btShrink);

        // Create and register the handler
        btEnlarge.setOnAction(e -> circlePane.enlarge());
        btShrink.setOnAction(e -> circlePane.shrink());
```
The `CirclePane` class (line 12) is already defined in Listing 15.3 and can be reused in this program.

A handler for mouse clicked events is created in lines 29–36. If the left mouse button is clicked, the circle is enlarged (lines 30–32); if the right mouse button is clicked, the circle is shrunk (lines 33–35).

A handler for key pressed events is created in lines 38–45. If the U key is pressed, the circle is enlarged (lines 39–41); if the D key is pressed, the circle is shrunk (lines 42–44).

Invoking `requestFocus()` on `circlePane` (line 58) makes `circlePane` to receive key events. Note that after you click a button, `circlePane` is no longer focused. To fix the problem, invoke `requestFocus()` on `circlePane` again after each button is clicked.

15.16 What methods do you use to register handlers for key pressed, key released, and key typed events? In which classes are these methods defined? (See Table 15.1)

15.17 What method do you use to get the key character for a key-typed event? What method do you use to get the key code for a key-pressed or key-released event?

15.18 How do you set focus on a node so it can listen for key events?

15.10 Listeners for Observable Objects

You can add a listener to process a value change in an observable object.

An instance of `Observable` is known as an observable object, which contains the `addListener(InvalidationListener listener)` method for adding a listener. The listener class must implement the `InvalidationListener` interface to override the `invalidated(Observable o)` method for handling the value change. Once
the value is changed in the Observable object, the listener is notified by invoking its invalidated(Observable o) method. Every binding property is an instance of Observable. Listing 15.10 gives an example of observing and handling a change in a observable object DoubleProperty object balance.

**LISTING 15.10 ObservablePropertyDemo.java**

```java
import javafx.beans.InvalidationListener;
import javafx.beans.Observable;
import javafx.beans.property.DoubleProperty;
import javafx.beans.property.SimpleDoubleProperty;

public class ObservablePropertyDemo {
    public static void main(String[] args) {
        DoubleProperty balance = new SimpleDoubleProperty();
        balance.addListener(new InvalidationListener() {
            public void invalidated(Observable ov) {
                System.out.println("The new value is "+
                    balance.doubleValue());
            }
        });
        balance.set(4.5);
    }
}
```

The new value is 4.5

When line 16 is executed, it causes a change in balance, which notifies the listener by invoking the listener’s invalidated method.

Note that the anonymous inner class in lines 9–14 can be simplified using a lambda expression as follows:

```java
balance.addListener(ov -> {
    System.out.println("The new value is "+
        balance.doubleValue());
});
```

Recall that in Listing 14.20 DisplayClock.java, the clock pane size is not changed when you resize the window. The problem can be fixed by adding a listener to change the clock pane size and register the listener to the window’s width and height properties, as shown in Listing 15.11.

**LISTING 15.11 DisplayResizableClock.java**

```java
import javafx.application.Application;
import javafx.geometry.Pos;
import javafx.stage.Stage;
import javafx.scene.Scene;
import javafx.scene.control.Label;
import javafx.scene.layout.BorderPane;

public class DisplayResizableClock extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a clock and a label
        ClockPane clock = new ClockPane();
        String timeString = clock.getHour() + ":" + clock.getMinute() + ":" + clock.getSecond();
```
Label lblCurrentTime = new Label(timeString);

// Place clock and label in border pane
BorderPane pane = new BorderPane();
pane.setCenter(clock);
pane.setBottom(lblCurrentTime);
BorderPane.setAlignment(lblCurrentTime, Pos.TOP_CENTER);

// Create a scene and place it in the stage
Scene scene = new Scene(pane, 250, 250);
primaryStage.setTitle("DisplayClock"); // Set the stage title
primaryStage.setScene(scene); // Place the scene in the stage
primaryStage.show(); // Display the stage

pane.widthProperty().addListener(ov ->
    clock.setW(pane.getWidth()));

pane.heightProperty().addListener(ov ->
    clock.setH(pane.getHeight()));

The program is identical to Listing 14.19 except that you added the code in lines 29–35 to register listeners for resizing the clock pane upon a change of the width or height of the scene. The code ensures that the clock pane size is synchronized with the scene size.

What would happen if you replace **pane** with **scene** or **primaryStage** in lines 29 and 33?

### 15.11 Animation

**JavaFX provides the Animation class with the core functionality for all animations.**

Suppose you want to write a program that animates a rising flag, as shown in Figure 15.14. How do you accomplish the task? There are several ways to program this. An effective one is to use the subclasses of the JavaFX **Animation** class, which is the subject of this section.

The abstract **Animation** class provides the core functionalities for animations in JavaFX, as shown in Figure 15.15. Many concrete subclasses of **Animation** are provided in JavaFX. This section introduces **PathTransition**, **FadeTransition** and **Timeline**.
The `autoReverse` is a Boolean property that indicates whether an animation will reverse its direction on the next cycle. The `cycleCount` indicates the number of the cycles for the animation. You can use the constant `Timeline.INDEFINITE` to indicate an indefinite number of cycles. The `rate` defines the speed of the animation. A negative rate value indicates the opposite direction for the animation. The `status` is a read-only property that indicates the status of the animation (`Animation.Status.PAUSED`, `Animation.Status.RUNNING`, and `Animation.Status.STOPPED`). The methods `pause()`, `play()`, and `stop()` pauses, plays, and stops an animation.

### 15.11.1 PathTransition

The `PathTransition` class animates the moves of a node along a path from one end to the other over a given time. `PathTransition` is a subtype of `Animation`. The UML class diagram for the class is shown in Figure 15.16.

The `Duration` class defines a duration of time. It is an immutable class. The class defines constants `INDEFINITE`, `ONE`, `UNKNOWN`, and `ZERO` to represent an indefinite duration, 1 millisecond, unknown, and 0 duration. You can use `new Duration(double millis)` to create
an instance of `Duration`, the `add`, `subtract`, `multiply`, and `divide` methods to perform arithmetic operations, and the `toHours()`, `toMinutes()`, `toSeconds()`, and `toMillis()` to return the number of hours, minutes, seconds, and milliseconds in this duration. You can also use `compareTo` to compare two durations.

The constants `NONE` and `ORTHOGONAL_TO_TANGENT` are defined in `PathTransition.OrientationType`. The latter specifies that the node is kept perpendicular to the path’s tangent along the geometric path.

Listing 15.12 gives an example that moves a rectangle along the outline of a circle, as shown in Figure 15.17a.

### Listing 15.12 PathTransitionDemo.java

```java
import javafx.animation.PathTransition;
import javafx.animation.Timeline;
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Rectangle;
import javafx.scene.shape.Circle;
import javafx.stage.Stage;
import javafx.util.Duration;

public class PathTransitionDemo extends Application {

    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Create a pane
        Pane pane = new Pane();

        // Create a rectangle
        Rectangle rectangle = new Rectangle(0, 0, 25, 50);
        rectangle.setFill(Color.ORANGE);

        // Create a circle
        Circle circle = new Circle(125, 100, 50);
        circle.setFill(Color.WHITE);
        circle.setStroke(Color.BLACK);

        // Add circle and rectangle to the pane
        pane.getChildren().add(circle);
        pane.getChildren().add(rectangle);

        // Create a path transition
        PathTransition pt = new PathTransition();
        pt.setDuration(Duration.millis(4000));
        pt.setPath(circle);
        pt.setNode(rectangle);
        pt.setOrientation(PathTransition.OrientationType.ORTHOGONAL_TO_TANGENT);
        pt.setCycleCount(Timeline.INDEFINITE);
        pt.setAutoReverse(true);
        pt.play(); // Start animation

        circle.setOnMousePressed(e -> pt.pause());
        circle.setOnMouseReleased(e -> pt.play());

        // Create a scene and place it in the stage
        Scene scene = new Scene(pane, 250, 200);
        primaryStage.setTitle("PathTransitionDemo"); // Set the stage title
    }
}
```
The program creates a pane (line 16), a rectangle (line 19), and a circle (line 23). The circle and rectangle are placed in the pane (lines 28 and 29). If the circle was not placed in the pane, you will see the screen shot as shown in Figure 15.17b.

The program creates a path transition (line 32), sets its duration to 4 seconds for one cycle of animation (line 33), sets circle as the path (line 34), sets rectangle as the node (line 35), and sets the orientation to orthogonal to tangent (line 36).

The cycle count is set to indefinite (line 38) so the animation continues forever. The auto reverse is set to true (line 39) so that the direction of the move is reversed in the alternating cycle. The program starts animation by invoking the \texttt{play()} method (line 40).

If the \texttt{pause()} method is replaced by the \texttt{stop()} method in line 42, the animation will start over from the beginning when it restarts.

Listing 15.13 gives the program that animates a flag rising, as shown in Figure 15.14.

\textbf{Listing 15.13} FlagRisingAnimation.java

\begin{verbatim}
import javafx.animation.PathTransition;
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.image.ImageView;
import javafx.scene.layout.Pane;
import javafx.scene.shape.Line;
import javafx.stage.Stage;
import javafx.util.Duration;

public class FlagRisingAnimation extends Application {
    @Override
    public void start(Stage primaryStage) {
        // Create a pane
        Pane pane = new Pane();
        // Add an image view and add it to pane
        ImageView imageView = new ImageView("image/us.gif");
        pane.getChildren().add(imageView);
        // Create a path transition
        PathTransition pt = new PathTransition(Duration.millis(10000),
        // Place the scene in the stage
        primaryStage.setScene(scene);
        // Display the stage
        primaryStage.show();
    }
}
\end{verbatim}
set cycle count
play animation

The program creates a pane (line 14), an image view from an image file (line 17), and places the image view to the page (line 18). A path transition is created with duration of 10 seconds using a line as a path and the image view as the node (lines 21 and 22). The image view will move along the line. Since the line is not placed in the scene, you will not see the line in the window.

The cycle count is set to 5 (line 23) so that the animation is repeated five times.

### 15.11.2 FadeTransition

The `FadeTransition` class animates the change of the opacity in a node over a given time. `FadeTransition` is a subtype of `Animation`. The UML class diagram for the class is shown in Figure 15.18.

Listing 15.14 gives an example that applies a fade transition to the filled color in an ellipse, as shown in Figure 15.19.

**Listing 15.14**  
`FadeTransitionDemo.java`

```java
import javafx.animation.FadeTransition;
import javafx.animation.Timeline;
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Ellipse;
import javafx.stage.Stage;
```

The duration of this transition.
The target node of this transition.
The start opacity for this animation.
The stop opacity for this animation.
The incremental value on the opacity for this animation.

Creates an empty `FadeTransition`.
Creates a `FadeTransition` with the specified duration.
Creates a `FadeTransition` with the specified duration and node.

**Figure 15.18**  
The `FadeTransition` class defines an animation for the change of opacity in a node.

```java
+FadeTransition()
+FadeTransition(duration: Duration)
+FadeTransition(duration: Duration, node: Node)
```
import javafx.util.Duration;

public class FadeTransitionDemo extends Application {
  @Override // Override the start method in the Application class
  public void start(Stage primaryStage) {
    // Place an ellipse to the pane
    Pane pane = new Pane();
    Ellipse ellipse = new Ellipse(10, 10, 100, 50);
    ellipse.setFill(Color.RED);
    ellipse.setStroke(Color.BLACK);
    ellipse.centerXProperty().bind(pane.widthProperty().divide(2));
    ellipse.centerYProperty().bind(pane.heightProperty().divide(2));
    ellipse.radiusXProperty().bind(pane.widthProperty().multiply(0.4));
    ellipse.radiusYProperty().bind(pane.heightProperty().multiply(0.4));
    pane.getChildren().add(ellipse);

    // Apply a fade transition to ellipse
    FadeTransition ft = new FadeTransition(Duration.millis(3000), ellipse);
    ft.setFromValue(1.0);
    ft.setToValue(0.1);
    ft.setCycleCount(Timeline.INDEFINITE);
    ft.setAutoReverse(true);
    ft.play(); // Start animation

    // Control animation
    ellipse.setOnMousePressed(e -> ft.pause());
    ellipse.setOnMouseReleased(e -> ft.play());

    // Create a scene and place it in the stage
    Scene scene = new Scene(pane, 200, 150);
    primaryStage.setTitle("FadeTransitionDemo"); // Set the stage title
    primaryStage.setScene(scene); // Place the scene in the stage
    primaryStage.show(); // Display the stage
  }
}

Figure 15.19 The FadeTransition animates the change of opacity in the ellipse.

The program creates a pane (line 15) and an ellipse (line 16) and places the ellipse into the pane (line 25). The ellipse’s centerX, centerY, radiusX, and radiusY properties are bound to the pane’s size (lines 19–24).

A fade transition is created with a duration of 3 seconds for the ellipse (line 29). It sets the start opaque to 1.0 (line 30) and the stop opaque 0.1 (line 31). The cycle count is set to infinite so the animation is repeated indefinitely (line 32). When the mouse is pressed, the animation is paused (line 37). When the mouse is released, the animation resumes from where it was paused (line 38).
15.11.3 Timeline

PathTransition and FadeTransition define specialized animations. The Timeline class can be used to program any animation using one or more KeyFrames. Each KeyFrame is executed sequentially at a specified time interval. Timeline inherits from Animation. You can construct a Timeline using the constructor new Timeline(KeyFrame... keyframes). A KeyFrame can be constructed using

new KeyFrame(Duration duration, EventHandler<ActionEvent> onFinished)

The handler onFinished is called when the duration for the key frame is elapsed.

Listing 15.15 gives an example that displays a flashing text, as shown in Figure 15.20. The text is on and off alternating to animate flashing.

**Listing 15.15 TimelineDemo.java**

```java
import javafx.animation.Animation;
import javafx.application.Application;
import javafx.stage.Stage;
import javafx.animation.KeyFrame;
import javafx.animation.Timeline;
import javafx.event.ActionEvent;
import javafx.event.EventHandler;
import javafx.scene.Scene;
import javafx.scene.layout.StackPane;
import javafx.scene.paint.Color;
import javafx.scene.text.Text;
import javafx.util.Duration;

public class TimelineDemo extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        StackPane pane = new StackPane();
        Text text = new Text(20, 50, "Programming is fun");
        text.setFill(Color.RED);
        pane.getChildren().add(text); // Place text into the stack pane

        EventHandler<ActionEvent> eventHandler = e -> {
            if (text.getText().length() != 0) {
                text.setText("");
            } else {
                text.setText("Programming is fun");
            }
        };

        Timeline animation = new Timeline(new KeyFrame(Duration.millis(500), eventHandler));
        animation.setCycleCount(Timeline.INDEFINITE);
        animation.play(); // Start animation

        text.setOnMouseClicked(e -> {
            if (animation.getStatus() == Animation.Status.PAUSED) {
                animation.play();
            } else {
                animation.pause();
            }
        });
    }
}
```
// Create a scene and place it in the stage
Scene scene = new Scene(pane, 250, 250);
primaryStage.setTitle("TimelineDemo"); // Set the stage title
primaryStage.setScene(scene); // Place the scene in the stage
primaryStage.show(); // Display the stage

Figure 15.20 The handler is called to set the text to Programming is fun or empty in turn.

The program creates a stack pane (line 17) and a text (line 18) and places the text into the pane (line 20). A handler is created to change the text to empty (lines 24–26) if it is not empty or to Programming is fun if it is empty (lines 27–29). A KeyFrame is created to run an action event in every half second (line 34). A Timeline animation is created to contain a key frame (lines 33 and 34). The animation is set to run indefinitely (line 35).

The mouse clicked event is set for the text (lines 39–46). A mouse click on the text resumes the animation if the animation is paused (lines 40–42), and a mouse click on the text pauses the animation if the animation is running (lines 43–45).

In Section 14.12, Case Study: The ClockPane Class, you drew a clock to show the current time. The clock does not tick after it is displayed. What can you do to make the clock display a new current time every second? The key to making the clock tick is to repaint it every second with a new current time. You can use a Timeline to control the repainting of the clock with the code in Listing 15.16. The sample run of the program is shown in Figure 15.21.

Listing 15.16 ClockAnimation.java

```java
import javafx.application.Application;
import javafx.stage.Stage;
import javafx.animation.KeyFrame;
import javafx.animation.Timeline;
import javafx.event.ActionEvent;
import javafx.event.EventHandler;
import javafx.scene.Scene;
import javafx.util.Duration;

public class ClockAnimation extends Application {
    @Override
    public void start(Stage primaryStage) {
        ClockPane clock = new ClockPane(); // Create a clock
        EventHandler<ActionEvent> eventHandler = e -> {
            clock.setCurrentTime(); // Set a new clock time
            }
        EventHandler<ActionEvent> eventHandler = e -> {
            clock.setCurrentTime(); // Set a new clock time
        }
        Timeline animation = new Timeline(); // Create a time line
    }
```
new KeyFrame(Duration.millis(1000), eventHandler));
animation.setCycleCount(Timeline.INDEFINITE);
animation.play(); // Start animation

// Create a scene and place it in the stage
Scene scene = new Scene(clock, 250, 50);
primaryStage.setTitle("ClockAnimation"); // Set the stage title
primaryStage.setScene(scene); // Place the scene in the stage
primaryStage.show(); // Display the stage

Figure 15.21 A live clock is displayed in the window.

The program creates an instance clock of ClockPane for displaying a clock (line 13). The ClockPane class is defined in Listing 14.21. The clock is placed in the scene in line 27. An event handler is created for setting the current time in the clock (lines 16–18). This handler is called every second in the key frame in the time line animation (lines 21–24). So the clock time is updated every second in the animation.

15.20 How do you set the cycle count of an animation to infinite? How do you auto reverse an animation? How do you start, pause, and stop an animation?

15.21 Are PathTransition, FadeTransition, and Timeline a subtype of Animation?
15.22 How do you create a PathTransition? How do you create a FadeTransition? How do you create a Timeline?
15.23 How do you create a KeyFrame?

15.12 Case Study: Bouncing Ball

This section presents an animation that displays a ball bouncing in a pane.

The program uses Timeline to animation ball bouncing, as shown in Figure 15.22.

Figure 15.22 A ball is bouncing in a pane.
Here are the major steps to write this program:

1. Define a subclass of Pane named BallPane to display a ball bouncing, as shown in Listing 15.17.

2. Define a subclass of Application named BounceBallControl to control the bouncing ball with mouse actions, as shown in Listing 15.18. The animation pauses when the mouse is pressed and resumes when the mouse is released. Pressing the UP and DOWN arrow keys increases/decreases animation speed.

The relationship among these classes is shown in Figure 15.23.

**LISTING 15.17  BallPane.java**

```java
import javafx.animation.KeyFrame;
import javafx.animation.Timeline;
import javafx.beans.property.DoubleProperty;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Circle;
import javafx.util.Duration;

public class BallPane extends Pane {
    public final double radius = 20;
    private double x = radius, y = radius;
    private double dx = 1, dy = 1;
    private Circle circle = new Circle(x, y, radius);
    private Timeline animation;

    public BallPane() {
        circle.setFill(Color.GREEN); // Set ball color
        getChildren().add(circle); // Place a ball into this pane
    }
}
```
// Create an animation for moving the ball
animation = new Timeline(
    new KeyFrame(Duration.millis(50), e -> moveBall()));

animation.setCycleCount(Timeline.INDEFINITE);
animation.play(); // Start animation

public void play() {
    animation.play();
}

public void pause() {
    animation.pause();
}

public void increaseSpeed() {
    animation.setRate(animation.getRate() + 0.1);
}

decrease animation rate
public void decreaseSpeed() {
    animation.setRate(
        animation.getRate() > 0 ? animation.getRate() - 0.1 : 0);
}

protected DoubleProperty rateProperty() {
    return animation.rateProperty();
}

protected void moveBall() {
    // Check boundaries
    if (x < radius || x > getWidth() - radius) {
        dx *= -1; // Change ball move direction
    }

    if (y < radius || y > getHeight() - radius) {
        dy *= -1; // Change ball move direction
    }

    // Adjust ball position
    x += dx;
y += dy;
circle.setCenterX(x);
circle.setCenterY(y);
}

BallPane extends Pane to display a moving ball (line 9). An instance of Timeline is created to control animation (lines 21 and 22). This instance contains a KeyFrame object that invokes the moveBall() method at a fixed rate. The moveBall() method moves the ball to simulate animation. The center of the ball is at \((x, y)\), which changes to \((x + dx, y + dy)\) on the next move (lines 58–61). When the ball is out of the horizontal boundary, the sign of \(dx\) is changed (from positive to negative or vice versa) (lines 50–52). This causes the ball to change its horizontal movement direction. When the ball is out of the vertical boundary, the sign of \(dy\) is changed (from positive to negative or vice versa) (lines 53–55). This causes the ball to change its vertical movement direction. The pause and play methods (lines 27–33) can be used to pause and resume the animation. The increaseSpeed() and decreaseSpeed() methods (lines 35–42) can be used to increase and decrease animation speed. The rateProperty()
method (lines 44–46) returns a binding property value for rate. This binding property is useful for binding the rate in future applications in the next chapter.

### Listing 15.18 BounceBallControl.java

```java
import javafx.application.Application;
import javafx.stage.Stage;
import javafx.scene.Scene;
import javafx.scene.input.KeyCode;

public class BounceBallControl extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        BallPane ballPane = new BallPane(); // Create a ball pane
        ballPane.setOnMousePressed(e -> ballPane.pause()); // Pause and resume animation
        ballPane.setOnMouseReleased(e -> ballPane.play());
        ballPane.setOnKeyPressed(e -> {
            if (e.getCode() == KeyCode.UP) {
                ballPane.increaseSpeed();
            } else if (e.getCode() == KeyCode.DOWN) {
                ballPane.decreaseSpeed();
            }
        });

        Scene scene = new Scene(ballPane, 250, 150);
        primaryStage.setTitle("BounceBallControl"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
        ballPane.requestFocus(); // Must request focus after the primary stage is displayed
    }
}
```

The BounceBallControl class is the main JavaFX class that extends Application to display the ball pane with control functions. The mouse-pressed and mouse-released handlers are implemented for the ball pane to pause the animation and resume the animation (lines 12 and 13). When the UP arrow key is pressed, the ball pane’s increaseSpeed() method is invoked to increase the ball’s movement (line 18). When the DOWN arrow key is pressed, the ball pane’s decreaseSpeed() method is invoked to reduce the ball’s movement (line 21).

Invoking ballPane.requestFocus() in line 32 sets the input focus to ballPane.

15.24 How does the program make the ball moving?
15.25 How does the code in Listing 15.17 BallPane.java change the direction of the ball movement?
15.26 What does the program do when the mouse is pressed on the ball pane? What does the program do when the mouse is released on the ball pane?
15.27 If line 32 in Listing 15.18 BounceBallControl.java is not in the program, what would happen when you press the UP or the DOWN arrow key?
15.28 If line 23 is not in Listing 15.17, what would happen?
**Key Terms**

- anonymous inner class 594
- event 588
- event-driven programming 588
- event handler 589
- event-handler interface 589
- event object 588
- event source object 588
- functional interface 598
- lambda expression 597
- inner class 591
- key code 604
- observable object 607
- single abstract method interface 598

**Chapter Summary**

1. The root class of the JavaFX event classes is `javafx.event.Event`, which is a subclass of `java.util.EventObject`. The subclasses of `Event` deal with special types of events, such as action events, window events, mouse events, and key events. If a node can fire an event, any subclass of the node can fire the same type of event.

2. The handler object’s class must implement the corresponding `event-handler interface`. JavaFX provides a handler interface `EventHandler<T extends Event>` for every event class `T`. The handler interface contains the `handle(T e)` method for handling event `e`.

3. The handler object must be registered by the `source object`. Registration methods depend on the event type. For an action event, the method is `setOnAction`. For a mouse-pressed event, the method is `setOnMousePressed`. For a key-pressed event, the method is `setOnKeyPressed`.

4. An `inner class`, or `nested class`, is defined within the scope of another class. An inner class can reference the data and methods defined in the outer class in which it nests, so you need not pass the reference of the outer class to the constructor of the inner class.

5. An anonymous inner class can be used to shorten the code for event handling. Furthermore, a lambda expression can be used to greatly simplify the event-handling code for functional interface handlers.

6. A `functional interface` is an interface with exactly one abstract method. This is also known as a single abstract method (SAM) interface.

7. A `MouseEvent` is fired whenever a mouse button is pressed, released, clicked, moved, or dragged on a node or a scene. The `getButton()` method can be used to detect which mouse button is pressed for the event.

8. A `KeyEvent` is fired whenever a key is pressed, released, or typed on a node or a scene. The `getCode()` method can be used to return the code value for the key.

9. An instance of `Observable` is known as an observable object, which contains the `addListener(InvalidationListener listener)` method for adding a listener. Once the value is changed in the property, a listener is notified. The listener class should implement the `InvalidationListener` interface, which uses the `invalidated` method to handle the property value change.

10. The abstract `Animation` class provides the core functionalities for animations in JavaFX. `PathTransition`, `FadeTransition`, and `Timeline` are specialized classes for implementing animations.
Quiz

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

Programming Exercises

Sections 15.2–15.7

*15.1 (Pick four cards) Write a program that lets the user click the Refresh button to display four cards from a deck of 52 cards, as shown in Figure 15.24a. (See the hint in Programming Exercise 14.3 on how to obtain four random cards.)

Figure 15.24 (a) Exercise 15.1 displays four cards randomly. (b) Exercise 15.2 rotates the rectangle. (c) Exercise 15.3 uses the buttons to move the ball.

15.2 (Rotate a rectangle) Write a program that rotates a rectangle 15 degrees right when the Rotate button is clicked, as shown in Figure 15.24b.

*15.3 (Move the ball) Write a program that moves the ball in a pane. You should define a pane class for displaying the ball and provide the methods for moving the ball left, right, up, and down, as shown in Figure 15.24c. Check the boundary to prevent the ball from moving out of sight completely.

*15.4 (Create a simple calculator) Write a program to perform addition, subtraction, multiplication, and division, as shown in Figure 15.25a.

Figure 15.25 (a) Exercise 15.4 performs addition, subtraction, multiplication, and division on double numbers. (b) The user enters the investment amount, years, and interest rate to compute future value.

*15.5 (Create an investment-value calculator) Write a program that calculates the future value of an investment at a given interest rate for a specified number of years. The formula for the calculation is:

\[
\text{futureValue} = \text{investmentAmount} \times (1 + \text{monthlyInterestRate})^{\text{years} \times 12}
\]
Use text fields for the investment amount, number of years, and annual interest rate. Display the future amount in a text field when the user clicks the *Calculate* button, as shown in Figure 15.25b.

**Sections 15.8 and 15.9**

**15.6** *(Alternate two messages)* Write a program to display the text *Java is fun* and *Java is powerful* alternately with a mouse click.

**15.7** *(Change color using a mouse)* Write a program that displays the color of a circle as black when the mouse button is pressed and as white when the mouse button is released.

**15.8** *(Display the mouse position)* Write two programs, such that one displays the mouse position when the mouse button is clicked (see Figure 15.26a) and the other displays the mouse position when the mouse button is pressed and ceases to display it when the mouse button is released.

![Figure 15.26](image)

*(a)* Exercise 15.8 displays the mouse position. *(b)* Exercise 15.9 uses the arrow keys to draw the lines.

**15.9** *(Draw lines using the arrow keys)* Write a program that draws line segments using the arrow keys. The line starts from the center of the pane and draws toward east, north, west, or south when the right-arrow key, up-arrow key, left-arrow key, or down-arrow key is pressed, as shown in Figure 15.26b.

**15.10** *(Enter and display a string)* Write a program that receives a string from the keyboard and displays it on a pane. The *Enter* key signals the end of a string. Whenever a new string is entered, it is displayed on the pane.

**15.11** *(Move a circle using keys)* Write a program that moves a circle up, down, left, or right using the arrow keys.

**15.12** *(Geometry: inside a circle?)* Write a program that draws a fixed circle centered at *(100, 60)* with radius 50. Whenever the mouse is moved, display a message indicating whether the mouse point is inside the circle at the mouse point or outside of it, as shown in Figure 15.27a.

![Figure 15.27](image)

Detect whether a point is inside a circle, a rectangle, or a polygon.
**15.13 (Geometry: inside a rectangle?)** Write a program that draws a fixed rectangle centered at \((100, 60)\) with width \(100\) and height \(40\). Whenever the mouse is moved, display a message indicating whether the mouse point is inside the rectangle at the mouse point or outside of it, as shown in Figure 15.27b. To detect whether a point is inside a polygon, use the `contains` method defined in the `Node` class.

**15.14 (Geometry: inside a polygon?)** Write a program that draws a fixed polygon with points at \((40, 20)\), \((70, 40)\), \((60, 80)\), \((45, 45)\), and \((20, 60)\). Whenever the mouse is moved, display a message indicating whether the mouse point is inside the polygon at the mouse point or outside of it, as shown in Figure 15.27c. To detect whether a point is inside a polygon, use the `contains` method defined in the `Node` class.

**15.15 (Geometry: add and remove points)** Write a program that lets the user click on a pane to dynamically create and remove points (see Figure 15.28a). When the user left-clicks the mouse (primary button), a point is created and displayed at the mouse point. The user can remove a point by pointing to it and right-clicking the mouse (secondary button).

**15.16 (Two movable vertices and their distances)** Write a program that displays two circles with radius \(10\) at location \((40, 40)\) and \((120, 150)\) with a line connecting the two circles, as shown in Figure 15.28b. The distance between the circles is displayed along the line. The user can drag a circle. When that happens, the circle and its line are moved and the distance between the circles is updated.

**15.17 (Geometry: find the bounding rectangle)** Write a program that enables the user to add and remove points in a two-dimensional plane dynamically, as shown in Figure 15.29a. A minimum bounding rectangle is updated as the points are added and removed. Assume that the radius of each point is \(10\) pixels.
**15.18** *(Move a rectangle using mouse)* Write a program that displays a rectangle. You can point the mouse inside the rectangle and drag (i.e., move with mouse pressed) the rectangle wherever the mouse goes. The mouse point becomes the center of the rectangle.

**15.19** *(Game: eye-hand coordination)* Write a program that displays a circle of radius 10 pixels filled with a random color at a random location on a pane, as shown in Figure 15.29b. When you click the circle, it disappears and a new random-color circle is displayed at another random location. After twenty circles are clicked, display the time spent in the pane, as shown in Figure 15.29c.

**15.20** *(Geometry: display angles)* Write a program that enables the user to drag the vertices of a triangle and displays the angles dynamically as the triangle shape changes, as shown in Figure 15.30a. The formula to compute angles is given in Listing 4.1.

![Figure 15.30](image)

(a) Exercise 15.20 enables the user to drag vertices and display the angles dynamically. (b) Exercise 15.21 enables the user to drag vertices along the circle and display the angles in the triangle dynamically.

**15.21** *(Drag points)* Draw a circle with three random points on the circle. Connect the points to form a triangle. Display the angles in the triangle. Use the mouse to drag a point along the perimeter of the circle. As you drag it, the triangle and angles are redisplayed dynamically, as shown in Figure 15.30b. For computing angles in a triangle, see Listing 4.1.

**Section 15.10**

**15.22** *(Auto resize cylinder)* Rewrite Programming Exercise 14.10 so that the cylinder’s width and height are automatically resized when the window is resized.

**15.23** *(Auto resize stop sign)* Rewrite Programming Exercise 14.15 so that the stop sign’s width and height are automatically resized when the window is resized.

**Section 15.11**

**15.24** *(Animation: palindrome)* Write a program that animates a palindrome swing as shown in Figure 15.31. Press/release the mouse to pause/resume the animation.

![Figure 15.31](image)

The program animates a palindrome swing.
15.25 (Animation: ball on curve) Write a program that animates a ball moving along a sine curve, as shown in Figure 15.32. When the ball gets to the right border, it starts over from the left. Enable the user to resume/pause the animation with a click on the left/right mouse button.

![Figure 15.32](image)

The program animates a ball traveling along a sine curve.

15.26 (Change opacity) Rewrite Programming Exercise 15.24 so that the ball’s opacity is changed as it swings.

15.27 (Control a moving text) Write a program that displays a moving text, as shown in Figure 15.33a and b. The text moves from left to right circularly. When it disappears in the right, it reappears from the left. The text freezes when the mouse is pressed and moves again when the button is released.

![Figure 15.33](image)

(a and b) A text is moving from left to right circularly. (c) The program simulates a fan running.

15.28 (Display a running fan) Write a program that displays a running fan, as shown in Figure 15.33c. Use the Pause, Resume, Reverse buttons to pause, resume, and reverse fan running.

15.29 (Racing car) Write a program that simulates car racing, as shown in Figure 15.34a. The car moves from left to right. When it hits the right end, it restarts from the left and continues the same process. You can use a timer to control animation. Redraw the car with a new base coordinates \((x, y)\), as shown in Figure 15.34b. Also let the user pause/resume the animation with a button press/release and increase/decrease the car speed by pressing the UP and DOWN arrow keys.

15.30 (Slide show) Twenty-five slides are stored as image files (slide0.jpg, slide1.jpg, . . . , slide24.jpg) in the image directory downloadable along with the source code in the book. The size of each image is 800 \(\times\) 600. Write a program that automatically displays the slides repeatedly. Each slide is shown for
two seconds. The slides are displayed in order. When the last slide finishes, the first slide is redisplayed, and so on. Click to pause if the animation is currently playing. Click to resume if the animation is currently paused.

**15.31** (Geometry: pendulum) Write a program that animates a pendulum swinging, as shown in Figure 15.35. Press the UP arrow key to increase the speed and the DOWN key to decrease it. Press the S key to stop animation and the R key to resume it.

![Image of pendulum animation](image)

**Figure 15.35** Exercise 15.31 animates a pendulum swinging.

---

*15.32* (Control a clock) Modify Listing 14.21, ClockPane.java, to add the animation into this class and add two methods `start()` and `stop()` to start and stop the clock. Write a program that lets the user control the clock with the Start and Stop buttons, as shown in Figure 15.36a.

![Image of clock control](image)

**Figure 15.36** (a) Exercise 15.32 allows the user to start and stop a clock. (b and c) The balls are dropped into the bean machine.
***15.33  (Game: bean-machine animation) Write a program that animates the bean machine introduced in Programming Exercise 7.21. The animation terminates after ten balls are dropped, as shown in Figure 15.36b and c.

***15.34  (Simulation: self-avoiding random walk) A self-avoiding walk in a lattice is a path from one point to another that does not visit the same point twice. Self-avoiding walks have applications in physics, chemistry, and mathematics. They can be used to model chain-like entities such as solvents and polymers. Write a program that displays a random path that starts from the center and ends at a point on the boundary, as shown in Figure 15.37 or ends at a dead-end point (i.e., surrounded by four points that have already been visited), as shown in Figure 15.37b. Assume the size of the lattice is 16 by 16.

***15.35  (Animation: self-avoiding random walk) Revise the preceding exercise to display the walk step by step in an animation, as shown in Figure 15.37c and d.

***15.36  (Simulation: self-avoiding random walk) Write a simulation program to show that the chance of getting dead-end paths increases as the grid size increases. Your program simulates lattices with size from 10 to 80. For each lattice size, simulate a self-avoiding random walk 10,000 times and display the probability of the dead-end paths, as shown in the following sample output:

```
For a lattice of size 10, the probability of dead-end paths is 10.6%
For a lattice of size 11, the probability of dead-end paths is 14.0%
...
For a lattice of size 80, the probability of dead-end paths is 99.5%
```
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Objectives

- To create graphical user interfaces with various user-interface controls (§§16.2–16.11).
- To create a label with text and graphic using the Label class and explore properties in the abstract Labeled class (§16.2).
- To create a button with text and graphic using the Button class and set a handler using the setOnAction method in the abstract ButtonBase class (§16.3).
- To create a check box using the CheckBox class (§16.4).
- To create a radio button using the RadioButton class and group radio buttons using a ToggleGroup (§16.5).
- To enter data using the TextField class and password using the PasswordField class (§16.6).
- To enter data in multiple lines using the TextArea class (§16.7).
- To select a single item using ComboBox (§16.8).
- To select a single or multiple items using ListView (§16.9).
- To select a range of values using ScrollBar (§16.10).
- To select a range of values using Slider and explore differences between ScrollBar and Slider (§16.11).
- To develop a tic-tac-toe game (§16.12).
- To view and play video and audio using the Media, MediaPlayer, and MediaView (§16.13).
- To develop a case study for showing the national flag and playing anthem (§16.14).
16.1 Introduction

JavaFX provides many UI controls for developing a comprehensive user interface.

A graphical user interface (GUI) makes a system user-friendly and easy to use. Creating a GUI requires creativity and knowledge of how UI controls work. Since the UI controls in JavaFX are very flexible and versatile, you can create a wide assortment of useful user interfaces for rich Internet applications.

Oracle provides tools for visually designing and developing GUIs. This enables the programmer to rapidly assemble the elements of a GUI with minimum coding. Tools, however, cannot do everything. You have to modify the programs they produce. Consequently, before you begin to use the visual tools, you must understand the basic concepts of JavaFX GUI programming.

Previous chapters used UI controls such as Button, Label, and TextField. This chapter introduces the frequently used UI controls in detail (see Figure 16.1).

![Figure 16.1 These UI controls are frequently used to create user interfaces.](image)

**Figure 16.1** These UI controls are frequently used to create user interfaces.

**Note** Throughout this book, the prefixes **lbl**, **bt**, **chk**, **rb**, **tf**, **pf**, **ta**, **cbo**, **lv**, **scb**, **sld**, and **mp** are used to name reference variables for Label, Button, CheckBox, RadioButton, TextField, PasswordField, TextArea, ComboBox, ListView, ScrollBar, Slider, and MediaPlayer.

16.2 Labeled and Label

A label is a display area for a short text, a node, or both. It is often used to label other controls (usually text fields). Labels and buttons share many common properties. These common properties are defined in the **Labeled** class, as shown in Figure 16.2.

A **Label** can be constructed using one of the three constructors as shown in Figure 16.3.

The **graphic** property can be any node such as a shape, an image, or a control. Listing 16.1 gives an example that displays several labels with text and images in the label, as shown in Figure 16.4.

**Listing 16.1** **LabelWithGraphic.java**

```java
import javafx.application.Application;
import javafx.stage.Stage;
import javafx.scene.Scene;
import javafx.scene.control.ContentDisplay;
import javafx.scene.control.Label;
```

![Diagram](image)
import javafx.scene.image.Image;
import javafx.scene.image.ImageView;
import javafx.scene.layout.HBox;
import javafx.scene.layout.StackPane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Circle;
import javafx.scene.shape.Rectangle;
import javafx.scene.shape.Ellipse;

public class LabelWithGraphic extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        ImageView us = new ImageView(new Image("image/us.gif"));
        Label lb1 = new Label("US
50 States", us);
        lb1.setStyle("-fx-border-color: green; -fx-border-width: 2");
        lb1.setContentDisplay(ContentDisplay.BOTTOM);
        lb1.setTextFill(Color.RED);

        Label lb2 = new Label("Circle", new Circle(50, 50, 25));
        lb2.setContentDisplay(ContentDisplay.TOP);
        lb2.setTextFill(Color.ORANGE);

        Label lb3 = new Label("Rectangle", new Rectangle(10, 10, 50, 25));
        lb3.setContentDisplay(ContentDisplay.RIGHT);

        Label lb4 = new Label("Ellipse", new Ellipse(50, 50, 50, 25));
        lb4.setContentDisplay(ContentDisplay.LEFT);
    }
}

FIGURE 16.2 Labeled defines common properties for Label, Button, CheckBox, and RadioButton.

javafx.scene.control.Labeled
-alignment: ObjectProperty<Pos>
-contentDisplay: ObjectProperty<ContentDisplay>
-graphic: ObjectProperty<Node>
-graphicTextGap: DoubleProperty
-textFill: ObjectProperty<Paint>
-text: StringProperty
-underline: BooleanProperty
-wrapText: BooleanProperty

The getter and setter methods for property values and a getter for property itself are provided in the class, but omitted in the UML diagram for brevity.

Specifies the alignment of the text and node in the labeled.
Specifies the position of the node relative to the text using the constants TOP, BOTTOM, LEFT, and RIGHT defined in ContentDisplay.
A graphic for the labeled.
The gap between the graphic and the text.
The paint used to fill the text.
A text for the labeled.
Whether text should be underlined.
Whether text should be wrapped if the text exceeds the width.

FIGURE 16.3 Label is created to display a text or a node, or both.

javafx.scene.control.Labeled
+Label()
+Label(text: String)
+Label(text: String, graphic: Node)

Creates an empty label.
Creates a label with the specified text.
Creates a label with the specified text and graphic.
Ellipse ellipse = new Ellipse(50, 50, 50, 25);
ellipse.setStroke(Color.GREEN);
ellipse.setFill(Color.WHITE);
StackPane stackPane = new StackPane();
stackPane.getChildren().addAll(ellipse, new Label("JavaFX");
Label lb5 = new Label("A pane inside a label", stackPane);
lb5.setContentDisplay(ContentDisplay.BOTTOM);
HBox pane = new HBox(20);
pane.getChildren().addAll(lb1, lb2, lb3, lb4, lb5);
// Create a scene and place it in the stage
Scene scene = new Scene(pane, 450, 150);
primaryStage.setTitle("LabelWithGraphic"); // Set the stage title
primaryStage.setScene(scene); // Place the scene in the stage
primaryStage.show(); // Display the stage
}

create a label
add labels to pane

Figure 16.4 The program displays labels with texts and nodes.

The program creates a label with a text and an image (line 19). The text is US\n50 States so it is displayed in two lines. Line 21 specifies that the image is placed at the bottom of the text.

The program creates a label with a text and a circle (line 24). The circle is placed on top of the text (line 25). The program creates a label with a text and a rectangle (line 28). The rectangle is placed on the right of the text (line 29). The program creates a label with a text and an ellipse (line 31). The ellipse is placed on the left of the text (line 32).

The program creates an ellipse (line 34), places it along with a label to a stack pane (line 38), and creates a label with a text and the stack pane as the node (line 39). As seen from this example, you can place any node in a label.

The program creates an HBox (line 42) and places all five labels into the HBox (line 43).

16.1 How do you create a label with a node without a text?
16.2 How do you place a text on the right of the node in a label?
16.3 Can you display multiple lines of text in a label?
16.4 Can the text in a label be underlined?

16.3 Button

A button is a control that triggers an action event when clicked. JavaFX provides regular buttons, toggle buttons, check box buttons, and radio buttons. The common features of these buttons are defined in ButtonBase and Labeled classes as shown in Figure 16.5.

The Labeled class defines the common properties for labels and buttons. A button is just like a label except that the button has the onAction property defined in the ButtonBase class, which sets a handler for handling a button’s action.
Listing 16.2 gives a program that uses the buttons to control the movement of a text, as shown in Figure 16.6.

LISTING 16.2 ButtonDemo.java

```java
import javafx.application.Application;
import javafx.stage.Stage;
import javafx.geometry.Pos;
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.scene.image.ImageView;
import javafx.scene.layout.BorderPane;
import javafx.scene.layout.HBox;
import javafx.scene.text.Text;

public class ButtonDemo extends Application {
    protected Text text = new Text(50, 50, "JavaFX Programming");

    protected BorderPane getPane() {
        HBox paneForButtons = new HBox(20);
        Button btLeft = new Button("Left", new ImageView("image/left.gif"));
        Button btRight = new Button("Right", new ImageView("image/right.gif"));
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().addAll(btLeft, btRight);
        paneForButtons.setAlignment(Pos.CENTER);
        paneForButtons.setStyle("-fx-border-color: green");
        paneForButtons.getChildren().add(text);

        return pane;
    }
}
```

FIGURE 16.5 ButtonBase extends Labeled and defines common features for all buttons.
36   }
37  
38  @Override // Override the start method in the Application class
39  public void start(Stage primaryStage) {
40    // Create a scene and place it in the stage
41      Scene scene = new Scene(getPane(), 450, 200);
42      primaryStage.setTitle("ButtonDemo"); // Set the stage title
43      primaryStage.setScene(scene); // Place the scene in the stage
44      primaryStage.show(); // Display the stage
45  }
46  }

FIGURE 16.6 The program demonstrates using buttons.

set pane to scene

The program creates two buttons btLeft and btRight with each button containing a text and an image (lines 17–20). The buttons are placed in an HBox (line 21) and the HBox is placed in the bottom of a border pane (line 26). A text is created in line 13 and is placed in the center of the border pane (line 30). The action handler for btLeft moves the text to the left (line 32). The action handler for btRight moves the text to the right (line 33).

The program purposely defines a protected getPane() method to return a pane (line 15). This method will be overridden by subclasses in the upcoming examples to add more nodes in the pane. The text is declared protected so that it can be accessed by subclasses (line 13).

getPane() protected

16.5 How do you create a button with a text and a node? Can you apply all the methods for Labeled to Button?

16.6 Why is the getPane() method protected in Listing 16.2? Why is the data field text protected?

16.7 How do you set a handler for processing a button-clicked action?

16.4 CheckBox

A CheckBox is used for the user to make a selection. Like Button, CheckBox inherits all the properties such as onAction, text, graphic, alignment, graphicTextGap, textFill, contentDisplay from ButtonBase and Labeled, as shown in Figure 16.7. Additionally, it provides the selection property to indicate whether a check box is selected.

Here is an example of a check box with text US, a graphic image, green text color, and black border, and initially selected.

CheckBox chkUS = new CheckBox("US");
chkUS.setGraphic(new ImageView("image/usIcon.gif"));
chkUS.setTextFill(Color.GREEN);
chkUS.setContentDisplay(ContentDisplay.LEFT);
chkUS.setStyle("-fx-border-color: black");
chkUS.setSelected(true);
chkUS.setPadding(new Insets(5, 5, 5, 5));

✓ Point

✓ Check
When a check box is clicked (checked or unchecked), it fires an ActionEvent. To see if a check box is selected, use the isSelected() method.

We now write a program that adds two check boxes named Bold and Italic to the preceding example to let the user specify whether the message is in bold or italic, as shown in Figure 16.8.

When a check box is clicked (checked or unchecked), it fires an ActionEvent. To see if a check box is selected, use the isSelected() method.

There are at least two approaches to writing this program. The first is to revise the preceding ButtonDemo class to insert the code for adding the check boxes and processing their events. The second is to define a subclass that extends ButtonDemo. Please implement the first approach as an exercise. Listing 16.3 gives the code to implement the second approach.

**LISTING 16.3 CheckBoxDemo.java**

```java
import javafx.event.ActionEvent;
import javafx.event.EventHandler;
import javafx.geometry.Insets;
import javafx.scene.control.CheckBox;
import javafx.scene.layout.BorderPane;
import javafx.scene.layout.VBox;
import javafx.scene.text.Font;
import javafx.scene.text.FontPosture;
import javafx.scene.text.FontWeight;

public class CheckBoxDemo extends ButtonDemo {
    @Override
    protected BorderPane getPane() {
        BorderPane pane = super.getPane();
    }
}
```
Font fontBoldItalic = Font.font("Times New Roman", FontWeight.BOLD, FontPosture.ITALIC, 20);
Font fontBold = Font.font("Times New Roman", FontWeight.BOLD, FontPosture.REGULAR, 20);
Font fontItalic = Font.font("Times New Roman", FontWeight.NORMAL, FontPosture.ITALIC, 20);
Font fontNormal = Font.font("Times New Roman", FontWeight.NORMAL, FontPosture.REGULAR, 20);
text.setFont(fontNormal);

VBox paneForCheckBoxes = new VBox(20);
paneForCheckBoxes.setPadding(new Insets(5, 5, 5, 5));
paneForCheckBoxes.setStyle("-fx-border-color: green");

CheckBox chkBold = new CheckBox("Bold");
CheckBox chkItalic = new CheckBox("Italic");
paneForCheckBoxes.getChildren().addAll(chkBold, chkItalic);
pane.setRight(paneForCheckBoxes);

EventHandler<ActionEvent> handler = e -> {
  if (chkBold.isSelected() && chkItalic.isSelected()) {
    text.setFont(fontBoldItalic); // Both check boxes checked
  } else if (chkBold.isSelected()) {
    text.setFont(fontBold); // The Bold check box checked
  } else if (chkItalic.isSelected()) {
    text.setFont(fontItalic); // The Italic check box checked
  } else {
    text.setFont(fontNormal); // Both check boxes unchecked
  }
};
chkBold.setOnAction(handler);
chkItalic.setOnAction(handler);

return pane; // Return a new pane

CheckBoxDemo extends ButtonDemo and overrides the getPane() method (line 13). The new getPane() method invokes the super.getPane() method from the ButtonDemo class to obtain a border pane that contains the buttons and a text (line 14). The check boxes are created and added to paneForCheckBoxes (lines 30–32). paneForCheckBoxes is added to the border pane (lines 33).

The handler for processing the action event on check boxes is created in lines 35–48. It sets the appropriate font based on the status of the check boxes.

The start method for this JavaFX program is defined in ButtonDemo and inherited in CheckBoxDemo. So when you run CheckBoxDemo, the start method in ButtonDemo is invoked. Since the getPane() method is overridden in CheckBoxDemo, the method in CheckBoxDemo is invoked from line 41 in Listing 16.2, ButtonDemo.java.

16.8 How do you test if a check box is selected?
16.9 Can you apply all the methods for Labeled to CheckBox?
16.10 Can you set a node for the graphic property in a check box?
16.5 RadioButton

Radio buttons, also known as option buttons, enable the user to choose a single item from a group of choices. In appearance radio buttons resemble check boxes, but check boxes display a square that is either checked or blank, whereas radio buttons display a circle that is either filled (if selected) or blank (if not selected).

RadioButton is a subclass of ToggleButton. The difference between a radio button and a toggle button is that a radio button displays a circle, but a toggle button is rendered similar to a button. The UML diagrams for ToggleButton and RadioButton are shown in Figure 16.9.

The getter and setter methods for property values and a getter for property itself are provided in the class, but omitted in the UML diagram for brevity.

The getter and setter methods for property values and a getter for property itself are provided in the class, but omitted in the UML diagram for brevity.

Here is an example of a radio button with text US, a graphic image, green text color, and black border, and initially selected.

```java
RadioButton rbUS = new RadioButton("US");
rbUS.setGraphic(new ImageView("image/usIcon.gif"));
rbUS.setTextFill(Color.GREEN);
rbUS.setContentType(ContentType.BORDERED);
rbUS.setStyle("-fx-border-color: black");
rbUS.setSelected(true);
rbUS.setPadding(new Insets(5, 5, 5, 5));
```

To group radio buttons, you need to create an instance of ToggleGroup and set a radio button’s toggleGroup property to join the group, as follows:

```java
ToggleButton group = new ToggleGroup();
rRed.setToggleGroup(group);
rGreen.setToggleGroup(group);
rBlue.setToggleGroup(group);
```

This code creates a button group for radio buttons rRed, rGreen, and rBlue so that buttons rRed, rGreen, and rBlue are selected mutually exclusively. Without grouping, these buttons would be independent.

When a radio button is changed (selected or deselected), it fires an ActionEvent. To see if a radio button is selected, use the isSelected() method.
We now give a program that adds three radio buttons named Red, Green, and Blue to the preceding example to let the user choose the color of the message, as shown in Figure 16.10.

Figure 16.10 The program demonstrates using radio buttons.

Again there are at least two approaches to writing this program. The first is to revise the preceding CheckBoxDemo class to insert the code for adding the radio buttons and processing their events. The second is to define a subclass that extends CheckBoxDemo. Listing 16.4 gives the code to implement the second approach.

Listing 16.4 RadioButtonDemo.java

```java
import javafx.geometry.Insets;
import javafx.scene.control.RadioButton;
import javafx.scene.control.ToggleGroup;
import javafx.scene.layout.BorderPane;
import javafx.scene.layout.VBox;
import javafx.scene.paint.Color;

public class RadioButtonDemo extends CheckBoxDemo {
    @Override
    protected BorderPane getPane() {
        BorderPane pane = super.getPane();

        VBox paneForRadioButtons = new VBox(20);
        paneForRadioButtons.setPadding(new Insets(5, 5, 5, 5));
        paneForRadioButtons.setStyle("-fx-border-color: green");
        paneForRadioButtons.setStyle("-fx-border-width: 2px; -fx-border-color: green");

        RadioButton rbRed = new RadioButton("Red");
        RadioButton rbGreen = new RadioButton("Green");
        RadioButton rbBlue = new RadioButton("Blue");

        paneForRadioButtons.getChildren().addAll(rbRed, rbGreen, rbBlue);
        pane.setLeft(paneForRadioButtons);

        ToggleGroup group = new ToggleGroup();
        rbRed.setToggleGroup(group);
        rbGreen.setToggleGroup(group);
        rbBlue.setToggleGroup(group);

        rbRed.setOnAction(e -> {
            if (rbRed.isSelected()) {
                text.setFill(Color.RED);
            }
        });

        rbGreen.setOnAction(e -> {
            if (rbGreen.isSelected()) {
                text.setFill(Color.GREEN);
            }
        });
        return pane;
    }
}
```
RadioButtonDemo extends CheckBoxDemo and overrides the getPane() method (line 10). The new getPane() method invokes the getPane() method from the CheckBoxDemo class to create a border pane that contains the check boxes, buttons, and a text (line 11). This border pane is returned from invoking super.getPane(). The radio buttons are created and added to paneForRadioButtons (lines 18–21). paneForRadioButtons is added to the border pane (lines 22).

The radio buttons are grouped together in lines 24–27. The handlers for processing the action event on radio buttons are created in lines 29–45. It sets the appropriate color based on the status of the radio buttons.

The start method for this JavaFX program is defined in ButtonDemo and inherited in CheckBoxDemo and then in RadioButtonDemo. So when you run RadioButtonDemo, the start method in ButtonDemo is invoked. Since the getPane() method is overridden in RadioButtonDemo, the method in RadioButtonDemo is invoked from line 41 in Listing 16.2, ButtonDemo.java.

16.11 How do you test if a radio button is selected?
16.12 Can you apply all the methods for Labeled to RadioButton?
16.13 Can you set any node in the graphic property in a radio button?
16.14 How do you group radio buttons?

16.6 TextField

A text field can be used to enter or display a string. TextField is a subclass of TextInputControl. Figure 16.11 lists the properties and constructors in TextField.

Here is an example of creating a noneditable text field with red text color, a specified font, and right horizontal alignment:

```
TextField tfMessage = new TextField("T-Strom");
tfMessage.setEditable(false);
tfMessage.setStyle("-fx-text-fill: red");
tfMessage.setFont(Font.font("Times", 20));
tfMessage.setAlignment(Pos.BASELINE_RIGHT);
```

When you move the cursor in the text field and press the Enter key, it fires an ActionEvent.

Listing 16.5 gives a program that adds a text field to the preceding example to let the user set a new message, as shown in Figure 16.12.

```
import javafx.geometry.Insets;
import javafx.geometry.Pos;
```
import javafx.scene.control.Label;
import javafx.scene.control.TextField;
import javafx.scene.layout.BorderPane;

public class TextFieldDemo extends RadioButtonDemo {

    @Override
    protected BorderPane getPane() {

        BorderPane pane = super.getPane();

        BorderPane paneForTextField = new BorderPane();
        paneForTextField.setPadding(new Insets(5, 5, 5, 5));
        paneForTextField.setStyle("-fx-border-color: green");
        paneForTextField.setLeft(new Label("Enter a new message: "));

        TextField tf = new TextField();
        tf.setAlignment(Pos.BOTTOM_RIGHT);
        paneForTextField.setCenter(tf);
        pane.setTop(paneForTextField);

        tf.setOnAction(e -> text.setText(tf.getText()));

        return pane;
    }
}

javaFX scene controls textField

Figure 16.11 TextField enables the user to enter or display a string.

Figure 16.12 The program demonstrates using text fields.
TextFieldDemo extends RadioButtonDemo (line 7) and adds a label and a text field to let the user enter a new text (lines 12–19). After you set a new text in the text field and press the Enter key, a new message is displayed (line 22). Pressing the Enter key on the text field triggers an action event.

Note
If a text field is used for entering a password, use PasswordField to replace TextField. PasswordField extends TextField and hides the input text with echo characters ******.

16.15 Can you disable editing of a text field?
16.16 Can you apply all the methods for TextInputControl to TextField?
16.17 Can you set a node as the graphic property in a text field?
16.18 How do you align the text in a text field to the right?

16.7 TextArea
A TextArea enables the user to enter multiple lines of text.

If you want to let the user enter multiple lines of text, you may create several instances of TextField. A better alternative, however, is to use TextArea, which enables the user to enter multiple lines of text. Figure 16.13 lists the properties and constructors in TextArea.

![Diagram of TextArea properties and constructors]

**Figure 16.13** TextArea enables the user to enter or display multiple lines of characters.

Here is an example of creating a text area with 5 rows and 20 columns, wrapped to the next line, red text color, and Courier font 20 pixels.

```
TextArea taNote = new TextArea("This is a text area");
taNote.setPrefColumnCount(20);
taNote.setPrefRowCount(5);
taNote.setWrapText(true);
taNote.setStyle("-fx-text-fill: red");
taNote.setFont(Font.font("Times", 20));
```
**TextArea** provides scrolling, but often it is useful to create a **ScrollPane** object to hold an instance of **TextArea** and let **ScrollPane** handle scrolling for **TextArea**, as follows:

```java
// Create a scroll pane to hold text area
ScrollPane scrollPane = new ScrollPane(taNote);
```

**ScrollPane**

**Tip**
You can place any node in a **ScrollPane**. **ScrollPane** provides vertical and horizontal scrolling automatically if the control is too large to fit in the viewing area.

We now give a program that displays an image and a short text in a label, and a long text in a text area, as shown in Figure 16.14.

![Figure 16.14](image1)

**Figure 16.14** The program displays an image in a label, a title in a label, and text in the text area.

Here are the major steps in the program:

1. Define a class named **DescriptionPane** that extends **BorderPane**, as shown in Listing 16.6. This class contains a text area inside a scroll pane, and a label for displaying an image icon and a title. The class **DescriptionPane** will be reused in later examples.

2. Define a class named **TextAreaDemo** that extends **Application**, as shown in Listing 16.7. Create an instance of **DescriptionPane** and add it to the scene. The relationship between **DescriptionPane** and **TextAreaDemo** is shown in Figure 16.15.

![Figure 16.15](image2)

**Figure 16.15** **TextAreaDemo** uses **DescriptionPane** to display an image, title, and text description of a national flag.

**Listing 16.6** **DescriptionPane.java**

```java
1 import javafx.geometry.Insets;
2 import javafx.scene.control.Label;
3 import javafx.scene.control.ContentDisplay;
```

```java
import javafx.geometry.Insets;
import javafx.scene.control.Label;
import javafx.scene.control.ContentDisplay;
```
import javafx.scene.control.ScrollPane;
import javafx.scene.control.TextArea;
import javafx.scene.image.ImageView;
import javafx.scene.layout.BorderPane;
import javafx.scene.text.Font;

public class DescriptionPane extends BorderPane {

    /** Label for displaying an image and a title */
    private Label lblImageTitle = new Label();

    /** Text area for displaying text */
    private TextArea taDescription = new TextArea();

    public DescriptionPane() {
        // Center the icon and text and place the text under the icon
        lblImageTitle.setContentDisplay(ContentDisplay.TOP);
        lblImageTitle.setPrefSize(200, 100);

        // Set the font in the label and the text field
        lblImageTitle.setFont(new Font("SansSerif", 16));
        taDescription.setFont(new Font("Serif", 14));

        taDescription.setWrapText(true);
        taDescription.setEditable(false);

        // Create a scroll pane to hold the text area
        ScrollPane scrollPane = new ScrollPane(taDescription);

        // Place label and scroll pane in the border pane
        setLeft(lblImageTitle);
        setCenter(scrollPane);
        setPadding(new Insets(5, 5, 5, 5));
    }

    /** Set the title */
    public void setTitle(String title) {
        lblImageTitle.setText(title);
    }

    /** Set the image view */
    public void setImageView(ImageView icon) {
        lblImageTitle.setGraphic(icon);
    }

    /** Set the text description */
    public void setDescription(String text) {
        taDescription.setText(text);
    }
}

The text area is inside a ScrollPane (line 30), which provides scrolling functions for the

text area.

The wrapText property is set to true (line 26) so that the line is automatically wrapped
when the text cannot fit in one line. The text area is set as noneditable (line 27), so you cannot
edit the description in the text area.

It is not necessary to define a separate class for DescriptionPane in this example. How-
ever, this class was defined for reuse in the next section, where you will use it to display a
description pane for various images.
Listing 16.7  TextAreaDemo.java

```java
import javafx.application.Application;
import javafx.stage.Stage;
import javafx.scene.Scene;
import javafx.scene.image.ImageView;

public class TextAreaDemo extends Application {
    @Override
    public void start(Stage primaryStage) {
        DescriptionPane descriptionPane = new DescriptionPane();

        descriptionPane.setTitle("Canada");
        String description = "The Canadian national flag ...";
        descriptionPane.setImageView(new ImageView("image/ca.gif"));
        descriptionPane.setDescription(description);

        Scene scene = new Scene(descriptionPane, 450, 200);
        primaryStage.setTitle("TextAreaDemo");
        primaryStage.setScene(scene);
        primaryStage.show();
    }
}
```

The program creates an instance of DescriptionPane (line 10), and sets the title (line 13), image (line 15), and text in the description pane (line 16). DescriptionPane is a subclass of Pane. DescriptionPane contains a label for displaying an image and a title, and a text area for displaying a description of the image.

16.19 How do you create a text area with 10 rows and 20 columns?
16.20 How do you obtain the text from a text area?
16.21 Can you disable editing of a text area?
16.22 What method do you use to wrap text to the next line in a text area?

16.8 ComboBox

A combo box, also known as a choice list or drop-down list, contains a list of items from which the user can choose.

A combo box is useful for limiting a user’s range of choices and avoids the cumbersome validation of data input. Figure 16.16 lists several frequently used properties and constructors in ComboBox. ComboBox is defined as a generic class. The generic type T specifies the element type for the elements stored in a combo box.

The following statements create a combo box with four items, red color, and value set to the first item.

```java
ComboBox<String> cbo = new ComboBox<>();
cbo.getItems().addAll("Item 1", "Item 2", "Item 3", "Item 4");
cbo.setStyle("-fx-color: red");
cbo.setValue("Item 1");
```
ComboBox inherits from ComboBoxBase. ComboBox can fire an ActionEvent. Whenever an item is selected, an ActionEvent is fired. ObservableList is a subinterface of java.util.List. So you can apply all the methods defined in List for an ObservableList. For convenience, JavaFX provides the static method FXCollections.observableArrayList(arrayOfElements) for creating an ObservableList from an array of elements.

Listing 16.8 gives a program that lets the user view an image and a description of a country’s flag by selecting the country from a combo box, as shown in Figure 16.17.

Here are the major steps in the program:

1. Create the user interface.
   Create a combo box with country names as its selection values. Create a DescriptionPane object (the DescriptionPane class was introduced in the preceding section). Place the combo box at the top of the border pane and the description pane in the center of the border pane.

2. Process the event.
   Create a handler for handling action event from the combo box to set the flag title, image, and text in the description pane for the selected country name.
Listing 16.8 ComboBoxDemo.java

```java
import javafx.application.Application;
import javafx.stage.Stage;
import javafx.collections.FXCollections;
import javafx.collections.ObservableList;
import javafx.scene.Scene;
import javafx.scene.control.ComboBox;
import javafx.scene.control.Label;
import javafx.scene.image.ImageView;
import javafx.scene.layout.BorderPane;

public class ComboBoxDemo extends Application {

    private String[] flagTitles = {
        "Canada", "China", "Denmark", "France", "Germany", "India", "Norway", "United Kingdom", "United States of America";
    }

    private ImageView[] flagImage = {
        new ImageView("image/ca.gif"),
        new ImageView("image/china.gif"),
        new ImageView("image/denmark.gif"),
        new ImageView("image/fr.gif"),
        new ImageView("image/germany.gif"),
        new ImageView("image/india.gif"),
        new ImageView("image/norway.gif"),
        new ImageView("image/uk.gif"),
        new ImageView("image/us.gif")};

    private String[] flagDescription = new String[9];

    private DescriptionPane descriptionPane = new DescriptionPane();

    private ComboBox<String> cbo = new ComboBox<>();

    @Override
    public void start(Stage primaryStage) {
        flagDescription[0] = "The Canadian national flag ... ";
        flagDescription[1] = "Description for China ... ";
        flagDescription[2] = "Description for Denmark ... ";
        flagDescription[3] = "Description for France ... ";
        flagDescription[4] = "Description for Germany ... ";
        flagDescription[5] = "Description for India ... ";
        flagDescription[6] = "Description for Norway ... ";
        flagDescription[7] = "Description for UK ... ";
        flagDescription[8] = "Description for US ... ";

        setDisplay(0);

        addComboBoxAndDescriptionPaneToBorderPane();
    }

    public void setDisplay(int index) {
        descriptionPane.setTop(flagImage[index].getImage());
    }

    public void addComboBoxAndDescriptionPaneToBorderPane() {
        BorderPane pane = new BorderPane();
        pane.setVisible(true);
        pane.setTop(descriptionPane);
    }
}
```

Countries

Images

Description

ComboBox
cbo.setPrefWidth(400);
cbo.setValue("Canada");
ObservableList<String> items = FXCollections.observableArrayList(flagTitles);
cbo.getItems().addAll(items);
pane.setCenter(descriptionPane);

// Display the selected country
cbo.setOnAction(e -> setDisplay(items.indexOf(cbo.getValue())));

// Create a scene and place it in the stage
Scene scene = new Scene(pane, 450, 170);
primaryStage.setTitle("ComboBoxDemo"); // Set the stage title
primaryStage.setScene(scene); // Place the scene in the stage
primaryStage.show(); // Display the stage

/** Set display information on the description pane */
public void setDisplay(int index) {
    descriptionPane.setTitle(flagTitles[index]);
descriptionPane.setImageView(flagImage[index]);
descriptionPane.setDescription(flagDescription[index]);
}

The program stores the flag information in three arrays: flagTitles, flagImage, and flagDescription (lines 13–28). The array flagTitles contains the names of nine countries, the array flagImage contains image views of the nine countries’ flags, and the array flagDescription contains descriptions of the flags.

The program creates an instance of DescriptionPane (line 31), which was presented in Listing 16.6, DescriptionPane.java. The program creates a combo box with values from flagTitles (lines 62–63). The getItems() method returns a list from the combo box (line 64) and the addAll method adds multiple items into the list.

When the user selects an item in the combo box, the action event triggers the execution of the handler. The handler finds the selected index (line 68) and invokes the setDisplay(int index) method to set its corresponding flag title, flag image, and flag description on the pane (lines 78–82).

16.23 How do you create a combo box and add three items to it?
16.24 How do you retrieve an item from a combo box? How do you retrieve a selected item from a combo box?
16.25 How do you get the number of items in a combo box? How do you retrieve an item at a specified index in a combo box?
16.26 What events would a ComboBox fire upon selecting a new item?

16.9 ListView

A list view is a control that basically performs the same function as a combo box, but it enables the user to choose a single value or multiple values.

Figure 16.18 lists several frequently used properties and constructors in ListView. ListView is defined as a generic class. The generic type T specifies the element type for the elements stored in a list view.
The `getSelectionModel()` method returns an instance of `SelectionModel`, which contains the methods for setting a selection mode and obtaining selected indices and items. The selection mode is defined in one of the two constants `SelectionMode.MULTIPLE` and `SelectionMode.SINGLE`, which indicates whether a single item or multiple items can be selected. The default value is `SelectionMode.SINGLE`. Figure 16.19a shows a single selection and Figure 16.19b–c show multiple selections.

The following statements create a list view of six items with multiple selections allowed.

```java
ObservableList<String> items = FXCollections.observableArrayList("Item 1", "Item 2", "Item 3", "Item 4", "Item 5", "Item 6");
ListView<String> lv = new ListView<>(items);
lv.getSelectionModel().setSelectionMode(SelectionMode.MULTIPLE);
```

The selection model in a list view has the `selectedItemProperty` property, which is an instance of `Observable`. As discussed in Section 15.10, you can add a listener to this property for handling the property change as follows:

```java
lv.getSelectionModel().selectedItemProperty().addListener(new InvalidationListener() {
    public void invalidated(Observable ov) {
        System.out.println("Selected indices: "+ lv.getSelectionModel().getSelectedIndices());
    }
});
```
System.out.println("Selected items: "+lv.getSelectionModel().getSelectedItems());
});

This anonymous inner class can be simplified using a lambda expression as follows:

```
 lv.getSelectionModel().selectedItemProperty().addListener(ov -> {
   System.out.println("Selected indices: "+lv.getSelectionModel().getSelectedIndices());
   System.out.println("Selected items: "+lv.getSelectionModel().getSelectedItems());
 });
```

Listing 16.9 gives a program that lets users select the countries in a list view and displays the flags of the selected countries in the image views. Figure 16.20 shows a sample run of the program.

![Figure 16.20](image)

**Figure 16.20** When the countries in the list view are selected, corresponding images of their flags are displayed in the image views.

Here are the major steps in the program:

1. Create the user interface.
   Create a list view with nine country names as selection values, and place the list view inside a scroll pane. Place the scroll pane on the left of a border pane. Create nine image views to be used to display the countries’ flag images. Create a flow pane to hold the image views and place the pane in the center of the border pane.

2. Process the event.
   Create a listener to implement the invalidated method in the InvalidationListener interface to place the selected countries’ flag image views in the pane.

**Listing 16.9** ListViewDemo.java

```
import javax.application.Application;
import javax.stage.Stage;
import javax.collections.FXCollections;
import javax.scene.Scene;
import javax.scene.control.ListView;
import javax.scene.control.ScrollPane;
import javax.scene.control.SelectionMode;
import javax.scene.image.ImageView;
import javax.scene.layout.BorderPane;
import javax.scene.layout.FlowPane;

public class ListViewDemo extends Application {

```
// Declare an array of Strings for flag titles
private String[] flagTitles = {
    "Canada", "China", "Denmark", "France", "Germany", "India", "Norway", "United Kingdom",
    "United States of America"};

// Declare an ImageView array for the national flags of 9 countries
private ImageView[] ImageViews = {
    new ImageView("image/ca.gif"),
    new ImageView("image/china.gif"),
    new ImageView("image/denmark.gif"),
    new ImageView("image/fr.gif"),
    new ImageView("image/germany.gif"),
    new ImageView("image/india.gif"),
    new ImageView("image/norway.gif"),
    new ImageView("image/uk.gif"),
    new ImageView("image/us.gif")};

@override // Override the start method in the Application class
public void start(Stage primaryStage) {
    ListView<String> lv = new ListView<> (FXCollections.observableArrayList(flagTitles));
    lv.setPrefSize(400, 400);
    lv.getSelectionModel().setSelectionMode(SelectionMode.MULTIPLE);

    // Create a pane to hold image views
    FlowPane imagePane = new FlowPane(10, 10);
    BorderPane pane = new BorderPane();
    pane.setLeft(new ScrollPane(lv));
    pane.setCenter(imagePane);

    lv.getSelectionModel().selectedItemProperty().addListener(
        ov -> {
            imagePane.getChildren().clear();
            for (Integer i: lv.getSelectionModel().getSelectedIndices()) {
                imagePane.getChildren().add(ImageViews[i]);
            }
        });

    // Create a scene and place it in the stage
    Scene scene = new Scene(pane, 450, 170);
    primaryStage.setTitle("ListViewDemo"); // Set the stage title
    primaryStage.setScene(scene); // Place the scene in the stage
    primaryStage.show(); // Display the stage
}

The program creates an array of strings for countries (lines 14–16) and an array of nine image views for displaying flag images for nine countries (lines 19–29) in the same order as in the array of countries. The items in the list view are from the array of countries (line 34). Thus, the index 0 of the image view array corresponds to the first country in the list view.

The list view is placed in a scroll pane (line 41) so that it can be scrolled when the number of items in the list extends beyond the viewing area.

By default, the selection mode of the list view is single. The selection mode for the list view is set to multiple (line 36), which allows the user to select multiple items in the list view. When the user selects countries in the list view, the listener’s handler (lines 44–50) is executed, which gets the indices of the selected items and adds their corresponding image views to the flow pane.
### 16.10 ScrollBar

**ScrollBar** is a control that enables the user to select from a range of values.

Figure 16.21 shows a scroll bar. Normally, the user changes the value of a scroll bar by making a gesture with the mouse. For example, the user can drag the scroll bar’s thumb, click on the scroll bar track, or the scroll bar’s left or right buttons.

![Figure 16.21](image)

A scroll bar represents a range of values graphically.

**ScrollBar** has the following properties, as shown in Figure 16.22.

```java
javafx.scene.control.ScrollBar
- blockIncrement: DoubleProperty
- max: DoubleProperty
- min: DoubleProperty
- unitIncrement: DoubleProperty

-value: DoubleProperty
-visibleAmount: DoubleProperty
-orientation: ObjectProperty<Orientation>

+ScrollBar()
+increment()
+decrement()
```

**Note**

The width of the scroll bar’s track corresponds to `max + visibleAmount`. When a scroll bar is set to its maximum value, the left side of the bubble is at `max`, and the right side is at `max + visibleAmount`.
When the user changes the value of the scroll bar, it notifies the listener of the change. You can register a listener on the scroll bar’s `valueProperty` for responding to this change as follows:

```java
ScrollBar sb = new ScrollBar();
sb.valueProperty().addListener(ov -> {
    System.out.println("old value: " + oldVal);
    System.out.println("new value: " + newVal);
});
```

Listing 16.10 gives a program that uses horizontal and vertical scroll bars to move a text displayed on a pane. The horizontal scroll bar is used to move the text to the left and the right, and the vertical scroll bar to move it up and down. A sample run of the program is shown in Figure 16.23.

![Figure 16.23](image)

**Figure 16.23** The scroll bars move the message on a pane horizontally and vertically.

Here are the major steps in the program:

1. Create the user interface.
   Create a `Text` object and place it in the center of the border pane. Create a vertical scroll bar and place it on the right of the border pane. Create a horizontal scroll bar and place it at the bottom of the border pane.

2. Process the event.
   Create listeners to move the text according to the bar movement in the scroll bars upon the change of the `value` property.

**LISTING 16.10 ScrollBarDemo.java**

```java
import javafx.application.Application;
import javafx.stage.Stage;
import javafx.geometry.Orientation;
import javafx.scene.Scene;
import javafx.scene.control.ScrollBar;
import javafx.scene.layout.BorderPane;
import javafx.scene.layout.Pane;
import javafx.scene.text.Text;

public class ScrollBarDemo extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        Text text = new Text(20, 20, "JavaFX Programming");
        ScrollBar sbHorizontal = new ScrollBar();
        ScrollBar sbVertical = new ScrollBar();
        sbVertical.setOrientation(Orientation.VERTICAL);
        // Create a text in a pane
```
Pane paneForText = new Pane();
paneForText.getChildren().add(text);  // add text to a pane

// Create a border pane to hold text and scroll bars
BorderPane pane = new BorderPane();
pane.setCenter(paneForText);
pane.setBottom(sbHorizontal);
pane.setRight(sbVertical);

// Listener for horizontal scroll bar value change
sbHorizontal.valueProperty().addListener(ov ->
    text.setX(sbHorizontal.getValue() * paneForText.getWidth() / sbHorizontal.getMax()));

// Listener for vertical scroll bar value change
sbVertical.valueProperty().addListener(ov ->
    text.setY(sbVertical.getValue() * paneForText.getHeight() / sbVertical.getMax()));

// Create a scene and place it in the stage
Scene scene = new Scene(pane, 450, 170);
primaryStage.setTitle("ScrollBarDemo"); // Set the stage title
primaryStage.setScene(scene); // Place the scene in the stage
primaryStage.show(); // Display the stage

The program creates a text (line 13) and two scroll bars (sbHorizontal and sbVertical) (lines 15–16). The text is placed in a pane (line 21) that is then placed in the center of the border pane (line 25). If the text were directly placed in the center of the border pane, the position of the text cannot be changed by resetting its x and y properties. The sbHorizontal and sbVertical are placed on the right and at the bottom of the border pane (lines 26–27), respectively.

You can specify the properties of the scroll bar. By default, the property value is 100 for max, 0 for min, 10 for blockIncrement, and 15 for visibleAmount.

A listener is registered to listen for the sbHorizontal value property change (lines 30–32). When the value of the scroll bar changes, the listener is notified by invoking the handler to set a new x value for the text that corresponds to the current value of sbHorizontal (lines 31–32).

A listener is registered to listen for the sbVertical value property change (lines 35–37). When the value of the scroll bar changes, the listener is notified by invoking the handler to set a new y value for the text that corresponds to the current value of sbVertical (lines 36–37).

Alternatively, the code in lines 30–37 can be replaced by using binding properties as follows:

```java
    text.xProperty().bind(sbHorizontal.valueProperty().
        multiply(paneForText.widthProperty()).
        divide(sbHorizontal.maxProperty()));

    text.yProperty().bind(sbVertical.valueProperty().multiply(
        paneForText.heightProperty()).divide(
            sbVertical.maxProperty()));
```

16.31 How do you create a horizontal scroll bar? How do you create a vertical scroll bar?
16.32 How do you write the code to respond to the value property change of a scroll bar?
16.33 How do you get the value from a scroll bar? How do you get the maximum value from a scroll bar?
16.11 Slider

Slider is similar to ScrollBar, but Slider has more properties and can appear in many forms.

Figure 16.24 shows two sliders. Slider lets the user graphically select a value by sliding a knob within a bounded interval. The slider can show both major tick marks and minor tick marks between them. The number of pixels between the tick marks is specified by the majorTickUnit and minorTickUnit properties. Sliders can be displayed horizontally or vertically, with or without ticks, and with or without labels.

![Figure 16.24](image)

The frequently used constructors and properties in Slider are shown in Figure 16.25.

![Figure 16.25](image)

The values of a vertical scroll bar increase from top to bottom, but the values of a vertical slider decrease from top to bottom.

You can add a listener to listen for the value property change in a slider in the same way as in a scroll bar. We now rewrite the program in the preceding section using the sliders to move a text displayed on a pane in Listing 16.11. A sample run of the program is shown in Figure 16.24.
Listing 16.11  SliderDemo.java

1  import javafx.application.Application;
2  import javafx.stage.Stage;
3  import javafx.geometry.Orientation;
4  import javafx.scene.Scene;
5  import javafx.scene.control.Slider;
6  import javafx.scene.layout.BorderPane;
7  import javafx.scene.layout.Pane;
8  import javafx.scene.text.Text;
9
10 public class SliderDemo extends Application {
11    @Override // Override the start method in the Application class
12    public void start(Stage primaryStage) {
13      Text text = new Text(20, 20, "JavaFX Programming");
14
15      Slider slHorizontal = new Slider();
16      slHorizontal.setShowTickLabels(true);
17      slHorizontal.setShowTickMarks(true);
18
19      Slider slVertical = new Slider();
20      slVertical.setOrientation(Orientation.VERTICAL);
21      slVertical.setShowTickLabels(true);
22      slVertical.setShowTickMarks(true);
23      slVertical.setValue(100);
24
25      // Create a text in a pane
26      Pane paneForText = new Pane();
27      paneForText.getChildren().add(text);
28
29      // Create a border pane to hold text and scroll bars
30      BorderPane pane = new BorderPane();
31      pane.setCenter(paneForText);
32      pane.setBottom(slHorizontal);
33      pane.setRight(slVertical);
34
35      slHorizontal.valueProperty().addListener(ov ->
36          text.setX(slHorizontal.getValue() * paneForText.getWidth() / slHorizontal.getMax()));
37
38      slVertical.valueProperty().addListener(ov ->
39          text.setY((slVertical.getMax() - slVertical.getValue()) * paneForText.getHeight() / slVertical.getMax()));
40
41      // Create a scene and place it in the stage
42      Scene scene = new Scene(pane, 450, 170);
43      primaryStage.setTitle("SliderDemo"); // Set the stage title
44      primaryStage.setScene(scene); // Place the scene in the stage
45      primaryStage.show(); // Display the stage
46    }
47  }

Slider is similar to ScrollBar but has more features. As shown in this example, you can specify labels, major ticks, and minor ticks on a Slider (lines 16–17).

A listener is registered to listen for the slHorizontal value property change (lines 35–37) and another one is for the sbVertical value property change (lines 39–41). When the value of the slider changes, the listener is notified by invoking the handler to set a new position for the text (lines 36–37, 40–41). Note that since the value of a vertical slider decreases from top to bottom, the corresponding y value for the text is adjusted accordingly.
The code in lines 35–41 can be replaced by using binding properties as follows:

```java
    text.xProperty().bind(slHorizontal.valueProperty().
           multiply(paneForText.widthProperty()).
           divide(slHorizontal.maxProperty()));

    text.yProperty().bind((slVertical.maxProperty().subtract(
           slVertical.valueProperty()).multiply(
           paneForText.heightProperty().divide(
           slVertical.maxProperty()))));
```

Listing 15.17 gives a program that displays a bouncing ball. You can add a slider to control the speed of the ball movement as shown in Figure 16.26. The new program is given in Listing 16.12.

![Figure 16.26](image)

**Figure 16.26** You can increase or decrease the speed of the ball using a slider.

**Listing 16.12** BounceBallSlider.java

```java
import javafx.application.Application;
import javafx.stage.Stage;
import javafx.scene.Scene;
import javafx.scene.control.Slider;
import javafx.scene.layout.BorderPane;

public class BounceBallSlider extends Application {

    @Override
    public void start(Stage primaryStage) {
      BallPane ballPane = new BallPane();
      Slider slSpeed = new Slider();
      slSpeed.setMax(20);
      ballPane.rateProperty().bind(slSpeed.valueProperty());

      BorderPane pane = new BorderPane();
      pane.setCenter(ballPane);
      pane.setBottom(slSpeed);

      Scene scene = new Scene(pane, 250, 250);
      primaryStage.setTitle("BounceBallSlider");
      primaryStage.setScene(scene);
      primaryStage.show();
    }
}
```

The BallPane class defined in Listing 15.17 animates a ball bouncing in a pane. The rateProperty() method in BallPane returns a property value for animation rate.
The animation stops if the rate is 0. If the rate is greater than 20, the animation will be too fast. So, we purposely set the rate to a value between 0 and 20. This value is bound to the slider value (line 13). So the slider max value is set to 20 (line 12).

16.34 How do you create a horizontal slider? How do you create a vertical slider?
16.35 How do you add a listener to handle the property value change of a slider?
16.36 How do you get the value from a slider? How do you get the maximum value from a slider?

16.12 Case Study: Developing a Tic-Tac-Toe Game

This section develops a program for playing tic-tac-toe.

From the many examples in this and earlier chapters you have learned about objects, classes, arrays, class inheritance, GUI, and event-driven programming. Now it is time to put what you have learned to work in developing comprehensive projects. In this section, we will develop a JavaFX program with which to play the popular game of tic-tac-toe.

Two players take turns marking an available cell in a 3 \times 3 grid with their respective tokens (either X or O). When one player has placed three tokens in a horizontal, vertical, or diagonal row on the grid, the game is over and that player has won. A draw (no winner) occurs when all the cells on the grid have been filled with tokens and neither player has achieved a win. Figure 16.27 shows the representative sample runs of the game.

All the examples you have seen so far show simple behaviors that are easy to model with classes. The behavior of the tic-tac-toe game is somewhat more complex. To define classes that model the behavior, you need to study and understand the game.

Assume that all the cells are initially empty, and that the first player takes the X token and the second player the O token. To mark a cell, the player points the mouse to the cell and clicks it. If the cell is empty, the token (X or O) is displayed. If the cell is already filled, the player’s action is ignored.

From the preceding description, it is obvious that a cell is a GUI object that handles the mouse-click event and displays tokens. There are many choices for this object. We will use a pane to model a cell and to display a token (X or O). How do you know the state of the cell (empty, X, or O)? You use a property named token of the char type in the Cell class. The Cell class is responsible for drawing the token when an empty cell is clicked, so you need to write the code for listening to the mouse-clicked action and for painting the shapes for tokens X and O. The Cell class can be defined as shown in Figure 16.28.
The tic-tac-toe board consists of nine cells, created using `new Cell[3][3]`. To determine which player’s turn it is, you can introduce a variable named `whoseTurn` of the `char` type. `whoseTurn` is initially ’X’, then changes to ’O’, and subsequently changes between ’X’ and ’O’ whenever a new cell is occupied. When the game is over, set `whoseTurn` to ’ ’.

How do you know whether the game is over, whether there is a winner, and who the winner, if any? You can define a method named `isWon(char token)` to check whether a specified token has won and a method named `isFull()` to check whether all the cells are occupied.

Clearly, two classes emerge from the foregoing analysis. One is the `Cell` class, which handles operations for a single cell; the other is the `TicTacToe` class, which plays the whole game and deals with all the cells. The relationship between these two classes is shown in Figure 16.29.

Since the `Cell` class is only to support the `TicTacToe` class, it can be defined as an inner class in `TicTacToe`. The complete program is given in Listing 16.13.

### Listing 16.13  TicTacToe.java

```java
import javafx.application.Application;
import javafx.stage.Stage;
import javafx.scene.Scene;
import javafx.scene.control.Label;
import javafx.scene.layout.BorderPane;
```
16.12 Case Study: Developing a Tic-Tac-Toe Game

```java
import javafx.scene.layout.GridPane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Line;
import javafx.scene.shape.Ellipse;

public class TicTacToe extends Application {
    private char whoseTurn = 'X';

    private Cell[][] cell = new Cell[3][3];

    private Label lblStatus = new Label("X's turn to play");

    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        GridPane pane = new GridPane();
        for (int i = 0; i < 3; i++)
            for (int j = 0; j < 3; j++)
                pane.add(cell[i][j] = new Cell(), j, i);

        BorderPane borderPane = new BorderPane();
        borderPane.setCenter(pane);
        borderPane.setBottom(lblStatus);

        Scene scene = new Scene(borderPane, 450, 170);
        primaryStage.setTitle("TicTacToe"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }

    /** Determine if the cell are all occupied */
    public boolean isFull() {
        for (int i = 0; i < 3; i++)
            for (int j = 0; j < 3; j++)
                if (cell[i][j].getToken() == ' ')
                    return false;
        return true;
    }

    /** Determine if the player with the specified token wins */
    public boolean isWon(char token) {
        for (int i = 0; i < 3; i++)
            if (cell[i][0].getToken() == token
                && cell[i][1].getToken() == token
                && cell[i][2].getToken() == token) {
                return true;
            }

        for (int j = 0; j < 3; j++)
            if (cell[0][j].getToken() == token
                && cell[1][j].getToken() == token
                && cell[2][j].getToken() == token) {
                return true;
            }
    }
}
```

if (cell[0][0].getToken() == token
    && cell[1][1].getToken() == token
    && cell[2][2].getToken() == token) {
    return true;
}

check subdiagonal
if (cell[0][2].getToken() == token
    && cell[1][1].getToken() == token
    && cell[2][0].getToken() == token) {
    return true;
}

return false;
}

// An inner class for a cell
inner class Cell
public class Cell extends Pane {
    // Token used for this cell
    private char token = ' ';

    public Cell() {
        setStyle("-fx-border-color: black");
        this.setPrefSize(2000, 2000);
        this.setOnMouseClicked(e -> handleMouseClick());
    }

    /** Return token */
    public char getToken() {
        return token;
    }

    /** Set a new token */
    public void setToken(char c) {
        token = c;
    }

    if (token == 'X') {
        Line line1 = new Line(10, 10,
            this.getWidth() - 10, this.getHeight() - 10);
        line1.endXProperty().bind(this.widthProperty().subtract(10));
        line1.endYProperty().bind(this.heightProperty().subtract(10));
        Line line2 = new Line(10, this.getHeight() - 10,
            this.getWidth() - 10, 10);
        line2.startYProperty().bind(
            this.heightProperty().subtract(10));
        line2.endXProperty().bind(this.widthProperty().subtract(10));
        line1.setChildren().addAll(line1, line2);
    }

    if (token == 'O') {
        Ellipse ellipse = new Ellipse(this.getWidth() / 2,
            this.getHeight() / 2, this.getWidth() / 2 - 10,
            this.getHeight() / 2 - 10);
        ellipse.centerXProperty().bind(
            this.widthProperty().divide(2));
        ellipse.centerYProperty().bind(
            this.heightProperty().divide(2));
        ellipse.radiusXProperty().bind(
            this.widthProperty().divide(2).subtract(10));
    }
ellipses.radiusYProperty().bind(
    this.heightProperty().divide(2).subtract(10));
ellipse.setStroke(Color.BLACK);
ellipse.setFill(Color.WHITE);

getChildren().add(ellipse); // Add the ellipse to the pane

/* Handle a mouse click event */
private void handleMouseClick() {
    // If cell is empty and game is not over
    if (token == ' ' && whoseTurn != ' ')
    {
        setToken(whoseTurn); // Set token in the cell
        // Check game status
        if (isWon(whoseTurn))
        {
            lblStatus.setText(whoseTurn + " won! The game is over");
            whoseTurn = ' '; // Game is over
        }
        else if (isFull())
        {
            lblStatus.setText("Draw! The game is over");
            whoseTurn = ' '; // Game is over
        }
        else
        {
            // Change the turn
            whoseTurn = (whoseTurn == 'X') ? 'O' : 'X';
            // Display whose turn
            lblStatus.setText(whoseTurn + "'s turn");
        }
    }
}

The TicTacToe class initializes the user interface with nine cells placed in a grid pane (lines 25–28). A label named lblStatus is used to show the status of the game (line 20). The variable whoseTurn (line 14) is used to track the next type of token to be placed in a cell. The methods isFull (lines 42–49) and isWon (lines 52–80) are for checking the status of the game.

Since Cell is an inner class in TicTacToe, the variable (whoseTurn) and methods (isFull and isWon) defined in TicTacToe can be referenced from the Cell class. The inner class makes programs simple and concise. If Cell were not defined as an inner class of TicTacToe, you would have to pass an object of TicTacToe to Cell in order for the variables and methods in TicTacToe to be used in Cell.

The listener for the mouse-click action is registered for the cell (line 90). If an empty cell is clicked and the game is not over, a token is set in the cell (line 138). If the game is over, whoseTurn is set to ' ' (lines 144, 148). Otherwise, whoseTurn is alternated to a new turn (line 152).

Tip

Use an incremental approach in developing and testing a Java project of this kind. For example, this program can be divided into five steps:

1. Lay out the user interface and display a fixed token X on a cell.
2. Enable the cell to display a fixed token X upon a mouse click.
3. Coordinate between the two players so as to display tokens X and O alternately.
4. Check whether a player wins, or whether all the cells are occupied without a winner.
5. Implement displaying a message on the label upon each move by a player.
16.37 When the game starts, what value is in whoseTurn? When the game is over, what value is in whoseTurn?

16.38 What happens when the user clicks on an empty cell if the game is not over? What happens when the user clicks on an empty cell if the game is over?

16.39 How does the program check whether a player wins? How does the program check whether all cells are filled?

16.13 Video and Audio

You can use the Media class to obtain the source of the media, the MediaPlayer class to play and control the media, and the MediaView class to display the video.

Media (video and audio) is essential in developing rich Internet applications. JavaFX provides the Media, MediaPlayer, and MediaView classes for working with media. Currently, JavaFX supports MP3, AIFF, WAV, and MPEG-4 audio formats and FLV and MPEG-4 video formats.

The Media class represents a media source with properties duration, width, and height, as shown in Figure 16.30. You can construct a Media object from an Internet URL string.

![Figure 16.30](image)

The get and set methods for property values and a getter for property itself are provided in the class, but omitted in the UML diagram for brevity.

The durations in seconds of the source media.

The width in pixels of the source video.

The height in pixels of the source video.

Creates a Media from a URL source.

The MediaPlayer class plays and controls the media with properties such as autoPlay, currentCount, cycleCount, mute, volume, and totalDuration, as shown in Figure 16.31. You can construct a MediaPlayer object from a media and use the pause() and play() method to pause and resume playing.

![Figure 16.31](image)

Specifies whether the playing should start automatically.

The number of completed playback cycles.

Specifies the number of times the media will be played.

Specifies whether the audio is muted.

The volume for the audio.

The amount of time to play the media from start to finish.

Creates a player for a specified media.

Plays the media.

Pauses the media.

Seeks the player to a new playback time.
The MediaView class is a subclass of Node that provides a view of the Media being played by a MediaPlayer. The MediaView class provides the properties for viewing the media, as shown in Figure 16.32.

FIGURE 16.32 MediaView provides the properties for viewing the media.

Listing 16.14 gives an example that displays a video in a view, as shown in Figure 16.33. You can use the play/pause button to play or pause the video and use the rewind button to restart the video, and use the slider to control the volume of the audio.

FIGURE 16.33 The program controls and plays a video.

LISTING 16.14 MediaDemo.java

```java
import javafx.application.Application;
import javafx.stage.Stage;
import javafx.geometry.Pos;
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.scene.control.Label;
import javafx.scene.control.Slider;
import javafx.scene.layout.BorderPane;
import javafx.scene.layout.HBox;
import javafx.scene.media.Media;
```
12 import javafx.scene.media.MediaPlayer;
13 import javafx.scene.media.MediaView;
14 import javafx.util.Duration;
15
16 public class MediaDemo extends Application {
17    private static final String MEDIA_URL =
18        "http://cs.armstrong.edu/liang/common/sample.mp4";
19
20    @Override // Override the start method in the Application class
21    public void start(Stage primaryStage) {
22        Media media = new Media(MEDIA_URL);
23        MediaPlayer mediaPlayer = new MediaPlayer(media);
24        MediaView mediaView = new MediaView(mediaPlayer);
25
26        Button playButton = new Button(">");
27        playButton.setOnAction(e -> {
28            if (playButton.getText().equals("")) {
29                mediaPlayer.play();
30                playButton.setText("||");
31            } else {
32                mediaPlayer.pause();
33                playButton.setText(">");
34            }
35        });
26
27        Button rewindButton = new Button("<<");
28        rewindButton.setOnAction(e -> mediaPlayer.seek(Duration.ZERO));
29
30        Slider slVolume = new Slider();
31        slVolume.setPrefWidth(150);
32        slVolume.setMaxWidth(Region.USE_PREF_SIZE);
33        slVolume.setMinWidth(30);
34        slVolume.setValue(50);
35        mediaPlayer.volumeProperty().bind(
36            slVolume.valueProperty().divide(100));
37
38        HBox hBox = new HBox(10);
39        hBox.setAlignment(Pos.CENTER);
40        hBox.getChildren().addAll(playButton, rewindButton,
41            new Label("Volume"), slVolume);
42
43        BorderPane pane = new BorderPane();
44        pane.setCenter(mediaView);
45        pane.setBottom(hBox);
46
47        // Create a scene and place it in the stage
48        Scene scene = new Scene(pane, 650, 500);
49        primaryStage.setTitle("MediaDemo"); // Set the stage title
50        primaryStage.setScene(scene); // Place the scene in the stage
51        primaryStage.show(); // Display the stage
52    }
53}

The source of the media is a URL string defined in lines 17 and 18. The program creates a Media object from this URL (line 22), a MediaPlayer from the Media object (line 23), and a MediaView from the MediaPlayer object (line 24). The relationship among these three objects is shown in Figure 16.34.
16.14 Case Study: National Flags and Anthems

This case study presents a program that displays a nation’s flag and plays its anthem.

The images for seven national flags, named flag0.gif, flag1.gif, . . . , flag6.gif for Denmark, Germany, China, India, Norway, United Kingdom, and United States are stored under www.cs.armstrong.edu/liang/common/image. The audio consists of national anthems for these seven nations, named anthem0.mp3, anthem1.mp3, . . . , and anthem6.mp3. They are stored under www.cs.armstrong.edu/liang/common/audio.

The program enables the user to select a nation from a combo box and then displays its flag and plays its anthem. The user can suspend the audio by clicking the || button and resume it by clicking the < button, as shown in Figure 16.35.

![FlagAnthem](image1)

**Figure 16.35** The program displays a national flag and plays its anthem.
Chapter 16  JavaFX UI Controls and Multimedia

The program is given in Listing 16.15.

**LISTING 16.15 FlagAnthem.java**

```java
public class FlagAnthem extends Application {

    private final static int NUMBER_OF_NATIONS = 7;
    private final static String URLBase = "http://cs.armstrong.edu/liang/common";

    public void start(Stage primaryStage) {
        Image[] images = new Image[NUMBER_OF_NATIONS];
        MediaPlayer[] mp = new MediaPlayer[NUMBER_OF_NATIONS];

        for (int i = 0; i < NUMBER_OF_NATIONS; i++) {
            images[i] = new Image(URLBase + "image/flag" + i + "gif");
            mp[i] = new MediaPlayer(new Media(
                URLBase + "audio/anthem/anthem" + i + "mp3"));
        }

        Button btPlayPause = new Button(">");
        btPlayPause.setOnAction(e -> {
            if (btPlayPause.getText().equals("")) {
                btPlayPause.setText("||");
                mp[currentIndex].pause();
            } else {
                btPlayPause.setText(">");
                mp[currentIndex].play();
            }
        });

        ImageView imageView = new ImageView(images[currentIndex]);
        ObservableList<String> items = FXCollections.observableArrayList("Denmark", "Germany", "China", "India", "Norway", "UK", "US");
        cboNation = new ComboBox<>(items);
        cboNation.setValue(items.get(0));
        cboNation.setOnAction(e -> {
            mp[currentIndex].stop();
            currentIndex = items.indexOf(cboNation.getValue());
            imageView.setImage(images[currentIndex]);
            mp[currentIndex].play();
        });
    }

    public void start(Stage primaryStage) {
        Scene scene = new Scene(new BorderPane());
        scene.getStylesheets().add("/css/chapter16.css");
        primaryStage.setScene(scene);
        primaryStage.show();
    }
}
```

58      HBox hbox = new HBox(10);
59      hbox.getChildren().addAll(btPlayPause,
60          new Label("Select a nation: "), cboNation);
61      hbox.setAlignment(Pos.CENTER);
62
63 // Create a pane to hold nodes
64      BorderPane pane = new BorderPane();
65      pane.setCenter(imageView);
66      pane.setBottom(hbox);
67
68 // Create a scene and place it in the stage
69      Scene scene = new Scene(pane, 350, 270);
70      primaryStage.setTitle("FlagAnthem"); // Set the stage title
71      primaryStage.setScene(scene); // Place the scene in the stage
72      primaryStage.show(); // Display the stage
73  }
74 }

The program loads the image and audio from the Internet (lines 29–33). A play/pause button is created to control the playing of the audio (line 35). When the button is clicked, if the button’s current text is > (line 37), its text is changed to || (line 38) and the player is paused (line 39); if the button’s current text is ||, it is changed to > (line 41) and the player is paused (line 42).

An image view is created to display a flag image (line 46). A combo box is created for selecting a nation (line 47–49). When a new country name in the combo box is selected, the current audio is stopped (line 53) and the newly selected nation’s image is displayed (line 55) and the new anthem is played (line 56).

JavaFX also provides the AudioClip class for creating auto clips. An AudioClip object can be created using new AudioClip(URL). An audio clip stores the audio in memory. AudioClip is more efficient for playing a small audio clip in the program than using MediaPlayer. AudioClip has the similar methods as in the MediaPlayer class.

16.43 In Listing 16.15, which code sets the initial image icon and which code plays the audio?

16.44 In Listing 16.15, what does the program do when a new nation is selected in the combo box?

**Chapter Summary**

1. The abstract Labeled class is the base class for Label, Button, CheckBox, and RadioButton. It defines properties alignment, contentDisplay, text, graphic, graphicTextGap, textFill, underline, and wrapText.

2. The abstract ButtonBase class is the base class for Button, CheckBox, and RadioButton. It defines the onAction property for specifying a handler for action events.

3. The abstract TextInputControl class is the base class for TextField and TextArea. It defines the properties text and editable.

4. A TextField fires an action event when clicking the Enter key with the text field focused. A TextArea is often used for editing a multiline text.

5. ComboBox<T> and ListView<T> are generic classes for storing elements of type T. The elements in a combo box or a list view are stored in an observable list.
6. A **ComboBox** fires an action event when a new item is selected.

7. You can set a single item or multiple item selection for a **ListView** and add a listener for processing selected items.

8. You can use a **ScrollBar** or **Slider** to select a range of values and add a listener to the **value** property to respond to the change of the value.

9. JavaFX provides the **Media** class for loading a media, the **MediaPlayer** class for controlling a media, and the **MediaView** for displaying a media.

**Quiz**

Answer the quiz for this chapter online at [www.cs.armstrong.edu/liang/intro10e/quiz.html](http://www.cs.armstrong.edu/liang/intro10e/quiz.html).

**MyProgrammingLab**

**Programming Exercises**

Sections 16.2–16.5

*16.1* *(Use radio buttons)* Write a GUI program as shown in Figure 16.36a. You can use buttons to move the message to the left and right and use the radio buttons to change the color for the message displayed.

![Figure 16.36](image)

(a) The <= and => buttons move the message, and the radio buttons change the color for the message displayed. (b) The program displays a circle, rectangle, and ellipse when you select a shape type.

*16.2* *(Select geometric figures)* Write a program that draws various figures, as shown in Figure 16.36b. The user selects a figure from a radio button and uses a check box to specify whether it is filled.

**16.3** *(Traffic lights)* Write a program that simulates a traffic light. The program lets the user select one of three lights: red, yellow, or green. When a radio button is selected, the light is turned on. Only one light can be on at a time (see Figure 16.37a). No light is on when the program starts.
*16.4 (Create a miles/kilometers converter) Write a program that converts miles and kilometers, as shown in Figure 16.37b. If you enter a value in the Mile text field and press the Enter key, the corresponding kilometer measurement is displayed in the Kilometer text field. Likewise, if you enter a value in the Kilometer text field and press the Enter key, the corresponding miles is displayed in the Mile text field.

*16.5 (Convert numbers) Write a program that converts between decimal, hex, and binary numbers, as shown in Figure 16.37c. When you enter a decimal value in the decimal-value text field and press the Enter key, its corresponding hex and binary numbers are displayed in the other two text fields. Likewise, you can enter values in the other fields and convert them accordingly. (Hint: Use the Integer.parseInt(s, radix) method to parse a string to a decimal and use Integer.toHexString(decimal) and Integer.toBinaryString(decimal) to obtain a hex number or a binary number from a decimal.)

*16.6 (Demonstrate TextField properties) Write a program that sets the horizontal-alignment and column-size properties of a text field dynamically, as shown in Figure 16.38a.

---

**Figure 16.37** (a) The radio buttons are grouped to let you turn only one light on at a time. (b) The program converts miles to kilometers, and vice versa. (c) The program converts between decimal, hex, and binary numbers.

**Figure 16.38** (a) You can set a text field’s properties for the horizontal alignment and column size dynamically. (b) The program displays the time specified in the text fields.
16.7 (Set clock time) Write a program that displays a clock and sets the time with the input from three text fields, as shown in Figure 16.38b. Use the ClockPane in Listing 14.21. Resize the clock to the center of the pane.

16.8 (Geometry: two circles intersect?) Write a program that enables the user to specify the location and size of the circles and displays whether the two circles intersect, as shown in Figure 16.39a. Enable the user to point the mouse inside a circle and drag it. As the circle is being dragged, the circle’s center coordinates in the text fields are updated.

![Figure 16.39](image)

Check whether two circles and two rectangles are overlapping.

16.9 (Geometry: two rectangles intersect?) Write a program that enables the user to specify the location and size of the rectangles and displays whether the two rectangles intersect, as shown in Figure 16.39b. Enable the user to point the mouse inside a rectangle and drag it. As the rectangle is being dragged, the rectangle’s center coordinates in the text fields are updated.

Sections 16.6–16.8

16.10 (Text viewer) Write a program that displays a text file in a text area, as shown in Figure 16.40a. The user enters a file name in a text field and clicks the View button; the file is then displayed in a text area.

![Figure 16.40](image)
**16.11  (Create a histogram for occurrences of letters) Write a program that reads a file and displays a histogram to show the occurrences of each letter in the file, as shown in Figure 16.40b. The file name is entered from a text field. Pressing the Enter key on the text field causes the program to start to read and process the file and displays the histogram. The histogram is displayed in the center of the window. Define a class named Histogram that extends Pane. The class contains the property counts that is an array of 26 elements. counts[0] stores the number of A, counts[1] the number of B, and so on. The class also contains a setter method for setting a new counts and displaying the histogram for the new counts.

**16.12  (Demonstrate TextArea properties) Write a program that demonstrates the properties of a text area. The program uses a check box to indicate whether the text is wrapped onto next line, as shown in Figure 16.41a.

*16.13  (Compare loans with various interest rates) Rewrite Programming Exercise 5.21 to create a GUI, as shown in Figure 16.41b. Your program should let the user enter the loan amount and loan period in the number of years from text fields, and it should display the monthly and total payments for each interest rate starting from 5 percent to 8 percent, with increments of one-eighth, in a text area.

**16.14  (Select a font) Write a program that can dynamically change the font of a text in a label displayed on a stack pane. The text can be displayed in bold and italic at the same time. You can select the font name or font size from combo boxes, as shown in Figure 16.42a. The available font names can be obtained using Font.getFamilies(). The combo box for the font size is initialized with numbers from 1 to 100.

![Figure 16.41](a) You can set the options to enable text editing and text wrapping. (b) The program displays a table for monthly payments and total payments on a given loan based on various interest rates.

![Figure 16.42](a) You can dynamically set the font for the message. (b) You can set the alignment and text-position properties of a label dynamically.
**16.15 (Demonstrate Label properties) Write a program to let the user dynamically set the properties `contentDisplay` and `graphicTextGap`, as shown in Figure 16.42b.

*16.16 (Use ComboBox and ListView) Write a program that demonstrates selecting items in a list. The program uses a combo box to specify a selection mode, as shown in Figure 16.43a. When you select items, they are displayed in a label below the list.

Figure 16.43 (a) You can choose single or multiple selection mode in a list. (b) The color changes in the text as you adjust the scroll bars. (c) The program simulates a running fan.

Sections 16.6–16.8

**16.17 (Use ScrollBar and Slider) Write a program that uses scroll bars or sliders to select the color for a text, as shown in Figure 16.43b. Four horizontal scroll bars are used for selecting the colors: red, green, blue, and opacity percentages.

**16.18 (Simulation: a running fan) Rewrite Programming Exercise 15.28 to add a slider to control the speed of the fan, as shown in Figure 16.43c.

**16.19 (Control a group of fans) Write a program that displays three fans in a group, with control buttons to start and stop all of them, as shown in Figure 16.44.

Figure 16.44 The program runs and controls a group of fans.

*16.20 (Count-up stopwatch) Write a program that simulates a stopwatch, as shown in Figure 16.45a. When the user clicks the `Start` button, the button’s label is changed to `Pause`, as shown in Figure 16.45b. When the user clicks the `Pause`
button, the button’s label is changed to Resume, as shown in Figure 16.45c. The
Clear button resets the count to 0 and resets the button’s label to Start.

*16.21 (Count-down stopwatch) Write a program that allows the user to enter time in
seconds in the text field and press the Enter key to count down the seconds,
as shown in Figure 16.45d. The remaining seconds are redisplayed every
one second. When the seconds are expired, the program starts to play music
continuously.

16.22 (Play, loop, and stop a sound clip) Write a program that meets the following
requirements:

- Get an audio file from the class directory using AudioClip.
- Place three buttons labeled Play, Loop, and Stop, as shown in Figure 16.46a.
- If you click the Play button, the audio file is played once. If you click the
  Loop button, the audio file keeps playing repeatedly. If you click the Stop
  button, the playing stops.
**16.23 (Create an image animator with audio) Create animation in Figure 16.46b to meet the following requirements:

- Allow the user to specify the animation speed in a text field.
- Get the number of images and image’s file-name prefix from the user. For example, if the user enters \( n \) for the number of images and \( L \) for the image prefix, then the files are \( L1.gif \), \( L2.gif \), and so on, to \( Ln.gif \). Assume that the images are stored in the image directory, a subdirectory of the program’s class directory. The animation displays the images one after the other.
- Allow the user to specify an audio file URL. The audio is played while the animation runs.

**16.24 (Revise Listing 16.14 MediaDemo.java) Add a slider to enable the user to set the current time for the video and a label to display the current time and the total time for the video. As shown in Figure 16.47a, the total time is 5 minutes and 3 seconds and the current time is 3 minutes and 58 seconds. As the video plays, the slider value and current time are continuously updated.

**16.25 (Racing cars) Write a program that simulates four cars racing, as shown in Figure 16.47b. You can set the speed for each car, with maximum 100.

**16.26 (Simulation: raise flag and play anthem) Write a program that displays a flag rising up, as shown in Figure 15.14. As the national flag rises, play the national anthem. (You may use a flag image and anthem audio file from Listing 16.15.)

**Comprehensive

**16.27 (Display country flag and flag description) Listing 16.4, ComboBoxDemo.java, gives a program that lets the user view a country’s flag image and description by selecting the country from a combo box. The description is a string coded in the program. Rewrite the program to read the text description from a file. Suppose that the descriptions are stored in the files `description0.txt`, `description1.txt`, and
**16.28** *(Slide show)* Programming Exercise 15.30 developed a slide show using images. Rewrite that program to develop a slide show using text files. Suppose ten text files named *slide0.txt*, *slide1.txt*, . . . , and *slide9.txt* are stored in the *text* directory. Each slide displays the text from one file. Each slide is shown for one second, and the slides are displayed in order. When the last slide finishes, the first slide is redisplayed, and so on. Use a text area to display the slide.

**16.29** *(Display a calendar)* Write a program that displays the calendar for the current month. You can use the *Prior* and *Next* buttons to show the calendar of the previous or next month. Display the dates in the current month in black and display the dates in the previous month and next month in gray, as shown in Figure 16.48.

![Figure 16.48](image)

The program displays the calendar for the current month.

**16.30** *(Pattern recognition: consecutive four equal numbers)* Write a GUI program for Programming Exercise 8.19, as shown in Figure 16.49a–b. Let the user enter the numbers in the text fields in a grid of 6 rows and 7 columns. The user can click the *Solve* button to highlight a sequence of four equal numbers, if it exists. Initially, the values in the text fields are filled with numbers from 0 to 9 randomly.

![Figure 16.49](image)

(a) (b) (c) Clicking the *Solve* button highlights the four consecutive numbers in a row, a column, or a diagonal. (c) The program enables two players to play the connect-four game.
16.31 (Game: connect four) Programming Exercise 8.20 enables two players to play the connect-four game on the console. Rewrite a GUI version for the program, as shown in Figure 16.49c. The program enables two players to place red and yellow discs in turn. To place a disk, the player needs to click an available cell. An available cell is unoccupied and its downward neighbor is occupied. The program flashes the four winning cells if a player wins and reports no winners if all cells are occupied with no winners.
Binary I/O

Objectives

■ To discover how I/O is processed in Java (§17.2).
■ To distinguish between text I/O and binary I/O (§17.3).
■ To read and write bytes using FileInputStream and FileOutputStream (§17.4.1).
■ To filter data using the base classes FilterInputStream and FilterOutputStream (§17.4.2).
■ To read and write primitive values and strings using DataInputStream and DataOutputStream (§17.4.3).
■ To improve I/O performance by using BufferedInputStream and BufferedOutputStream (§17.4.4).
■ To write a program that copies a file (§17.5).
■ To store and restore objects using ObjectOutputStream and ObjectInputStream (§17.6).
■ To implement the Serializable interface to make objects serializable (§17.6.1).
■ To serialize arrays (§17.6.2).
■ To read and write files using the RandomAccessFile class (§17.7).
17.1 Introduction

*Java provides many classes for performing text I/O and binary I/O.*

Files can be classified as either text or binary. A file that can be processed (read, created, or modified) using a text editor such as Notepad on Windows or vi on UNIX is called a *text file*. All the other files are called *binary files*. You cannot read binary files using a text editor—they are designed to be read by programs. For example, Java source programs are text files and can be read by a text editor, but Java class files are binary files and are read by the JVM.

Although it is not technically precise and correct, you can envision a text file as consisting of a sequence of characters and a binary file as consisting of a sequence of bits. Characters in a text file are encoded using a character encoding scheme such as ASCII or Unicode. For example, the decimal integer 199 is stored as a sequence of three characters 1, 9, 9 in a text file, and the same integer is stored as a byte-type value C7 in a binary file, because decimal 199 equals hex C7 ($199 = 12 \times 16^1 + 7$). The advantage of binary files is that they are more efficient to process than text files.

Java offers many classes for performing file input and output. These can be categorized as *text I/O classes* and *binary I/O classes*. In Section 12.11, File Input and Output, you learned how to read and write strings and numeric values from/to a text file using *Scanner* and *PrintWriter*. This chapter introduces the classes for performing binary I/O.

17.2 How Is Text I/O Handled in Java?

*Text data are read using the Scanner class and written using the PrintWriter class.*

Recall that a *File* object encapsulates the properties of a file or a path but does not contain the methods for reading/writing data from/to a file. In order to perform I/O, you need to create objects using appropriate Java I/O classes. The objects contain the methods for reading/writing data from/to a file. For example, to write text to a file named *temp.txt*, you can create an object using the *PrintWriter* class as follows:

```java
PrintWriter output = new PrintWriter("temp.txt");
```

You can now invoke the *print* method on the object to write a string to the file. For example, the following statement writes *Java 101* to the file.

```java
output.print("Java 101");
```

The next statement closes the file.

```java
output.close();
```

There are many I/O classes for various purposes. In general, these can be classified as input classes and output classes. An *input class* contains the methods to read data, and an *output class* contains the methods to write data. *PrintWriter* is an example of an output class, and *Scanner* is an example of an input class. The following code creates an input object for the file *temp.txt* and reads data from the file.

```java
Scanner input = new Scanner(new File("temp.txt"));
System.out.println(input.nextLine());
```

If *temp.txt* contains the text *Java 101*, `input.nextLine()` returns the string "*Java 101". Figure 17.1 illustrates Java I/O programming. An input object reads a *stream* of data from a file, and an output object writes a stream of data to a file. An input object is also called an *input stream* and an output object an *output stream*. 
17.1 What is a text file and what is a binary file? Can you view a text file or a binary file using a text editor?

17.2 How do you read or write text data in Java? What is a stream?

17.3 Text I/O vs. Binary I/O

Binary I/O does not involve encoding or decoding and thus is more efficient than text I/O.

Computers do not differentiate between binary files and text files. All files are stored in binary format, and thus all files are essentially binary files. Text I/O is built upon binary I/O to provide a level of abstraction for character encoding and decoding, as shown in Figure 17.2a. Encoding and decoding are automatically performed for text I/O. The JVM converts Unicode to a file-specific encoding when writing a character, and it converts a file-specific encoding to Unicode when reading a character. For example, suppose you write the string "199" using text I/O to a file, each character is written to the file. Since the Unicode for character 1 is 0x0031, the Unicode 0x0031 is converted to a code that depends on the encoding scheme for the file. (Note that the prefix 0x denotes a hex number.) In the United States, the default encoding for text files on Windows is ASCII. The ASCII code for character 1 is 49 (0x31 in
hex) and for character 9 is 57 (0x39 in hex). Thus, to write the characters 199, three bytes—0x31, 0x39, and 0x39—are sent to the output, as shown in Figure 17.2a.

Binary I/O does not require conversions. If you write a numeric value to a file using binary I/O, the exact value in the memory is copied into the file. For example, a byte-type value 199 is represented as 0xC7 (199 = 12 * 16 + 7) in the memory and appears exactly as 0xC7 in the file, as shown in Figure 17.2b. When you read a byte using binary I/O, one byte value is read from the input.

In general, you should use text input to read a file created by a text editor or a text output program, and use binary input to read a file created by a Java binary output program.

Binary I/O is more efficient than text I/O, because binary I/O does not require encoding and decoding. Binary files are independent of the encoding scheme on the host machine and thus are portable. Java programs on any machine can read a binary file created by a Java program. This is why Java class files are binary files. Java class files can run on a JVM on any machine.

Note
For consistency, this book uses the extension .txt to name text files and .dat to name binary files.

17.3 What are the differences between text I/O and binary I/O?
17.4 How is a Java character represented in the memory, and how is a character represented in a text file?
17.5 If you write the string "ABC" to an ASCII text file, what values are stored in the file?
17.6 If you write the string "100" to an ASCII text file, what values are stored in the file?
   If you write a numeric byte-type value 100 using binary I/O, what values are stored in the file?
17.7 What is the encoding scheme for representing a character in a Java program? By default, what is the encoding scheme for a text file on Windows?

17.4 Binary I/O Classes

The abstract InputStream is the root class for reading binary data, and the abstract OutputStream is the root class for writing binary data.

The design of the Java I/O classes is a good example of applying inheritance, where common operations are generalized in superclasses, and subclasses provide specialized operations. Figure 17.3 lists some of the classes for performing binary I/O. InputStream is the root for...
17.4 Binary I/O Classes

17.4.1 FileInputStream/FileOutputStream

FileInputStream/FileOutputStream is for reading/writing bytes from/to files. All the methods in these classes are inherited from InputStream and OutputStream. FileInputStream/FileOutputStream does not introduce new methods. To construct a FileInputStream, use the constructors shown in Figure 17.6.

A java.io.FileNotFoundException will occur if you attempt to create a FileInputStream with a nonexistent file.

To construct a FileOutputStream, use the constructors shown in Figure 17.7. If the file does not exist, a new file will be created. If the file already exists, the first two constructors will delete the current content of the file. To retain the current content and append new data into the file, use the last two constructors and pass true to the append parameter.

Note
All the methods in the binary I/O classes are declared to throw java.io.IOException or a subclass of java.io.IOException.

throws IOException
Almost all the methods in the I/O classes throw `java.io.IOException`. Therefore, you have to declare to throw `java.io.IOException` in the method or place the code in a try-catch block, as shown below:

```java
import java.io.*;

public class TestFileStream {
    public static void main(String[] args) throws IOException {
        try {
            FileOutputStream output = new FileOutputStream("temp.dat");
            for (int i = 1; i <= 10; i++)
                output.write(i);
        } catch (IOException ex) {
            ex.printStackTrace();
        }
    }
}
```

Listing 17.1 uses binary I/O to write ten byte values from 1 to 10 to a file named `temp.dat` and reads them back from the file.

Listing 17.1 TestFileStream.java

```java
import java.io.*;

public class TestFileStream {
    public static void main(String[] args) throws IOException {
        try {
            FileOutputStream output = new FileOutputStream("temp.dat");
            for (int i = 1; i <= 10; i++)
                output.write(i);
        }
```
17.4 Binary I/O Classes

```java
// Create an input stream for the file
FileInputStream input = new FileInputStream("temp.dat");

// Read values from the file
int value;
while ((value = input.read()) != -1) {
    System.out.print(value + " ");
}
```

The program uses the try-with-resources to declare and create input and output streams so that they will be automatically closed after they are used. The `java.io.InputStream` and `java.io.OutputStream` classes implement the `AutoClosable` interface. The `AutoClosable` interface defines the `close()` method that closes a resource. Any object of the `AutoClosable` type can be used with the try-with-resources syntax for automatic closing.

A `FileOutputStream` is created for the file `temp.dat` in line 7. The `for` loop writes ten byte values into the file (lines 10–11). Invoking `write(i)` is the same as invoking `write((byte)i)`. Line 16 creates a `FileInputStream` for the file `temp.dat`. Values are read from the file and displayed on the console in lines 19–21. The expression `((value = input.read()) != -1)` (line 20) reads a byte from `input.read()`, assigns it to `value`, and checks whether it is `-1`. The input value of `-1` signifies the end of a file.

The file `temp.dat` created in this example is a binary file. It can be read from a Java program but not from a text editor, as shown in Figure 17.8.

![Binary data](image)

**Figure 17.8** A binary file cannot be displayed in text mode.

**Tip**
When a stream is no longer needed, always close it using the `close()` method or automatically close it using a try-with-resource statement. Not closing streams may cause data corruption in the output file, or other programming errors.

**Note**
The root directory for the file is the classpath directory. For the example in this book, the root directory is `c:\book`, so the file `temp.dat` is located at `c:\book`. If you wish to place `temp.dat` in a specific directory, replace line 6 with

```java
FileOutputStream output =
    new FileOutputStream ("directory/temp.dat");
```

**Note**
An instance of `FileInputStream` can be used as an argument to construct a `Scanner`, and an instance of `FileOutputStream` can be used as an argument to construct a `PrintWriter`. You can create a `PrintWriter` to append text into a file using

```java
FileOutputStream output =
    new FileOutputStream ("directory/temp.dat");
```
new PrintWriter(new FileOutputStream("temp.txt", true));

If temp.txt does not exist, it is created. If temp.txt already exists, new data are appended to the file.

17.4.2 FilterInputStream/FilterOutputStream

Filter streams are streams that filter bytes for some purpose. The basic byte input stream provides a read method that can be used only for reading bytes. If you want to read integers, doubles, or strings, you need a filter class to wrap the byte input stream. Using a filter class enables you to read integers, doubles, and strings instead of bytes and characters. FilterInputStream and FilterOutputStream are the base classes for filtering data. When you need to process primitive numeric types, use DataInputStream and DataOutputStream to filter bytes.

17.4.3 DataInputStream/DataOutputStream

DataInputStream reads bytes from the stream and converts them into appropriate primitive-type values or strings. DataOutputStream converts primitive-type values or strings into bytes and outputs the bytes to the stream.

DataInputStream extends FilterInputStream and implements the DataInput interface, as shown in Figure 17.9. DataOutputStream extends FilterOutputStream and implements the DataOutput interface, as shown in Figure 17.10.

**FIGURE 17.9** DataInputStream filters an input stream of bytes into primitive data-type values and strings.

<table>
<thead>
<tr>
<th>DataInputStream</th>
<th>DataOutputStream</th>
</tr>
</thead>
<tbody>
<tr>
<td>+readBoolean(): boolean</td>
<td>+writeBoolean(): boolean</td>
</tr>
<tr>
<td>+readByte(): byte</td>
<td>+writeByte(): byte</td>
</tr>
<tr>
<td>+readChar(): char</td>
<td>+writeChar(): char</td>
</tr>
<tr>
<td>+readFloat(): float</td>
<td>+writeFloat(): float</td>
</tr>
<tr>
<td>+readDouble(): double</td>
<td>+writeDouble(): double</td>
</tr>
<tr>
<td>+readInt(): int</td>
<td>+writeInt(): int</td>
</tr>
<tr>
<td>+readLong(): long</td>
<td>+writeLong(): long</td>
</tr>
<tr>
<td>+readShort(): short</td>
<td>+writeShort(): short</td>
</tr>
<tr>
<td>+readLine(): String</td>
<td>+writeBytes(): String</td>
</tr>
<tr>
<td>+readUTF(): String</td>
<td></td>
</tr>
</tbody>
</table>

Reads a Boolean from the input stream. Reads a byte from the input stream. Reads a character from the input stream. Reads a float from the input stream. Reads a double from the input stream. Reads an int from the input stream. Reads a long from the input stream. Reads a short from the input stream. Reads a line of characters from input. Reads a string in UTF format.

DataInputStream implements the methods defined in the DataInput interface to read primitive data-type values and strings. DataOutputStream implements the methods defined in the DataOutput interface to write primitive data-type values and strings. Primitive values are copied from memory to the output without any conversions. Characters in a string may be written in several ways, as discussed in the next section.

Characters and Strings in Binary I/O

A Unicode character consists of two bytes. The writeChar(char c) method writes the Unicode of character c to the output. The writeChars(String s) method writes the Unicode for each character in the string s to the output. The writeBytes(String s) method writes the lower byte of the Unicode for each character in the string s to the output. The high byte of the Unicode is discarded. The writeBytes method is suitable for strings that consist
of ASCII characters, since an ASCII code is stored only in the lower byte of a Unicode. If a string consists of non-ASCII characters, you have to use the `writeChars` method to write the string.

The `writeUTF(String s)` method writes two bytes of length information to the output stream, followed by the modified UTF-8 representation of every character in the string `s`. UTF-8 is a coding scheme that allows systems to operate with both ASCII and Unicode. Most operating systems use ASCII. Java uses Unicode. The ASCII character set is a subset of the Unicode character set. Since most applications need only the ASCII character set, it is a waste to represent an 8-bit ASCII character as a 16-bit Unicode character. The modified UTF-8 scheme stores a character using one, two, or three bytes. Characters are coded in one byte if their code is less than or equal to `0x7F`, in two bytes if their code is greater than `0x7F` and less than or equal to `0x7FF`, or in three bytes if their code is greater than `0x7FF`.

The initial bits of a UTF-8 character indicate whether a character is stored in one byte, two bytes, or three bytes. If the first bit is `0`, it is a one-byte character. If the first bits are `110`, it is the first byte of a two-byte sequence. If the first bits are `1110`, it is the first byte of a three-byte sequence. The information that indicates the number of characters in a string is stored in the first two bytes preceding the UTF-8 characters. For example, `writeUTF("ABCDEF")` actually writes eight bytes (i.e., `00 06 41 42 43 44 45 46`) to the file, because the first two bytes store the number of characters in the string.

The `writeUTF(String s)` method converts a string into a series of bytes in the UTF-8 format and writes them into an output stream. The `readUTF()` method reads a string that has been written using the `writeUTF` method.

The UTF-8 format has the advantage of saving a byte for each ASCII character, because a Unicode character takes up two bytes and an ASCII character in UTF-8 only one byte. If most of the characters in a long string are regular ASCII characters, using UTF-8 is more efficient.

Creating `DataInputStream/DataOutputStream`

`DataInputStream/DataOutputStream` are created using the following constructors (see Figures 17.9 and 17.10):

```java
public DataInputStream(InputStream instream)
public DataOutputStream(OutputStream outstream)
```
The following statements create data streams. The first statement creates an input stream for the file \texttt{in.dat}; the second statement creates an output stream for the file \texttt{out.dat}.

\begin{verbatim}
DataInputStream input =
    new DataInputStream(new FileInputStream("in.dat"));
DataOutputStream output =
    new DataOutputStream(new FileOutputStream("out.dat"));
\end{verbatim}

Listing 17.2 writes student names and scores to a file named \texttt{temp.dat} and reads the data back from the file.

\textbf{Listing 17.2} \hspace{1em} \texttt{TestDataStream.java}

\begin{verbatim}
import java.io.*;

public class TestDataStream {
    public static void main(String[] args) throws IOException {
        try { // Create an output stream for file temp.dat
            DataOutputStream output =
                new DataOutputStream(new FileOutputStream("temp.dat"));
            // Write student test scores to the file
            output.writeUTF("John");
            output.writeDouble(85.5);
            output.writeUTF("Jim");
            output.writeDouble(185.5);
            output.writeUTF("George");
            output.writeDouble(105.25);
        }
        try { // Create an input stream for file temp.dat
            DataInputStream input =
                new DataInputStream(new FileInputStream("temp.dat"));
            // Read student test scores from the file
            System.out.println(input.readUTF() + " " + input.readDouble());
            System.out.println(input.readUTF() + " " + input.readDouble());
            System.out.println(input.readUTF() + " " + input.readDouble());
        }
    }
}
\end{verbatim}

A \texttt{DataOutputStream} is created for file \texttt{temp.dat} in lines 6 and 7. Student names and scores are written to the file in lines 10–15. A \texttt{DataInputStream} is created for the same file in lines 19–20. Student names and scores are read back from the file and displayed on the console in lines 23–25.

\texttt{DataInputStream} and \texttt{DataOutputStream} read and write Java primitive-type values and strings in a machine-independent fashion, thereby enabling you to write a data file on one machine and read it on another machine that has a different operating system or file structure. An application uses a data output stream to write data that can later be read by a program using a data input stream.

\texttt{DataInputStream} filters data from an input stream into appropriate primitive-type values or strings. \texttt{DataOutputStream} converts primitive-type values or strings into bytes and
outputs the bytes to an output stream. You can view `DataInputStream/FileInputStream` and `DataOutputStream/FileOutputStream` working in a pipe line as shown in Figure 17.11.

```
    DataInputStream  FileInputStream   External File
                     int, double, string ...  01000110011 ...

    DataOutputStream FileOutputStream External File
                     int, double, string ...  01000110011 ...
```

**FIGURE 17.11** `DataInputStream` filters an input stream of byte to data and `DataOutputStream` converts data into a stream of bytes.

**Caution**
You have to read data in the same order and format in which they are stored. For example, since names are written in UTF-8 using `writeUTF`, you must read names using `readUTF`.

**Detecting the End of a File**
If you keep reading data at the end of an `InputStream`, an `EOFException` will occur. This exception can be used to detect the end of a file, as shown in Listing 17.3.

**Listing 17.3** DetectEndOfFile.java

```java
import java.io.*;

public class DetectEndOfFile {
    public static void main(String[] args) {
        try {
            try (DataOutputStream output =
                     new DataOutputStream(new FileOutputStream("test.dat"))) {
                output.writeDouble(4.5);
                output.writeDouble(43.25);
                output.writeDouble(3.2);
            }
            try (DataInputStream input =
                     new DataInputStream(new FileInputStream("test.dat"))) {
                while (true)
                    System.out.println(input.readDouble());
            }
        } catch (EOFException ex) {
            System.out.println("All data were read");
        } catch (IOException ex) {
            ex.printStackTrace();
        }
    }
}
```
The program writes three double values to the file using `DataOutputStream` (lines 6–11) and reads the data using `DataInputStream` (lines 13–17). When reading past the end of the file, an `EOFException` is thrown. The exception is caught in line 19.

### 17.4.4 BufferedInputStream/BufferedOutputStream

`BufferedInputStream/BufferedOutputStream` can be used to speed up input and output by reducing the number of disk reads and writes. Using `BufferedInputStream`, the whole block of data on the disk is read into the buffer in the memory once. The individual data are then delivered to your program from the buffer, as shown in Figure 17.12a. Using `BufferedOutputStream`, the individual data are first written to the buffer in the memory. When the buffer is full, all data in the buffer are written to the disk once, as shown in Figure 17.12b.

**Figure 17.12** Buffer I/O places data in a buffer for fast processing.

*BufferedInputStream/BufferedOutputStream* does not contain new methods. All the methods in `BufferedInputStream/BufferedOutputStream` are inherited from the `InputStream/OutputStream` classes. `BufferedInputStream/BufferedOutputStream` manages a buffer behind the scene and automatically reads/writes data from/to disk on demand.

You can wrap a `BufferedInputStream/BufferedOutputStream` on any `InputStream/OutputStream` using the constructors shown in Figures 17.13 and 17.14.

**Figure 17.13** `BufferedInputStream` buffers an input stream.
If no buffer size is specified, the default size is 512 bytes. You can improve the performance of the `TestDataStream` program in Listing 17.2 by adding buffers in the stream in lines 6–7 and lines 19–20, as follows:

```java
DataOutputStream output = new DataOutputStream(new BufferedOutputStream(new FileOutputStream("temp.dat")));
DataInputStream input = new DataInputStream(new BufferedInputStream(new FileInputStream("temp.dat")));
```

**Tip**
You should always use buffered I/O to speed up input and output. For small files, you may not notice performance improvements. However, for large files—over 100 MB—you will see substantial improvements using buffered I/O.

17.8 Why do you have to declare to throw `IOException` in the method or use a try-catch block to handle `IOException` for Java I/O programs?

17.9 Why should you always close streams? How do you close streams?

17.10 The `read()` method in `InputStream` reads a byte. Why does it return an `int` instead of a `byte`? Find the abstract methods in `InputStream` and `OutputStream`.

17.11 Does `FileInputStream/FileOutputStream` introduce any new methods beyond the methods inherited from `InputStream/OutputStream`? How do you create a `FileInputStream/FileOutputStream`?

17.12 What will happen if you attempt to create an input stream on a nonexistent file? What will happen if you attempt to create an output stream on an existing file? Can you append data to an existing file?

17.13 How do you append data to an existing text file using `java.io.PrintWriter`?

17.14 Suppose a file contains an unspecified number of `double` values that were written to the file using the `writeDouble` method using a `DataOutputStream`, how do you write a program to read all these values? How do you detect the end of a file?

17.15 What is written to a file using `writeByte(91)` on a `FileOutputStream`?

17.16 How do you check the end of a file in an input stream (`FileInputStream`, `DataInputStream`)?

17.17 What is wrong in the following code?

```java
import java.io.*;

public class Test {
```
public static void main(String[] args) {
    try {
        FileInputStream fis = new FileInputStream("test.dat");
    } catch (IOException ex) {
        ex.printStackTrace();
    } catch (FileNotFoundException ex) {
        ex.printStackTrace();
    }
}

17.18 Suppose you run the following program on Windows using the default ASCII encoding after the program is finished, how many bytes are there in the file t.txt? Show the contents of each byte.

public class Test {
    public static void main(String[] args) throws IOException {
        try (java.io.PrintWriter output = new java.io.PrintWriter("t.txt");) {
            output.printf("%s", "1234");
            output.printf("%s", "5678");
            output.close();
        }
    }
}

17.19 After the following program is finished, how many bytes are there in the file t.dat? Show the contents of each byte.

import java.io.*;

public class Test {
    public static void main(String[] args) throws IOException {
        try (DataOutputStream output = new DataOutputStream(new FileOutputStream("t.dat");) {
            output.writeInt(1234);
            output.writeInt(5678);
            output.close();
        }
    }
}

17.20 For each of the following statements on a DataOutputStream output, how many bytes are sent to the output?

output.writeChar('A');
output.writeChars("BC");
output.writeUTF("DEF");

17.21 What are the advantages of using buffered streams? Are the following statements correct?

BufferedInputStream input1 = new BufferedInputStream(new FileInputStream("t.dat"););
DataInputStream input2 = new DataInputStream(new BufferedInputStream(new FileInputStream("t.dat");));
DataOutputStream output = new DataOutputStream(new BufferedOutputStream(new FileOutputStream("t.dat");));
17.5 Case Study: Copying Files

This section develops a useful utility for copying files.

In this section, you will learn how to write a program that lets users copy files. The user needs to provide a source file and a target file as command-line arguments using the command:

```
java Copy source target
```

The program copies the source file to the target file and displays the number of bytes in the file. The program should alert the user if the source file does not exist or if the target file already exists. A sample run of the program is shown in Figure 17.15.

![Figure 17.15](image)

**Figure 17.15** The program copies a file.

To copy the contents from a source file to a target file, it is appropriate to use an input stream to read bytes from the source file and an output stream to send bytes to the target file, regardless of the file’s contents. The source file and the target file are specified from the command line. Create an `InputStream` for the source file and an `OutputStream` for the target file. Use the `read()` method to read a byte from the input stream, and then use the `write(b)` method to write the byte to the output stream. Use `BufferedInputStream` and `BufferedOutputStream` to improve the performance. Listing 17.4 gives the solution to the problem.

**Listing 17.4 Copy.java**

```java
import java.io.*;

public class Copy {

    /** Main method */
    public static void main(String[] args) throws IOException {

        // Check command-line parameter usage
        if (args.length != 2) {
            System.out.println("Usage: java Copy sourceFile targetFile");
            System.exit(1);
        }

        // Check if source file exists
        File sourceFile = new File(args[0]);
        if (!sourceFile.exists()) {
            System.out.println("Source file " + args[0] + " does not exist");
        } else {
            // Read source file
            FileInputStream source = new FileInputStream(sourceFile);
            int b;
            while ((b = source.read()) >= 0) {
                // Write to target file
                FileOutputStream target = new FileOutputStream(args[1]);
                target.write(b);
                target.close();
                source.close();
            }
        }
    }
}
```
System.exit(2);

// Check if target file exists
File targetFile = new File(args[1]);
if (targetFile.exists()) {
    System.out.println("Target file " + args[1] + " already exists");
    System.exit(3);
}

try {
    // Create an input stream
    BufferedInputStream input = new BufferedInputStream(new FileInputStream(sourceFile));

    // Create an output stream
    BufferedOutputStream output = new BufferedOutputStream(new FileOutputStream(targetFile));

    // Continuously read a byte from input and write it to output
    int r, numberOfBytesCopied = 0;
    while ((r = input.read()) != -1) {
        output.write((byte)r);
        numberOfBytesCopied++;
    }

    // Display the file size
    System.out.println(numberOfBytesCopied + " bytes copied");
} 

The program first checks whether the user has passed the two required arguments from the command line in lines 10–14.

The program uses the File class to check whether the source file and target file exist. If the source file does not exist (lines 18–22) or if the target file already exists (lines 25–30), the program ends.

An input stream is created using BufferedInputStream wrapped on FileInputStream in lines 34 and 35, and an output stream is created using BufferedOutputStream wrapped on FileOutputStream in lines 38 and 39.

The expression ((r = input.read()) != -1) (line 43) reads a byte from input.read(), assigns it to r, and checks whether it is -1. The input value of -1 signifies the end of a file. The program continuously reads bytes from the input stream and sends them to the output stream until all of the bytes have been read.

17.22 How does the program check if a file already exists?
17.23 How does the program detect the end of the file while reading data?
17.24 How does the program count the number of bytes read from the file?

17.6 Object I/O

ObjectInputStream/ObjectOutputStream classes can be used to read/write serializable objects.

DataInputStream/DataOutputStream enables you to perform I/O for primitive-type values and strings. ObjectInputStream/ObjectOutputStream enables you to perform I/O
for objects in addition to primitive-type values and strings. Since `ObjectInputStream/ObjectOutputStream` contains all the functions of `DataInputStream/DataOutputStream`, you can replace `DataInputStream/DataOutputStream` completely with `ObjectInputStream/ObjectOutputStream`.

`ObjectInputStream` extends `InputStream` and implements `ObjectInput` and `ObjectStreamConstants`, as shown in Figure 17.16. `ObjectInput` is a subinterface of `DataInput` (`DataInput` is shown in Figure 17.9). `ObjectStreamConstants` contains the constants to support `ObjectInputStream/ObjectOutputStream`.

**FIGURE 17.16** `ObjectInputStream` can read objects, primitive-type values, and strings.

`ObjectOutputStream` extends `OutputStream` and implements `ObjectOutput` and `ObjectStreamConstants`, as shown in Figure 17.17. `ObjectOutput` is a subinterface of `DataOutput` (`DataOutput` is shown in Figure 17.10).

**FIGURE 17.17** `ObjectOutputStream` can write objects, primitive-type values, and strings.

You can wrap an `ObjectInputStream/ObjectOutputStream` on any `InputStream/OutputStream` using the following constructors:

```java
// Create an ObjectInputStream
public ObjectInputStream(InputStream in)

// Create an ObjectOutputStream
public ObjectOutputStream(OutputStream out)
```

Listing 17.5 writes student names, scores, and the current date to a file named `object.dat`.

**LISTING 17.5** `TestObjectOutputStream.java`

```java
1 import java.io.*;
2
3 public class TestObjectOutputStream {
```
Chapter 17  Binary I/O

```java
public static void main(String[] args) throws IOException {
    try { // Create an output stream for file object.dat
        ObjectOutputStream output =
            new ObjectOutputStream(new FileOutputStream("object.dat"));
        // Write a string, double value, and object to the file
        output.writeUTF("John");
        output.writeDouble(85.5);
        output.writeObject(new java.util.Date());
    }
}
```

An ObjectOutputStream is created to write data into the file object.dat in lines 6 and 7. A string, a double value, and an object are written to the file in lines 10–12. To improve performance, you may add a buffer in the stream using the following statement to replace lines 6 and 7:

```java
ObjectOutputStream output =
    new ObjectOutputStream(new BufferedOutputStream(
        new FileOutputStream("object.dat")));
```

Multiple objects or primitives can be written to the stream. The objects must be read back from the corresponding ObjectInputStream with the same types and in the same order as they were written. Java’s safe casting should be used to get the desired type. Listing 17.6 reads data from object.dat.

**LISTING 17.6  TestObjectInputStream.java**

```java
import java.io.*;

public class TestObjectInputStream {
    public static void main(String[] args)
        throws ClassNotFoundException, IOException {
        try { // Create an input stream for file object.dat
            ObjectInputStream input =
                new ObjectInputStream(new FileInputStream("object.dat"));
            // Read a string, double value, and object from the file
            String name = input.readUTF();
            double score = input.readDouble();
            java.util.Date date = (java.util.Date)(input.readObject());
            System.out.println(name + " " + score + " " + date);
        }
    }
}
```

The readObject() method may throw java.lang.ClassNotFoundException, because when the JVM restores an object, it first loads the class for the object if the class has not been loaded. Since ClassNotFoundException is a checked exception, the main method declares to throw it in line 5. An ObjectInputStream is created to read input from object.dat in lines 7 and 8. You have to read the data from the file in the same order and format as they were written to the file. A string, a double value, and an object are read in lines 11–13. Since readObject() returns an Object, it is cast into Date and assigned to a Date variable in line 13.
17.6 Object I/O

17.6.1 The Serializable Interface

Not every object can be written to an output stream. Objects that can be so written are said to be **serializable**. A serializable object is an instance of the `java.io.Serializable` interface, so the object’s class must implement `Serializable`.

The `Serializable` interface is a marker interface. Since it has no methods, you don’t need to add additional code in your class that implements `Serializable`. Implementing this interface enables the Java serialization mechanism to automate the process of storing objects and arrays.

To appreciate this automation feature, consider what you otherwise need to do in order to store an object. Suppose you wish to store an `ArrayList` object. To do this you need to store all the elements in the list. Each element is an object that may contain other objects. As you can see, this would be a very tedious process. Fortunately, you don’t have to go through it manually. Java provides a built-in mechanism to automate the process of writing objects. This process is referred as **object serialization**, which is implemented in `ObjectOutputStream`. In contrast, the process of reading objects is referred as **object deserialization**, which is implemented in `ObjectInputStream`.

Many classes in the Java API implement `Serializable`. All the wrapper classes for primitive type values, `java.math.BigInteger`, `java.math.BigDecimal`, `java.lang.String`, `java.lang.StringBuilder`, `java.lang.StringBuffer`, `java.util.Date`, and `java.util.ArrayList` implement `java.io.Serializable`. Attempting to store an object that does not support the `Serializable` interface would cause a `NotSerializableException`.

When a serializable object is stored, the class of the object is encoded; this includes the class name and the signature of the class, the values of the object’s instance variables, and the closure of any other objects referenced by the object. The values of the object’s static variables are not stored.

**Note**

**Nonserializable fields**

If an object is an instance of `Serializable` but contains nonserializable instance data fields, can it be serialized? The answer is no. To enable the object to be serialized, mark these data fields with the `transient` keyword to tell the JVM to ignore them when writing the object to an object stream. Consider the following class:

```java
public class C implements java.io.Serializable {
    private int v1;
    private static double v2;
    private transient A v3 = new A();
}

class A { }  // A is not serializable
```

When an object of the `C` class is serialized, only variable `v1` is serialized. Variable `v2` is not serialized because it is a static variable, and variable `v3` is not serialized because it is marked `transient`. If `v3` were not marked `transient`, a `java.io.NotSerializableException` would occur.

**Note**

**Duplicate objects**

If an object is written to an object stream more than once, will it be stored in multiple copies? No, it will not. When an object is written for the first time, a serial number is created for it. The JVM writes the complete contents of the object along with the serial number into the object stream. After the first time, only the serial number is stored if the
same object is written again. When the objects are read back, their references are the same since only one object is actually created in the memory.

### 17.6.2 Serializing Arrays

An array is serializable if all its elements are serializable. An entire array can be saved into a file using `writeObject` and later can be restored using `readObject`. Listing 17.7 stores an array of five `int` values and an array of three strings and reads them back to display on the console.

#### Listing 17.7 TestObjectStreamForArray.java

```java
import java.io.*;

public class TestObjectStreamForArray {
    public static void main(String[] args) throws ClassNotFoundException, IOException {
        int[] numbers = {1, 2, 3, 4, 5};
        String[] strings = {"John", "Susan", "Kim"};

        try (ObjectOutputStream output = new ObjectOutputStream(new FileOutputStream("array.dat"), true)) {
            output.writeObject(numbers);
            output.writeObject(strings);
        }

        try (ObjectInputStream input = new ObjectInputStream(new FileInputStream("array.dat"))) {
            int[] newNumbers = (int[])(input.readObject());
            String[] newStrings = (String[])(input.readObject());

            // Display arrays
            for (int i = 0; i < newNumbers.length; i++)
                System.out.print(newNumbers[i] + " ");
            System.out.println();
            for (int i = 0; i < newStrings.length; i++)
                System.out.print(newStrings[i] + " ");
        }
    }
}
```

Lines 14 and 15 write two arrays into file `array.dat`. Lines 22 and 23 read two arrays back in the same order they were written. Since `readObject()` returns `Object`, casting is used to cast the objects into `int[]` and `String[]`.

### Check Point

17.25 What types of objects can be stored using the `ObjectOutputStream`? What is the method for writing an object? What is the method for reading an object? What is the return type of the method that reads an object from `ObjectInputStream`?
17.26 If you serialize two objects of the same type, will they take the same amount of space? If not, give an example.

17.27 Is it true that any instance of `java.io.Serializable` can be successfully serialized? Are the static variables in an object serialized? How do you mark an instance variable not to be serialized?

17.28 Can you write an array to an `ObjectOutputStream`?

17.29 Is it true that `DataInputStream/DataOutputStream` can always be replaced by `ObjectInputStream/ObjectOutputStream`?

17.30 What will happen when you attempt to run the following code?

```java
import java.io.*;

public class Test {
    public static void main(String[] args) throws IOException {
        try (ObjectOutputStream output = new ObjectOutputStream(new FileOutputStream("object.dat"))) {
            output.writeObject(new A());
        }
    }
}

class A implements Serializable {
    B b = new B();
}

class B {
}
```

17.7 Random-Access Files

Java provides the `RandomAccessFile` class to allow data to be read from and written to at any locations in the file.

All of the streams you have used so far are known as read-only or write-only streams. These streams are called sequential streams. A file that is opened using a sequential stream is called a sequential-access file. The contents of a sequential-access file cannot be updated. However, it is often necessary to modify files. Java provides the `RandomAccessFile` class to allow data to be read from and written to at any locations in a file. A file that is opened using the `RandomAccessFile` class is known as a random-access file.

The `RandomAccessFile` class implements the `DataInput` and `DataOutput` interfaces, as shown in Figure 17.18. The `DataInput` interface (see Figure 17.9) defines the methods for reading primitive-type values and strings (e.g., `readInt`, `readDouble`, `readChar`, `readBoolean`, `readUTF`) and the `DataOutput` interface (see Figure 17.10) defines the methods for writing primitive-type values and strings (e.g., `writeInt`, `writeDouble`, `writeChar`, `writeBoolean`, `writeUTF`).

When creating a `RandomAccessFile`, you can specify one of two modes: r or rw. Mode r means that the stream is read-only, and mode rw indicates that the stream allows both read and write. For example, the following statement creates a new stream, `raf`, that allows the program to read from and write to the file `test.dat`:

```java
RandomAccessFile raf = new RandomAccessFile("test.dat", "rw");
```

If `test.dat` already exists, `raf` is created to access it; if `test.dat` does not exist, a new file named `test.dat` is created, and `raf` is created to access the new file. The method `raf.length()` returns the number of bytes in `test.dat` at any given time. If you append new data into the file, `raf.length()` increases.
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If the file is not intended to be modified, open it with the r mode. This prevents unintentional modification of the file.

A random-access file consists of a sequence of bytes. A special marker called a file pointer is positioned at one of these bytes. A read or write operation takes place at the location of the file pointer. When a file is opened, the file pointer is set at the beginning of the file. When you read or write data to the file, the file pointer moves forward to the next data item. For example, if you read an int value using readInt(), the JVM reads 4 bytes from the file pointer, and now the file pointer is 4 bytes ahead of the previous location, as shown in Figure 17.19.

For a RandomAccessFile raf, you can use the raf.seek(position) method to move the file pointer to a specified position. raf.seek(0) moves it to the beginning of the file, and raf.seek(raf.length()) moves it to the end of the file. Listing 17.8 demonstrates...
RandomAccessFile. A large case study of using RandomAccessFile to organize an address book is given in Supplement VI.D.

**Listing 17.8 TestRandomAccessFile.jav**

```
import java.io.*;

public class TestRandomAccessFile {
  public static void main(String[] args) throws IOException {
    try (RandomAccessFile inout = new RandomAccessFile("inout.dat", "rw");) {
      // Clear the file to destroy the old contents if exists
      inout.setLength(0);

      // Write new integers to the file
      for (int i = 0; i < 200; i++)
        inout.writeInt(i);

      // Display the current length of the file
      System.out.println("Current file length is " + inout.length());

      // Retrieve the first number
      inout.seek(0); // Move the file pointer to the beginning
      System.out.println("The first number is " + inout.readInt());

      // Retrieve the second number
      inout.seek(1 * 4); // Move the file pointer to the second number
      System.out.println("The second number is " + inout.readInt());

      // Retrieve the tenth number
      inout.seek(9 * 4); // Move the file pointer to the tenth number
      System.out.println("The tenth number is " + inout.readInt());

      // Modify the eleventh number
      inout.writeInt(555);

      // Append a new number
      inout.seek(inout.length()); // Move the file pointer to the end
      inout.writeInt(999);

      // Display the new length
      System.out.println("The new length is " + inout.length());

      // Retrieve the new eleventh number
      inout.seek(10 * 4); // Move the file pointer to the eleventh number
      System.out.println("The eleventh number is " + inout.readInt());
    }
  }
}
```

Current file length is 800
The first number is 0
The second number is 1
The tenth number is 9
The new length is 804
The eleventh number is 555
A RandomAccessFile is created for the file named inout.dat with mode rw to allow both read and write operations in line 6.

inout.setLength(0) sets the length to 0 in line 9. This, in effect, destroys the old contents of the file.

The for loop writes 200 int values from 0 to 199 into the file in lines 12 and 13. Since each int value takes 4 bytes, the total length of the file returned from inout.length() is now 800 (line 16), as shown in the sample output.

Invoking inout.seek(0) in line 19 sets the file pointer to the beginning of the file. inout.readInt() reads the first value in line 20 and moves the file pointer to the next number. The second number is read in line 24.

inout.seek(9 * 4) (line 27) moves the file pointer to the tenth number. inout.readInt() reads the tenth number and moves the file pointer to the eleventh number in line 28. inout.writeInt(555) writes a new eleventh number at the current position (line 31). The previous eleventh number is destroyed.

inout.seek(inout.length()) moves the file pointer to the end of the file (line 34). inout.writeInt(999) writes a 999 to the file (line 35). Now the length of the file is increased by 4, so inout.length() returns 804 (line 38).

inout.seek(10 * 4) moves the file pointer to the eleventh number in line 41. The new eleventh number, 555, is displayed in line 42.

17.31 Can RandomAccessFile streams read and write a data file created by DataOutputStream? Can RandomAccessFile streams read and write objects?

17.32 Create a RandomAccessFile stream for the file address.dat to allow the updating of student information in the file. Create a DataOutputStream for the file address.dat. Explain the differences between these two statements.

17.33 What happens if the file test.dat does not exist when you attempt to compile and run the following code?

```java
import java.io.*;

public class Test {
    public static void main(String[] args) {
        try (RandomAccessFile raf = new RandomAccessFile("test.dat", "r")) {
            int i = raf.readInt();
        }
        catch (IOException ex) {
            System.out.println("IO exception");
        }
    }
}
```

**Key Terms**

<table>
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<th>binary I/O</th>
<th>678</th>
</tr>
</thead>
<tbody>
<tr>
<td>deserialization</td>
<td>695</td>
</tr>
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<td>file pointer</td>
<td>698</td>
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<td>random-access file</td>
<td>697</td>
</tr>
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<td>sequential-access file</td>
<td>697</td>
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<td>serialization</td>
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</table>
CHAPTER SUMMARY

1. I/O can be classified into text I/O and binary I/O. Text I/O interprets data in sequences of characters. Binary I/O interprets data as raw binary values. How text is stored in a file depends on the encoding scheme for the file. Java automatically performs encoding and decoding for text I/O.

2. The InputStream and OutputStream classes are the roots of all binary I/O classes. FileInputStream/FileOutputStream associates a file for input/output. BufferedInputStream/BufferedOutputStream can be used to wrap any binary I/O stream to improve performance. DataInputStream/DataOutputStream can be used to read/write primitive values and strings.

3. ObjectInputStream/ObjectOutputStream can be used to read/write objects in addition to primitive values and strings. To enable object serialization, the object’s defining class must implement the java.io.Serializable marker interface.

4. The RandomAccessFile class enables you to read and write data to a file. You can open a file with the r mode to indicate that it is read-only or with the rw mode to indicate that it is updateable. Since the RandomAccessFile class implements DataInput and DataOutput interfaces, many methods in RandomAccessFile are the same as those in DataInputStream and DataOutputStream.

QUIZ

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

PROGRAMMING EXERCISES

Section 17.3

*17.1 (Create a text file) Write a program to create a file named Exercise17_01.txt if it does not exist. Append new data to it if it already exists. Write 100 integers created randomly into the file using text I/O. Integers are separated by a space.

Section 17.4

*17.2 (Create a binary data file) Write a program to create a file named Exercise17_02.dat if it does not exist. Append new data to it if it already exists. Write 100 integers created randomly into the file using binary I/O.

*17.3 (Sum all the integers in a binary data file) Suppose a binary data file named Exercise17_03.dat has been created and its data are created using writeInt(int) in DataOutputStream. The file contains an unspecified number of integers. Write a program to find the sum of the integers.

*17.4 (Convert a text file into UTF) Write a program that reads lines of characters from a text file and writes each line as a UTF-8 string into a binary file. Display the sizes of the text file and the binary file. Use the following command to run the program:

    java Exercise17_04 Welcome.java Welcome.utf
Section 17.6

*17.5 (Store objects and arrays in a file) Write a program that stores an array of the five int values 1, 2, 3, 4, and 5, a Date object for the current time, and the double value 5.5 into the file named Exercise17_05.dat.

*17.6 (Store Loan objects) The Loan class in Listing 10.2 does not implement Serializable. Rewrite the Loan class to implement Serializable. Write a program that creates five Loan objects and stores them in a file named Exercise17_06.dat.

*17.7 (Restore objects from a file) Suppose a file named Exercise17_07.dat has been created using the ObjectOutputStream. The file contains Loan objects. The Loan class in Listing 10.2 does not implement Serializable. Rewrite the Loan class to implement Serializable. Write a program that reads the Loan objects from the file and displays the total loan amount. Suppose you don’t know how many Loan objects are there in the file, use EOFException to end the loop.

Section 17.7

*17.8 (Update count) Suppose you wish to track how many times a program has been executed. You can store an int to count the file. Increase the count by 1 each time this program is executed. Let the program be Exercise17_08 and store the count in Exercise17_08.dat.

***17.9 (Address book) Write a program that stores, retrieves, adds, and updates addresses as shown in Figure 17.20. Use a fixed-length string for storing each attribute in the address. Use random access file for reading and writing an address. Assume that the size of name, street, city, state, and zip is 32, 32, 20, 2, 5 bytes, respectively.

Figure 17.20 The application can store, retrieve, and update addresses from a file.

Comprehensive

*17.10 (Split files) Suppose you want to back up a huge file (e.g., a 10-GB AVI file) to a CD-R. You can achieve it by splitting the file into smaller pieces and backing up these pieces separately. Write a utility program that splits a large file into smaller ones using the following command:

```java
java Exercise17_10 SourceFile numberOfPieces
```

The command creates the files SourceFile.1, SourceFile.2, . . . , SourceFile.n, where n is numberOfPieces and the output files are about the same size.

**17.11 (Split files GUI) Rewrite Exercise 17.10 with a GUI, as shown in Figure 17.21a.

*17.12 (Combine files) Write a utility program that combines the files together into a new file using the following command:

```java
java Exercise17_12 SourceFile1 . . . SourceFilen TargetFile
```

The command combines SourceFile1, . . . , and SourceFilen into TargetFile.
17.13 (Combine files GUI) Rewrite Exercise 17.12 with a GUI, as shown in Figure 17.21b.

17.14 (Encrypt files) Encode the file by adding 5 to every byte in the file. Write a program that prompts the user to enter an input file name and an output file name and saves the encrypted version of the input file to the output file.

17.15 (Decrypt files) Suppose a file is encrypted using the scheme in Programming Exercise 17.14. Write a program to decode an encrypted file. Your program should prompt the user to enter an input file name for the encrypted file and an output file name for the unencrypted version of the input file.

17.16 (Frequency of characters) Write a program that prompts the user to enter the name of an ASCII text file and displays the frequency of the characters in the file.

17.17 (BitOutputStream) Implement a class named \texttt{BitOutputStream}, as shown in Figure 17.22, for writing bits to an output stream. The \texttt{writeBit(char bit)} method stores the bit in a byte variable. When you create a \texttt{BitOutputStream}, the byte is empty. After invoking \texttt{writeBit('1')}, the byte becomes 00000001. After invoking \texttt{writeBit("0101")}, the byte becomes 00010101. The first three bits are not filled yet. When a byte is full, it is sent to the output stream. Now the byte is reset to empty. You must close the stream by invoking the \texttt{close()} method. If the byte is neither empty nor full, the \texttt{close()} method first fills the zeros to make a full 8 bits in the byte, and then outputs the byte and closes the stream. For a hint, see Programming Exercise 5.44. Write a test program that sends the bits 010000100100001001101 to the file named \texttt{Exercise17_17.dat}.

**17.18 (View bits) Write the following method that displays the bit representation for the last byte in an integer:

\begin{verbatim}
public static String getBits(int value)
\end{verbatim}

For a hint, see Programming Exercise 5.44. Write a program that prompts the user to enter a file name, reads bytes from the file, and displays each byte's binary representation.
*17.19 (View hex) Write a program that prompts the user to enter a file name, reads bytes from the file, and displays each byte’s hex representation. (Hint: You can first convert the byte value into an 8-bit string, then convert the bit string into a two-digit hex string.)

**17.20 (Binary editor) Write a GUI application that lets the user enter a file name in the text field and press the Enter key to display its binary representation in a text area. The user can also modify the binary code and save it back to the file, as shown in Figure 17.23a.

**17.21 (Hex editor) Write a GUI application that lets the user enter a file name in the text field and press the Enter key to display its hex representation in a text area. The user can also modify the hex code and save it back to the file, as shown in Figure 17.23b.

Figure 17.23 The programs enable the user to manipulate the contents of the file in (a) binary and (b) hex.
Recursion

Objectives

- To describe what a recursive method is and the benefits of using recursion (§18.1).
- To develop recursive methods for recursive mathematical functions (§§18.2–18.3).
- To explain how recursive method calls are handled in a call stack (§§18.2–18.3).
- To solve problems using recursion (§18.4).
- To use an overloaded helper method to design a recursive method (§18.5).
- To implement a selection sort using recursion (§18.5.1).
- To implement a binary search using recursion (§18.5.2).
- To get the directory size using recursion (§18.6).
- To solve the Tower of Hanoi problem using recursion (§18.7).
- To draw fractals using recursion (§18.8).
- To discover the relationship and difference between recursion and iteration (§18.9).
- To know tail-recursive methods and why they are desirable (§18.10).
18.1 Introduction

Recursion is a technique that leads to elegant solutions to problems that are difficult to program using simple loops.

Suppose you want to find all the files under a directory that contain a particular word. How do you solve this problem? There are several ways to do so. An intuitive and effective solution is to use recursion by searching the files in the subdirectories recursively.

H-trees, depicted in Figure 18.1, are used in a very large-scale integration (VLSI) design as a clock distribution network for routing timing signals to all parts of a chip with equal propagation delays. How do you write a program to display H-trees? A good approach is to use recursion.

![Figure 18.1](image)

An H-tree can be displayed using recursion.

To use recursion is to program using recursive methods—that is, to use methods that invoke themselves. Recursion is a useful programming technique. In some cases, it enables you to develop a natural, straightforward, simple solution to an otherwise difficult problem. This chapter introduces the concepts and techniques of recursive programming and illustrates with examples of how to “think recursively.”

18.2 Case Study: Computing Factorials

A recursive method is one that invokes itself.

Many mathematical functions are defined using recursion. Let’s begin with a simple example. The factorial of a number \( n \) can be recursively defined as follows:

\[
0! = 1; \\
n! = n \times (n - 1)!; \ n > 0
\]

How do you find \( n! \) for a given \( n \)? To find \( 1! \) is easy, because you know that \( 0! \) is \( 1 \), and \( 1! \) is \( 1 \times 0! \). Assuming that you know \( (n - 1)! \), you can obtain \( n! \) immediately by using \( n \times (n - 1)! \). Thus, the problem of computing \( n! \) is reduced to computing \( (n - 1)! \). When computing \( (n - 1)! \), you can apply the same idea recursively until \( n \) is reduced to \( 0 \).

Let \( \text{factorial}(n) \) be the method for computing \( n! \). If you call the method with \( n = 0 \), it immediately returns the result. The method knows how to solve the simplest case, which is referred to as the base case or the stopping condition. If you call the method with \( n > 0 \), it reduces the problem into a subproblem for computing the factorial of \( n - 1 \). The subproblem is essentially the same as the original problem, but it is simpler or smaller. Because the subproblem has the same property as the original problem, you can call the method with a different argument, which is referred to as a recursive call.

The recursive algorithm for computing \( \text{factorial}(n) \) can be simply described as follows:

\[
\text{if} \ (n == 0) \\
\text{return} \ 1;
\]
A recursive call can result in many more recursive calls, because the method keeps on dividing a subproblem into new subproblems. For a recursive method to terminate, the problem must eventually be reduced to a stopping case, at which point the method returns a result to its caller. The caller then performs a computation and returns the result to its own caller. This process continues until the result is passed back to the original caller. The original problem can now be solved by multiplying $n$ by the result of $\text{factorial}(n - 1)$.

Listing 18.1 gives a complete program that prompts the user to enter a nonnegative integer and displays the factorial for the number.

**LISTING 18.1 ComputeFactorial.java**

```java
import java.util.Scanner;

public class ComputeFactorial {
   public static void main(String[] args) {
      // Create a Scanner
      Scanner input = new Scanner(System.in);
      System.out.print("Enter a nonnegative integer: ");
      int n = input.nextInt();

      // Display factorial
      System.out.println("Factorial of "+ n + " is " + factorial(n));
   }

   /** Return the factorial for the specified number */
   public static long factorial(int n) {
      if (n == 0) // Base case
         return 1;
      else
         return n * factorial(n - 1); // Recursive call
   }
}
```

Enter a nonnegative integer: 4
Factorial of 4 is 24

Enter a nonnegative integer: 10
Factorial of 10 is 3628800

The `factorial` method (lines 16–21) is essentially a direct translation of the recursive mathematical definition for the factorial into Java code. The call to `factorial` is recursive because it calls itself. The parameter passed to `factorial` is decremented until it reaches the base case of 0.

You see how to write a recursive method. How does recursion work behind the scenes?
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**Figure 18.2** Invoking `factorial(4)` spawns recursive calls to `factorial`.

**Figure 18.3** When `factorial(4)` is being executed, the `factorial` method is called recursively, causing stack space to dynamically change.
Pedagogical Note

It is simpler and more efficient to implement the `factorial` method using a loop. However, we use the recursive `factorial` method here to demonstrate the concept of recursion. Later in this chapter, we will present some problems that are inherently recursive and are difficult to solve without using recursion.

If recursion does not reduce the problem in a manner that allows it to eventually converge into the base case or a base case is not specified, infinite recursion can occur. For example, suppose you mistakenly write the `factorial` method as follows:

```java
public static long factorial(int n) {
    return n * factorial(n - 1);
}
```

The method runs infinitely and causes a `StackOverflowError`.

The example discussed in this section shows a recursive method that invokes itself. This is known as direct recursion. It is also possible to create indirect recursion. This occurs when method A invokes method B, which in turn invokes method A. There can even be several more methods involved in the recursion. For example, method A invokes method B, which invokes method C, which invokes method A.

18.1 What is a recursive method? What is an infinite recursion?

18.2 How many times is the `factorial` method in Listing 18.1 invoked for `factorial(6)`?

18.3 Show the output of the following programs and identify base cases and recursive calls.

18.4 Write a recursive mathematical definition for computing $2^n$ for a positive integer $n$.

18.5 Write a recursive mathematical definition for computing $x^n$ for a positive integer $n$ and a real number $x$.

18.6 Write a recursive mathematical definition for computing $1 + 2 + 3 + \ldots + n$ for a positive integer $n$.

18.3 Case Study: Computing Fibonacci Numbers

In some cases, recursion enables you to create an intuitive, straightforward, simple solution to a problem.

The `factorial` method in the preceding section could easily be rewritten without using recursion. In this section, we show an example for creating an intuitive solution to a problem using recursion. Consider the well-known Fibonacci-series problem:
The series: 0 1 1 2 3 5 8 13 21 34 55 89 ...
indexes: 0 1 2 3 4 5 6 7 8 9 10 11

The Fibonacci series begins with 0 and 1, and each subsequent number is the sum of the preceding two. The series can be recursively defined as:

\[ \begin{align*}
    fib(0) &= 0; \\
    fib(1) &= 1; \\
    fib(index) &= fib(index - 2) + fib(index - 1); \text{ index } \geq 2
\end{align*} \]

The Fibonacci series was named for Leonardo Fibonacci, a medieval mathematician, who originated it to model the growth of the rabbit population. It can be applied in numeric optimization and in various other areas.

How do you find \( fib(index) \) for a given index? It is easy to find \( fib(2) \), because you know \( fib(0) \) and \( fib(1) \). Assuming that you know \( fib(index - 2) \) and \( fib(index - 1) \), you can obtain \( fib(index) \) immediately. Thus, the problem of computing \( fib(index) \) is reduced to computing \( fib(index - 2) \) and \( fib(index - 1) \). When doing so, you apply the idea recursively until \( index \) is reduced to 0 or 1.

The base case is \( index = 0 \) or \( index = 1 \). If you call the method with \( index = 0 \) or \( index = 1 \), it immediately returns the result. If you call the method with \( index \geq 2 \), it divides the problem into two subproblems for computing \( fib(index - 1) \) and \( fib(index - 2) \) using recursive calls. The recursive algorithm for computing \( fib(index) \) can be simply described as follows:

\[ \begin{align*}
    \text{if} \ (index == 0) & \quad \text{return} \ 0; \\
    \text{else if} \ (index == 1) & \quad \text{return} \ 1; \\
    \text{else} & \quad \text{return} \ fib(index - 1) + fib(index - 2);
\end{align*} \]

Listing 18.2 gives a complete program that prompts the user to enter an index and computes the Fibonacci number for that index.

**Listing 18.2 ComputeFibonacci.java**

```
import java.util.Scanner;

public class ComputeFibonacci {
    /** Main method */
    public static void main(String[] args) {
        // Create a Scanner
        Scanner input = new Scanner(System.in);
        System.out.print("Enter an index for a Fibonacci number: ");
        int index = input.nextInt();
        // Find and display the Fibonacci number
        System.out.println("The Fibonacci number at index " + index + " is " + fib(index));
    }

    /** The method for finding the Fibonacci number */
    public static long fib(long index) {
        if (index == 0) // Base case
            return 0;
    }
}
```
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```java
20    else if (index == 1) // Base case
21        return 1;        // base case
22    else // Reduction and recursive calls
23        return fib(index - 1) + fib(index - 2); // recursion
24    }
25 }
```

![Image](https://via.placeholder.com/150)

Enter an index for a Fibonacci number: 1
The Fibonacci number at index 1 is 1

Enter an index for a Fibonacci number: 6
The Fibonacci number at index 6 is 8

Enter an index for a Fibonacci number: 7
The Fibonacci number at index 7 is 13

The program does not show the considerable amount of work done behind the scenes by the computer. Figure 18.4, however, shows the successive recursive calls for evaluating fib(4). The original method, fib(4), makes two recursive calls, fib(3) and fib(2), and then returns fib(3) + fib(2). But in what order are these methods called? In Java, operands are evaluated from left to right, so fib(2) is called after fib(3) is completely evaluated. The labels in Figure 18.4 show the order in which the methods are called.

![Figure 18.4](https://via.placeholder.com/150)

Invoking fib(4) spawns recursive calls to fib.

As shown in Figure 18.4, there are many duplicated recursive calls. For instance, fib(2) is called twice, fib(1) three times, and fib(0) twice. In general, computing fib(index) requires roughly twice as many recursive calls as does computing fib(index - 1). As you try larger index values, the number of calls substantially increases, as shown in Table 18.1.

<table>
<thead>
<tr>
<th>index</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>10</th>
<th>20</th>
<th>30</th>
<th>40</th>
<th>50</th>
</tr>
</thead>
<tbody>
<tr>
<td># of calls</td>
<td>3</td>
<td>5</td>
<td>9</td>
<td>177</td>
<td>2,189</td>
<td>2,692,537</td>
<td>331,160,281</td>
<td>2,075,316,483</td>
</tr>
</tbody>
</table>
18.7 Show the output of the following two programs:

```java
public class Test {
    public static void main(String[] args) {
        xMethod(5);
    }

    public static void xMethod(int n) {
        if (n > 0) {
            System.out.print(n + " ");
            xMethod(n - 1);
        }
    }
}
```

```java
public class Test {
    public static void main(String[] args) {
        xMethod(5);
    }

    public static void xMethod(int n) {
        if (n > 0) {
            xMethod(n - 1);
            System.out.print(n + " ");
        }
    }
}
```

18.8 What is wrong in the following method?

```java
public class Test {
    public static void main(String[] args) {
        xMethod(1234567);
    }

    public static void xMethod(double n) {
        if (n != 0) {
            System.out.print(n);
            xMethod(n / 10);
        }
    }
}
```

```java
public class Test {
    public static void main(String[] args) {
        Test test = new Test();
        System.out.println(test.toString());
    }

    public Test() {
        Test test = new Test();
    }
}
```

18.9 How many times is the fib method in Listing 18.2 invoked for fib(6)?

18.4 Problem Solving Using Recursion

*If you think recursively, you can solve many problems using recursion.*

The preceding sections presented two classic recursion examples. All recursive methods have the following characteristics:

- **if-else**
  - The method is implemented using an if-else or a switch statement that leads to different cases.

- **base cases**
  - One or more base cases (the simplest case) are used to stop recursion.

- **reduction**
  - Every recursive call reduces the original problem, bringing it increasingly closer to a base case until it becomes that case.

In general, to solve a problem using recursion, you break it into subproblems. Each subproblem is the same as the original problem but smaller in size. You can apply the same approach to each subproblem to solve it recursively.
Recursion is everywhere. It is fun to think recursively. Consider drinking coffee. You may describe the procedure recursively as follows:

```java
public static void drinkCoffee(Cup cup) {
    if (!cup.isEmpty()) {
        cup.takeOneSip(); // Take one sip
        drinkCoffee(cup);
    }
}
```

Assume `cup` is an object for a cup of coffee with the instance methods `isEmpty()` and `takeOneSip()`. You can break the problem into two subproblems: one is to drink one sip of coffee and the other is to drink the rest of the coffee in the cup. The second problem is the same as the original problem but smaller in size. The base case for the problem is when the cup is empty.

Consider the problem of printing a message \( n \) times. You can break the problem into two subproblems: one is to print the message one time and the other is to print it \( n - 1 \) times. The second problem is the same as the original problem but it is smaller in size. The base case for the problem is \( n == 0 \). You can solve this problem using recursion as follows:

```java
public static void nPrintln(String message, int times) {
    if (times >= 1) {
        System.out.println(message);
        nPrintln(message, times - 1);
    } // The base case is times == 0
}
```

Note that the `fib` method in the preceding section returns a value to its caller, but the `drinkCoffee` and `nPrintln` methods are `void` and they do not return a value.

If you think recursively, you can use recursion to solve many of the problems presented in earlier chapters of this book. Consider the palindrome problem in Listing 5.14. Recall that a string is a palindrome if it reads the same from the left and from the right. For example, “mom” and “dad” are palindromes, but “uncle” and “aunt” are not. The problem of checking whether a string is a palindrome can be divided into two subproblems:

- Check whether the first character and the last character of the string are equal.
- Ignore the two end characters and check whether the rest of the substring is a palindrome.

The second subproblem is the same as the original problem but smaller in size. There are two base cases: (1) the two end characters are not the same, and (2) the string size is 0 or 1. In case 1, the string is not a palindrome; in case 2, the string is a palindrome. The recursive method for this problem can be implemented as shown in Listing 18.3.

**Listing 18.3 RecursivePalindromeUsingSubstring.java**

```java
public class RecursivePalindromeUsingSubstring {
    public static boolean isPalindrome(String s) {
        if (s.length() <= 1) // Base case
            return true;
        else if (s.charAt(0) != s.charAt(s.length() - 1)) // Base case
            return false;
        else
            return isPalindrome(s.substring(1, s.length() - 1)); // Recursive call
    }

    public static void main(String[] args) {
        System.out.println("Is moon a palindrome? ")
    }
```
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```java
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13        + isPalindrome("moon");
14      System.out.println("Is noon a palindrome? "
15        + isPalindrome("noon");
16      System.out.println("Is a a palindrome? " + isPalindrome("a"));
17      System.out.println("Is aba a palindrome? " +
18        isPalindrome("aba");
19      System.out.println("Is ab a palindrome? " + isPalindrome("ab");
20    }
21  }

Is moon a palindrome? false
Is noon a palindrome? true
Is a a palindrome? true
Is aba a palindrome? true
Is ab a palindrome? false

The `substring` method in line 8 creates a new string that is the same as the original string except without the first and last characters. Checking whether a string is a palindrome is equivalent to checking whether the substring is a palindrome if the two end characters in the original string are the same.

18.10 Describe the characteristics of recursive methods.

18.11 For the `isPalindrome` method in Listing 18.3, what are the base cases? How many times is this method called when invoking `isPalindrome("abdxcdba")`?

18.12 Show the call stack for `isPalindrome("abcba")` using the method defined in Listing 18.3.

18.5 Recursive Helper Methods

Sometimes you can find a solution to the original problem by defining a recursive function to a problem similar to the original problem. This new method is called a recursive helper method. The original problem can be solved by invoking the recursive helper method.

The recursive `isPalindrome` method in Listing 18.3 is not efficient, because it creates a new string for every recursive call. To avoid creating new strings, you can use the low and high indices to indicate the range of the substring. These two indices must be passed to the recursive method. Since the original method is `isPalindrome(String s)`, you have to create the new method `isPalindrome(String s, int low, int high)` to accept additional information on the string, as shown in Listing 18.4.

LISTING 18.4 RecursivePalindrome.java

```java
public class RecursivePalindrome {

public static boolean isPalindrome(String s) {
    return isPalindrome(s, 0, s.length() - 1);
}

private static boolean isPalindrome(String s, int low, int high) {
    if (high <= low) // Base case
        return true;
    else if (s.charAt(low) != s.charAt(high)) // Base case
        return false;
    else
        return isPalindrome(s, low + 1, high - 1);
}
```
18.5 Recursive Helper Methods

Two overloaded isPalindrome methods are defined. The first, `isPalindrome(String s)`, checks whether a string is a palindrome, and the second, `isPalindrome(String s, int low, int high)`, checks whether a substring `s(low..high)` is a palindrome. The first method passes the string `s` with `low = 0` and `high = s.length() – 1` to the second method. The second method can be invoked recursively to check a palindrome in an ever-shrinking substring. It is a common design technique in recursive programming to define a second method that receives additional parameters. Such a method is known as a recursive helper method.

Helper methods are very useful in designing recursive solutions for problems involving strings and arrays. The sections that follow give two more examples.

### 18.5.1 Recursive Selection Sort

Selection sort was introduced in Section 7.11. Recall that it finds the smallest element in the list and swaps it with the first element. It then finds the smallest element remaining and swaps it with the first element in the remaining list, and so on until the remaining list contains only a single element. The problem can be divided into two subproblems:

- Find the smallest element in the list and swap it with the first element.
- Ignore the first element and sort the remaining smaller list recursively.

The base case is that the list contains only one element. Listing 18.5 gives the recursive sort method.

**Listing 18.5** RecursiveSelectionSort.java

```java
public class RecursiveSelectionSort {
    public static void sort(double[] list) {
        sort(list, 0, list.length - 1); // Sort the entire list
    }

    private static void sort(double[] list, int low, int high) {
        if (low < high) {
            // Find the smallest number and its index in list[low .. high]
            int indexOfMin = low;
            double min = list[low];
            for (int i = low + 1; i <= high; i++) {
                if (list[i] < min) {
                    min = list[i];
                    indexOfMin = i;
                }
            }
            // Swap the smallest in list[low .. high] with list[low]
            list[indexOfMin] = list[low];
            list[low] = min;
        }
    }
}
```
Two overloaded sort methods are defined. The first method, sort(double[] list), sorts an array in list[0..list.length - 1] and the second method, sort(double[] list, int low, int high), sorts an array in list[low..high]. The second method can be invoked recursively to sort an ever-shrinking subarray.

18.5.2 Recursive Binary Search

Binary search was introduced in Section 7.10.2. For binary search to work, the elements in the array must be in increasing order. The binary search first compares the key with the element in the middle of the array. Consider the following three cases:

- **Case 1:** If the key is less than the middle element, recursively search for the key in the first half of the array.
- **Case 2:** If the key is equal to the middle element, the search ends with a match.
- **Case 3:** If the key is greater than the middle element, recursively search for the key in the second half of the array.

Case 1 and Case 3 reduce the search to a smaller list. Case 2 is a base case when there is a match. Another base case is that the search is exhausted without a match. Listing 18.6 gives a clear, simple solution for the binary search problem using recursion.

**LISTING 18.6 Recursive Binary Search Method**

```java
public class RecursiveBinarySearch {
  public static int recursiveBinarySearch(int[] list, int key) {
    int low = 0;
    int high = list.length - 1;
    return recursiveBinarySearch(list, key, low, high);
  }

  private static int recursiveBinarySearch(int[] list, int key, int low, int high) {
    if (low > high) // The list has been exhausted without a match
      return -low - 1;
    int mid = (low + high) / 2;
    if (key < list[mid])
      return recursiveBinarySearch(list, key, low, mid - 1);
    else if (key == list[mid])
      return mid;
    else
      return recursiveBinarySearch(list, key, mid + 1, high);
  }
}
```

The first method finds a key in the whole list. The second method finds a key in the list with index from low to high.

The first binarySearch method passes the initial array with low = 0 and high = list.length - 1 to the second binarySearch method. The second method is invoked recursively to find the key in an ever-shrinking subarray.
18.13 Show the call stack for `isPalindrome("abcba")` using the method defined in Listing 18.4.

18.14 Show the call stack for `selectionSort(new double[]{2, 3, 5, 1})` using the method defined in Listing 18.5.

18.15 What is a recursive helper method?

18.6 Case Study: Finding the Directory Size

Recursive methods are efficient for solving problems with recursive structures.

The preceding examples can easily be solved without using recursion. This section presents a problem that is difficult to solve without using recursion. The problem is to find the size of a directory. The size of a directory is the sum of the sizes of all files in the directory. A directory `d` may contain subdirectories. Suppose a directory contains files `f_1, f_2, \ldots, f_m` and subdirectories `d_1, d_2, \ldots, d_n`, as shown in Figure 18.5.

![Figure 18.5](image.png)  
**Figure 18.5** A directory contains files and subdirectories.

The size of the directory can be defined recursively as follows:

\[
\text{size}(d) = \text{size}(f_1) + \text{size}(f_2) + \ldots + \text{size}(f_m) + \text{size}(d_1) + \text{size}(d_2) + \ldots + \text{size}(d_n)
\]

The `File` class, introduced in Section 12.10, can be used to represent a file or a directory and obtain the properties for files and directories. Two methods in the `File` class are useful for this problem:

- The `length()` method returns the size of a file.
- The `listFiles()` method returns an array of `File` objects under a directory.

Listing 18.7 gives a program that prompts the user to enter a directory or a file and displays its size.

**Listing 18.7 DirectorySize.java**

```java
import java.io.File;
import java.util.Scanner;

public class DirectorySize {
    public static void main(String[] args) {
        // Prompt the user to enter a directory or a file
        System.out.print("Enter a directory or a file: ");
        Scanner input = new Scanner(System.in);
        String directory = input.nextLine();

        // Display the size
        System.out.println(getSize(new File(directory)) + " bytes");
    }
}
```
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```java
public static long getSize(File file) {
    long size = 0;  // Store the total size of all files
    if (file.isDirectory()) {
        File[] files = file.listFiles(); // All files and subdirectories
        for (int i = 0; files != null && i < files.length; i++) {
            size += getSize(files[i]); // Recursive call
        }
    } else { // Base case
        size += file.length();
    }
    return size;
}
```

If the file object represents a directory (line 18), each subitem (file or subdirectory) in the directory is recursively invoked to obtain its size (line 21). If the file object represents a file (line 24), the file size is obtained and added to the total size (line 25).

What happens if an incorrect or a nonexistent directory is entered? The program will detect that it is not a directory and invoke file.length() (line 25), which returns 0. Thus, in this case, the getSize method will return 0.

**Tip**
To avoid mistakes, it is a good practice to test all cases. For example, you should test the program for an input of file, an empty directory, a nonexistent directory, and a nonexistent file.

18.16  What is the base case for the getSize method?
18.17  How does the program get all files and directories under a given directory?
18.18  How many times will the getSize method be invoked for a directory if the directory has three subdirectories and each subdirectory has four files?
18.19  Will the program work if the directory is empty (i.e., it does not contain any files)?
18.20  Will the program work if line 20 is replaced by the following code?
```java
for (int i = 0; i < files.length; i++)
```
18.21 Will the program work if lines 20–21 is replaced by the following code?

```java
for (File file: files)
    size += getSize(file); // Recursive call
```

18.7 Case Study: Tower of Hanoi

The Tower of Hanoi problem is a classic problem that can be solved easily using recursion, but it is difficult to solve otherwise.

The problem involves moving a specified number of disks of distinct sizes from one tower to another while observing the following rules:

- There are \( n \) disks labeled 1, 2, 3, \ldots, \( n \) and three towers labeled A, B, and C.
- No disk can be on top of a smaller disk at any time.
- All the disks are initially placed on tower A.
- Only one disk can be moved at a time, and it must be the smallest disk on a tower.

The objective of the problem is to move all the disks from A to B with the assistance of C. For example, if you have three disks, the steps to move all of the disks from A to B are shown in Figure 18.6.

**Figure 18.6** The goal of the Tower of Hanoi problem is to move disks from tower A to tower B without breaking the rules.
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Note
The Tower of Hanoi is a classic computer-science problem, to which many websites are devoted. One of them worth looking at is www.cut-the-knot.com/recurrence/hanoi.shtml.

In the case of three disks, you can find the solution manually. For a larger number of disks, however—even for four—the problem is quite complex. Fortunately, the problem has an inherently recursive nature, which leads to a straightforward recursive solution.

The base case for the problem is \( n = 1 \). If \( n = 1 \), you could simply move the disk from A to B. When \( n > 1 \), you could split the original problem into the following three subproblems and solve them sequentially.

1. Move the first \( n - 1 \) disks from A to C recursively with the assistance of tower B, as shown in Step 1 in Figure 18.7.
2. Move disk \( n \) from A to B, as shown in Step 2 in Figure 18.7.
3. Move \( n - 1 \) disks from C to B recursively with the assistance of tower A, as shown in Step 3 in Figure 18.7.

The following method moves \( n \) disks from the \texttt{fromTower} to the \texttt{toTower} with the assistance of the \texttt{auxTower}:

```c
void moveDisks(int n, char fromTower, char toTower, char auxTower)
```

The algorithm for the method can be described as:

```c
if (n == 1) // Stopping condition
    Move disk 1 from the fromTower to the toTower;
else {
    moveDisks(n - 1, fromTower, auxTower, toTower);
    Move disk n from the fromTower to the toTower;
    moveDisks(n - 1, auxTower, toTower, fromTower);
}
```

![Figure 18.7](image-url) The Tower of Hanoi problem can be decomposed into three subproblems.
Listing 18.8 gives a program that prompts the user to enter the number of disks and invokes the recursive method `moveDisks` to display the solution for moving the disks.

**LISTING 18.8  TowerOfHanoi.java**

```java
import java.util.Scanner;

public class TowerOfHanoi {

  public static void main(String[] args) {
    // Create a Scanner
    Scanner input = new Scanner(System.in);
    System.out.print("Enter number of disks: ");
    int n = input.nextInt();

    // Find the solution recursively
    System.out.println("The moves are:");
    moveDisks(n, 'A', 'B', 'C');
  }

  public static void moveDisks(int n, char fromTower, char toTower, char auxTower) {
    if (n == 1) // Stopping condition
      System.out.println("Move disk "+n+" from "+fromTower+" to "+toTower);
    else {
      moveDisks(n - 1, fromTower, auxTower, toTower);
      System.out.println("Move disk "+n+" from "+fromTower+" to "+toTower);
      moveDisks(n - 1, auxTower, toTower, fromTower);
    }
  }
}
```

Enter number of disks: 4
The moves are:
Move disk 1 from A to C
Move disk 2 from A to B
Move disk 1 from C to B
Move disk 3 from A to C
Move disk 1 from B to A
Move disk 2 from B to C
Move disk 1 from A to C
Move disk 4 from A to B
Move disk 1 from C to B
Move disk 2 from C to A
Move disk 1 from A to B
Move disk 3 from C to B
Move disk 1 from A to C
Move disk 2 from A to B
Move disk 1 from C to B
This problem is inherently recursive. Using recursion makes it possible to find a natural, simple solution. It would be difficult to solve the problem without using recursion.

Consider tracing the program for \( n = 3 \). The successive recursive calls are shown in Figure 18.8. As you can see, writing the program is easier than tracing the recursive calls. The system uses stacks to manage the calls behind the scenes. To some extent, recursion provides a level of abstraction that hides iterations and other details from the user.

**Figure 18.8** Invoking `moveDisks(3, 'A', 'B', 'C')` spawns calls to `moveDisks` recursively.

### 18.22 How many times is the `moveDisks` method in Listing 18.8 invoked for `moveDisks(5, 'A', 'B', 'C')`?

### 18.8 Case Study: Fractals

*Using recursion is ideal for displaying fractals, because fractals are inherently recursive.*

A fractal is a geometrical figure, but unlike triangles, circles, and rectangles, fractals can be divided into parts, each of which is a reduced-size copy of the whole. There are many interesting examples of fractals. This section introduces a simple fractal, the **Sierpinski triangle**, named after a famous Polish mathematician.

A Sierpinski triangle is created as follows:

1. Begin with an equilateral triangle, which is considered to be a Sierpinski fractal of order (or level) 0, as shown in Figure 18.9a.
2. Connect the midpoints of the sides of the triangle of order 0 to create a Sierpinski triangle of order 1 (Figure 18.9b).
3. Leave the center triangle intact. Connect the midpoints of the sides of the three other triangles to create a Sierpinski triangle of order 2 (Figure 18.9c).
4. You can repeat the same process recursively to create a Sierpinski triangle of order 3, 4, . . ., and so on (Figure 18.9d).

The problem is inherently recursive. How do you develop a recursive solution for it? Consider the base case when the order is 0. It is easy to draw a Sierpinski triangle of order 0. How do you draw a Sierpinski triangle of order 1? The problem can be reduced to drawing three Sierpinski triangles of order 0. How do you draw a Sierpinski triangle of order 2? The problem can be reduced to drawing three Sierpinski triangles of order 1, so the problem of
drawing a Sierpinski triangle of order \( n \) can be reduced to drawing three Sierpinski triangles of order \( n - 1 \).

Listing 18.9 gives a program that displays a Sierpinski triangle of any order, as shown in Figure 18.9. You can enter an order in a text field to display a Sierpinski triangle of the specified order.

**LISTING 18.9**  SierpinskiTriangle.java

```java
import javafx.application.Application;
import javafx.geometry.Point2D;
import javafx.geometry.Pos;
import javafx.scene.Scene;
import javafx.scene.control.Label;
import javafx.scene.control.TextField;
import javafx.scene.layout.BorderPane;
import javafx.scene.layout.HBox;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Polygon;
import javafx.stage.Stage;

public class SierpinskiTriangle extends Application {
    @Override
    public void start(Stage primaryStage) {
        SierpinskiTrianglePane trianglePane = new SierpinskiTrianglePane();
        TextField tfOrder = new TextField();
        tfOrder.setOnAction(recursive triangle pane);
        primaryStage.setTitle("Sierpinski Triangle");
        Scene scene = new Scene(trianglePane, 400, 400);
        scene.getStylesheets().add("application.css");
        primaryStage.setScene(scene);
        primaryStage.show();
    }
    
    public static void main(String[] args) {
        launch(args);
    }
}
```

**FIGURE 18.9**  A Sierpinski triangle is a pattern of recursive triangles.
listener for text field
20        e -> trianglePane.setOrder(Integer.parseInt(tfOrder.getText()));
21      tfOrder.setPrefColumnCount(4);
22      tfOrder.setAlignment(Pos.BOTTOM_RIGHT);
23
24      // Pane to hold label, text field, and a button
25      HBox hBox = new HBox(10);
26      hBox.getChildren().addAll(new Label("Enter an order: "), tfOrder);
27      hBox.setAlignment(Pos.CENTER);
28
29      BorderPane borderPane = new BorderPane();
30      borderPane.setCenter(trianglePane);
31      borderPane.setBottom(hBox);
32
33      // Create a scene and place it in the stage
34      Scene scene = new Scene(borderPane, 200, 210);
35      primaryStage.setTitle("SierpinskiTriangle"); // Set the stage title
36      primaryStage.setScene(scene); // Place the scene in the stage
37      primaryStage.show(); // Display the stage
38
39      scene.widthProperty().addListener(ov -> trianglePane.paint());
40      scene.heightProperty().addListener(ov -> trianglePane.paint());
41    }
42
43    /** Pane for displaying triangles */
44    static class SierpinskiTrianglePane extends Pane {
45      private int order = 0;
46
47      /** Set a new order */
48      public void setOrder(int order) {
49        this.order = order;
50        paint();
51      }
52
53      SierpinskiTrianglePane() {
54      }
55
56      protected void paint() {
57        // Select three points in proportion to the pane size
58        Point2D p1 = new Point2D(getWidth() / 2, 10);
59        Point2D p2 = new Point2D(10, getHeight() - 10);
60        Point2D p3 = new Point2D(getWidth() - 10, getHeight() - 10);
61
62        this.getChildren().clear(); // Clear the pane before redisplay
63
64        displayTriangles(order, p1, p2, p3);
65      }
66
67      private void displayTriangles(int order, Point2D p1, Point2D p2, Point2D p3) {
68        if (order == 0) {
69          // Draw a triangle to connect three points
70          Polygon triangle = new Polygon();
71          triangle.getPoints().addAll(p1.getX(), p1.getY(), p2.getX(), p2.getY(), p3.getX(), p3.getY());
72          triangle.setStroke(Color.BLACK);
73          triangle.setFill(Color.WHITE);
74          this.getChildren().add(triangle);
75        } else {
76          // Create a triangle
77          Polygon triangle = new Polygon();
78          triangle.getPoints().addAll(p1.getX(), p1.getY(), p2.getX(), p2.getY(), p3.getX(), p3.getY());
79          triangle.setStroke(Color.BLACK);
80          triangle.setFill(Color.WHITE);
81          this.getChildren().add(triangle);
82        }
83      }
18.8 Case Study: Fractals

```java
80     // Get the midpoint on each edge in the triangle
81     point2D p12 = p1.midpoint(p2);
82     point2D p23 = p2.midpoint(p3);
83     point2D p31 = p3.midpoint(p1);
84
85     // Recursively display three triangles
86     displayTriangles(order - 1, p1, p12, p31);
87     displayTriangles(order - 1, p12, p2, p23);
88     displayTriangles(order - 1, p31, p23, p3);
89  }
90 }
91 }
92 }
```

The initial triangle has three points set in proportion to the pane size (lines 58–60). If `order == 0`, the `displayTriangles(order, p1, p2, p3)` method displays a triangle that connects the three points `p1`, `p2`, and `p3` in lines 71–77, as shown in Figure 18.10a. Otherwise, it performs the following tasks:

1. Obtain the midpoint between `p1` and `p2` (line 81), the midpoint between `p2` and `p3` (line 82), and the midpoint between `p3` and `p1` (line 83), as shown in Figure 18.10b.

2. Recursively invoke `displayTriangles` with a reduced order to display three smaller Sierpinski triangles (lines 86–88). Note that each small Sierpinski triangle is structurally identical to the original big Sierpinski triangle except that the order of a small triangle is one less, as shown in Figure 18.10b.

![Figure 18.10](image)

**Figure 18.10** Drawing a Sierpinski triangle spawns calls to draw three small Sierpinski triangles recursively.

A Sierpinski triangle is displayed in a `SierpinskiTrianglePane`. The `order` property in the inner class `SierpinskiTrianglePane` specifies the order for the Sierpinski triangle. The `Point2D` class, introduced in Section 9.8, The `Point2D` Class, represents a point with
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- and y-coordinates. Invoking \( p1\.midpoint(p2) \) returns a new \( \text{Point2D} \) object that is the midpoint between \( p1 \) and \( p2 \) (lines 81–83).

18.23 How do you obtain the midpoint between two points?
18.24 What is the base case for the \( \text{displayTriangles} \) method?
18.25 How many times is the \( \text{displayTriangles} \) method invoked for a Sierpinski triangle of order 0, order 1, order 2, and order \( n \)?
18.26 What happens if you enter a negative order? How do you fix this problem in the code?
18.27 Instead of drawing a triangle using a polygon, rewrite the code to draw a triangle by drawing three lines to connect the points in lines 71–77.

18.9 Recursion vs. Iteration

Recursion is an alternative form of program control. It is essentially repetition without a loop.

When you use loops, you specify a loop body. The repetition of the loop body is controlled by the loop control structure. In recursion, the method itself is called repeatedly. A selection statement must be used to control whether to call the method recursively or not.

Recursion bears substantial overhead. Each time the program calls a method, the system must allocate memory for all of the method’s local variables and parameters. This can consume considerable memory and requires extra time to manage the memory.

Any problem that can be solved recursively can be solved nonrecursively with iterations. Recursion has some negative aspects: it uses up too much time and too much memory. Why, then, should you use it? In some cases, using recursion enables you to specify a clear, simple solution for an inherently recursive problem that would otherwise be difficult to obtain. Examples are the directory-size problem, the Tower of Hanoi problem, and the fractal problem, which are rather difficult to solve without using recursion.

The decision whether to use recursion or iteration should be based on the nature of, and your understanding of, the problem you are trying to solve. The rule of thumb is to use whichever approach can best develop an intuitive solution that naturally mirrors the problem. If an iterative solution is obvious, use it. It will generally be more efficient than the recursive option.

Note

Recursive programs can run out of memory, causing a \( \text{StackOverflowError} \).

Tip

If you are concerned about your program’s performance, avoid using recursion, because it takes more time and consumes more memory than iteration. In general, recursion can be used to solve the inherent recursive problems such as Tower of Hanoi, recursive directories, and Sierpinski triangles.

18.28 Which of the following statements are true?

a. Any recursive method can be converted into a nonrecursive method.
b. Recursive methods take more time and memory to execute than nonrecursive methods.
c. Recursive methods are \textit{always} simpler than nonrecursive methods.
d. There is always a selection statement in a recursive method to check whether a base case is reached.

18.29 What is a cause for a stack-overflow exception?
18.10 Tail Recursion

A tail recursive method is efficient for reducing stack size.

A recursive method is said to be tail recursive if there are no pending operations to be performed on return from a recursive call, as illustrated in Figure 18.11a. However, method B in Figure 18.11b is not tail recursive because there are pending operations after a method call is returned.

For example, the recursive `isPalindrome` method (lines 6–13) in Listing 18.4 is tail recursive because there are no pending operations after recursively invoking `isPalindrome` in line 12. However, the recursive `factorial` method (lines 16–21) in Listing 18.1 is not tail recursive, because there is a pending operation, namely multiplication, to be performed on return from each recursive call.

Tail recursion is desirable: because the method ends when the last recursive call ends, there is no need to store the intermediate calls in the stack. Compilers can optimize tail recursion to reduce stack size.

A nontail-recursive method can often be converted to a tail-recursive method by using auxiliary parameters. These parameters are used to contain the result. The idea is to incorporate the pending operations into the auxiliary parameters in such a way that the recursive call no longer has a pending operation. You can define a new auxiliary recursive method with the auxiliary parameters. This method may overload the original method with the same name but a different signature. For example, the `factorial` method in Listing 18.1 is written in a tail-recursive way in Listing 18.10.

### Listing 18.10  ComputeFactorialTailRecursion.java

```java
1 public class ComputeFactorialTailRecursion {
2    /** Return the factorial for a specified number */
3    public static long factorial(int n) {
4        return factorial(n, 1); // Call auxiliary method
5    }
6
7    /** Auxiliary tail-recursive method for factorial */
8    private static long factorial(int n, int result) {
9        if (n == 0)
10            return result;
11        else
12            return factorial(n - 1, n * result); // Recursive call
13    }
14}
```

The first `factorial` method (line 3) simply invokes the second auxiliary method (line 4). The second method contains an auxiliary parameter `result` that stores the result for the factorial of `n`. This method is invoked recursively in line 12. There is no pending operation after
a call is returned. The final result is returned in line 10, which is also the return value from invoking \texttt{factorial(n, 1)} in line 4.

\textbf{Check Point} \hspace{1em} \textbf{18.30} Identify tail-recursive methods in this chapter.

\textbf{18.31} Rewrite the \texttt{fib} method in Listing 18.2 using tail recursion.

\textbf{KEY TERMS}

\begin{tabular}{l l l l}
\text{base case} & 706 & \text{recursive helper method} & 715 \\
\text{direct recursion} & 709 & \text{recursive method} & 706 \\
\text{indirect recursion} & 709 & \text{stopping condition} & 706 \\
\text{infinite recursion} & 709 & \text{tail recursion} & 727 \\
\end{tabular}

\textbf{CHAPTER SUMMARY}

1. A \textit{recursive method} is one that directly or indirectly invokes itself. For a recursive method to terminate, there must be one or more \textit{base cases}.

2. \textit{Recursion} is an alternative form of program control. It is essentially repetition without a loop control. It can be used to write simple, clear solutions for inherently recursive problems that would otherwise be difficult to solve.

3. Sometimes the original method needs to be modified to receive additional parameters in order to be invoked recursively. A \textit{recursive helper method} can be defined for this purpose.

4. Recursion bears substantial overhead. Each time the program calls a method, the system must allocate memory for all of the method’s local variables and parameters. This can consume considerable memory and requires extra time to manage the memory.

5. A recursive method is said to be \textit{tail recursive} if there are no pending operations to be performed on return from a recursive call. Some compilers can optimize tail recursion to reduce stack size.

\textbf{QUIZ}

Answer the quiz for this chapter online at \url{www.cs.armstrong.edu/liang/intro10e/quiz.html}.

\textbf{PROGRAMMING EXERCISES}

\textbf{Sections 18.2–18.3}

\begin{itemize}
\item \textbf{*18.1} \textit{(Factorial)} Using the \texttt{BigInteger} class introduced in Section 10.9, you can find the factorial for a large number (e.g., 100!). Implement the \texttt{factorial} method using recursion. Write a program that prompts the user to enter an integer and displays its factorial.

\item \textbf{*18.2} \textit{(Fibonacci numbers)} Rewrite the \texttt{fib} method in Listing 18.2 using iterations. \textit{Hint:} To compute \texttt{fib}(n) without recursion, you need to obtain \texttt{fib}(n - 2) and \texttt{fib}(n - 1) first. Let \texttt{f0} and \texttt{f1} denote the two previous Fibonacci
numbers. The current Fibonacci number would then be \( f_0 + f_1 \). The algorithm can be described as follows:

\[
f_0 = 0; \quad // \text{For } \text{fib}(0) \\
f_1 = 1; \quad // \text{For } \text{fib}(1) \\
\]

\[
\text{for} \; (\text{int } i = 1; \; i \leq n; \; i++) \{ \\
\quad \text{currentFib} = f_0 + f_1; \\
\quad f_0 = f_1; \\
\quad f_1 = \text{currentFib}; \\
\} \\
\// \text{After the loop, currentFib is fib(n)}
\]

Write a test program that prompts the user to enter an index and displays its Fibonacci number.

*18.3  (Compute greatest common divisor using recursion) The \( \text{gcd}(m, \; n) \) can also be defined recursively as follows:

- If \( m \% n \) is 0, \( \text{gcd}(m, \; n) \) is \( n \).
- Otherwise, \( \text{gcd}(m, \; n) \) is \( \text{gcd}(n, \; m \% n) \).

Write a recursive method to find the GCD. Write a test program that prompts the user to enter two integers and displays their GCD.

18.4  (Sum series) Write a recursive method to compute the following series:

\[
m(i) = 1 + \frac{1}{2} + \frac{1}{3} + \ldots + \frac{1}{i}
\]

Write a test program that displays \( m(i) \) for \( i = 1, 2, \ldots, 10 \).

18.5  (Sum series) Write a recursive method to compute the following series:

\[
m(i) = \frac{1}{3} + \frac{2}{5} + \frac{3}{7} + \frac{4}{9} + \frac{5}{11} + \frac{6}{13} + \ldots + \frac{i}{2i+1}
\]

Write a test program that displays \( m(i) \) for \( i = 1, 2, \ldots, 10 \).

*18.6  (Sum series) Write a recursive method to compute the following series:

\[
m(i) = \frac{1}{2} + \frac{2}{3} + \ldots + \frac{i}{i+1}
\]

Write a test program that displays \( m(i) \) for \( i = 1, 2, \ldots, 10 \).

*18.7  (Fibonacci series) Modify Listing 18.2, ComputeFibonacci.java, so that the program finds the number of times the \text{fib} method is called. (Hint: Use a static variable and increment it every time the method is called.)

Section 18.4

*18.8  (Print the digits in an integer reversely) Write a recursive method that displays an \text{int} value reversely on the console using the following header:

public static void reverseDisplay(int value)

For example, \text{reverseDisplay(12345)} displays 54321. Write a test program that prompts the user to enter an integer and displays its reversal.

*18.9  (Print the characters in a string reversely) Write a recursive method that displays a string reversely on the console using the following header:

public static void reverseDisplay(String value)
For example, `reverseDisplay("abcd")` displays `dcba`. Write a test program that prompts the user to enter a string and displays its reversal.

*18.10  *(Occurrences of a specified character in a string)* Write a recursive method that finds the number of occurrences of a specified letter in a string using the following method header:

```java
public static int count(String str, char a)
```

For example, `count("Welcome", 'e')` returns `2`. Write a test program that prompts the user to enter a string and a character, and displays the number of occurrences for the character in the string.

*18.11  *(Sum the digits in an integer using recursion)* Write a recursive method that computes the sum of the digits in an integer. Use the following method header:

```java
public static int sumDigits(long n)
```

For example, `sumDigits(234)` returns `2 + 3 + 4 = 9. Write a test program that prompts the user to enter an integer and displays its sum.

**Section 18.5**

*18.12  *(Print the characters in a string reversely)* Rewrite Programming Exercise 18.9 using a helper method to pass the substring `high` index to the method. The helper method header is:

```java
public static void reverseDisplay(String value, int high)
```

*18.13  *(Find the largest number in an array)* Write a recursive method that returns the largest integer in an array. Write a test program that prompts the user to enter a list of eight integers and displays the largest element.

*18.14  *(Find the number of uppercase letters in a string)* Write a recursive method to return the number of uppercase letters in a string. Write a test program that prompts the user to enter a string and displays the number of uppercase letters in the string.

*18.15  *(Occurrences of a specified character in a string)* Rewrite Programming Exercise 18.10 using a helper method to pass the substring `high` index to the method. The helper method header is:

```java
public static int count(String str, char a, int high)
```

*18.16  *(Find the number of uppercase letters in an array)* Write a recursive method to return the number of uppercase letters in an array of characters. You need to define the following two methods. The second one is a recursive helper method.

```java
public static int count(char[] chars)
public static int count(char[] chars, int high)
```

Write a test program that prompts the user to enter a list of characters in one line and displays the number of uppercase letters in the list.

*18.17  *(Occurrences of a specified character in an array)* Write a recursive method that finds the number of occurrences of a specified character in an array. You need to define the following two methods. The second one is a recursive helper method.

```java
public static int count(char[] chars, char ch)
public static int count(char[] chars, char ch, int high)
```
Write a test program that prompts the user to enter a list of characters in one line, and a character, and displays the number of occurrences of the character in the list.

Sections 18.6–18.10

*18.18 (Tower of Hanoi) Modify Listing 18.8, TowerOfHanoi.java, so that the program finds the number of moves needed to move \( n \) disks from tower A to tower B. (Hint: Use a static variable and increment it every time the method is called.)

*18.19 (Sierpinski triangle) Revise Listing 18.9 to develop a program that lets the user use the + and – buttons to increase or decrease the current order by 1, as shown in Figure 18.12a. The initial order is 0. If the current order is 0, the Decrease button is ignored.

![Figure 18.12](a) Programming Exercise 18.19 uses the + and – buttons to increase or decrease the current order by 1. (b) Programming Exercise 18.20 draws ovals using a recursive method.

*18.20 (Display circles) Write a Java program that displays ovals, as shown in Figure 18.12b. The circles are centered in the pane. The gap between two adjacent circles is 10 pixels, and the gap between the border of the pane and the largest circle is also 10.

*18.21 (Decimal to binary) Write a recursive method that converts a decimal number into a binary number as a string. The method header is:

```java
public static String dec2Bin(int value)
```

Write a test program that prompts the user to enter a decimal number and displays its binary equivalent.

*18.22 (Decimal to hex) Write a recursive method that converts a decimal number into a hex number as a string. The method header is:

```java
public static String dec2Hex(int value)
```

Write a test program that prompts the user to enter a decimal number and displays its hex equivalent.

*18.23 (Binary to decimal) Write a recursive method that parses a binary number as a string into a decimal integer. The method header is:

```java
public static int bin2Dec(String binaryString)
```

Write a test program that prompts the user to enter a binary string and displays its decimal equivalent.
**18.24** *(Hex to decimal)* Write a recursive method that parses a hex number as a string into a decimal integer. The method header is:

```java
public static int hex2Dec(String hexString)
```

Write a test program that prompts the user to enter a hex string and displays its decimal equivalent.

**18.25** *(String permutation)* Write a recursive method to print all the permutations of a string. For example, for the string *abc*, the permutation is:

```
abc 
acb 
bac 
bca 
cab 
cba
```

*(Hint: Define the following two methods. The second is a helper method.)*

```java
public static void displayPermutation(String s)
public static void displayPermutation(String s1, String s2)
```

The first method simply invokes `displayPermutation(" ", s)`. The second method uses a loop to move a character from `s2` to `s1` and recursively invokes it with a new `s1` and `s2`. The base case is that `s2` is empty and prints `s1` to the console.

Write a test program that prompts the user to enter a string and displays all its permutations.

**18.26** *(Create a maze)* Write a program that will find a path in a maze, as shown in Figure 18.13a. The maze is represented by an $8 \times 8$ board. The path must meet the following conditions:

- The path is between the upper-left corner cell and the lower-right corner cell in the maze.

![Figure 18.13](image)

(a) Correct path  
(b) Illegal path

*Figure 18.13* The program finds a path from the upper-left corner to the bottom-right corner.
The program enables the user to place or remove a mark on a cell. A path consists of adjacent unmarked cells. Two cells are said to be adjacent if they are horizontal or vertical neighbors, but not if they are diagonal neighbors.

- The path does not contain cells that form a square. The path in Figure 18.13b, for example, does not meet this condition. (The condition makes a path easy to identify on the board.)

**18.27** (Koch snowflake fractal) The text presented the Sierpinski triangle fractal. In this exercise, you will write a program to display another fractal, called the Koch snowflake, named after a famous Swedish mathematician. A Koch snowflake is created as follows:

1. Begin with an equilateral triangle, which is considered to be the Koch fractal of order (or level) 0, as shown in Figure 18.14a.
2. Divide each line in the shape into three equal line segments and draw an outward equilateral triangle with the middle line segment as the base to create a Koch fractal of order 1, as shown in Figure 18.14b.
3. Repeat Step 2 to create a Koch fractal of order 2, 3, . . . , and so on, as shown in Figure 18.14c–d.

**18.28** (Nonrecursive directory size) Rewrite Listing 18.7, DirectorySize.java, without using recursion.

**18.29** (Number of files in a directory) Write a program that prompts the user to enter a directory and displays the number of the files in the directory.

**18.30** (Find words) Write a program that finds all occurrences of a word in all the files under a directory, recursively. Pass the parameters from the command line as follows:

```
java Exercise18_30 dirName word
```

**18.31** (Replace words) Write a program that replaces all occurrences of a word with a new word in all the files under a directory, recursively. Pass the parameters from the command line as follows:

```
java Exercise18_31 dirName oldWord newWord
```

**18.32** (Game: Knight’s Tour) The Knight’s Tour is an ancient puzzle. The objective is to move a knight, starting from any square on a chessboard, to every other square once, as shown in Figure 18.15a. Note that the knight makes only L-shaped moves (two spaces in one direction and one space in a perpendicular direction). As shown in Figure 18.15b, the knight can move to eight squares. Write
a program that displays the moves for the knight, as shown in Figure 18.15c. When you click a cell, the knight is placed at the cell. This cell will be starting point for the knight. Clicking the Solve button to display the path for a solution.

Figure 18.15  (a) A knight traverses all squares once. (b) A knight makes an L-shaped move. (c) A program displays a Knight’s Tour path.

(Figure: A brute-force approach for this problem is to move the knight from one square to another available square arbitrarily. Using such an approach, your program will take a long time to finish. A better approach is to employ some heuristics. A knight has two, three, four, six, or eight possible moves, depending on its location. Intuitively, you should attempt to move the knight to the least accessible squares first and leave those more accessible squares open, so there will be a better chance of success at the end of the search.)

**18.33 (Game: Knight’s Tour animation) Write a program for the Knight’s Tour problem. Your program should let the user move a knight to any starting square and click the Solve button to animate a knight moving along the path, as shown in Figure 18.16.

Figure 18.16  A knight traverses along the path.

**18.34 (Game: Eight Queens) The Eight Queens problem is to find a solution to place a queen in each row on a chessboard such that no two queens can attack each other. Write a program to solve the Eight Queens problem using recursion and display the result as shown in Figure 18.17.
**18.35** (*H-tree fractal*) An H-tree (introduced at the beginning of this chapter in Figure 18.1) is a fractal defined as follows:

1. Begin with a letter H. The three lines of the H are of the same length, as shown in Figure 18.1a.
2. The letter H (in its sans-serif form, H) has four endpoints. Draw an H centered at each of the four endpoints to an H-tree of order 1, as shown in Figure 18.1b. These Hs are half the size of the H that contains the four endpoints.
3. Repeat Step 2 to create an H-tree of order 2, 3, . . . , and so on, as shown in Figure 18.1c–d.

Write a program that draws an H-tree, as shown in Figure 18.1.

**18.36** (*Sierpinski triangle*) Write a program that lets the user to enter the order and display the filled Sierpinski triangles as shown in Figure 18.18.

**18.37** (*Hilbert curve*) The Hilbert curve, first described by German mathematician David Hilbert in 1891, is a space-filling curve that visits every point in a square grid with a size of $2 \times 2, 4 \times 4, 8 \times 8, 16 \times 16$, or any other power of 2. Write a program that displays a Hilbert curve for the specified order, as shown in Figure 18.19.
**18.38** *(Recursive tree)* Write a program to display a recursive tree as shown in Figure 18.20.

**18.39** *(Dragging the tree)* Revise Programming Exercise 18.38 to move the tree to where the mouse is dragged.
Objectives

- To describe the benefits of generics (§19.2).
- To use generic classes and interfaces (§19.2).
- To define generic classes and interfaces (§19.3).
- To explain why generic types can improve reliability and readability (§19.3).
- To define and use generic methods and bounded generic types (§19.4).
- To develop a generic sort method to sort an array of Comparable objects (§19.5).
- To use raw types for backward compatibility (§19.6).
- To explain why wildcard generic types are necessary (§19.7).
- To describe generic type erasure and list certain restrictions and limitations on generic types caused by type erasure (§19.8).
- To design and implement generic matrix classes (§19.9).
19.1 Introduction

Generics enable you to detect errors at compile time rather than at runtime.

You have used a generic class `ArrayList` in Chapter 11 and generic interface `Comparable` in Chapter 13. Generics let you parameterize types. With this capability, you can define a class or a method with generic types that the compiler can replace with concrete types. For example, Java defines a generic `ArrayList` class for storing the elements of a generic type. From this generic class, you can create an `ArrayList` object for holding strings and an `ArrayList` object for holding numbers. Here, strings and numbers are concrete types that replace the generic type.

The key benefit of generics is to enable errors to be detected at compile time rather than at runtime. A generic class or method permits you to specify allowable types of objects that the class or method can work with. If you attempt to use an incompatible object, the compiler will detect that error.

This chapter explains how to define and use generic classes, interfaces, and methods and demonstrates how generics can be used to improve software reliability and readability. It can be intertwined with Chapter 13, Abstract Classes and Interfaces.

19.2 Motivations and Benefits

The motivation for using Java generics is to detect errors at compile time.

Java has allowed you to define generic classes, interfaces, and methods since JDK 1.5. Several interfaces and classes in the Java API were modified using generics. For example, prior to JDK 1.5 the `java.lang.Comparable` interface was defined as shown in Figure 19.1a, but since JDK 1.5 it is modified as shown in Figure 19.1b.

```
package java.lang;
public interface Comparable {
    public int compareTo(Object o);
}

package java.lang;
public interface Comparable<T> {
    public int compareTo(T o);
}
```

(a) Prior to JDK 1.5
(b) JDK 1.5

Figure 19.1 The `java.lang.Comparable` interface was modified in JDK 1.5 with a generic type

Here, `<T>` represents a *formal generic type*, which can be replaced later with an *actual concrete type*. Replacing a generic type is called a *generic instantiation*. By convention, a single capital letter such as `E` or `T` is used to denote a formal generic type.

To see the benefits of using generics, let us examine the code in Figure 19.2. The statement in Figure 19.2a declares that `c` is a reference variable whose type is `Comparable` and invokes the `compareTo` method to compare a `Date` object with a string. The code compiles fine, but it has a runtime error because a string cannot be compared with a date.

```
Comparable c = new Date();
System.out.println(c.compareTo("red"));
```

(a) Prior to JDK 1.5

```
Comparable<Date> c = new Date();
System.out.println(c.compareTo("red"));
```

(b) JDK 1.5

Figure 19.2 The new generic type detects possible errors at compile time.

The statement in Figure 19.2b declares that `c` is a reference variable whose type is `Comparable<Date>` and invokes the `compareTo` method to compare a `Date` object with a string. This code generates a compile error, because the argument passed to the `compareTo`
**Motivations and Benefits**

A method must be of the `Date` type. Since the errors can be detected at compile time rather than runtime, the generic type makes the program more reliable.

An `ArrayList` was introduced in Section 11.11, The `ArrayList` Class. This class has been a generic class since JDK 1.5. Figure 19.3 shows the class diagram for `ArrayList` before and since JDK 1.5, respectively.

![Class Diagram](image)

**Figure 19.3** `ArrayList` is a generic class since JDK 1.5.

For example, the following statement creates a list for strings:

```java
ArrayList<String> list = new ArrayList<>();
```

You can now add only strings into the list. For instance,

```java
list.add("Red");
```

If you attempt to add a nonstring, a compile error will occur. For example, the following statement is now illegal, because `list` can contain only strings.

```java
list.add(new Integer(1));
```

Generic types must be reference types. You cannot replace a generic type with a primitive type such as `int`, `double`, or `char`. For example, the following statement is wrong:

```java
ArrayList<Integer> intList = new ArrayList<>();
```

To create an `ArrayList` object for `int` values, you have to use:

```java
ArrayList<Integer> intList = new ArrayList<>();
```

You can add an `int` value to `intList`. For example,

```java
intList.add(5);
```

Java automatically wraps `5` into `new Integer(5)`. This is called *autoboxing*, as introduced in Section 10.8, Automatic Conversion between Primitive Types and Wrapper Class Types.
Casting is not needed to retrieve a value from a list with a specified element type, because the compiler already knows the element type. For example, the following statements create a list that contains strings, add strings to the list, and retrieve strings from the list.

```java
1  ArrayList<String> list = new ArrayList<>();
2  list.add("Red");
3  list.add("White");
4  String s = list.get(0); // No casting is needed
```

Prior to JDK 1.5, without using generics, you would have had to cast the return value to `String` as:

```java
String s = (String)(list.get(0)); // Casting needed prior to JDK 1.5
```

If the elements are of wrapper types, such as `Integer`, `Double`, and `Character`, you can directly assign an element to a primitive type variable. This is called autounboxing, as introduced in Section 10.8. For example, see the following code:

```java
1  ArrayList<Double> list = new ArrayList<>();
2  list.add(5.5); // 5.5 is automatically converted to new Double(5.5)
3  list.add(3.0); // 3.0 is automatically converted to new Double(3.0)
4  Double doubleObject = list.get(0); // No casting is needed
5  double d = list.get(1); // Automatically converted to double
```

In lines 2 and 3, `5.5` and `3.0` are automatically converted into `Double` objects and added to `list`. In line 4, the first element in `list` is assigned to a `Double` variable. No casting is necessary, because `list` is declared for `Double` objects. In line 5, the second element in `list` is assigned to a `double` variable. The object in `list.get(1)` is automatically converted into a primitive type value.

### 19.1 Are there any compile errors in (a) and (b)?

- (a) Prior to JDK 1.5
  ```java
  ArrayList dates = new ArrayList();
  dates.add(new Date());
  dates.add(new String());
  ```

- (b) Since JDK 1.5
  ```java
  ArrayList<Date> dates = new ArrayList<>();
  dates.add(new Date());
  dates.add(new String());
  ```

### 19.2 What is wrong in (a)? Is the code in (b) correct?

- (a) Prior to JDK 1.5
  ```java
  ArrayList dates = new ArrayList();
  dates.add(new Date());
  Date date = dates.get(0);
  ```

- (b) Since JDK 1.5
  ```java
  ArrayList<Date> dates = new ArrayList<>();
  dates.add(new Date());
  Date date = dates.get(0);
  ```

### 19.3 What are the benefits of using generic types?

**A generic type can be defined for a class or interface. A concrete type must be specified when using the class to create an object or using the class or interface to declare a reference variable.**
Let us revise the stack class in Section 11.13, Case Study: A Custom Stack Class, to generalize the element type with a generic type. The new stack class, named `GenericStack`, is shown in Figure 19.4 and is implemented in Listing 19.1.

```
GenericStack<E>
- list: java.util.ArrayList<E>
+ GenericStack()
+ getSize(): int
+ peek(): E
+ pop(): E
+ push(o: E): void
+ isEmpty(): boolean

FIGURE 19.4 The GenericStack class encapsulates the stack storage and provides the operations for manipulating the stack.
```

### Listing 19.1 `GenericStack.java`

```java
public class GenericStack<E> {
  private java.util.ArrayList<E> list = new java.util.ArrayList<>();

  public int getSize() {
    return list.size();
  }

  public E peek() {
    return list.get(getSize() - 1);
  }

  public void push(E o) {
    list.add(o);
  }

  public E pop() {
    E o = list.get(getSize() - 1);
    list.remove(getSize() - 1);
    return o;
  }

  public boolean isEmpty() {
    return list.isEmpty();
  }

  @Override
  public String toString() {
    return "stack: " + list.toString();
  }
}
```

The following example creates a stack to hold strings and adds three strings to the stack:

```java
GenericStack<String> stack1 = new GenericStack<>();
stack1.push("London");
stack1.push("Paris");
stack1.push("Berlin");
```
This example creates a stack to hold integers and adds three integers to the stack:

```java
GenericStack<Integer> stack2 = new GenericStack<>();
stack2.push(1); // autoboxing 1 to new Integer(1)
stack2.push(2);
stack2.push(3);
```

Instead of using a generic type, you could simply make the type element `Object`, which can accommodate any object type. However, using generic types can improve software reliability and readability, because certain errors can be detected at compile time rather than at runtime. For example, because `stack1` is declared `GenericStack<String>`, only strings can be added to the stack. It would be a compile error if you attempted to add an integer to `stack1`.

---

**Caution**

To create a stack of strings, you use `new GenericStack<String>()` or `new GenericStack<>()`. This could mislead you into thinking that the constructor of `GenericStack` should be defined as

```
public GenericStack<E>()
```

This is wrong. It should be defined as

```
public GenericStack()
```

---

**Note**

Occasionally, a generic class may have more than one parameter. In this case, place the parameters together inside the brackets, separated by commas—for example, `<E1, E2, E3>`.

---

**Note**

You can define a class or an interface as a subtype of a generic class or interface. For example, the `java.lang.String` class is defined to implement the `Comparable` interface in the Java API as follows:

```
public class String implements Comparable<String>
```

---

19.4 What is the generic definition for `java.lang.Comparable` in the Java API?

19.5 Since you create an instance of `ArrayList` of strings using `new ArrayList<String>()`, should the constructor in the `ArrayList` class be defined as

```
public ArrayList<E>()
```

19.6 Can a generic class have multiple generic parameters?

19.7 How do you declare a generic type in a class?

---

### 19.4 Generic Methods

A generic type can be defined for a static method.

You can define generic interfaces (e.g., the `Comparable` interface in Figure 19.1b) and classes (e.g., the `GenericStack` class in Listing 19.1). You can also use generic types to define generic methods. For example, Listing 19.2 defines a generic method `print` (lines 10–14) to print an array of objects. Line 6 passes an array of integer objects to invoke the generic `print` method. Line 7 invokes `print` with an array of strings.
To declare a generic method, you place the generic type `<E>` immediately after the keyword `static` in the method header. For example,

```
public static <E> void print(E[] list) {
    for (int i = 0; i < list.length; i++)
        System.out.print(list[i] + " ");
    System.out.println();
}
```

to invoke a generic method, prefix the method name with the actual type in angle brackets. For example,

```
GenericMethodDemo.<Integer>print(integers);
GenericMethodDemo.<String>print(strings);
```
or simply invoke it as follows:

```
print(integers);
print(strings);
```

In the latter case, the actual type is not explicitly specified. The compiler automatically discovers the actual type.

A generic type can be specified as a subtype of another type. Such a generic type is called bounded. For example, Listing 19.3 revises the `equalArea` method in Listing 13.4, `TestGeometricObject.java`, to test whether two geometric objects have the same area. The bounded generic type `<E extends GeometricObject>` (line 7) specifies that `E` is a generic subtype of `GeometricObject`. You must invoke `equalArea` by passing two instances of `GeometricObject`.

```
public static <E extends GeometricObject> boolean equalArea(E object1, E object2) {
    return object1.getArea() == object2.getArea();
}
```
Note
An unbounded generic type <E> is the same as <E extends Object>.

Note
To define a generic type for a class, place it after the class name, such as GenericStack<E>. To define a generic type for a method, place the generic type before the method return type, such as <E> void max(E o1, E o2).

19.8 How do you declare a generic method? How do you invoke a generic method?
19.9 What is a bounded generic type?

19.5 Case Study: Sorting an Array of Objects
You can develop a generic method for sorting an array of Comparable objects.

This section presents a generic method for sorting an array of Comparable objects. The objects are instances of the Comparable interface, and they are compared using the compareTo method. To test the method, the program sorts an array of integers, an array of double numbers, an array of characters, and an array of strings. The program is shown in Listing 19.4.

Listing 19.4 GenericSort.java

```java
public class GenericSort {
    public static void main(String[] args) {
        // Create an Integer array
        Integer[] intArray = {new Integer(2), new Integer(4),
                              new Integer(3)};

        // Create a Double array
        Double[] doubleArray = {new Double(3.4), new Double(1.3),
                                new Double(-22.1)};

        // Create a Character array
        Character[] charArray = {new Character('a'),
                                 new Character('J'), new Character('r')};

        // Create a String array
        String[] stringArray = {"Tom", "Susan", "Kim"};

        // Sort the arrays
        sort(intArray);
        sort(doubleArray);
        sort(charArray);
        sort(stringArray);

        // Display the sorted arrays
        System.out.print("Sorted Integer objects: ");
        printList(intArray);
        System.out.print("Sorted Double objects: ");
        printList(doubleArray);
        System.out.print("Sorted Character objects: ");
        printList(charArray);
        System.out.print("Sorted String objects: ");
        printList(stringArray);
    }
}
```

sort Integer objects
sort Double objects
sort Character objects
sort String objects
19.5 Case Study: Sorting an Array of Objects

```java
/** Sort an array of comparable objects */
public static <E extends Comparable<E>> void sort(E[] list) {
    E currentMin;
    int currentMinIndex;

    for (int i = 0; i < list.length - 1; i++) {
        // Find the minimum in the list[i+1..list.length-2]
        currentMin = list[i];
        currentMinIndex = i;

        for (int j = i + 1; j < list.length; j++) {
            if (currentMin.compareTo(list[j]) > 0) {
                currentMin = list[j];
                currentMinIndex = j;
            }
        }

        // Swap list[i] with list[currentMinIndex] if necessary;
        if (currentMinIndex != i) {
            list[currentMinIndex] = list[i];
            list[i] = currentMin;
        }
    }

    /** Print an array of objects */
    public static void printList(Object[] list) {
        for (int i = 0; i < list.length; i++)
            System.out.print(list[i] + " ");
        System.out.println();
    }
}
```

Sorted Integer objects: 2 3 4
Sorted Double objects: -22.1 1.3 3.4
Sorted Character objects: J a r
Sorted String objects: Kim Susan Tom

The algorithm for the `sort` method is the same as in Listing 7.8, SelectionSort.java. The `sort` method in that program sorts an array of `double` values. The `sort` method in this example can sort an array of any object type, provided that the objects are also instances of the `Comparable` interface. The generic type is defined as `<E extends Comparable<E>>` (line 36). This has two meanings. First, it specifies that `E` is a subtype of `Comparable`. Second, it specifies that the elements to be compared are of the `E` type as well.

The `sort` method uses the `compareTo` method to determine the order of the objects in the array (line 46). `Integer`, `Double`, `Character`, and `String` implement `Comparable`, so the objects of these classes can be compared using the `compareTo` method. The program creates arrays of `Integer` objects, `Double` objects, `Character` objects, and `String` objects (lines 4–16) and invoke the `sort` method to sort these arrays (lines 19–22).

19.10 Given `int[] list = {1, 2, -1}`, can you invoke `sort(list)` using the `sort` method in Listing 19.4?

19.11 Given `int[] list = {new Integer(1), new Integer(2), new Integer(-1)}`, can you invoke `sort(list)` using the `sort` method in Listing 19.4?
19.6 Raw Types and Backward Compatibility

A generic class or interface used without specifying a concrete type, called a raw type, enables backward compatibility with earlier versions of Java.

You can use a generic class without specifying a concrete type like this:

```java
GenericStack stack = new GenericStack(); // raw type
```

This is roughly equivalent to

```java
GenericStack<Object> stack = new GenericStack<Object>();
```

A generic class such as `GenericStack` and `ArrayList` used without a type parameter is called a raw type. Using raw types allows for backward compatibility with earlier versions of Java. For example, a generic type has been used in `java.lang.Comparable` since JDK 1.5, but a lot of code still uses the raw type `Comparable`, as shown in Listing 19.5:

```
LISTING 19.5 Max.java
1 public class Max {
2     /** Return the maximum of two objects */
3     public static Comparable max(Comparable o1, Comparable o2) {
4         if (o1.compareTo(o2) > 0)
5             return o1;
6         else
7             return o2;
8     }
9 }
```

`Comparable o1` and `Comparable o2` are raw type declarations. Be careful: raw types are unsafe. For example, you might invoke the `max` method using

```java
Max.max("Welcome", 23); // 23 is autoboxed into new Integer(23)
```

This would cause a runtime error, because you cannot compare a string with an integer object. The Java compiler displays a warning on line 3 when compiled with the option `-Xlint:unchecked`, as shown in Figure 19.5.

```
FIGURE 19.5 The unchecked warnings are displayed using the compiler option
-Xlint:unchecked.
```

A better way to write the `max` method is to use a generic type, as shown in Listing 19.6.

```
LISTING 19.6 MaxUsingGenericType.java
1 public class MaxUsingGenericType {
2     /** Return the maximum of two objects */
3     public static <E extends Comparable<E>> E max(E o1, E o2) {
4         if (o1.compareTo(o2) > 0)
5             return o1;
6         else
7             return o2;
8     }
9 }
```

If you invoke the `max` method using

```java
    // 23 is autoboxed into new Integer(23)
    MaxUsingGenericType.max("Welcome", 23);
```

a compile error will be displayed, because the two arguments of the `max` method in `MaxUsingGenericType` must have the same type (e.g., two strings or two integer objects). Furthermore, the type `E` must be a subtype of `Comparable<E>`.

As another example, in the following code you can declare a raw type `stack` in line 1, assign `new GenericStack<String>` to it in line 2, and push a string and an integer object to the stack in lines 3 and 4.

```java
1  GenericStack stack;
2  stack = new GenericStack<String>();
3  stack.push("Welcome to Java");
4  stack.push(new Integer(2));
```

However, line 4 is unsafe because the stack is intended to store strings, but an `Integer` object is added into the stack. Line 3 should be okay, but the compiler will show warnings for both line 3 and line 4, because it cannot follow the semantic meaning of the program. All the compiler knows is that stack is a raw type, and performing certain operations is unsafe. Therefore, warnings are displayed to alert potential problems.

**Tip**

Since raw types are unsafe, this book will not use them from here on.

19.12 What is a raw type? Why is a raw type unsafe? Why is the raw type allowed in Java?

19.13 What is the syntax to declare an `ArrayList` reference variable using the raw type and assign a raw type `ArrayList` object to it?

### 19.7 Wildcard Generic Types

You can use unbounded wildcards, bounded wildcards, or lower-bound wildcards to specify a range for a generic type.

What are wildcard generic types and why are they needed? Listing 19.7 gives an example to demonstrate the needs. The example defines a generic `max` method for finding the maximum in a stack of numbers (lines 12–22). The main method creates a stack of integer objects, adds three integers to the stack, and invokes the `max` method to find the maximum number in the stack.

**Listing 19.7 WildCardNeedDemo.java**

```java
public class WildCardNeedDemo {
    public static void main(String[] args) {
        GenericStack<Integer> intStack = new GenericStack<>();
        intStack.push(1); // 1 is autoboxed into new Integer(1)
        intStack.push(2);
        intStack.push(-2);
        System.out.print("The max number is "+ max(intStack));
    }
}
```
/** Find the maximum in a stack of numbers */

public static double max(GenericStack<Number> stack) {
    double max = stack.pop().doubleValue(); // Initialize max
    while (!stack.isEmpty()) {
        double value = stack.pop().doubleValue();
        if (value > max)
            max = value;
    }
    return max;
}

The program in Listing 19.7 has a compile error in line 8 because intStack is not an instance of GenericStack<Number>. Thus, you cannot invoke max(intStack).

The fact is that Integer is a subtype of Number, but GenericStack<Integer> is not a subtype of GenericStack<Number>. To circumvent this problem, use wildcard generic types. A wildcard generic type has three forms: ? and ? extends T, as well as ? super T, where T is a generic type.

The first form, ?, called an unbounded wildcard, is the same as ? extends Object. The second form, ? extends T, called a bounded wildcard, represents T or a subtype of T. The third form, ? super T, called a lower-bound wildcard, denotes T or a supertype of T.

You can fix the error by replacing line 12 in Listing 19.7 as follows:

    public static double max(GenericStack<? extends Number> stack) {
        // ...
    }

<? extends Number> is a wildcard type that represents Number or a subtype of Number, so it is legal to invoke max(new GenericStack<Integer>()) or max(new GenericStack<Double>().

Listing 19.8 shows an example of using the ? wildcard in the print method that prints objects in a stack and empties the stack. <?> is a wildcard that represents any object type. It is equivalent to <? extends Object>. What happens if you replace GenericStack<?> with GenericStack<Object>? It would be wrong to invoke print(intStack), because intStack is not an instance of GenericStack<Object>. Please note that GenericStack<Integer> is not a subtype of GenericStack<Object>, even though Integer is a subtype of Object.

**LISTING 19.8 AnyWildCardDemo.java**

```java
public class AnyWildCardDemo {
    public static void main(String[] args) {
        GenericStack<Integer> intStack = new GenericStack<>();
        intStack.push(1); // 1 is autoboxed into new Integer(1)
        intStack.push(2);
        intStack.push(-2);
        print(intStack);
    }
    public static void print(GenericStack<?> stack) {
        while (!stack.isEmpty()) {
            System.out.print(stack.pop() + " ");
        }
    }
}
```
When is the wildcard $<? \text{ super } T>$ needed? Consider the example in Listing 19.9. The example creates a stack of strings in $\text{stack1}$ (line 3) and a stack of objects in $\text{stack2}$ (line 4), and invokes $\text{add(stack1, stack2)}$ (line 8) to add the strings in $\text{stack1}$ into $\text{stack2}$. $\text{GenericStack}\langle ? \text{ super } T \rangle$ is used to declare $\text{stack2}$ in line 13. If $\langle ? \text{ super } T \rangle$ is replaced by $\langle T \rangle$, a compile error will occur on $\text{add(stack1, stack2)}$ in line 8, because $\text{stack1}$’s type is $\text{GenericStack}\langle \text{String} \rangle$ and $\text{stack2}$’s type is $\text{GenericStack}\langle \text{Object} \rangle$. $\langle ? \text{ super } T \rangle$ represents type $T$ or a supertype of $T$. $\text{Object}$ is a supertype of $\text{String}$.

**LISTING 19.9**  
**SuperWildCardDemo.java**

```java
1 public class SuperWildCardDemo {
2   public static void main(String[] args) {
3     GenericStack<String> stack1 = new GenericStack<>();
4     GenericStack<Object> stack2 = new GenericStack<>();
5     stack2.push("Java");
6     stack2.push(2);
7     stack1.push("Sun");
8     add(stack1, stack2);
9     AnyWildCardDemo.print(stack2);
10   }
11
12   public static <T> void add(GenericStack<T> stack1,
13                               GenericStack<? super T> stack2) {
14     while (!stack1.isEmpty())
15       stack2.push(stack1.pop());
16   }
17 }
```

This program will also work if the method header in lines 12–13 is modified as follows:

```java
12   public static <T> void add(GenericStack<? super T> stack1,
13                               GenericStack<T> stack2)
```

The inheritance relationship involving generic types and wildcard types is summarized in Figure 19.6. In this figure, $A$ and $B$ represent classes or interfaces, and $E$ is a generic type parameter.

![Figure 19.6](image)

**FIGURE 19.6**  
The relationship between generic types and wildcard types.

19.14 Is $\text{GenericStack}$ the same as $\text{GenericStack}\langle \text{Object} \rangle$?  
19.15 What are an unbounded wildcard, a bounded wildcard, and a lower-bound wildcard?  
19.16 What happens if lines 12–13 in Listing 19.9 are changed to

```java
12   public static <T> void add(GenericStack<T> stack1,
13                               GenericStack<T> stack2)
```
19.17 What happens if lines 12–13 in Listing 19.9 are changed to

```
public static <T> void add(GenericStack<? extends T> stack1, GenericStack<T> stack2)
```

19.8 Erasure and Restrictions on Generics

The information on generics is used by the compiler but is not available at runtime. This is called type erasure.

Generics are implemented using an approach called type erasure: The compiler uses the generic type information to compile the code, but erases it afterward. Thus, the generic information is not available at runtime. This approach enables the generic code to be backward compatible with the legacy code that uses raw types.

The generics are present at compile time. Once the compiler confirms that a generic type is used safely, it converts the generic type to a raw type. For example, the compiler checks whether the following code in (a) uses generics correctly and then translates it into the equivalent code in (b) for runtime use. The code in (b) uses the raw type.

```
ArrayList<String> list = new ArrayList<>();
list.add("Oklahoma");
String state = list.get(0);
```

(a)  
```
ArrayList list = new ArrayList();
list.add("Oklahoma");
String state = (String)(list.get(0));
```

(b)

replace generic type

When generic classes, interfaces, and methods are compiled, the compiler replaces the generic type with the `Object` type. For example, the compiler would convert the following method in (a) into (b).

```
public static <E> void print(E[] list) {
    for (int i = 0; i < list.length; i++)
        System.out.print(list[i] + " ");
    System.out.println();
}
```

(a)  
```
public static void print(Object[] list) {
    for (int i = 0; i < list.length; i++)
        System.out.print(list[i] + " ");
    System.out.println();
}
```

(b)

replace bounded type

If a generic type is bounded, the compiler replaces it with the `Object` type. For example, the compiler would convert the following method in (a) into (b).

```
public static <E extends GeometricObject> boolean equalArea(
    E object1,
    E object2) {
    return object1.getArea() == 
        object2.getArea();
}
```

(a)  
```
public static boolean equalArea(
    GeometricObject object1,
    GeometricObject object2) {
    return object1.getArea() ==
        object2.getArea();
}
```

(b)

important fact

It is important to note that a generic class is shared by all its instances regardless of its actual concrete type. Suppose `list1` and `list2` are created as follows:

```
ArrayList<String> list1 = new ArrayList<>();
ArrayList<Integer> list2 = new ArrayList<>();
```
Although `ArrayList<String>` and `ArrayList<Integer>` are two types at compile time, only one `ArrayList` class is loaded into the JVM at runtime. `list1` and `list2` are both instances of `ArrayList`, so the following statements display `true`:

```java
System.out.println(list1 instanceof ArrayList);
System.out.println(list2 instanceof ArrayList);
```

However, the expression `list1 instanceof ArrayList<String>` is wrong. Since `ArrayList<String>` is not stored as a separate class in the JVM, using it at runtime makes no sense.

Because generic types are erased at runtime, there are certain restrictions on how generic types can be used. Here are some of the restrictions:

**Restriction 1: Cannot Use `new E()`**

You cannot create an instance using a generic type parameter. For example, the following statement is wrong:

```java
E object = new E();
```

The reason is that `new E()` is executed at runtime, but the generic type `E` is not available at runtime.

**Restriction 2: Cannot Use `new E[]`**

You cannot create an array using a generic type parameter. For example, the following statement is wrong:

```java
E[] elements = new E[capacity];
```

You can circumvent this limitation by creating an array of the `Object` type and then casting it to `E[]`, as follows:

```java
E[] elements = (E[]) new Object[capacity];
```

However, casting to `(E[])` causes an unchecked compile warning. The warning occurs because the compiler is not certain that casting will succeed at runtime. For example, if `E` is `String` and `new Object[]` is an array of `Integer` objects, `(String[])(new Object[])` will cause a `ClassCastException`. This type of compile warning is a limitation of Java generics and is unavoidable.

**Restriction 3: A Generic Type Parameter of a Class Is Not Allowed in a Static Context**

Since all instances of a generic class have the same runtime class, the static variables and methods of a generic class are shared by all its instances. Therefore, it is illegal to refer to
a generic type parameter for a class in a static method, field, or initializer. For example, the following code is illegal:

```java
public class Test<E> {
    public static void m(E o1) { // Illegal
    }
    public static E o1; // Illegal
    static {
        E o2; // Illegal
    }
}
```

**Restriction 4: Exception Classes Cannot Be Generic**

A generic class may not extend `java.lang.Throwable`, so the following class declaration would be illegal:

```java
public class MyException<T> extends Exception {
}
```

Why? If it were allowed, you would have a `catch` clause for `MyException<T>` as follows:

```java
try {
    ...
} catch (MyException<T> ex) {
    ...
}
```

The JVM has to check the exception thrown from the `try` clause to see if it matches the type specified in a `catch` clause. This is impossible, because the type information is not present at runtime.

**19.18** What is erasure? Why are Java generics implemented using erasure?

**19.19** If your program uses `ArrayList<String>` and `ArrayList<Date>`, does the JVM load both of them?

**19.20** Can you create an instance using `new E()` for a generic type `E`? Why?

**19.21** Can a method that uses a generic class parameter be static? Why?

**19.22** Can you define a custom generic exception class? Why?

**19.9 Case Study: Generic Matrix Class**

This section presents a case study on designing classes for matrix operations using generic types.

The addition and multiplication operations for all matrices are similar except that their element types differ. Therefore, you can design a superclass that describes the common operations shared by matrices of all types regardless of their element types, and you can define subclasses tailored to specific types of matrices. This case study gives implementations for two types: `int` and `Rational`. For the `int` type, the wrapper class `Integer` should be used to wrap an `int` value into an object, so that the object is passed in the methods for operations.

The class diagram is shown in Figure 19.7. The methods `addMatrix` and `multiplyMatrix` add and multiply two matrices of a generic type `E[][]`. The static method `printResult` displays the matrices, the operator, and their result. The methods `add`, `multiply`, and `zero` are abstract, because their implementations depend on the specific type of the array elements. For example, the `zero()` method returns `0` for the
**Case Study: Generic Matrix Class**

The **GenericMatrix** class is an abstract superclass for **IntegerMatrix** and **RationalMatrix**.

**Integer** type and 0/1 for the **Rational** type. These methods will be implemented in the subclasses in which the matrix element type is specified.

**IntegerMatrix** and **RationalMatrix** are concrete subclasses of **GenericMatrix**. These two classes implement the `add`, `multiply`, and `zero` methods defined in the **GenericMatrix** class.

Listing 19.10 implements the **GenericMatrix** class. `<E extends Number>` in line 1 specifies that the generic type is a subtype of **Number**. Three abstract methods—`add`, `multiply`, and `zero`—are defined in lines 3, 6, and 9. These methods are abstract because we cannot implement them without knowing the exact type of the elements. The `addMatrix` (lines 12–30) and `multiplyMatrix` (lines 33–57) methods implement the methods for adding and multiplying two matrices. All these methods must be nonstatic, because they use generic type `E` for the class. The `printResult` method (lines 60–84) is static because it is not tied to specific instances.

The matrix element type is a generic subtype of **Number**. This enables you to use an object of any subclass of **Number** as long as you can implement the abstract `add`, `multiply`, and `zero` methods in subclasses.

The `addMatrix` and `multiplyMatrix` methods (lines 12–57) are concrete methods. They are ready to use as long as the `add`, `multiply`, and `zero` methods are implemented in the subclasses.

The `addMatrix` and `multiplyMatrix` methods check the bounds of the matrices before performing operations. If the two matrices have incompatible bounds, the program throws an exception (lines 16, 36).

**Listing 19.10  GenericMatrix.java**

```java
public abstract class GenericMatrix<E extends Number> {
    /** Abstract method for adding two elements of the matrices */
    protected abstract E add(E o1, E o2);

    /** Abstract method for multiplying two elements of the matrices */
    protected abstract E multiply(E o1, E o2);

    /** Abstract method for defining zero for the matrix element */
    protected abstract E zero();

    /** Add two matrices */
    public E[][] addMatrix(E[][] matrix1, E[][] matrix2) {
        // Check bounds of the two matrices
        if ((matrix1.length != matrix2.length) ||
            (matrix1[0].length != matrix2[0].length)) {
            throw new RuntimeException(
                "The matrices do not have the same size");
        }
    }
}
```

**Figure 19.7** The **GenericMatrix** class is an abstract superclass for **IntegerMatrix** and **RationalMatrix**.
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```java
E[][] result =
    (E[][])new Number[matrix1.length][matrix1[0].length];

    for (int i = 0; i < result.length; i++)
        for (int j = 0; j < result[i].length; j++) {
            result[i][j] = add(matrix1[i][j], matrix2[i][j]);
        }
    return result;
}

/** Multiply two matrices */
public E[][] multiplyMatrix(E[][] matrix1, E[][] matrix2) {
    if (matrix1[0].length != matrix2.length) {
        throw new RuntimeException(
            "The matrices do not have compatible size");
    }

    E[][] result = (E[][])new Number[matrix1.length][matrix2[0].length];

    for (int i = 0; i < result.length; i++) {
        for (int j = 0; j < result[i].length; j++) {
            result[i][j] = zero();
            for (int k = 0; k < matrix1[0].length; k++) {
                result[i][j] = add(result[i][j],
                                   multiply(matrix1[i][k], matrix2[k][j]));
            }
        }
    }
    return result;
}

/** Print matrices, the operator, and their operation result */
public static void printResult(
    Number[][] m1, Number[][] m2, Number[][] m3, char op) {
    for (int i = 0; i < m1.length; i++) {
        for (int j = 0; j < m1[0].length; j++)
            System.out.print(" "+ m1[i][j]);
        System.out.print(" = ");
    }
}
```
Listing 19.11 implements the `IntegerMatrix` class. The class extends `GenericMatrix<Integer>` in line 1. After the generic instantiation, the `add` method in `GenericMatrix<Integer>` is now `Integer add(Integer o1, Integer o2)`. The `add`, `multiply`, and `zero` methods are implemented for `Integer` objects. These methods are still protected, because they are invoked only by the `addMatrix` and `multiplyMatrix` methods.

```java
public class IntegerMatrix extends GenericMatrix<Integer> {
    @Override /** Add two integers */
    protected Integer add(Integer o1, Integer o2) {
        return o1 + o2;
    }

    @Override /** Multiply two integers */
    protected Integer multiply(Integer o1, Integer o2) {
        return o1 * o2;
    }

    @Override /** Specify zero for an integer */
    protected Integer zero() {
        return 0;
    }
}
```

Listing 19.12 implements the `RationalMatrix` class. The `Rational` class was introduced in Listing 13.13 Rational.java. `Rational` is a subtype of `Number`. The `RationalMatrix` class extends `GenericMatrix<Rational>` in line 1. After the generic instantiation, the `add` method in `GenericMatrix<Rational>` is now `Rational add(Rational r1, Rational r2)`. The `add`, `multiply`, and `zero` methods are implemented for `Rational` objects. These methods are still protected, because they are invoked only by the `addMatrix` and `multiplyMatrix` methods.

```java
public class RationalMatrix extends GenericMatrix<Rational> {
    @Override /** Add two rational numbers */
    protected Rational add(Rational r1, Rational r2) {
        return r1.add(r2);
    }

    @Override /** Multiply two rational numbers */
    protected Rational multiply(Rational r1, Rational r2) {
        return r1.multiply(r2);
    }

    @Override /** Specify zero for a Rational number */
    protected Rational zero() {
        return new Rational(0, 1);
    }
}
```
Listing 19.13 gives a program that creates two Integer matrices (lines 4–5) and an IntegerMatrix object (line 8), and adds and multiplies two matrices in lines 12 and 16.

**LISTING 19.13** TestIntegerMatrix.java

```java
public class TestIntegerMatrix {
    public static void main(String[] args) {
        // Create Integer arrays m1, m2
        Integer[][] m1 = new Integer[][] {{1, 2, 3}, {4, 5, 6}, {1, 1, 1}};
        Integer[][] m2 = new Integer[][] {{1, 1, 1}, {2, 2, 2}, {0, 0, 0}};

        // Create an instance of IntegerMatrix
        IntegerMatrix integerMatrix = new IntegerMatrix();

        System.out.println("m1 + m2 is ");
        GenericMatrix.printResult(m1, m2, integerMatrix.addMatrix(m1, m2), '+');

        System.out.println("m1 * m2 is ");
        GenericMatrix.printResult(m1, m2, integerMatrix.multiplyMatrix(m1, m2), '*');
    }
}
```

```
m1 + m2 is
1 2 3  1 1 1  2 3 4
4 5 6  +  2 2 2  =  6 7 8
1 1 1  0 0 0  1 1 1

m1 * m2 is
1 2 3  1 1 1  5 5 5
4 5 6  *  2 2 2  =  14 14 14
1 1 1  0 0 0  3 3 3
```

Listing 19.14 gives a program that creates two Rational matrices (lines 4–10) and a RationalMatrix object (line 13) and adds and multiplies two matrices in lines 17 and 19.

**LISTING 19.14** TestRationalMatrix.java

```java
public class TestRationalMatrix {
    public static void main(String[] args) {
        // Create two Rational arrays m1 and m2
        Rational[][] m1 = new Rational[3][3];
        Rational[][] m2 = new Rational[3][3];

        for (int i = 0; i < m1.length; i++)
            for (int j = 0; j < m1[0].length; j++) {
                m1[i][j] = new Rational(i + 1, j + 5);
                m2[i][j] = new Rational(i + 1, j + 6);
            }

        // Create an instance of RationalMatrix
        RationalMatrix rationalMatrix = new RationalMatrix();

        System.out.println("m1 + m2 is ");
        GenericMatrix.printResult(m1, m2, rationalMatrix.addMatrix(m1, m2), '+');

        System.out.println("m1 * m2 is ");
        GenericMatrix.printResult(m1, m2, rationalMatrix.multiplyMatrix(m1, m2), '*');
    }
}
```
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19.23 Why are the `add`, `multiple`, and `zero` methods defined abstract in the `GenericMatrix` class?

19.24 How are the `add`, `multiple`, and `zero` methods implemented in the `IntegerMatrix` class?

19.25 How are the `add`, `multiple`, and `zero` methods implemented in the `RationalMatrix` class?

19.26 What would be wrong if the `printResult` method defined as follows?

   ```java
   public static void printResult(
       E[][] m1, E[][] m2, E[][] m3,
       char op)
   ```

---

### Key Terms

- **actual concrete type**: 738
- **bounded generic type**: 743
- **bounded wildcard**: 748
- **formal generic type**: 738
- **lower-bound wildcard**: (`<? super E>`) 748
- **raw type**: 746
- **unbounded wildcard**: (`<?`) 748

---

### Chapter Summary

1. **Generics** give you the capability to parameterize types. You can define a class or a method with generic types, which the compiler replaces with concrete types.

2. The key benefit of generics is to enable errors to be detected at compile time rather than at runtime.

3. A generic class or method permits you to specify allowable types of objects that the class or method can work with. If you attempt to use a class or method with an incompatible object, the compiler will detect the error.

4. A generic type defined in a class, interface, or a static method is called a **formal generic type**, which can be replaced later with an **actual concrete type**. Replacing a generic type is called a **generic instantiation**.
5. A generic class such as `ArrayList` used without a type parameter is called a **raw type**. Use of raw types is allowed for backward compatibility with the earlier versions of Java.

6. A wildcard generic type has three forms: `?`, `? extends T`, and `? super T`, where `T` is a generic type. The first form, `?`, called an **unbounded wildcard**, is the same as `? extends Object`. The second form, `? extends T`, called a **bounded wildcard**, represents `T` or a subtype of `T`. The third form, `? super T`, called a **lower-bound wildcard**, denotes `T` or a supertype of `T`.

7. Generics are implemented using an approach called **type erasure**. The compiler uses the generic type information to compile the code but erases it afterward, so the generic information is not available at runtime. This approach enables the generic code to be backward compatible with the legacy code that uses raw types.

8. You cannot create an instance using a generic type parameter.

9. You cannot create an array using a generic type parameter.

10. You cannot use a generic type parameter of a class in a static context.

11. Generic type parameters cannot be used in exception classes.

**Quiz**

Answer the quiz for this chapter online at [www.cs.armstrong.edu/liang/intro10e/quiz.html](http://www.cs.armstrong.edu/liang/intro10e/quiz.html).

**Programming Exercises**

19.1 *(Revising Listing 19.1)* Revise the `GenericStack` class in Listing 19.1 to implement it using an array rather than an `ArrayList`. You should check the array size before adding a new element to the stack. If the array is full, create a new array that doubles the current array size and copy the elements from the current array to the new array.

19.2 *(Implement `GenericStack` using inheritance)* In Listing 19.1, `GenericStack` is implemented using composition. Define a new stack class that extends `ArrayList`. Draw the UML diagram for the classes and then implement `GenericStack`. Write a test program that prompts the user to enter five strings and displays them in reverse order.

19.3 *(Distinct elements in `ArrayList`)* Write the following method that returns a new `ArrayList`. The new list contains the non-duplicate elements from the original list.

```java
public static <E> ArrayList<E> removeDuplicates(ArrayList<E> list)
```

19.4 *(Generic linear search)* Implement the following generic method for linear search.

```java
public static <E extends Comparable<E>> int linearSearch(E[] list, E key)
```

19.5 *(Maximum element in an array)* Implement the following method that returns the maximum element in an array.

```java
public static <E extends Comparable<E>> E max(E[] list)
```
19.6 (Maximum element in a two-dimensional array) Write a generic method that returns the maximum element in a two-dimensional array.

```java
public static <E extends Comparable<E>> E max(E[][] list)
```

19.7 (Generic binary search) Implement the following method using binary search.

```java
public static <E extends Comparable<E>>
int binarySearch(E[] list, E key)
```

19.8 (Shuffle ArrayList) Write the following method that shuffles an ArrayList:

```java
public static <E> void shuffle(ArrayList<E> list)
```

19.9 (Sort ArrayList) Write the following method that sorts an ArrayList:

```java
public static <E extends Comparable<E>>
void sort(ArrayList<E> list)
```

19.10 (Largest element in ArrayList) Write the following method that returns the largest element in an ArrayList:

```java
public static <E extends Comparable<E>> E max(ArrayList<E> list)
```

19.11 (ComplexMatrix) Use the Complex class introduced in Programming Exercise 13.17 to develop the ComplexMatrix class for performing matrix operations involving complex numbers. The ComplexMatrix class should extend the GenericMatrix class and implement the add, multiple, and zero methods. You need to modify GenericMatrix and replace every occurrence of Number by Object, because Complex is not a subtype of Number. Write a test program that creates the following two matrices and displays the result of addition and multiplication of the matrices by invoking the printResult method.
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Lists, Stacks, Queues, and Priority Queues

Objectives

- To explore the relationship between interfaces and classes in the Java Collections Framework hierarchy (§20.2).
- To use the common methods defined in the `Collection` interface for operating collections (§20.2).
- To use the `Iterator` interface to traverse the elements in a collection (§20.3).
- To use a foreach loop to traverse the elements in a collection (§20.3).
- To explore how and when to use `ArrayList` or `LinkedList` to store a list of elements (§20.4).
- To compare elements using the `Comparable` interface and the `Comparator` interface (§20.5).
- To use the static utility methods in the `Collections` class for sorting, searching, shuffling lists, and finding the largest and smallest element in collections (§20.6).
- To develop a multiple bouncing balls application using `ArrayList` (§20.7).
- To distinguish between `Vector` and `ArrayList` and to use the `Stack` class for creating stacks (§20.8).
- To explore the relationships among `Collection`, `Queue`, `LinkedList`, and `PriorityQueue` and to create priority queues using the `PriorityQueue` class (§20.9).
- To use stacks to write a program to evaluate expressions (§20.10).
20.1 Introduction

Choosing the best data structures and algorithms for a particular task is one of the keys to developing high-performance software.

A data structure is a collection of data organized in some fashion. The structure not only stores data but also supports operations for accessing and manipulating the data.

In object-oriented thinking, a data structure, also known as a container or container object, is an object that stores other objects, referred to as data or elements. To define a data structure is essentially to define a class. The class for a data structure should use data fields to store data and provide methods to support such operations as search, insertion, and deletion. To create a data structure is therefore to create an instance from the class. You can then apply the methods on the instance to manipulate the data structure, such as inserting an element into or deleting an element from the data structure.

Section 11.11 introduced the ArrayList class, which is a data structure to store elements in a list. Java provides several more data structures that can be used to organize and manipulate data efficiently. These are commonly known as Java Collections Framework. We will introduce the applications of lists, vectors, stacks, queues, and priority queues in this chapter and sets and maps in the next chapter. The implementation of these data structures will be discussed in Chapters 24–27.

20.2 Collections

The Collection interface defines the common operations for lists, vectors, stacks, queues, priority queues, and sets.

The Java Collections Framework supports two types of containers:

- One for storing a collection of elements is simply called a collection.
- The other, for storing key/value pairs, is called a map.

Maps are efficient data structures for quickly searching an element using a key. We will introduce maps in the next chapter. Now we turn our attention to the following collections.

- Sets store a group of nonduplicate elements.
- Lists store an ordered collection of elements.
- Stacks store objects that are processed in a last-in, first-out fashion.
- Queues store objects that are processed in a first-in, first-out fashion.
- PriorityQueues store objects that are processed in the order of their priorities.

The common features of these collections are defined in the interfaces, and implementations are provided in concrete classes, as shown in Figure 20.1.

Note
All the interfaces and classes defined in the Java Collections Framework are grouped in the java.util package.

Design Guide
The design of the Java Collections Framework is an excellent example of using interfaces, abstract classes, and concrete classes. The interfaces define the framework. The abstract classes provide partial implementation. The concrete classes implement the interfaces with concrete data structures. Providing an abstract class that partially implements an interface makes it convenient for the user to write the code. The user can simply define
20.2 Collections

A concrete class that extends the abstract class rather implements all the methods in the interface. The abstract classes such as `AbstractCollection` are provided for convenience. For this reason, they are called `convenience abstract classes`.

The `Collection` interface is the root interface for manipulating a collection of objects. Its public methods are listed in Figure 20.2. The `AbstractCollection` class provides partial implementation for the `Collection` interface. It implements all the methods in `Collection` except the `add`, `size`, and `iterator` methods. These are implemented in appropriate concrete subclasses.

The `Collection` interface provides the basic operations for adding and removing elements in a collection. The `add` method adds an element to the collection. The `addAll` method adds all the elements in the specified collection to this collection. The `remove` method removes an element from the collection. The `removeAll` method removes the elements from this collection that are present in the specified collection. The `retainAll` method retains the elements in this collection that are also present in the specified collection. All these methods return `boolean`. The return value is `true` if the collection is changed as a result of the method execution. The `clear()` method simply removes all the elements from the collection.

**Note**

The methods `addAll`, `removeAll`, and `retainAll` are similar to the set union, difference, and intersection operations.

The `Collection` interface provides various query operations. The `size` method returns the number of elements in the collection. The `contains` method checks whether the collection contains the specified element. The `containsAll` method checks whether the collection contains all the elements in the specified collection. The `isEmpty` method returns `true` if the collection is empty.

The `Collection` interface provides the `toArray()` method, which returns an array representation for the collection.

**Design Guide**

Some of the methods in the `Collection` interface cannot be implemented in the concrete subclass. In this case, the method would throw `java.lang`
Chapter 20  Lists, Stacks, Queues, and Priority Queues

UnsupportedOperationException, a subclass of RuntimeException. This is a good design that you can use in your project. If a method has no meaning in the subclass, you can implement it as follows:

```java
public void someMethod() {
    throw new UnsupportedOperationException("Method not supported");
}
```

Listing 20.1 gives an example to use the methods defined in the Collection interface.

**LISTING 20.1  TestCollection.java**

```java
import java.util.*;

public class TestCollection {
    public static void main(String[] args) {
        ArrayList<String> collection1 = new ArrayList<>();
        collection1.add("New York");
        collection1.add("Atlanta");
        collection1.add("Dallas");
        collection1.add("Madison");
    }
}
```

Figure 20.2 The Collection interface contains the methods for manipulating the elements in a collection, and you can obtain an iterator object for traversing elements in the collection.

Figure 20.2 The Collection interface contains the methods for manipulating the elements in a collection, and you can obtain an iterator object for traversing elements in the collection.

Unsupported operations

```
+add(o: E): boolean
+addAll(c: Collection<? extends E>): boolean
+contains(o: Object): boolean
+containsAll(c: Collection<?>): boolean
+equals(o: Object): boolean
+hashCode(): int
+isEmpty(): boolean
+remove(o: Object): boolean
+removeAll(c: Collection<?>): boolean
+retainAll(c: Collection<?>): boolean
+size(): int
+toArray(): Object[]
```

Returns an iterator for the elements in this collection.

```
+iterator(): Iterator<E>
```

Adds a new element \( o \) to this collection.

```
+addAll(c: Collection<? extends E>): boolean
```

Adds all the elements in the collection \( c \) to this collection.

```
+clear(): void
```

Removes all the elements from this collection.

```
+contains(o: Object): boolean
```

Returns true if this collection contains the element \( o \).

```
+containsAll(c: Collection<?>): boolean
```

Returns true if this collection contains all the elements in \( c \).

```
+equals(o: Object): boolean
```

Returns true if this collection is equal to another collection \( o \).

```
+hashCode(): int
```

Returns the hash code for this collection.

```
+isEmpty(): boolean
```

Returns true if this collection contains no elements.

```
+remove(o: Object): boolean
```

Removes the element \( o \) from this collection.

```
+removeAll(c: Collection<?>): boolean
```

Removes all the elements in \( c \) from this collection.

```
+retainAll(c: Collection<?>): boolean
```

Retains the elements that are both in \( c \) and in this collection.

```
+size(): int
```

Returns the number of elements in this collection.

```
+toArray(): Object[]
```

Returns an array of Object for the elements in this collection.

```
+hasNext(): boolean
```

Returns true if this iterator has more elements to traverse.

```
+next(): E
```

Returns the next element from this iterator.

```
+remove(): void
```

Removes the last element obtained using the next method.
The program creates a concrete collection object using ArrayList (line 5), and invokes the Collection interface’s contains method (line 15), remove method (line 17), size method (line 18), addAll method (line 31), retainAll method (line 36), and removeAll method (line 41).

For this example, we use ArrayList. You can use any concrete class of Collection such as HashSet, LinkedList, Vector, and Stack to replace ArrayList to test these methods defined in the Collection interface.
The program creates a copy of an array list (lines 30, 35, 40). The purpose of this is to keep the original array list intact and use its copy to perform `addAll`, `retainAll`, and `removeAll` operations.

**Note**
All the concrete classes in the Java Collections Framework implement the `java.lang.Cloneable` and `java.io.Serializable` interfaces except that `java.util.PriorityQueue` does not implement the `Cloneable` interface. Thus, all instances of `Cloneable` except priority queues can be cloned and all instances of `Cloneable` can be serialized.

20.1 What is a data structure?
20.2 Describe the Java Collections Framework. List the interfaces, convenience abstract classes, and concrete classes under the `Collection` interface.
20.3 Can a collection object be cloned and serialized?
20.4 What method do you use to add all the elements from one collection to another collection?
20.5 When should a method throw an `UnsupportedOperationException`?

### 20.3 Iterators

*Each collection is Iterable. You can obtain its Iterator object to traverse all the elements in the collection.*

**Iterator** is a classic design pattern for walking through a data structure without having to expose the details of how data is stored in the data structure.

The `Collection` interface extends the `Iterable` interface. The `Iterable` interface defines the `iterator` method, which returns an iterator. The `Iterator` interface provides a uniform way for traversing elements in various types of collections. The `iterator()` method in the `Iterable` interface returns an instance of `Iterator`, as shown in Figure 20.2, which provides sequential access to the elements in the collection using the `next()` method. You can also use the `hasNext()` method to check whether there are more elements in the iterator, and the `remove()` method to remove the last element returned by the iterator.

Listing 20.2 gives an example that uses the iterator to traverse all the elements in an array list.

**Listing 20.2** TestIterator.java

```java
import java.util.*;

public class TestIterator {
    public static void main(String[] args) {
        Collection<String> collection = new ArrayList<>();
        collection.add("New York");
        collection.add("Atlanta");
        collection.add("Dallas");
        collection.add("Madison");

        Iterator<String> iterator = collection.iterator();
        while (iterator.hasNext()) {
            System.out.print(iterator.next().toUpperCase() + " ");
        }
        System.out.println();
    }
}
```
The program creates a concrete collection object using `ArrayList` (line 5) and adds four strings into the list (lines 6–9). The program then obtains an iterator for the collection (line 11) and uses the iterator to traverse all the strings in the list and displays the strings in uppercase (lines 12–14).

**Tip**
You can simplify the code in lines 11–14 using a foreach loop without using an iterator, as follows:

```java
for (String element: collection)
    System.out.print(element.toUpperCase() + " ");
```

This loop is read as “for each element in the collection, do the following.” The foreach loop can be used for arrays (see Section 7.2.7) as well as any instance of `Iterable`.

### 20.6 How do you obtain an iterator from a collection object?

### 20.7 What method do you use to obtain an element in the collection from an iterator?

### 20.8 Can you use a foreach loop to traverse the elements in any instance of `Collection`?

### 20.9 When using a foreach loop to traverse all elements in a collection, do you need to use the `next()` or `hasNext()` methods in an iterator?

---

**20.4 Lists**

The `List` interface extends the `Collection` interface and defines a collection for storing elements in a sequential order. To create a list, use one of its two concrete classes: `ArrayList` or `LinkedList`.

We used `ArrayList` to test the methods in the `Collection` interface in the preceding sections. Now we will examine `ArrayList` in more depth. We will also introduce another useful list, `LinkedList`, in this section.

**20.4.1 The Common Methods in the `List` Interface**

`ArrayList` and `LinkedList` are defined under the `List` interface. The `List` interface extends `Collection` to define an ordered collection with duplicates allowed. The `List` interface adds position-oriented operations, as well as a new list iterator that enables the user to traverse the list bidirectionally. The methods introduced in the `List` interface are shown in Figure 20.3.

The `add(index, element)` method is used to insert an element at a specified index, and the `addAll(index, collection)` method to insert a collection of elements at a specified index. The `remove(index)` method is used to remove an element at the specified index from the list. A new element can be set at the specified index using the `set(index, element)` method.

The `indexOf(element)` method is used to obtain the index of the specified element’s first occurrence in the list, and the `lastIndexOf(element)` method to obtain the index of its last occurrence. A sublist can be obtained by using the `subList(fromIndex, toIndex)` method.
The `listIterator()` or `listIterator(startIndex)` method returns an instance of `ListIterator`. The `ListIterator` interface extends the `Iterator` interface to add bidirectional traversal of the list. The methods in `ListIterator` are listed in Figure 20.4.

**Figure 20.3** The `List` interface stores elements in sequence and permits duplicates.

```java
+add(index: int, element: Object): boolean
+addAll(index: int, c: Collection<? extends E>): boolean
+get(index: int): E
+indexOf(element: Object): int
+lastIndexOf(element: Object): int
+listIterator(): ListIterator<E>
+listIterator(startIndex: int): ListIterator<E>
+remove(index: int): E
+set(index: int, element: Object): Object
+subList(fromIndex: int, toIndex: int): List<E>
```

**Figure 20.4** `ListIterator` enables traversal of a list bidirectionally.

The `add(element)` method inserts the specified element into the list. The element is inserted immediately before the next element that would be returned by the `next()` method defined in the `Iterator` interface, if any, and after the element that would be returned by the `previous()` method, if any. If the list doesn’t contain any elements, the new element becomes the sole element in the list. The `set(element)` method can be used to replace the last element returned by the `next` method or the `previous` method with the specified element.

The `hasNext()` method defined in the `Iterator` interface is used to check whether the iterator has more elements when traversed in the forward direction, and the `hasPrevious()`
method to check whether the iterator has more elements when traversed in the backward direction.

The `next()` method defined in the `Iterator` interface returns the next element in the iterator, and the `previous()` method returns the previous element in the iterator. The `nextIndex()` method returns the index of the next element in the iterator, and the `previousIndex()` returns the index of the previous element in the iterator.

The `AbstractList` class provides a partial implementation for the `List` interface. The `AbstractSequentialList` class extends `AbstractList` to provide support for linked lists.

### 20.4.2 The ArrayList and LinkedList Classes

The `ArrayList` class and the `LinkedList` class are two concrete implementations of the `List` interface. `ArrayList` stores elements in an array. The array is dynamically created. If the capacity of the array is exceeded, a larger new array is created and all the elements from the current array are copied to the new array. `LinkedList` stores elements in a linked list. Which of the two classes you use depends on your specific needs. If you need to support random access through an index without inserting or removing elements at the beginning of the list, `ArrayList` offers the most efficient collection. If, however, your application requires the insertion or deletion of elements at the beginning of the list, you should choose `LinkedList`. A list can grow or shrink dynamically. Once it is created, an array is fixed. If your application does not require the insertion or deletion of elements, an array is the most efficient data structure.

`ArrayList` is a resizable-array implementation of the `List` interface. It also provides methods for manipulating the size of the array used internally to store the list, as shown in Figure 20.5. Each `ArrayList` instance has a capacity, which is the size of the array used to store the elements in the list. It is always at least as large as the list size. As elements are added to an `ArrayList`, its capacity grows automatically. An `ArrayList` does not automatically shrink. You can use the `trimToSize()` method to reduce the array capacity to the size of the list. An `ArrayList` can be constructed using its no-arg constructor, `ArrayList(Collection)`, or `ArrayList(initialCapacity)`.

![java.util.ArrayList<E>](image)

- `java.util.ArrayList<E>`
- `java.util.AbstractList<E>`
- `+ArrayList()`  
- `+ArrayList(c: Collection<? extends E>)`  
- `+ArrayList(initialCapacity: int)`  
- `+trimToSize(): void`

**Figure 20.5** `ArrayList` implements `List` using an array.

`LinkedList` is a linked list implementation of the `List` interface. In addition to implementing the `List` interface, this class provides the methods for retrieving, inserting, and removing elements from both ends of the list, as shown in Figure 20.6. A `LinkedList` can be constructed using its no-arg constructor or `LinkedList(Collection)`. 

![java.util.LinkedList](image)
Chapter 20  Lists, Stacks, Queues, and Priority Queues

Listing 20.3 gives a program that creates an array list filled with numbers and inserts new elements into specified locations in the list. The example also creates a linked list from the array list and inserts and removes elements from the list. Finally, the example traverses the list forward and backward.

**LISTING 20.3  TestArrayAndLinkedList.java**

```java
import java.util.*;

public class TestArrayAndLinkedList {
    public static void main(String[] args) {
        List<Integer> arrayList = new ArrayList<>();
        arrayList.add(1); // 1 is autoboxed to new Integer(1)
        arrayList.add(2);
        arrayList.add(3);
        arrayList.add(1);
        arrayList.add(4);
        arrayList.add(0, 10);
        arrayList.add(3, 30);

        System.out.println("A list of integers in the array list:");
        System.out.println(arrayList);

        LinkedList<Object> linkedList = new LinkedList<>(arrayList);
        linkedList.add(1, "red");
        linkedList.removeLast();
        linkedList.addFirst("green");

        System.out.println("Display the linked list forward:");
        ListIterator<Object> listIterator = linkedList.listIterator();
        while (listIterator.hasNext()) {
            System.out.print(listIterator.next() + " ");
        }
        System.out.println();

        System.out.println("Display the linked list backward:");
        listIterator = linkedList.listIterator(linkedList.size());
        while (listIterator.hasPrevious()) {
            System.out.print(listIterator.previous() + " ");
        }
    }
}
```

**Figure 20.6**  *LinkedList* provides methods for adding and inserting elements at both ends of the list.
A list can hold identical elements. Integer 1 is stored twice in the list (lines 6, 9). ArrayList and LinkedList operate similarly. The critical difference between them pertains to internal implementation, which affects their performance. ArrayList is efficient for retrieving elements and LinkedList is efficient for inserting and removing elements at the beginning of the list. Both have the same performance for inserting and removing elements in the middle or at the end of the list.

The get(i) method is available for a linked list, but it is a time-consuming operation. Do not use it to traverse all the elements in a list as shown in (a). Instead you should use an iterator as shown in (b). Note that a foreach loop uses an iterator implicitly. You will know the reason when you learn how to implement a linked list in Chapter 24.

A list of integers in the array list:
[10, 1, 2, 30, 3, 1, 4]
Display the linked list forward:
green 10 red 1 2 30 3 1
display the linked list backward:
1 3 30 2 1 red 10 green

Tip
Java provides the static asList method for creating a list from a variable-length list of arguments. Thus you can use the following code to create a list of strings and a list of integers:

```java
List<String> list1 = Arrays.asList("red", "green", "blue");
List<Integer> list2 = Arrays.asList(10, 20, 30, 40, 50);
```

20.10 How do you add and remove elements from a list? How do you traverse a list in both directions?
20.11 Suppose that list1 is a list that contains the strings red, yellow, and green, and that list2 is another list that contains the strings red, yellow, and blue. Answer the following questions:
a. What are list1 and list2 after executing list1.addAll(list2)?
b. What are list1 and list2 after executing list1.add(list2)?
c. What are list1 and list2 after executing list1.removeAll(list2)?
d. What are list1 and list2 after executing list1.remove(list2)?
e. What are list1 and list2 after executing list1.retainAll(list2)?
f. What is list1 after executing list1.clear()?
20.12 What are the differences between ArrayList and LinkedList? Which list should you use to insert and delete elements at the beginning of a list?
20.13 Are all the methods in ArrayList also in LinkedList? What methods are in LinkedList but not in ArrayList?
20.14 How do you create a list from an array of objects?
20.5 The Comparator Interface

Comparator can be used to compare the objects of a class that doesn’t implement Comparable.

You have learned how to compare elements using the Comparable interface (introduced in Section 13.6). Several classes in the Java API, such as String, Date, Calendar, BigInteger, BigDecimal, and all the numeric wrapper classes for the primitive types, implement the Comparable interface. The Comparable interface defines the compareTo method, which is used to compare two elements of the same class that implement the Comparable interface.

What if the elements’ classes do not implement the Comparable interface? Can these elements be compared? You can define a comparator to compare the elements of different classes. To do so, define a class that implements the java.util.Comparator<T> interface and overrides its compare method.

    public int compare(T element1, T element2)
    Returns a negative value if element1 is less than element2, a positive value if element1 is greater than element2, and zero if they are equal.

The GeometricObject class was introduced in Section 13.2, Abstract Classes. The GeometricObject class does not implement the Comparable interface. To compare the objects of the GeometricObject class, you can define a comparator class, as shown in Listing 20.4.

Listing 20.4 GeometricObjectComparator.java

```java
import java.util.Comparator;

public class GeometricObjectComparator implements Comparator<GeometricObject>, java.io.Serializable {
    public int compare(GeometricObject o1, GeometricObject o2) {
        double area1 = o1.getArea();
        double area2 = o2.getArea();
        if (area1 < area2)
            return -1;
        else if (area1 == area2)
            return 0;
        else
            return 1;
    }
}
```

Line 4 implements Comparator<GeometricObject>. Line 5 overrides the compare method to compare two geometric objects. The class also implements Serializable. It is generally a good idea for comparators to implement Serializable, as they may be used as ordering methods in serializable data structures. In order for the data structure to serialize successfully, the comparator (if provided) must implement Serializable.

Listing 20.5 gives a method that returns a larger object between two geometric objects. The objects are compared using the GeometricObjectComparator.

Listing 20.5 TestComparator.java

```java
import java.util.Comparator;

public class TestComparator {
    public static void main(String[] args) {
```
The program creates a Rectangle and a Circle object in lines 5–6 (the Rectangle and Circle classes were defined in Section 13.2, Abstract Classes). They are all subclasses of GeometricObject. The program invokes the max method to obtain the geometric object with the larger area (lines 8–9).

The GeometricObjectComparator is created and passed to the max method (line 9) and this comparator is used in the max method to compare the geometric objects in line 17.

### 20.15 What are the differences between the Comparable interface and the Comparator interface? In which package is Comparable, and in which package is Comparator?

### 20.16 How do you define a class A that implements the Comparable interface? Are two instances of class A comparable? How do you define a class B that implements the Comparator interface and override the compare method to compare to objects of type B1? How do you invoke the sort method to sort a list of objects of the type B1?

### 20.6 Static Methods for Lists and Collections

*The Collections class contains static methods to perform common operations in a collection and a list.*

Section 11.12 introduced several static methods in the Collections class for array lists. The Collections class contains the sort, binarySearch, reverse, shuffle, copy, and fill methods for lists, and max, min, disjoint, and frequency methods for collections, as shown in Figure 20.7.
### java.util.Collections

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>sort(list: List): void</code></td>
<td>Sorts the specified list.</td>
</tr>
<tr>
<td><code>sort(list: List, c: Comparator): void</code></td>
<td>Sorts the specified list with the comparator.</td>
</tr>
<tr>
<td><code>binarySearch(list: List, key: Object): int</code></td>
<td>Searches the key in the sorted list using binary search.</td>
</tr>
<tr>
<td><code>binarySearch(list: List, key: Object, c: Comparator): int</code></td>
<td>Searches the key in the sorted list using binary search with the comparator.</td>
</tr>
<tr>
<td><code>reverse(list: List): void</code></td>
<td>Reverses the specified list.</td>
</tr>
<tr>
<td><code>reverseOrder(): Comparator</code></td>
<td>Returns a comparator with the reverse ordering.</td>
</tr>
<tr>
<td><code>shuffle(list: List): void</code></td>
<td>Shuffles the specified list randomly.</td>
</tr>
<tr>
<td><code>shuffle(list: List, rmd: Random): void</code></td>
<td>Shuffles the specified list with a random object.</td>
</tr>
<tr>
<td><code>copy(des: List, src: List): void</code></td>
<td>Copies from the source list to the destination list.</td>
</tr>
<tr>
<td><code>nCopies(n: int, o: Object): List</code></td>
<td>Returns a list consisting of ( n ) copies of the object.</td>
</tr>
<tr>
<td><code>fill(list: List, o: Object): void</code></td>
<td>Fills the list with the object.</td>
</tr>
<tr>
<td><code>max(c: Collection): Object</code></td>
<td>Returns the ( \text{max} ) object in the collection.</td>
</tr>
<tr>
<td><code>max(c: Collection, c: Comparator): Object</code></td>
<td>Returns the ( \text{max} ) object using the comparator.</td>
</tr>
<tr>
<td><code>min(c: Collection): Object</code></td>
<td>Returns the ( \text{min} ) object in the collection.</td>
</tr>
<tr>
<td><code>min(c: Collection, c: Comparator): Object</code></td>
<td>Returns the ( \text{min} ) object using the comparator.</td>
</tr>
<tr>
<td><code>disjoint(c1: Collection, c2: Collection): boolean</code></td>
<td>Returns true if ( c1 ) and ( c2 ) have no elements in common.</td>
</tr>
<tr>
<td><code>frequency(c: Collection, o: Object): int</code></td>
<td>Returns the number of occurrences of the specified element in the collection.</td>
</tr>
</tbody>
</table>

#### Figure 20.7

The **Collections** class contains static methods for manipulating lists and collections.

You can sort the comparable elements in a list in its natural order with the `compareTo` method in the `Comparable` interface. You may also specify a comparator to sort elements. For example, the following code sorts strings in a list.

```java
List<String> list = Arrays.asList("red", "green", "blue");
Collections.sort(list);
System.out.println(list);
```

The output is `[blue, green, red]`.

The preceding code sorts a list in ascending order. To sort it in descending order, you can simply use the `Collections.reverseOrder()` method to return a `Comparator` object that orders the elements in reverse of their natural order. For example, the following code sorts a list of strings in descending order.

```java
List<String> list = Arrays.asList("yellow", "red", "green", "blue");
Collections.sort(list, Collections.reverseOrder());
System.out.println(list);
```

The output is `[yellow, red, green, blue]`.

You can use the `binarySearch` method to search for a key in a list. To use this method, the list must be sorted in increasing order. If the key is not in the list, the method returns \(-1\) (\(\text{insertion point} + 1\)). Recall that the insertion point is where the item would fall in the list if it were present. For example, the following code searches the keys in a list of integers and a list of strings.

```java
List<Integer> list1 = Arrays.asList(2, 4, 7, 10, 11, 45, 50, 59, 60, 66);
System.out.println("(1) Index: "+ Collections.binarySearch(list1, 7));
```
System.out.println("(2) Index: " + Collections.binarySearch(list1, 9));

List<String> list2 = Arrays.asList("blue", "green", "red");
System.out.println("(3) Index: " +
    Collections.binarySearch(list2, "red");
System.out.println("(4) Index: " +
    Collections.binarySearch(list2, "cyan");

The output of the preceding code is:

(1) Index: 2
(2) Index: -4
(3) Index: 2
(4) Index: -2

You can use the `reverse` method to reverse the elements in a list. For example, the following code displays `[blue, green, red, yellow].`

List<String> list = Arrays.asList("yellow", "red", "green", "blue");
Collections.reverse(list);
System.out.println(list);

You can use the `shuffle(List)` method to randomly reorder the elements in a list. For example, the following code shuffles the elements in `list`.

List<String> list = Arrays.asList("yellow", "red", "green", "blue");
Collections.shuffle(list);
System.out.println(list);

You can also use the `shuffle(List, Random)` method to randomly reorder the elements in a list with a specified `Random` object. Using a specified `Random` object is useful to generate a list with identical sequences of elements for the same original list. For example, the following code shuffles the elements in `list`.

List<String> list1 = Arrays.asList("yellow", "red", "green", "blue");
List<String> list2 = Arrays.asList("yellow", "red", "green", "blue");
Collections.shuffle(list1, new Random(20));
Collections.shuffle(list2, new Random(20));
System.out.println(list1);
System.out.println(list2);

You will see that `list1` and `list2` have the same sequence of elements before and after the shuffling.

You can use the `copy(dest, src)` method to copy all the elements from a source list to a `copy` destination list on the same index. The destination list must be as long as the source list. If it is longer, the remaining elements in the source list are not affected. For example, the following code copies `list2` to `list1`.

List<String> list1 = Arrays.asList("yellow", "red", "green", "blue");
List<String> list2 = Arrays.asList("white", "black");
Collections.copy(list1, list2);
System.out.println(list1);
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The output for list1 is [white, black, green, blue]. The copy method performs a shallow copy: only the references of the elements from the source list are copied.

You can use the nCopies(int n, Object o) method to create an immutable list that consists of n copies of the specified object. For example, the following code creates a list with five Calendar objects.

```
List<GregorianCalendar> list1 = Collections.nCopies(5, new GregorianCalendar(2005, 0, 1));
```

The list created from the nCopies method is immutable, so you cannot add, remove, or update elements in the list. All the elements have the same references.

You can use the fill(List list, Object o) method to replace all the elements in the list with the specified element. For example, the following code displays [black, black, black].

```
List<String> list = Arrays.asList("red", "green", "blue");
Collections.fill(list, "black");
System.out.println(list);
```

You can use the max and min methods for finding the maximum and minimum elements in a collection. The elements must be comparable using the Comparable interface or the Comparator interface. For example, the following code displays the largest and smallest strings in a collection.

```
Collection<String> collection = Arrays.asList("red", "green", "blue");
System.out.println(Collections.max(collection));
System.out.println(Collections.min(collection));
```

The disjoint(collection1, collection2) method returns true if the two collections have no elements in common. For example, in the following code, disjoint(collection1, collection2) returns false, but disjoint(collection1, collection3) returns true.

```
Collection<String> collection1 = Arrays.asList("red", "cyan");
Collection<String> collection2 = Arrays.asList("red", "blue");
Collection<String> collection3 = Arrays.asList("pink", "tan");
System.out.println(Collections.disjoint(collection1, collection2));
System.out.println(Collections.disjoint(collection1, collection3));
```

The frequency(collection, element) method finds the number of occurrences of the element in the collection. For example, frequency(collection, "red") returns 2 in the following code.

```
Collection<String> collection = Arrays.asList("red", "cyan", "red");
System.out.println(Collections.frequency(collection, "red"));
```

20.17 Are all the methods in the Collections class static?

20.18 Which of the following static methods in the Collections class are for lists, and which are for collections?

   sort, binarySearch, reverse, shuffle, max, min, disjoint, frequency

20.19 Show the output of the following code:

   ```java
   import java.util.*;
   
   public class Test {
       public static void main(String[] args) {
   ```
List<String> list =
    Arrays.asList("yellow", "red", "green", "blue");
Collections.reverse(list);
System.out.println(list);

List<String> list1 =
    Arrays.asList("yellow", "red", "green", "blue");
List<String> list2 = Arrays.asList("white", "black");
Collections.copy(list1, list2);
System.out.println(list1);

Collection<String> c1 = Arrays.asList("red", "cyan");
Collection<String> c2 = Arrays.asList("red", "blue");
Collection<String> c3 = Arrays.asList("pink", "tan");
System.out.println(Collections.disjoint(c1, c2));
System.out.println(Collections.disjoint(c1, c3));

Collection<String> collection =
    Arrays.asList("red", "cyan", "red");
System.out.println(Collections.frequency(collection, "red");

20.20 Which method can you use to sort the elements in an ArrayList or a LinkedList?
Which method can you use to sort an array of strings?

20.21 Which method can you use to perform binary search for elements in an ArrayList or a LinkedList? Which method can you use to perform binary search for an array of strings?

20.22 Write a statement to find the largest element in an array of comparable objects.

20.7 Case Study: Bouncing Balls

This section presents a program that displays bouncing balls and enables the user to add and remove balls.

Section 15.12 presents a program that displays one bouncing ball. This section presents a program that displays multiple bouncing balls. You can use two buttons to suspend and resume the movement of the balls, a scroll bar to control the ball speed, and the + or – button add or remove a ball, as shown in Figure 20.8.

![Figure 20.8](image)

Pressing the + or – button adds or removes a ball.

The example in Section 15.12 only had to store one ball. How do you store the multiple balls in this example? The Pane’s `getChildren()` method returns an `ObservableList<Node>`, a subtype of `List<Node>`, for storing the nodes in the pane. Initially, the list is empty. When a new ball is created, add it to the end of the list. To remove a ball, simply remove the last one in the list.
Each ball has its state: the \( x \)-, \( y \)-coordinates, color, and direction to move. You can define a class named \texttt{Ball} that extends \texttt{javafx.scene.shape.Circle}. The \( x \)-, \( y \)-coordinates and the color are already defined in \texttt{Circle}. When a ball is created, it starts from the upper-left corner and moves downward to the right. A random color is assigned to a new ball.

The \texttt{MultipleBallPane} class is responsible for displaying the ball and the \texttt{MultipleBounceBall} class places the control components and implements the control. The relationship of these classes is shown in Figure 20.9. Listing 20.6 gives the program.

![Class Diagram](image)

**Figure 20.9** MultipleBounceBall contains MultipleBallPane, and MultipleBallPane contains Ball.

**Listing 20.6** MultipleBounceBall.java

```java
import javafx.animation.KeyFrame;
import javafx.animation.Timeline;
import javafx.application.Application;
import javafx.beans.property.DoubleProperty;
import javafx.geometry.Pos;
import javafx.scene.Node;
import javafx.stage.Stage;
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.scene.control.ScrollBar;
import javafx.scene.layout.BorderPane;
import javafx.scene.layout.HBox;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Circle;
import javafx.util.Duration;

public class MultipleBounceBall extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        MultipleBallPane ballPane = new MultipleBallPane();
        ballPane.setStyle("-fx-border-color: yellow");
        Button btAdd = new Button("+");
    }
}
```
Button btSubtract = new Button("-");
HBox hBox = new HBox(10);
hBox.getChildren().addAll(btAdd, btSubtract);  // add buttons to HBox
hBox.setAlignment(Pos.CENTER);

// Add or remove a ball
btAdd.setOnAction(e -> ballPane.add());
btSubtract.setOnAction(e -> ballPane.subtract());  // remove a ball

// Pause and resume animation
ballPane.setOnMousePressed(e -> ballPane.pause());
ballPane.setOnMouseReleased(e -> ballPane.play());  // resume animation

// Use a scroll bar to control animation speed
ScrollBar sbSpeed = new ScrollBar();  // create a scroll bar
sbSpeed.setMax(20);
sbSpeed.setValue(10);
bballPane.rateProperty().bind(sbSpeed.valueProperty());  // bind animation rate

BorderPane pane = new BorderPane();
pane.setCenter(ballPane);
pane.setTop(sbSpeed);
pane.setBottom(hBox);

// Create a scene and place the pane in the stage
Scene scene = new Scene(pane, 250, 150);
primaryStage.setTitle("MultipleBounceBall");  // Set the stage title
primaryStage.setScene(scene);  // Place the scene in the stage
primaryStage.show();  // Display the stage

private class MultipleBallPane extends Pane {
    
    public MultipleBallPane() {
        // Create an animation for moving the ball
        animation = new Timeline(
                new KeyFrame(Duration.millis(50), e -> moveBall()));
        animation.setCycleCount(Timeline.INDEFINITE);
        animation.play();  // Start animation
    }

    public void add() {
        Color color = new Color(Math.random(),
                Math.random(), Math.random(), 0.5);
        getChildren().add(new Ball(30, 30, 20, color));  // add a ball to pane
    }

    public void subtract() {
        if (getChildren().size() > 0) {
            getChildren().remove(getChildren().size() - 1);  // remove a ball
        }
    }

    public void play() {
        animation.play();
    }

    public void pause() {
        
    }
}
public void increaseSpeed() {
    animation.setRate(animation.getRate() + 0.1);
}

public void decreaseSpeed() {
    animation.setRate(
        animation.getRate() > 0 ? animation.getRate() - 0.1 : 0);
}

public DoubleProperty rateProperty() {
    return animation.rateProperty();
}

protected void moveBall() {
    for (Node node: this.getChildren()) {
        Ball ball = (Ball)node;
        // Check boundaries
        if (ball.getCenterX() < ball.getRadius() ||
            ball.getCenterX() > getWidth() - ball.getRadius()) {
            ball.dx *= -1; // Change ball move direction
        }
        if (ball.getCenterY() < ball.getRadius() ||
            ball.getCenterY() > getHeight() - ball.getRadius()) {
            ball.dy *= -1; // Change ball move direction
        }
        // Adjust ball position
        ball.setCenterX(ball.dx + ball.getCenterX());
        ball.setCenterY(ball.dy + ball.getCenterY());
    }
}

class Ball extends Circle {
    private double dx = 1, dy = 1;

class Ball extends Circle {
    private double dx = 1, dy = 1;

    Ball(double x, double y, double radius, Color color) {
        super(x, y, radius);
        setFill(color); // Set ball color
    }
}

The add() method creates a new ball with a random color and adds it to the pane (line 70). The pane stores all the balls in a list. The subtract() method removes the last ball in the list (line 75).

When the user clicks the + button, a new ball is added to the pane (line 31). When the user clicks the − button, the last ball in the array list is removed (line 32).

The moveBall() method in the MultipleBallPane class gets every ball in the pane’s list and adjusts the balls’ positions (lines 114–115).

What is the return value from invoking pane.getChildren() for a pane?
20.24 How do you modify the code in the MultipleBallApp program to remove the first ball in the list when the button is clicked?

20.25 How do you modify the code in the MultipleBallApp program so that each ball will get a random radius between 10 and 20?

20.8 Vector and Stack Classes

Vector is a subclass of AbstractList, and Stack is a subclass of Vector in the Java API.

The Java Collections Framework was introduced in Java 2. Several data structures were supported earlier, among them the Vector and Stack classes. These classes were redesigned to fit into the Java Collections Framework, but all their old-style methods are retained for compatibility.

Vector is the same as ArrayList, except that it contains synchronized methods for accessing and modifying the vector. Synchronized methods can prevent data corruption when a vector is accessed and modified by two or more threads concurrently. We will discuss synchronization in Chapter 30, Multithreading and Parallel Programming. For the many applications that do not require synchronization, using ArrayList is more efficient than using Vector.

The Vector class extends the AbstractList class. It also has the methods contained in the original Vector class defined prior to Java 2, as shown in Figure 20.10.

```
java.util.AbstractList<E>

java.util.Vector<E>

+Vector()
+Vector(c: Collection<? extends E>)
+Vector(initialCapacity: int)
+Vector(initCapacity: int, capacityIncr: int)
+addElement(o: E): void
+capacity(): int
+copyInto(anArray: Object[]): void
+elementAt(index: int): E
+elements(): Enumeration<E>
+ensureCapacity(): void
+firstElement(): E
+insertElementAt(o: E, index: int): void
+lastElement(): E
+removeAllElements(): void
+removeElement(o: Object): boolean
+removeElementAt(index: int): void
+setElementAt(o: E, index: int): void
+setSize(newSize: int): void
+trimToSize(): void
```

FIGURE 20.10 Starting in Java 2, the Vector class extends AbstractList and also retains all the methods in the original Vector class.
Most of the methods in the `Vector` class listed in the UML diagram in Figure 20.10 are similar to the methods in the `List` interface. These methods were introduced before the Java Collections Framework. For example, `addElement(Object element)` is the same as the `add(Object element)` method, except that the `addElement` method is synchronized. Use the `ArrayList` class if you don’t need synchronization. It works much faster than `Vector`.

**Note**
The `elements()` method returns an `Enumeration`. The `Enumeration` interface was introduced prior to Java 2 and was superseded by the `Iterator` interface.

**Note**
`Vector` is widely used in Java legacy code because it was the Java resizable array implementation before Java 2.

In the Java Collections Framework, `Stack` is implemented as an extension of `Vector`, as illustrated in Figure 20.11.

![Figure 20.11](image)

The `Stack` class extends `Vector` to provide a last-in, first-out data structure.

The `Stack` class was introduced prior to Java 2. The methods shown in Figure 20.11 were used before Java 2. The `empty()` method is the same as `isEmpty()`. The `peek()` method looks at the element at the top of the stack without removing it. The `pop()` method removes the top element from the stack and returns it. The `push(Object element)` method adds the specified element to the stack. The `search(Object element)` method checks whether the specified element is in the stack.

**Check Point**

20.26 How do you create an instance of `Vector`? How do you add or insert a new element into a vector? How do you remove an element from a vector? How do you find the size of a vector?

20.27 How do you create an instance of `Stack`? How do you add a new element to a stack? How do you remove an element from a stack? How do you find the size of a stack?

20.28 Does Listing 20.1, TestCollection.java, compile and run if all the occurrences of `ArrayList` are replaced by `LinkedList`, `Vector`, or `Stack`?
20.9 Queues and Priority Queues

In a priority queue, the element with the highest priority is removed first.

A queue is a first-in, first-out data structure. Elements are appended to the end of the queue and are removed from the beginning of the queue. In a priority queue, elements are assigned priorities. When accessing elements, the element with the highest priority is removed first. This section introduces queues and priority queues in the Java API.

20.9.1 The Queue Interface

The Queue interface extends java.util.Collection with additional insertion, extraction, and inspection operations, as shown in Figure 20.12.

Figures 20.12 and 20.13. The Queue interface extends Collection to provide additional insertion, extraction, and inspection operations.

The offer method is used to add an element to the queue. This method is similar to the add method in the Collection interface, but the offer method is preferred for queues. The poll and remove methods are similar, except that poll() returns null if the queue is empty, whereas remove() throws an exception. The peek and element methods are similar, except that peek() returns null if the queue is empty, whereas element() throws an exception.

20.9.2 Deque and LinkedList

The LinkedList class implements the Deque interface, which extends the Queue interface, as shown in Figure 20.13. Therefore, you can use LinkedList to create a queue. LinkedList is ideal for queue operations because it is efficient for inserting and removing elements from both ends of a list.

Deque supports element insertion and removal at both ends. The name deque is short for “double-ended queue” and is usually pronounced “deck.” The Deque interface extends Queue with additional methods for inserting and removing elements from both ends of the queue. The methods addFirst(e), removeFirst(), addLast(e), removeLast(), getFirst(), and getLast() are defined in the Deque interface.
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Listing 20.7 shows an example of using a queue to store strings. Line 4 creates a queue using LinkedList. Four strings are added to the queue in lines 5–8. The size() method defined in the Collection interface returns the number of elements in the queue (line 10). The remove() method retrieves and removes the element at the head of the queue (line 11).

LISTING 20.7  TestQueue.java

```java
public class TestQueue {
    public static void main(String[] args) {
        java.util.Queue<String> queue = new java.util.LinkedList<>();
        queue.offer("Oklahoma");
        queue.offer("Indiana");
        queue.offer("Georgia");
        queue.offer("Texas");

        while (queue.size() > 0)
            System.out.print(queue.remove() + " ");
    }
}
```

FIGURE 20.13  LinkedList implements List and Deque.

Listing 20.7 shows an example of using a queue to store strings. Line 4 creates a queue using LinkedList. Four strings are added to the queue in lines 5–8. The size() method defined in the Collection interface returns the number of elements in the queue (line 10). The remove() method retrieves and removes the element at the head of the queue (line 11).

LISTING 20.7  TestQueue.java

```java
public class TestQueue {
    public static void main(String[] args) {
        java.util.Queue<String> queue = new java.util.LinkedList<>();
        queue.offer("Oklahoma");
        queue.offer("Indiana");
        queue.offer("Georgia");
        queue.offer("Texas");

        while (queue.size() > 0)
            System.out.print(queue.remove() + " ");
    }
}
```

The PriorityQueue class implements a priority queue, as shown in Figure 20.14. By default, the priority queue orders its elements according to their natural ordering using Comparable. The element with the least value is assigned the highest priority and thus is removed from the queue first. If there are several elements with the same highest priority, the tie is broken arbitrarily. You can also specify an ordering using Comparator in the constructor PriorityQueue(initialCapacity, comparator).

Listing 20.8 shows an example of using a priority queue to store strings. Line 5 creates a priority queue for strings using its no-arg constructor. This priority queue orders the strings using their natural order, so the strings are removed from the queue in increasing order. Lines 16–17 create a priority queue using the comparator obtained from Collections.reverseOrder(), which orders the elements in reverse order, so the strings are removed from the queue in decreasing order.
20.9 Queues and Priority Queues

LISTING 20.8 PriorityQueueDemo.java

```java
import java.util.*;

public class PriorityQueueDemo {
    public static void main(String[] args) {
        PriorityQueue<String> queue1 = new PriorityQueue<>();
        queue1.offer("Oklahoma");
        queue1.offer("Indiana");
        queue1.offer("Georgia");
        queue1.offer("Texas");

        System.out.println("Priority queue using Comparable:");
        while (queue1.size() > 0) {
            System.out.print(queue1.remove() + " ");
        }

        PriorityQueue<String> queue2 = new PriorityQueue<>(
                Collections.reverseOrder());
        queue2.offer("Oklahoma");
        queue2.offer("Indiana");
        queue2.offer("Georgia");
        queue2.offer("Texas");

        System.out.println("\nPriority queue using Comparator:");
        while (queue2.size() > 0) {
            System.out.print(queue2.remove() + " ");
        }
    }
}
```

Priority queue using Comparable:
Georgia Indiana Oklahoma Texas
Priority queue using Comparator:
Texas Oklahoma Indiana Georgia

20.29 Is `java.util.Queue` a subinterface of `java.util.Collection`, `java.util.Set`, or `java.util.List`? Does `LinkedList` implement `Queue`?
How do you create a priority queue for integers? By default, how are elements ordered in a priority queue? Is the element with the least value assigned the highest priority in a priority queue?

How do you create a priority queue that reverses the natural order of the elements?

20.10 Case Study: Evaluating Expressions

Stacks can be used to evaluate expressions.

Stacks and queues have many applications. This section gives an application that uses stacks to evaluate expressions. You can enter an arithmetic expression from Google to evaluate the expression, as shown in Figure 20.15.

How does Google evaluate an expression? This section presents a program that evaluates a compound expression with multiple operators and parentheses (e.g., $(15 + 2) \times 34 - 2$). For simplicity, assume that the operands are integers and the operators are of four types: $+$, $-$, $\times$, and $/$.

The problem can be solved using two stacks, named operandStack and operatorStack, for storing operands and operators, respectively. Operands and operators are pushed into the stacks before they are processed. When an operator is processed, it is popped from operatorStack and applied to the first two operands from operandStack (the two operands are popped from operandStack). The resultant value is pushed back to operandStack.

The algorithm proceeds in two phases:

Phase 1: Scanning the expression

The program scans the expression from left to right to extract operands, operators, and the parentheses.

1.1. If the extracted item is an operand, push it to operandStack.

1.2. If the extracted item is a $+$ or $-$ operator, process all the operators at the top of operatorStack and push the extracted operator to operatorStack.

1.3. If the extracted item is a $\times$ or $/$ operator, process the $\times$ or $/$ operators at the top of operatorStack and push the extracted operator to operatorStack.
1.4. If the extracted item is a ( symbol, push it to operatorStack.

1.5. If the extracted item is a ) symbol, repeatedly process the operators from the top of operatorStack until seeing the ( symbol on the stack.

**Phase 2: Clearing the stack**

Repeatedly process the operators from the top of operatorStack until operatorStack is empty.

Table 20.1 shows how the algorithm is applied to evaluate the expression \((1 + 2) \times 4 - 3\).

<table>
<thead>
<tr>
<th>Expression</th>
<th>Scan</th>
<th>Action</th>
<th>operandStack</th>
<th>operatorStack</th>
</tr>
</thead>
<tbody>
<tr>
<td>((1 + 2)\times 4 - 3)</td>
<td>(</td>
<td>Phase 1.4</td>
<td>[]</td>
<td>[ )</td>
</tr>
<tr>
<td>(1 + 2) \times 4 - 3</td>
<td>1</td>
<td>Phase 1.1</td>
<td>1</td>
<td>(</td>
</tr>
<tr>
<td>((1 + 2)\times 4 - 3) +</td>
<td></td>
<td>Phase 1.2</td>
<td>1</td>
<td>+</td>
</tr>
<tr>
<td>((1 + 2)\times 4 - 3)</td>
<td>2</td>
<td>Phase 1.1</td>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>((1 + 2)\times 4 - 3) )</td>
<td></td>
<td>Phase 1.5</td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>((1 + 2)\times 4 - 3) *</td>
<td></td>
<td>Phase 1.3</td>
<td>3</td>
<td>*</td>
</tr>
<tr>
<td>((1 + 2)\times 4 - 3)</td>
<td>4</td>
<td>Phase 1.1</td>
<td>4</td>
<td>3</td>
</tr>
<tr>
<td>((1 + 2)\times 4 - 3) –</td>
<td></td>
<td>Phase 1.2</td>
<td>12</td>
<td>–</td>
</tr>
<tr>
<td>((1 + 2)\times 4 - 3)</td>
<td>3</td>
<td>Phase 1.1</td>
<td>3</td>
<td>12</td>
</tr>
<tr>
<td>((1 + 2)\times 4 - 3) none</td>
<td></td>
<td>Phase 2</td>
<td>9</td>
<td></td>
</tr>
</tbody>
</table>

Listing 20.9 gives the program, and Figure 20.16 shows some sample output.
```java
public class EvaluateExpression {
  public static void main(String[] args) {
    // Check number of arguments passed
    if (args.length != 1) {
      System.out.println("Usage: java EvaluateExpression \"expression\"");
      System.exit(1);
    }

    try {
      System.out.println(evaluateExpression(args[0]));
    }
    catch (Exception ex) {
      System.out.println("Wrong expression: " + args[0]);
    }
  }

  /** Evaluate an expression */
  public static int evaluateExpression(String expression) {
    // Create operandStack to store operands
    Stack<Integer> operandStack = new Stack<>();
    Stack<Character> operatorStack = new Stack<>();

    // Insert blanks around (, ), +, -, /, and *
    expression = insertBlanks(expression);

    // Extract operands and operators
    String[] tokens = expression.split(" ");

    // Phase 1: Scan tokens
    for (String token: tokens) {
      if (token.length() == 0) // Blank space
        continue; // Back to the while loop to extract the next token
      else if (token.charAt(0) == '+' || token.charAt(0) == '-') {
        // Process all +, -, *, / in the top of the operator stack
        while (!operatorStack.isEmpty() &&
          (operatorStack.peek() == '+' ||
           operatorStack.peek() == '-' ||
           operatorStack.peek() == '*' ||
           operatorStack.peek() == '/')) {
          processAnOperator(operandStack, operatorStack);
        }

        // Push the + or - operator into the operator stack
        operatorStack.push(token.charAt(0));
      }
      else if (token.charAt(0) == '*' || token.charAt(0) == '/') {
        // Process all *, / in the top of the operator stack
        while (!operatorStack.isEmpty() &&
          (operatorStack.peek() == '*' ||
           operatorStack.peek() == '/')) {
          processAnOperator(operandStack, operatorStack);
        }

        // Push the * or / operator into the operator stack
        operatorStack.push(token.charAt(0));
      }
    }
  }
}
```
20.10 Case Study: Evaluating Expressions

```java
// Push the * or / operator into the operator stack
operatorStack.push(token.charAt(0));
}
else if (token.trim().charAt(0) == '(') {
    operatorStack.push('('); // Push '(' to stack
}
else if (token.trim().charAt(0) == ')') {
    // Process all the operators in the stack until seeing '(
    while (operatorStack.peek() != '(') {
        processAnOperator(operandStack, operatorStack);
    }
    operatorStack.pop(); // Pop the '(' symbol from the stack
}
else { // An operand scanned
    // Push an operand to the stack
    operandStack.push(new Integer(token));
}

// Phase 2: Process all the remaining operators in the stack
while (!operatorStack.isEmpty()) {
    processAnOperator(operandStack, operatorStack);
}

// Return the result
return operandStack.pop();

/** Process one operator: Take an operator from operatorStack and
 * apply it on the operands in the operandStack */
public static void processAnOperator(
    Stack<Integer> operandStack, Stack<Character> operatorStack) {
    char op = operatorStack.pop();
    int op1 = operandStack.pop();
    int op2 = operandStack.pop();
    if (op == '+') {
        operandStack.push(op2 + op1);
    } else if (op == '-') {
        operandStack.push(op2 - op1);
    } else if (op == '*') {
        operandStack.push(op2 * op1);
    } else if (op == '/') {
        operandStack.push(op2 / op1);
    }
}

public static String insertBlanks(String s) {
    String result = "";
    for (int i = 0; i < s.length(); i++) {
        if (s.charAt(i) == '(' || s.charAt(i) == ')') {
            result += " " + s.charAt(i) + " ";
        } else {
            result += s.charAt(i);
        }
    }
    return result;
}
```
You can use the `GenericStack` class provided by the book or the `java.util.Stack` class defined in the Java API for creating stacks. This example uses the `java.util.Stack` class. The program will work if it is replaced by `GenericStack`.

The program takes an expression as a command-line argument in one string.

The `evaluateExpression` method creates two stacks, `operandStack` and `operatorStack` (lines 23, 26), and extracts operands, operators, and parentheses delimited by space (lines 29–32). The `insertBlanks` method is used to ensure that operands, operators, and parentheses are separated by at least one blank (line 29).

The program scans each token in the `for` loop (lines 35–77). If a token is empty, skip it (line 37). If a token is an operand, push it to `operandStack` (line 75). If a token is a `+` or `–` operator (line 38), process all the operators from the top of `operatorStack`, if any (lines 40–46), and push the newly scanned operator into the stack (line 49). If a token is a `*` or `/` operator (line 51), process all the `*` and `/` operators from the top of `operatorStack`, if any (lines 53–57), and push the newly scanned operator to the stack (line 60). If a token is a `(` symbol (line 62), push it into `operatorStack`. If a token is a `)` symbol (line 65), process all the operators from the top of `operatorStack` until seeing the `)` symbol (lines 67–69) and pop the `)` symbol from the stack.

After all tokens are considered, the program processes the remaining operators in `operatorStack` (lines 80–82).

The `processAnOperator` method (lines 90–103) processes an operator. The method pops the operator from `operatorStack` (line 92) and pops two operands from `operandStack` (lines 93–94). Depending on the operator, the method performs an operation and pushes the result of the operation back to `operandStack` (lines 96, 98, 100, 102).

20.32 Can the `EvaluateExpression` program evaluate the following expressions "1+2", "1 + 2", "(1) + 2", "((1)) + 2", and "(1 + 2)"?

20.33 Show the change of the contents in the stacks when evaluating "3 + (4 + 5) * (3 + 5) + 4 * 5" using the `EvaluateExpression` program.

20.34 If you enter an expression "4 + 5 5 5", the program will display 10. How do you fix this problem?

### Key Terms

- **collection** 762
- **comparator** 772
- **convenience abstract class** 762
- **data structure** 762
- **linked list** 769
- **list** 762
- **priority queue** 783
- **queue** 762

### Chapter Summary

1. The Java Collections Framework supports *sets, lists, queues, and maps*. They are defined in the interfaces `Set`, `List`, `Queue`, and `Map`.

2. A *list* stores an ordered *collection* of elements.

3. All the concrete classes except `PriorityQueue` in the Java Collections Framework implement the `Cloneable` and `Serializable` interfaces. Thus, their instances can be cloned and serialized.
4. To allow duplicate elements to be stored in a collection, you need to use a list. A list not only can store duplicate elements but also allows the user to specify where they are stored. The user can access elements by an index.

5. Two types of lists are supported: `ArrayList` and `LinkedList`. `ArrayList` is a resizable-array implementation of the `List` interface. All the methods in `ArrayList` are defined in `List`. `LinkedList` is a `linked-list` implementation of the `List` interface. In addition to implementing the `List` interface, this class provides the methods for retrieving, inserting, and removing elements from both ends of the list.

6. `Comparator` can be used to compare the objects of a class that doesn’t implement `Comparable`.

7. The `Vector` class extends the `AbstractList` class. Starting with Java 2, `Vector` has been the same as `ArrayList`, except that the methods for accessing and modifying the vector are synchronized. The `Stack` class extends the `Vector` class and provides several methods for manipulating the stack.

8. The `Queue` interface represents a queue. The `PriorityQueue` class implements `Queue` for a priority queue.

**Quiz**

Answer the quiz for this chapter online at [www.cs.armstrong.edu/liang/intro10e/quiz.html](http://www.cs.armstrong.edu/liang/intro10e/quiz.html).

**Programming Exercises**

Sections 20.2–20.7

*20.1* (Display words in ascending alphabetical order) Write a program that reads words from a text file and displays all the words (duplicates allowed) in ascending alphabetical order. The words must start with a letter. The text file is passed as a command-line argument.

*20.2* (Store numbers in a linked list) Write a program that lets the user enter numbers from a graphical user interface and displays them in a text area, as shown in Figure 20.17a. Use a linked list to store the numbers. Do not store duplicate numbers. Add the buttons `Sort`, `Shuffle`, and `Reverse` to sort, shuffle, and reverse the list.

![Figure 20.17](http://www.cs.armstrong.edu/liang/intro10e/quiz.html)

(a) The numbers are stored in a list and displayed in the text area. (b) The colliding balls are combined.
**20.3 (Guessing the capitals)** Rewrite Programming Exercise 8.37 to store the pairs of states and capitals so that the questions are displayed randomly.

**20.4 (Sort points in a plane)** Write a program that meets the following requirements:

- Define a class named `Point` with two data fields `x` and `y` to represent a point’s `x`- and `y`-coordinates. Implement the `Comparable` interface for comparing the points on `x`-coordinates. If two points have the same `x`-coordinates, compare their `y`-coordinates.

- Define a class named `CompareY` that implements `Comparator<Point>`. Implement the `compare` method to compare two points on their `y`-coordinates. If two points have the same `y`-coordinates, compare their `x`-coordinates.

- Randomly create 100 points and apply the `Arrays.sort` method to display the points in increasing order of their `x`-coordinates and in increasing order of their `y`-coordinates, respectively.

***20.5 (Combine colliding bouncing balls)** The example in Section 20.7 displays multiple bouncing balls. Extend the example to detect collisions. Once two balls collide, remove the later ball that was added to the pane and add its radius to the other ball, as shown in Figure 20.17b. Use the `Suspend` button to suspend the animation and the `Resume` button to resume the animation. Add a mouse pressed handler that removes a ball when the mouse is pressed on the ball.

**20.6 (Use iterators on linked lists)** Write a test program that stores 5 million integers in a linked list and test the time to traverse the list using an iterator vs. using the `get(index)` method.

***20.7 (Game: hangman)** Programming Exercise 7.35 presents a console version of the popular hangman game. Write a GUI program that lets a user play the game. The user guesses a word by entering one letter at a time, as shown in Figure 20.18. If the user misses seven times, a hanging man swings. Once a word is finished, the user can press the `Enter` key to continue to guess another word.

**20.8 (Game: lottery)** Revise Programming Exercise 3.15 to add an additional $2,000 award if two digits from the user input are in the lottery number. (Hint: Sort the three digits in the lottery number and three digits in the user input into two lists, and use the `Collection`’s `containsAll` method to check whether the two digits in the user input are in the lottery number.)

Sections 20.8–20.10

***20.9 (Remove the largest ball first)** Modify Listing 20.6, `MultipleBallApp.java` to assign a random radius between 2 and 20 when a ball is created. When the – button is clicked, one of largest balls is removed.


***20.11 (Match grouping symbols)** A Java program contains various pairs of grouping symbols, such as:

- Parentheses: `( )`
- Braces: `{ }`
- Brackets: `[ ]`

Note that the grouping symbols cannot overlap. For example, `(a{b})` is illegal. Write a program to check whether a Java source-code file has correct pairs of grouping symbols. Pass the source-code file name as a command-line argument.
Figure 20.18  The program displays a hangman game.
20.12 (Clone PriorityQueue) Define MyPriorityQueue class that extends PriorityQueue to implement the Cloneable interface and implement the clone() method to clone a priority queue.

**20.13 (Game: the 24-point card game) The 24-point game is to pick any 4 cards from 52 cards, as shown in Figure 20.19. Note that the Jokers are excluded. Each card represents a number. An Ace, King, Queen, and Jack represent 1, 13, 12, and 11, respectively. You can click the Shuffle button to get four new cards. Enter an expression that uses the four numbers from the four selected cards. Each number must be used once and only once. You can use the operators (addition, subtraction, multiplication, and division) and parentheses in the expression. The expression must evaluate to 24. After entering the expression, click the Verify button to check whether the numbers in the expression are currently selected and whether the result of the expression is correct. Display the verification in a label before the Shuffle button. Assume that images are stored in files named 1.png, 2.png, ..., 52.png, in the order of spades, hearts, diamonds, and clubs. So, the first 13 images are for spades 1, 2, 3, ..., and 13.

**20.14 (Postfix notation) Postfix notation is a way of writing expressions without using parentheses. For example, the expression \((1 + 2) \times 3\) would be written as \(1 \ 2 \ + \ 3 \ \times\). A postfix expression is evaluated using a stack. Scan a postfix expression from left to right. A variable or constant is pushed into the stack. When an operator is encountered, apply the operator with the top two operands in the stack and replace the two operands with the result. The following diagram shows how to evaluate \(1 \ 2 \ + \ 3 \ \times\).

```
  1
  2
  3
  3
  9
```

scanned scanned scanned scanned scanned
Write a program to evaluate postfix expressions. Pass the expression as a command-line argument in one string.

***20.15 (Game: the 24-point card game) Improve Programming Exercise 20.13 to enable the computer to display the expression if one exists, as shown in Figure 20.20. Otherwise, report that the expression does not exist. Place the label for verification result at the bottom of UI. The expression must use all four cards and evaluates to 24.

**20.16 (Convert infix to postfix) Write a method that converts an infix expression into a postfix expression using the following header:

```
public static String infixToPostfix(String expression)
```

For example, the method should convert the infix expression 
\((1 + 2) \times 3\) to 
1 2 + 3 *
and 
2 \times (1 + 3)\) to 2 1 3 + *.

***20.17 (Game: the 24-point card game) This exercise is a variation of the 24-point card game described in Programming Exercise 20.13. Write a program to check whether there is a 24-point solution for the four specified numbers. The program lets the user enter four values, each between 1 and 13, as shown in Figure 20.21. The user can then click the Solve button to display the solution or display “No solution” if none exist.

*20.18 (Directory size) Listing 20.7, DirectorySize.java, gives a recursive method for finding a directory size. Rewrite this method without using recursion. Your
program should use a queue to store the subdirectories under a directory. The algorithm can be described as follows:

```java
long getSize(File directory) {
    long size = 0;
    add directory to the queue;

    while (queue is not empty) {
        Remove an item from the queue into t;
        if (t is a file)
            size += t.length();
        else
            add all the files and subdirectories under t into the queue;
    }

    return size;
}
```

***20.19 (Game: solution ratio for 24-point game)*** When you pick four cards from a deck of 52 cards for the 24-point game introduced in Programming Exercise 20.13, the four cards may not have a 24-point solution. What is the number of all possible picks of four cards from 52 cards? Among all possible picks, how many of them have 24-point solutions? What is the success ratio—that is, (number of picks with solutions)/ (number of all possible picks of four cards)? Write a program to find these answers.

**20.20 (Directory size)** Rewrite Programming Exercise 18.28 using a stack instead of a queue.

**20.21 (Use Comparator)** Write the following generic method using selection sort and a comparator.

```java
public static <E> void selectionSort(E[] list, Comparator<? super E> comparator)
```

Write a test program that creates an array of 10 GeometricObject s and invokes this method using the GeometricObjectComparator introduced in Listing 20.4 to sort the elements. Display the sorted elements. Use the following statement to create the array.

```java
GeometricObject[] list = {new Circle(5), new Rectangle(4, 5),
        new Circle(5.5), new Rectangle(2.4, 5), new Circle(0.5),
        new Rectangle(4, 65), new Circle(4.5), new Rectangle(4.4, 1),
        new Circle(6.5), new Rectangle(4, 5)};
```

**20.22 (Nonrecursive Tower of Hanoi)** Implement the moveDisks method in Listing 18.8 using a stack instead of using recursion.

**20.23 (Evaluate expression)** Modify Listing 20.9 EvaluateExpression.java to add operators ^ for exponent and % for modulus. For example, 3 ^ 2 is 9 and 3 % 2 is 1. The ^ operator has the highest precedence and the % operator has the same precedence as the * and / operators. Your program should prompt the user to enter an expression. Here is a sample run of the program:

```
Enter an expression: (5 * 2 ^ 3 + 2 * 3 % 2) * 4
(5 * 2 ^ 3 + 2 * 3 % 2) * 4 = 160
```
Sets and Maps

Objectives

- To store unordered, nonduplicate elements using a set (§21.2).
- To explore how and when to use HashSet (§21.2.1), LinkedHashSet (§21.2.2), or TreeSet (§21.2.3) to store a set of elements.
- To compare the performance of sets and lists (§21.3).
- To use sets to develop a program that counts the keywords in a Java source file (§21.4).
- To tell the differences between Collection and Map and describe when and how to use HashMap, LinkedHashMap, or TreeMap to store values associated with keys (§21.5).
- To use maps to develop a program that counts the occurrence of the words in a text (§21.6).
- To obtain singleton sets, lists, and maps, and unmodifiable sets, lists, and maps, using the static methods in the Collections class (§21.7).
Chapter 21  Sets and Maps

21.1 Introduction

A set is an efficient data structure for storing and processing nonduplicate elements. A map is like a dictionary that provides a quick lookup to retrieve a value using a key.

The “No-Fly” list is a list, created and maintained by the U.S. government’s Terrorist Screening Center, of people who are not permitted to board a commercial aircraft for travel in or out of the United States. Suppose we need to write a program that checks whether a person is on the No-Fly list. You can use a list to store names in the No-Fly list. However, a more efficient data structure for this application is a set.

Suppose your program also needs to store detailed information about terrorists in the No-Fly list. The detailed information such as gender, height, weight, and nationality can be retrieved using the name as the key. A map is an efficient data structure for such a task.

This chapter introduces sets and maps in the Java Collections Framework.

21.2 Sets

You can create a set using one of its three concrete classes: HashSet, LinkedHashSet, or TreeSet.

The Set interface extends the Collection interface, as shown in Figure 20.1. It does not introduce new methods or constants, but it stipulates that an instance of Set contains no duplicate elements. The concrete classes that implement Set must ensure that no duplicate elements can be added to the set. That is, no two elements e1 and e2 can be in the set such that e1.equals(e2) is true.

The AbstractSet class extends AbstractCollection and partially implements Set. The AbstractSet class provides concrete implementations for the equals method and the hashCode method. The hash code of a set is the sum of the hash codes of all the elements in the set. Since the size method and iterator method are not implemented in the AbstractSet class, AbstractSet is an abstract class.

Three concrete classes of Set are HashSet, LinkedHashSet, and TreeSet, as shown in Figure 21.1.

21.2.1 HashSet

The HashSet class is a concrete class that implements Set. You can create an empty hash set using its no-arg constructor or create a hash set from an existing collection. By default, the initial capacity is 16 and the load factor is 0.75. If you know the size of your set, you can specify the initial capacity and load factor in the constructor. Otherwise, use the default setting. The load factor is a value between 0.0 and 1.0.

The load factor measures how full the set is allowed to be before its capacity is increased. When the number of elements exceeds the product of the capacity and load factor, the capacity is automatically doubled. For example, if the capacity is 16 and load factor is 0.75, the capacity will be doubled to 32 when the size reaches 12 (16 * 0.75 = 12). A higher load factor decreases the space costs but increases the search time. Generally, the default load factor 0.75 is a good trade-off between time and space costs. We will discuss more on the load factor in Chapter 27, Hashing.

A HashSet can be used to store duplicate-free elements. For efficiency, objects added to a hash set need to implement the hashCode method in a manner that properly disperses the hash code. Recall that hashCode is defined in the Object class. The hash codes of two objects must be the same if the two objects are equal. Two unequal objects may have the same hash code, but you should implement the hashCode method to avoid too many such cases. Most of the classes in the Java API implement the hashCode method. For example, the hashCode in the Integer class returns its int value. The hashCode in the Character class returns the Unicode of the character. The hashCode in the String class returns $s_0 \cdot 31^{(n-1)} + s_1 \cdot 31^{(n-2)} + \ldots + s_{n-1}$, where $s_i$ is s.charAt(i).
Listing 21.1 gives a program that creates a hash set to store strings and uses a foreach loop to traverse the elements in the set.

**Listing 21.1  TestHashSet.java**

```java
import java.util.*;

public class TestHashSet {
    public static void main(String[] args) {
        // Create a hash set
        Set<String> set = new HashSet<>();

        // Add strings to the set
        set.add("London");
        set.add("Paris");
        set.add("New York");
        set.add("San Francisco");
        set.add("Beijing");
    }
}
```

![Java Collections Framework](image)

**Figure 21.1** The Java Collections Framework provides three concrete set classes.
The strings are added to the set (lines 9–14). New York is added to the set more than once, but only one string is stored, because a set does not allow duplicates.

As shown in the output, the strings are not stored in the order in which they are inserted into the set. There is no particular order for the elements in a hash set. To impose an order on them, you need to use the LinkedHashSet class, which is introduced in the next section.

Recall that the Collection interface extends the Iterable interface, so the elements in a set are iterable. A foreach loop is used to traverse all the elements in the set (lines 19–21).

Since a set is an instance of Collection, all methods defined in Collection can be used for sets. Listing 21.2 gives an example that applies the methods in the Collection interface on sets.

**LISTING 21.2 TestMethodsInCollection.java**

```java
public class TestMethodsInCollection {
    public static void main(String[] args) {
        // Create set1
        java.util.Set<String> set1 = new java.util.HashSet<>();
        // Add strings to set1
        set1.add("London");
        set1.add("Paris");
        set1.add("New York");
        set1.add("San Francisco");
        set1.add("Beijing");
        System.out.println("set1 is "+set1);
        System.out.println(set1.size()+" elements in set1");
        // Delete a string from set1
        set1.remove("London");
        System.out.println("\nset1 is "+set1);
        System.out.println(set1.size()+" elements in set1");
        // Create set2
        java.util.Set<String> set2 = new java.util.HashSet<>();
        // Add strings to set2
        set2.add("London");
        set2.add("Shanghai");
        set2.add("Paris");
        System.out.println("\nset2 is "+set2);
        System.out.println(set2.size()+" elements in set2");
    }
}
```

[San Francisco, New York, Paris, Beijing, London]
SAN FRANCISCO NEW YORK PARIS BEIJING LONDON
21.2 Sets

```
30  System.out.println("\nIs Taipei in set2? ");
31      + set2.contains("Taipei") + "
32  System.out.println("After adding set2 to set1, set1 is ");
33  + set1);
34  set1.addAll(set2);
35  System.out.println("After adding set2 to set1, set1 is ");
36  + set1);
37  set1.removeAll(set2);
38  System.out.println("After removing set2 from set1, set1 is ");
39  + set1);
40  set1.retainAll(set2);
41  System.out.println("After removing common elements in set2 ");
42  + "from set1, set1 is " + set1);
43  }
44  }
45  
set1 is [San Francisco, New York, Paris, Beijing, London]
5 elements in set1
set1 is [San Francisco, New York, Paris, Beijing]
4 elements in set1
set2 is [Shanghai, Paris, London]
3 elements in set2
Is Taipei in set2? false
After adding set2 to set1, set1 is [San Francisco, New York, Shanghai, Paris, Beijing, London]
After removing set2 from set1, set1 is [San Francisco, New York, Beijing]
After removing common elements in set2 from set1, set1 is []
```

The program creates two sets (lines 4, 22). The `size()` method returns the number of the elements in a set (line 14). Line 17

```
set1.remove("London");
```

removes `London` from `set1`. The `contains` method (line 32) checks whether an element is in the set. Line 34

```
set1.addAll(set2);
```


```
set1.removeAll(set2);
```

removes `set2` from `set1`. Thus, `set1` becomes `[San Francisco, New York, Beijing]`. Line 42

```
set1.retainAll(set2);
```
Chapter 21  Sets and Maps

retains the common elements in set1. Since set1 and set2 have no common elements, set1 becomes empty.

21.2.2  LinkedHashSet

LinkedHashSet extends HashSet with a linked-list implementation that supports an ordering of the elements in the set. The elements in a HashSet are not ordered, but the elements in a LinkedHashSet can be retrieved in the order in which they were inserted into the set. A LinkedHashSet can be created by using one of its four constructors, as shown in Figure 21.1. These constructors are similar to the constructors for HashSet.

Listing 21.3 gives a test program for LinkedHashSet. The program simply replaces HashSet by LinkedHashSet in Listing 21.1.

**LISTING 21.3  TestLinkedHashSet.java**

```java
import java.util.*;

public class TestLinkedHashSet {
  public static void main(String[] args) {
    // Create a hash set
    Set<String> set = new LinkedHashSet<>();
    // Add strings to the set
    set.add("London");
    set.add("Paris");
    set.add("New York");
    set.add("San Francisco");
    set.add("Beijing");
    set.add("New York");
    System.out.println(set);
    // Display the elements in the hash set
    for (Object element : set)
      System.out.print(element.toLowerCase() + " ");
  }
}
```

A LinkedHashSet is created in line 6. As shown in the output, the strings are stored in the order in which they are inserted. Since LinkedHashSet is a set, it does not store duplicate elements.

The LinkedHashSet maintains the order in which the elements are inserted. To impose a different order (e.g., increasing or decreasing order), you can use the TreeSet class, which is introduced in the next section.

**Tip**

If you don’t need to maintain the order in which the elements are inserted, use HashSet, which is more efficient than LinkedHashSet.

21.2.3  TreeSet

SortedSet is a subinterface of Set, which guarantees that the elements in the set are sorted. Additionally, it provides the methods first() and last() for returning the first and last elements in the set, and headSet(toElement) and tailSet(fromElement) for returning
a portion of the set whose elements are less than toElement and greater than or equal to fromElement, respectively.

NavigableSet extends SortedSet to provide navigation methods lower(e), floor(e), ceiling(e), and higher(e) that return elements respectively less than, less than or equal, greater than or equal, and greater than a given element and return null if there is no such element. The pollFirst() and pollLast() methods remove and return the first and last element in the tree set, respectively.

TreeSet implements the SortedSet interface. To create a TreeSet, use a constructor, as shown in Figure 21.1. You can add objects into a tree set as long as they can be compared with each other.

As discussed in Section 20.5, the elements can be compared in two ways: using the Comparable interface or the Comparator interface.

Listing 21.4 gives an example of ordering elements using the Comparable interface. The preceding example in Listing 21.3 displays all the strings in their insertion order. This example rewrites the preceding example to display the strings in alphabetical order using the TreeSet class.

**Listing 21.4 TestTreeSet.java**

```java
import java.util.*;

public class TestTreeSet {
    public static void main(String[] args) {
        // Create a hash set
        Set<String> set = new HashSet<>();
        // Add strings to the set
        set.add("London");
        set.add("Paris");
        set.add("New York");
        set.add("San Francisco");
        set.add("Beijing");
        // Create a tree set
        TreeSet<String> treeSet = new TreeSet<>(set);
        System.out.println("Sorted tree set: "+ treeSet);
        // Use the methods in SortedSet interface
        System.out.println("first(): "+ treeSet.first());
        System.out.println("last(): "+ treeSet.last());
        System.out.println("headSet("New York")": "+
            treeSet.headSet("New York");
        System.out.println("tailSet("New York")": "+
            treeSet.tailSet("New York");
        // Use the methods in NavigableSet interface
        System.out.println("lower("P")": " + treeSet.lower("P");
        System.out.println("higher("P")": " + treeSet.higher("P");
        System.out.println("floor("P")": " + treeSet.floor("P");
        System.out.println("ceiling("P")": " + treeSet.ceiling("P");
        System.out.println("pollFirst(): " + treeSet.pollFirst());
        System.out.println("pollLast(): " + treeSet.pollLast());
        System.out.println("New tree set: " + treeSet);
    }
}
```

first(): Beijing
last(): San Francisco
The example creates a hash set filled with strings, then creates a tree set for the same strings. The strings are sorted in the tree set using the `compareTo` method in the `Comparable` interface.

The elements in the set are sorted once you create a `TreeSet` object from a `HashSet` object using `new TreeSet<String>(set)` (line 16). You may rewrite the program to create an instance of `TreeSet` using its no-arg constructor, and add the strings into the `TreeSet` object.

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>treeSet.first()</code></td>
<td>Returns the first element in <code>treeSet</code> (line 20)</td>
</tr>
<tr>
<td><code>treeSet.last()</code></td>
<td>Returns the last element in <code>treeSet</code> (line 21)</td>
</tr>
<tr>
<td><code>treeSet.headSet(&quot;New York&quot;)</code></td>
<td>Returns the elements in <code>treeSet</code> before New York (lines 22–23).</td>
</tr>
<tr>
<td><code>treeSet.tailSet(&quot;New York&quot;)</code></td>
<td>Returns the elements in <code>treeSet</code> after New York, including New York (lines 24–25).</td>
</tr>
<tr>
<td><code>treeSet.lower(&quot;P&quot;)</code></td>
<td>Returns the largest element less than <code>P</code> in <code>treeSet</code> (line 28).</td>
</tr>
<tr>
<td><code>treeSet.higher(&quot;P&quot;)</code></td>
<td>Returns the smallest element greater than <code>P</code> in <code>treeSet</code> (line 29).</td>
</tr>
<tr>
<td><code>treeSet.floor(&quot;P&quot;)</code></td>
<td>Returns the largest element less than or equal to <code>P</code> in <code>treeSet</code> (line 30).</td>
</tr>
<tr>
<td><code>treeSet.ceiling(&quot;P&quot;)</code></td>
<td>Returns the smallest element greater than or equal to <code>P</code> in <code>treeSet</code> (line 31).</td>
</tr>
<tr>
<td><code>treeSet.pollFirst()</code></td>
<td>Removes the first element in <code>treeSet</code> and returns the removed element (line 32).</td>
</tr>
<tr>
<td><code>treeSet.pollLast()</code></td>
<td>Removes the last element in <code>treeSet</code> and returns the removed element (line 33).</td>
</tr>
</tbody>
</table>

**Note**

All the concrete classes in Java Collections Framework (see Figure 20.1) have at least two constructors. One is the no-arg constructor that constructs an empty collection. The other constructs instances from a collection. Thus the `TreeSet` class has the constructor `TreeSet(Collection c)` for constructing a `TreeSet` from a collection `c`. In this example, `new TreeSet<> (set)` creates an instance of `TreeSet` from the collection `set`.

**Tip**

If you don’t need to maintain a sorted set when updating a set, you should use a hash set, because it takes less time to insert and remove elements in a hash set. When you need a sorted set, you can create a tree set from the hash set.

If you create a `TreeSet` using its no-arg constructor, the `compareTo` method is used to compare the elements in the set, assuming that the class of the elements implements the `Comparable` interface. To use a comparator, you have to use the constructor `TreeSet(Comparator comparator)` to create a sorted set that uses the `compare` method in the comparator to order the elements in the set.

Listing 21.5 gives a program that demonstrates how to sort elements in a tree set using the `Comparator` interface.

**Listing 21.5  TestTreeSetWithComparator.java**

```java
import java.util.*;
```
21.2 Sets

```java
public class TestTreeSetWithComparator {
public static void main(String[] args) {
    // Create a tree set for geometric objects using a comparator
    Set<GeometricObject> set =
            new TreeSet<>(new GeometricObjectComparator());
    set.add(new Rectangle(4, 5));
    set.add(new Circle(40));
    set.add(new Circle(40));
    set.add(new Rectangle(4, 1));

    // Display geometric objects in the tree set
    System.out.println("A sorted set of geometric objects");
    for (GeometricObject element: set)
        System.out.println("area = " + element.getArea());
}
}
```

The `GeometricObjectComparator` class is defined in Listing 20.4. The program creates a tree set of geometric objects using the `GeometricObjectComparator` for comparing the elements in the set (lines 6–7).

The `Circle` and `Rectangle` classes were defined in Section 13.2, Abstract Classes. They are all subclasses of `GeometricObject`. They are added to the set (lines 8–11).

Two circles of the same radius are added to the tree set (lines 9–10), but only one is stored, because the two circles are equal and the set does not allow duplicates.

21.1 How do you create an instance of `Set`? How do you insert a new element in a set? How do you remove an element from a set? How do you find the size of a set?

21.2 If two objects `o1` and `o2` are equal, what is `o1.equals(o2)` and `o1.hashCode() == o2.hashCode()`?

21.3 What are the differences between `HashSet`, `LinkedHashSet`, and `TreeSet`?

21.4 How do you traverse the elements in a set?

21.5 How do you sort the elements in a set using the `compareTo` method in the `Comparable` interface? How do you sort the elements in a set using the `Comparator` interface? What would happen if you added an element that could not be compared with the existing elements in a tree set?

21.6 Suppose that `set1` is a set that contains the strings `red`, `yellow`, and `green`, and that `set2` is another set that contains the strings `red`, `yellow`, and `blue`. Answer the following questions:

- What are in `set1` and `set2` after executing `set1.addAll(set2)`?
- What are in `set1` and `set2` after executing `set1.add(set2)`?
- What are in `set1` and `set2` after executing `set1.removeAll(set2)`?
- What are in `set1` and `set2` after executing `set1.remove(set2)`?
- What are in `set1` and `set2` after executing `set1.retainAll(set2)`?
- What is in `set1` after executing `set1.clear()`?
21.7 Show the output of the following code:

```java
import java.util.*;

public class Test {
    public static void main(String[] args) {
        LinkedHashSet<String> set1 = new LinkedHashSet<>();
        set1.add("New York");
        LinkedHashSet<String> set2 = set1;
        LinkedHashSet<String> set3 = (LinkedHashSet<String>)(set1.clone());
        set1.add("Atlanta");
        System.out.println("set1 is " + set1);
        System.out.println("set2 is " + set2);
        System.out.println("set3 is " + set3);
    }
}
```

21.8 Show the output of the following code:

```java
import java.util.*;
import java.io.*;

public class Test {
    public static void main(String[] args) throws Exception {
        ObjectOutputStream output = new ObjectOutputStream(
            new FileOutputStream("c:\test.dat"));
        LinkedHashSet<String> set1 = new LinkedHashSet<>();
        set1.add("New York");
        LinkedHashSet<String> set2 = (LinkedHashSet<String>)(set1.clone());
        set1.add("Atlanta");
        output.writeObject(set1);
        output.writeObject(set2);
        output.close();

        ObjectInputStream input = new ObjectInputStream(
            new FileInputStream("c:\test.dat"));
        set1 = (LinkedHashSet<String>)input.readObject();
        set2 = (LinkedHashSet<String>)input.readObject();
        System.out.println(set1);
        System.out.println(set2);
        output.close();
    }
}
```

21.9 What will the output be if lines 6–7 in Listing 21.5 is replaced by the following code:

```java
Set<GeometricObject> set = new HashSet<>();
```

21.3 Comparing the Performance of Sets and Lists

*Sets are more efficient than lists for storing nonduplicate elements. Lists are useful for accessing elements through the index.*

The elements in a list can be accessed through the index. However, sets do not support indexing, because the elements in a set are unordered. To traverse all elements in a set, use a foreach loop. We now conduct an interesting experiment to test the performance of sets and lists. Listing 21.6 gives a program that shows the execution time of (1) testing whether an element
is in a hash set, linked hash set, tree set, array list, and linked list, and (2) removing elements from a hash set, linked hash set, tree set, array list, and linked list.

**Listing 21.6 SetListPerformanceTest.java**

```java
import java.util.*;

public class SetListPerformanceTest {
    static final int N = 50000;

    public static void main(String[] args) {
        // Add numbers 0, 1, 2, ..., N - 1 to the array list
        List<Integer> list = new ArrayList<>();
        for (int i = 0; i < N; i++)
            list.add(i);
        Collections.shuffle(list); // Shuffle the array list

        // Create a hash set, and test its performance
        Collection<Integer> set1 = new HashSet<>(list);
        System.out.println("Member test time for hash set is " +
            getTestTime(set1) + " milliseconds");
        System.out.println("Remove element time for hash set is " +
            getRemoveTime(set1) + " milliseconds");

        // Create a linked hash set, and test its performance
        Collection<Integer> set2 = new LinkedHashSet<>(list);
        System.out.println("Member test time for linked hash set is " +
            getTestTime(set2) + " milliseconds");
        System.out.println("Remove element time for linked hash set is " +
            getRemoveTime(set2) + " milliseconds");

        // Create a tree set, and test its performance
        Collection<Integer> set3 = new TreeSet<>(list);
        System.out.println("Member test time for tree set is " +
            getTestTime(set3) + " milliseconds");
        System.out.println("Remove element time for tree set is " +
            getRemoveTime(set3) + " milliseconds");

        // Create an array list, and test its performance
        Collection<Integer> list1 = new ArrayList<>(list);
        System.out.println("Member test time for array list is " +
            getTestTime(list1) + " milliseconds");
        System.out.println("Remove element time for array list is " +
            getRemoveTime(list1) + " milliseconds");

        // Create a linked list, and test its performance
        Collection<Integer> list2 = new LinkedList<>(list);
        System.out.println("Member test time for linked list is " +
            getTestTime(list2) + " milliseconds");
        System.out.println("Remove element time for linked list is " +
            getRemoveTime(list2) + " milliseconds");
    }

    public static long getTestTime(Collection<Integer> c) {
        long startTime = System.currentTimeMillis();
        for (int i = 0; i < N; i++)
            c.contains((int)(Math.random() * 2 * N));
        return System.currentTimeMillis() - startTime;
    }

    public static long getRemoveTime(Collection<Integer> c) {
        long startTime = System.currentTimeMillis();
        for (int i = 0; i < N; i++)
            c.remove(new Integer((int)(Math.random() * 2 * N)));
        return System.currentTimeMillis() - startTime;
    }
}
```
public static long getRemoveTime(Collection<Integer> c) {
    long startTime = System.currentTimeMillis();
    for (int i = 0; i < N; i++)
        c.remove(i);
    return System.currentTimeMillis() - startTime;
}

Member test time for hash set is 20 milliseconds
Remove element time for hash set is 27 milliseconds
Member test time for linked hash set is 27 milliseconds
Remove element time for linked hash set is 26 milliseconds
Member test time for tree set is 47 milliseconds
Remove element time for tree set is 34 milliseconds
Member test time for array list is 39802 milliseconds
Remove element time for array list is 16196 milliseconds
Member test time for linked list is 52197 milliseconds
Remove element time for linked list is 14870 milliseconds

The program creates a list for numbers from 0 to N-1 (for N = 50000) (lines 8–10) and shuffles the list (line 11). From this list, the program creates a hash set (line 14), a linked hash set (line 21), a tree set (line 28), an array list (line 35), and a linked list (line 42). The program obtains the execution time for testing whether a number is in the hash set (line 16), linked hash set (line 23), tree set (line 30), array list (line 37), and linked list (line 44), and obtains the execution time for removing the elements from the hash set (line 18), linked hash set (line 25), tree set (line 32), array list (line 39), and linked list (line 46).

The getTestTime method invokes the contains method to test whether a number is in the container (line 54) and the getRemoveTime method invokes the remove method to remove an element from the container (line 63).

As these runtimes illustrate, sets are much more efficient than lists for testing whether an element is in a set or a list. Therefore, the No-Fly list should be implemented using a set instead of a list, because it is much faster to test whether an element is in a set than in a list.

You may wonder why sets are more efficient than lists. The questions will be answered in Chapters 24 and 27 when we introduce the implementations of lists and sets.

21.10 Suppose you need to write a program that stores unordered non-duplicate elements, what data structure should you use?

21.11 Suppose you need to write a program that stores non-duplicate elements in the order of insertion, what data structure should you use?

21.12 Suppose you need to write a program that stores non-duplicate elements in increasing order of the element values, what data structure should you use?

21.13 Suppose you need to write a program that stores a fixed number of the elements (possibly duplicates), what data structure should you use?

21.14 Suppose you need to write a program that stores the elements in a list with frequent operations to add and insert elements at the end of the list, what data structure should you use?

21.15 Suppose you need to write a program that stores the elements in a list with frequent operations to add and insert elements at the beginning of the list, what data structure should you use?
21.4 Case Study: Counting Keywords

This section presents an application that counts the number of the keywords in a Java source file.

For each word in a Java source file, we need to determine whether the word is a keyword. To handle this efficiently, store all the keywords in a `HashSet` and use the `contains` method to test if a word is in the keyword set. Listing 21.7 gives this program.

**Listing 21.7 CountKeywords.java**

```java
import java.util.*;
import java.io.*;

public class CountKeywords {
  public static void main(String[] args) throws Exception {
    Scanner input = new Scanner(System.in);
    System.out.print("Enter a Java source file: ");
    String filename = input.nextLine();

    File file = new File(filename);
    if (file.exists()) {
      System.out.println("The number of keywords in ", filename + " is " + countKeywords(file));
    }
    else {
      System.out.println("File ", filename, " does not exist");
    }
  }

  public static int countKeywords(File file) throws Exception {
    // Array of all Java keywords + true, false and null

    Set<String> keywordSet = new HashSet<>(Arrays.asList(keywordString));
    Scanner input = new Scanner(file);
    int count = 0;

    while (input.hasNext()) {
      String word = input.next();
      if (keywordSet.contains(word)) count++;
    }

    return count;
  }
}
```

**Key Point**
- Enter a filename
- File exists?
- Count keywords
- Keyword set
Enter a Java source file: c:\Welcome.java
The number of keywords in c:\Welcome.java is 5

Enter a Java source file: c:\TTT.java
File c:\TTT.java does not exist

The program prompts the user to enter a Java source filename (line 7) and reads the filename (line 8). If the file exists, the countKeywords method is invoked to count the keywords in the file (line 13).

The countKeywords method creates an array of strings for the keywords (lines 22–31) and creates a hash set from this array (lines 33–34). It then reads each word from the file and tests if the word is in the set (line 41). If so, the program increases the count by 1 (line 42).

You may rewrite the program to use a LinkedHashSet, TreeSet, ArrayList, or LinkedList to store the keywords. However, using a HashSet is the most efficient for this program.

21.16 Will the CountKeywords program work if lines 33–34 are changed to

```java
Set<String> keywordSet =
   new LinkedHashSet<>(Arrays.asList(keywordString));
```

21.17 Will the CountKeywords program work if lines 33–34 are changed to

```java
List<String> keywordSet =
   new ArrayList<>(Arrays.asList(keywordString));
```

21.5 Maps

You can create a map using one of its three concrete classes: HashMap, LinkedHashMap, or TreeMap.

A map is a container object that stores a collection of key/value pairs. It enables fast retrieval, deletion, and updating of the pair through the key. A map stores the values along with the keys. The keys are like indexes. In List, the indexes are integers. In Map, the keys can be any objects.

A map cannot contain duplicate keys. Each key maps to one value. A key and its corresponding value form an entry stored in a map, as shown in Figure 21.2a. Figure 21.2b shows a map in which each entry consists of a Social Security number as the key and a name as the value.

![Diagram of a map with key/value pairs](image)

**Figure 21.2** The entries consisting of key/value pairs are stored in a map.
There are three types of maps: HashMap, LinkedHashMap, and TreeMap. The common features of these maps are defined in the Map interface. Their relationship is shown in Figure 21.3.

**SortedMap**  **NavigableMap**  **TreeMap**

Map  AbstractMap  Hashmap  LinkedHashMap

**Interfaces**  **Abstract Classes**  **Concrete Classes**

**FIGURE 21.3** A map stores key/value pairs.

The Map interface provides the methods for querying, updating, and obtaining a collection of values and a set of keys, as shown in Figure 21.4.

```
@interface
java.util.Map<K,V>
+
clear(): void
+containsKey(key: Object): boolean
+containsValue(value: Object): boolean
+entrySet(): Set<Map.Entry<K,V>>
+get(key: Object): V
+isEmpty(): boolean
+keySet(): Set<K>
+put(key: K, value: V): V
+putAll(m: Map<? extends K,? extends V>): void
+remove(key: Object): V
+size(): int
+values(): Collection<V>
```

**update methods**
- The clear() method removes all entries from this map.
- The put(K key, V value) method adds an entry for the specified key and value in the map. If the map formerly contained an entry for this key, the old value is replaced by the new value and the old value associated with the key is returned.
- The putAll(Map m) method adds all entries in m to this map. The remove(Object key) method removes the entry for the specified key from the map.

**query methods**
- The containsKey(Object key) method checks whether the map contains an entry for the specified key. The containsValue(Object value) method checks whether the map contains an entry for this value. The isEmpty() method checks whether the map contains any entries. The size() method returns the number of entries in the map.

**FIGURE 21.4** The Map interface maps keys to values.

The update methods include clear, put, putAll, and remove. The clear() method removes all entries from the map. The put(K key, V value) method adds an entry for the specified key and value in the map. If the map formerly contained an entry for this key, the old value is replaced by the new value and the old value associated with the key is returned. The putAll(Map m) method adds all entries in m to this map. The remove(Object key) method removes the entry for the specified key from the map.

The query methods include containsKey, containsValue, isEmpty, and size. The containsKey(Object key) method checks whether the map contains an entry for the specified key. The containsValue(Object value) method checks whether the map contains an entry for this value. The isEmpty() method checks whether the map contains any entries. The size() method returns the number of entries in the map.
You can obtain a set of the keys in the map using the `keySet()` method, and a collection of the values in the map using the `values()` method. The `entrySet()` method returns a set of entries. The entries are instances of the `Map.Entry<K, V>` interface, where `Entry` is an inner interface for the `Map` interface, as shown in Figure 21.5. Each entry in the set is a key/value pair in the underlying map.

Figure 21.5 The `Map.Entry` interface operates on an entry in the map.

AbstractMap concrete implementations

The `AbstractMap` class is a convenience abstract class that implements all the methods in the `Map` interface except the `entrySet()` method.

The `HashMap`, `LinkedHashMap`, and `TreeMap` classes are three concrete implementations of the `Map` interface, as shown in Figure 21.6.

Figure 21.6 The Java Collections Framework provides three concrete map classes.
The **HashMap** class is efficient for locating a value, inserting an entry, and deleting an entry. **LinkedHashMap** extends **HashMap** with a linked-list implementation that supports an ordering of the entries in the map. The entries in a **HashMap** are not ordered, but the entries in a **LinkedHashMap** can be retrieved either in the order in which they were inserted into the map (known as the *insertion order*) or in the order in which they were last accessed, from least recently to most recently accessed (*access order*). The no-arg constructor constructs a **LinkedHashMap** with the insertion order. To construct a **LinkedHashMap** with the access order, use **LinkedHashMap(initialCapacity, loadFactor, true)**.

The **TreeMap** class is efficient for traversing the keys in a sorted order. The keys can be sorted using the **Comparable** interface or the **Comparator** interface. If you create a **TreeMap** using its no-arg constructor, the **compareTo** method in the **Comparable** interface is used to compare the keys in the map, assuming that the class for the keys implements the **Comparable** interface. To use a comparator, you have to use the **TreeMap(Comparator comparator)** constructor to create a sorted map that uses the **compare** method in the comparator to order the entries in the map based on the keys.

**SortedMap** is a subinterface of **Map**, which guarantees that the entries in the map are sorted. Additionally, it provides the methods **firstKey()** and **lastKey()** for returning the first and last keys in the map, and **headMap(toKey)** and **tailMap(fromKey)** for returning a portion of the map whose keys are less than **toKey** and greater than or equal to **fromKey**, respectively.

**NavigableMap** extends **SortedMap** to provide the navigation methods **lowerKey(key)**, **floorKey(key)**, **ceilingKey(key)**, and **higherKey(key)** that return keys respectively less than, less than or equal, greater than or equal, and greater than a given key and return **null** if there is no such key. The **pollFirstEntry()** and **pollLastEntry()** methods remove and return the first and last entry in the tree map, respectively.

**Note**
Prior to Java 2, **java.util.Hashtable** was used for mapping keys with values. **Hashtable** was redesigned to fit into the Java Collections Framework with all its methods retained for compatibility. **Hashtable** implements the **Map** interface and is used in the same way as **HashMap**, except that the update methods in **Hashtable** are synchronized.

Listing 21.8 gives an example that creates a hash map, a linked hash map, and a tree map for mapping students to ages. The program first creates a hash map with the student’s name as its key and the age as its value. The program then creates a tree map from the hash map and displays the entries in ascending order of the keys. Finally, the program creates a linked hash map, adds the same entries to the map, and displays the entries.

**LISTING 21.8 TestMap.java**

```java
import java.util.*;

public class TestMap {
    public static void main(String[] args) {
        // Create a HashMap
        Map<String, Integer> hashMap = new HashMap<>();
        hashMap.put("Smith", 30);
        hashMap.put("Anderson", 31);
        hashMap.put("Lewis", 29);
        hashMap.put("Cook", 29);

        System.out.println("Display entries in HashMap");
        System.out.println(hashMap + "\n");

        // Create a TreeMap from the preceding HashMap
        Map<String, Integer> treeMap = new TreeMap<>(hashMap);
        System.out.println("Display entries in TreeMap");
        System.out.println(treeMap + "\n");

        // Create a LinkedHashMap from the preceding HashMap
        Map<String, Integer> linkedHashMap = new LinkedHashSet<>(hashMap);
        System.out.println("Display entries in LinkedHashSet");
        System.out.println(linkedHashMap + "\n");
    }
}
```
new TreeMap<>(hashMap);
System.out.println("Display entries in ascending order of key");
System.out.println(treeMap);

// Create a LinkedHashMap
Map<String, Integer> linkedHashMap =
    new LinkedHashMap<>(16, 0.75f, true);
linkedHashMap.put("Smith", 30);
linkedHashMap.put("Anderson", 31);
linkedHashMap.put("Lewis", 29);
linkedHashMap.put("Cook", 29);

// Display the age for Lewis
System.out.println("\nThe age for " + "Lewis is " +
    linkedHashMap.get("Lewis");
System.out.println("Display entries in LinkedHashMap");
System.out.println(linkedHashMap);
}

As shown in the output, the entries in the HashMap are in random order. The entries in the TreeMap are in increasing order of the keys. The entries in the LinkedHashMap are in the order of their access, from least recently accessed to most recently.

All the concrete classes that implement the Map interface have at least two constructors. One is the no-arg constructor that constructs an empty map, and the other constructs a map from an instance of Map. Thus, new TreeMap<String, Integer>(hashMap) (lines 16–17) constructs a tree map from a hash map.

You can create an insertion-ordered or access-ordered linked hash map. An access-ordered linked hash map is created in lines 22–21. The most recently accessed entry is placed at the end of the map. The entry with the key Lewis is last accessed in line 31, so it is displayed last in line 34.

Tip
If you don’t need to maintain an order in a map when updating it, use a HashMap. When you need to maintain the insertion order or access order in the map, use a LinkedHashMap. When you need the map to be sorted on keys, use a TreeMap.

21.18 How do you create an instance of Map? How do you add an entry to a map consisting of a key and a value? How do you remove an entry from a map? How do you find the size of a map? How do you traverse entries in a map?

21.19 Describe and compare HashMap, LinkedHashMap, and TreeMap.
21.20 Show the output of the following code:

```java
class Test {
    public static void main(String[] args) {
        Map<String, String> map = new LinkedHashMap<>();
        map.put("123", "John Smith");
        map.put("111", "George Smith");
        map.put("123", "Steve Yao");
        map.put("222", "Steve Yao");
        System.out.println("(1) "+ map);
        System.out.println("(2) "+ new TreeMap<>(map));
    }
}
```

21.6 Case Study: Occurrences of Words

This case study writes a program that counts the occurrences of words in a text and displays the words and their occurrences in alphabetical order of the words.

The program uses a TreeMap to store an entry consisting of a word and its count. For each word, check whether it is already a key in the map. If not, add an entry to the map with the word as the key and value 1. Otherwise, increase the value for the word (key) by 1 in the map. Assume the words are case insensitive; e.g., Good is treated the same as good.

Listing 21.9 gives the solution to the problem.

**Listing 21.9 CountOccurrenceOfWords.java**

```java
import java.util.*;

public class CountOccurrenceOfWords {
    public static void main(String[] args) {
        // Set text in a string
        String text = "Good morning. Have a good class. "+
        "Have a good visit. Have fun!"
        .toLowerCase();
        // Create a TreeMap to hold words as key and count as value
        Map<String, Integer> map = new TreeMap<>();
        String[] words = text.split("\n\t\r,.;:!?(){");
        for (int i = 0; i < words.length; i++) {
            String key = words[i].toLowerCase();
            if (key.length() > 0) {
                if (!map.containsKey(key)) {
                    map.put(key, 1);
                } else {
                    int value = map.get(key);
                    value++;
                    map.put(key, value);
                }
            }
        }
        // Get all entries into a set
        Set<Map.Entry<String, Integer>> entrySet = map.entrySet();
    }
}
```
The program creates a `TreeMap` (line 10) to store pairs of words and their occurrence counts. The words serve as the keys. Since all values in the map must be stored as objects, the count is wrapped in an `Integer` object.

The program extracts a word from a text using the `split` method (line 12) in the `String` class (see Section 10.10.4). For each word extracted, the program checks whether it is already stored as a key in the map (line 17). If not, a new pair consisting of the word and its initial count (1) is stored in the map (line 18). Otherwise, the count for the word is incremented by 1 (lines 21–23).

The program obtains the entries of the map in a set (line 29), and traverses the set to display the count and the key in each entry (lines 32–33).

Since the map is a tree map, the entries are displayed in increasing order of words. To display them in ascending order of the occurrence counts, see Programming Exercise 21.8.

Now sit back and think how you would write this program without using map. Your new program would be longer and more complex. You will find that map is a very efficient and powerful data structure for solving problems such as this.

### Check Point

21.21 Will the `CountOccurrenceOfWords` program work if line 10 is changed to

```java
Map<String, Integer> map = new TreeMap<>();
```

21.22 Will the `CountOccurrenceOfWords` program work if line 17 is changed to

```java
if (map.get(key) == null) {
```

21.23 Will the `CountOccurrenceOfWords` program work if lines 32–33 are changed to

```java
for (String key: map)
    System.out.println(key + "\t" + map.getValue(key));
```

### 21.7 Singleton and Unmodifiable Collections and Maps

You can create singleton sets, lists, and maps and unmodifiable sets, lists, and maps using the static methods in the `Collections` class.

The `Collections` class contains the static methods for lists and collections. It also contains the methods for creating immutable singleton sets, lists, and maps, and for creating read-only sets, lists, and maps, as shown in Figure 21.7.

The `Collections` class defines three constants—`EMPTY_SET`, `EMPTY_LIST`, and `EMPTY_MAP`—for an empty set, an empty list, and an empty map. These collections are immutable. The class also provides the `singleton(Object o)` method for creating an immutable set containing only a single item, the `singletonList(Object o)` method for creating
an immutable list containing only a single item, and the `singletonMap(Object key, Object value)` method for creating an immutable map containing only a single entry.

The Collections class also provides six static methods for returning read-only views for collections: `unmodifiableCollection(Collection c)`, `unmodifiableList(List list)`, `unmodifiableMap(Map m)`, `unmodifiableSet(Set s)`, `unmodifiableSortedMap(SortedMap m)`, and `unmodifiableSortedSet(SortedSet s)`. This type of view is like a reference to the actual collection. But you cannot modify the collection through a read-only view. Attempting to modify a collection through a read-only view will cause an `UnsupportedOperationException`.

21.24 What is wrong in the following code?

```java
Set<String> set = Collections.singleton("Chicago");
set.add("Dallas");
```

21.25 What happens when you run the following code?

```java
List list = Collections.unmodifiableList(Arrays.asList("Chicago", "Boston"));
list.remove("Dallas");
```

**Key Terms**

- hash map 813
- hash set 798
- linked hash map 813
- linked hash set 802
- map 810
- set 798
- read-only view 817
- tree map 813
- tree set 803

**Chapter Summary**

1. A set stores nonduplicate elements. To allow duplicate elements to be stored in a collection, you need to use a list.

2. A map stores key/value pairs. It provides a quick lookup for a value using a key.

3. Three types of sets are supported: HashSet, LinkedHashSet, and TreeSet. HashSet stores elements in an unpredictable order. LinkedHashSet stores elements in the order
they were inserted. **TreeSet** stores elements sorted. All the methods in **HashSet**, **LinkedHashSet**, and **TreeSet** are inherited from the **Collection** interface.

4. The **Map** interface maps keys to the elements. The keys are like indexes. In **List**, the indexes are integers. In **Map**, the keys can be any objects. A map cannot contain duplicate keys. Each key can map to at most one value. The **Map** interface provides the methods for querying, updating, and obtaining a collection of values and a set of keys.

5. Three types of maps are supported: **HashMap**, **LinkedHashMap**, and **TreeMap**. **HashMap** is efficient for locating a value, inserting an entry, and deleting an entry. **LinkedHashMap** supports ordering of the entries in the map. The entries in a **HashMap** are not ordered, but the entries in a **LinkedHashMap** can be retrieved either in the order in which they were inserted into the map (known as the **insertion order**) or in the order in which they were last accessed, from least recently accessed to most recently (access order). **TreeMap** is efficient for traversing the keys in a sorted order. The keys can be sorted using the **Comparable** interface or the **Comparator** interface.

**Quiz**

Answer the quiz for this chapter online at [www.cs.armstrong.edu/liang/intro10e/quiz.html](http://www.cs.armstrong.edu/liang/intro10e/quiz.html).

**PROGRAMMING EXERCISES**

**Sections 21.2–21.4**

**21.1** (Perform set operations on hash sets) Create two linked hash sets {"George", "Jim", "John", "Blake", "Kevin", "Michael"} and {"George", "Katie", "Kevin", "Michelle", "Ryan"} and find their union, difference, and intersection. (You can clone the sets to preserve the original sets from being changed by these set methods.)

**21.2** (Display nonduplicate words in ascending order) Write a program that reads words from a text file and displays all the nonduplicate words in ascending order. The text file is passed as a command-line argument.

**21.3** (Count the keywords in Java source code) Revise the program in Listing 21.7. If a keyword is in a comment or in a string, don’t count it. Pass the Java file name from the command line. Assume that the Java source code is correct and line comments and paragraph comments do not overlap.

**21.4** (Count consonants and vowels) Write a program that prompts the user to enter a text file name and displays the number of vowels and consonants in the file. Use a set to store the vowels **A**, **E**, **I**, **O**, and **U**.

**21.5** (Syntax highlighting) Write a program that converts a Java file into an HTML file. In the HTML file, the keywords, comments, and literals are displayed in bold navy, green, and blue, respectively. Use the command line to pass a Java file and an HTML file. For example, the following command

```
java Exercise21_05 Welcome.java Welcome.html
```

converts **Welcome.java** into **Welcome.html**. Figure 21.8a shows a Java file. The corresponding HTML file is shown in Figure 21.8b.
**21.6 (Count the occurrences of numbers entered)** Write a program that reads an unspecified number of integers and finds the one that has the most occurrences. The input ends when the input is 0. For example, if you entered 2 3 0 3 5 4 – 3 3 2 0, the number 3 occurred most often. If not one but several numbers have the most occurrences, all of them should be reported. For example, since 9 and 3 appear twice in the list 9 3 0 3 9 3 2 4, both occurrences should be reported.

**21.7 (Revise Listing 21.9, CountOccurrenceOfWords.java)** Rewrite Listing 21.9 to display the words in ascending order of occurrence counts.

(Hint: Create a class named `WordOccurrence` that implements the `Comparable` interface. The class contains two fields, `word` and `count`. The `compareTo` method compares the counts. For each pair in the hash set in Listing 21.9, create an instance of `WordOccurrence` and store it in an array list. Sort the array list using the `Collections.sort` method. What would be wrong if you stored the instances of `WordOccurrence` in a tree set?)

**21.8 (Count the occurrences of words in a text file)** Rewrite Listing 21.9 to read the text from a text file. The text file is passed as a command-line argument. Words are delimited by whitespace characters, punctuation marks (,.;?:"), quotation marks ("), and parentheses. Count words in case-insensitive fashion (e.g., consider Good and good to be the same word). The words must start with a letter. Display the output in alphabetical order of words, with each word preceded by its occurrence count.

**21.9 (Guess the capitals using maps)** Rewrite Programming Exercise 8.37 to store pairs of each state and its capital in a map. Your program should prompt the user to enter a state and should display the capital for the state.

**21.10 (Count the occurrences of each keyword)** Rewrite Listing 21.7 CountKeywords.java to read in a Java source code file and count the occurrence of each keyword in the file, but don’t count the keyword if it is in a comment or in a string literal.

**21.11 (Baby name popularity ranking)** Use the data files from Programming Exercise 12.31 to write a program that enables the user to select a year, gender, and enter a name to display the ranking of the name for the selected year and gender, as shown in Figure 21.9. To achieve the best efficiency, create two arrays for boy’s names and girl’s names, respectively. Each array has 10 elements for 10 years. Each element is a map that stores a name and its ranking in a pair with the name as the key. Assume the data files are stored at www.cs.armstrong.edu/liang/data/babynamesranking2001.txt, . . . , and www.cs.armstrong.edu/liang/data/babynamesranking2010.txt.

---

**Sections 21.5–21.7**

*21.6 (Count the occurrences of numbers entered)** Write a program that reads an unspecified number of integers and finds the one that has the most occurrences. The input ends when the input is 0. For example, if you entered 2 3 0 3 5 4 – 3 3 2 0, the number 3 occurred most often. If not one but several numbers have the most occurrences, all of them should be reported. For example, since 9 and 3 appear twice in the list 9 3 0 3 9 3 2 4, both occurrences should be reported.

**21.7 (Revise Listing 21.9, CountOccurrenceOfWords.java)** Rewrite Listing 21.9 to display the words in ascending order of occurrence counts.

(Hint: Create a class named `WordOccurrence` that implements the `Comparable` interface. The class contains two fields, `word` and `count`. The `compareTo` method compares the counts. For each pair in the hash set in Listing 21.9, create an instance of `WordOccurrence` and store it in an array list. Sort the array list using the `Collections.sort` method. What would be wrong if you stored the instances of `WordOccurrence` in a tree set?)

**21.8 (Count the occurrences of words in a text file)** Rewrite Listing 21.9 to read the text from a text file. The text file is passed as a command-line argument. Words are delimited by whitespace characters, punctuation marks (,.;?:"), quotation marks ("), and parentheses. Count words in case-insensitive fashion (e.g., consider Good and good to be the same word). The words must start with a letter. Display the output in alphabetical order of words, with each word preceded by its occurrence count.

**21.9 (Guess the capitals using maps)** Rewrite Programming Exercise 8.37 to store pairs of each state and its capital in a map. Your program should prompt the user to enter a state and should display the capital for the state.

**21.10 (Count the occurrences of each keyword)** Rewrite Listing 21.7 CountKeywords.java to read in a Java source code file and count the occurrence of each keyword in the file, but don’t count the keyword if it is in a comment or in a string literal.

**21.11 (Baby name popularity ranking)** Use the data files from Programming Exercise 12.31 to write a program that enables the user to select a year, gender, and enter a name to display the ranking of the name for the selected year and gender, as shown in Figure 21.9. To achieve the best efficiency, create two arrays for boy’s names and girl’s names, respectively. Each array has 10 elements for 10 years. Each element is a map that stores a name and its ranking in a pair with the name as the key. Assume the data files are stored at www.cs.armstrong.edu/liang/data/babynamesranking2001.txt, . . . , and www.cs.armstrong.edu/liang/data/babynamesranking2010.txt.
**21.12** *(Name for both genders)* Write a program that prompts the user to enter one of the filenames described in Programming Exercise 12.31 and displays the names that are used for both genders in the file. Use sets to store names and find common names in two sets. Here is a sample run:

Enter a file name for baby name ranking: babynamesranking2001.txt
69 names used for both genders
They are Tyler Ryan Christian ...

**21.13** *(Baby name popularity ranking)* Revise Programming Exercise 21.11 to prompt the user to enter year, gender, and name and display the ranking for the name. Prompt the user to enter another inquiry or exit the program. Here is a sample run:

Enter the year: 2010
Enter the gender: M
Enter the name: Javier
Boy name Javier is ranked #190 in year 2010
Enter another inquiry? Y
Enter the year: 2001
Enter the gender: F
Enter the name: Emily
Girl name Emily is ranked #1 in year 2001
Enter another inquiry? N

**21.14** *(Web crawler)* Rewrite Listing 12.18, WebCrawler.java, to improve the performance by using appropriate new data structures for `listOfPendingURLs` and `listOfTraversedURLs`.

**21.15** *(Addition quiz)* Rewrite Programming Exercise 11.16 to store the answers in a set rather than a list.
DEVELOPING EFFICIENT ALGORITHMS

Objectives

■ To estimate algorithm efficiency using the Big $O$ notation (§22.2).
■ To explain growth rates and why constants and nondominating terms can be ignored in the estimation (§22.2).
■ To determine the complexity of various types of algorithms (§22.3).
■ To analyze the binary search algorithm (§22.4.1).
■ To analyze the selection sort algorithm (§22.4.2).
■ To analyze the Tower of Hanoi algorithm (§22.4.3).
■ To describe common growth functions (constant, logarithmic, log-linear, quadratic, cubic, exponential) (§22.4.4).
■ To design efficient algorithms for finding Fibonacci numbers using dynamic programming (§22.5).
■ To find the GCD using Euclid’s algorithm (§22.6).
■ To find prime numbers using the sieve of Eratosthenes (§22.7).
■ To design efficient algorithms for finding the closest pair of points using the divide-and-conquer approach (§22.8).
■ To solve the Eight Queens problem using the backtracking approach (§22.9).
■ To design efficient algorithms for finding a convex hull for a set of points (§22.10).
22.1 Introduction

Algorithm design is to develop a mathematical process for solving a problem. Algorithm analysis is to predict the performance of an algorithm.

The preceding two chapters introduced classic data structures (lists, stacks, queues, priority queues, sets, and maps) and applied them to solve problems. This chapter will use a variety of examples to introduce common algorithmic techniques (dynamic programming, divide-and-conquer, and backtracking) for developing efficient algorithms. Later in the book, we will introduce efficient algorithms in Chapters 23–29. Before introducing developing efficient algorithms, we need to address the question on how to measure algorithm efficiency.

22.2 Measuring Algorithm Efficiency Using Big O Notation

The Big O notation obtains a function for measuring algorithm time complexity based on the input size. You can ignore multiplicative constants and nondominating terms in the function.

Suppose two algorithms perform the same task, such as search (linear search vs. binary search). Which one is better? To answer this question, you might implement these algorithms and run the programs to get execution time. But there are two problems with this approach:

- First, many tasks run concurrently on a computer. The execution time of a particular program depends on the system load.
- Second, the execution time depends on specific input. Consider, for example, linear search and binary search. If an element to be searched happens to be the first in the list, linear search will find the element quicker than binary search.

It is very difficult to compare algorithms by measuring their execution time. To overcome these problems, a theoretical approach was developed to analyze algorithms independent of computers and specific input. This approach approximates the effect of a change on the size of the input. In this way, you can see how fast an algorithm’s execution time increases as the input size increases, so you can compare two algorithms by examining their growth rates.

Consider linear search. The linear search algorithm compares the key with the elements in the array sequentially until the key is found or the array is exhausted. If the key is not in the array, it requires $n$ comparisons for an array of size $n$. If the key is in the array, it requires $n/2$ comparisons on average. The algorithm’s execution time is proportional to the size of the array. If you double the size of the array, you will expect the number of comparisons to double. The algorithm grows at a linear rate. The growth rate has an order of magnitude of $n$. Computer scientists use the Big O notation to represent the “order of magnitude.” Using this notation, the complexity of the linear search algorithm is $O(n)$, pronounced as “order of $n$.” We call an algorithm with a time complexity of $O(n)$ a linear algorithm, and it exhibits a linear growth rate.

For the same input size, an algorithm’s execution time may vary, depending on the input. An input that results in the shortest execution time is called the best-case input, and an input that results in the longest execution time is the worst-case input. Best-case analysis and worst-case analysis are to analyze the algorithms for their best-case input and worst-case input. Best-case and worst-case analysis are not representative, but worst-case analysis is very useful. You can be assured that the algorithm will never be slower than the worst case. An average-case analysis attempts to determine the average amount of time among all possible inputs of the same size. Average-case analysis is ideal, but difficult to perform, because for many problems it is hard to determine the relative probabilities and distributions of various input instances. Worst-case analysis is easier to perform, so the analysis is generally conducted for the worst case.
The linear search algorithm requires \( n \) comparisons in the worst case and \( n/2 \) comparisons in the average case if you are nearly always looking for something known to be in the list. Using the Big \( O \) notation, both cases require \( O(n) \) time. The multiplicative constant \((1/2)\) can be omitted. Algorithm analysis is focused on growth rate. The multiplicative constants have no impact on growth rates. The growth rate for \( n/2 \) or \( 100n \) is the same as for \( n \), as illustrated in Table 22.1. Therefore, \( O(n) = O(n/2) = O(100n) \).

<table>
<thead>
<tr>
<th>( n )</th>
<th>( f(n) )</th>
<th>( n )</th>
<th>( n/2 )</th>
<th>( 100n )</th>
</tr>
</thead>
<tbody>
<tr>
<td>100</td>
<td>100</td>
<td>50</td>
<td>10000</td>
<td></td>
</tr>
<tr>
<td>200</td>
<td>200</td>
<td>100</td>
<td>20000</td>
<td></td>
</tr>
</tbody>
</table>

Consider the algorithm for finding the maximum number in an array of \( n \) elements. To find the maximum number if \( n \) is 2, it takes one comparison; if \( n \) is 3, two comparisons. In general, it takes \( n - 1 \) comparisons to find the maximum number in a list of \( n \) elements. Algorithm analysis is for large input size. If the input size is small, there is no significance in estimating an algorithm’s efficiency. As \( n \) grows larger, the \( n \) part in the expression \( n - 1 \) dominates the complexity. The Big \( O \) notation allows you to ignore the nondominating part (e.g., \(-1\) in the expression \( n - 1 \)) and highlight the important part (e.g., \( n \) in the expression \( n - 1 \)). Therefore, the complexity of this algorithm is \( O(n) \).

The Big \( O \) notation estimates the execution time of an algorithm in relation to the input size. If the time is not related to the input size, the algorithm is said to take constant time with the notation \( O(1) \). For example, a method that retrieves an element at a given index in an array takes constant time, because the time does not grow as the size of the array increases.

The following mathematical summations are often useful in algorithm analysis:

\[
1 + 2 + 3 + \ldots + (n - 2) + (n - 1) = \frac{n(n - 1)}{2} = O(n^2)
\]

\[
1 + 2 + 3 + \ldots + (n - 1) + n = \frac{n(n + 1)}{2} = O(n^2)
\]

\[
a^0 + a^1 + a^2 + a^3 + \ldots + a^{(n-1)} + a^n = \frac{a^{n+1} - 1}{a - 1} = O(a^n)
\]

\[
2^0 + 2^1 + 2^2 + 2^3 + \ldots + 2^{(n-1)} + 2^n = \frac{2^{n+1} - 1}{2 - 1} = 2^{n+1} - 1 = O(2^n)
\]

**Note**

Time complexity is a measure of execution time using the Big-O notation. Similarly, you can also measure space complexity using the Big-O notation. Space complexity measures the amount of memory space used by an algorithm. The space complexity for most algorithms presented in the book is \( O(n) \), i.e., they exhibit linear growth rate to the input size. For example, the space complexity for linear search is \( O(n) \).

---

**22.1** Why is a constant factor ignored in the Big \( O \) notation? Why is a nondominating term ignored in the Big \( O \) notation?

**22.2** What is the order of each of the following functions?

\[
\frac{(n^2 + 1)^2}{n}, \frac{(n^2 + \log^2 n)^2}{n}, n^3 + 100n^2 + n, 2^n + 100n^2 + 45n, n2^n + n^22^n
\]
22.3 Examples: Determining Big O

This section gives several examples of determining Big O for repetition, sequence, and selection statements.

Example 1

Consider the time complexity for the following loop:

```java
for (int i = 1; i <= n; i++) {
    k = k + 5;
}
```

It is a constant time, $c$, for executing

$$k = k + 5;$$

Since the loop is executed $n$ times, the time complexity for the loop is

$$T(n) = (\text{a constant } c) \cdot n = O(n).$$

The theoretical analysis predicts the performance of the algorithm. To see how this algorithm performs, we run the code in Listing 22.1 to obtain the execution time for $n = 1000000, 10000000, 100000000, \text{ and } 1000000000.$

**LISTING 22.1 PerformanceTest.java**

```java
public class PerformanceTest {
    public static void main(String[] args) {
        getTime(1000000);
        getTime(10000000);
        getTime(100000000);
        getTime(1000000000);
    }

    public static void getTime (long n) {
        long startTime = System.currentTimeMillis();
        long k = 0;
        for (int i = 1; i <= n; i++) {
            k = k + 5;
        }
        long endTime = System.currentTimeMillis();
        System.out.println("Execution time for n = "+ n + " is "+ (endTime - startTime) + " milliseconds");
    }
}
```

Our analysis predicts a linear time complexity for this loop. As shown in the sample output, when the input size increases 10 times, the runtime increases roughly 10 times. The execution confirms to the prediction.

Example 2

What is the time complexity for the following loop?

```java
for (int i = 1; i <= n; i++) {
    for (int j = 1; j <= n; j++) {
```
It is a constant time, $c$, for executing

$$k = k + i + j;$$

The outer loop executes $n$ times. For each iteration in the outer loop, the inner loop is executed $n$ times. Thus, the time complexity for the loop is

$$T(n) = (\text{a constant } c) \cdot n \cdot n = O(n^2)$$

An algorithm with the $O(n^2)$ time complexity is called a \textit{quadratic algorithm} and it exhibits a quadratic growth rate. The quadratic algorithm grows quickly as the problem size increases. If you double the input size, the time for the algorithm is quadrupled. Algorithms with a nested loop are often quadratic.

\textbf{Example 3}

Consider the following loop:

```java
for (int i = 1; i <= n; i++) {
    for (int j = 1; j <= i; j++) {
        k = k + i + j;
    }
}
```

The outer loop executes $n$ times. For $i = 1, 2, \ldots, n$, the inner loop is executed one time, two times, and $n$ times. Thus, the time complexity for the loop is

$$T(n) = c + 2c + 3c + 4c + \ldots + nc$$

$$= cn(n + 1)/2$$

$$= (c/2) n^2 + (c/2)n$$

$$= O(n^2)$$

\textbf{Example 4}

Consider the following loop:

```java
for (int i = 1; i <= n; i++) {
    for (int j = 1; j <= 20; j++) {
        k = k + i + j;
    }
}
```

The inner loop executes 20 times, and the outer loop $n$ times. Therefore, the time complexity for the loop is

$$T(n) = 20 \cdot c \cdot n = O(n)$$

\textbf{Example 5}

Consider the following sequences:

```java
for (int j = 1; j <= 10; j++) {
    k = k + 4;
}
```

```java
for (int i = 1; i <= n; i++) {
    \text{...}
}
```
Chapter 22  Developing Efficient Algorithms

```java
for (int j = 1; j <= 20; j++) {
    k = k + i + j;
}
```

The first loop executes 10 times, and the second loop \(20 \times n\) times. Thus, the time complexity for the loop is

\[T(n) = 10c + 20c\times n = O(n)\]

**Example 6**
Consider the following selection statement:

```java
if (list.contains(e)) {
    System.out.println(e);
} else {
    for (Object t : list) {
        System.out.println(t);
    }
}
```

Suppose the list contains \(n\) elements. The execution time for `list.contains(e)` is \(O(n)\). The loop in the `else` clause takes \(O(n)\) time. Hence, the time complexity for the entire statement is

\[T(n) = \text{if test time} + \text{worst-case time (if clause, else clause)} = O(n) + O(n) = O(n)\]

**Example 7**
Consider the computation of \(a^n\) for an integer \(n\). A simple algorithm would multiply \(a\) \(n\) times, as follows:

```java
result = 1;
for (int i = 1; i <= n; i++)
    result *= a;
```

The algorithm takes \(O(n)\) time. Without loss of generality, assume \(n = 2^k\). You can improve the algorithm using the following scheme:

```java
result = a;
for (int i = 1; i <= k; i++)
    result = result * result;
```

The algorithm takes \(O(\log n)\) time. For an arbitrary \(n\), you can revise the algorithm and prove that the complexity is still \(O(\log n)\). (See Checkpoint Question 22.7.)

**Note**
For simplicity, since \(O(\log n) = O(\log_2 n) = O(\log_a n)\), the constant base is omitted.

**Check Point**
Count the number of iterations in the following loops.

(a) ```java
int count = 1;
while (count < 30) {
    count = count * 2;
}
```

(b) ```java
int count = 15;
while (count < 30) {
    count = count * 3;
}
```
22.4 How many stars are displayed in the following code if n is 10? How many if n is 20? Use the Big O notation to estimate the time complexity.

```java
int count = 1;
while (count < n) {
    count = count * 2;
}
```

```java
int count = 15;
while (count < n) {
    count = count * 3;
}
```

(a) (b)

```java
for (int i = 0; i < n; i++) {
    System.out.print('*');
}
```

```java
for (int i = 0; i < n; i++) {
    for (int j = 0; j < n; j++) {
        System.out.print('*');
    }
}
```

(c) (d)

22.5 Use the Big O notation to estimate the time complexity of the following methods:

```java
public static void mA(int n) {
    for (int i = 0; i < n; i++) {
        System.out.print(Math.random());
    }
}
```

```java
public static void mB(int n) {
    for (int i = 0; i < n; i++) {
        for (int j = 0; j < i; j++)
            System.out.print(Math.random());
    }
}
```

(a) (b)

```java
public static void mC(int[] m) {
    for (int i = 0; i < m.length; i++) {
        System.out.print(m[i]);
    }
    for (int i = m.length - 1; i >= 0; )
    {
        System.out.print(m[i]);
        i--;
    }
}
```

```java
public static void mD(int[] m) {
    for (int i = 0; i < m.length; i++) {
        for (int j = 0; j < i; j++)
            System.out.print(m[i] * m[j]);
    }
}
```

(c) (d)

22.6 Design an O(n) time algorithm for computing the sum of numbers from n1 to n2 for (n1 < n2). Can you design an O(1) for performing the same task?

22.7 Example 7 in Section 22.3 assumes \( n = 2^k \). Revise the algorithm for an arbitrary \( n \) and prove that the complexity is still \( O(\log n) \).
22.4 Analyzing Algorithm Time Complexity

This section analyzes the complexity of several well-known algorithms: binary search, selection sort, and Tower of Hanoi.

22.4.1 Analyzing Binary Search

The binary search algorithm presented in Listing 7.7, BinarySearch.java, searches for a key in a sorted array. Each iteration in the algorithm contains a fixed number of operations, denoted by c. Let \( T(n) \) denote the time complexity for a binary search on a list of \( n \) elements. Without loss of generality, assume \( n \) is a power of 2 and \( k = \log n \). Since a binary search eliminates half of the input after two comparisons,

\[
T(n) = T\left(\frac{n}{2}\right) + c = T\left(\frac{n}{2^2}\right) + c + \cdots = T\left(\frac{n}{2^k}\right) + kc
\]

\[= T(1) + c \log n = 1 + (\log n)c\]

\[= O(\log n)\]

Ignoring constants and nondominating terms, the complexity of the binary search algorithm is \( O(\log n) \). An algorithm with the \( O(\log n) \) time complexity is called a logarithmic algorithm and it exhibits a logarithmic growth rate. The base of the log is 2, but the base does not affect a logarithmic growth rate, so it can be omitted. The logarithmic algorithm grows slowly as the problem size increases. In the case of binary search, each time you double the array size, at most one more comparison will be required. If you square the input size of any logarithmic time algorithm, you only double the time of execution. So a logarithmic-time algorithm is very efficient.

22.4.2 Analyzing Selection Sort

The selection sort algorithm presented in Listing 7.8, SelectionSort.java, finds the smallest element in the list and swaps it with the first element. It then finds the smallest element remaining and swaps it with the first element in the remaining list, and so on until the remaining list contains only one element left to be sorted. The number of comparisons is \( n - 1 \) for the first iteration, \( n - 2 \) for the second iteration, and so on. Let \( T(n) \) denote the complexity for selection sort and \( c \) denote the total number of other operations such as assignments and additional comparisons in each iteration. Thus,

\[
T(n) = (n - 1) + c + (n - 2) + c + \ldots + 2 + c + 1 + c
\]

\[= \frac{(n - 1)(n - 1 + 1)}{2} + c(n - 1) = \frac{n^2}{2} - \frac{n}{2} + cn - c\]

Therefore, the complexity of the selection sort algorithm is \( O(n^2) \).

22.4.3 Analyzing the Tower of Hanoi Problem

The Tower of Hanoi problem presented in Listing18.8, TowerOfHanoi.java, recursively moves \( n \) disks from tower A to tower B with the assistance of tower C as follows:

1. Move the first \( n - 1 \) disks from A to C with the assistance of tower B.
2. Move disk \( n \) from A to B.
3. Move \( n - 1 \) disks from C to B with the assistance of tower A.

The complexity of this algorithm is measured by the number of moves. Let \( T(n) \) denote the number of moves for the algorithm to move \( n \) disks from tower A to tower B with \( T(1) = 1 \). Thus,

\[
T(n) = T(n - 1) + 1 + T(n - 1)
= 2T(n - 1) + 1
= 2(2T(n - 2) + 1) + 1
= 2(2(2T(n - 3) + 1) + 1) + 1
= 2^{n-1}T(1) + 2^{n-2} + \ldots + 2 + 1
= 2^{n-1} + 2^{n-2} + \ldots + 2 + 1 = (2^n - 1) = O(2^n)
\]

An algorithm with \( O(2^n) \) time complexity is called an exponential algorithm, and it exhibits an exponential growth rate. As the input size increases, the time for the exponential algorithm grows exponentially. Exponential algorithms are not practical for large input size. Suppose the disk is moved at a rate of 1 per second. It would take \( \frac{2^{32}}{365*24*60*60} \approx 136 \) years to move 32 disks and \( \frac{2^{64}}{365*24*60*60} \approx 585 \) billion years to move 64 disks.

### 22.4.4 Common Recurrence Relations

Recurrence relations are a useful tool for analyzing algorithm complexity. As shown in the preceding examples, the complexity for binary search, selection sort, and the Tower of Hanoi is

- Binary search, Euclid’s GCD
- Checkpoint Question 22.20
- Merge sort (Chapter 23)
- Selection sort
- Recursive Fibonacci algorithm

### Table 22.2 Common Recurrence Functions

<table>
<thead>
<tr>
<th>Recurrence Relation</th>
<th>Result</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>( T(n) = T(n/2) + O(1) )</td>
<td>( T(n) = O(\log n) )</td>
<td>Binary search, Euclid’s GCD</td>
</tr>
<tr>
<td>( T(n) = T(n - 1) + O(1) )</td>
<td>( T(n) = O(n) )</td>
<td>Linear search</td>
</tr>
<tr>
<td>( T(n) = 2T(n/2) + O(1) )</td>
<td>( T(n) = O(n) )</td>
<td>Checkpoint Question 22.20</td>
</tr>
<tr>
<td>( T(n) = 2T(n/2) + O(n) )</td>
<td>( T(n) = O(n \log n) )</td>
<td>Merge sort (Chapter 23)</td>
</tr>
<tr>
<td>( T(n) = T(n - 1) + O(n) )</td>
<td>( T(n) = O(n^2) )</td>
<td>Selection sort</td>
</tr>
<tr>
<td>( T(n) = 2T(n - 1) + O(1) )</td>
<td>( T(n) = O(2^n) )</td>
<td>Tower of Hanoi</td>
</tr>
<tr>
<td>( T(n) = T(n - 1) + T(n - 2) + O(1) )</td>
<td>( T(n) = O(2^n) )</td>
<td>Recursive Fibonacci algorithm</td>
</tr>
</tbody>
</table>

### 22.4.5 Comparing Common Growth Functions

The preceding sections analyzed the complexity of several algorithms. Table 22.3 lists some common growth functions and shows how growth rates change as the input size doubles from \( n = 25 \) to \( n = 50 \).
Chapter 22  Developing Efficient Algorithms

These functions are ordered as follows, as illustrated in Figure 22.1.

\[ O(1) < O(\log n) < O(n) < O(n \log n) < O(n^2) < O(n^3) < O(2^n) \]

**Table 22.3  Change of Growth Rates**

<table>
<thead>
<tr>
<th>Function</th>
<th>Name</th>
<th>( n = 25 )</th>
<th>( n = 50 )</th>
<th>( f(50)/f(25) )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( O(1) )</td>
<td>Constant time</td>
<td>1</td>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>( O(\log n) )</td>
<td>Logarithmic time</td>
<td>4.64</td>
<td>5.64</td>
<td>1.21</td>
</tr>
<tr>
<td>( O(n) )</td>
<td>Linear time</td>
<td>25</td>
<td>50</td>
<td>2</td>
</tr>
<tr>
<td>( O(n \log n) )</td>
<td>Log-linear time</td>
<td>116</td>
<td>282</td>
<td>2.43</td>
</tr>
<tr>
<td>( O(n^2) )</td>
<td>Quadratic time</td>
<td>625</td>
<td>2,500</td>
<td>4</td>
</tr>
<tr>
<td>( O(n^3) )</td>
<td>Cubic time</td>
<td>15,625</td>
<td>125,000</td>
<td>8</td>
</tr>
<tr>
<td>( O(2^n) )</td>
<td>Exponential time</td>
<td>(3.36 \times 10^7)</td>
<td>(1.27 \times 10^{15})</td>
<td>(3.35 \times 10^7)</td>
</tr>
</tbody>
</table>

**Figure 22.1**  As the size \( n \) increases, the function grows.

22.8 Put the following growth functions in order:

\[
\frac{5n^3}{4032}, 44 \log n, 10n \log n, 500, 2n^2, \frac{2n}{45}, 3n
\]

22.9 Estimate the time complexity for adding two \( n \times m \) matrices, and for multiplying an \( n \times m \) matrix by an \( m \times k \) matrix.

22.10 Describe an algorithm for finding the occurrence of the max element in an array. Analyze the complexity of the algorithm.

22.11 Describe an algorithm for removing duplicates from an array. Analyze the complexity of the algorithm.

22.12 Analyze the following sorting algorithm:

```java
for (int i = 0; i < list.length - 1; i++) {
    if (list[i] > list[i + 1]) {
        swap list[i] with list[i + 1];
        i = -1;
    }
}
```

22.13 Analyze the complexity for computing a polynomial \( f(x) \) of degree \( n \) for a given \( x \) value using a brute-force approach and the Horner’s approach, respectively. A brute-force approach is to compute each term in the polynomial and add them together. The Horner’s approach was introduced in Section 6.7.

\[ f(x) = a_n x^n + a_{n-1} x^{n-1} + a_{n-2} x^{n-2} + \ldots + a_1 x^1 + a_0 \]
22.5 Finding Fibonacci Numbers Using Dynamic Programming

This section analyzes and designs an efficient algorithm for finding Fibonacci numbers using dynamic programming.

Section 18.3, Case Study: Computing Fibonacci Numbers, gave a recursive method for finding the Fibonacci number, as follows:

```java
/** The method for finding the Fibonacci number */
public static long fib(long index) {
    if (index == 0) // Base case
        return 0;
    else if (index == 1) // Base case
        return 1;
    else // Reduction and recursive calls
        return fib(index - 1) + fib(index - 2);
}
```

We can now prove that the complexity of this algorithm is \(O(2^n)\). For convenience, let the index be \(n\). Let \(T(n)\) denote the complexity for the algorithm that finds \(fib(n)\) and \(c\) denote the constant time for comparing the index with 0 and 1; that is, \(T(1)\) and \(T(0)\) are \(c\). Thus,

\[
T(n) = T(n-1) + T(n-2) + c \\
\leq 2T(n-1) + c \\
\leq 2(2T(n-2) + c) + c \\
= 2^2T(n-2) + 2c + c
\]

Similar to the analysis of the Tower of Hanoi problem, we can show that \(T(n)\) is \(O(2^n)\).

However, this algorithm is not efficient. Is there an efficient algorithm for finding a Fibonacci number? The trouble with the recursive \(fib\) method is that the method is invoked redundantly with the same arguments. For example, to compute \(fib(4)\), \(fib(3)\) and \(fib(2)\) are invoked. To compute \(fib(3)\), \(fib(2)\) and \(fib(1)\) are invoked. Note that \(fib(2)\) is redundantly invoked. We can improve it by avoiding repeatedly calling of the \(fib\) method with the same argument. Note that a new Fibonacci number is obtained by adding the preceding two numbers in the sequence. If you use the two variables \(f_0\) and \(f_1\) to store the two preceding numbers, the new number, \(f_2\), can be immediately obtained by adding \(f_0\) with \(f_1\). Now you should update \(f_0\) and \(f_1\) by assigning \(f_1\) to \(f_0\) and assigning \(f_2\) to \(f_1\), as shown in Figure 22.2.

![Figure 22.2](image-url)

**Figure 22.2** Variables \(f_0\), \(f_1\), and \(f_2\) store three consecutive Fibonacci numbers in the series.
The new method is implemented in Listing 22.2.

**LISTING 22.2  ImprovedFibonacci.java**

```java
import java.util.Scanner;

public class ImprovedFibonacci {
    public static void main(String args[]) {
        // Create a Scanner
        Scanner input = new Scanner(System.in);
        System.out.print("Enter an index for the Fibonacci number: ");
        int index = input.nextInt();
        // Find and display the Fibonacci number
        System.out.println("Fibonacci number at index "+ index + " is "+ fib(index));
    }

    /** The method for finding the Fibonacci number */
    public static long fib(long n) {
        long f0 = 0; // For fib(0)
        long f1 = 1; // For fib(1)
        long f2 = 1; // For fib(2)
        if (n == 0)
            return f0;
        else if (n == 1)
            return f1;
        else if (n == 2)
            return f2;
        for (int i = 3; i <= n; i++) {
            f0 = f1;
            f1 = f2;
            f2 = f0 + f1;
        }
        return f2;
    }
}
```

Enter an index for the Fibonacci number: 6
Fibonacci number at index 6 is 8

Enter an index for the Fibonacci number: 7
Fibonacci number at index 7 is 13

Obviously, the complexity of this new algorithm is \(O(n)\). This is a tremendous improvement over the recursive \(O(2^n)\) algorithm.

The algorithm for computing Fibonacci numbers presented here uses an approach known as dynamic programming. Dynamic programming is the process of solving subproblems, then combining the solutions of the subproblems to obtain an overall solution. This naturally leads to a recursive solution. However, it would be inefficient to use recursion, because the
22.14 What is dynamic programming? Give an example of dynamic programming.
22.15 Why is the recursive Fibonacci algorithm inefficient, but the nonrecursive Fibonacci algorithm efficient?

22.6 Finding Greatest Common Divisors Using Euclid’s Algorithm

This section presents several algorithms in the search for an efficient algorithm for finding the greatest common divisor of two integers.

The greatest common divisor (GCD) of two integers is the largest number that can evenly divide both integers. Listing 5.9, GreatestCommonDivisor.java, presented a brute-force algorithm for finding the greatest common divisor of two integers \( m \) and \( n \). Brute force refers to an algorithmic approach that solves a problem in the simplest or most direct or obvious way. As a result, such an algorithm can end up doing far more work to solve a given problem than a cleverer or more sophisticated algorithm might do. On the other hand, a brute-force algorithm is often easier to implement than a more sophisticated one and, because of this simplicity, sometimes it can be more efficient.

The brute-force algorithm checks whether \( k \) (for \( k = 2, 3, 4 \), and so on) is a common divisor for \( n_1 \) and \( n_2 \), until \( k \) is greater than \( n_1 \) or \( n_2 \). The algorithm can be described as follows:

```java
public static int gcd(int m, int n) {
    int gcd = 1;
    for (int k = 2; k <= m && k <= n; k++) {
        if (m % k == 0 && n % k == 0) {
            gcd = k;
        }
    }
    return gcd;
}
```

Assuming \( m \geq n \), the complexity of this algorithm is obviously \( O(n) \).

Is there a better algorithm for finding the GCD? Rather than searching a possible divisor from 1 up, it is more efficient to search from \( n \) down. Once a divisor is found, the divisor is the GCD. Therefore, you can improve the algorithm using the following loop:

```java
for (int k = n; k >= 1; k--) {
    if (m % k == 0 && n % k == 0) {
        gcd = k;
        break;
    }
}
```

This algorithm is better than the preceding one, but its worst-case time complexity is still \( O(n) \).

A divisor for a number \( n \) cannot be greater than \( n / 2 \), so you can further improve the algorithm using the following loop:

```java
for (int k = m / 2; k >= 1; k--) {
    if (m % k == 0 && n % k == 0) {
        gcd = k;
    }
}
```
However, this algorithm is incorrect, because $n$ can be a divisor for $m$. This case must be considered. The correct algorithm is shown in Listing 22.3.

**Listing 22.3 GCD.java**

```java
import java.util.Scanner;

public class GCD {
    /** Find GCD for integers $m$ and $n$ */
    public static int gcd(int $m$, int $n$) {
        int gcd = 1;
        if ($m$ % $n$ == 0) return $n$;
        for (int $k$ = $n$ / 2; $k$ >= 1; $k$--) {
            if ($m$ % $k$ == 0 && $n$ % $k$ == 0) {
                gcd = $k$;
                break;
            }
        }
        return gcd;
    }
}
```

```
import java.util.Scanner;

public class GCD {
    /** Find GCD for integers $m$ and $n$ */
    public static int gcd(int $m$, int $n$) {
        int gcd = 1;
        if ($m$ % $n$ == 0) return $n$;
        for (int $k$ = $n$ / 2; $k$ >= 1; $k$--) {
            if ($m$ % $k$ == 0 && $n$ % $k$ == 0) {
                gcd = $k$;
                break;
            }
        }
        return gcd;
    }
}
```

Enter first integer: 2525
Enter second integer: 125
The greatest common divisor for 2525 and 125 is 25

Enter first integer: 3
Enter second integer: 3
The greatest common divisor for 3 and 3 is 3

Assuming $m \geq n$, the for loop is executed at most $n/2$ times, which cuts the time by half from the previous algorithm. The time complexity of this algorithm is still $O(n)$, but practically, it is much faster than the algorithm in Listing 5.9.
22.6 Finding Greatest Common Divisors Using Euclid’s Algorithm

Note

The Big O notation provides a good theoretical estimate of algorithm efficiency. However, two algorithms of the same time complexity are not necessarily equally efficient. As shown in the preceding example, both algorithms in Listings 5.9 and 22.3 have the same complexity, but in practice the one in Listing 22.3 is obviously better.

A more efficient algorithm for finding the GCD was discovered by Euclid around 300 B.C. This is one of the oldest known algorithms. It can be defined recursively as follows:

Let $gcd(m, n)$ denote the GCD for integers $m$ and $n$:

- If $m \% n = 0$, $gcd(m, n)$ is $n$.
- Otherwise, $gcd(m, n)$ is $gcd(n, m \% n)$.

It is not difficult to prove the correctness of this algorithm. Suppose $m \% n = r$. Thus, $m = qn + r$, where $q$ is the quotient of $m / n$. Any number that is divisible by $m$ and $n$ must also be divisible by $r$. Therefore, $gcd(m, n)$ is the same as $gcd(n, r)$, where $r = m \% n$. The algorithm can be implemented as in Listing 22.4.

**Listing 22.4** GCDEuclid.java

```java
import java.util.Scanner;

public class GCDEuclid {
    public static int gcd(int m, int n) {
        if (m % n == 0) return n; // base case
        else return gcd(n, m % n); // reduction
    }

    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        // Create a Scanner
        // Prompt the user to enter two integers
        System.out.println("Enter first integer: ");
        int m = input.nextInt(); // input
        System.out.println("Enter second integer: ");
        int n = input.nextInt(); // input
        System.out.println("The greatest common divisor for "+ m + " and "+ n + " is " + gcd(m, n));
    }
}
```

Enter first integer: 2525
Enter second integer: 125
The greatest common divisor for 2525 and 125 is 25

Enter first integer: 3
Enter second integer: 3
The greatest common divisor for 3 and 3 is 3
In the best case when $m \% n = 0$, the algorithm takes just one step to find the GCD. It is difficult to analyze the average case. However, we can prove that the worst-case time complexity is $O(\log n)$.

Assuming $m \geq n$, we can show that $m \% n < m / 2$, as follows:

- If $n \leq m / 2$, $m \% n < m / 2$, since the remainder of $m$ divided by $n$ is always less than $n$.
- If $n > m / 2$, $m \% n = m - n < m / 2$. Therefore, $m \% n < m / 2$.

Euclid’s algorithm recursively invokes the $\text{gcd}$ method. It first calls $\text{gcd}(m, n)$, then calls $\text{gcd}(n, m \% n)$, and $\text{gcd}(m \% n, n % (m \% n))$, and so on, as follows:

\[
\text{gcd}(m, n) \\
= \text{gcd}(n, m \% n) \\
= \text{gcd}(m \% n, n % (m \% n)) \\
= \ldots
\]

Since $m \% n < m / 2$ and $n \% (m \% n) < n / 2$, the argument passed to the $\text{gcd}$ method is reduced by half after every two iterations. After invoking $\text{gcd}$ two times, the second parameter is less than $n/2$. After invoking $\text{gcd}$ four times, the second parameter is less than $n/4$. After invoking $\text{gcd}$ six times, the second parameter is less than $n/8$. Let $k$ be the number of times the $\text{gcd}$ method is invoked. After invoking $\text{gcd}$ $k$ times, the second parameter is less than $\frac{n}{2^{(k/2)}}$, which is greater than or equal to 1. That is,

\[
\frac{n}{2^{(k/2)}} \geq 1 \Rightarrow n \geq 2^{(k/2)} \Rightarrow \log n \geq k/2 \Rightarrow k \leq 2 \log n
\]

Therefore, $k \leq 2 \log n$. So the time complexity of the $\text{gcd}$ method is $O(\log n)$.

The worst case occurs when the two numbers result in the most divisions. It turns out that two successive Fibonacci numbers will result in the most divisions. Recall that the Fibonacci series begins with 0 and 1, and each subsequent number is the sum of the preceding two numbers in the series, such as:

\[
0 1 1 2 3 5 8 13 21 34 55 89 \ldots
\]

The series can be recursively defined as

\[
\text{fib}(0) = 0; \\
\text{fib}(1) = 1; \\
\text{fib}(\text{index}) = \text{fib}(\text{index} - 2) + \text{fib}(\text{index} - 1); \text{index} \geq 2
\]

For two successive Fibonacci numbers $\text{fib(\text{index})}$ and $\text{fib(\text{index} - 1)}$,

\[
\text{gcd}(\text{fib(\text{index})}, \text{fib(\text{index} - 1)}) \\
= \text{gcd}(\text{fib(\text{index} - 1)}, \text{fib(\text{index} - 2))} \\
= \text{gcd}(\text{fib(\text{index} - 2)}, \text{fib(\text{index} - 3))} \\
= \text{gcd}(\text{fib(\text{index} - 3)}, \text{fib(\text{index} - 4))} \\
= \ldots \\
= \text{gcd}(2, 1) \\
= 1
\]

For example,

\[
\text{gcd}(21, 13) \\
= \text{gcd}(13, 8) \\
= \text{gcd}(8, 5) \\
= \text{gcd}(5, 3)
\]
22.7 Efficient Algorithms for Finding Prime Numbers

The number of times the \texttt{gcd} method is invoked is the same as the index. We can prove that \( \text{index} \leq 1.44 \log n \), where \( n = \text{fib(index} - 1) \). This is a tighter bound than \( \text{index} \leq 2 \log n \).

Table 22.4 summarizes the complexity of three algorithms for finding the GCD.

\textbf{Table 22.4} Comparisons of GCD Algorithms

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Complexity</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Listing 5.9</td>
<td>( O(n) )</td>
<td>Brute-force, checking all possible divisors</td>
</tr>
<tr>
<td>Listing 22.3</td>
<td>( O(n) )</td>
<td>Checking half of all possible divisors</td>
</tr>
<tr>
<td>Listing 22.4</td>
<td>( O(\log n) )</td>
<td>Euclid’s algorithm</td>
</tr>
</tbody>
</table>

\(22.16\) Prove that the following algorithm for finding the GCD of the two integers \( m \) and \( n \) is incorrect.

\begin{verbatim}
int gcd = 1;
for (int k = Math.min(Math.sqrt(n), Math.sqrt(m)); k >= 1; k--) {
    if (m % k == 0 && n % k == 0) {
        gcd = k;
        break;
    }
}
\end{verbatim}

\(22.7\) Efficient Algorithms for Finding Prime Numbers

This section presents several algorithms in the search for an efficient algorithm for finding prime numbers.

A $150,000 award awaits the first individual or group who discovers a prime number with at least 100,000,000 decimal digits (w2.eff.org/awards/coop-prime-rules.php).

Can you design a fast algorithm for finding prime numbers?

An integer greater than \( 1 \) is prime if its only positive divisor is \( 1 \) or itself. For example, \( 2, 3, 5, \) and \( 7 \) are prime numbers, but \( 4, 6, 8, \) and \( 9 \) are not.

How do you determine whether a number \( n \) is prime? Listing 5.15 presented a brute-force algorithm for finding prime numbers. The algorithm checks whether \( 2, 3, 4, 5, \ldots, \) or \( n - 1 \) is divisible by \( n \). If not, \( n \) is prime. This algorithm takes \( O(n) \) time to check whether \( n \) is prime. Note that you need to check only whether \( 2, 3, 4, 5, \ldots, \) and \( n/2 \) is divisible by \( n \). If not, \( n \) is prime. This algorithm is slightly improved, but it is still of \( O(n) \).

In fact, we can prove that if \( n \) is not a prime, \( n \) must have a factor that is greater than \( 1 \) and less than or equal to \( \sqrt{n} \). Here is the proof. Since \( n \) is not a prime, there exist two numbers \( p \) and \( q \) such that \( n = pq \) with \( 1 < p \leq q \). Note that \( n = \sqrt{n} \sqrt{n} \). \( p \) must be less than or equal to \( \sqrt{n} \). Hence, you need to check only whether \( 2, 3, 4, 5, \ldots, \) or \( \sqrt{n} \) is divisible by \( n \). If not, \( n \) is prime. This significantly reduces the time complexity of the algorithm to \( O(\sqrt{n}) \).

Now consider the algorithm for finding all the prime numbers up to \( n \). A straightforward implementation is to check whether \( i \) is prime for \( i = 2, 3, 4, \ldots, n \). The program is given in Listing 22.5.
LISTING 22.5  PrimeNumbers.java

1  import java.util.Scanner;
2  
3  public class PrimeNumbers {
4      public static void main(String[] args) {
5          Scanner input = new Scanner(System.in);
6          System.out.print("Find all prime numbers <= n, enter n: ");
7          int n = input.nextInt();
8          
9          final int NUMBER_PER_LINE = 10; // Display 10 per line
10          int count = 0; // Count the number of prime numbers
11          int number = 2; // A number to be tested for primeness
12          
13          System.out.println("The prime numbers are: ");
14          
15          // Repeatedly find prime numbers
16          while (number <= n) {
17              // Assume the number is prime
18              boolean isPrime = true; // Is the current number prime?
19              
20              // Test if number is prime
21              for (int divisor = 2; divisor <= (int)(Math.sqrt(number)); divisor++) {
22                  if (number % divisor == 0) { // If true, number is not prime
23                      isPrime = false; // Set isPrime to false
24                      break; // Exit the for loop
25                  }
26              }
27              
28              // Print the prime number and increase the count
29              if (isPrime) {
30                  count++; // Increase the count
31                  
32                  if (count % NUMBER_PER_LINE == 0) {
33                      // Print the number and advance to the new line
34                      System.out.printf("%7d
", number);
35                  }
36                  else
37                      System.out.printf("%7d", number);
38              }
39          }
40          
41          // Check if the next number is prime
42          number++;
43          
44          System.out.println("\n" + count + " prime(s) less than or equal to " + n);
45      }
46  }
47  
48  

The program is not efficient if you have to compute `Math.sqrt(number)` for every iteration of the `for` loop (line 21). A good compiler should evaluate `Math.sqrt(number)` only once for the entire `for` loop. To ensure this happens, you can explicitly replace line 21 with the following two lines:

```java
int squareRoot = (int)(Math.sqrt(number));
for (int divisor = 2; divisor <= squareRoot; divisor++) {
```

In fact, there is no need to actually compute `Math.sqrt(number)` for every `number`. You need look only for the perfect squares such as 4, 9, 16, 25, 36, 49, and so on. Note that for all the numbers between 36 and 48, inclusively, their `(int)(Math.sqrt(number))` is 6. With this insight, you can replace the code in lines 16–26 with the following:

```java
int squareRoot = 1;
// Repeatedly find prime numbers
while (number <= n) {
    // Assume the number is prime
    boolean isPrime = true; // Is the current number prime?
    if (squareRoot * squareRoot < number) squareRoot++;
    // Test if number is prime
    for (int divisor = 2; divisor <= squareRoot; divisor++) {
        if (number % divisor == 0) { // If true, number is not prime
            isPrime = false; // Set isPrime to false
            break; // Exit the for loop
        }
    }
    ...
```

Now we turn our attention to analyzing the complexity of this program. Since it takes $\sqrt{i}$ steps in the `for` loop (lines 21–27) to check whether number $i$ is prime, the algorithm takes $\sqrt{2} + \sqrt{3} + \sqrt{4} + \ldots + \sqrt{n}$ steps to find all the prime numbers less than or equal to $n$. Observe that

$$\sqrt{2} + \sqrt{3} + \sqrt{4} + \ldots + \sqrt{n} \leq n\sqrt{n}$$

Therefore, the time complexity for this algorithm is $O(n\sqrt{n})$.

To determine whether $i$ is prime, the algorithm checks whether 2, 3, 4, 5, ..., and $\sqrt{i}$ are divisible by $i$. This algorithm can be further improved. In fact, you need to check only whether the prime numbers from 2 to $\sqrt{i}$ are possible divisors for $i$.

We can prove that if $i$ is not prime, there must exist a prime number $p$ such that $i = pq$ and $p \leq q$. Here is the proof. Assume that $i$ is not prime; let $p$ be the smallest factor of $i$. $p$ must be prime, otherwise, $p$ has a factor $k$ with $2 \leq k < p$. $k$ is also a factor of $i$, which contradicts that $p$ be the smallest factor of $i$. Therefore, if $i$ is not prime, you can find a prime number from 2 to $\sqrt{i}$ that is divisible by $i$. This leads to a more efficient algorithm for finding all prime numbers up to $n$, as shown in Listing 22.6.

**LISTING 22.6 EfficientPrimeNumbers.java**

```java
import java.util.Scanner;

public class EfficientPrimeNumbers {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        System.out.print("Find all prime numbers <= n, enter n: ");
```
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```java
int n = input.nextInt();

// A list to hold prime numbers
java.util.List<Integer> list =
    new java.util.ArrayList<>();

final int NUMBER_PER_LINE = 10; // Display 10 per line
int count = 0; // Count the number of prime numbers
int number = 2; // A number to be tested for primeness
int squareRoot = 1; // Check whether number <= squareRoot

System.out.println("The prime numbers are \\
    ");

// Repeatedly find prime numbers
while (number <= n) {
    // Assume the number is prime
    boolean isPrime = true; // Is the current number prime?
    
    if (squareRoot * squareRoot < number) squareRoot++;
    
    // Test whether number is prime
    for (int k = 0; k < list.size() && list.get(k) <= squareRoot; k++) {
        if (number % list.get(k) == 0) { // If true, not prime
            isPrime = false; // Set isPrime to false
            break; // Exit the for loop
        }
    }
    
    // Print the prime number and increase the count
    if (isPrime) {
        count++; // Increase the count
        list.add(number); // Add a new prime to the list
        if (count % NUMBER_PER_LINE == 0) {
            System.out.println(number);
        } else
            System.out.print(number + " ");
    }

    // Check whether the next number is prime
    number++;
}

System.out.println("\n" + count + 
    " prime(s) less than or equal to " + n);
```

Find all prime numbers <= n, enter n: 1000
The prime numbers are:

```
  2   3   5   7  11  13  17  19  23  29
  31  37  41  43  47  53  59  61  67  71
  ... ...
168 prime(s) less than or equal to 1000
```
Let \( \pi(i) \) denote the number of prime numbers less than or equal to \( i \). The primes under 20 are 2, 3, 5, 7, 11, 13, 17, and 19. Therefore, \( \pi(2) \) is 1, \( \pi(3) \) is 2, \( \pi(6) \) is 3, and \( \pi(20) \) is 8.

It has been proved that \( \pi(i) \) is approximately \( \frac{i}{ \log i} \) (see primes.utm.edu/howmany.shtml).

For each number \( i \), the algorithm checks whether a prime number less than or equal to \( 2i \) is divisible by \( i \). The number of the prime numbers less than or equal to \( 2i \) is

\[
\frac{\sqrt{i}}{ \log \sqrt{i}} = 2\sqrt{i} \log \frac{\sqrt{i}}{ \log i}
\]

Thus, the complexity for finding all prime numbers up to \( n \) is

\[
\frac{2\sqrt{2}}{ \log 2} + \frac{2\sqrt{3}}{ \log 3} + \frac{2\sqrt{4}}{ \log 4} + \frac{2\sqrt{5}}{ \log 5} + \frac{2\sqrt{6}}{ \log 6} + \frac{2\sqrt{7}}{ \log 7} + \frac{2\sqrt{8}}{ \log 8} + \ldots + \frac{2\sqrt{n}}{ \log n}
\]

Since \( \frac{\sqrt{i}}{ \log i} < \frac{\sqrt{n}}{ \log n} \) for \( i < n \) and \( n \geq 16 \),

\[
\frac{2\sqrt{2}}{ \log 2} + \frac{2\sqrt{3}}{ \log 3} + \frac{2\sqrt{4}}{ \log 4} + \frac{2\sqrt{5}}{ \log 5} + \frac{2\sqrt{6}}{ \log 6} + \frac{2\sqrt{7}}{ \log 7} + \frac{2\sqrt{8}}{ \log 8} + \ldots + \frac{2\sqrt{n}}{ \log n} < \frac{2n\sqrt{n}}{ \log n}
\]

Therefore, the complexity of this algorithm is \( O\left(\frac{n\sqrt{n}}{ \log n}\right) \).

This algorithm is another example of dynamic programming. The algorithm stores the results of the subproblems in the array list and uses them later to check whether a new number is prime.

Is there any algorithm better than \( O\left(\frac{n\sqrt{n}}{ \log n}\right) \)? Let us examine the well-known Eratosthenes algorithm for finding prime numbers. Eratosthenes (276–194 B.C.) was a Greek mathematician who devised a clever algorithm, known as the Sieve of Eratosthenes, for finding all prime numbers \( \leq n \). His algorithm is to use an array named \( \text{primes} \) of \( n \) Boolean values. Initially, all elements in \( \text{primes} \) are set \( \text{true} \). Since the multiples of 2 are not prime, set \( \text{primes}[2 \times i] \) to \( \text{false} \) for all \( 2 \leq i \leq n/2 \), as shown in Figure 22.3. Since we don’t care about \( \text{primes}[0] \) and \( \text{primes}[1] \), these values are marked \( \times \) in the figure.

Since the multiples of 3 are not prime, set \( \text{primes}[3 \times i] \) to \( \text{false} \) for all \( 3 \leq i \leq n/3 \). Because the multiples of 5 are not prime, set \( \text{primes}[5 \times i] \) to \( \text{false} \) for all \( 5 \leq i \leq n/5 \). Note that you don’t need to consider the multiples of 4, because the multiples of 4 are also the multiples of 2, which have already been considered. Similarly, multiples of 6, 8, and 9 need not be considered. You only need to consider the multiples of a prime number \( k = 2, 3, 5, 7, 11, \ldots \), and set the corresponding element in \( \text{primes} \) to \( \text{false} \). Afterward, if \( \text{primes}[i] \) is
still true, then \( i \) is a prime number. As shown in Figure 22.3, \( 2, 3, 5, 7, 11, 13, 17, 19, \) and \( 23 \) are prime numbers. Listing 22.7 gives the program for finding the prime numbers using the Sieve of Eratosthenes algorithm.

**LISTING 22.7 SieveOfEratosthenes.java**

```java
import java.util.Scanner;

public class SieveOfEratosthenes {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        System.out.print("Find all prime numbers \( \leq n \), enter \( n \): ");
        int n = input.nextInt();

        boolean[] primes = new boolean[n + 1]; // Prime number sieve

        // Initialize primes[i] to true
        for (int i = 0; i < primes.length; i++) {
            primes[i] = true;
        }

        // Nonprime
        for (int k = 2; k <= n / k; k++) {
            if (primes[k]) {
                for (int i = k; i <= n / k; i++) {
                    primes[k * i] = false; // k * i is not prime
                }
            }
        }

        int count = 0; // Count the number of prime numbers found so far

        // Print prime numbers
        for (int i = 2; i < primes.length; i++) {
            if (primes[i]) {
                count++;
                if (count % 10 == 0)
                    System.out.printf("%7d\n", i);
                else
                    System.out.printf("%7d", i);
            }
        }

        System.out.println("\n" + count + " prime(s) less than or equal to " + n);
    }
}
```

Find all prime numbers \( \leq n \), enter \( n \): 1000 Enter
The prime numbers are:

<table>
<thead>
<tr>
<th>2</th>
<th>3</th>
<th>5</th>
<th>7</th>
<th>11</th>
<th>13</th>
<th>17</th>
<th>19</th>
<th>23</th>
<th>29</th>
</tr>
</thead>
<tbody>
<tr>
<td>31</td>
<td>37</td>
<td>41</td>
<td>43</td>
<td>47</td>
<td>53</td>
<td>59</td>
<td>61</td>
<td>67</td>
<td>71</td>
</tr>
</tbody>
</table>

... ...
168 prime(s) less than or equal to 1000

Note that \( k \leq n / k \) (line 16). Otherwise, \( k * i \) would be greater than \( n \) (line 19). What is the time complexity of this algorithm?
This upper bound $O\left(\frac{n\sqrt{n}}{\log n}\right)$ is very loose. The actual time complexity is much better than $O\left(\frac{n\sqrt{n}}{\log n}\right)$. The Sieve of Eratosthenes algorithm is good for a small $n$ such that the array $\text{primes}$ can fit in the memory.

Table 22.5 summarizes the complexity of these three algorithms for finding all prime numbers up to $n$.

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Complexity</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Listing 5.15</td>
<td>$O(n^2)$</td>
<td>Brute-force, checking all possible divisors</td>
</tr>
<tr>
<td>Listing 22.5</td>
<td>$O(n\sqrt{n})$</td>
<td>Checking divisors up to $\sqrt{n}$</td>
</tr>
<tr>
<td>Listing 22.6</td>
<td>$O\left(\frac{n\sqrt{n}}{\log n}\right)$</td>
<td>Checking prime divisors up to $\sqrt{n}$</td>
</tr>
<tr>
<td>Listing 22.7</td>
<td>$O\left(\frac{n\sqrt{n}}{\log n}\right)$</td>
<td>Sieve of Eratosthenes</td>
</tr>
</tbody>
</table>

22.17 Prove that if $n$ is not prime, there must exist a prime number $p$ such that $p \leq \sqrt{n}$ and $p$ is a factor of $n$.

22.18 Describe how the sieve of Eratosthenes is used to find the prime numbers.

22.8 Finding the Closest Pair of Points Using Divide-and-Conquer

This section presents efficient algorithms for finding the closest pair of points using divide-and-conquer.

Given a set of points, the closest-pair problem is to find the two points that are nearest to each other. As shown in Figure 22.4, a line is drawn to connect the two nearest points in the closest-pair animation.

Section 8.6, Case Study: Finding the Closest Pair, presented a brute-force algorithm for finding the closest pair of points. The algorithm computes the distances between all pairs of points and finds the one with the minimum distance. Clearly, the algorithm takes $O(n^2)$ time.

Can we design a more efficient algorithm?
We will use an approach called divide-and-conquer to solve this problem. The approach divides the problem into subproblems, solves the subproblems, then combines the solutions of the subproblems to obtain the solution for the entire problem. Unlike the dynamic programming approach, the subproblems in the divide-and-conquer approach don’t overlap. A subproblem is like the original problem with a smaller size, so you can apply recursion to solve the problem. In fact, all the solutions for recursive problems follow the divide-and-conquer approach.

Listing 22.8 describes how to solve the closest pair problem using the divide-and-conquer approach.

**Listing 22.8 Algorithm for Finding the Closest Pair**

Step 1: Sort the points in increasing order of $x$-coordinates. For the points with the same $x$-coordinates, sort on $y$-coordinates. This results in a sorted list $S$ of points.

Step 2: Divide $S$ into two subsets, $S_1$ and $S_2$, of equal size using the midpoint in the sorted list. Let the midpoint be in $S_1$. Recursively find the closest pair in $S_1$ and $S_2$. Let $d_1$ and $d_2$ denote the distance of the closest pairs in the two subsets, respectively.

Step 3: Find the closest pair between a point in $S_1$ and a point in $S_2$ and denote their distance as $d_3$. The closest pair is the one with the distance $\min(d_1, d_2, d_3)$.

Selection sort takes $O(n^2)$ time. In Chapter 23 we will introduce merge sort and heap sort. These sorting algorithms take $O(n \log n)$ time. Step 1 can be done in $O(n \log n)$ time.

Step 3 can be done in $O(n)$ time. Let $d = \min(d_1, d_2)$. We already know that the closest-pair distance cannot be larger than $d$. For a point in $S_1$ and a point in $S_2$ to form the closest pair in $S$, the left point must be in stripL and the right point in stripR, as illustrated in Figure 22.5a.

For a point $p$ in stripL, you need only consider a right point within the $d \times 2d$ rectangle, as shown in 22.5b. Any right point outside the rectangle cannot form the closest pair with $p$. Since the closest-pair distance in $S_2$ is greater than or equal to $d$, there can be at most six points in the rectangle. Thus, for each point in stripL, at most six points in stripR need to be considered.

For each point $p$ in stripL, how do you locate the points in the corresponding $d \times 2d$ rectangle area in stripR? This can be done efficiently if the points in stripL and stripR are sorted in increasing order of their $y$-coordinates. Let pointsOrderedOnY be the list of the points sorted in increasing order of $y$-coordinates. pointsOrderedOnY can be obtained beforehand in the algorithm. stripL and stripR can be obtained from pointsOrderedOnY in Step 3 as shown in Listing 22.9.
Finding the Closest Pair of Points Using Divide-and-Conquer

**LISTING 22.9** Algorithm for Obtaining stripL and stripR

```plaintext
1 for each point p in pointsOrderedOnY
2   if (p is in S1 and mid.x - p.x <= d)
3      append p to stripL;
4   else if (p is in S2 and p.x - mid.x <= d)
5      append p to stripR;
```

Let the points in stripL and stripR be \{p_0, p_1, ..., p_k\} and \{q_0, q_1, ..., q_l\}, as shown in Figure 22.5c. The closest pair between a point in stripL and a point in stripR can be found using the algorithm described in Listing 22.10.

**LISTING 22.10** Algorithm for Finding the Closest Pair in Step 3

```plaintext
1 d = min(d_1, d_2);
2 r = 0; // r is the index of a point in stripR
3 for (each point p in stripL) {
4   // Skip the points in stripR below p.y - d
5   while (r < stripR.length && q[r].y <= p.y - d)
6      r++;
7  }
8 let r1 = r;
9 while (r1 < stripR.length && |q[r1].y - p.y| <= d) {
10   // Check if (p, q[r1]) is a possible closest pair
11   if (distance(p, q[r1]) < d) {
12      d = distance(p, q[r1]);
13      (p, q[r1]) is now the current closest pair;
14   }
15  r1 = r1 + 1;
16 }
```

The points in stripL are considered from p_0, p_1, ..., p_k in this order. For a point p in stripL, skip the points in stripR that are below p.y - d (lines 5–6). Once a point is skipped, it will no longer be considered. The while loop (lines 9–17) checks whether (p, q[r1]) is a possible closest pair. There are at most six such q[r1] pairs, because the distance between two points in stripR cannot be less than d. So the complexity for finding the closest pair in Step 3 is \(O(n)\).
Note that Step 1 in Listing 22.8 is performed only once to presort the points. Assume that all the points are presorted. Let $T(n)$ denote the time complexity for this algorithm. Thus,

\[
T(n) = 2T(n/2) + O(n) = O(n \log n)
\]

Therefore, the closest pair of points can be found in $O(n \log n)$ time. The complete implementation of this algorithm is left as an exercise (see Programming Exercise 22.7).

22.19 What is the divide-and-conquer approach? Give an example.

22.20 What is the difference between divide-and-conquer and dynamic programming?

22.21 Can you design an algorithm for finding the minimum element in a list using divide-and-conquer? What is the complexity of this algorithm?

22.9 Solving the Eight Queens Problem Using Backtracking

This section solves the Eight Queens problem using the backtracking approach.

The Eight Queens problem is to find a solution to place a queen in each row on a chessboard such that no two queens can attack each other. The problem can be solved using recursion (See Programming Exercise 18.34). In this section, we will introduce a common algorithm design technique called backtracking for solving this problem. The backtracking approach searches for a candidate solution incrementally, abandoning that option as soon as it determines that the candidate cannot possibly be a valid solution, and then looks for a new candidate.

You can use a two-dimensional array to represent a chessboard. However, since each row can have only one queen, it is sufficient to use a one-dimensional array to denote the position of the queen in the row. Thus, you can define the **queens** array as:

```java
int[] queens = new int[8];
```

Assign $j$ to $\text{queens}[i]$ to denote that a queen is placed in row $i$ and column $j$. Figure 22.6a shows the contents of the **queens** array for the chessboard in Figure 22.6b.

```
queens[0] 0
queens[1] 4
queens[2] 7
queens[3] 5
queens[4] 2
queens[5] 6
queens[6] 1
queens[7] 3
```

(a) (b)

**Figure 22.6** **queens**[$i$] denotes the position of the queen in row $i$.

The search starts from the first row with $k = 0$, where $k$ is the index of the current row being considered. The algorithm checks whether a queen can be possibly placed in the $j$th column in the row for $j = 0, 1, \ldots, 7$, in this order. The search is implemented as follows:

- If successful, it continues to search for a placement for a queen in the next row. If the current row is the last row, a solution is found.
- If not successful, it backtracks to the previous row and continues to search for a new placement in the next column in the previous row.
- If the algorithm backtracks to the first row and cannot find a new placement for a queen in this row, no solution can be found.
To see how the algorithm works, go to [www.cs.armstrong.edu/liang/animation/EightQueensAnimation.html](http://www.cs.armstrong.edu/liang/animation/EightQueensAnimation.html).

Listing 22.11 gives the program that displays a solution for the Eight Queens problem.

**LISTING 22.11 EightQueens.java**

```java
import javafx.application.Application;
import javafx.geometry.Pos;
import javafx.stage.Stage;
import javafx.scene.Scene;
import javafx.scene.control.Label;
import javafx.scene.image.Image;
import javafx.scene.image.ImageView;
import javafx.scene.layout.GridPane;

public class EightQueens extends Application {

    public static final int SIZE = 8; // The size of the chess board
    // queens are placed at (i, queens[i])
    // -1 indicates that no queen is currently placed in the ith row
    // Initially, place a queen at (0, 0) in the 0th row
    private int[] queens = {-1, -1, -1, -1, -1, -1, -1, -1};

    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        search(); // Search for a solution

        // Display chess board
        GridPane chessBoard = new GridPane();
        chessBoard.setAlignment(Pos.CENTER);
        Label[][] labels = new Label[SIZE][SIZE];
        for (int i = 0; i < SIZE; i++)
            for (int j = 0; j < SIZE; j++) {
                chessBoard.add(labels[i][j] = new Label(), j, i);
                labels[i][j].setStyle("-fx-border-color: black");
                labels[i][j].setPrefSize(55, 55);
            }

        // Display queens
        Image image = new Image("image/queen.jpg");
        for (int i = 0; i < SIZE; ++i)
            labels[i][queens[i]].setGraphic(new ImageView(image));

        // Create a scene and place it in the stage
        Scene scene = new Scene(chessBoard, 55 * SIZE, 55 * SIZE);
        primaryStage.setTitle("EightQueens"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }

    /** Search for a solution */
    private boolean search() {
        // k - 1 indicates the number of queens placed so far
        // We are looking for a position in the kth row to place a queen
        int k = 0;
        while (k >= 0 && k < SIZE) {
            // Find a position to place a queen in the kth row
            int j = findPosition(k);
            if (j < 0) {
                queens[k] = -1;
                k--; // back track to the previous row
            } else {
                // Find a column
                // Find a position to place a queen in the kth row
                // back track to the previous row
            }
        }
    }
}
```
place a queen
search the next row

```java
56       queens[k] = j;
57       k++;
58   }
59 }
60
61 if (k == -1)
62   return false; // No solution
63 else
64   return true; // A solution is found
65 }
66
67 public int findPosition(int k) {
68   int start = queens[k] + 1; // Search for a new placement
69   for (int j = start; j < SIZE; j++) {
70     if (isValid(k, j))
71       return j; // (k, j) is the place to put the queen now
72   }
73   return -1;
74 }
75
76 /** Return true if a queen can be placed at (row, column) */
77 public boolean isValid(int row, int column) {
78   for (int i = 1; i <= row; i++)
79     if (queens[row - i] == column // Check column
80         || queens[row - i] == column - i // Check upleft diagonal
81         || queens[row - i] == column + i) // Check upright diagonal
82       return false; // There is a conflict
83   return true; // No conflict
84 }
85 }
```

The program invokes `search()` (line 19) to search for a solution. Initially, no queens are placed in any rows (line 15). The search now starts from the first row with \( k = 0 \) (line 48) and finds a place for the queen (line 51). If successful, place it in the row (line 56) and consider the next row (line 57). If not successful, backtrack to the previous row (lines 53–54).

The `findPosition(k)` method searches for a possible position to place a queen in row \( k \) starting from \( \text{queen}[k] + 1 \) (line 68). It checks whether a queen can be placed at \( \text{start} \), \( \text{start} + 1 \), ..., and \( 7 \), in this order (lines 70–73). If possible, return the column index (line 72); otherwise, return \(-1\) (line 75).

The `isValid(row, column)` method is called to check whether placing a queen at the specified position causes a conflict with the queens placed earlier (line 71). It ensures that no queen is placed in the same column (line 81), in the upper-left diagonal (line 82), or in the upper-right diagonal (line 83), as shown in Figure 22.7.

![Figure 22.7](image)

**Figure 22.7** Invoking `isValid(row, column)` checks whether a queen can be placed at (row, column).
22.10 Computational Geometry: Finding a Convex Hull

*This section presents efficient geometric algorithms for finding a convex hull for a set of points.*

Computational geometry is to study the algorithms for geometrical problems. It has applications in computer graphics, games, pattern recognition, image processing, robotics, geographical information systems, and computer-aided design and manufacturing. Section 22.8 presented a geometrical algorithm for finding the closest pair of points. This section introduces geometrical algorithms for finding a convex hull.

Given a set of points, a *convex hull* is the smallest convex polygon that encloses all these points, as shown in Figure 22.8a. A polygon is convex if every line connecting two vertices is inside the polygon. For example, the vertices v0, v1, v2, v3, v4, and v5 in Figure 22.8a form a convex polygon, but not in Figure 22.8b, because the line that connects v3 and v1 is not inside the polygon.

![Convex Hull Animation](image)

**Figure 22.8** A convex hull is the smallest convex polygon that contains a set of points.

A convex hull has many applications in game programming, pattern recognition, and image processing. Before we introduce the algorithms, it is helpful to get acquainted with the concept using an interactive tool from www.cs.armstrong.edu/liang-animation/ConvexHull.html, as shown in Figure 22.8c. This tool allows you to add and remove points and displays the convex hull dynamically.

Many algorithms have been developed to find a convex hull. This section introduces two popular algorithms: the gift-wrapping algorithm and Graham’s algorithm.

### 22.10.1 Gift-Wrapping Algorithm

An intuitive approach, called the *gift-wrapping algorithm*, works as shown in Listing 22.12:

**Listing 22.12 Finding a Convex Hull Using Gift-Wrapping Algorithm**

Step 1: Given a list of points S, let the points in S be labeled s0, s1, ..., sk. Select the rightmost lowest point S. As shown in Figure 22.9a, h0 is such a point. Add h0 to list H. (H is initially empty. H will hold all points in the convex hull after the algorithm is finished.) Let t0 be h0.
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Step 2: Let \( t_1 \) be \( s_0 \).

For every point \( p \) in \( S \), if \( p \) is on the right side of the direct line from \( t_0 \) to \( t_1 \), then let \( t_1 \) be \( p \).

(After Step 2, no points lie on the right side of the direct line from \( t_0 \) to \( t_1 \), as shown in Figure 22.9b.)

Step 3: If \( t_1 \) is \( h_0 \) (see Figure 22.9d), the points in \( H \) form a convex hull for \( S \). Otherwise, add \( t_1 \) to \( H \), let \( t_0 \) be \( t_1 \), and go back to Step 2 (see Figure 22.9c).

The convex hull is expanded incrementally. The correctness is supported by the fact that no points lie on the right side of the direct line from \( t_0 \) to \( t_1 \) after Step 2. This ensures that every line segment with two points in \( S \) falls inside the polygon.

Finding the rightmost lowest point in Step 1 can be done in \( O(n) \) time. Whether a point is on the left side of a line, right side, or on the line can be determined in \( O(1) \) time (see Programming Exercise 3.32). Thus, it takes \( O(n) \) time to find a new point \( t_1 \) in Step 2. Step 2 is repeated \( h \) times, where \( h \) is the size of the convex hull. Therefore, the algorithm takes \( O(hn) \) time. In the worst-case, \( h \) is \( n \).

The implementation of this algorithm is left as an exercise (see Programming Exercise 22.9).

22.10.2 Graham’s Algorithm

A more efficient algorithm was developed by Ronald Graham in 1972, as shown in Listing 22.13.

LISTING 22.13 Finding a Convex Hull Using Graham’s Algorithm

Step 1: Given a list of points \( S \), select the rightmost lowest point and name it \( p_0 \). As shown in Figure 22.10a, \( p_0 \) is such a point.

Step 2: Sort the points in \( S \) angularly along the x-axis with \( p_0 \) as the center, as shown in Figure 22.10b. If there is a tie and two points have the same angle, discard the one that is closer to \( p_0 \). The points in \( S \) are now sorted as \( p_0, p_1, p_2, \ldots, p_{n-1} \).

Figure 22.9  (a) \( h_0 \) is the rightmost lowest point in \( S \). (b) Step 2 finds point \( t_1 \). (c) A convex hull is expanded repeatedly. (d) A convex hull is found when \( t_1 \) becomes \( h_0 \).

Figure 22.10  (a) \( p_0 \) is the rightmost lowest point in \( S \). (b) Points are sorted by their angles. (c–d) A convex hull is discovered incrementally.
Step 3: Push \( p_0 \), \( p_1 \), and \( p_2 \) into stack \( H \). (After the algorithm finishes, \( H \) contains all the points in the convex hull.)

Step 4:

\[
i = 3; \\
\text{while } (i < n) \{ \\
\text{Let } t_1 \text{ and } t_2 \text{ be the top first and second element in stack } H; \\
\text{if (} p_i \text{ is on the left side of the direct line from } t_2 \text{ to } t_1 \text{)} \{ \\
\text{Push } p_i \text{ to } H; \\
i++; \text{// Consider the next point in } S. \\
\} \\
\text{else} \\
\text{Pop the top element off stack } H. \\
\}
\]

Step 5: The points in \( H \) form a convex hull.

The convex hull is discovered incrementally. Initially, \( p_0 \), \( p_1 \), and \( p_2 \) form a convex hull. Consider \( p_3 \). \( p_3 \) is outside of the current convex hull since points are sorted in increasing order of their angles. If \( p_3 \) is strictly on the left side of the line from \( p_1 \) to \( p_2 \) (see Figure 22.10c), push \( p_3 \) into \( H \). Now \( p_0 \), \( p_1 \), and \( p_3 \) form a convex hull. If \( p_3 \) is on the right side of the line from \( p_1 \) to \( p_2 \) (see Figure 22.10d), pop \( p_2 \) out of \( H \) and push \( p_3 \) into \( H \). Now \( p_0 \), \( p_1 \), and \( p_3 \) form a convex hull and \( p_2 \) is inside of this convex hull. You can prove by induction that all the points in \( H \) in Step 5 form a convex hull for all the points in the input list \( S \).

Finding the rightmost lowest point in Step 1 can be done in \( O(n) \) time. The angles can be computed using trigonometry functions. However, you can sort the points without actually computing their angles. Observe that \( p_2 \) would make a greater angle than \( p_1 \) if and only if \( p_2 \) lies on the left side of the line from \( p_0 \) to \( p_1 \). Whether a point is on the left side of a line can be determined in \( O(1) \) time, as shown in Programming Exercise 3.32. Sorting in Step 2 can be done in \( O(n \log n) \) time using the merge-sort or heap-sort algorithms that will be introduced in Chapter 23. Step 4 can be done in \( O(n) \) time. Therefore, the algorithm takes \( O(n \log n) \) time.

The implementation of this algorithm is left as an exercise (see Programming Exercise 22.11).

22.24 What is a convex hull?

22.25 Describe the gift-wrapping algorithm for finding a convex hull. Should list \( H \) be implemented using an ArrayList or a LinkedList?

22.26 Describe Graham’s algorithm for finding a convex hull. Why does the algorithm use a stack to store the points in a convex hull?

**KEY TERMS**

- average-case analysis 822
- backtracking approach 846
- best-case input 822
- Big \( O \) notation 822
- brute force 833
- constant time 823
- convex hull 849
- divide-and-conquer approach 844
- dynamic programming approach 832
- exponential time 829
- growth rate 822
- logarithmic time 828
- quadratic time 825
- space complexity 823
- time complexity 823
- worst-case input 822

**Chapter Summary**

1. The Big \( O \) notation is a theoretical approach for analyzing the performance of an algorithm. It estimates how fast an algorithm’s execution time increases as the input size increases, which enables you to compare two algorithms by examining their growth rates.
2. An input that results in the shortest execution time is called the _best-case_ input and one that results in the longest execution time is called the _worst-case_ input. Best case and worst case are not representative, but worst-case analysis is very useful. You can be assured that the algorithm will never be slower than the worst case.

3. An _average-case analysis_ attempts to determine the average amount of time among all possible input of the same size. Average-case analysis is ideal, but difficult to perform, because for many problems it is hard to determine the relative probabilities and distributions of various input instances.

4. If the time is not related to the input size, the algorithm is said to take _constant time_ with the notation $O(1)$.

5. Linear search takes $O(n)$ time. An algorithm with the $O(n)$ time complexity is called a _linear algorithm_ and it exhibits a linear growth rate. Binary search takes $O(\log n)$ time. An algorithm with the $O(\log n)$ time complexity is called a _logarithmic algorithm_, and it exhibits a logarithmic growth rate.

6. The worst-time complexity for selection sort is $O(n^2)$. An algorithm with the $O(n^2)$ time complexity is called a _quadratic algorithm_, and it exhibits a quadratic growth rate.

7. The time complexity for the Tower of Hanoi problem is $O(2^n)$. An algorithm with the $O(2^n)$ time complexity is called an _exponential algorithm_, and it exhibits an exponential growth rate.

8. A Fibonacci number at a given index can be found in $O(n)$ time using dynamic programming.

9. Dynamic programming is the process of solving subproblems, then combining the solutions of the subproblems to obtain an overall solution. The key idea behind dynamic programming is to solve each subproblem only once and store the results for subproblems for later use to avoid redundant computing of the subproblems.

10. Euclid’s GCD algorithm takes $O(\log n)$ time.

11. All prime numbers less than or equal to $n$ can be found in $O\left(\frac{n \sqrt{n}}{\log n}\right)$ time.

12. The closest pair can be found in $O(n \log n)$ time using the _divide-and-conquer approach_.

13. The _divide-and-conquer approach_ divides the problem into subproblems, solves the subproblems, then combines the solutions of the subproblems to obtain the solution for the entire problem. Unlike the dynamic programming approach, the subproblems in the _divide-and-conquer approach_ don’t overlap. A subproblem is like the original problem with a smaller size, so you can apply recursion to solve the problem.

14. The Eight Queens problem can be solved using _backtracking_.

15. The _backtracking approach_ searches for a candidate solution incrementally, abandoning that option as soon as it determines that the candidate cannot possibly be a valid solution, and then looks for a new candidate.

16. A _convex hull_ for a set of points can be found in $O(n^3)$ time using the gift-wrapping algorithm and in $O(n \log n)$ time using the Graham’s algorithm.
**Quiz**

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/test.html.

**PROGRAMMING EXERCISES**

*22.1* *(Maximum consecutive increasingly ordered substring)* Write a program that prompts the user to enter a string and displays the maximum consecutive increasingly ordered substring. Analyze the time complexity of your program. Here is a sample run:

```
Enter a string: abcabcdgabxy
abcdg
```

```
Enter a string: abcabcdgabmnsxy
abmnsxy
```

**22.2** *(Maximum increasingly ordered subsequence)* Write a program that prompts the user to enter a string and displays the maximum increasingly ordered subsequence of characters. Analyze the time complexity of your program. Here is a sample run:

```
Enter a string: Welcome
Welo
```

*22.3* *(Pattern matching)* Write a program that prompts the user to enter two strings and tests whether the second string is a substring of the first string. *Suppose the neighboring characters in the string are distinct.* *(Don’t use the indexOf method in the String class.)* Analyze the time complexity of your algorithm. Your algorithm needs to be at least \( O(n) \) time. Here is a sample run of the program:

```
Enter a string s1: Welcome to Java
Enter a string s2: come
matched at index 3
```

*22.4* *(Pattern matching)* Write a program that prompts the user to enter two strings and tests whether the second string is a substring of the first string. *(Don’t use the indexOf method in the String class.)* Analyze the time complexity of your algorithm. Here is a sample run of the program:

```
Enter a string s1: Mississippi
Enter a string s2: sip
matched at index 6
```
**22.5** (Same-number subsequence) Write an \(O(n)\) program that prompts the user to enter a sequence of integers ending with 0 and finds the longest subsequence with the same number. Here is a sample run of the program:

```
Enter a series of numbers ending with 0:
2 4 4 8 8 8 2 4 4 0
The longest same number sequence starts at index 3 with 4 values of 8
```

**22.6** (Execution time for GCD) Write a program that obtains the execution time for finding the GCD of every two consecutive Fibonacci numbers from the index 40 to index 45 using the algorithms in Listings 22.3 and 22.4. Your program should print a table like this:

<table>
<thead>
<tr>
<th></th>
<th>40</th>
<th>41</th>
<th>42</th>
<th>43</th>
<th>44</th>
<th>45</th>
</tr>
</thead>
<tbody>
<tr>
<td>Listing 22.3 GCD</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Listing 22.4 GCDEuclid</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

*(Hint: You can use the following code template to obtain the execution time.)*

```java
long startTime = System.currentTimeMillis();
perform the task;
long endTime = System.currentTimeMillis();
long executionTime = endTime - startTime;
```

**22.7** (Closest pair of points) Section 22.8 introduced an algorithm for finding the closest pair of points using a divide-and-conquer approach. Implement the algorithm to meet the following requirements:

- Define the classes `Point` and `CompareY` in the same way as in Programming Exercise 20.4.
- Define a class named `Pair` with the data fields `p1` and `p2` to represent two points, and a method named `getDistance()` that returns the distance between the two points.
- Implement the following methods:

  ```java
  /** Return the distance of the closest pair of points */
  public static Pair getClosestPair(double[][] points)
  
  /** Return the distance of the closest pair of points */
  public static Pair getClosestPair(Point[] points)
  
  /** Return the distance of the closest pair of points
   * in pointsOrderedOnX[low..high]. This is a recursive
   * method. pointsOrderedOnX and pointsOrderedOnY are
   * not changed in the subsequent recursive calls.
   */
  public static Pair distance(Point[] pointsOrderedOnX,
                              int low, int high, Point[] pointsOrderedOnY)
  ```
/** Compute the distance between two points p1 and p2 */
public static double distance(Point p1, Point p2)

/** Compute the distance between points (x1, y1) and (x2, y2) */
public static double distance(double x1, double y1,
   double x2, double y2)

**22.8 (All prime numbers up to 10,000,000,000) Write a program that finds all prime numbers up to 10,000,000,000. There are approximately 455,052,511 such prime numbers. Your program should meet the following requirements:

- Your program should store the prime numbers in a binary data file, named PrimeNumbers.dat. When a new prime number is found, the number is appended to the file.
- To find whether a new number is prime, your program should load the prime numbers from the file to an array of the Long type of size 10000. If no number in the array is a divisor for the new number, continue to read the next 10000 prime numbers from the data file, until a divisor is found or all numbers in the file are read. If no divisor is found, the new number is prime.
- Since this program takes a long time to finish, you should run it as a batch job from a UNIX machine. If the machine is shut down and rebooted, your program should resume by using the prime numbers stored in the binary data file rather than start over from scratch.

**22.9 (Geometry: gift-wrapping algorithm for finding a convex hull) Section 22.10.1 introduced the gift-wrapping algorithm for finding a convex hull for a set of points. Assume that the Java’s coordinate system is used for the points. Implement the algorithm using the following method:

/** Return the points that form a convex hull */
public static ArrayList<Point2D> getConvexHull(double[][] s)

Point2D is defined in Section 9.6.

Write a test program that prompts the user to enter the set size and the points and displays the points that form a convex hull. Here is a sample run:

How many points are in the set? 6
Enter 6 points: 1 2.4 2.5 2 1.5 34.5 5.5 6 6 2.4 5.5 9
The convex hull is
(1.5, 34.5) (5.5, 9.0) (6.0, 2.4) (2.5, 2.0) (1.0, 2.4)

22.10 (Number of prime numbers) Programming Exercise 22.8 stores the prime numbers in a file named PrimeNumbers.dat. Write a program that finds the number of prime numbers that are less than or equal to 10, 100, 1,000, 10,000, 100,000, 1,000,000, 10,000,000, 100,000,000, 1,000,000,000, and 10,000,000,000. Your program should read the data from PrimeNumbers.dat.
Chapter 22  Developing Efficient Algorithms

**22.11** (Geometry: Graham’s algorithm for finding a convex hull) Section 22.10.2 introduced Graham’s algorithm for finding a convex hull for a set of points. Assume that the Java’s coordinate system is used for the points. Implement the algorithm using the following method:

```java
/** Return the points that form a convex hull */
public static ArrayList<MyPoint> getConvexHull(double[][] s)
```

MyPoint is a static inner class defined as follows:

```java
private static class MyPoint implements Comparable<MyPoint> {
    double x, y;
    MyPoint(double x, double y) {
        this.x = x; this.y = y;
    }
    public void setRightMostLowestPoint(MyPoint p) {
        rightMostLowestPoint = p;
    }
    @Override
    public int compareTo(MyPoint o) {
        // Implement it to compare this point with point o
        // angularly along the x-axis with rightMostLowestPoint
        // as the center, as shown in Figure 22.10b. By implementing
        // the Comparable interface, you can use the Array.sort
        // method to sort the points to simplify coding.
    }
}
```

Write a test program that prompts the user to enter the set size and the points and displays the points that form a convex hull. Here is a sample run:

```
How many points are in the set? 6
Enter 6 points: 1 2.4 2.5 2 1.5 34.5 5.5 6 6 2.4 5.5 9
The convex hull is
(1.5, 34.5) (5.5, 9.0) (6.0, 2.4) (2.5, 2.0) (1.0, 2.4)
```

**22.12** (Last 100 prime numbers) Programming Exercise 22.8 stores the prime numbers in a file named PrimeNumbers.dat. Write an efficient program that reads the last 100 numbers in the file. (Hint: Don’t read all numbers from the file. Skip all numbers before the last 100 numbers in the file.)

**22.13** (Geometry: convex hull animation) Programming Exercise 22.11 finds a convex hull for a set of points entered from the console. Write a program that enables the user to add/remove points by clicking the left/right mouse button, and displays a convex hull, as shown in Figure 22.8c.

**22.14** (Execution time for prime numbers) Write a program that obtains the execution time for finding all the prime numbers less than 8,000,000, 10,000,000,
12,000,000, 14,000,000, 16,000,000, and 18,000,000 using the algorithms in Listings 22.5–22.7. Your program should print a table like this:

<table>
<thead>
<tr>
<th></th>
<th>8000000</th>
<th>10000000</th>
<th>12000000</th>
<th>14000000</th>
<th>16000000</th>
<th>18000000</th>
</tr>
</thead>
<tbody>
<tr>
<td>Listing 22.5</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Listing 22.6</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Listing 22.7</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

**22.15** *(Geometry: non-cross polygon)* Write a program that enables the user to add/remove points by clicking the left/right mouse button, and displays a non-crossed polygon that links all the points, as shown in Figure 22.11(a). A polygon is crossed if two or more sides intersect, as shown in Figure 22.11b. Use the following algorithm to construct a polygon from a set of points.

Step 1: Given a set of points \( S \), select the rightmost lowest point \( p_0 \) in the set \( S \).

Step 2: Sort the points in \( S \) angularly along the \( x \)-axis with \( p_0 \) as the center. If there is a tie and two points have the same angle, the one that is closer to \( p_0 \) is considered greater. The points in \( S \) are now sorted as \( p_0, p_1, p_2, \ldots, p_{n-1} \).

Step 3: The sorted points form a non-cross polygon.

**22.16** *(Linear search animation)* Write a program that animates the linear search algorithm. Create an array that consists of 20 distinct numbers from 1 to 20 in a random order. The array elements are displayed in a histogram, as shown in Figure 22.12. You need to enter a search key in the text field. Clicking the Step button causes the program to perform one comparison in the algorithm and repaints the histogram with a bar indicating the search position. This button also freezes the text field to prevent its value from being changed. When the algorithm is finished, display the status in the label at the top of the border pane to inform the user. Clicking the Reset button creates a new random array for a new start. This button also makes the text field editable.
**22.17** (*Closest-pair animation*) Write a program that enables the user to add/remove points by clicking the left/right mouse button, and displays a line that connects the pair of nearest points, as shown in Figure 22.4.

**22.18** (*Binary search animation*) Write a program that animates the binary search algorithm. Create an array with numbers from 1 to 20 in this order. The array elements are displayed in a histogram, as shown in Figure 22.13. You need to enter a search key in the text field. Clicking the *Step* button causes the program to perform one comparison in the algorithm. Use a light-gray color to paint the bars for the numbers in the current search range and use a black color to paint the a bar indicating the middle number in the search range. The *Step* button also freezes the text field to prevent its value from being changed. When the algorithm is finished, display the status in a label at the top of a border pane. Clicking the *Reset* button enables a new search to start. This button also makes the text field editable.

*22.19* (*Largest block*) The problem for finding a largest block is described in Programming Exercise 8.35. Design a dynamic programming algorithm for solving this problem in $O(n^2)$ time. Write a test program that displays a 10-by-10 square matrix, as shown in Figure 22.14a. Each element in the matrix is 0 or 1, randomly generated with a click of the *Refresh* button. Display each number centered in a text field. Use a text field for each entry. Allow the user to change the entry value. Click the *Find Largest Block* button to find a largest square submatrix that consists of 1s. Highlight the numbers in the block, as shown in Figure 22.14b. See [www.cs.armstrong.edu/liang/animation/FindLargestBlock.html](http://www.cs.armstrong.edu/liang/animation/FindLargestBlock.html) for an interactive test.
22.20 (Game: multiple Sudoku solutions) The complete solution for the Sudoku problem is given in Supplement VI.A. A Sudoku problem may have multiple solutions. Modify Sudoku.java in Supplement VI.A to display the total number of the solutions. Display two solutions if multiple solutions exist.

22.21 (Game: Sudoku) The complete solution for the Sudoku problem is given in Supplement VI.C. Write a program that lets the user enter the input from the text fields, as shown in Figure 22.15a. Clicking the Solve button displays the result, as shown in Figure 22.15b–c.

22.22 (Game: recursive Sudoku) Write a recursive solution for the Sudoku problem.

22.23 (Game: multiple Eight Queens solution) Write a program to display all possible solutions for the Eight Queens puzzle in a scroll pane, as shown in Figure 22.16. For each solution, put a label to denote the solution number. (Hint: Place all solution panes into an HBox and place this one pane into a ScrollPane.)

22.24 (Find the smallest number) Write a method that uses the divide-and-conquer approach to find the smallest number in a list.
22.25 (Game: Sudoku) Revise Programming Exercise 22.21 to display all solutions for the Sudoku game, as shown in Figure 22.17a. When you click the Solve button, the program stores all solutions in an ArrayList. Each element in the list is a two-dimensional 9-by-9 grid. If the program has multiple solutions, the Next button appears as shown in Figure 22.17b. You can click the Next button to display the next solution and also a label to show the solution count. When the Clear button is clicked, the cells are cleared and the Next button is hidden as shown in Figure 22.17c.

Figure 22.17 The program can display multiple Sudoku solutions.
SORTING

Objectives

- To study and analyze time complexity of various sorting algorithms (§§23.2–23.7).
- To design, implement, and analyze insertion sort (§23.2).
- To design, implement, and analyze bubble sort (§23.3).
- To design, implement, and analyze merge sort (§23.4).
- To design, implement, and analyze quick sort (§23.5).
- To design and implement a binary heap (§23.6).
- To design, implement, and analyze heap sort (§23.6).
- To design, implement, and analyze bucket sort and radix sort (§23.7).
- To design, implement, and analyze external sort for files that have a large amount of data (§23.8).
**23.1 Introduction**

*Sorting algorithms are good examples for studying algorithm design and analysis.*

When presidential candidate Barack Obama visited Google in 2007, Google CEO Eric Schmidt asked Obama the most efficient way to sort a million 32-bit integers (www.youtube.com/watch?v=k4RRi_ntQc8). Obama answered that the bubble sort would be the wrong way to go. Was he right? We will examine different sorting algorithms in this chapter and see if he was correct.

Sorting is a classic subject in computer science. There are three reasons to study sorting algorithms.

- First, sorting algorithms illustrate many creative approaches to problem solving, and these approaches can be applied to solve other problems.
- Second, sorting algorithms are good for practicing fundamental programming techniques using selection statements, loops, methods, and arrays.
- Third, sorting algorithms are excellent examples to demonstrate algorithm performance.

The data to be sorted might be integers, doubles, characters, or objects. Section 7.11, Sorting Arrays, presented selection sort. The selection sort algorithm was extended to sort an array of objects in Section 19.5, Case Study: Sorting an Array of Objects. The Java API contains several overloaded sort methods for sorting primitive type values and objects in the `java.util.Arrays` and `java.util.Collections` classes. For simplicity, this chapter assumes:

1. data to be sorted are integers,
2. data are stored in an array, and
3. data are sorted in ascending order.

The programs can be easily modified to sort other types of data, to sort in descending order, or to sort data in an `ArrayList` or a `LinkedList`.

There are many algorithms for sorting. You have already learned selection sort. This chapter introduces insertion sort, bubble sort, merge sort, quick sort, bucket sort, radix sort, and external sort.

**23.2 Insertion Sort**

*The insertion-sort algorithm sorts a list of values by repeatedly inserting a new element into a sorted sublist until the whole list is sorted.*

Figure 23.1 shows how to sort the list `{2, 9, 5, 4, 8, 1, 6}` using insertion sort.

The algorithm can be described as follows:

```java
for (int i = 1; i < list.length; i++) {
    insert list[i] into a sorted sublist list[0..i-1] so that
    list[0..i] is sorted.
}
```

To insert `list[i]` into `list[0..i-1]`, save `list[i]` into a temporary variable, say `currentState`. Move `list[i-1]` to `list[i]` if `list[i-1] > currentState`, move `list[i-2]` to `list[i-1]` if `list[i-2] > currentState`, and so on, until `list[i-k] <= currentState` or `k > i` (we pass the first element of the sorted list). Assign `currentState` to `list[i-k+1]`. For example, to insert 4 into `{2, 5, 9}` in Step 4 in Figure 23.2, move `list[2]` (9) to `list[3]` since 9 > 4, and move `list[1]` (5) to `list[2]` since 5 > 4. Finally, move `currentState` (4) to `list[1]`. 
Step 1: Initially, the sorted sublist contains the first element in the list. Insert 9 into the sublist.

Step 2: The sorted sublist is [2, 9]. Insert 5 into the sublist.

Step 3: The sorted sublist is [2, 5, 9]. Insert 4 into the sublist.

Step 4: The sorted sublist is [2, 4, 5, 9]. Insert 8 into the sublist.

Step 5: The sorted sublist is [2, 4, 5, 8, 9]. Insert 1 into the sublist.

Step 6: The sorted sublist is [1, 2, 4, 5, 8, 9]. Insert 6 into the sublist.

Step 7: The entire list is now sorted.

**Figure 23.1** Insertion sort repeatedly inserts a new element into a sorted sublist.

```
list  2 5 9 4
Step 1: Save 4 to a temporary variable `currentElement`
currentElement: 4
list  2 5 9 4

list  2 5 9
Step 2: Move `list[2]` to `list[3]`

list  2 5 9
Step 3: Move `list[1]` to `list[2]`

list  2 4 5 9
Step 4: Assign `currentElement` to `list[1]`
```

**Figure 23.2** A new element is inserted into a sorted sublist.

The algorithm can be expanded and implemented as in Listing 23.1.

**Listing 23.1** InsertionSort.java

```java
1 public class InsertionSort {
2     /** The method for sorting the numbers */
3     public static void insertionSort(int[] list) {
4         for (int i = 1; i < list.length; i++) {
5             /** Insert list[i] into a sorted sublist list[0..i-1] so that
6                 list[0..i] is sorted. */
7             int currentElement = list[i];
8             int k;
9             for (k = i - 1; k >= 0 && list[k] > currentElement; k--) {
10                list[k + 1] = list[k];
11            }
12            list[k + 1] = currentElement;
13         }
14     }
15 }
```
Chapter 23 Sorting

```java
11        }
12
13    // Insert the current element into list[k + 1]
14    list[k + 1] = currentElement;
15
16  }
17 }
```

The `insertionSort(int[] list)` method sorts any array of `int` elements. The method is implemented with a nested `for` loop. The outer loop (with the loop control variable `i`) (line 4) is iterated in order to obtain a sorted sublist, which ranges from `list[0]` to `list[i]`. The inner loop (with the loop control variable `k`) inserts `list[i]` into the sublist from `list[0]` to `list[i-1].`

To better understand this method, trace it with the following statements:

```java
int[] list = {1, 9, 4, 6, 5, -4};
InsertionSort.insertionSort(list);
```

The insertion sort algorithm presented here sorts a list of elements by repeatedly inserting a new element into a sorted partial array until the whole array is sorted. At the `k`th iteration, to insert an element into an array of size `k`, it may take `k` comparisons to find the insertion position, and `k` moves to insert the element. Let `T(n)` denote the complexity for insertion sort and `c` denote the total number of other operations such as assignments and additional comparisons in each iteration. Thus,

\[
T(n) = (2 + c) + (2 \times 2 + c) + \cdots + (2 \times (n - 1) + c) \\
= 2(1 + 2 + \cdots + n - 1) + c(n - 1) \\
= \frac{2(n - 1)n}{2} + cn - c = n^2 - n + cn - c \\
= O(n^2)
\]

Therefore, the complexity of the insertion sort algorithm is `O(n^2)`. Hence, the selection sort and insertion sort are of the same time complexity.

### Check Point

23.1 Describe how an insertion sort works. What is the time complexity for an insertion sort?

23.2 Use Figure 23.1 as an example to show how to apply a bubble sort on `{45, 11, 50, 59, 60, 2, 4, 7, 10}`.

23.3 If a list is already sorted, how many comparisons will the `insertionSort` method perform?

### 23.3 Bubble Sort

*A bubble sort sorts the array in multiple phases. Each pass successively swaps the neighboring elements if the elements are not in order.*

The bubble sort algorithm makes several passes through the array. On each pass, successive neighboring pairs are compared. If a pair is in decreasing order, its values are swapped; otherwise, the values remain unchanged. The technique is called a *bubble sort* or *sinking sort*, because the smaller values gradually “bubble” their way to the top and the larger values sink to the bottom. After the first pass, the last element becomes the largest in the array. After the second pass, the second-to-last element becomes the second largest in the array. This process is continued until all elements are sorted.
Figure 23.3a shows the first pass of a bubble sort on an array of six elements (2 9 5 4 8 1). Compare the elements in the first pair (2 and 9), and no swap is needed because they are already in order. Compare the elements in the second pair (9 and 5), and swap 9 with 5 because 9 is greater than 5. Compare the elements in the third pair (9 and 4), and swap 9 with 4. Compare the elements in the fourth pair (9 and 8), and swap 9 with 8. Compare the elements in the fifth pair (9 and 1), and swap 9 with 1. The pairs being compared are highlighted and the numbers already sorted are italicized in Figure 23.3.

The first pass places the largest number (9) as the last in the array. In the second pass, as shown in Figure 23.3b, you compare and order pairs of elements sequentially. There is no need to consider the last element, because the last element in the array is already the largest. In the third pass, as shown in Figure 23.3c, you compare and order pairs of elements sequentially except the last two elements, because they are already in order. So in the 4th pass, you don’t need to consider the last \( k - 1 \) elements, because they are already ordered.

The algorithm for a bubble sort is described in Listing 23.2.

**LISTING 23.2 Bubble Sort Algorithm**

```java
1 for (int k = 1; k < list.length; k++) {
2     // Perform the kth pass
3     for (int i = 0; i < list.length - k; i++) {
4         if (list[i] > list[i + 1])
5             swap list[i] with list[i + 1];
6     }
7 }
```

Note that if no swap takes place in a pass, there is no need to perform the next pass, because all the elements are already sorted. You can use this property to improve the algorithm in Listing 23.2 as in Listing 23.3.

**LISTING 23.3 Improved Bubble Sort Algorithm**

```java
1 boolean needNextPass = true;
2 for (int k = 1; k < list.length && needNextPass; k++) {
3     // Array may be sorted and next pass not needed
4     needNextPass = false;
5     // Perform the kth pass
6     for (int i = 0; i < list.length - k; i++) {
7         if (list[i] > list[i + 1]) {
8             swap list[i] with list[i + 1];
9             needNextPass = true; // Next pass still needed
10         }
11     }
12 }
```
The algorithm can be implemented in Listing 23.4.

**Listing 23.4  BubbleSort.java**

```java
public class BubbleSort {
    /** Bubble sort method */
    public static void bubbleSort(int[] list) {
        boolean needNextPass = true;

        for (int k = 1; k < list.length && needNextPass; k++) {
            // Array may be sorted and next pass not needed
            needNextPass = false;
            for (int i = 0; i < list.length - k; i++) {
                // Swap list[i] with list[i + 1]
                if (list[i] > list[i + 1]) {
                    int temp = list[i];
                    list[i] = list[i + 1];
                    list[i + 1] = temp;
                    needNextPass = true; // Next pass still needed
                }
            }
        }

        /** A test method */
        public static void main(String[] args) {
            int[] list = {2, 3, 2, 5, 6, 1, -2, 3, 14, 12};
            bubbleSort(list);
            for (int i = 0; i < list.length; i++)
                System.out.print(list[i] + " ");
        }
    }
}
```

In the best case, the bubble sort algorithm needs just the first pass to find that the array is already sorted—no next pass is needed. Since the number of comparisons is \( n - 1 \) in the first pass, the best-case time for a bubble sort is \( O(n) \).

In the worst case, the bubble sort algorithm requires \( n - 1 \) passes. The first pass makes \( n - 1 \) comparisons; the second pass makes \( n - 2 \) comparisons; and so on; the last pass makes 1 comparison. Thus, the total number of comparisons is:

\[
(n - 1) + (n - 2) + \cdots + 2 + 1 = \frac{(n - 1)n}{2} = \frac{n^2}{2} - \frac{n}{2} = O(n^2)
\]

Therefore, the worst-case time for a bubble sort is \( O(n^2) \).

**Check Point**

23.4 Describe how a bubble sort works. What is the time complexity for a bubble sort?

23.5 Use Figure 23.3 as an example to show how to apply a bubble sort on \{45, 11, 50, 59, 60, 2, 4, 7, 10\}.

23.6 If a list is already sorted, how many comparisons will the `bubbleSort` method perform?
23.4 Merge Sort

The merge sort algorithm can be described recursively as follows: The algorithm divides the array into two halves and applies a merge sort on each half recursively. After the two halves are sorted, merge them.

The algorithm for a merge sort is given in Listing 23.5.

Listing 23.5 Merge Sort Algorithm

```java
public static void mergeSort(int[] list) {
    if (list.length > 1) {
        mergeSort(list[0 ... list.length / 2]);
        mergeSort(list[list.length / 2 + 1 ... list.length]);
        list[list.length / 2 + 1 ... list.length] = merge(list[0 ... list.length / 2], list[list.length / 2 + 1 ... list.length]);
    }
}
```

Figure 23.4 illustrates a merge sort of an array of eight elements (2 9 5 4 8 1 6 7). The original array is split into (2 9 5 4) and (8 1 6 7). Apply a merge sort on these two subarrays recursively to split (2 9 5 4) into (2 9) and (5 4) and (8 1 6 7) into (8 1) and (6 7). This process continues until the subarray contains only one element. For example, array (2 9) is split into the subarrays (2) and (9). Since array (2) contains a single element, it cannot be further split. Now merge (2) with (9) into a new sorted array (2 9); merge (5) with (4) into a new sorted array (4 5). Merge (2 9) with (4 5) into a new sorted array (2 4 5 9), and finally merge (2 4 5 9) with (1 6 7 8) into a new sorted array (1 2 4 5 6 7 8 9).

The recursive call continues dividing the array into subarrays until each subarray contains only one element. The algorithm then merges these small subarrays into larger sorted subarrays until one sorted array results.

The merge sort algorithm is implemented in Listing 23.6.

Listing 23.6 MergeSort.java

```java
public class MergeSort {
    /** The method for sorting the numbers */
    public static void mergeSort(int[] list) {
        if (list.length > 1) {
            base case
```
// Merge sort the first half
int[] firstHalf = new int[list.length / 2];
System.arraycopy(list, 0, firstHalf, 0, list.length / 2);

// Merge sort the second half
int secondHalfLength = list.length - list.length / 2;
int[] secondHalf = new int[secondHalfLength];
System.arraycopy(list, list.length / 2, secondHalf, 0, secondHalfLength);

// Merge firstHalf with secondHalf into list
merge(firstHalf, secondHalf, list);

/** Merge two sorted lists */
public static void merge(int[] list1, int[] list2, int[] temp) {
    int current1 = 0; // Current index in list1
    int current2 = 0; // Current index in list2
    int current3 = 0; // Current index in temp

    while (current1 < list1.length && current2 < list2.length) {
        if (list1[current1] < list2[current2])
            temp[current3++] = list1[current1++];
        else
            temp[current3++] = list2[current2++];
    }
    while (current1 < list1.length)
        temp[current3++] = list1[current1++];
    while (current2 < list2.length)
        temp[current3++] = list2[current2++];
}

/** A test method */
public static void main(String[] args) {
    int[] list = {2, 3, 2, 5, 6, 1, -2, 3, 14, 12};
    mergeSort(list);
    for (int i = 0; i < list.length; i++)
        System.out.print(list[i] + " ");
}

The **mergeSort** method (lines 3–20) creates a new array **firstHalf**, which is a copy of the first half of **list** (line 7). The algorithm invokes **mergeSort** recursively on **firstHalf** (line 8). The length of the **firstHalf** is **list.length / 2** and the length of the **secondHalf** is **list.length - list.length / 2**. The new array **secondHalf** was created to contain the second part of the original array **list**. The algorithm invokes **mergeSort** recursively on **secondHalf** (line 15). After **firstHalf** and **secondHalf** are sorted, they are merged to **list** (line 18). Thus, array **list** is now sorted.

The **merge** method (lines 23–40) merges two sorted arrays **list1** and **list2** into array **temp**. **current1** and **current2** point to the current element to be considered in **list1** and **list2** (lines 24–26). The method repeatedly compares the current elements from **list1** and **list2** and moves the smaller one to **temp.current1**. **current1** is increased by 1 (line 30) if the smaller one is in **list1** and **current2** is increased by 1 (line 32) if the smaller one is
in \texttt{list2}. Finally, all the elements in one of the lists are moved to \texttt{temp}. If there are still unmoved elements in \texttt{list1}, copy them to \texttt{temp} (lines 35–36). If there are still unmoved elements in \texttt{list2}, copy them to \texttt{temp} (lines 38–39).

Figure 23.5 illustrates how to merge the two arrays \texttt{list1} (2 4 5 9) and \texttt{list2} (1 6 7 8). Initially the current elements to be considered in the arrays are 2 and 1. Compare them and move the smaller element 1 to \texttt{temp}, as shown in Figure 23.5a. \texttt{current2} and \texttt{current3} are increased by 1. Continue to compare the current elements in the two arrays and move the smaller one to \texttt{temp} until one of the arrays is completely moved. As shown in Figure 23.5b, all the elements in \texttt{list2} are moved to \texttt{temp} and \texttt{current1} points to element 9 in \texttt{list1}. Copy 9 to \texttt{temp}, as shown in Figure 23.5c.

![Figure 23.5](image)

**Figure 23.5** Two sorted arrays are merged into one sorted array.

The \texttt{mergeSort} method creates two temporary arrays (lines 6, 12) during the dividing process, copies the first half and the second half of the array into the temporary arrays (lines 7, 13), sorts the temporary arrays (lines 8, 15), and then merges them into the original array (line 18), as shown in Figure 23.6a. You can rewrite the code to recursively sort the first half of the array and the second half of the array without creating new temporary arrays, and then merge the two arrays into a temporary array and copy its contents to the original array, as shown in Figure 23.6b. This is left for you to do in Programming Exercise 23.20.

![Figure 23.6](image)

**Figure 23.6** Temporary arrays are created to support a merge sort.

**Note**

A merge sort can be implemented efficiently using parallel processing. See Section 30.16, Parallel Programming, for a parallel implementation of a merge sort.
Let $T(n)$ denote the time required for sorting an array of $n$ elements using a merge sort. Without loss of generality, assume $n$ is a power of 2. The merge sort algorithm splits the array into two subarrays, sorts the subarrays using the same algorithm recursively, and then merges the subarrays. Therefore,

$$T(n) = T\left(\frac{n}{2}\right) + T\left(\frac{n}{2}\right) + \text{mergetime}$$

The first $T\left(\frac{n}{2}\right)$ is the time for sorting the first half of the array, and the second $T\left(\frac{n}{2}\right)$ is the time for sorting the second half. To merge two subarrays, it takes at most $n - 1$ comparisons to compare the elements from the two subarrays and $n$ moves to move elements to the temporary array. Thus, the total time is $2n - 1$. Therefore,

$$T(n) = T\left(\frac{n}{2}\right) + T\left(\frac{n}{2}\right) + 2n - 1 = O(n \log n)$$

The complexity of a merge sort is $O(n \log n)$. This algorithm is better than selection sort, insertion sort, and bubble sort, because the time complexity of these algorithms is $O(n^2)$. The sort method in the java.util.Arrays class is implemented using a variation of the merge sort algorithm.

### Check Point

23.7 Describe how a merge sort works. What is the time complexity for a merge sort?

23.8 Use Figure 23.4 as an example to show how to apply a merge sort on {45, 11, 50, 59, 60, 2, 4, 7, 10}.

23.9 What is wrong if lines 6–15 in Listing 23.6, MergeSort.java, are replaced by the following code?

```java
// Merge sort the first half
int[] firstHalf = new int[list.length / 2 + 1];
System.arraycopy(list, 0, firstHalf, 0, list.length / 2 + 1);
mergeSort(firstHalf);

// Merge sort the second half
int secondHalfLength = list.length - list.length / 2 - 1;
int[] secondHalf = new int[secondHalfLength];
System.arraycopy(list, list.length / 2 + 1,
secondHalf, 0, secondHalfLength);
mergeSort(secondHalf);
```

### 23.5 Quick Sort

A quick sort works as follows: The algorithm selects an element, called the pivot, in the array. It divides the array into two parts, so that all the elements in the first part are less than or equal to the pivot and all the elements in the second part are greater than the pivot. The quick sort algorithm is then recursively applied to the first part and then the second part.

The quick sort algorithm, developed by C.A.R. Hoare in 1962, is described in Listing 23.7.

### Listing 23.7 Quick Sort Algorithm

```java
public static void quickSort(int[] list) {
    if (list.length > 1) {
        select a pivot;
        partition list into list1 and list2 such that
```
23.5 Quick Sort

Each partition places the pivot in the right place. The selection of the pivot affects the performance of the algorithm. Ideally, the algorithm should choose the pivot that divides the two parts evenly. For simplicity, assume the first element in the array is chosen as the pivot. (Programming Exercise 23.4 proposes an alternative strategy for selecting the pivot.)

Figure 23.7 illustrates how to sort an array (5 2 9 3 8 4 0 1 6 7) using quick sort. Choose the first element, 5, as the pivot. The array is partitioned into two parts, as shown in Figure 23.7b. The highlighted pivot is placed in the right place in the array. Apply quick sort on two partial arrays (4 2 1 3 0) and then (8 9 6 7). The pivot 4 partitions (4 2 1 3 0) into just one partial array (0 2 1 3), as shown in Figure 23.7c. Apply quick sort on (0 2 1 3). The pivot 0 partitions it into just one partial array (2 1 3), as shown in Figure 23.7d. Apply quick sort on (2 1 3). The pivot 2 partitions it into (1) and (3), as shown in Figure 23.7e. Since the array contains just one element, no further partition is needed.

The quick sort algorithm is implemented in Listing 23.8. There are two overloaded quickSort methods in the class. The first method (line 2) is used to sort an array. The second is a helper method (line 6) that sorts a partial array with a specified range.

**LISTING 23.8 QuickSort.java**

```java
1 public class QuickSort {
2     public static void quickSort(int[] list) {
3         quickSort(list, 0, list.length - 1);
4     }
5
6     public static void quickSort(int[] list, int first, int last) {
7         if (last > first) {
8             int pivotIndex = partition(list, first, last);
9             quickSort(list, first, pivotIndex - 1);
10             quickSort(list, pivotIndex + 1, last);
11         }
12     }
```
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12 */
13 public static int partition(int[] list, int first, int last) {
14     int pivot = list[first]; // Choose the first element as the pivot
15     int low = first + 1; // Index for forward search
16     int high = last; // Index for backward search
17     while (high > low) {
18         // Search forward from left
19         while (low <= high && list[low] <= pivot)
20             low++;
21         // Search backward from right
22         while (low <= high && list[high] > pivot)
23             high--;
24         // Swap two elements in the list
25         if (high > low) {
26             int temp = list[high];
27             list[high] = list[low];
28             list[low] = temp;
29         }
30     }
31     while (high > first && list[high] >= pivot)
32         high--;
33     // Swap pivot with list[high]
34     if (pivot > list[high]) {
35         list[first] = list[high];
36         list[high] = pivot;
37         return high;
38     } else {
39         return first;
40     }
41 }
42 /** A test method */
43 public static void main(String[] args) {
44     int[] list = {2, 3, 2, 5, 1, -2, 3, 14, 12};
45     quickSort(list);
46     for (int i = 0; i < list.length; i++)
47         System.out.print(list[i] + " ");
48 }
49 }
50
51 The partition method (lines 15–49) partitions the array list[first..last] using the pivot. The first element in the partial array is chosen as the pivot (line 16). Initially low points to the second element in the partial array (line 17) and high points to the last element in the partial array (line 18).

Starting from the left, the method searches forward in the array for the first element that is greater than the pivot (lines 22–23), then searches from the right backward for the first element in the array that is less than or equal to the pivot (lines 26–27). It then swaps these two
elements and repeats the same search and swap operations until all the elements are searched in a \textbf{while} loop (lines 20–35).

The method returns the new index for the pivot that divides the partial array into two parts if the pivot has been moved (line 44). Otherwise, it returns the original index for the pivot (line 47).

Figure 23.8 illustrates how to partition an array (5 2 9 3 8 4 0 1 6 7). Choose the first element, 5, as the pivot. Initially \texttt{low} is the index that points to element 2 and \texttt{high} points to element 7, as shown in Figure 23.8a. Advance index \texttt{low} forward to search for the first element (9) that is greater than the pivot and move index \texttt{high} backward to search for the first element (1) that is less than or equal to the pivot, as shown in Figure 23.8b. Swap 9 with 1, as shown in Figure 23.8c. Continue the search and move \texttt{low} to point to element 8 and \texttt{high} to point to element 0, as shown in Figure 23.8d. Swap element 8 with 0, as shown in Figure 23.8e. Continue to move \texttt{low} until it passes \texttt{high}, as shown in Figure 23.8f. Now all the elements are examined. Swap the pivot with element 4 at index \texttt{high}. The final partition is shown in Figure 23.8g. The index of the pivot is returned when the method is finished.

To partition an array of \( n \) elements, it takes \( n \) comparisons and \( n \) moves in the worst case. Thus, the time required for partition is \( O(n) \).

In the worst case, the pivot divides the array each time into one big subarray with the other array empty. The size of the big subarray is one less than the one before divided. The algorithm requires \((n - 1) + (n - 2) + \cdots + 2 + 1 = O(n^2)\) time.
In the best case, the pivot divides the array each time into two parts of about the same size. Let $T(n)$ denote the time required for sorting an array of $n$ elements using quick sort. Thus,

$$T(n) = T\left(\frac{n}{2}\right) + T\left(\frac{n}{2}\right) + n.$$ 

Similar to the merge sort analysis, $T(n) = O(n \log n)$.

On the average, the pivot will not divide the array into two parts of the same size or one empty part each time. Statistically, the sizes of the two parts are very close. Therefore, the average time is $O(n \log n)$. The exact average-case analysis is beyond the scope of this book.

Both merge sort and quick sort employ the divide-and-conquer approach. For merge sort, the bulk of the work is to merge two sublists, which takes place after the sublists are sorted. For quick sort, the bulk of the work is to partition the list into two sublists, which takes place before the sublists are sorted. Merge sort is more efficient than quick sort in the worst case, but the two are equally efficient in the average case. Merge sort requires a temporary array for sorting two subarrays. Quick sort does not need additional array space. Thus, quick sort is more space efficient than merge sort.

23.10 Describe how quick sort works. What is the time complexity for a quick sort?

23.11 Why is quick sort more space efficient than merge sort?

23.12 Use Figure 23.7 as an example to show how to apply a quick sort on \{45, 11, 50, 59, 60, 2, 4, 7, 10\}.

23.6 Heap Sort

A heap sort uses a binary heap. It first adds all the elements to a heap and then removes the largest elements successively to obtain a sorted list.

Heap sorts use a binary heap, which is a complete binary tree. A binary tree is a hierarchical structure. It either is empty or it consists of an element, called the root, and two distinct binary trees, called the left subtree and right subtree. The length of a path is the number of the edges in the path. The depth of a node is the length of the path from the root to the node.

A binary heap is a binary tree with the following properties:

- **Shape property:** It is a complete binary tree.
- **Heap property:** Each node is greater than or equal to any of its children.

A binary tree is complete if each of its levels is full, except that the last level may not be full and all the leaves on the last level are placed leftmost. For example, in Figure 23.9, the binary trees in (a) and (b) are complete, but the binary trees in (c) and (d) are not complete. Further, the binary tree in (a) is a heap, but the binary tree in (b) is not a heap, because the root (39) is less than its right child (42).

![Figure 23.9](image)

*Figure 23.9* A binary heap is a special complete binary tree.
Note
Heap is a term with many meanings in computer science. In this chapter, heap means a binary heap.

Pedagogical Note
A heap can be implemented efficiently for inserting keys and for deleting the root. For an interactive demo on how a heap works, go to www.cs.armstrong.edu/liang/animation/web/Heap.html, as shown in Figure 23.10.

23.6.1 Storing a Heap
A heap can be stored in an ArrayList or an array if the heap size is known in advance. The heap in Figure 23.11a can be stored using the array in Figure 23.11b. The root is at position 0, and its two children are at positions 1 and 2. For a node at position $i$, its left child is at position $2i + 1$, its right child is at position $2i + 2$, and its parent is $(i - 1)/2$. For example, the node for element 39 is at position 4, so its left child (element 14) is at 9 ($2 \times 4 + 1$), its right child (element 33) is at 10 ($2 \times 4 + 2$), and its parent (element 42) is at 1 ($(4 - 1)/2$).

23.6.2 Adding a New Node
To add a new node to the heap, first add it to the end of the heap and then rebuild the tree as follows:

Let the last node be the current node;
while (the current node is greater than its parent) {

Figure 23.11 A binary heap can be implemented using an array.
Swap the current node with its parent;
Now the current node is one level up;
}

Suppose a heap is initially empty. That heap is shown in Figure 23.12, after adding numbers 3, 5, 1, 19, 11, and 22 in this order.

![Figure 23.12](image)

FIGURE 23.12  Elements 3, 5, 1, 19, 11, and 22 are inserted into the heap.

Now consider adding 88 into the heap. Place the new node 88 at the end of the tree, as shown in Figure 23.13a. Swap 88 with 19, as shown in Figure 23.13b. Swap 88 with 22, as shown in Figure 23.13c.

![Figure 23.13](image)

FIGURE 23.13  Rebuild the heap after adding a new node.

23.6.3 Removing the Root

Often you need to remove the maximum element, which is the root in a heap. After the root is removed, the tree must be rebuilt to maintain the heap property. The algorithm for rebuilding the tree can be described as follows:

Move the last node to replace the root;
Let the root be the current node;
while (the current node has children and the current node is smaller than one of its children) {
  Swap the current node with the larger of its children;
  Now the current node is one level down;
}

Figure 23.14 shows the process of rebuilding a heap after the root 62 is removed from Figure 23.11a. Move the last node, 9, to the root, as shown in Figure 23.14a. Swap 9 with 59, as shown in Figure 23.14b; swap 9 with 44, as shown in Figure 23.14c; and swap 9 with 30, as shown in Figure 23.14d.
Figure 23.15 shows the process of rebuilding a heap after the root, 59, is removed from Figure 23.14d. Move the last node, 17, to the root, as shown in Figure 23.15a. Swap 17 with 44, as shown in Figure 23.15b, and then swap 17 with 30, as shown in Figure 23.15c.

Figure 23.14 Rebuild the heap after the root 62 is removed.

23.6.4 The Heap Class
Now you are ready to design and implement the Heap class. The class diagram is shown in Figure 23.16. Its implementation is given in Listing 23.9.
Listing 23.9 Heap.java

```java
public class Heap<E extends Comparable<E>> {
  private java.util.ArrayList<E> list = new java.util.ArrayList<>();

  // no-arg constructor
  public Heap() {
    /** Create a default heap */
    public Heap() {
      list = new java.util.ArrayList<>();
    }
  }

  // constructor
  public Heap(E[] objects) {
    /** Create a heap from an array of objects */
    for (int i = 0; i < objects.length; i++)
      add(objects[i]);
  }

  // add a new object
  public void add(E newObject) {
    list.add(newObject); // Append to the heap
    int currentIndex = list.size() - 1; // The index of the last node
    while (currentIndex > 0) {
      int parentIndex = (currentIndex - 1) / 2;
      // Swap if the current object is greater than its parent
      if (list.get(currentIndex).compareTo(list.get(parentIndex)) > 0) {
        E temp = list.get(currentIndex);
        list.set(currentIndex, list.get(parentIndex));
        list.set(parentIndex, temp);
      } else
        break; // The tree is a heap now
    }
  }

  // remove the root from the heap
  public E remove() {
    if (list.size() == 0) return null;
    E removedObject = list.get(0);
    list.set(0, list.get(list.size() - 1));
    list.remove(list.size() - 1);
    int currentIndex = 0;
    while (currentIndex < list.size()) {
      // root
      int parentIndex = (currentIndex - 1) / 2;
      // new root
      list.set(0, list.get(list.size() - 1));
      list.remove(list.size() - 1);
      int currentIndex = 0;
      while (currentIndex < list.size()) {
        // swap with parent
        E temp = list.get(currentIndex);
        list.set(currentIndex, list.get(parentIndex));
        list.set(parentIndex, temp);
      } else
        break; // The tree is a heap now
    }
  }

  // getSize:
  public int getSize() {
    return list.size();
  }
}
```

Figure 23.16 The Heap class provides operations for manipulating a heap.
45 \textbf{int} leftChildIndex = 2 * currentIndex + 1;
46 \textbf{int} rightChildIndex = 2 * currentIndex + 2;
47
48 // Find the maximum between two children
49 \textbf{if} (leftChildIndex >= list.size()) \textbf{break}; // The tree is a heap
50 \textbf{int} maxIndex = leftChildIndex;
51 \textbf{if} (rightChildIndex < list.size()) {
52 \hspace{1em} \textbf{if} (list.get(maxIndex).compareTo(
53 \hspace{2em} list.get(rightChildIndex)) < 0) {
54 \hspace{3em} maxIndex = rightChildIndex;
55 \hspace{2em} }
56 \hspace{1em} }
57
58 // Swap if the current node is less than the maximum
59 \textbf{if} (list.get(currentIndex).compareTo(
60 \hspace{2em} list.get(maxIndex)) < 0) {
61 \hspace{3em} E temp = list.get(maxIndex);
62 \hspace{3em} list.set(maxIndex, list.get(currentIndex));
63 \hspace{3em} list.set(currentIndex, temp);
64 \hspace{3em} currentIndex = maxIndex;
65 \hspace{1em} }
66 \hspace{1em} else \textbf{break}; // The tree is a heap
67 \hspace{1em} }
68 \hspace{1em} }
69 \hspace{1em} \textbf{return} removedObject;
70 \hspace{1em} }
71 \hspace{1em} }
72 /** Get the number of nodes in the tree */
73 \textbf{public int} getSize() {
74 \hspace{1em} \textbf{return} list.size();
75 \hspace{1em} }
76 \hspace{1em} }
77 }\textbf{public class} HeapSort {
78 /** Heap sort method */
79 \textbf{public static }<\textbf{E}\textbf{ extends} \textbf{Comparable}<\textbf{E}>> \textbf{void} heapSort(\textbf{E}[] list) {
80 \hspace{1em} // Create a Heap of integers
81 \hspace{2em} \textbf{Heap}<\textbf{E}> heap = \textbf{new} \textbf{Heap}<>();
82 \hspace{1em} // create a Heap

A heap is represented using an array list internally (line 2). You can change the array list to other data structures, but the \textit{Heap} class contract will remain unchanged.

The \textit{add(\textit{E} \textit{newObject})} method (lines 15–33) appends the object to the tree and then swaps the object with its parent if the object is greater than its parent. This process continues until the new object becomes the root or is not greater than its parent.

The \textit{remove()} method (lines 36–71) removes and returns the root. To maintain the heap property, the method moves the last object to the root position and swaps it with its larger child if it is less than the larger child. This process continues until the last object becomes a leaf or is not less than its children.

\subsection{Sorting Using the \textit{Heap} Class}

To sort an array using a heap, first create an object using the \textit{Heap} class, add all the elements to the heap using the \textit{add} method, and remove all the elements from the heap using the \textit{remove} method. The elements are removed in descending order. Listing 23.10 gives a program for sorting an array using a heap.

\textbf{Listing 23.10} \textit{HeapSort.java}

1 \textbf{public class} HeapSort {
2 \hspace{1em} /** Heap sort method */
3 \hspace{2em} \textbf{public static }<\textbf{E}\textbf{ extends} \textbf{Comparable}<\textbf{E}>> \textbf{void} heapSort(\textbf{E}[] list) {
4 \hspace{3em} // Create a Heap of integers
5 \hspace{4em} \textbf{Heap}<\textbf{E}> heap = \textbf{new} \textbf{Heap}<>();
6 \hspace{3em} // create a Heap
// Add elements to the heap
for (int i = 0; i < list.length; i++)
    heap.add(list[i]);

// Remove elements from the heap
for (int i = list.length - 1; i >= 0; i--)
    list[i] = heap.remove();
}

/** A test method */
public static void main(String[] args) {
    Integer[] list = {-44, -5, -3, 3, 3, 1, -4, 0, 1, 2, 4, 5, 53};
    heapSort(list);
    for (int i = 0; i < list.length; i++)
        System.out.print(list[i] + " ");
}

23.6.6 Heap Sort Time Complexity

Let us turn our attention to analyzing the time complexity for the heap sort. Let $h$ denote the height for a heap of $n$ elements. The height of a heap is the number of nodes in the longest path from the root to a leaf node. Since a heap is a complete binary tree, the first level has 1 node, the second level has 2 nodes, the $k$th level has $2^{k-1}$ nodes, the $(h-1)$th level has $2^{h-2}$ nodes, and the $h$th level has at least 1 and at most $2^{h-1}$ nodes. Therefore,

$$1 + 2 + \cdots + 2^{h-2} + n \leq 2^h - 1 + 2 + \cdots + 2 + 2^{h-1}$$

That is,

$$2^{h-1} - 1 < n \leq 2^h - 1$$

Thus, $h < \log(n + 1) + 1$ and $\log(n + 1) \leq h$. Therefore, $\log(n + 1) \leq h < \log(n + 1) + 1$. Hence, the height of the heap is $O(\log n)$.

Since the `add` method traces a path from a leaf to a root, it takes at most $h$ steps to add a new element to the heap. Thus, the total time for constructing an initial heap is $O(n \log n)$ for an array of $n$ elements. Since the `remove` method traces a path from a root to a leaf, it takes at most $h$ steps to rebuild a heap after removing the root from the heap. Since the `remove` method is invoked $n$ times, the total time for producing a sorted array from a heap is $O(n \log n)$.

Both merge sorts and heap sorts require $O(n \log n)$ time. A merge sort requires a temporary array for merging two subarrays; a heap sort does not need additional array space. Therefore, a heap sort is more space efficient than a merge sort.

Check Point

23.13 What is a complete binary tree? What is a heap? Describe how to remove the root from a heap and how to add a new object to a heap.

23.14 What is the return value from invoking the `remove` method if the heap is empty?

23.15 Add the elements 4, 5, 1, 2, 9, and 3 into a heap in this order. Draw the diagrams to show the heap after each element is added.

23.16 Show the heap after the root in the heap in Figure 23.15c is removed.

23.17 What is the time complexity of inserting a new element into a heap and what is the time complexity of deleting an element from a heap?
23.18 Show the steps of creating a heap using {45, 11, 50, 59, 60, 2, 4, 7, 10}.

23.19 Given the following heap, show the steps of removing all nodes from the heap.

```
22 29
32
42
62
14 33
39
17 30
44
9
13
```

23.20 Which of the following statements are wrong?

1. `Heap<Object> heap1 = new Heap<>();`
2. `Heap<Number> heap2 = new Heap<>();`
3. `Heap<BigInteger> heap3 = new Heap<>();`
4. `Heap<Calendar> heap4 = new Heap<>();`
5. `Heap<String> heap5 = new Heap<>();`

23.7 Bucket Sort and Radix Sort

Bucket sorts and radix sorts are efficient for sorting integers.

All sort algorithms discussed so far are general sorting algorithms that work for any types of keys (e.g., integers, strings, and any comparable objects). These algorithms sort the elements by comparing their keys. It has been proven that no sorting algorithms based on comparisons can perform better than $O(n \log n)$. However, if the keys are integers, you can use a bucket sort without having to compare the keys.

The bucket sort algorithm works as follows. Assume the keys are in the range from 0 to $t$. We need $t + 1$ buckets labeled 0, 1, ..., and $t$. If an element’s key is $i$, the element is put into the bucket $i$. Each bucket holds the elements with the same key value.

You can use an `ArrayList` to implement a bucket. The bucket sort algorithm for sorting a list of elements can be described as follows:

```java
void bucketSort(E[] list) {
    E[] bucket = (E[])new java.util.ArrayList[t+1];

    // Distribute the elements from list to buckets
    for (int i = 0; i < list.length; i++) {
        int key = list[i].getKey(); // Assume element has the getKey() method
        if (bucket[key] == null)
            bucket[key] = new java.util.ArrayList<>();

        bucket[key].add(list[i]);
    }
```

Key Point
// Now move the elements from the buckets back to list
int k = 0;  // k is an index for list
for (int i = 0; i < bucket.length; i++) {
    if (bucket[i] != null) {
        for (int j = 0; j < bucket[i].size(); j++)
            list[k++] = bucket[i].get(j);
    }
}

Clearly, it takes \(O(n + t)\) time to sort the list and uses \(O(n + t)\) space, where \(n\) is the list size.

Note that if \(t\) is too large, using the bucket sort is not desirable. Instead, you can use a radix sort. The radix sort is based on the bucket sort, but a radix sort uses only ten buckets.

It is worthwhile to note that a bucket sort is stable, meaning that if two elements in the original list have the same key value, their order is not changed in the sorted list. That is, if element \(e_1\) and element \(e_2\) have the same key and \(e_1\) precedes \(e_2\) in the original list, \(e_1\) still precedes \(e_2\) in the sorted list.

Assume that the keys are positive integers. The idea for the \textit{radix sort} is to divide the keys into subgroups based on their radix positions. It applies a bucket sort repeatedly for the key values on radix positions, starting from the least-significant position.

Consider sorting the elements with the following keys:

\[331, 454, 230, 34, 343, 45, 59, 453, 345, 231, 9\]

Apply the bucket sort on the last radix position, and the elements are put into the buckets as follows:

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>230</td>
<td>331</td>
<td></td>
<td>343</td>
<td>454</td>
<td>45</td>
<td>345</td>
<td></td>
<td></td>
<td>59</td>
</tr>
</tbody>
</table>

After being removed from the buckets, the elements are in the following order:

\[230, 331, 231, 343, 453, 454, 34, 45, 345, 453, 59, 9\]

Apply the bucket sort on the second-to-last radix position, and the elements are put into the buckets as follows:

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>9</td>
<td></td>
<td></td>
<td></td>
<td>230</td>
<td>331</td>
<td>231</td>
<td>343</td>
<td>454</td>
<td>453</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>34</td>
<td>45</td>
<td>454</td>
<td>59</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

After being removed from the buckets, the elements are in the following order:

\[9, 230, 331, 231, 34, 343, 45, 345, 453, 454, 59\]

(Note that \(9\) is \(009\).)

Apply the bucket sort on the third-to-last radix position, and the elements are put into the buckets as follows:

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>9</td>
<td>34</td>
<td>45</td>
<td>59</td>
<td>230</td>
<td>331</td>
<td>231</td>
<td>343</td>
<td>453</td>
<td>454</td>
</tr>
</tbody>
</table>
After being removed from the buckets, the elements are in the following order:

9, 34, 45, 59, 230, 231, 331, 343, 345, 453, 454

The elements are now sorted.

Radix sort takes $O(dn)$ time to sort $n$ elements with integer keys, where $d$ is the maximum number of the radix positions among all keys.

23.21 Can you sort a list of strings using a bucket sort?
23.22 Show how the radix sort works using the numbers 454, 34, 23, 43, 74, 86, and 76.

23.8 External Sort

You can sort a large amount data using an external sort.

All the sort algorithms discussed in the preceding sections assume that all the data to be sorted are available at one time in internal memory, such as in an array. To sort data stored in an external file, you must first bring the data to the memory and then sort it internally. However, if the file is too large, all the data in the file cannot be brought to memory at one time. This section discusses how to sort data in a large external file. This is called an external sort.

For simplicity, assume that two million int values are stored in a binary file named largedata.dat. This file was created using the program in Listing 23.11.

Listing 23.11 CreateLargeFile.java

import java.io.*;

public class CreateLargeFile {
    public static void main(String[] args) throws Exception {
        DataOutputStream output = new DataOutputStream(new BufferedOutputStream(new FileOutputStream("largedata.dat")));

        for (int i = 0; i < 800004; i++)
            output.writeInt((int)(Math.random() * 1000000));

        output.close();

        // Display first 100 numbers
        DataInputStream input = new DataInputStream(new BufferedInputStream(new FileInputStream("largedata.dat")));
        for (int i = 0; i < 100; i++)
            System.out.print(input.readInt() + " ");

        input.close();
    }
}

A variation of merge sort can be used to sort this file in two phases:

Phase I: Repeatedly bring data from the file to an array, sort the array using an internal sorting algorithm, and output the data from the array to a temporary file. This process is shown in Figure 23.17. Ideally, you want to create a large array, but its maximum size depends on how much memory is allocated to the JVM by the operating system. Assume that the maximum array size is 100,000 int values. In the temporary file, every 100,000...
**int** values are sorted. They are denoted as \( S_1, S_2, \ldots, \) and \( S_k \), where the last segment, \( S_k \), may contain less than 100000 values.

![Diagram of sorting process](image)

**FIGURE 23.17** The original file is sorted in segments.

**Phase II:** Merge a pair of sorted segments (e.g., \( S_1 \) with \( S_2, S_3 \) with \( S_4, \ldots \), and so on) into a larger sorted segment and save the new segment into a new temporary file. Continue the same process until only one sorted segment results. Figure 23.18 shows how to merge eight segments.

![Diagram of merging sorted segments](image)

**FIGURE 23.18** Sorted segments are merged iteratively.

**Note**
It is not necessary to merge two successive segments. For example, you can merge \( S_1 \) with \( S_5 \), \( S_2 \) with \( S_6 \), \( S_3 \) with \( S_7 \) and \( S_4 \) with \( S_8 \), in the first merge step. This observation is useful in implementing Phase II efficiently.

### 23.8.1 Implementing Phase I

Listing 23.12 gives the method that reads each segment of data from a file, sorts the segment, and stores the sorted segments into a new file. The method returns the number of segments.

**LISTING 23.12 Creating Initial Sorted Segments**

```java
1  /** Sort original file into sorted segments */
2  private static int initializeSegments(
3      int segmentSize, String originalFile, String f1)
4  throws Exception {
5      int[] list = new int[segmentSize];
6      DataInputStream input = new DataInputStream(
```
```java
new BufferedInputStream(new FileInputStream(originalFile)));  // original file
DataOutputStream output = new DataOutputStream(
new BufferedOutputStream(new FileOutputStream(f1))));  // file with sorted segments

int numberOfSegments = 0;
while (input.available() > 0) {
    numberOfSegments++;
    int i = 0;
    for (; input.available() > 0 && i < segmentSize; i++) {
        list[i] = input.readInt();
    }
    // Sort an array list[0..i-1]
    java.util.Arrays.sort(list, 0, i);
    // Write the array to f1.dat
    for (int j = 0; j < i; j++) {
        output.writeInt(list[j]);
    }
}
input.close();
output.close();
return numberOfSegments;
```

The method creates an array with the maximum size in line 5, a data input stream for the original file in line 6, and a data output stream for a temporary file in line 8. Buffered streams are used to improve performance.

Lines 14–17 read a segment of data from the file into the array. Line 20 sorts the array. Lines 23–25 write the data in the array to the temporary file.

The number of segments is returned in line 31. Note that every segment has `MAX_ARRAY_SIZE` number of elements except the last segment, which may have fewer elements.

### 23.8.2 Implementing Phase II

In each merge step, two sorted segments are merged to form a new segment. The size of the new segment is doubled. The number of segments is reduced by half after each merge step. A segment is too large to be brought to an array in memory. To implement a merge step, copy half the number of segments from the file `f1.dat` to a temporary file `f2.dat`. Then merge the first remaining segment in `f1.dat` with the first segment in `f2.dat` into a temporary file named `f3.dat`, as shown in Figure 23.19.

```
<table>
<thead>
<tr>
<th>S1</th>
<th>S2</th>
<th>S3</th>
<th>S4</th>
<th>S5</th>
<th>S6</th>
<th>S7</th>
<th>S8</th>
</tr>
</thead>
<tbody>
<tr>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
```

Copy to `f2.dat`

```
<table>
<thead>
<tr>
<th>S1</th>
<th>S2</th>
<th>S3</th>
<th>S4</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
```

Figure 23.19 Sorted segments are merged iteratively.
Note

*f1.dat* may have one segment more than *f2.dat*. If so, move the last segment into *f3.dat* after the merge.

Listing 23.13 gives a method that copies the first half of the segments in *f1.dat* to *f2.dat*. Listing 23.14 gives a method that merges a pair of segments in *f1.dat* and *f2.dat*. Listing 23.15 gives a method that merges two segments.

**LISTING 23.13 Copying First Half Segments**

```java
private static void copyHalfToF2(int numberOfSegments, int segmentSize, DataInputStream f1, DataOutputStream f2) throws Exception {
    for (int i = 0; i < (numberOfSegments / 2) * segmentSize; i++) {
        f2.writeInt(f1.readInt());
    }
}
```

**LISTING 23.14 Merging All Segments**

```java
private static void mergeSegments(int numberOfSegments, int segmentSize, DataInputStream f1, DataInputStream f2, DataOutputStream f3) throws Exception {
    for (int i = 0; i < numberOfSegments; i++) {
        mergeTwoSegments(segmentSize, f1, f2, f3);
    }
    // If f1 has one extra segment, copy it to f3
    while (f1.available() > 0) {
        f3.writeInt(f1.readInt());
    }
}
```

**LISTING 23.15 Merging Two Segments**

```java
private static void mergeTwoSegments(int segmentSize, DataInputStream f1, DataInputStream f2, DataOutputStream f3) throws Exception {
    int intFromF1 = f1.readInt();
    int intFromF2 = f2.readInt();
    int f1Count = 1;
    int f2Count = 1;
    while (true) {
        if (intFromF1 < intFromF2) {
            f3.writeInt(intFromF1);
            if (f1.available() == 0 || f1Count++ >= segmentSize) {
                f3.writeInt(intFromF2);
                break;
            }
        } else {
            intFromF1 = f1.readInt();
            if (f2.available() == 0 || f2Count++ >= segmentSize) {
                f3.writeInt(intFromF1);
                break;
            }
        }
        if (f1.available() == 0) {
            f3.writeInt(intFromF2);
            break;
        }
        if (f2.available() == 0) {
            f3.writeInt(intFromF1);
            break;
        }
    }
}
```
else {
    intFromF2 = f2.readInt();
}

while (f1.available() > 0 && f1Count++ < segmentSize) {
    f3.writeInt(f1.readInt());
}

while (f2.available() > 0 && f2Count++ < segmentSize) {
    f3.writeInt(f2.readInt());
}

23.8.3 Combining Two Phases

Listing 23.16 gives the complete program for sorting int values in largedata.dat and storing the sorted data in sortedfile.dat.

**LISTING 23.16 SortLargeFile.java**

```java
import java.io.*;

public class SortLargeFile {
    public static final int MAX_ARRAY_SIZE = 100000;
    public static final int BUFFER_SIZE = 100000;

    public static void main(String[] args) throws Exception {
        // Sort largedata.dat to sortedfile.dat
        sort("largedata.dat", "sortedfile.dat");

        // Display the first 100 numbers in the sorted file
        displayFile("sortedfile.dat");
    }

    /** Sort data in source file into target file */
    public static void sort(String sourcefile, String targetfile) throws Exception {
        // Implement Phase 1: Create initial segments
        int numberOfSegments = initializeSegments(MAX_ARRAY_SIZE, sourcefile, "f1.dat");

        // Implement Phase 2: Merge segments recursively
        merge(numberOfSegments, MAX_ARRAY_SIZE, "f1.dat", "f2.dat", "f3.dat", targetfile);
    }

    /** Sort original file into sorted segments */
    private static int initializeSegments(int segmentSize, String originalFile, String f1) throws Exception {
        // Same as Listing 23.12, so omitted
    }

    private static void merge(int numberOfSegments, int segmentSize,
        String f1, String f2, String f3, String targetfile) throws Exception {
        if (numberOfSegments > 1) {
            mergeOneStep(numberOfSegments, segmentSize, f1, f2, f3);
        }
    }
}
```
private static void mergeOneStep(int numberOfSegments, int segmentSize, String f1, String f2, String f3)
    throws Exception {
    DataInputStream f1Input = new DataInputStream(new BufferedInputStream(new FileInputStream(f1), BUFFER_SIZE));
    DataOutputStream f2Output = new DataOutputStream(new BufferedOutputStream(new FileOutputStream(f2), BUFFER_SIZE));
    copyHalfToF2(numberOfSegments, segmentSize, f1Input, f2Output);
    f2Output.close();
    DataInputStream f2Input = new DataInputStream(new BufferedInputStream(new FileInputStream(f2), BUFFER_SIZE));
    DataOutputStream f3Output = new DataOutputStream(new BufferedOutputStream(new FileOutputStream(f3), BUFFER_SIZE));
    mergeSegments(numberOfSegments / 2, segmentSize, f1Input, f2Input, f3Output);
    f1Input.close();
    f2Input.close();
    f3Output.close();
}

/** Copy half number of segments from f1.dat to f2.dat */
private static void copyHalfToF2(int numberOfSegments, int segmentSize, DataInputStream f1, DataOutputStream f2)
    throws Exception {
    // Same as Listing 23.13, so omitted
}

/** Merge all segments */
private static void mergeSegments(int numberOfSegments, int segmentSize, DataInputStream f1, DataInputStream f2, DataOutputStream f3) throws Exception {
    // Same as Listing 23.14, so omitted
}

/** Merges two segments */
private static void mergeTwoSegments(int segmentSize, DataInputStream f1, DataInputStream f2, DataOutputStream f3) throws Exception {
    // Same as Listing 23.15, so omitted
}

/** Display the first 100 numbers in the specified file */
public static void displayFile(String filename) {
    try {
    }
DataInputStream input = new DataInputStream(new FileInputStream(filename));
for (int i = 0; i < 100; i++)
    System.out.print(input.readInt() + " ");
input.close();
catch (IOException ex) {
    ex.printStackTrace();
}

Before you run this program, first run Listing 23.11, CreateLargeFile.java, to create the file largedata.dat. Invoking sort("largedata.dat", "sortedfile.dat") (line 9) reads data from largedata.dat and writes sorted data to sortedfile.dat. Invoking displayFile("sortedfile.dat") (line 12) displays the first 100 numbers in the specified file. Note that the files are created using binary I/O. You cannot view them using a text editor such as Notepad.

The sort method first creates initial segments from the original array and stores the sorted segments in a new file, f1.dat (lines 19–20), then produces a sorted file in targetfile (lines 23–24).

The merge method

merge(int numberOfSegments, int segmentSize,
       String f1, String f2, String f3, String targetfile)

merges the segments in f1 into f3 using f2 to assist the merge. The merge method is invoked recursively with many merge steps. Each merge step reduces the numberOfSegments by half and doubles the sorted segment size. After the completion of one merge step, the next merge step merges the new segments in f3 to f2 using f1 to assist the merge. The statement to invoke the new merge method is

merge((numberOfSegments + 1) / 2, segmentSize * 2,
       f3, f1, f2, targetfile);

The numberOfSegments for the next merge step is (numberOfSegments + 1) / 2. For example, if numberOfSegments is 5, numberOfSegments is 3 for the next merge step, because every two segments are merged but one is left unmerged.

The recursive merge method ends when numberOfSegments is 1. In this case, f1 contains sorted data. File f1 is renamed to targetfile (line 45).

23.8.4 External Sort Complexity

In the external sort, the dominating cost is that of I/O. Assume n is the number of elements to be sorted in the file. In Phase I, n number of elements are read from the original file and output to a temporary file. Therefore, the I/O for Phase I is O(n).

In Phase II, before the first merge step, the number of sorted segments is \( \frac{n}{c} \), where c is MAX_ARRAY_SIZE. Each merge step reduces the number of segments by half. Thus, after the first merge step, the number of segments is \( \frac{n}{2c} \). After the second merge step, the number of segments is \( \frac{n}{2^2c} \), and after the third merge step the number of segments is \( \frac{n}{2^3c} \). After \( \log_2 \left( \frac{n}{c} \right) \)
merge steps, the number of segments is reduced to 1. Therefore, the total number of merge
steps is \( \log \left( \frac{n}{c} \right) \).

In each merge step, half the number of segments are read from file \( f_1 \) and then written into
a temporary file \( f_2 \). The remaining segments in \( f_1 \) are merged with the segments in \( f_2 \). The
number of I/Os in each merge step is \( O(n) \). Since the total number of merge steps is \( \log \left( \frac{n}{c} \right) \),
the total number of I/Os is

\[
O(n) \times \log \left( \frac{n}{c} \right) = O(n \log n)
\]

Therefore, the complexity of the external sort is \( O(n \log n) \).

23.23 Describe how external sort works. What is the complexity of the external sort algorithm?

23.24 Ten numbers \( \{2, 3, 4, 0, 5, 6, 7, 9, 8, 1\} \) are stored in the external file \texttt{largetdata.dat}.
Trace the \texttt{SortLargeFile} program by hand with \texttt{MAX_ARRAY_SIZE} 2.

**Key Terms**

- bubble sort 864
- bucket sort 881
- complete binary tree 874
- external sort 883
- heap 875
- heap sort 874
- height of a heap 880
- merge sort 867
- quick sort 870
- radix sort 882

**Chapter Summary**

1. The worst-case complexity for a selection sort, insertion sort, bubble sort, and quick sort
   is \( O(n^2) \).

2. The average-case and worst-case complexity for a merge sort is \( O(n \log n) \). The average
time for a quick sort is also \( O(n \log n) \).

3. Heaps are a useful data structure for designing efficient algorithms such as sorting. You
   learned how to define and implement a heap class, and how to insert and delete elements
to/from a heap.

4. The time complexity for a heap sort is \( O(n \log n) \).

5. Bucket sorts and radix sorts are specialized sorting algorithms for integer keys. These
   algorithms sort keys using buckets rather than by comparing keys. They are more
efficient than general sorting algorithms.

6. A variation of the merge sort—called an external sort—can be applied to sort large
   amounts of data from external files.

**Quiz**

Answer the quiz for this chapter online at \url{www.cs.armstrong.edu/liang/intro10e/test.html}.
Sections 23.3–23.5

23.1 (Generic bubble sort) Write the following two generic methods using bubble sort. The first method sorts the elements using the `Comparable` interface and the second uses the `Comparator` interface.

```java
public static <E extends Comparable<? super E>> void bubbleSort(E[] list)
public static <E> void bubbleSort(E[] list, Comparator<? super E> comparator)
```

23.2 (Generic merge sort) Write the following two generic methods using merge sort. The first method sorts the elements using the `Comparable` interface and the second uses the `Comparator` interface.

```java
public static <E extends Comparable<? super E>> void mergeSort(E[] list)
public static <E> void mergeSort(E[] list, Comparator<? super E> comparator)
```

23.3 (Generic quick sort) Write the following two generic methods using quick sort. The first method sorts the elements using the `Comparable` interface and the second uses the `Comparator` interface.

```java
public static <E extends Comparable<? super E>> void quickSort(E[] list)
public static <E> void quickSort(E[] list, Comparator<? super E> comparator)
```

23.4 (Improve quick sort) The quick sort algorithm presented in the book selects the first element in the list as the pivot. Revise it by selecting the median among the first, middle, and last elements in the list.

*23.5 (Generic heap sort) Write the following two generic methods using heap sort. The first method sorts the elements using the `Comparable` interface and the second uses the `Comparator` interface.

```java
public static <E extends Comparable<? super E>> void heapSort(E[] list)
public static <E> void heapSort(E[] list, Comparator<? super E> comparator)
```

23.6 (Check order) Write the following overloaded methods that check whether an array is ordered in ascending order or descending order. By default, the method checks ascending order. To check descending order, pass `false` to the ascending argument in the method.

```java
public static boolean ordered(int[] list)
public static boolean ordered(int[] list, boolean ascending)
public static boolean ordered(double[] list)
public static boolean ordered(double[] list, boolean ascending)
public static <E extends Comparable<? super E>> boolean ordered(E[] list)
public static <E extends Comparable<? super E>> boolean ordered(E[] list, boolean ascending)
public static <E> boolean ordered(E[] list,
```
Chapter 23  Sorting

Comparator<? super E> comparator)
public static <E> boolean ordered(E[] list, Comparator<? super E> comparator, boolean ascending)

Section 23.6

23.7 (Min-heap) The heap presented in the text is also known as a max-heap, in which each node is greater than or equal to any of its children. A min-heap is a heap in which each node is less than or equal to any of its children. Min-heaps are often used to implement priority queues. Revise the Heap class in Listing 23.9 to implement a min-heap.

*23.8 (Sort using a heap) Implement the following sort method using a heap.

public static <E extends Comparable<E>> void sort(E[] list)

*23.9 (Generic Heap using Comparator) Revise Heap in Listing 23.9, using a generic parameter and a Comparator for comparing objects. Define a new constructor with a Comparator as its argument as follows:

Heap(Comparator<? super E> comparator)

**23.10 (Heap visualization) Write a program that displays a heap graphically, as shown in Figure 23.10. The program lets you insert and delete an element from the heap.

23.11 (Heap clone and equals) Implement the clone and equals method in the Heap class.

Section 23.7

*23.12 (Radix sort) Write a program that randomly generates 1,000,000 integers and sorts them using radix sort.

*23.13 (Execution time for sorting) Write a program that obtains the execution time of selection sort, bubble sort, merge sort, quick sort, heap sort, and radix sort for input size 50,000, 100,000, 150,000, 200,000, 250,000, and 300,000. Your program should create data randomly and print a table like this:

<table>
<thead>
<tr>
<th>Array size</th>
<th>Selection Sort</th>
<th>Bubble Sort</th>
<th>Merge Sort</th>
<th>Quick Sort</th>
<th>Heap Sort</th>
<th>Radix Sort</th>
</tr>
</thead>
<tbody>
<tr>
<td>50,000</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>100,000</td>
<td></td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>150,000</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>200,000</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>250,000</td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>300,000</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

(Hint: You can use the following code template to obtain the execution time.)

long startTime = System.currentTimeMillis();
perform the task;
long endTime = System.currentTimeMillis();
long executionTime = endTime - startTime;

The text gives a recursive quick sort. Write a nonrecursive version in this exercise.
Section 23.8

*23.14 (Execution time for external sorting) Write a program that obtains the execution time of external sorts for integers of size 5,000,000, 10,000,000, 15,000,000, 20,000,000, 25,000,000, and 30,000,000. Your program should print a table like this:

<table>
<thead>
<tr>
<th>File size</th>
<th>5,000,000</th>
<th>10,000,000</th>
<th>15,000,000</th>
<th>20,000,000</th>
<th>25,000,000</th>
<th>30,000,000</th>
</tr>
</thead>
<tbody>
<tr>
<td>Time</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Comprehensive

*23.15 (Selection sort animation) Write a program that animates the selection sort algorithm. Create an array that consists of 20 distinct numbers from 1 to 20 in a random order. The array elements are displayed in a histogram, as shown in Figure 23.20a. Clicking the Step button causes the program to perform an iteration of the outer loop in the algorithm and repaints the histogram for the new array. Color the last bar in the sorted subarray. When the algorithm is finished, display a message to inform the user. Clicking the Reset button creates a new random array for a new start. (You can easily modify the program to animate the insertion algorithm.)

*23.16 (Bubble sort animation) Write a program that animates the bubble sort algorithm. Create an array that consists of 20 distinct numbers from 1 to 20 in a random order. The array elements are displayed in a histogram, as shown in Figure 23.20b. Clicking the Step button causes the program to perform one comparison in the algorithm and repaints the histogram for the new array. Color the bar that represents the number being considered in the swap. When the algorithm is finished, display a message to inform the user. Clicking the Reset button creates a new random array for a new start.

*23.17 (Radix sort animation) Write a program that animates the radix sort algorithm. Create an array that consists of 20 random numbers from 0 to 1,000. The array elements are displayed, as shown in Figure 23.21. Clicking the Step button causes the program to place a number in a bucket. The number that has just been placed is displayed in red. Once all the numbers are placed in the buckets, clicking the Step button collects all the numbers from the buckets and moves...
them back to the array. When the algorithm is finished, clicking the Step button displays a message to inform the user. Clicking the Reset button creates a new random array for a new start.

**Figure 23.21** The program animates radix sort.

*23.18* *(Merge animation)* Write a program that animates the merge of two sorted lists. Create two arrays, `list1` and `list2`, each of which consists of 8 random numbers from 1 to 999. The array elements are displayed, as shown in Figure 23.22a. Clicking the Step button causes the program to move an element from `list1` or `list2` to temp. Clicking the Reset button creates two new random arrays for a new start. When the algorithm is finished, clicking the Step button displays a message to inform the user.

**Figure 23.22** The program animates a merge of two sorted lists. (b) The program animates a partition for quick sort.

*23.19* *(Quick sort partition animation)* Write a program that animates the partition for a quick sort. The program creates a list that consists of 20 random numbers from 1 to 999. The list is displayed, as shown in Figure 23.22b. Clicking the Step button causes the program to move low to the right or high to the left, or swap the elements at low and high. Clicking the Reset button creates a new list of random numbers for a new start. When the algorithm is finished, clicking the Step button displays a message to inform the user.

*23.20* *(Modify merge sort)* Rewrite the `mergeSort` method to recursively sort the first half of the array and the second half of the array without creating new temporary arrays, and then merge the two into a temporary array and copy its contents to the original array, as shown in Figure 23.6b.
IMPLEMENTING LISTS, STACKS, QUEUES, AND PRIORITY QUEUES

Objectives

■ To design common features of lists in an interface and provide skeleton implementation in a convenience abstract class (§24.2).
■ To design and implement an array list using an array (§24.3).
■ To design and implement a linked list using a linked structure (§24.4).
■ To design and implement a stack class using an array list and a queue class using a linked list (§24.5).
■ To design and implement a priority queue using a heap (§24.6).
Chapter 24  Implementing Lists, Stacks, Queues, and Priority Queues

24.1 Introduction

This chapter focuses on implementing data structures.

Lists, stacks, queues, and priority queues are classic data structures typically covered in a data structures course. They are supported in the Java API, and their uses were presented in Chapter 20, Lists, Stacks, Queues, and Priority Queues. This chapter will examine how these data structures are implemented under the hood. Implementation of sets and maps is covered in Chapter 27. Through these examples, you will learn how to design and implement custom data structures.

24.2 Common Features for Lists

Common features of lists are defined in the List interface.

A list is a popular data structure for storing data in sequential order—for example, a list of students, a list of available rooms, a list of cities, a list of books. You can perform the following operations on a list:

- Retrieve an element from the list.
- Insert a new element into the list.
- Delete an element from the list.
- Find out how many elements are in the list.
- Determine whether an element is in the list.
- Check whether the list is empty.

There are two ways to implement a list. One is to use an array to store the elements. Array size is fixed. If the capacity of the array is exceeded, you need to create a new, larger array and copy all the elements from the current array to the new array. The other approach is to use a linked structure. A linked structure consists of nodes. Each node is dynamically created to hold an element. All the nodes are linked together to form a list. Thus you can define two classes for lists. For convenience, let’s name these two classes MyArrayList and MyLinkedList. These two classes have common operations but different implementations.

Design Guide

The common operations can be generalized in an interface or an abstract class. A good strategy is to combine the virtues of interfaces and abstract classes by providing both an interface and a convenience abstract class in the design so that the user can use either of them, whichever is convenient. The abstract class provides a skeletal implementation of the interface, which minimizes the effort required to implement the interface.

Pedagogical Note

For an interactive demo on how array lists and linked lists work, go to www.cs.armstrong.edu/liang/animation/web/ArrayList.html and www.cs.armstrong.edu/liang/animation/web/LinkedList.html, as shown in Figure 24.1.

Let us name the interface MyList and the convenience abstract class MyAbstractList. Figure 24.2 shows the relationship of MyList, MyAbstractList, MyArrayList, and MyLinkedList. The methods in MyList and the methods implemented in MyAbstractList are shown in Figure 24.3. Listing 24.1 gives the source code for MyList.
24.2 Common Features for Lists

**LISTING 24.1** MyList.java

```java
public interface MyList<E> extends java.lang.Iterable<E> {
    /** Add a new element at the end of this list */
    public void add(E e);
    /** Add a new element at the specified index in this list */
    public void add(int index, E e);
    /** Clear the list */
    public void clear();
    /** Return true if this list contains the element */
    public boolean contains(E e);
    /** Return the element from this list at the specified index */
    public E get(int index);
    /** Return the index of the first matching element in this list.
     * Return -1 if no match. */
    public int indexOf(E e);
    /** Return true if this list doesn't contain any elements */
    public boolean isEmpty();
    /** Return the index of the last matching element in this list
     * Return -1 if no match. */
    public int lastIndexOf(E e);
    /** Remove the first occurrence of the element e from this list.
     * Shift any subsequent elements to the left.
     * Return true if the element is removed. */
    public boolean remove(E e);
}
```

**FIGURE 24.2** MyList defines a common interface for MyAbstractList, MyArrayList, and MyLinkedList.

**FIGURE 24.1** The animation tool enables you to see how array lists and linked lists work.
Chapter 24  Implementing Lists, Stacks, Queues, and Priority Queues

```java
public boolean remove(E e);
/** Remove the element at the specified position in this list.
   * Shift any subsequent elements to the left.
   * Return the element that was removed from the list. */
public E remove(int index);
/** Replace the element at the specified position in this list
   * with the specified element and return the old element. */
public Object set(int index, E e);
/** Return the number of elements in this list */
public int size();
```
24.2 Common Features for Lists

LISTING 24.2 MyAbstractList.java

```java
public abstract class MyAbstractList<E> implements MyList<E> {
    protected int size = 0; // The size of the list

    /** Create a default list */
    protected MyAbstractList() {
    }

    /** Create a list from an array of objects */
    protected MyAbstractList(E[] objects) {
        for (int i = 0; i < objects.length; i++)
            add(objects[i]);
    }

    @Override /** Add a new element at the end of this list */
    public void add(E e) {
        add(size, e);
    }

    @Override /** Return true if this list doesn't contain any elements */
    public boolean isEmpty() {
        return size == 0;
    }

    @Override /** Return the number of elements in this list */
    public int size() {
        return size;
    }

    @Override /** Remove the first occurrence of the element e from this list. Shift any subsequent elements to the left. */
    public boolean remove(E e) {
        if (indexOf(e) >= 0) {
            remove(indexOf(e));
            return true;
        } else
            return false;
    }
}
```

The following sections give the implementation for MyArrayList and MyLinkedList, respectively.

Design Guide

Protected data fields are rarely used. However, making size a protected data field in the MyAbstractList class is a good choice. The subclass of MyAbstractList can access size, but nonsubclasses of MyAbstractList in different packages cannot access it. As a general rule, you can declare protected data fields in abstract classes.

24.1 Suppose list is an instance of MyList, can you get an iterator for list using list.iterator()?
24.2 Can you create a list using new MyAbstractList()?
24.3 What methods in MyList are overridden in MyAbstractList?
24.4 What are the benefits of defining both the MyList interface and the MyAbstractList class?
Chapter 24  Implementing Lists, Stacks, Queues, and Priority Queues

24.3 Array Lists

An array list is implemented using an array.

An array is a fixed-size data structure. Once an array is created, its size cannot be changed. Nevertheless, you can still use arrays to implement dynamic data structures. The trick is to create a larger new array to replace the current array, if the current array cannot hold new elements in the list.

Initially, an array, say data of E[] type, is created with a default size. When inserting a new element into the array, first make sure that there is enough room in the array. If not, create a new array twice as large as the current one. Copy the elements from the current array to the new array. The new array now becomes the current array. Before inserting a new element at a specified index, shift all the elements after the index to the right and increase the list size by 1, as shown in Figure 24.4.

**FIGURE 24.4** Inserting a new element into the array requires that all the elements after the insertion point be shifted one position to the right, so that the new element can be inserted at the insertion point.

**Note**
The data array is of type E[]. Each cell in the array actually stores the reference of an object.

To remove an element at a specified index, shift all the elements after the index to the left by one position and decrease the list size by 1, as shown in Figure 24.5.

**FIGURE 24.5** Deleting an element from the array requires that all the elements after the deletion point be shifted one position to the left.

MyArrayList uses an array to implement MyAbstractList, as shown in Figure 24.6. Its implementation is given in Listing 24.3.
24.3 Array Lists

LISTING 24.3 MyArrayList.java

```java
public class MyArrayList<E> extends MyAbstractList<E> {

    public static final int INITIAL_CAPACITY = 16;
    private E[] data = (E[]) new Object[INITIAL_CAPACITY];

    // Create a default list */
    public MyArrayList() {
    }

    // Create a list from an array of objects */
    public MyArrayList(E[] objects) {
        for (int i = 0; i < objects.length; i++)
            add(objects[i]); // Warning: don't use super(objects)!
    }

    @Override // Add a new element at the specified index */
    public void add(int index, E e) {
        ensureCapacity();
        // Move the elements to the right after the specified index
        for (int i = size - 1; i >= index; i--)
            data[i + 1] = data[i];
        // Insert new element to data[index]
        data[index] = e;
        // Increase size by 1
        size++;
    }

    // Create a new larger array, double the current size + 1 */
    private void ensureCapacity() {
        if (size >= data.length) {
            E[] newData = (E[]) (new Object[size * 2 + 1]);
            System.arraycopy(data, 0, newData, 0, size);
            data = newData;
        }
    }
}
```

FIGURE 24.6 MyArrayList implements a list using an array.
@Override /** Clear the list */
public void clear() {
    data = (E[]) new Object[INITIAL_CAPACITY];
    size = 0;
}

@Override /** Return true if this list contains the element */
public boolean contains(E e) {
    for (int i = 0; i < size; i++)
        if (e.equals(data[i])) return true;
    return false;
}

@Override /** Return the element at the specified index */
public E get(int index) {
    checkIndex(index);
    return data[index];
}

private void checkIndex(int index) {
    if (index < 0 || index >= size)
        throw new IndexOutOfBoundsException(
            "index " + index + " out of bounds");
}

@Override /** Return the index of the first matching element
     *  in this list. Return -1 if no match. */
public int indexOf(E e) {
    for (int i = 0; i < size; i++)
        if (e.equals(data[i])) return i;
    return -1;
}

@Override /** Return the index of the last matching element
     *  in this list. Return -1 if no match. */
public int lastIndexOf(E e) {
    for (int i = size - 1; i >= 0; i--)
        if (e.equals(data[i])) return i;
    return -1;
}

@Override /** Remove the element at the specified position
     *  in this list. Shift any subsequent elements to the left.
     *  Return the element that was removed from the list. */
public E remove(int index) {
    checkIndex(index);
    E e = data[index];

    // Shift data to the left
    for (int j = index; j < size - 1; j++)
        data[j] = data[j + 1];

    data[size - 1] = null; // This element is now null

    // Decrement size
    size--;
}
24.3 Array Lists 903
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return e;
}
@Override /** Replace the element at the specified position
* in this list with the specified element. */
public E set(int index, E e) {
checkIndex(index);
E old = data[index];
data[index] = e;
return old;
}
@Override
public String toString() {
StringBuilder result = new StringBuilder("[");

set

toString

for (int i = 0; i < size; i++) {
result.append(data[i]);
if (i < size - 1) result.append(", ");
}
return result.toString() + "]";
}
/** Trims the capacity to current size */
public void trimToSize() {
if (size != data.length) {
E[] newData = (E[])(new Object[size]);
System.arraycopy(data, 0, newData, 0, size);
data = newData;
} // If size == capacity, no need to trim
}
@Override /** Override iterator() defined in Iterable */
public java.util.Iterator<E> iterator() {
return new ArrayListIterator();
}
private class ArrayListIterator
implements java.util.Iterator<E> {
private int current = 0; // Current index
@Override
public boolean hasNext() {
return (current < size);
}
@Override
public E next() {
return data[current++];
}
@Override
public void remove() {
MyArrayList.this.remove(current);
}
}
}

trimToSize

iterator


The constant `INITIAL_CAPACITY` (line 2) is used to create an initial array `data` (line 3). Owing to generics type erasure, you cannot create a generic array using the syntax `new E[INITIAL_CAPACITY]`. To circumvent this limitation, an array of the `Object` type is created in line 3 and cast into `E[]`.

Note that the implementation of the second constructor in `MyArrayList` is the same as for `MyAbstractList`. Can you replace lines 11–12 with `super(objects)`? See Checkpoint Question 24.8 for answers.

The `add(int index, E e)` method (lines 16–28) inserts element `e` at the specified index in the array. This method first invokes `ensureCapacity()` (line 17), which ensures that there is a space in the array for the new element. It then shifts all the elements after the index one position to the right before inserting the element (lines 20–21). After the element is added, `size` is incremented by 1 (line 27). Note that the variable `size` is defined as `protected` in `MyAbstractList`, so it can be accessed in `MyArrayList`.

The `ensureCapacity()` method (lines 31–37) checks whether the array is full. If so, the program creates a new array that doubles the current array size + 1, copies the current array to the new array using the `System.arraycopy` method, and sets the new array as the current array.

The `clear()` method (lines 40–43) creates a new array using the size as `INITIAL_CAPACITY` and resets the variable `size` to 0. The class will work if line 41 is deleted. However, the class will have a memory leak, because the elements are still in the array, although they are no longer needed. By creating a new array and assigning it to `data`, the old array and the elements stored in the old array become garbage, which will be automatically collected by the JVM.

The `contains(E e)` method (lines 46–51) checks whether element `e` is contained in the array by comparing `e` with each element in the array using the `equals` method.

The `get(int index)` method (lines 54–57) checks if `index` is within the range and returns `data[index]` if `index` is in the range.

The `checkIndex(int index)` method (lines 59–63) checks if `index` is within the range. If not, the method throws an `IndexOutOfBoundsException` (line 61).

The `indexOf(E e)` method (lines 67–72) compares element `e` with the elements in the array, starting from the first one. If a match is found, the index of the element is returned; otherwise, `-1` is returned.

The `lastIndexOf(E e)` method (lines 76–81) compares element `e` with the elements in the array, starting from the last one. If a match is found, the index of the element is returned; otherwise, `-1` is returned.

The `remove(int index)` method (lines 86–101) shifts all the elements after the index one position to the left (lines 92–93) and decrements `size` by 1 (line 98). The last element is not used anymore and is set to `null` (line 95).

The `set(int index, E e)` method (lines 105–110) simply assigns `e` to `data[index]` to replace the element at the specified index with element `e`.

The `toString()` method (lines 113–122) overrides the `toString` method in the `Object` class to return a string representing all the elements in the list.

The `trimToSize()` method (lines 125–131) creates a new array whose size matches the current array-list size (line 127), copies the current array to the new array using the `System.arraycopy` method (line 128), and sets the new array as the current array (line 129). Note that if `size == capacity`, there is no need to trim the size of the array.

The `iterator()` method defined in the `java.lang.Iterable` interface is implemented to return an instance on `java.util.Iterator` (lines 134–136). The `ArrayListIterator` class implements `Iterator` with concrete methods for `hasNext`, `next`, and `remove` (lines 143–155). It uses `current` to denote the current position of the element being traversed (line 140).

Listing 24.4 gives an example that creates a list using `MyArrayList`. It uses the `add` method to add strings to the list and the `remove` method to remove strings. Since
MyArrayList implements Iterable, the elements can be traversed using a for-each loop (lines 35–36).

**Listing 24.4** TestMyArrayList.java

```java
public class TestMyArrayList {
    public static void main(String[] args) {
        // Create a list
        MyList<String> list = new MyArrayList<String>();
        create a list

        // Add elements to the list
        list.add("America"); // Add it to the list
        add to list
        System.out.println("(1) " + list);

        list.add(0, "Canada"); // Add it to the beginning of the list
        System.out.println("(2) " + list);

        list.add("Russia"); // Add it to the end of the list
        System.out.println("(3) " + list);

        list.add("France"); // Add it to the end of the list
        System.out.println("(4) " + list);

        list.add(2, "Germany"); // Add it to the list at index 2
        System.out.println("(5) " + list);

        list.add(5, "Norway"); // Add it to the list at index 5
        System.out.println("(6) " + list);

        // Remove elements from the list
        list.remove("Canada"); // Same as list.remove(0) in this case
        remove from list
        System.out.println("(7) " + list);

        list.remove(2); // Remove the element at index 2
        System.out.println("(8) " + list);

        list.remove(list.size() - 1); // Remove the last element
        System.out.println("(9) " + list + "\n(10) ");

        for (String s: list) {
            System.out.print(s.toUpperCase() + " ");
        }
        using iterator
    }
}
```

(1) [America]
(2) [Canada, America]
(3) [Canada, America, Russia]
(4) [Canada, America, Russia, France]
(5) [Canada, America, Germany, Russia, France]
(6) [Canada, America, Germany, Russia, France, Norway]
(7) [America, Germany, Russia, France, Norway]
(8) [America, Germany, France, Norway]
(9) [America, Germany, France]
(10) AMERICA GERMANY FRANCE

24.5 What are the limitations of the array data type?

24.6 MyArrayList is implemented using an array, and an array is a fixed-size data structure. Why is MyArrayList considered a dynamic data structure?
Show the length of the array in `MyArrayList` after each of the following statements is executed.

1. `MyArrayList<Double> list = new MyArrayList<>();
2. list.add(1.5);
3. list.trimToSize();
4. list.add(3.4);
5. list.add(7.4);
6. list.add(17.4);

What is wrong if lines 11–12 in Listing 24.3, `MyArrayList.java`, for

```java
for (int i = 0; i < objects.length; i++)
    add(objects[i]);
```

are replaced by

```java
super(objects);
```

or

```java
data = objects;
size = objects.length;
```

If you change the code in line 33 in Listing 24.3, `MyArrayList.java`, from

```java
E[] newData = (E[])(new Object[size * 2 + 1]);
```

to

```java
E[] newData = (E[])(new Object[size * 2]);
```

the program is incorrect. Can you find the reason?

Will the `MyArrayList` class have memory leak if the following code in line 41 is deleted?

```java
data = (E[])new Object[INITIAL_CAPACITY];
```

The `get(index)` method invokes the `checkIndex(index)` method (lines 59–63 in Listing 24.3) to throw an `IndexOutOfBoundsException` if the index is out of bounds. Suppose the `add(index, e)` is implemented as follows:

```java
public void add(int index, E e) {
    checkIndex(index);
    // Same as lines 17-27 in Listing 24.3 MyArrayList.java
}
```

What will happen if you run the following code?

```java
MyArrayList<String> list = new MyArrayList<>();
list.add("New York");
```

Linked Lists

A linked list is implemented using a linked structure.

Since `MyArrayList` is implemented using an array, the methods `get(int index)` and `set(int index, E e)` for accessing and modifying an element through an index and the
add(E e) method for adding an element at the end of the list are efficient. However, the methods add(int index, E e) and remove(int index) are inefficient, because they require shifting a potentially large number of elements. You can use a linked structure to implement a list to improve efficiency for adding and removing an element at the beginning of a list.

24.4.1 Nodes

In a linked list, each element is contained in an object, called the node. When a new element is added to the list, a node is created to contain it. Each node is linked to its next neighbor, as shown in Figure 24.7.

A node can be created from a class defined as follows:

```java
public class Node<E> {
    E element;
    Node<E> next;

    public Node(E e) {
        element = e;
    }
}
```

![Figure 24.7](image-url)

**Figure 24.7** A linked list consists of any number of nodes chained together.

We use the variable head to refer to the first node in the list, and the variable tail to the last node. If the list is empty, both head and tail are null. Here is an example that creates a linked list to hold three nodes. Each node stores a string element.

Step 1: Declare head and tail.

```java
Node<String> head = null;   // The list is empty now
Node<String> tail = null;
```

head and tail are both null. The list is empty.

Step 2: Create the first node and append it to the list, as shown in Figure 24.8. After the first node is inserted in the list, head and tail point to this node.

```java
head = new Node<"Chicago">();
tail = head;
```

**Figure 24.8** Append the first node to the list. Both head and tail point to this node.

Step 3: Create the second node and append it into the list, as shown in Figure 24.9a. To append the second node to the list, link the first node with the new node. The new node is now the tail node, so you should move tail to point to this new node, as shown in Figure 24.9b.
Step 4: Create the third node and append it to the list, as shown in Figure 24.10a. To append the new node to the list, link the last node in the list with the new node. The new node is now the tail node, so you should move tail to point to this new node, as shown in Figure 24.10b.

Each node contains the element and a data field named next that points to the next element. If the node is the last in the list, its pointer data field next contains the value null. You can use this property to detect the last node. For example, you can write the following loop to traverse all the nodes in the list.

```java
Node current = head;
while (current != null) {
    System.out.println(current.element);
    current = current.next;
}
```

The variable current points initially to the first node in the list (line 1). In the loop, the element of the current node is retrieved (line 3), and then current points to the next node (line 4). The loop continues until the current node is null.

### 24.4.2 The MyLinkedList Class

The MyLinkedList class uses a linked structure to implement a dynamic list. It extends MyAbstractList. In addition, it provides the methods addFirst, addLast, removeFirst, removeLast, getFirst, and getLast, as shown in Figure 24.11.
Assuming that the class has been implemented, Listing 24.5 gives a test program that uses the class.

**Listing 24.5 TestMyLinkedList.java**

```java
public class TestMyLinkedList {
    public static void main(String[] args) {
        // Create a list for strings
        MyLinkedList<String> list = new MyLinkedList<>();

        // Add elements to the list
        list.add("America"); // Add it to the list
        System.out.println("(1) " + list);

        list.add(0, "Canada"); // Add it to the beginning of the list
        System.out.println("(2) " + list);

        list.add("Russia"); // Add it to the end of the list
        System.out.println("(3) " + list);

        list.addLast("France"); // Add it to the end of the list
        System.out.println("(4) " + list);

        list.add(2, "Germany"); // Add it to the list at index 2
        System.out.println("(5) " + list);

        list.add(5, "Norway"); // Add it to the list at index 5
        System.out.println("(6) " + list);

        list.add(0, "Poland"); // Same as list.addFirst("Poland")
        System.out.println("(7) " + list);

        // Remove elements from the list
        list.remove(0); // Same as list.remove("Poland") in this case
        System.out.println("(8) " + list);
    }
}
```

**Figure 24.11** MyLinkedList implements a list using a linked list of nodes.
24.4.3 Implementing `MyLinkedList`

Now let us turn our attention to implementing the `MyLinkedList` class. We will discuss how to implement the methods `addFirst`, `addLast`, `add(index, e)`, `removeFirst`, `removeLast`, and `remove(index)` and leave the other methods in the `MyLinkedList` class as exercises.

24.4.3.1 Implementing `addFirst(e)`

The `addFirst(e)` method creates a new node for holding element `e`. The new node becomes the first node in the list. It can be implemented as follows:

```java
public void addFirst(E e) {
    Node<E> newNode = new Node<>(e); // Create a new node
    newNode.next = head; // Link the new node with the head
    head = newNode; // Head points to the new node
    size++; // Increase list size

    if (tail == null) // The new node is the only node in list
        tail = head;
}
```

The `addFirst(e)` method creates a new node to store the element (line 2) and inserts the node at the beginning of the list (line 3), as shown in Figure 24.12a. After the insertion, `head` should point to this new element node (line 4), as shown in Figure 24.12b.
24.4 Linked Lists

If the list is empty (line 7), both head and tail will point to this new node (line 8). After the node is created, size should be increased by 1 (line 5).

24.4.3.2 Implementing addLast(e)

The addLast(e) method creates a node to hold the element and appends the node at the end of the list. It can be implemented as follows:

```java
public void addLast(E e) {
    Node<E> newNode = new Node<>(e); // Create a new node for e

    if (tail == null) {
        head = tail = newNode; // The only node in list
    } else {
        tail.next = newNode; // Link the new node with the last node
        tail = tail.next; // tail now points to the last node
    }
    size++; // Increase size
}
```

The addLast(e) method creates a new node to store the element (line 2) and appends it to the end of the list. Consider two cases:

1. If the list is empty (line 4), both head and tail will point to this new node (line 5);
2. Otherwise, link the node with the last node in the list (line 8). tail should now point to this new node (line 9). Figure 24.13a and Figure 24.13b show the new node for element e before and after the insertion.

In any case, after the node is created, the size should be increased by 1 (line 12).
### 24.4.3.3 Implementing `add(index, e)`

The `add(index, e)` method inserts an element into the list at the specified index. It can be implemented as follows:

```java
public void add(int index, E e) {
    if (index == 0) addFirst(e); // Insert first
    else if (index >= size) addLast(e); // Insert last
    else { // Insert in the middle
        Node<E> current = head;
        for (int i = 1; i < index; i++)
            current = current.next;
        Node<E> temp = current.next;
        current.next = new Node<E>(e);
        (current.next).next = temp;
        size++;
    }
}
```

There are three cases when inserting an element into the list:

1. If `index` is `0`, invoke `addFirst(e)` (line 2) to insert the element at the beginning of the list.
2. If `index` is greater than or equal to `size`, invoke `addLast(e)` (line 3) to insert the element at the end of the list.
3. Otherwise, create a new node to store the new element and locate where to insert it. As shown in Figure 24.14a, the new node is to be inserted between the nodes `current` and `temp`. The method assigns the new node to `current.next` and assigns `temp` to the new node’s `next`, as shown in Figure 24.14b. The size is now increased by 1 (line 11).

### 24.4.3.4 Implementing `removeFirst()`

The `removeFirst()` method removes the first element from the list. It can be implemented as follows:

```java
public E removeFirst() {
    if (size == 0) return null; // Nothing to delete
    else {
```

Figure 24.13  A new element is added at the end of the list.

![Figure 24.13](image-url)
Consider two cases:

1. If the list is empty, there is nothing to delete, so return null (line 2).

2. Otherwise, remove the first node from the list by pointing head to the second node. Figure 24.15a and Figure 24.15b show the linked list before and after the deletion. The size is reduced by 1 after the deletion (line 6). If the list becomes empty, after removing the element, tail should be set to null (line 7).
24.4.3.5 Implementing `removeLast()`

The `removeLast()` method removes the last element from the list. It can be implemented as follows:

```java
public E removeLast() {
    if (size == 0) return null; // Nothing to remove
    else if (size == 1) { // Only one element in the list
        Node<E> temp = head;
        head = tail = null; // list becomes empty
        size = 0;
        return temp.element;
    } else {
        Node<E> current = head;
        for (int i = 0; i < size - 2; i++)
            current = current.next;
        Node<E> temp = tail;
        tail = current;
        tail.next = null;
        size--;
        return temp.element;
    }
}
```

Consider three cases:

1. If the list is empty, return `null` (line 2).
2. If the list contains only one node, this node is destroyed; `head` and `tail` both become `null` (line 5). The size becomes 0 after the deletion (line 6) and the element value of the deleted node is returned (line 7).
3. Otherwise, the last node is destroyed (line 17) and the `tail` is repositioned to point to the second-to-last node. Figure 24.16a and Figure 24.16b show the last node before and after it is deleted. The size is reduced by 1 after the deletion (line 18) and the element value of the deleted node is returned (line 19).

![Figure 24.16](image-url)
24.4.3.6 Implementing `remove(index)`

The `remove(index)` method finds the node at the specified index and then removes it. It can be implemented as follows:

```java
public E remove(int index) {
    if (index < 0 || index >= size) return null; // Out of range
    else if (index == 0) return removeFirst(); // Remove first
    else if (index == size - 1) return removeLast(); // Remove last
    else {
        Node<E> previous = head;
        for (int i = 1; i < index; i++) {
            previous = previous.next;
        }
        Node<E> current = previous.next;
        previous.next = current.next;
        size--;
        return current.element;
    }
}
```

Consider four cases:

1. If `index` is beyond the range of the list (i.e., `index < 0 || index >= size`), return `null` (line 2).
2. If `index` is 0, invoke `removeFirst()` to remove the first node (line 3).
3. If `index` is `size - 1`, invoke `removeLast()` to remove the last node (line 4).
4. Otherwise, locate the node at the specified `index`. Let `current` denote this node and `previous` denote the node before this node, as shown in Figure 24.17a. Assign `current.next` to `previous.next` to eliminate the current node, as shown in Figure 24.17b.

![Figure 24.17](image.png)

Listing 24.6 gives the implementation of `MyLinkedList`. The implementation of `get(index)`, `indexOf(e)`, `lastIndexOf(e)`, `contains(e)`, and `set(index, e)` is omitted and left as an exercise. The `iterator()` method defined in the `java.lang.Iterable` interface is implemented to return an instance on `java.util.Iterator` (lines 126–128). The `LinkedListIterator` class implements `Iterator` with concrete methods for `hasNext`, `next`, `remove`, `previous`, and `isEmpty`.
next, and remove (lines 134–149). This implementation uses current to point to the current position of the element being traversed (line 132). Initially, current points to the head of the list.

**LISTING 24.6** MyLinkedList.java

```java
public class MyLinkedList<E> extends MyAbstractList<E> {
    private Node<E> head, tail;

    /** Create a default list */
    public MyLinkedList() {
    }

    /** Create a list from an array of objects */
    public MyLinkedList(E[] objects) {
        super(objects);
    }

    /** Return the head element in the list */
    public E getFirst() {
        if (size == 0) {
            return null;
        } else {
            return head.element;
        }
    }

    /** Return the last element in the list */
    public E getLast() {
        if (size == 0) {
            return null;
        } else {
            return tail.element;
        }
    }

    /** Add an element to the beginning of the list */
    public void addFirst(E e) {
        // Implemented in Section 24.4.3.1, so omitted here
    }

    /** Add an element to the end of the list */
    public void addLast(E e) {
        // Implemented in Section 24.4.3.2, so omitted here
    }

    @Override /** Add a new element at the specified index
    * in this list. The index of the head element is 0 */
    public void add(int index, E e) {
        // Implemented in Section 24.4.3.3, so omitted here
    }

    /** Remove the head node and
     * return the object that is contained in the removed node. */
    public E removeFirst() {
        // Implemented in Section 24.4.3.4, so omitted here
    }
```
/** Remove the last node and return the object that is contained in the removed node. */

```java
public E removeLast() {
    // Implemented in Section 24.4.3.5, so omitted here
}
```

@override /** Remove the element at the specified position in this list. Return the element that was removed from the list. */

```java
public E remove(int index) {
    // Implemented earlier in Section 24.4.3.6, so omitted here
}
```

```java
public String toString() {
    Node<E> current = head;
    StringBuilder result = new StringBuilder("[");
    for (int i = 0; i < size; i++) {
        result.append(current.element);
        current = current.next;
        if (current != null) {
            result.append(", "); // Separate two elements with a comma
        } else {
            result.append("]"); // Insert the closing ] in the string
        }
    }

    return result.toString();
}
```

@override /** Clear the list */

```java
public void clear() {
    size = 0;
    head = tail = null;
}
```

@override /** Return true if this list contains the element e */

```java
public boolean contains(E e) {
    System.out.println("Implementation left as an exercise");
    return true;
}
```

@override /** Return the element at the specified index */

```java
public E get(int index) {
    System.out.println("Implementation left as an exercise");
    return null;
}
```

@override /** Return the index of the head matching element in this list. Return -1 if no match. */

```java
public int indexOf(E e) {
    System.out.println("Implementation left as an exercise");
    return 0;
}
```

@override /** Return the index of the last matching element in this list. Return -1 if no match. */

```java
public int lastIndexOf(E e) {
    System.out.println("Implementation left as an exercise");
}
```
return 0;
}

@Override /** Replace the element at the specified position in this list with the specified element. */
public E set(int index, E e) {
    System.out.println("Implementation left as an exercise");
    return null;
}

@Override /** Override iterator() defined in Iterable */
public java.util.Iterator<E> iterator() {
    return new LinkedListIterator();
}

private class LinkedListIterator implements java.util.Iterator<E> {
    private Node<E> current = head; // Current index

    @Override
    public boolean hasNext() {
        return (current != null);
    }

    @Override
    public E next() {
        E e = current.element;
        current = current.next;
        return e;
    }

    @Override
    public void remove() {
        System.out.println("Implementation left as an exercise");
    }
}

// This class is only used in LinkedList, so it is private.
// This class does not need to access any instance members of LinkedList, so it is defined static.
private static class Node<E> {
    public Node(E element) {
        this.element = element;
        Node<E> next;
    }
}

24.4.4 MyArrayList vs. MyLinkedList
Both MyArrayList and MyLinkedList can be used to store a list. MyArrayList is implemented using an array and MyLinkedList is implemented using a linked list. The overhead of MyArrayList is smaller than that of MyLinkedList. However, MyLinkedList is more efficient if you need to insert elements into and delete elements from the beginning of the list. Table 24.1 summarizes the complexity of the methods in MyArrayList and MyLinkedList.

Note that MyArrayList is the same as java.util.ArrayList and MyLinkedList is the same as java.util.LinkedList.
24.4 Linked Lists

24.4.5 Variations of Linked Lists

The linked list introduced in the preceding sections is known as a *singly linked list*. It contains a pointer to the list’s first node, and each node contains a pointer to the next node sequentially. Several variations of the linked list are useful in certain applications.

A *circular, singly linked list* is like a singly linked list, except that the pointer of the last node points back to the first node, as shown in Figure 24.18a. Note that `tail` is not needed for circular linked lists. `head` points to the current node in the list. Insertion and deletion take place at the current node. A good application of a circular linked list is in the operating system that serves multiple users in a timesharing fashion. The system picks a user from a circular list and grants a small amount of CPU time, then moves on to the next user in the list.

<table>
<thead>
<tr>
<th>Methods</th>
<th>MyArrayList/ArrayList</th>
<th>MyLinkedList/LinkedList</th>
</tr>
</thead>
<tbody>
<tr>
<td>add(e: E)</td>
<td>$O(1)$</td>
<td>$O(1)$</td>
</tr>
<tr>
<td>add(index: int, e: E)</td>
<td>$O(n)$</td>
<td>$O(n)$</td>
</tr>
<tr>
<td>clear()</td>
<td>$O(1)$</td>
<td>$O(1)$</td>
</tr>
<tr>
<td>contains(e: E)</td>
<td>$O(n)$</td>
<td>$O(n)$</td>
</tr>
<tr>
<td>get(index: int)</td>
<td>$O(1)$</td>
<td>$O(n)$</td>
</tr>
<tr>
<td>indexOf(e: E)</td>
<td>$O(n)$</td>
<td>$O(n)$</td>
</tr>
<tr>
<td>isEmpty()</td>
<td>$O(1)$</td>
<td>$O(1)$</td>
</tr>
<tr>
<td>remove(e: E)</td>
<td>$O(n)$</td>
<td>$O(n)$</td>
</tr>
<tr>
<td>size()</td>
<td>$O(1)$</td>
<td>$O(1)$</td>
</tr>
<tr>
<td>remove(index: int)</td>
<td>$O(n)$</td>
<td>$O(n)$</td>
</tr>
<tr>
<td>set(index: int, e: E)</td>
<td>$O(n)$</td>
<td>$O(n)$</td>
</tr>
<tr>
<td>addFirst(e: E)</td>
<td>$O(n)$</td>
<td>$O(1)$</td>
</tr>
<tr>
<td>removeFirst()</td>
<td>$O(n)$</td>
<td>$O(1)$</td>
</tr>
</tbody>
</table>

**TABLE 24.1** Time Complexities for Methods in `MyArrayList` and `MyLinkedList`

**FIGURE 24.18**  Linked lists may appear in various forms.
A doubly linked list contains nodes with two pointers. One points to the next node and the other to the previous node, as shown in Figure 24.18b. These two pointers are conveniently called a forward pointer and a backward pointer. Thus, a doubly linked list can be traversed forward and backward. The `java.util.LinkedList` class is implemented using a doubly linked list, and it supports traversing of the list forward and backward using the `ListIterator`.

A circular, doubly linked list is like a doubly linked list, except that the forward pointer of the last node points to the first node and the backward pointer of the first node points to the last node, as shown in Figure 24.18c.

The implementations of these linked lists are left as exercises.

24.12 Both `MyArrayList` and `MyLinkedList` are used to store a list of objects. Why do we need both types of lists?

24.13 Draw a diagram to show the linked list after each of the following statements is executed.
```java
MyLinkedList<Double> list = new MyLinkedList<>();
list.add(1.5);
list.add(6.2);
list.add(3.4);
list.add(7.4);
list.remove(1.5);
list.remove(2);
```

24.14 What is the time complexity of the `addFirst(e)` and `removeFirst()` methods in `MyLinkedList`?

24.15 Suppose you need to store a list of elements. If the number of elements in the program is fixed, what data structure should you use? If the number of elements in the program changes, what data structure should you use?

24.16 If you have to add or delete the elements at the beginning of a list, should you use `MyArrayList` or `MyLinkedList`? If most of the operations on a list involve retrieving an element at a given index, should you use `MyArrayList` or `MyLinkedList`?

24.17 Simplify the code in lines 75-80 in Listing 24.6 using a conditional expression.

24.5 Stacks and Queues

`Stacks can be implemented using array lists and queues can be implemented using linked lists.`

A stack can be viewed as a special type of list whose elements are accessed, inserted, and deleted only from the end (top), as shown in Figure 10.11. A queue represents a waiting list. It can be viewed as a special type of list whose elements are inserted into the end (tail) of the queue, and are accessed and deleted from the beginning (head), as shown in Figure 24.19.
Pedagogical Note
For an interactive demo on how stacks and queues work, go to www.cs.armstrong.edu/liang/animation/web/Stack.html, and www.cs.armstrong.edu/liang/animation/web/Queue.html, as shown in Figure 24.20.

**Figure 24.20** The animation tool enables you to see how stacks and queues work.

Since the insertion and deletion operations on a stack are made only at the end of the stack, it is more efficient to implement a stack with an array list than a linked list. Since deletions are made at the beginning of the list, it is more efficient to implement a queue using a linked list than an array list. This section implements a stack class using an array list and a queue class using a linked list.

There are two ways to design the stack and queue classes:

- Using inheritance: You can define a stack class by extending `ArrayList`, and a queue class by extending `LinkedList`, as shown in Figure 24.21a.
- Using composition: You can define an array list as a data field in the stack class, and a linked list as a data field in the queue class, as shown in Figure 24.21b.

**Figure 24.21** `GenericStack` and `GenericQueue` may be implemented using inheritance or composition.

Both designs are fine, but using composition is better because it enables you to define a completely new stack class and queue class without inheriting the unnecessary and inappropriate methods from the array list and linked list. The implementation of the stack class using the composition approach was given in Listing 19.1, GenericStack.java. Listing 24.7 implements the `GenericQueue` class using the composition approach. Figure 24.22 shows the UML of the class.
Chapter 24  Implementing Lists, Stacks, Queues, and Priority Queues

LISTING 24.7  GenericQueue.java

```java
public class GenericQueue<E> {
    private java.util.LinkedList<E> list = new java.util.LinkedList<>();

    public void enqueue(E e) {
        list.addLast(e);
    }

    public E dequeue() {
        return list.removeFirst();
    }

    public int getSize() {
        return list.size();
    }

    @Override
    public String toString() {
        return "Queue: " + list.toString();
    }
}
```

A linked list is created to store the elements in a queue (lines 2–3). The `enqueue(e)` method (lines 5–7) adds element `e` into the tail of the queue. The `dequeue()` method (lines 9–11) removes an element from the head of the queue and returns the removed element. The `getSize()` method (lines 13–15) returns the number of elements in the queue.

Listing 24.8 gives an example that creates a stack using `GenericStack` and a queue using `GenericQueue`. It uses the `push (enqueue)` method to add strings to the stack (queue) and the `pop (dequeue)` method to remove strings from the stack (queue).

LISTING 24.8  TestStackQueue.java

```java
public class TestStackQueue {
    public static void main(String[] args) {
        // Create a stack
        GenericStack<String> stack = new GenericStack<>();

        // Add elements to the stack
        stack.push("Tom"); // Push it to the stack
        System.out.println("(1) " + stack);
        stack.push("Susan"); // Push it to the the stack
        System.out.println("(2) " + stack);
        stack.push("Kim"); // Push it to the stack
        stack.push("Michael"); // Push it to the stack
        System.out.println("(3) " + stack);
    }
}
```
// Remove elements from the stack
System.out.println("(4) " + stack.pop());
System.out.println("(5) " + stack.pop());
System.out.println("(6) " + stack);

// Create a queue
GenericQueue<String> queue = new GenericQueue<>();

// Add elements to the queue
queue.enqueue("Tom"); // Add it to the queue
System.out.println("(7) " + queue);
queue.enqueue("Susan"); // Add it to the queue
System.out.println("(8) " + queue);
queue.enqueue("Kim"); // Add it to the queue
queue.enqueue("Michael"); // Add it to the queue
System.out.println("(9) " + queue);

// Remove elements from the queue
System.out.println("(10) " + queue.dequeue());
System.out.println("(11) " + queue.dequeue());
System.out.println("(12) " + queue);
}

(1) stack: [Tom]
(2) stack: [Tom, Susan]
(3) stack: [Tom, Susan, Kim, Michael]
(4) Michael
(5) Kim
(6) stack: [Tom, Susan]
(7) Queue: [Tom]
(8) Queue: [Tom, Susan]
(9) Queue: [Tom, Susan, Kim, Michael]
(10) Tom
(11) Susan
(12) Queue: [Kim, Michael]

For a stack, the push(e) method adds an element to the top of the stack, and the pop() method removes the top element from the stack and returns the removed element. It is easy to see that the time complexity for the push and pop methods is O(1).

For a queue, the enqueue(e) method adds an element to the tail of the queue, and the dequeue() method removes the element from the head of the queue. It is easy to see that the time complexity for the enqueue and dequeue methods is O(1).

24.18 You can use inheritance or composition to design the data structures for stacks and queues. Discuss the pros and cons of these two approaches.

24.19 If LinkedList is replaced by ArrayList in lines 2–3 in Listing 24.7 GenericQueue.java, what will be the time complexity for the enqueue and dequeue methods?

24.20 Which lines of the following code are wrong?
1 List<String> list = new ArrayList<>();
2 list.add("Tom");
3 list = new LinkedList<>();
4 list.add("Tom");
5 list = new GenericStack<>();
6 list.add("Tom");
24.6 Priority Queues

Priority queues can be implemented using heaps.

An ordinary queue is a first-in, first-out data structure. Elements are appended to the end of the queue and removed from the beginning. In a priority queue, elements are assigned with priorities. When accessing elements, the element with the highest priority is removed first. For example, the emergency room in a hospital assigns priority numbers to patients; the patient with the highest priority is treated first.

A priority queue can be implemented using a heap, in which the root is the object with the highest priority in the queue. Heaps were introduced in Section 23.6, Heap Sort. The class diagram for the priority queue is shown in Figure 24.23. Its implementation is given in Listing 24.9.

![Figure 24.23 MyPriorityQueue uses a heap to provide a largest-in, first-out data structure.](image)

### LISTING 24.9 MyPriorityQueue.java

```java
public class MyPriorityQueue<E extends Comparable<E>> {
    private Heap<E> heap = new Heap<>();

    public void enqueue(E newObject) {
        heap.add(newObject);
    }

    public E dequeue() {
        return heap.remove();
    }

    public int getSize() {
        return heap.getSize();
    }
}
```

Listing 24.10 gives an example of using a priority queue for patients. The `Patient` class is defined in lines 19–37. Four patients are created with associated priority values in lines 3–6. Line 8 creates a priority queue. The patients are enqueued in lines 10–13. Line 16 dequeues a patient from the queue.

### LISTING 24.10 TestPriorityQueue.java

```java
public class TestPriorityQueue {
    public static void main(String[] args) {
        Patient patient1 = new Patient("John", 2);
        Patient patient2 = new Patient("Jim", 1);
        Patient patient3 = new Patient("Tim", 5);
        Patient patient4 = new Patient("Cindy", 7);

        MyPriorityQueue<Patient> priorityQueue = new MyPriorityQueue<>();
        priorityQueue.enqueue(patient1);
        priorityQueue.enqueue(patient2);
    }
```
```java
        priorityQueue.enqueue(patient3);
        priorityQueue.enqueue(patient4);
        while (priorityQueue.getSize() > 0)
            System.out.print(priorityQueue.dequeue() + " ");
    }
    static class Patient implements Comparable<Patient> {
        private String name;
        private int priority;
        public Patient(String name, int priority) {
            this.name = name;
            this.priority = priority;
        }
        @Override
        public String toString() {
            return name + "(priority:" + priority + ")";
        }
        @Override
        public int compareTo(Patient patient) {
            return this.priority - patient.priority;
        }
    }
```

Cindy(priority:7) Tim(priority:5) John(priority:2) Jim(priority:1)

### 24.21 What is a priority queue?  

### 24.22 What are the time complexity of the `enqueue`, `dequeue`, and `getSize` methods in `MyPriorityQueue`?  

### 24.23 Which of the following statements are wrong?

1. MyPriorityQueue<Object> q1 = new MyPriorityQueue<>();
2. MyPriorityQueue<Number> q2 = new MyPriorityQueue<>();
3. MyPriorityQueue<Integer> q3 = new MyPriorityQueue<>();
4. MyPriorityQueue<Date> q4 = new MyPriorityQueue<>();
5. MyPriorityQueue<String> q5 = new MyPriorityQueue<>();

### Chapter Summary

1. You learned how to implement array lists, linked lists, stacks, and queues.
2. To define a data structure is essentially to define a class. The class for a data structure should use data fields to store data and provide methods to support operations such as insertion and deletion.
3. To create a data structure is to create an instance from the class. You can then apply the methods on the instance to manipulate the data structure, such as inserting an element into the data structure or deleting an element from the data structure.
4. You learned how to implement a priority queue using a heap.
**Quiz**

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/test.html.

**PROGRAMMING EXERCISES**

**24.1** *(Add set operations in MyList)* Define the following methods in `MyList` and implement them in `MyAbstractList`:

```java
/** Adds the elements in otherList to this list. * Returns true if this list changed as a result of the call */
public boolean addAll(MyList<E> otherList);
```

```java
/** Removes all the elements in otherList from this list * Returns true if this list changed as a result of the call */
public boolean removeAll(MyList<E> otherList);
```

```java
/** Retains the elements in this list that are also in otherList * Returns true if this list changed as a result of the call */
public boolean retainAll(MyList<E> otherList);
```

Write a test program that creates two `MyArrayList` s, `list1` and `list2`, with the initial values `"Tom", "George", "Peter", "Jean", "Jane"` and `"Tom", "George", "Michael", "Michelle", "Daniel"`. Then perform the following operations:

- Invokes `list1.addAll(list2)`, and displays `list1` and `list2`.
- Recreates `list1` and `list2` with the same initial values, invokes `list1.removeAll(list2)`, and displays `list1` and `list2`.
- Recreates `list1` and `list2` with the same initial values, invokes `list1.retainAll(list2)`, and displays `list1` and `list2`.

**24.2** *(Implement MyLinkedList)* The implementations of the methods `contains(E e), get(int index), indexOf(E e), lastIndexOf(E e),` and `set(int index, E e)` are omitted in the text. Implement these methods.

**24.3** *(Implement a doubly linked list)* The `MyLinkedList` class used in Listing 24.6 is a one-way directional linked list that enables one-way traversal of the list. Modify the `Node` class to add the new data field name `previous` to refer to the previous node in the list, as follows:

```java
public class Node<E> {
  E element;
  Node<E> next;
  Node<E> previous;

  public Node(E e) {
    element = e;
  }
}
```

Implement a new class named `TwoWayLinkedList` that uses a doubly linked list to store elements. The `MyLinkedList` class in the text extends `MyAbstractList`. Define `TwoWayLinkedList` to extend the `java.util.AbstractSequentialList` class. You need to implement all the methods defined in `MyLinkedList` as well as the methods `ListIterator()`
and `listIterator(int index)`. Both return an instance of `java.util.ListIterator<T>`. The former sets the cursor to the head of the list and the latter to the element at the specified index.

24.4 *(Use the `GenericStack` class)* Write a program that displays the first 50 prime numbers in descending order. Use a stack to store the prime numbers.

24.5 *(Implement `GenericQueue` using inheritance)* In Section 24.5, Stacks and Queues, `GenericQueue` is implemented using composition. Define a new queue class that extends `java.util.LinkedList`.

**24.6 *(Generic `PriorityQueue` using `Comparator`)* Revise `MyPriorityQueue` in Listing 24.9, using a generic parameter for comparing objects. Define a new constructor with a `Comparator` as its argument as follows:

```java
PriorityQueue(Comparator<? super E> comparator)
```

**24.7 *(Animation: linked list)* Write a program to animate search, insertion, and deletion in a linked list, as shown in Figure 24.1b. The `Search` button searches the specified value in the list. The `Delete` button deletes the specified value from the list. The `Insert` button appends the value into the list if the index is not specified; otherwise, it inserts the value into the specified index in the list.

**24.8 *(Animation: array list)* Write a program to animate search, insertion, and deletion in an array list, as shown in Figure 24.1a. The `Search` button searches the specified value in the list. The `Delete` button deletes the specified value from the list. The `Insert` button appends the value into the list if the index is not specified; otherwise, it inserts the value into the specified index in the list.

**24.9 *(Animation: array list in slow motion)* Improve the animation in the preceding programming exercise by showing the insertion and deletion operations in a slow motion, as shown at `http://www.cs.armstrong.edu/liang/animation/ArrayListAnimationInSlowMotion.html`.

24.10 *(Animation: stack)* Write a program to animate push and pop in a stack, as shown in Figure 24.20a.

**24.11 *(Animation: doubly linked list)* Write a program to animate search, insertion, and deletion in a doubly linked list, as shown in Figure 24.24. The `Search` button searches the specified value in the list. The `Delete` button deletes the specified value from the list. The `Insert` button appends the value into the list if the index is not specified; otherwise, it inserts the value into the specified index in the list. Also add two buttons named `Forward Traversal` and `Backward Traversal` for displaying the elements in a forward and backward order, respectively, using iterators.

![Exercise24_11: Doubly Linked List Animation](image)

**Figure 24.24** The program animates the work of a doubly linked list.
**24.12** (*Animation: queue*) Write a program to animate the **enqueue** and **dequeue** operations on a queue, as shown in Figure 24.20b.

**24.13** (*Fibonacci number iterator*) Define an iterator class named **FibonacciIterator** for iterating Fibonacci numbers. The constructor takes an argument that specifies the limit of the maximum Fibonacci number. For example, new **FibonacciIterator(23302)** creates an iterator that iterates Fibonacci numbers less than or equal to 23302. Write a test program that uses this iterator to display all Fibonacci numbers less than or equal to **100000**.

**24.14** (*Prime number iterator*) Define an iterator class named **PrimeIterator** for iterating prime numbers. The constructor takes an argument that specifies the limit of the maximum prime number. For example, new **PrimeIterator(23302)** creates an iterator that iterates prime numbers less than or equal to 23302. Write a test program that uses this iterator to display all prime numbers less than or equal to **100000**.

**24.15** (Test **MyArrayList**) Design and write a complete test program to test if the **MyArrayList** class in Listing 24.3 meets all requirements.

**24.16** (Test **MyLinkedList**) Design and write a complete test program to test if the **MyLinkedList** class in Listing 24.6 meets all requirements.
Binary Search Trees

Objectives

- To design and implement a binary search tree (§25.2).
- To represent binary trees using linked data structures (§25.2.1).
- To search an element in a binary search tree (§25.2.2).
- To insert an element into a binary search tree (§25.2.3).
- To traverse elements in a binary tree (§25.2.4).
- To design and implement the Tree interface, AbstractTree class, and the BST class (§25.2.5).
- To delete elements from a binary search tree (§25.3).
- To display a binary tree graphically (§25.4).
- To create iterators for traversing a binary tree (§25.5).
- To implement Huffman coding for compressing data using a binary tree (§25.6).
25.1 Introduction

A tree is a classic data structure with many important applications.

A tree provides a hierarchical organization in which data are stored in the nodes. This chapter introduces binary search trees. You will learn how to construct a binary search tree, how to search an element, insert an element, delete an element, and traverse elements in a binary search tree. You will also learn how to define and implement a custom data structure for a binary search tree.

25.2 Binary Search Trees

A binary search tree can be implemented using a linked structure.

Recall that lists, stacks, and queues are linear structures that consist of a sequence of elements. A binary tree is a hierarchical structure. It either is empty or consists of an element, called the root, and two distinct binary trees, called the left subtree and right subtree, either or both of which may be empty. Examples of binary trees are shown in Figure 25.1.

FIGURE 25.1 Each node in a binary tree has zero, one, or two subtrees.

The length of a path is the number of the edges in the path. The depth of a node is the length of the path from the root to the node. The set of all nodes at a given depth is sometimes called a level of the tree. Siblings are nodes that share the same parent node. The root of a left (right) subtree of a node is called a left (right) child of the node. A node without children is called a leaf. The height of a nonempty tree is the length of the path from the root node to its furthest leaf. The height of a tree that contains a single node is 0. Conventionally, the height of an empty tree is −1. Consider the tree in Figure 25.1a. The length of the path from node 60 to 45 is 2. The depth of node 60 is 0, the depth of node 55 is 1, and the depth of node 45 is 2. The height of the tree is 2. Nodes 45 and 57 are siblings. Nodes 45, 57, 67, and 107 are at the same level.

A special type of binary tree called a binary search tree (BST) is often useful. A BST (with no duplicate elements) has the property that for every node in the tree, the value of any node in its left subtree is less than the value of the node, and the value of any node in its right subtree is greater than the value of the node. The binary trees in Figure 25.1 are all BSTs.

Pedagogical Note

For an interactive GUI demo to see how a BST works, go to www.cs.armstrong.edu/liang/animation/web/BST.html, as shown in Figure 25.2.
25.2 Binary Search Trees

25.2.1 Representing Binary Search Trees

A binary tree can be represented using a set of linked nodes. Each node contains a value and two links named left and right that reference the left child and right child, respectively, as shown in Figure 25.3.

A node can be defined as a class, as follows:

```java
class TreeNode<E> {
    protected E element;
    protected TreeNode<E> left;
    protected TreeNode<E> right;

    public TreeNode(E e) {
        element = e;
    }
}
```
Chapter 25  Binary Search Trees

The variable `root` refers to the root node of the tree. If the tree is empty, `root` is `null`. The following code creates the first three nodes of the tree in Figure 25.3.

```java
// Create the root node
TreeNode<Integer> root = new TreeNode<>(60);

// Create the left child node
root.left = new TreeNode<>(55);

// Create the right child node
root.right = new TreeNode<>(100);
```

### 25.2.2 Searching for an Element

To search for an element in the BST, you start from the root and scan down from it until a match is found or you arrive at an empty subtree. The algorithm is described in Listing 25.1.

Let `current` point to the root (line 2). Repeat the following steps until `current` is `null` (line 4) or the element matches `current.element` (line 12).

- If `element` is less than `current.element`, assign `current.left` to `current` (line 6).
- If `element` is greater than `current.element`, assign `current.right` to `current` (line 9).
- If `element` is equal to `current.element`, return `true` (line 12).

If `current` is `null`, the subtree is empty and the element is not in the tree (line 14).

**Listing 25.1 Searching for an Element in a BST**

```java
public boolean search(E element) {
    TreeNode<E> current = root; // Start from the root
    while (current != null) {
        if (element < current.element) {
            current = current.left; // Go left
        } else if (element > current.element) {
            current = current.right; // Go right
        } else { // Element matches current.element
            return true; // Element is found
        }
    }
    return false; // Element is not in the tree
}
```

### 25.2.3 Inserting an Element into a BST

To insert an element into a BST, you need to locate where to insert it in the tree. The key idea is to locate the parent for the new node. Listing 25.2 gives the algorithm.

**Listing 25.2 Inserting an Element into a BST**

```java
boolean insert(E e) {
    if (tree is empty) {
        // Create the node for e as the root;
        else {
            // Locate the parent node
            parent = current = root;
            while (current != null)
```
if (e < the value in current.element) {
    parent = current; // Keep the parent
    current = current.left; // Go left
}
else if (e > the value in current.element) {
    parent = current; // Keep the parent
    current = current.right; // Go right
}
else
    return false; // Duplicate node not inserted

// Create a new node for e and attach it to parent
return true; // Element inserted

If the tree is empty, create a root node with the new element (lines 2–3). Otherwise, locate the parent node for the new element node (lines 6–17). Create a new node for the element and link this node to its parent node. If the new element is less than the parent element, the node for the new element will be the left child of the parent. If the new element is greater than the parent element, the node for the new element will be the right child of the parent.

For example, to insert 101 into the tree in Figure 25.3, after the while loop finishes in the algorithm, parent points to the node for 107, as shown in Figure 25.4a. The new node for 101 becomes the left child of the parent. To insert 59 into the tree, after the while loop finishes in the algorithm, the parent points to the node for 57, as shown in Figure 25.4b. The new node for 59 becomes the right child of the parent.

25.2.4 Tree Traversal

Tree traversal is the process of visiting each node in the tree exactly once. There are several ways to traverse a tree. This section presents inorder, postorder, preorder, depth-first, and breadth-first traversals.

With inorder traversal, the left subtree of the current node is visited first recursively, then the current node, and finally the right subtree of the current node recursively. The inorder traversal displays all the nodes in a BST in increasing order.

With postorder traversal, the left subtree of the current node is visited recursively first, then recursively the right subtree of the current node, and finally the current node itself. An application of postorder is to find the size of the directory in a file system. As shown in...
Figure 25.5, each directory is an internal node and a file is a leaf node. You can apply postorder to get the size of each file and subdirectory before finding the size of the root directory.

With preorder traversal, the current node is visited first, then recursively the left subtree of the current node, and finally the right subtree of the current node recursively. Depth-first traversal is the same as preorder traversal. An application of preorder is to print a structured document. As shown in Figure 25.6, you can print a book’s table of contents using preorder traversal.

**FIGURE 25.5** A directory contains files and subdirectories.

**FIGURE 25.6** A tree can be used to represent a structured document such as a book and its chapters and sections.

**Note**

You can reconstruct a binary search tree by inserting the elements in their preorder. The reconstructed tree preserves the parent and child relationship for the nodes in the original binary search tree.

With breadth-first traversal, the nodes are visited level by level. First the root is visited, then all the children of the root from left to right, then the grandchildren of the root from left to right, and so on.

For example, in the tree in Figure 25.4b, the inorder is

45 55 57 59 60 67 100 101 107

The postorder is

45 59 57 55 67 101 107 100 60

The preorder is

60 55 45 57 59 100 67 107 101

The breadth-first traversal is

60 55 100 45 57 67 107 59 101
You can use the following tree to help remember inorder, postorder, and preorder.

The inorder is 1 + 2, the postorder is 1 2 +, and the preorder is + 1 2.

25.2.5 The BST Class
Following the design pattern of the Java Collections Framework API, we use an interface named Tree to define all common operations for trees and provide an abstract class named AbstractTree that partially implements Tree, as shown in Figure 25.7. A concrete BST class can be defined to extend AbstractTree, as shown in Figure 25.8.

![Figure 25.7 The Tree interface defines common operations for trees, and the AbstractTree class partially implements Tree.](image)

Listings 25.3, 25.4, and 25.5 give the implementations for Tree, AbstractTree, and BST.

**LISTING 25.3 Tree.java**

```java
1 public interface Tree<E> extends Iterable<E> {
2     // Returns true if the element is in the tree */
3     public boolean search(E e);
4     // Insert element e into the binary search tree.
5     // Return true if the element is inserted successfully. */
6     public boolean insert(E e);
7     // Returns an iterator for traversing the elements in this collection
8     Iterator<E> iterator();
9     // Returns true if the specified element is in the tree.
10    public boolean search(E e);
11    // Returns true if the element is added successfully.
12    public boolean insert(E e);
13    // Returns true if the element is removed from the tree successfully.
14    public boolean delete(E e);
15    // Prints the nodes in inorder traversal.
16    public void preorder();
17    // Prints the nodes in preorder traversal.
18    public void inorder();
19    // Prints the nodes in postorder traversal.
20    public void postorder();
21    // Returns the number of elements in the tree.
22    public int getSize();
23    // Returns true if the tree is empty.
24    public boolean isEmpty();
25    // Removes all elements from the tree.
26    public void clear();
`
/** Delete the specified element from the tree. */
public boolean delete(E e);

/** Inorder traversal from the root */
public void inorder();

/** Postorder traversal from the root */
public void postorder();

/** Preorder traversal from the root */
public void preorder();

/** Get the number of nodes in the tree */
public int getSize();

/** Return true if the tree is empty */
public boolean isEmpty();
25.2 Binary Search Trees

```java
public boolean isEmpty() {
    return getSize() == 0;
}
```

LISTING 25.5 BST.java

```java
public class BST<E extends Comparable<E>> extends AbstractTree<E> {
    protected TreeNode<E> root;
    protected int size = 0;

    /* Create a default binary search tree */
    public BST() {
    }

    /* Create a binary search tree from an array of objects */
    public BST(E[] objects) {
        for (int i = 0; i < objects.length; i++)
            insert(objects[i]);
    }

    @Override /* Return true if the element is in the tree */
    public boolean search(E e) {
        TreeNode<E> current = root; // Start from the root
        while (current != null) {
            if (e.compareTo(current.element) < 0) {
                current = current.left;
            } else if (e.compareTo(current.element) > 0) {
                current = current.right;
            } else // element matches current.element
                return true; // Element is found
        }
        return false;
    }

    @Override /* Insert element e into the binary search tree. */
    * Return true if the element is inserted successfully. */
    public boolean insert(E e) {
        if (root == null)
            root = createNewNode(e); // Create a new root
        else {
            // Locate the parent node
            TreeNode<E> parent = null;
            TreeNode<E> current = root;
            while (current != null) {
                if (e.compareTo(current.element) < 0) {
                    parent = current;
                    current = current.left;
                } else if (e.compareTo(current.element) > 0) {
                    parent = current;
                    current = current.right;
                } else // element already in tree
                    return false; // Duplicate node not inserted
            }
        }
        return true; // Element is inserted successfully.
    }
```
// Create the new node and attach it to the parent node
if (e.compareTo(parent.element) < 0)
    parent.left = createNewNode(e);
else
    parent.right = createNewNode(e);
}

size++;
return true; // Element inserted successfully
}

protected TreeNode<E> createNewNode(E e) {
    return new TreeNode<>(e);
}

@Override /** Inorder traversal from the root */
public void inorder() {
inorder(root);
}

/** Inorder traversal from a subtree */
protected void inorder(TreeNode<E> root) {
    if (root == null)
return;
    inorder(root.left);
    System.out.print(root.element + " ");
inorder(root.right);
}

@Override /** Postorder traversal from the root */
public void postorder() {
postorder(root);
}

/** Postorder traversal from a subtree */
protected void postorder(TreeNode<E> root) {
    if (root == null)
return;
    System.out.print(root.element + " ");
    postorder(root.left);
    postorder(root.right);
}

@Override /** Preorder traversal from the root */
public void preorder() {
preorder(root);
}

/** Preorder traversal from a subtree */
protected void preorder(TreeNode<E> root) {
    if (root == null)
return;
    System.out.print(root.element + " ");
    preorder(root.left);
    preorder(root.right);
}

/** This inner class is static, because it does not access
 any instance members defined in its outer class */
public static class TreeNode<E extends Comparable<E>> {
protected E element;
protected TreeNode<E> left;
protected TreeNode<E> right;

public TreeNode(E e) {
    element = e;
}

@Override /** Get the number of nodes in the tree */
public int getSize() {
    return size;
}

/** Returns the root of the tree */
public TreeNode<E> getRoot() {
    return root;
}

/** Returns a path from the root leading to the specified element */
public java.util.ArrayList<TreeNode<E>> path(E e) {
    java.util.ArrayList<TreeNode<E>> list =
    new java.util.ArrayList<>();
    TreeNode<E> current = root; // Start from the root

    while (current != null) {
        list.add(current); // Add the node to the list
        if (e.compareTo(current.element) < 0) {
            current = current.left;
        } else if (e.compareTo(current.element) > 0) {
            current = current.right;
        } else
            break;
    }

    return list; // Return an array list of nodes
}

@Override /** Delete an element from the binary search tree. */
public boolean delete(E e) {
    TreeNode<E> parent = null;
    TreeNode<E> current = root; // Start from the root

    while (current != null) {
        if (e.compareTo(current.element) < 0) {
            parent = current;
            current = current.left;
        } else if (e.compareTo(current.element) > 0) {
            parent = current;
            current = current.right;
        } else
            break; // Element is in the tree pointed at by current
    }

    if (current == null)
        return false; // Element is not in the tree

    return false; // Element is not in the tree
Case 1

// Case 1: current has no left child
if (current.left == null) {
    // Connect the parent with the right child of the current node
    if (parent == null) {
        root = current.right;
    } else {
        if (e.compareTo(parent.element) < 0)
            parent.left = current.right;
        else
            parent.right = current.right;
    }
}

Case 2

// Case 2: The current node has a left child.
locate parentOfRightMost
TreeNode<E> parentOfRightMost = current;
locate rightMost
TreeNode<E> rightMost = current.left;

while (rightMost.right != null) {
    parentOfRightMost = rightMost;
    rightMost = rightMost.right; // Keep going to the right
}

// Replace the element in current by the element in rightMost
current.element = rightMost.element;

// Eliminate rightmost node
if (parentOfRightMost.right == rightMost)
    parentOfRightMost.right = rightMost.left;
else
    // Special case: parentOfRightMost == current
    parentOfRightMost.left = rightMost.left;

reduce size
size--;

successful deletion
return true; // Element deleted successfully

@Override /** Obtain an iterator. Use inorder. */
public java.util.Iterator<E> iterator() {
    return new InorderIterator();
}

// Inner class InorderIterator
private class InorderIterator implements java.util.Iterator<E> {
    // Store the elements in a list
    private java.util.ArrayList<E> list =
        new java.util.ArrayList<>();
    int current = 0; // Point to the current element in list
    public InorderIterator() {
        inorder(); // Traverse binary tree and store elements in list
    }

    /** Inorder traversal from the root*/
    private void inorder() {
        inorder(root);
    }
234 }  
235 /** Inorder traversal from a subtree */  
236 private void inorder(TreeNode<E> root) {  
237     if (root == null) return;  
238     inorder(root.left);  
239     list.add(root.element);  
240     inorder(root.right);  
241 }  
242  
243 @Override /** More elements for traversing? */  
244 public boolean hasNext() {  
245     if (current < list.size())  
246         return true;  
247     return false;  
248 }  
249  
250 @Override /** Get the current element and move to the next */  
251 public E next() {  
252     return list.get(current++);  
253 }  
254  
255 @Override /** Remove the current element */  
256 public void remove() {  
257     delete(list.get(current)); // Delete the current element  
258     list.clear(); // Clear the list  
259     inorder(); // Rebuild the list  
260 }  
261  
262 /** Remove all elements from the tree */  
263 public void clear() {  
264     root = null;  
265     size = 0;  
266 }  
267  
268 The insert(E e) method (lines 36–64) creates a node for element e and inserts it into the tree. If the tree is empty, the node becomes the root. Otherwise, the method finds an appropriate parent for the node to maintain the order of the tree. If the element is already in the tree, the method returns false; otherwise it returns true.

The inorder() method (lines 71–81) invokes inorder(root) to traverse the entire tree. The method inorder(TreeNode root) traverses the tree with the specified root. This is a recursive method. It recursively traverses the left subtree, then the root, and finally the right subtree. The traversal ends when the tree is empty.

The postorder() method (lines 84–94) and the preorder() method (lines 97–107) are implemented similarly using recursion.

The path(E e) method (lines 132–150) returns a path of the nodes as an array list. The path starts from the root leading to the element. The element may not be in the tree. For example, in Figure 25.4a, path(45) contains the nodes for elements 60, 55, and 45, and path(58) contains the nodes for elements 60, 55, and 57.

The implementation of delete() and iterator() (lines 155–269) will be discussed in Sections 25.3 and 25.5.

Listing 25.6 gives an example that creates a binary search tree using BST (line 4). The program adds strings into the tree (lines 5–11), traverses the tree in inorder, postorder, and preorder (lines 14–20), searches for an element (line 24), and obtains a path from the node containing Peter to the root (lines 28–31).
List 25.6  TestBST.java

```java
public class TestBST {
    public static void main(String[] args) {
        // Create a BST
        BST<String> tree = new BST<>();
        tree.insert("George");
        tree.insert("Michael");
        tree.insert("Tom");
        tree.insert("Adam");
        tree.insert("Jones");
        tree.insert("Peter");
        tree.insert("Daniel");

        // Traverse tree
        System.out.print("Inorder (sorted): ");
        tree.inorder();
        System.out.print("Postorder: ");
        tree.postorder();
        System.out.print("Preorder: ");
        tree.preorder();
        System.out.print("The number of nodes is "+ tree.getSize());

        // Search for an element
        System.out.print("Is Peter in the tree? "+
                tree.search("Peter"));

        // Get a path from the root to Peter
        System.out.print("A path from the root to Peter is: ");
        java.util.ArrayList<BST.TreeNode<String>> path = tree.path("Peter");
        for (int i = 0; path != null && i < path.size(); i++)
            System.out.print(path.get(i).element + " ");

        Integer[] numbers = {2, 4, 3, 1, 8, 5, 6, 7};
        BST<Integer> intTree = new BST<>(numbers);
        System.out.print("Inorder (sorted): ");
        intTree.inorder();
    }
}
```

Inorder (sorted): Adam Daniel George Jones Michael Peter Tom
Postorder: Daniel Adam Jones Peter Tom Michael George
Preorder: George Adam Daniel Michael Jones Tom Peter
The number of nodes is 7
Is Peter in the tree? true
A path from the root to Peter is: George Michael Tom Peter

The program checks path != null in line 30 to ensure that the path is not null before invoking path.get(i). This is an example of defensive programming to avoid potential runtime errors.

The program creates another tree for storing int values (line 34). After all the elements are inserted in the trees, the trees should appear as shown in Figure 25.9.

If the elements are inserted in a different order (e.g., Daniel, Adam, Jones, Peter, Tom, Michael, George), the tree will look different. However, the inorder traversal prints elements in the same order as long as the set of elements is the same. The inorder traversal displays a sorted list.
25.1 Show the result of inserting 44 into Figure 25.4b.

25.2 Show the inorder, preorder, and postorder of traversing the elements in the binary tree shown in Figure 25.1b.

25.3 If a set of elements is inserted into a BST in two different orders, will the two corresponding BSTs look the same? Will the inorder traversal be the same? Will the postorder traversal be the same? Will the preorder traversal be the same?

25.4 What is the time complexity of inserting an element into a BST?

25.5 Implement the search(element) method using recursion.

25.3 Deleting Elements from a BST

To delete an element from a BST, first locate it in the tree and then consider two cases—whether or not the node has a left child—before deleting the element and reconnecting the tree.

The insert(element) method was presented in Section 25.2.3. Often you need to delete an element from a binary search tree. Doing so is far more complex than adding an element into a binary search tree.

To delete an element from a binary search tree, you need to first locate the node that contains the element and also its parent node. Let current point to the node that contains the element in the binary search tree and parent point to the parent of the current node. The current node may be a left child or a right child of the parent node. There are two cases to consider.

Case 1: The current node does not have a left child, as shown in Figure 25.10a. In this case, simply connect the parent with the right child of the current node, as shown in Figure 25.10b.

For example, to delete node 10 in Figure 25.11a, you would connect the parent of node 10 with the right child of node 10, as shown in Figure 25.11b.
Note
If the current node is a leaf, it falls into Case 1. For example, to delete element 16 in Figure 25.11a, connect its right child (in this case, it is null) to the parent of node 16.

Case 2: The current node has a left child. Let rightMost point to the node that contains the largest element in the left subtree of the current node and parentOfRightMost point to the parent node of the rightMost node, as shown in Figure 25.12a. Note that the rightMost node cannot have a right child but may have a left child. Replace the element value in the current node with the one in the rightMost node, connect the parentOfRightMost node with the left child of the rightMost node, and delete the rightMost node, as shown in Figure 25.12b.

For example, consider deleting node 20 in Figure 25.13a. The rightMost node has the element value 16. Replace the element value 20 with 16 in the current node and make node 10 the parent for node 14, as shown in Figure 25.13b.

Note
If the left child of current does not have a right child, current.left points to the large element in the left subtree of current. In this case, rightMost is current.left and parentOfRightMost is current. You have to take care of this special case to reconnect the right child of rightMost with parentOfRightMost.
The algorithm for deleting an element from a binary search tree can be described in Listing 25.7.

**LISTING 25.7 Deleting an Element from a BST**

```java
1  boolean delete(E e) {
2    Locate element e in the tree; not in the tree
3    if element e is not found
4    return false; // Element not found
5
6    // If e is a leaf node
7    if (e.leftChild == null && e.rightChild == null)
8        return true; // Element found and removed
9
10   // If e has only one child
11   if (e.leftChild == null)
12      e = e.rightChild; // Replace e with right child
13   else if (e.rightChild == null)
14      e = e.leftChild; // Replace e with left child
15
16   // If e has two children
17   E rightMost = findRightMost(e.rightChild); // Find the rightmost node
18   e.value = rightMost.value; // Copy the value
19   delete(rightMost); // Delete the rightmost node
20   return true; // Element found and removed
21 }
22
```

The algorithm works by searching for the element `e` in the tree. If `e` is found, it is deleted according to one of the following cases:

1. If `e` is a leaf node (has no children), it is removed.
2. If `e` has only one child, that child replaces `e`.
3. If `e` has two children, the rightmost node in its right subtree is found and its value is copied to `e`, then the rightmost node is deleted.

**Figure 25.12** Case 2: The current node has a left child.

**Figure 25.13** Case 2: Deleting node 20 from (a) results in (b).
return true;

Let current be the node that contains e and parent be
the parent of current;

if (current has no left child) // Case 1
    Connect the right child of
current with parent; now current is not referenced, so
it is eliminated;
else // Case 2
    Locate the rightmost node in the left subtree of current.
    Copy the element value in the rightmost node to current.
    Connect the parent of the rightmost node to the left child
    of rightmost node;

return true; // Element deleted
}

The complete implementation of the delete method is given in lines 155–213 in Listing
25.5. The method locates the node (named current) to be deleted and also locates its parent
(named parent) in lines 157–170. If current is null, the element is not in the tree. Therefore, the method returns false (line 173). Please note that if current is root, parent is
null. If the tree is empty, both current and parent are null.

Case 1 of the algorithm is covered in lines 176–187. In this case, the current node has
no left child (i.e., current.left == null). If parent is null, assign current.right to
root (lines 178–180). Otherwise, assign current.right to either parent.left or
parent.right, depending on whether current is a left or right child of parent (182–185).

Case 2 of the algorithm is covered in lines 188–209. In this case, current has a left child.
The algorithm locates the rightmost node (named rightMost) in the left subtree of the cur-
rent node and also its parent (named parentOfRightMost) (lines 195–198). Replace the element in current by the element in rightMost (line 201); assign rightMost.left to either parentOfRightMost.right or parentOfRightMost.left (lines 204–208),
depending on whether rightMost is a right or left child of parentOfRightMost.

Listing 25.8 gives a test program that deletes the elements from the binary search tree.

**LISTING 25.8 TestBSTDelete.java**

```java
public class TestBSTDelete {
    public static void main(String[] args) {
        BST<String> tree = new BST<>();
        tree.insert("George");
        tree.insert("Michael");
        tree.insert("Tom");
        tree.insert("Adam");
        tree.insert("Jones");
        tree.insert("Peter");
        tree.insert("Daniel");
        printTree(tree);

        System.out.println("\nAfter delete George: ");
        tree.delete("George");
        printTree(tree);

        System.out.println("\nAfter delete Adam: ");
        tree.delete("Adam");
        printTree(tree);

        System.out.println("\nAfter delete Michael: ");
        tree.delete("Michael");
```
25.3 Deleting Elements from a BST

```java
public static void printTree(BST tree) {
    // Traverse tree
    System.out.print("Inorder (sorted): ");
    tree.inorder();
    System.out.print("\nPostorder: ");
    tree.postorder();
    System.out.print("\nPreorder: ");
    tree.preorder();
    System.out.print("\nThe number of nodes is "+ tree.getSize());
    System.out.println();
}
```

Inorder (sorted): Adam Daniel George Jones Michael Peter Tom
Postorder: Daniel Adam Jones Peter Tom Michael George
Preorder: George Adam Daniel Michael Jones Tom Peter
The number of nodes is 7

After delete George:
Inorder (sorted): Adam Daniel Jones Michael Peter Tom
Postorder: Adam Jones Peter Tom Michael Daniel
Preorder: Daniel Adam Michael Jones Tom Peter
The number of nodes is 6

After delete Adam:
Inorder (sorted): Daniel Jones Michael Peter Tom
Postorder: Jones Peter Tom Michael Daniel
Preorder: Daniel Michael Jones Tom Peter
The number of nodes is 5

After delete Michael:
Inorder (sorted): Daniel Jones Peter Tom
Postorder: Peter Tom Jones Daniel
Preorder: Daniel Jones Tom Peter
The number of nodes is 4

Figures 25.14–25.16 show how the tree evolves as the elements are deleted from it.

**FIGURE 25.14** Deleting George falls into Case 2.
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Note
It is obvious that the time complexity for the inorder, preorder, and postorder is $O(n)$, since each node is traversed only once. The time complexity for search, insertion, and deletion is the height of the tree. In the worst case, the height of the tree is $O(n)$. If a tree is well-balanced, the height would be $O(\log n)$. We will introduce well-balanced binary trees in Chapter 26 and bonus Chapters 40 and 41.

25.6 Show the result of deleting 55 from the tree in Figure 25.4b.
25.7 Show the result of deleting 60 from the tree in Figure 25.4b.
25.8 What is the time complexity of deleting an element from a BST?
25.9 Is the algorithm correct if lines 204–208 in Listing 25.5 in Case 2 of the delete() method are replaced by the following code?

parentOfRightMost.right = rightMost.left;
25.4 Tree Visualization and MVC

You can use recursion to display a binary tree.

Pedagogical Note

One challenge facing the data-structure course is to motivate students. Displaying a binary tree graphically will not only help you understand the working of a binary tree but perhaps also stimulate your interest in programming. This section introduces the techniques to visualize binary trees. You can also apply visualization techniques to other projects.

How do you display a binary tree? It is a recursive structure, so you can display a binary tree using recursion. You can simply display the root, then display the two subtrees recursively. The techniques for displaying the Sierpinski triangle (Listing 18.9, SierpinskiTriangle.java) can be applied to displaying a binary tree. For simplicity, we assume the keys are positive integers less than 100. Listings 25.9 and 25.10 give the program, and Figure 25.17 shows some sample runs of the program.

![Figure 25.17](image)

A binary tree is displayed graphically.

Listing 25.9 BSTAnimation.java

```java
public class BSTAnimation extends Application {
    @Override
    public void start(Stage primaryStage) {
        BST<Integer> tree = new BST<>(); // Create a tree
        BorderPane pane = new BorderPane();
        BTView view = new BTView(tree); // Create a BTView
        pane.setCenter(view);
        TextField tfKey = new TextField();
        tfKey.setPrefColumnCount(3);
        tfKey.setAlignment(Pos.BASELINE_RIGHT);
        Button btInsert = new Button("Insert");
        Button btDelete = new Button("Delete");
        HBox hBox = new HBox(5);
        hBox.getChildren().addAll(new Label("Enter a key: "),
```

```java
```
```
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```java
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Circle;
import javafx.scene.shape.Line;
import javafx.scene.text.Text;

public class BTView extends Pane {
    private BST<Integer> tree = new BST<>();
    private double radius = 15; // Tree node radius
    private double vGap = 50; // Gap between two levels in a tree

    BTView(BST<Integer> tree) {
        this.tree = tree;
        setStatus("Tree is empty");
    }

    public void setStatus(String msg) {
        getChildren().add(new Text(20, 20, msg));
    }
}
```

Listing 25.10  BTView.java
25.4 Tree Visualization and MVC 951

```java
public void displayTree() {
    this.getChildren().clear(); // Clear the pane
display tree recursively
    if (tree.getRoot() != null) {
        // Display tree recursively
        displayTree(tree.getRoot(), getWidth() / 2, vGap, getWidth() / 4);
    }
}
```

In Listing 25.9, BSTAnimation.java, a tree is created (line 14) and a tree view is placed in the pane (line 18). After a new key is inserted into the tree (line 37), the tree is repainted (line 38) to reflect the change. After a key is deleted (line 49), the tree is repainted (line 50) to reflect the change.

In Listing 25.10, BTView.java, the node is displayed as a circle with radius 15 (line 48). The distance between two levels in the tree is defined in vGap 50 (line 25). hGap (line 32) defines the distance between two nodes horizontally. This value is reduced by half (hGap / 2) in the next level when the displayTree method is called recursively (lines 44, 51). Note that vGap is not changed in the tree.

The method displayTree is recursively invoked to display a left subtree (lines 33–38) and a right subtree (lines 40–45) if a subtree is not empty. A line is added to the pane to connect two nodes (lines 35, 42). Note that the method first adds the lines to the pane and then adds the circle into the pane (line 52) so that the circles will be painted on top of the lines to achieve desired visual effects.

The program assumes that the keys are integers. You can easily modify the program with a generic type to display keys of characters or short strings.

Tree visualization is an example of the model-view-controller (MVC) software architecture. This is an important architecture for software development. The model is for storing and handling data. The view is for visually presenting the data. The controller handles the user interaction with the model and controls the view, as shown in Figure 25.18.
The MVC architecture separates data storage and handling from the visual representation of the data. It has two major benefits:

- It makes multiple views possible so that data can be shared through the same model. For example, you can create a new view that displays the tree with the root on the left and tree grows horizontally to the right (see Programming Exercise 25.11).

- It simplifies the task of writing complex applications and makes the components scalable and easy to maintain. Changes can be made to the view without affecting the model, and vice versa.

**25.10** How many times will the `displayTree` method be invoked if the tree is empty? How many times will the `displayTree` method be invoked if the tree has 100 nodes?

**25.11** In what order are the nodes in the tree visited by the `displayTree` method: inorder, preorder, or postorder?

**25.12** What would happen if the code in lines 47–52 in BTView.java is moved to line 33?

**25.13** What is MVC? What are the benefits of the MVC?

**25.5 Iterators**

BST is iterable because it is defined as a subtype of the `java.lang.Iterable` interface.

The methods `inorder()`, `preorder()`, and `postorder()` display the elements in `inorder`, `preorder`, and `postorder` in a binary tree. These methods are limited to displaying the elements in a tree. If you wish to process the elements in a binary tree rather than display them, these methods cannot be used. Recall that an iterator is provided for traversing the elements in a set or list. You can apply the same approach in a binary tree to provide a uniform way of traversing the elements in a binary tree.

The `java.lang.Iterable` interface defines the `iterator` method, which returns an instance of the `java.util.Iterator` interface. The `java.util.Iterator` interface (see Figure 25.19) defines the common features of iterators.

**Figure 25.18** The controller obtains data and stores it in a model. The view displays the data stored in the model.

**Figure 25.19** The `Iterator` interface defines a uniform way of traversing the elements in a container.
The Tree interface extends java.lang.Iterable. Since BST is a subclass of AbstractTree and AbstractTree implements Tree, BST is a subtype of Iterable. The Iterable interface contains the iterator() method that returns an instance of java.util.Iterator.

You can traverse a binary tree in inorder, preorder, or postorder. Since inorder is used frequently, we will use inorder for traversing the elements in a binary tree. We define an iterator class named InorderIterator to implement the java.util.Iterator interface in Listing 25.5 (lines 221–263). The iterator method simply returns an instance of InorderIterator (line 217).

The InorderIterator constructor invokes the inorder method (line 228). The inorder(root) method (lines 237–242) stores all the elements from the tree in list. The elements are traversed in inorder.

Once an Iterator object is created, its current value is initialized to 0 (line 225), which points to the first element in the list. Invoking the next() method returns the current element and moves current to point to the next element in the list (line 253).

The hasNext() method checks whether current is still in the range of list (line 246). The remove() method removes the current element from the tree (line 259). Afterward, a new list is created (lines 260–261). Note that current does not need to be changed.

Listing 25.11 gives a test program that stores the strings in a BST and displays all strings in uppercase.

**LISTING 25.11 TestBSTWithIterator.java**

1. public class TestBSTWithIterator {
2.   public static void main(String[] args) {
3.      BST<String> tree = new BST<>();
4.      tree.insert("George");
5.      tree.insert("Michael");
6.      tree.insert("Tom");
7.      tree.insert("Adam");
8.      tree.insert("Jones");
9.      tree.insert("Peter");
10.     tree.insert("Daniel");
11.    
12.     for (String s: tree)
13.        System.out.print(s.toUpperCase() + " ");
14.   }
15. }

The foreach loop (lines 12–13) uses an iterator to traverse all elements in the tree.

**Design Guide**

Iterator is an important software design pattern. It provides a uniform way of traversing the elements in a container, while hiding the container's structural details. By implementing the same interface java.util.Iterator, you can write a program that traverses the elements of all containers in the same way.

**Note**

java.util.Iterator defines a forward iterator, which traverses the elements in the iterator in a forward direction, and each element can be traversed only once. The Java API also provides the java.util.ListIterator, which supports traversing in both forward and backward directions. If your data structure warrants flexible traversing, you may define iterator classes as a subtype of java.util.ListIterator.
The implementation of the iterator is not efficient. Every time you remove an element through the iterator, the whole list is rebuilt (line 261 in Listing 25.5 BST.java). The client should always use the delete method in the BinaryTree class to remove an element. To prevent the user from using the remove method in the iterator, implement the iterator as follows:

```java
public void remove() {
    throw new UnsupportedOperationException("Removing an element from the iterator is not supported");
}
```

After making the remove method unsupported by the iterator class, you can implement the iterator more efficiently without having to maintain a list for the elements in the tree. You can use a stack to store the nodes, and the node on the top of the stack contains the element that is to be returned from the next() method. If the tree is well-balanced, the maximum stack size will be $O(\log n)$.

25.14 What is an iterator?
25.15 What method is defined in the java.lang.Iterable<E> interface?
25.16 Suppose you delete extends Iterable<E> from line 1 in Listing 25.3, Tree.java. Will Listing 25.11 still compile?
25.17 What is the benefit of being a subtype of Iterable<E>?

25.6 Case Study: Data Compression

Huffman coding compresses data by using fewer bits to encode characters that occur more frequently. The codes for the characters are constructed based on the occurrence of the characters in the text using a binary tree, called the Huffman coding tree.

Compressing data is a common task. There are many utilities available for compressing files. This section introduces Huffman coding, invented by David Huffman in 1952.

In ASCII, every character is encoded in 8 bits. If a text consists of 100 characters, it will take 800 bits to represent the text. The idea of Huffman coding is to use a fewer bits to encode frequently used characters in the text and more bits to encode less frequently used characters to reduce the overall size of the file. In Huffman coding, the characters’ codes are constructed based on the characters’ occurrence in the text using a binary tree, called the Huffman coding tree. Suppose the text is Mississippi. Its Huffman tree can be shown as in Figure 25.20a. The left and right edges of a node are assigned a value 0 and 1, respectively. Each character is a leaf in the tree. The code for the character consists of the edge values in the path from the root to the leaf, as shown in Figure 25.20b. Since i and s appear more than M and p in the text, they are assigned shorter codes.

Based on the coding scheme in Figure 25.20,

<table>
<thead>
<tr>
<th>Character</th>
<th>Code</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>M</td>
<td>000</td>
<td>1</td>
</tr>
<tr>
<td>p</td>
<td>001</td>
<td>1</td>
</tr>
<tr>
<td>s</td>
<td>01</td>
<td>4</td>
</tr>
<tr>
<td>i</td>
<td>1</td>
<td>4</td>
</tr>
</tbody>
</table>

(a) Huffman coding tree  
(b) Character code table

**Figure 25.20** The codes for characters are constructed based on the occurrence of characters in the text using a coding tree.
The coding tree is also used for decoding a sequence of bits into characters. To do so, start with the first bit in the sequence and determine whether to go to the left or right branch of the tree’s root based on the bit value. Consider the next bit and continue to go down to the left or right branch based on the bit value. When you reach a leaf, you have found a character. The next bit in the stream is the first bit of the next character. For example, the stream 011001 is decoded to sip, with 01 matching s, 1 matching i, and 001 matching p.

To construct a Huffman coding tree, use an algorithm as follows:

1. Begin with a forest of trees. Each tree contains a node for a character. The weight of the node is the frequency of the character in the text.
2. Repeat the following action to combine trees until there is only one tree: Choose two trees with the smallest weight and create a new node as their parent. The weight of the new tree is the sum of the weight of the subtrees.
3. For each interior node, assign its left edge a value 0 and right edge a value 1. All leaf nodes represent characters in the text.

Here is an example of building a coding tree for the text Mississippi. The frequency table for the characters is shown in Figure 25.20b. Initially the forest contains single-node trees, as shown in Figure 25.21a. The trees are repeatedly combined to form large trees until only one tree is left, as shown in Figure 25.21b–d.

![Coding Tree Diagram](image)

**Figure 25.21** The coding tree is built by repeatedly combining the two smallest-weighted trees.

It is worth noting that no code is a prefix of another code. This property ensures that the streams can be decoded unambiguously.

**Pedagogical Note**

For an interactive GUI demo to see how Huffman coding works, go to [www.cs.armstrong.edu/liang/animation/HuffmanCodingAnimation.html](http://www.cs.armstrong.edu/liang/animation/HuffmanCodingAnimation.html), as shown in Figure 25.22.
The algorithm used here is an example of a greedy algorithm. A greedy algorithm is often used in solving optimization problems. The algorithm makes the choice that is optimal locally in the hope that this choice will lead to a globally optimal solution. In this case, the algorithm always chooses two trees with the smallest weight and creates a new node as their parent. This intuitive optimal local solution indeed leads to a final optimal solution for constructing a Huffman tree. As another example, consider changing money into the fewest possible coins. A greedy algorithm would take the largest possible coin first. For example, for 98¢, you would use three quarters to make 75¢, additional two dimes to make 95¢, and additional three pennies to make the 98¢. The greedy algorithm finds an optimal solution for this problem. However, a greedy algorithm is not always going to find the optimal result; see the bin packing problem in Programming Exercise 25.22.

Listing 25.12 gives a program that prompts the user to enter a string, displays the frequency table of the characters in the string, and displays the Huffman code for each character.

```java
import java.util.Scanner;

public class HuffmanCode {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        System.out.print("Enter text: ");
        String text = input.nextLine();

        int[] counts = getCharacterFrequency(text); // Count frequency
        System.out.printf("%-15s%-15s%-15s%-15s
", "ASCII Code", "Character", "Frequency", "Code");

        Tree tree = getHuffmanTree(counts); // Create a Huffman tree
        String[] codes = getCode(tree.root); // Get codes

        for (int i = 0; i < codes.length; i++)
            if (counts[i] != 0) // (char)i is not in text if counts[i] is 0
                System.out.printf("%-15d%-15s%-15d%-15s\n",
```

**Figure 25.22** The animation tool enables you to create and view a Huffman tree, and it performs encoding and decoding using the tree.

**Listing 25.12** HuffmanCode.java

```java
import java.util.Scanner;

public class HuffmanCode {
    public static void main(String[] args) {
        Scanner input = new Scanner(System.in);
        System.out.print("Enter text: ");
        String text = input.nextLine();

        int[] counts = getCharacterFrequency(text); // Count frequency
        System.out.printf("%-15s%-15s%-15s%-15s
", "ASCII Code", "Character", "Frequency", "Code");

        Tree tree = getHuffmanTree(counts); // Create a Huffman tree
        String[] codes = getCode(tree.root); // Get codes

        for (int i = 0; i < codes.length; i++)
            if (counts[i] != 0) // (char)i is not in text if counts[i] is 0
                System.out.printf("%-15d%-15s%-15d%-15s\n",
```
```java
    i, (char)i + "", counts[i], codes[i]);

    /** Get Huffman codes for the characters
     * This method is called once after a Huffman tree is built
     */
    public static String[] getCode(Tree.Node root) {
        if (root == null) return null;
        String[] codes = new String[2 * 128];
        assignCode(root, codes);
        return codes;
    }

    /* Recursively get codes to the leaf node */
    private static void assignCode(Tree.Node root, String[] codes) {
        if (root.left != null) {
            root.left.code = root.code + "0";
            assignCode(root.left, codes);
            root.right.code = root.code + "1";
            assignCode(root.right, codes);
        } else {
            codes[(int)root.element] = root.code;
        }
    }

    /** Get a Huffman tree from the codes */
    public static Tree getHuffmanTree(int[] counts) {
        // Create a heap to hold trees
        Heap<Tree> heap = new Heap<>(); // Defined in Listing 23.9
        for (int i = 0; i < counts.length; i++) {
            if (counts[i] > 0)
                heap.add(new Tree(counts[i], (char)i)); // A leaf node tree
        }
        while (heap.getSize() > 1) {
            Tree t1 = heap.remove(); // Remove the smallest-weight tree
            Tree t2 = heap.remove(); // Remove the next smallest
            heap.add(new Tree(t1, t2)); // Combine two trees
        }
        return heap.remove(); // The final tree
    }

    /** Get the frequency of the characters */
    public static int[] getCharacterFrequency(String text) {
        int[] counts = new int[256]; // 256 ASCII characters
        for (int i = 0; i < text.length(); i++)
            counts[(int)text.charAt(i)]++;
        return counts;
    }

    /** Define a Huffman coding tree */
    public static class Tree implements Comparable<Tree> {
        Node root; // The root of the tree
        /*...*/
    }
```


```java
public Tree(Tree t1, Tree t2) {
    root = new Node();
    root.left = t1.root;
    root.right = t2.root;
    root.weight = t1.root.weight + t2.root.weight;
}

/** Create a tree containing a leaf node */
public Tree(int weight, char element) {
    root = new Node(weight, element);
}

@Override /** Compare trees based on their weights */
public int compareTo(Tree t) {
    if (root.weight < t.root.weight) // Purposely reverse the order
        return 1;
    else if (root.weight == t.root.weight)
        return 0;
    else
        return -1;
}

public class Node {
    char element; // Stores the character for a leaf node
    int weight; // weight of the subtree rooted at this node
    Node left; // Reference to the left subtree
    Node right; // Reference to the right subtree
    String code = ""; // The code of this node from the root

    /** Create an empty node */
    public Node() {
    }

    /** Create a node with the specified weight and character */
    public Node(int weight, char element) {
        this.weight = weight;
        this.element = element;
    }
}
```

The program prompts the user to enter a text string (lines 5–7) and counts the frequency of the characters in the text (line 9). The `getCharacterFrequency` method (lines 66–73) creates an array `counts` to count the occurrences of each of the 256 ASCII characters in the text. If a character appears in the text, its corresponding count is increased by 1 (line 70).
The program obtains a Huffman coding tree based on **counts** (line 14). The tree consists of linked nodes. The Node class is defined in lines 102–118. Each node consists of properties **element** (storing character), **weight** (storing weight of the subtree under this node), **left** (linking to the left subtree), **right** (linking to the right subtree), and **code** (storing the Huffman code for the character). The Tree class (lines 76–119) contains the root property. From the root, you can access all the nodes in the tree. The Tree class implements **Comparable**. The trees are comparable based on their weights. The compare order is purposely reversed (lines 93–100) so that the smallest-weight tree is removed first from the heap of trees.

The getHuffmanTree method returns a Huffman coding tree. Initially, the single-node trees are created and added to the heap (lines 50–54). In each iteration of the while loop (lines 56–60), two smallest-weight trees are removed from the heap and are combined to form a big tree, and then the new tree is added to the heap. This process continues until the heap contains just one tree, which is our final Huffman tree for the text.

The assignCode method assigns the code for each node in the tree (lines 34–45). The getCode method gets the code for each character in the leaf node (lines 26–31). The element codes[i] contains the code for character (char)i, where i is from 0 to 255. Note that codes[i] is null if (char)i is not in the text.

25.18 Every internal node in a Huffman tree has two children. Is it true?

25.19 What is a greedy algorithm? Give an example.

25.20 If the Heap class in line 50 in Listing 25.10 is replaced by java.util.PriorityQueue, will the program still work?

**Key Terms**

- **binary search tree** 930
- **binary tree** 930
- **breadth-first traversal** 934
- **depth-first traversal** 934
- **greedy algorithm** 956
- **Huffman coding** 954
- **inorder traversal** 933
- **postorder traversal** 933
- **preorder traversal** 934
- **tree traversal** 933

**Chapter Summary**

1. A **binary search tree** (BST) is a hierarchical data structure. You learned how to define and implement a BST class, how to insert and delete elements into/from a BST, and how to traverse a BST using **inorder**, **postorder**, **preorder**, depth-first, and breadth-first searches.

2. An iterator is an object that provides a uniform way of traversing the elements in a container, such as a set, a list, or a **binary tree**. You learned how to define and implement iterator classes for traversing the elements in a binary tree.

3. **Huffman coding** is a scheme for compressing data by using fewer bits to encode characters that occur more frequently. The codes for characters are constructed based on the occurrence of characters in the text using a binary tree, called the **Huffman coding tree**.

**Quiz**

Answer the quiz for this chapter online at [www.cs.armstrong.edu/liang/intro10e/quiz.html](http://www.cs.armstrong.edu/liang/intro10e/quiz.html).
**PROGRAMMING EXERCISES**

**Sections 25.2–25.6**

**25.1** (Add new methods in BST) Add the following new methods in BST.

```java
/** Displays the nodes in a breadth-first traversal */
public void breadthFirstTraversal()

/** Returns the height of this binary tree */
public int height()
```

**25.2** (Test full binary tree) A full binary tree is a binary tree with the leaves on the same level. Add a method in the BST class to return true if the tree is a full binary tree. (Hint: The number of nodes in a full binary tree is \(2^{\text{depth}} - 1\)).

```java
/** Returns true if the tree is a full binary tree */
boolean isFullBST()
```

**25.3** (Implement inorder traversal without using recursion) Implement the inorder method in BST using a stack instead of recursion. Write a test program that prompts the user to enter 10 integers, stores them in a BST, and invokes the inorder method to display the elements.

**25.4** (Implement preorder traversal without using recursion) Implement the preorder method in BST using a stack instead of recursion. Write a test program that prompts the user to enter 10 integers, stores them in a BST, and invokes the preorder method to display the elements.

**25.5** (Implement postorder traversal without using recursion) Implement the postorder method in BST using a stack instead of recursion. Write a test program that prompts the user to enter 10 integers, stores them in a BST, and invokes the postorder method to display the elements.

**25.6** (Find the leaves) Add a method in the BST class to return the number of the leaves as follows:

```java
/** Returns the number of leaf nodes */
public int getNumberOfLeaves()
```

**25.7** (Find the nonleaves) Add a method in the BST class to return the number of the nonleaves as follows:

```java
/** Returns the number of nonleaf nodes */
public int getNumberofNonLeaves()
```

**25.8** (Implement bidirectional iterator) The java.util.Iterator interface defines a forward iterator. The Java API also provides the java.util.ListIterator interface that defines a bidirectional iterator. Study ListIterator and define a bidirectional iterator for the BST class.

**25.9** (Tree clone and equals) Implement the clone and equals methods in the BST class. Two BST trees are equal if they contain the same elements. The clone method returns an identical copy of a BST.
25.10 (Preorder iterator) Add the following method in the BST class that returns an iterator for traversing the elements in a BST in preorder.

```java
/** Returns an iterator for traversing the elements in preorder */
java.util.Iterator<E> preorderIterator()
```

25.11 (Display tree) Write a new view class that displays the tree horizontally with the root on the left as shown in Figure 25.23.

![Figure 25.23](image)

**25.12 (Test BST) Design and write a complete test program to test if the BST class in Listing 25.5 meets all requirements.**

**25.13 (Add new buttons in BSTAnimation) Modify Listing 25.9, BSTAnimation.java, to add three new buttons—Show Inorder, Show Preorder, and Show Postorder—to display the result in a label, as shown in Figure 25.24. You need also to modify BST.java to implement the `inorderList()`, `preorderList()`, and `postorderList()` methods so that each of these methods returns a `List` of the node elements in inorder, preorder, and postorder, as follows:

```java
public java.util.List<E> inorderList();
public java.util.List<E> preorderList();
public java.util.List<E> postorderList();
```

![Figure 25.24](image)

**Figure 25.24** When you click the Show Inorder, Show Preorder, or Show Postorder button, the elements are displayed in an inorder, preorder, or postorder in a label.
25.14 (Generic BST using Comparator) Revise BST in Listing 25.5, using a generic parameter and a Comparator for comparing objects. Define a new constructor with a Comparator as its argument as follows:

```java
BST(Comparator<? super E> comparator)
```

25.15 (Parent reference for BST) Redefine TreeNode by adding a reference to a node’s parent, as shown below:

```java
BST.TreeNode<E>
#element: E
#left: TreeNode<E>
#right: TreeNode<E>
#parent: TreeNode<E>
```

Reimplement the insert and delete methods in the BST class to update the parent for each node in the tree. Add the following new method in BST:

```java
/**
 * Returns the node for the specified element.
 * Returns null if the element is not in the tree.
 */
private TreeNode<E> getNode(E element)

/**
 * Returns true if the node for the element is a leaf
 */
private boolean isLeaf(E element)

/**
 * Returns the path of elements from the specified element
to the root in an array list.
 */
public ArrayList<E> getPath(E e)
```

Write a test program that prompts the user to enter 10 integers, adds them to the tree, deletes the first integer from the tree, and displays the paths for all leaf nodes. Here is a sample run:

```
Enter 10 integers: 45 54 67 56 50 45 23 59 23 67
[50, 54, 23]
[59, 56, 67, 54, 23]
```

25.16 (Data compression: Huffman coding) Write a program that prompts the user to enter a file name, then displays the frequency table of the characters in the file and displays the Huffman code for each character.

25.17 (Data compression: Huffman coding animation) Write a program that enables the user to enter text and displays the Huffman coding tree based on the text, as shown in Figure 25.25a. Display the weight of the subtree inside the subtree’s root circle. Display each leaf node’s character. Display the encoded bits for the text in a label. When the user clicks the Decode Text button, a bit string is decoded into text displayed in the label, as shown in Figure 25.25b.
25.18 (Compress a file) Write a program that compresses a source file into a target file using the Huffman coding method. First use `ObjectOutputStream` to output the Huffman codes into the target file, and then use `BitOutputStream` in Programming Exercise 17.17 to output the encoded binary contents to the target file. Pass the files from the command line using the following command:

```java
java Exercise25_18 sourcefile targetfile
```

25.19 (Decompress a file) The preceding exercise compresses a file. The compressed file contains the Huffman codes and the compressed contents. Write a program that decompresses a source file into a target file using the following command:

```java
java Exercise25_19 sourcefile targetfile
```

25.20 (Bin packing using first fit) Write a program that packs the objects of various weights into containers. Each container can hold a maximum of 10 pounds. The program uses a greedy algorithm that places an object into the first bin in which it would fit. Your program should prompt the user to enter the total number of
objects and the weight of each object. The program displays the total number of containers needed to pack the objects and the contents of each container. Here is a sample run of the program:

Enter the number of objects: 6
Enter the weights of the objects: 7 5 2 3 5 8
Container 1 contains objects with weight 2 3 5
Container 2 contains objects with weight 5 3
Container 3 contains objects with weight 5
Container 4 contains objects with weight 8

Does this program produce an optimal solution, that is, finding the minimum number of containers to pack the objects?

25.21 (Bin packing with smallest object first) Rewrite the preceding program that uses a new greedy algorithm that places an object with the smallest weight into the first bin in which it would fit. Your program should prompt the user to enter the total number of objects and the weight of each object. The program displays the total number of containers needed to pack the objects and the contents of each container. Here is a sample run of the program:

Enter the number of objects: 6
Enter the weights of the objects: 7 5 2 3 5 8
Container 1 contains objects with weight 2 3 5
Container 2 contains objects with weight 5
Container 3 contains objects with weight 7
Container 4 contains objects with weight 8

Does this program produce an optimal solution, that is, finding the minimum number of containers to pack the objects?

25.22 (Bin packing with largest object first) Rewrite the preceding program that places an object with the largest weight into the first bin in which it would fit. Give an example to show that this program does not produce an optimal solution.

25.23 (Optimal bin packing) Rewrite the preceding program so that it finds an optimal solution that packs all objects using the smallest number of containers. Here is a sample run of the program:

Enter the number of objects: 6
Enter the weights of the objects: 7 5 2 3 5 8
Container 1 contains objects with weight 7 3
Container 2 contains objects with weight 5 5
Container 3 contains objects with weight 2 8
The optimal number of bins is 3

What is the time complexity of your program?
AVL Trees

Objectives

- To know what an AVL tree is (§26.1).
- To understand how to rebalance a tree using the LL rotation, LR rotation, RR rotation, and RL rotation (§26.2).
- To design the AVLTree class by extending the BST class (§26.3).
- To insert elements into an AVL tree (§26.4).
- To implement tree rebalancing (§26.5).
- To delete elements from an AVL tree (§26.6).
- To implement the AVLTree class (§26.7).
- To test the AVLTree class (§26.8).
- To analyze the complexity of search, insertion, and deletion operations in AVL trees (§26.9).
26.1 Introduction

AVL Tree is a balanced binary search tree.

Chapter 25 introduced binary search trees. The search, insertion, and deletion times for a binary tree depend on the height of the tree. In the worst case, the height is $O(n)$. If a tree is perfectly balanced—i.e., a complete binary tree—its height is $\log n$. Can we maintain a perfectly balanced tree? Yes, but doing so will be costly. The compromise is to maintain a well-balanced tree—that is, the heights of every node’s two subtrees are about the same. This chapter introduces AVL trees. Web Chapters 40 and 41 introduce 2–4 trees and red–black trees.

AVL trees are well balanced. AVL trees were invented in 1962 by two Russian computer scientists, G. M. Adelson-Velsky and E. M. Landis (hence the name AVL). In an AVL tree, the difference between the heights of every node’s two subtrees is 0 or 1. It can be shown that the maximum height of an AVL tree is $O(\log n)$.

The process for inserting or deleting an element in an AVL tree is the same as in a regular binary search tree, except that you may have to rebalance the tree after an insertion or deletion operation. The balance factor of a node is the height of its right subtree minus the height of its left subtree. A node is said to be balanced if its balance factor is $-1$, $0$, or $1$. A node is considered left-heavy if its balance factor is $-1$, and right-heavy if its balance factor is $+1$.

Pedagogical Note
For an interactive GUI demo to see how an AVL tree works, go to www.cs.armstrong.edu/liang/animation/web/AVLTree.html, as shown in Figure 26.1.

![AVL Tree Animation](www.cs.armstrong.edu/liang/animation/web/AVLTree.html)

Figure 26.1 The animation tool enables you to insert, delete, and search elements.

26.2 Rebalancing Trees

After inserting or deleting an element from an AVL tree, if the tree becomes unbalanced, perform a rotation operation to rebalance the tree.

If a node is not balanced after an insertion or deletion operation, you need to rebalance it. The process of rebalancing a node is called rotation. There are four possible rotations: LL, RR, LR, and RL.
**LL rotation:** An LL imbalance occurs at a node A, such that A has a balance factor of \(-2\) and a left child B with a balance factor of \(-1\) or \(0\), as shown in Figure 26.2a. This type of imbalance can be fixed by performing a single right rotation at A, as shown in Figure 26.2b.

**RR rotation:** An RR imbalance occurs at a node A, such that A has a balance factor of \(+2\) and a right child B with a balance factor of \(+1\) or \(0\), as shown in Figure 26.3a. This type of imbalance can be fixed by performing a single left rotation at A, as shown in Figure 26.3b.

**LR rotation:** An LR imbalance occurs at a node A, such that A has a balance factor of \(-2\) and a left child B with a balance factor of \(+1\), as shown in Figure 26.4a. Assume B’s right child is C. This type of imbalance can be fixed by performing a double rotation (first a single left rotation at B and then a single right rotation at A), as shown in Figure 26.4b.

**RL rotation:** An RL imbalance occurs at a node A, such that A has a balance factor of \(+2\) and a right child B with a balance factor of \(-1\), as shown in Figure 26.5a. Assume B’s left child is C. This type of imbalance can be fixed by performing a double rotation (first a single right rotation at B and then a single left rotation at A), as shown in Figure 26.5b.

26.1 What is an AVL tree? Describe the following terms: balance factor, left-heavy, and right-heavy.

26.2 Show the balance factor of each node in the trees shown in Figure 26.6.

26.3 Describe LL rotation, RR rotation, LR rotation, and RL rotation for an AVL tree.
FIGURE 26.4  An LR rotation fixes an LR imbalance.

FIGURE 26.5  An RL rotation fixes an RL imbalance.

FIGURE 26.6  A balance factor determines whether a node is balanced.
26.3 Designing Classes for AVL Trees

Since an AVL tree is a binary search tree, \texttt{AVLTree} is designed as a subclass of \texttt{BST}.

An AVL tree is a binary tree, so you can define the \texttt{AVLTree} class to extend the \texttt{BST} class, as shown in Figure 26.7. The \texttt{BST} and \texttt{TreeNode} classes were defined in Section 25.2.5.

In order to balance the tree, you need to know each node’s height. For convenience, store the height of each node in \texttt{AVLTreeNode} and define \texttt{AVLTreeNode} to be a subclass of \texttt{BST.TreeNode}. Note that \texttt{TreeNode} is defined as a static inner class in \texttt{BST}. \texttt{AVLTreeNode} will be defined as a static inner class in \texttt{AVLTree}. \texttt{TreeNode} contains the data fields \texttt{element}, \texttt{left}, and \texttt{right}, which are inherited by \texttt{AVLTreeNode}. Thus, \texttt{AVLTreeNode} contains four data fields, as shown in Figure 26.8.
In the BST class, the `createNewNode()` method creates a `TreeNode` object. This method is overridden in the `AVLTree` class to create an `AVLTreeNode`. Note that the return type of the `createNewNode()` method in the BST class is `TreeNode`, but the return type of the `createNewNode()` method in the AVLTree class is `AVLTreeNode`. This is fine, since `AVLTreeNode` is a subclass of `TreeNode`.

Searching for an element in an AVLTree is the same as searching in a regular binary tree, so the `search` method defined in the BST class also works for AVLTree.

The `insert` and `delete` methods are overridden to insert and delete an element and perform rebalancing operations if necessary to ensure that the tree is balanced.

### 26.4 What are the data fields in the `AVLTreeNode` class?

### 26.5 True or false: `AVLTreeNode` is a subclass of `TreeNode`?

### 26.6 True or false: `AVLTree` is a subclass of `BST`.

#### 26.4 Overriding the `insert` Method

Inserting an element into an AVL tree is the same as inserting it to a BST, except that the tree may need to be rebalanced.

A new element is always inserted as a leaf node. As a result of adding a new node, the heights of the new leaf node’s ancestors may increase. After inserting a new node, check the nodes along the path from the new leaf node up to the root. If an unbalanced node is found, perform an appropriate rotation using the algorithm in Listing 26.1.

### Listing 26.1 Balancing Nodes on a Path

```java
1  balancePath(E e) {
2      Get the path from the node that contains element e to the root,
3          as illustrated in Figure 26.9;
4      for each node A in the path leading to the root {
5            Update the height of A;
6            Let parentOfA denote the parent of A,
7                which is the next node in the path, or null if A is the root;
8            is balanced?
9            switch (balanceFactor(A)) {
10               case -2: if balanceFactor(A.left) == -1 or 0
11                  Perform LL rotation; // See Figure 26.2
12               else
13                  Perform LR rotation; // See Figure 26.4
14               break;
15               case +2: if balanceFactor(A.right) == +1 or 0
16                  Perform RR rotation; // See Figure 26.3
17               else
18                  Perform RL rotation; // See Figure 26.5
19            } // End of switch
20      } // End of for
21  } // End of method
```

The algorithm considers each node in the path from the new leaf node to the root. Update the height of the node on the path. If a node is balanced, no action is needed. If a node is not balanced, perform an appropriate rotation.

#### 26.7 For the AVL tree in Figure 26.6a, show the new AVL tree after adding element 40.

What rotation do you perform in order to rebalance the tree? Which node was unbalanced?
26.5 Implementing Rotations

An unbalanced tree becomes balanced by performing an appropriate rotation operation.

Section 26.2, Rebalancing Trees, illustrated how to perform rotations at a node. Listing 26.2 gives the algorithm for the LL rotation, as illustrated in Figure 26.2.

**LISTING 26.2  LL Rotation Algorithm**

```java
1  balanceLL(TreeNode A, TreeNode parentOfA) {
2    Let B be the left child of A.  // left child of A
3
4    if (A is the root)  // reconnect B's parent
5      Let B be the new root
6    else {
7      if (A is a left child of parentOfA)
8        Let B be a left child of parentOfA;
9      else
10        Let B be a right child of parentOfA;
11    }  // End of method
12
13    Make T2 the left subtree of A by assigning B.right to A.left;  // move subtrees
14    Make A the right child of B by assigning A to B.right;
15    Update the height of node A and node B;  // adjust height
16 } // End of method
```

Note that the height of nodes A and B can be changed, but the heights of other nodes in the tree are not changed. You can implement the RR, LR, and RL rotations in a similar manner.
26.6 Implementing the delete Method

Deleting an element from an AVL tree is the same as deleting it from a BST, except that the tree may need to be rebalanced.

As discussed in Section 25.3, Deleting Elements from a BST, to delete an element from a binary tree, the algorithm first locates the node that contains the element. Let current point to the node that contains the element in the binary tree and parent point to the parent of the current node. The current node may be a left child or a right child of the parent node. Two cases arise when deleting an element.

Case 1: The current node does not have a left child, as shown in Figure 25.10a. To delete the current node, simply connect the parent node with the right child of the current node, as shown in Figure 25.10b.

The height of the nodes along the path from the parent node up to the root may have decreased. To ensure that the tree is balanced, invoke

```
balancePath(parent.element); // Defined in Listing 26.1
```

Case 2: The current node has a left child. Let rightMost point to the node that contains the largest element in the left subtree of the current node and parentOfRightMost point to the parent node of the rightMost node, as shown in Figure 25.12a. The rightMost node cannot have a right child but it may have a left child. Replace the element value in the current node with the one in the rightMost node, connect the parentOfRightMost node with the left child of the rightMost node, and delete the rightMost node, as shown in Figure 25.12b.

The height of the nodes along the path from parentOfRightMost up to the root may have decreased. To ensure that the tree is balanced, invoke

```
balancePath(parentOfRightMost); // Defined in Listing 26.1
```

26.11 For the AVL tree in Figure 26.6a, show the new AVL tree after deleting element 107. What rotation do you perform in order to rebalance the tree? Which node was unbalanced?

26.12 For the AVL tree in Figure 26.6a, show the new AVL tree after deleting element 60. What rotation do you perform in order to rebalance the tree? Which node was unbalanced?

26.13 For the AVL tree in Figure 26.6a, show the new AVL tree after deleting element 55. What rotation did you perform in order to rebalance the tree? Which node was unbalanced?

26.14 For the AVL tree in Figure 26.6b, show the new AVL tree after deleting elements 67 and 87. What rotation did you perform in order to rebalance the tree? Which node was unbalanced?

26.7 The AVLTree Class

The AVLTree class extends the BST class to override the insert and delete methods to rebalance the tree if necessary.

Listing 26.3 gives the complete source code for the AVLTree class.

Listing 26.3 AVLTree.java

```
1 public class AVLTree<E extends Comparable<E>> extends BST<E> {
2     /** Create an empty AVL tree */
3     public AVLTree() {
```
26.7 The AVLTree Class

```java
/** Create an AVL tree from an array of objects */
public AVLTree(E[] objects) {
    super(objects);
}

@Override /** Override createNewNode to create an AVLTreeNode */
protected AVLTreeNode<E> createNewNode(E e) {
    return new AVLTreeNode<E>(e);
}

@Override /** Insert an element and rebalance if necessary */
public boolean insert(E e) {
    boolean successful = super.insert(e);
    if (!successful)
        return false; // e is already in the tree
    else {
        balancePath(e); // Balance from e to the root if necessary
    }
    return true; // e is inserted
}

/** Update the height of a specified node */
private void updateHeight(AVLTreeNode<E> node) {
    if (node.left == null && node.right == null) // node is a leaf
        node.height = 0;
    else if (node.left == null) // node has no left subtree
        node.height = 1 + ((AVLTreeNode<E>)(node.right)).height;
    else if (node.right == null) // node has no right subtree
        node.height = 1 + ((AVLTreeNode<E>)(node.left)).height;
    else
        node.height = 1 +
            Math.max(((AVLTreeNode<E>)(node.right)).height,
                ((AVLTreeNode<E>)(node.left)).height);
}

/** Balance the nodes in the path from the specified */
/** * node to the root if necessary */
private void balancePath(E e) {
    java.util.ArrayList<TreeNode<E>> path = path(e);
    for (int i = path.size() - 1; i >= 0; i––) {
        AVLTreeNode<E> A = (AVLTreeNode<E>)(path.get(i));
        updateHeight(A);
        AVLTreeNode<E> parentOfA = (A == root) ? null :
            (AVLTreeNode<E>)(path.get(i - 1));
        switch (balanceFactor(A)) {
            case -2:
                if (balanceFactor((AVLTreeNode<E>)(A.left)) <= 0) {
                    balanceLL(A, parentOfA); // Perform LL rotation
                } else {
                    balanceLR(A, parentOfA); // Perform LR rotation
                }
                break;
            case +2:
                break;
        }
    }
}
```
### Chapter 26  AVL Trees

#### RR rotation

```java
if (balanceFactor((AVLTreeNode<E>)A.right) >= 0) {
    balanceRR(A, parentOfA); // Perform RR rotation
}
else {
    balanceRL(A, parentOfA); // Perform RL rotation
}
```

#### RL rotation

```java
else {
    balanceRL(A, parentOfA); // Perform RL rotation
}
```

#### LL rotation

```java
private int balanceFactor(AVLTreeNode<E> node) {
    if (node.right == null) // node has no right subtree
        return -node.height;
    else if (node.left == null) // node has no left subtree
        return +node.height;
    else
        return ((AVLTreeNode<E>)node.right).height -
                ((AVLTreeNode<E>)node.left).height;
}
```

#### LR rotation

```java
private void balanceLL(TreeNode<E> A, TreeNode<E> parentOfA) {
    TreeNode<E> B = A.left; // A is left-heavy and B is left-heavy
    if (A == root) {
        root = B;
    } else {
        if (parentOfA.left == A) {
            parentOfA.left = B;
        } else {
            parentOfA.right = B;
        }

    }
    A.left = B.right; // Make T2 the left subtree of A
    B.right = A; // Make A the left child of B
    updateHeight((AVLTreeNode<E>)A);
    updateHeight((AVLTreeNode<E>)B);
}
```

#### Update height

```java
private void balanceLR(TreeNode<E> A, TreeNode<E> parentOfA) {
    TreeNode<E> B = A.left; // A is left-heavy
    TreeNode<E> C = B.right; // B is right-heavy
    if (A == root) {
        root = C;
    } else {
        if (parentOfA.left == A) {
            parentOfA.left = C;
        } else {
            parentOfA.right = C;
        }
```

**Get balance factor**

**Balance LL (see Figure 26.2)**

**Balance LR (see Figure 26.4)**

**RR rotation**

**RL rotation**

**Update height**

**LL rotation**

**LR rotation**
26.7 The AVLTree Class 975

A.left = C.right; // Make T3 the left subtree of A
B.right = C.left; // Make T2 the right subtree of B
C.left = B;
C.right = A;

// Adjust heights
updateHeight((AVLTreeNode<E>)A);
updateHeight((AVLTreeNode<E>)B);
updateHeight((AVLTreeNode<E>)C);

/** Balance RR (see Figure 26.3) */
private void balanceRR(TreeNode<E> A, TreeNode<E> parentOfA) {
  TreeNode<E> B = A.right; // A is right-heavy and B is right-heavy
  if (A == root) {
    root = B;
  } else {
    if (parentOfA.left == A) {
      parentOfA.left = B;
    } else {
      parentOfA.right = B;
    }
  }
  A.right = B.left; // Make T2 the right subtree of A
  B.left = A;
  updateHeight((AVLTreeNode<E>)A);
  updateHeight((AVLTreeNode<E>)B);
}

/** Balance RL (see Figure 26.5) */
private void balanceRL(TreeNode<E> A, TreeNode<E> parentOfA) {
  TreeNode<E> B = A.right; // A is right-heavy
  TreeNode<E> C = B.left; // B is left-heavy
  if (A == root) {
    root = C;
  } else {
    if (parentOfA.left == A) {
      parentOfA.left = C;
    } else {
      parentOfA.right = C;
    }
  }
  A.right = C.left; // Make T2 the right subtree of A
  B.left = C.right; // Make T3 the left subtree of B
  C.left = A;
  C.right = B;
  // Adjust heights
updateHeight((AVLTreeNode<E>)A);
updateHeight((AVLTreeNode<E>)B);
updateHeight((AVLTreeNode<E>)C);
}

@Override /** Delete an element from the AVL tree. 
* Return true if the element is deleted successfully
* Return false if the element is not in the tree */
public boolean delete(E element) {
    if (root == null)
        return false; // Element is not in the tree
    // Locate the node to be deleted and also locate its parent node
    TreeNode<E> parent = null;
    TreeNode<E> current = root;
    while (current != null) {
        if (element.compareTo(current.element) < 0) {
            parent = current;
            current = current.left;
        } else if (element.compareTo(current.element) > 0) {
            parent = current;
            current = current.right;
        } else
            break; // Element is in the tree pointed by current
    }
    if (current == null)
        return false; // Element is not in the tree

    // Case 1: current has no left children (See Figure 25.10)
    if (current.left == null) {
        // Connect the parent with the right child of the current node
        if (parent == null) {
            root = current.right;
        } else {
            if (element.compareTo(parent.element) < 0)
                parent.left = current.right;
            else
                parent.right = current.right;
        }
    } else {
        // Case 2: The current node has a left child
        // Locate the rightmost node in the left subtree of
        // the current node and also its parent
        TreeNode<E> parentOfRightMost = current;
        TreeNode<E> rightMost = current.left;
        while (rightMost.right != null) {
            parentOfRightMost = rightMost;
            rightMost = rightMost.right; // Keep going to the right
        }
    }
}
238    // Replace the element in current by the element in rightMost
239    current.element = rightMost.element;
240
241    // Eliminate rightmost node
242    if (parentOfRightMost.right == rightMost)
243        parentOfRightMost.right = rightMost.left;
244    else
245        // Special case: parentOfRightMost is current
246        parentOfRightMost.left = rightMost.left;
247
248    // Balance the tree if necessary
249    balancePath(parentOfRightMost.element); balance nodes
250 }
251
252    size--; return true; // Element inserted
253 }
254
255    /** AVLTreeNode is TreeNode plus height */
256    protected static class AVLTreeNode<E extends Comparable<E>>
257        extends BST.TreeNode<E> {
258        protected int height = 0; // New data field node height
259        public AVLTreeNode(E e) {
260            super(e);
261        }
262    } 
263
264

The AVLTree class extends BST. Like the BST class, the AVLTree class has a no-arg constructor that constructs an empty AVLTree (lines 3–4) and a constructor that creates an initial AVLTree from an array of elements (lines 7–9).

The createNewNode() method defined in the BST class creates a TreeNode. This method is overridden to return an AVLTreeNode (lines 12–14).

The insert method in AVLTree is overridden in lines 17–26. The method first invokes the insert method in BST, then invokes balancePath(e) (line 22) to ensure that the tree is balanced.

The balancePath method first gets the nodes on the path from the node that contains element e to the root (line 46). For each node in the path, update its height (line 49), check its balance factor (line 53), and perform appropriate rotations if necessary (lines 53–69).

Four methods for performing rotations are defined in lines 85–182. Each method is invoked with two TreeNode arguments—A and parentOfA—to perform an appropriate rotation at node A. How each rotation is performed is illustrated in Figures 26.2–26.5. After the rotation, the heights of nodes A, B, and C are updated (lines 102, 129, 152, 179).

The delete method in AVLTree is overridden in lines 187–264. The method is the same as the one implemented in the BST class, except that you have to rebalance the nodes after deletion in two cases (lines 224, 249).

26.15 Why is the createNewNode method defined protected?
26.16 When is the updateHeight method invoked? When is the balanceFactor method invoked? When is the balancePath method invoked?
26.17 What are data fields in the AVLTree class?
26.18 In the insert and delete methods, once you have performed a rotation to balance a node in the tree, is it possible that there are still unbalanced nodes?
26.8 Testing the AVLTree Class

This section gives an example of using the AVLTree class.

Listing 26.4 gives a test program. The program creates an AVLTree initialized with an array of the integers 25, 20, and 5 (lines 4–5), inserts elements in lines 9–18, and deletes elements in lines 22–28. Since AVLTree is a subclass of BST and the elements in a BST are iterable, the program uses a foreach loop to traverse all the elements in lines 33–35.

Listing 26.4 TestAVLTree.java

```java
public class TestAVLTree {
    public static void main(String[] args) {
        // Create an AVL tree
        AVLTree<Integer> tree = new AVLTree<>(new Integer[]{25, 20, 5});
        System.out.print("After inserting 25, 20, 5:");
        printTree(tree);

        // Insert elements
        tree.insert(34);
        System.out.print("After inserting 34, 50:");
        printTree(tree);
        tree.insert(30);
        System.out.print("After inserting 30");
        printTree(tree);
        tree.insert(10);
        System.out.print("After inserting 10");
        printTree(tree);

        // Delete elements
        tree.delete(34);
        System.out.print("After removing 34, 30, 50:");
        printTree(tree);
        tree.delete(5);
        System.out.print("After removing 5:");
        printTree(tree);

        // Traverse the elements in the tree
        for (int e : tree) {
            System.out.print(e + " ");
        }
    }

    public static void printTree(BST tree) {
        // Traverse tree
        System.out.print("Inorder (sorted): ");
        tree.inorder();
        System.out.print("Postorder: ");
        tree.postorder();
        System.out.print("Preorder: ");
        tree.preorder();
        System.out.print("The number of nodes is "+ tree.getSize());
    }
}
```
26.8 Testing the AVLTree Class

Figure 26.10 shows how the tree evolves as elements are added to the tree. After 25 and 20 are added, the tree is as shown in Figure 26.10a. 5 is inserted as a left child of 20, as shown in Figure 26.10b. The tree is not balanced. It is left-heavy at node 25. Perform an LL rotation to result in an AVL tree, as shown in Figure 26.10c.

After inserting 34, 50:
Inorder (sorted): 5 20 25 34 50
Postorder: 5 25 50 34 20
Preorder: 20 5 34 25 50
The number of nodes is 5

After inserting 30
Inorder (sorted): 5 20 25 30 34 50
Postorder: 5 25 30 50 34 20
Preorder: 25 20 5 34 30 50
The number of nodes is 6

After inserting 10
Inorder (sorted): 5 10 20 25 30 34 50
Postorder: 5 20 10 30 50 34 25
Preorder: 25 10 5 20 34 30 50
The number of nodes is 7

After removing 34, 30, 50:
Inorder (sorted): 5 10 20 25
Postorder: 5 20 25 10
Preorder: 10 5 25 20
The number of nodes is 4

After removing 5:
Inorder (sorted): 10 20 25
Postorder: 10 25 20
Preorder: 20 10 25
The number of nodes is 3
Traverse the elements in the tree: 10 20 25

Figure 26.10 shows how the tree evolves as elements are added to the tree. After 25 and 20 are added, the tree is as shown in Figure 26.10a. 5 is inserted as a left child of 20, as shown in Figure 26.10b. The tree is not balanced. It is left-heavy at node 25. Perform an LL rotation to result in an AVL tree, as shown in Figure 26.10c.

After inserting 34, the tree is shown in Figure 26.10d. After inserting 50, the tree is as shown in Figure 26.10e. The tree is not balanced. It is right-heavy at node 25. Perform an RR rotation to result in an AVL tree, as shown in Figure 26.10f.

After inserting 30, the tree is as shown in Figure 26.10g. The tree is not balanced. Perform an RL rotation to result in an AVL tree, as shown in Figure 26.10h.

After inserting 10, the tree is as shown in Figure 26.10i. The tree is not balanced. Perform an LR rotation to result in an AVL tree, as shown in Figure 26.10j.

```java
47    System.out.println();
48    }
49  }
```
Chapter 26  AVL Trees

Figure 26.11 shows how the tree evolves as elements are deleted. After deleting 34, 30, and 50, the tree is as shown in Figure 26.11b. The tree is not balanced. Perform an LL rotation to result in an AVL tree, as shown in Figure 26.11c.

After deleting 5, the tree is as shown in Figure 26.11d. The tree is not balanced. Perform an RL rotation to result in an AVL tree, as shown in Figure 26.11e.

Figure 26.11 shows how the tree evolves as elements are deleted. After deleting 34, 30, and 50, the tree is as shown in Figure 26.11b. The tree is not balanced. Perform an LL rotation to result in an AVL tree, as shown in Figure 26.11c.

After deleting 5, the tree is as shown in Figure 26.11d. The tree is not balanced. Perform an RL rotation to result in an AVL tree, as shown in Figure 26.11e.

26.19 Show the change of an AVL tree when inserting 1, 2, 3, 4, 10, 9, 7, 5, 8, 6 into the tree, in this order.

26.20 For the tree built in the preceding question, show its change after 1, 2, 3, 4, 10, 9, 7, 5, 8, 6 are deleted from the tree in this order.

26.21 Can you traverse the elements in an AVL tree using a foreach loop?
26.9 AVL Tree Time Complexity Analysis

Since the height of an AVL tree is $O(\log n)$, the time complexity of the **search**, **insert**, and **delete** methods in **AVLTree** is $O(\log n)$.

The time complexity of the **search**, **insert**, and **delete** methods in **AVLTree** depends on the height of the tree. We can prove that the height of the tree is $O(\log n)$.

Let $G(h)$ denote the minimum number of the nodes in an AVL tree with height $h$. Obviously, $G(1) = 1$ and $G(2) = 2$. The minimum number of nodes in an AVL tree with height $h \geq 3$ must have two minimum subtrees: one with height $h - 1$ and the other with height $h - 2$. Thus,

$$G(h) = G(h - 1) + G(h - 2) + 1$$

Recall that a Fibonacci number at index $i$ can be described using the recurrence relation $F(i) = F(i - 1) + F(i - 2)$. Therefore, the function $G(h)$ is essentially the same as $F(i)$. It can be proven that

$$h < 1.4405 \log(n + 2) - 1.3277$$

where $n$ is the number of nodes in the tree. Hence, the height of an AVL tree is $O(\log n)$.

The **search**, **insert**, and **delete** methods involve only the nodes along a path in the tree. The **updateHeight** and **balanceFactor** methods are executed in a constant time for each node in the path. The **balancePath** method is executed in a constant time for a node in the path. Thus, the time complexity for the **search**, **insert**, and **delete** methods is $O(\log n)$.

**Check Point**

26.22 What is the maximum/minimum height for an AVL tree of 3 nodes, 5 nodes, and 7 nodes?

26.23 If an AVL tree has a height of 3, what maximum number of nodes can the tree have? What minimum number of nodes can the tree have?

26.24 If an AVL tree has a height of 4, what maximum number of nodes can the tree have? What minimum number of nodes can the tree have?
CHAPTER SUMMARY

1. An AVL tree is a well-balanced binary tree. In an AVL tree, the difference between the heights of two subtrees for every node is 0 or 1.

2. The process for inserting or deleting an element in an AVL tree is the same as in a regular binary search tree. The difference is that you may have to rebalance the tree after an insertion or deletion operation.

3. Imbalances in the tree caused by insertions and deletions are rebalanced through subtree rotations at the node of the imbalance.

4. The process of rebalancing a node is called a rotation. There are four possible rotations: LL rotation, LR rotation, RR rotation, and RL rotation.

5. The height of an AVL tree is $O(\log n)$. Therefore, the time complexities for the search, insert, and delete methods are $O(\log n)$.

Quiz

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

PROGRAMMING EXERCISES

*26.1 (Display AVL tree graphically) Write a program that displays an AVL tree along with its balance factor for each node.

26.2 (Compare performance) Write a test program that randomly generates 500,000 numbers and inserts them into a BST, reshuffles the 500,000 numbers and performs a search, and reshuffles the numbers again before deleting them from the tree. Write another test program that does the same thing for an AVLTree. Compare the execution times of these two programs.

***26.3 (AVL tree animation) Write a program that animates the AVL tree insert, delete, and search methods, as shown in Figure 26.1.

**26.4 (Parent reference for BST) Suppose that the TreeNode class defined in BST contains a reference to the node’s parent, as shown in Programming Exercise 25.15. Implement the AVLTree class to support this change. Write a test program that adds numbers 1, 2, …, 100 to the tree and displays the paths for all leaf nodes.

**26.5 (The kth smallest element) You can find the kth smallest element in a BST in $O(n)$ time from an inorder iterator. For an AVL tree, you can find it in $O(\log n)$ time. To achieve this, add a new data field named size in AVLTreeNode to store the number of nodes in the subtree rooted at this node. Note that the size of
a node $v$ is one more than the sum of the sizes of its two children. Figure 26.12 shows an AVL tree and the size value for each node in the tree.

![AVL Tree Diagram]

**Figure 26.12** The size data field in AVLTreeNode stores the number of nodes in the subtree rooted at the node.

In the AVLTree class, add the following method to return the $k$th smallest element in the tree.

```java
public E find(int k)
```

The method returns null if $k < 1$ or $k >$ the size of the tree. This method can be implemented using the recursive method `find(k, root)`, which returns the $k$th smallest element in the tree with the specified root. Let $A$ and $B$ be the left and right children of the root, respectively. Assuming that the tree is not empty and $k \leq root.size$, `find(k, root)` can be recursively defined as follows:

```
find(k, root) =
  root.element, if A is null and k is 1;
  B.element, if A is null and k is 2;
  find(k, A), if $k \leq A.size$;
  root.element, if $k = A.size + 1$;
  find(k - A.size - 1, B), if $k > A.size + 1$;
```

Modify the insert and delete methods in AVLTree to set the correct value for the size property in each node. The insert and delete methods will still be in $O(\log n)$ time. The find(k) method can be implemented in $O(\log n)$ time. Therefore, you can find the $k$th smallest element in an AVL tree in $O(\log n)$ time.

Use the following main method to test your program:

```java
import java.util.Scanner;

public class Exercise26_05 {
    public static void main(String[] args) {
        AVLTree<Double> tree = new AVLTree<>();
        Scanner input = new Scanner(System.in);
        System.out.print("Enter 15 numbers: ");
        for (int i = 0; i < 15; i++) {
            tree.insert(input.nextDouble());
        }
        System.out.print("Enter k: ");
        System.out.println("The " + k + "th smallest number is " +
                  tree.find(k));
    }
}
```

**26.6 (Test AVLTree)** Design and write a complete test program to test if the AVLTree class in Listing 26.4 meets all requirements.
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Hashing

Objectives

- To understand what hashing is and what hashing is used for (§27.2).
- To obtain the hash code for an object and design the hash function to map a key to an index (§27.3).
- To handle collisions using open addressing (§27.4).
- To know the differences among linear probing, quadratic probing, and double hashing (§27.4).
- To handle collisions using separate chaining (§27.5).
- To understand the load factor and the need for rehashing (§27.6).
- To implement MyHashMap using hashing (§27.7).
- To implement MyHashSet using hashing (§27.8).
Chapter 27 Hashing

27.1 Introduction

Hashing is super-efficient. It takes $O(1)$ time to search, insert, and delete an element using hashing.

The preceding chapter introduced binary search trees. An element can be found in $O(\log n)$ time in a well-balanced search tree. Is there a more efficient way to search for an element in a container? This chapter introduces a technique called hashing. You can use hashing to implement a map or a set to search, insert, and delete an element in $O(1)$ time.

27.2 What Is Hashing?

Hashing uses a hashing function to map a key to an index.

Before introducing hashing, let us review map, which is a data structure that is implemented using hashing. Recall that a map (introduced in Section 21.5) is a container object that stores entries. Each entry contains two parts: a key and a value. The key, also called a search key, is used to search for the corresponding value. For example, a dictionary can be stored in a map, in which the words are the keys and the definitions of the words are the values.

A map is also called a dictionary, a hash table, or an associative array.

The Java Collections Framework defines the `java.util.Map` interface for modeling maps. Three concrete implementations are `java.util.HashMap`, `java.util.LinkedHashMap`, and `java.util.TreeMap`. `java.util.HashMap` is implemented using hashing, `java.util.LinkedHashMap` using `LinkedList`, and `java.util.TreeMap` using red-black trees. (Bonus Chapter 41 introduces red-black trees.) You will learn the concept of hashing and use it to implement a hash map in this chapter.

If you know the index of an element in the array, you can retrieve the element using the index in $O(1)$ time. So does that mean we can store the values in an array and use the key as the index to find the value? The answer is yes—if you can map a key to an index. The array that stores the values is called a hash table. The function that maps a key to an index in the hash table is called a hash function. As shown in Figure 27.1, a hash function obtains an index from a key and uses the index to retrieve the value for the key. Hashing is a technique that retrieves the value using the index obtained from the key without performing a search.

**Figure 27.1** A hash function maps a key to an index in the hash table.

How do you design a hash function that produces an index from a key? Ideally, we would like to design a function that maps each search key to a different index in the hash table. Such a function is called a perfect hash function. However, it is difficult to find a perfect hash
function. When two or more keys are mapped to the same hash value, we say that a collision has occurred. Although there are ways to deal with collisions, which are discussed later in this chapter, it is better to avoid collisions in the first place. Thus, you should design a fast and easy-to-compute hash function that minimizes collisions.

27.3 Hash Functions and Hash Codes

A typical hash function first converts a search key to an integer value called a hash code, then compresses the hash code into an index to the hash table.

Java’s root class Object has the hashCode method, which returns an integer hash code. By default, the method returns the memory address for the object. The general contract for the hashCode method is as follows:

1. You should override the hashCode method whenever the equals method is overridden to ensure that two equal objects return the same hash code.
2. During the execution of a program, invoking the hashCode method multiple times returns the same integer, provided that the object’s data are not changed.
3. Two unequal objects may have the same hash code, but you should implement the hashCode method to avoid too many such cases.

27.3.1 Hash Codes for Primitive Types

For search keys of the type byte, short, int, and char, simply cast them to int. Therefore, two different search keys of any one of these types will have different hash codes.

For a search key of the type float, use Float.floatToIntBits(key) as the hash code. Note that Float.floatToIntBits(float f) returns an int value whose bit representation is the same as the bit representation for the floating number f. Thus, two different search keys of the float type will have different hash codes.

For a search key of the type long, simply casting it to int would not be a good choice, because all keys that differ in only the first 32 bits will have the same hash code. To take the first 32 bits into consideration, divide the 64 bits into two halves and perform the exclusive-or operation to combine the two halves. This process is called folding. The hash code for a long key is

```java
int hashCode = (int)(key ^ (key >> 32));
```

Note that >> is the right-shift operator that shifts the bits 32 positions to the right. For example, 1010110 >> 2 yields 0010101. The ^ is the bitwise exclusive-or operator. It operates on two corresponding bits of the binary operands. For example, 1010110 ^ 0110111 yields 1100001. For more on bitwise operations, see Appendix G, Bitwise Operations.

For a search key of the type double, first convert it to a long value using the Double.doubleToLongBits method, and then perform a folding as follows:

```java
long bits = Double.doubleToLongBits(key);
int hashCode = (int)(bits ^ (bits >> 32));
```

27.3.2 Hash Codes for Strings

Search keys are often strings, so it is important to design a good hash function for strings. An intuitive approach is to sum the Unicode of all characters as the hash code for the string. This approach may work if two search keys in an application don’t contain the same letters, but...
it will produce a lot of collisions if the search keys contain the same letters, such as `tod` and `dot`.

A better approach is to generate a hash code that takes the position of characters into consideration. Specifically, let the hash code be

$$s_0 b^{(n-1)} + s_1 b^{(n-2)} + \ldots + s_{n-1}$$

where $s_i$ is `s.charAt(i)`. This expression is a polynomial for some positive $b$, so this is called a *polynomial hash code*. Using Horner’s rule for polynomial evaluation (see Section 6.7), the hash code can be calculated efficiently as follows:

$$(\ldots ((s_0 b + s_1) b + s_2) b + \ldots + s_{n-2}) b + s_{n-1}$$

This computation can cause an overflow for long strings, but arithmetic overflow is ignored in Java. You should choose an appropriate value $b$ to minimize collisions. Experiments show that good choices for $b$ are 31, 33, 37, 39, and 41. In the `String` class, the `hashCode` is overridden using the polynomial hash code with $b$ being 31.

### 27.3.3 Compressing Hash Codes

The hash code for a key can be a large integer that is out of the range for the hash-table index, so you need to scale it down to fit in the index’s range. Assume the index for a hash table is between 0 and $N-1$. The most common way to scale an integer to between 0 and $N-1$ is to use

$$h(\text{hashCode}) = \text{hashCode} \mod N$$

To ensure that the indices are spread evenly, choose $N$ to be a prime number greater than 2.

Ideally, you should choose a prime number for $N$. However, it is time consuming to find a large prime number. In the Java API implementation for `java.util.HashMap`, $N$ is set to a value of the power of 2. There is a good reason for this choice. When $N$ is a value of the power of 2,

$$h(\text{hashCode}) = \text{hashCode} \mod N$$

is the same as

$$h(\text{hashCode}) = \text{hashCode} \& (N - 1)$$

The ampersand, &, is a bitwise AND operator (see Appendix G, Bitwise Operations). The AND of two corresponding bits yields a 1 if both bits are 1. For example, assume $N = 4$ and \(\text{hashCode} = 11\), \(11 \mod 4 = 3\), which is the same as \(01011 \& 00011 = 11\). The & operator can be performed much faster than the % operator.

To ensure that the hashing is evenly distributed, a supplemental hash function is also used along with the primary hash function in the implementation of `java.util.HashMap`. This function is defined as:

```java
private static int supplementalHash(int h) {
    h ^= (h >>> 20) ^ (h >>> 12);
    return h ^ (h >>> 7) ^ (h >>> 4);
}
```

^ and >>> are bitwise exclusive-or and unsigned right-shift operations (also introduced in Appendix G). The bitwise operations are much faster than the multiplication, division, and remainder operations. You should replace these operations with the bitwise operations whenever possible.

The complete hash function is defined as:

$$h(\text{hashCode}) = \text{supplementalHash(hashCode)} \mod N$$
This is the same as
\[ h(\text{hashCode}) = \text{supplementalHash(hashCode)} \& (N - 1) \]
since \( N \) is a value of the power of 2.

27.2 What is a hash code? What is the hash code for \texttt{Byte}, \texttt{Short}, \texttt{Integer}, and \texttt{Character}?

27.3 How is the hash code for a \texttt{Float} object computed?

27.4 How is the hash code for a \texttt{Long} object computed?

27.5 How is the hash code for a \texttt{Double} object computed?

27.6 How is the hash code for a \texttt{String} object computed?

27.7 How is a hash code compressed to an integer representing the index in a hash table?

27.8 If \( N \) is a value of the power of 2, is \( N / 2 \) same as \( N \gg 1 \)?

27.9 If \( N \) is a value of the power of 2, is \( m \% N \) same as \( m \& (N - 1) \) for any integer \( m \)?

27.4 Handling Collisions Using Open Addressing

A collision occurs when two keys are mapped to the same index in a hash table. Generally, there are two ways for handling collisions: open addressing and separate chaining.

Open addressing is the process of finding an open location in the hash table in the event of a collision. Open addressing has several variations: linear probing, quadratic probing, and double hashing.

27.4.1 Linear Probing

When a collision occurs during the insertion of an entry to a hash table, linear probing finds the next available location sequentially. For example, if a collision occurs at \texttt{hashTable[k % N]}, check whether \texttt{hashTable[(k+1) % N]} is available. If not, check \texttt{hashTable[(k+2) % N]} and so on, until an available cell is found, as shown in Figure 27.2.

\[ \text{New element with key 26 to be inserted} \]
\[ \text{Probe 3 times before finding an empty cell} \]

For simplicity, only the keys are shown and the values are not shown. Here \( N \) is 11 and index = key \% N.

\[ \text{FIGURE 27.2} \quad \text{Linear probing finds the next available location sequentially.} \]
To search for an entry in the hash table, obtain the index, say \( k \), from the hash function for the key. Check whether \( \text{hashTable}[k \mod N] \) contains the entry. If not, check whether \( \text{hashTable}[(k+1) \mod N] \) contains the entry, and so on, until it is found, or an empty cell is reached.

To remove an entry from the hash table, search the entry that matches the key. If the entry is found, place a special marker to denote that the entry is available. Each cell in the hash table has three possible states: occupied, marked, or empty. Note that a marked cell is also available for insertion.

Linear probing tends to cause groups of consecutive cells in the hash table to be occupied. Each group is called a cluster. Each cluster is actually a probe sequence that you must search when retrieving, adding, or removing an entry. As clusters grow in size, they may merge into even larger clusters, further slowing down the search time. This is a big disadvantage of linear probing.

### Pedagogical Note

For an interactive GUI demo to see how linear probing works, go to [www.cs.armstrong.edu/liang/animation/HashingLinearProbingAnimation.html](http://www.cs.armstrong.edu/liang/animation/HashingLinearProbingAnimation.html), as shown in Figure 27.3.

#### 27.4.2 Quadratic Probing

Quadratic probing can avoid the clustering problem that can occur in linear probing. Linear probing looks at the consecutive cells beginning at index \( k \). Quadratic probing, on the other hand, looks at the cells at indices \( (k + j^2) \mod N \), for \( j \geq 0 \), that is, \( k \mod N, (k + 1)\mod N, (k + 4) \mod N, (k + 9)\mod N \), and so on, as shown in Figure 27.4.
27.4 Handling Collisions Using Open Addressing

Quadratic probing works in the same way as linear probing except for a change in the search sequence. Quadratic probing avoids linear probing’s clustering problem, but it has its own clustering problem, called secondary clustering; that is, the entries that collide with an occupied entry use the same probe sequence.

Linear probing guarantees that an available cell can be found for insertion as long as the table is not full. However, there is no such guarantee for quadratic probing.

**Pedagogical NOTE**

For an interactive GUI demo to see how quadratic probing works, go to [www.cs.armstrong.edu/liang/animation/HashingQuadraticProbingAnimation.html](http://www.cs.armstrong.edu/liang/animation/HashingQuadraticProbingAnimation.html), as shown in Figure 27.5.

### 27.4.3 Double Hashing

Another open addressing scheme that avoids the clustering problem is known as double hashing. Starting from the initial index \( k \), both linear probing and quadratic probing add an increment to \( k \) to define a search sequence. The increment is 1 for linear probing and \( j^2 \) for quadratic probing. These increments are independent of the keys. Double hashing uses a secondary hash function \( h'(key) \) on the keys to determine the increments to avoid the clustering problem. Specifically, double hashing looks at the cells at indices \( (k + j \cdot h'(key)) \mod N \), for \( j \geq 0 \), that is, \( k \mod N, (k + h'(key)) \mod N, (k + 2 \cdot h'(key)) \mod N, (k + 3 \cdot h'(key)) \mod N \), and so on.

For example, let the primary hash function \( h \) and secondary hash function \( h' \) on a hash table of size 11 be defined as follows:

\[
\begin{align*}
  h(key) &= key \mod 11; \\
  h'(key) &= 7 - key \mod 7;
\end{align*}
\]

For a search key of 12, we have

\[
\begin{align*}
  h(12) &= 12 \mod 11 = 1; \\
  h'(12) &= 7 - 12 \mod 7 = 2;
\end{align*}
\]

Suppose the elements with the keys 45, 58, 4, 28, and 21 are already placed in the hash table. We now insert the element with key 12. The probe sequence for key 12 starts at index 1. Since the cell at index 1 is already occupied, search the next cell at index 3 (1 + 1 \( \neq 2 \)). Since the cell at index 3 is already occupied, search the next cell at index 5 (1 + 2 \( \neq 2 \)). Since the cell at index 5 is empty, the element for key 12 is now inserted at this cell. The search process is illustrated in Figure 27.6.

The indices of the probe sequence are as follows: 1, 3, 5, 7, 9, 0, 2, 4, 6, 8, 10. This sequence reaches the entire table. You should design your functions to produce a probe sequence that
Chapter 27  Hashing

**Figure 27.5** The animation tool shows how quadratic probing works.

**Figure 27.6** The secondary hash function in a double hashing determines the increment of the next index in the probe sequence.

reaches the entire table. Note that the second function should never have a zero value, since zero is not an increment.

**27.10** What is open addressing? What is linear probing? What is quadratic probing? What is double hashing?

**27.11** Describe the clustering problem for linear probing.
27.12 What is secondary clustering?

27.13 Show the hash table of size 11 after inserting entries with keys 34, 29, 53, 44, 120, 39, 45, and 40, using linear probing.

27.14 Show the hash table of size 11 after inserting entries with keys 34, 29, 53, 44, 120, 39, 45, and 40, using quadratic probing.

27.15 Show the hash table of size 11 after inserting entries with keys 34, 29, 53, 44, 120, 39, 45, and 40, using double hashing with the following functions:

\[ h(k) = k \% 11; \]
\[ h'(k) = 7 - k \% 7; \]

27.5 Handling Collisions Using Separate Chaining

The separate chaining scheme places all entries with the same hash index in the same location, rather than finding new locations. Each location in the separate chaining scheme uses a bucket to hold multiple entries.

You can implement a bucket using an array, ArrayList, or LinkedList. We will use LinkedList for demonstration. You can view each cell in the hash table as the reference to the head of a linked list, and elements in the linked list are chained starting from the head, as shown in Figure 27.7.

![Figure 27.7](image)

27.16 Show the hash table of size 11 after inserting entries with the keys 34, 29, 53, 44, 120, 39, 45, and 40, using separate chaining.

27.6 Load Factor and Rehashing

The load factor measures how full a hash table is. If the load factor is exceeded, increase the hash-table size and reload the entries into a new larger hash table. This is called rehashing.

Load factor \( \lambda \) (lambda) measures how full a hash table is. It is the ratio of the number of elements to the size of the hash table, that is, \( \lambda = \frac{n}{N} \) where \( n \) denotes the number of elements and \( N \) the number of locations in the hash table.

Note that \( \lambda \) is zero if the hash table is empty. For the open addressing scheme, \( \lambda \) is between 0 and 1; \( \lambda \) is 1 if the hash table is full. For the separate chaining scheme, \( \lambda \) can be any value.
As $\lambda$ increases, the probability of a collision increases. Studies show that you should maintain the load factor under $0.5$ for the open addressing scheme and under $0.9$ for the separate chaining scheme.

Keeping the load factor under a certain threshold is important for the performance of hashing. In the implementation of the `java.util.HashMap` class in the Java API, the threshold $0.75$ is used. Whenever the load factor exceeds the threshold, you need to increase the hash-table size and rehash all the entries in the map into a new larger hash table. Notice that you need to change the hash functions, since the hash-table size has been changed. To reduce the likelihood of rehashing, since it is costly, you should at least double the hash-table size. Even with periodic rehashing, hashing is an efficient implementation for map.

**Pedagogical Note**
For an interactive GUI demo to see how separate chaining works, go to [www.cs.armstrong.edu/liang/animation/HashingUsingSeparateChainingAnimation.html](http://www.cs.armstrong.edu/liang/animation/HashingUsingSeparateChainingAnimation.html), as shown in Figure 27.8.

---

**Figure 27.8** The animation tool shows how separate chaining works.

---

**27.17** What is load factor? Assume the hash table has the initial size $4$ and its load factor is $0.5$; show the hash table after inserting entries with the keys $34, 29, 53, 44, 120, 39, 45,$ and $40$, using linear probing.

**27.18** Assume the hash table has the initial size $4$ and its load factor is $0.5$; show the hash table after inserting entries with the keys $34, 29, 53, 44, 120, 39, 45,$ and $40$, using quadratic probing.
27.19 Assume the hash table has the initial size 4 and its load factor is 0.5; show the hash table after inserting entries with the keys 34, 29, 53, 44, 120, 39, 45, and 40, using separate chaining.

27.7 Implementing a Map Using Hashing

A map can be implemented using hashing.

Now you understand the concept of hashing. You know how to design a good hash function to map a key to an index in a hash table, how to measure performance using the load factor, and how to increase the table size and rehash to maintain the performance. This section demonstrates how to implement a map using separate chaining.

We design our custom Map interface to mirror java.util.Map and name the interface MyMap and a concrete class MyHashMap, as shown in Figure 27.9.

**Figure 27.9** MyHashMap implements the MyMap interface.
How do you implement `MyHashMap`? If you use an `ArrayList` and store a new entry at the end of the list, the search time will be $O(n)$. If you implement `MyHashMap` using a binary tree, the search time will be $O(\log n)$ if the tree is well balanced. Nevertheless, you can implement `MyHashMap` using hashing to obtain an $O(1)$ time search algorithm. Listing 27.1 shows the `MyMap` interface and Listing 27.2 implements `MyHashMap` using separate chaining.

**Listing 27.1  MyMap.java**

```java
public interface MyMap<K, V> {
    public void clear();
    public boolean containsKey(K key);
    public boolean containsValue(V value);
    public java.util.Set<Entry<K, V>> entrySet();
    public V get(K key);
    public boolean isEmpty();
    public java.util.Set<K> keySet();
    public void remove(K key);
    public int size();
    public java.util.Set<V> values();

    public static class Entry<K, V> {
        public Entry(K key, V value) {
            this.key = key;
            this.value = value;
        }

        public K getKey() {
            return key;
        }

        public V getValue() {
            return value;
        }
    }
}
```
@Override
public String toString() {
    return "[" + key + ", " + value + "]";
}
}

LISTING 27.2  MyHashMap.java

```java
import java.util.LinkedList;

public class MyHashMap<K, V> implements MyMap<K, V> {
    // Define the default hash-table size. Must be a power of 2
    private static int DEFAULT_INITIAL_CAPACITY = 4;
    // Define the maximum hash-table size. 1 << 30 is same as 2^30
    private static int MAXIMUM_CAPACITY = 1 << 30;
    // Current hash-table capacity. Capacity is a power of 2
    private int capacity;
    // Define default load factor
    private static float DEFAULT_MAX_LOAD_FACTOR = 0.75f;
    // Specify a load factor used in the hash table
    private float loadFactorThreshold;
    // The number of entries in the map
    private int size = 0;
    // Hash table is an array with each cell being a linked list
    LinkedList<MyMap.Entry<K,V>>[] table;

    /** Construct a map with the default capacity and load factor */
    public MyHashMap() {
        this(DEFAULT_INITIAL_CAPACITY, DEFAULT_MAX_LOAD_FACTOR);
    }

    /** Construct a map with the specified initial capacity and *
     * default load factor */
    public MyHashMap(int initialCapacity) {
        this(initialCapacity, DEFAULT_MAX_LOAD_FACTOR);
    }

    /** Construct a map with the specified initial capacity *
     * and load factor */
    public MyHashMap(int initialCapacity, float loadFactorThreshold) {
        if (initialCapacity > MAXIMUM_CAPACITY)
            this.capacity = MAXIMUM_CAPACITY;
        else
            this.capacity = trimToPowerOf2(initialCapacity);
        this.loadFactorThreshold = loadFactorThreshold;
        table = new LinkedList[capacity];
    }

    @Override /** Remove all of the entries from this map */
    public void clear() {
        size = 0;
        removeEntries();
    }
```
@Override /** Return true if the specified key is in the map */
public boolean containsKey(K key) {
    if (get(key) != null)
        return true;
    else
        return false;
}

@Override /** Return true if this map contains the value */
public boolean containsValue(V value) {
    for (int i = 0; i < capacity; i++) {
        if (table[i] != null) {
            LinkedList<Entry<K, V>> bucket = table[i];
            for (Entry<K, V> entry: bucket)
                if (entry.getValue().equals(value))
                    return true;
        }
    }
    return false;
}

@Override /** Return a set of entries in the map */
public java.util.Set<MyMap.Entry<K,V>> entrySet() {
    java.util.Set<MyMap.Entry<K, V>> set =
        new java.util.HashSet<>();
    for (int i = 0; i < capacity; i++) {
        if (table[i] != null) {
            LinkedList<Entry<K, V>> bucket = table[i];
            for (Entry<K, V> entry: bucket)
                set.add(entry);
        }
    }
    return set;
}

@Override /** Return the value that matches the specified key */
public V get(K key) {
    int bucketIndex = hash(key.hashCode());
    if (table[bucketIndex] != null) {
        LinkedList<Entry<K, V>> bucket = table[bucketIndex];
        for (Entry<K, V> entry: bucket)
            if (entry.getKey().equals(key))
                return entry.getValue();
    }
    return null;
}

@Override /** Return true if this map contains no entries */
public boolean isEmpty() {
    return size == 0;
}

@Override /** Return a set consisting of the keys in this map */
public java.util.Set<K> keySet() {
    java.util.Set<K> set = new java.util.HashSet<>();

for (int i = 0; i < capacity; i++) {
    if (table[i] != null) {
        LinkedList<Entry<K, V>> bucket = table[i];
        for (Entry<K, V> entry: bucket)
            set.add(entry.getKey());
    }
}

return set;

@Override /** Add an entry (key, value) into the map */
public V put(K key, V value) {
    if (get(key) != null) { // The key is already in the map
        int bucketIndex = hash(key.hashCode());
        LinkedList<Entry<K, V>> bucket = table[bucketIndex];
        for (Entry<K, V> entry: bucket)
            if (entry.getKey().equals(key)) {
                V oldValue = entry.getValue();
                // Replace old value with new value
                entry.value = value;
                // Return the old value for the key
                return oldValue;
            }
    }

    // Check load factor
    if (size >= capacity * loadFactorThreshold) {
        if (capacity == MAXIMUM_CAPACITY)
            throw new RuntimeException("Exceeding maximum capacity");
        rehash();
    }

    int bucketIndex = hash(key.hashCode());

    // Create a linked list for the bucket if not already created
    if (table[bucketIndex] == null) {
        table[bucketIndex] = new LinkedList<Entry<K, V>>();
    }

    // Add a new entry (key, value) to hashTable[index]
    table[bucketIndex].add(new MyMap.Entry<K, V>(key, value));
    size++; // Increase size

    return value;
}

@Override /** Remove the entries for the specified key */
public void remove(K key) {
    int bucketIndex = hash(key.hashCode());

    // Remove the first entry that matches the key from a bucket
    if (table[bucketIndex] != null) {
        LinkedList<Entry<K, V>> bucket = table[bucketIndex];
        for (Entry<K, V> entry: bucket)
            if (entry.getKey().equals(key)) {
                bucket.remove(entry);
            }
    }
}
size--; // Decrease size
break; // Remove just one entry that matches the key
}
}

@Override /** Return the number of entries in this map */
public int size() {
  return size;
}

@Override /** Return a set consisting of the values in this map */
public java.util.Set<V> values() {
  java.util.Set<V> set = new java.util.HashSet<>();
  for (int i = 0; i < capacity; i++) {
    if (table[i] != null) {
      LinkedList<Entry<K, V>> bucket = table[i];
      for (Entry<K, V> entry: bucket)
        set.add(entry.getValue());
    }
  }
  return set;
}

/** Hash function */
private int hash(int hashCode) {
  return supplementalHash(hashCode) & (capacity - 1);
}

/** Ensure the hashing is evenly distributed */
private static int supplementalHash(int h) {
  h ^= (h >>> 20) ^ (h >>> 12);
  return h ^ (h >>> 7) ^ (h >>> 4);
}

/** Return a power of 2 for initialCapacity */
private int trimToPowerOf2(int initialCapacity) {
  int capacity = 1;
  while (capacity < initialCapacity) {
    capacity <<= 1; // Same as capacity *= 2. <= is more efficient
  }
  return capacity;
}

/** Remove all entries from each bucket */
private void removeEntries() {
  for (int i = 0; i < capacity; i++) {
    if (table[i] != null) {
      table[i].clear();
    }
  }
}

/** Rehash the map */
private void rehash() {
  java.util.Set<Entry<K, V>> set = entrySet(); // Get entries
  capacity <<= 1; // Same as capacity *= 2. <= is more efficient
27.7 Implementing a Map Using Hashing

```
233    table = new LinkedList[capacity]; // Create a new hash table
234    size = 0; // Reset size to 0
235    for (Entry<K, V> entry: set) {
236        put(entry.getKey(), entry.getValue()); // Store to new table
237    }
238  }
239
240  @Override /** Return a string representation for this map */
241  public String toString() {
242      StringBuilder builder = new StringBuilder("[");
243      for (int i = 0; i < capacity; i++) {
244        if (table[i] != null && table[i].size() > 0)
245          for (Entry<K, V> entry: table[i])
246            builder.append(entry);
247      }
248      builder.append("]");
249      return builder.toString();
250  }
```

The `MyHashMap` class implements the `MyMap` interface using separate chaining. The parameters that determine the hash-table size and load factors are defined in the class. The default initial capacity is 4 (line 5) and the maximum capacity is $2^{30}$ (line 8). The current hash-table capacity is designed as a value of the power of 2 (line 11). The default load-factor threshold is 0.75f (line 14). You can specify a custom load-factor threshold when constructing a map. The custom load-factor threshold is stored in `loadFactorThreshold` (line 17). The data field `size` denotes the number of entries in the map (line 20). The hash table is an array. Each cell in the array is a linked list (line 23).

Three constructors are provided to construct a map. You can construct a default map with the default capacity and load-factor threshold using the no-arg constructor (lines 26–28), a map with the specified capacity and a default load-factor threshold (lines 32–34), and a map with the specified capacity and load-factor threshold (lines 38–46).

The `clear` method removes all entries from the map (lines 49–52). It invokes `removeEntries()`, which deletes all entries in the buckets (lines 221–227). The `removeEntries()` method takes $O(\text{capacity})$ time to clear all entries in the table.

The `containsKey(key)` method checks whether the specified key is in the map by invoking the `get` method (lines 55–60). Since the `get` method takes $O(1)$ time, the `containsKey(key)` method takes $O(1)$ time.

The `containsValue(value)` method checks whether the value is in the map (lines 63–74). This method takes $O(\text{capacity} + \text{size})$ time. It is actually $O(\text{capacity})$, since \text{capacity} > \text{size}.

The `entrySet()` method returns a set that contains all entries in the map (lines 77–90). This method takes $O(\text{capacity})$ time.

The `get(key)` method returns the value of the first entry with the specified key (lines 93–103). This method takes $O(1)$ time.

The `isEmpty()` method simply returns true if the map is empty (lines 106–108). This method takes $O(1)$ time.

The `keySet()` method returns all keys in the map as a set. The method finds the keys from each bucket and adds them to a set (lines 111–123). This method takes $O(\text{capacity})$ time.

The `put(key, value)` method adds a new entry into the map. The method first tests if the key is already in the map (line 127), if so, it locates the entry and replaces the old value with the new value in the entry for the key (line 134) and the old value is returned (line 136). If
the key is new in the map, the new entry is created in the map (line 156). Before inserting the new entry, the method checks whether the size exceeds the load-factor threshold (line 141). If so, the program invokes `rehash()` (line 145) to increase the capacity and store entries into the new larger hash table.

The `rehash()` method first copies all entries in a set (line 231), doubles the capacity (line 232), creates a new hash table (line 233), and resets the size to 0 (line 234). The method then copies the entries into the new hash table (lines 236–238). The `rehash` method takes $O(\text{capacity})$ time. If no rehash is performed, the `put` method takes $O(1)$ time to add a new entry.

The `remove(key)` method removes the entry with the specified key in the map (lines 164–177). This method takes $O(1)$ time.

The `size()` method simply returns the size of the map (lines 180–182). This method takes $O(1)$ time.

The `values()` method returns all values in the map. The method examines each entry from all buckets and adds it to a set (lines 185–197). This method takes $O(\text{capacity})$ time.

The `hash()` method invokes the `supplementalHash` to ensure that the hashing is evenly distributed to produce an index for the hash table (lines 200–208). This method takes $O(1)$ time.

Table 27.1 summarizes the time complexities of the methods in `MyHashMap`.

Table 27.1 Time Complexities for Methods in `MyHashMap`

<table>
<thead>
<tr>
<th>Methods</th>
<th>Time</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>clear()</code></td>
<td>$O(\text{capacity})$</td>
</tr>
<tr>
<td><code>containsKey(key: Key)</code></td>
<td>$O(1)$</td>
</tr>
<tr>
<td><code>containsValue(value: V)</code></td>
<td>$O(\text{capacity})$</td>
</tr>
<tr>
<td><code>entrySet()</code></td>
<td>$O(\text{capacity})$</td>
</tr>
<tr>
<td><code>get(key: K)</code></td>
<td>$O(1)$</td>
</tr>
<tr>
<td><code>isEmpty()</code></td>
<td>$O(1)$</td>
</tr>
<tr>
<td><code>keySet()</code></td>
<td>$O(\text{capacity})$</td>
</tr>
<tr>
<td><code>put(key: K, value: V)</code></td>
<td>$O(1)$</td>
</tr>
<tr>
<td><code>remove(key: K)</code></td>
<td>$O(1)$</td>
</tr>
<tr>
<td><code>size()</code></td>
<td>$O(1)$</td>
</tr>
<tr>
<td><code>values()</code></td>
<td>$O(\text{capacity})$</td>
</tr>
<tr>
<td><code>rehash()</code></td>
<td>$O(\text{capacity})$</td>
</tr>
</tbody>
</table>

Since rehashing does not happen very often, the time complexity for the `put` method is $O(1)$. Note that the complexities of the `clear, entrySet, keySet, values,` and `rehash` methods depend on `capacity`, so to avoid poor performance for these methods you should choose an initial capacity carefully.

Listing 27.3 gives a test program that uses `MyHashMap`.

Listing 27.3 TestMyHashMap.java

```java
public class TestMyHashMap {
    public static void main(String[] args) {
        // Create a map
        MyMap<String, Integer> map = new MyHashMap<>();
        map.put("Smith", 30);
        map.put("Anderson", 31);
        map.put("Lewis", 29);
        map.put("Cook", 29);
```
map.put("Smith", 65);
System.out.println("Entries in map: "+ map);
System.out.println("The age for Lewis is "+ map.get("Lewis"));
System.out.println("Is Smith in the map? "+ map.containsKey("Smith"));
System.out.println("Is age 33 in the map? "+ map.containsValue(33));
map.remove("Smith");
System.out.println("Entries in map: "+ map);
map.clear();
System.out.println("Entries in map: "+ map);
}

Entries in map: [[Anderson, 31][Smith, 65][Lewis, 29][Cook, 29]]
The age for Lewis is 29
Is Smith in the map? true
Is age 33 in the map? false
Entries in map: [[Anderson, 31][Lewis, 29][Cook, 29]]
Entries in map: []

The program creates a map using MyHashMap (line 4) and adds five entries into the map (lines 5–9). Line 5 adds key Smith with value 30 and line 9 adds Smith with value 65. The latter value replaces the former value. The map actually has only four entries. The program displays the entries in the map (line 11), gets a value for a key (line 14), checks whether the map contains the key (line 17) and a value (line 19), removes an entry with the key Smith (line 21), and redisplays the entries in the map (line 22). Finally, the program clears the map (line 24) and displays an empty map (line 25).

27.20 What is 1 << 30 in line 8 in Listing 27.2? What are the integers resulted from 1 << 1, 1 << 2, and 1 << 3?

27.21 What are the integers resulted from 32 >> 1, 32 >> 2, 32 >> 3, and 32 >> 4?

27.22 In Listing 27.2, will the program work if LinkedList is replaced by ArrayList?
In Listing 27.2, how do you replace the code in lines 55–59 using one line of code?

27.23 Describe how the put(key, value) method is implemented in the MyHashMap class.

27.24 In Listing 27.5, the supplementalHash method is declared static, can the hash method be declared static?

27.25 Show the output of the following code.

MyMap<String, String> map = new MyHashMap<>();
map.put("Texas", "Dallas");
map.put("Oklahoma", "Norman");
map.put("Texas", "Austin");
map.put("Oklahoma", "Tulsa");
System.out.println(map.get("Texas");
System.out.println(map.size());
27.8 Implementing Set Using Hashing

A hash set can be implemented using a hash map.

A set (introduced in Chapter 21) is a data structure that stores distinct values. The Java Collections Framework defines the `java.util.Set` interface for modeling sets. Three concrete implementations are `java.util.HashSet`, `java.util.LinkedHashSet`, and `java.util.TreeSet`. `java.util.HashSet` is implemented using hashing, `java.util.LinkedHashSet` using `LinkedList`, and `java.util.TreeSet` using red-black trees.

You can implement `MyHashSet` using the same approach as for implementing `MyHashMap`. The only difference is that key/value pairs are stored in the map, while elements are stored in the set.

We design our custom `Set` interface to mirror `java.util.Set` and name the interface `MySet` and a concrete class `MyHashSet`, as shown in Figure 27.10.

**Key Point**

A hash set can be implemented using a hash map.

**Figure 27.10** `MyHashSet` implements the `MySet` interface.

Listing 27.4 shows the `MySet` interface and Listing 27.5 implements `MyHashSet` using separate chaining.

**Listing 27.4** `MySet.java`

```java
public interface MySet<E> extends java.lang.Iterable<E> {
    /** Remove all elements from this set */
    public void clear();
    /** Return true if the element is in the set */
    public boolean contains(E e);
    /** Adds the element to the set and returns true if the element is added successfully. */
    public boolean add(E e);
    /** Removes the element from the set and returns true if the set contained the element. */
    public boolean remove(E e);
    /** Returns true if this set does not contain any elements. */
    public boolean isEmpty();
    /** Returns the number of elements in this set. */
    public int size();
}
```

```java
public class MyHashSet<E> implements MySet<E> {
    // Implementation details...
}
```
public boolean contains(E e);  
/** Add an element to the set */
public boolean add(E e);  
/** Remove the element from the set */
public boolean remove(E e);  
/** Return true if the set doesn't contain any elements */
public boolean isEmpty();  
/** Return the number of elements in the set */
public int size();

LISTING 27.5  MyHashSet.java

import java.util.LinkedList;

public class MyHashSet<E> implements MySet<E> {
    // Define the default hash-table size. Must be a power of 2
    private static int DEFAULT_INITIAL_CAPACITY = 4;
    // Define the maximum hash-table size. 1 << 30 is same as 2^30
    private static int MAXIMUM_CAPACITY = 1 << 30;
    // Current hash-table capacity. Capacity is a power of 2
    private int capacity;
    // Define default load factor
    private static float DEFAULT_MAX_LOAD_FACTOR = 0.75f;
    // Specify a load-factor threshold used in the hash table
    private float loadFactorThreshold;
    // The number of elements in the set
    private int size = 0;
    // Hash table is an array with each cell being a linked list
    private LinkedList<E>[] table;
    /** Construct a set with the default capacity and load factor */
    public MyHashSet() {
        this(DEFAULT_INITIAL_CAPACITY, DEFAULT_MAX_LOAD_FACTOR);
    }
    /** Construct a set with the specified initial capacity and
     * default load factor */
    public MyHashSet(int initialCapacity) {
        this(initialCapacity, DEFAULT_MAX_LOAD_FACTOR);
    }
    /** Construct a set with the specified initial capacity
     * and load factor */
    public MyHashSet(int initialCapacity, float loadFactorThreshold) {
        if (initialCapacity > MAXIMUM_CAPACITY)
            this.capacity = MAXIMUM_CAPACITY;
        else
            this.capacity = trimToPowerOf2(initialCapacity);
```java
    this.loadFactorThreshold = loadFactorThreshold;
    table = new LinkedList[capacity];
  }

  /** Remove all elements from this set */
  public void clear() {
    size = 0;
    removeElements();
  }

  /** Return true if the element is in the set */
  public boolean contains(E e) {
    int bucketIndex = hash(e.hashCode());
    if (table[bucketIndex] != null) {
      LinkedList<E> bucket = table[bucketIndex];
      for (E element : bucket)
        if (element.equals(e))
          return true;
    }
    return false;
  }

  /** Add an element to the set */
  public boolean add(E e) {
    if (contains(e)) // Duplicate element not stored
      return false;
    if (size + 1 > capacity * loadFactorThreshold) {
      if (capacity == MAXIMUM_CAPACITY)
        throw new RuntimeException("Exceeding maximum capacity");
      rehash();
    }
    int bucketIndex = hash(e.hashCode());
    // Create a linked list for the bucket if not already created
    if (table[bucketIndex] == null) {
      table[bucketIndex] = new LinkedList<E>();
    }
    // Add e to hashTable[index]
    table[bucketIndex].add(e);
    size++; // Increase size
    return true;
  }

  /** Remove the element from the set */
  public boolean remove(E e) {
    if (!contains(e))
      return false;
    int bucketIndex = hash(e.hashCode());
    // Create a linked list for the bucket if not already created
    if (table[bucketIndex] != null) {
    }
```
LinkedList<E> bucket = table[bucketIndex];
for (E element: bucket)
  if (e.equals(element)) {
    bucket.remove(element);
    break;
  }
}
size--; // Decrease size
return true;

@Override /** Return true if the set contain no elements */
public boolean isEmpty() {
  return size == 0;
}

@Override /** Return the number of elements in the set */
public int size() {
  return size;
}

@Override /** Return an iterator for the elements in this set */
public java.util.Iterator<E> iterator() {
  return new MyHashSetIterator(this);
}

/** Inner class for iterator */
private class MyHashSetIterator implements java.util.Iterator<E> {
  // Store the elements in a list
  private java.util.ArrayList<E> list;
  private int current = 0; // Point to the current element in list
  private MyHashSet<E> set;

  /** Create a list from the set */
  public MyHashSetIterator(MyHashSet<E> set) {
    this.set = set;
    list = setToList();
  }

  @Override /** Next element for traversing? */
  public boolean hasNext() {
    if (current < list.size())
      return true;
    return false;
  }

  @Override /** Get current element and move cursor to the next */
  public E next() {
    return list.get(current++);
  }

  /** Remove the current element and refresh the list */
  public void remove() {
    // Delete the current element from the hash set
    set.remove(list.get(current));
    list.remove(current); // Remove current element from the list
Chapter 27 Hashing

```java
/** Hash function */
private int hash(int hashCode) {
    return supplementalHash(hashCode) & (capacity - 1);
}

/** Ensure the hashing is evenly distributed */
private static int supplementalHash(int h) {
    h ^= (h >>> 20) ^ (h >>> 12);
    return h ^ (h >>> 7) ^ (h >>> 4);
}

/** Return a power of 2 for initialCapacity */
private int trimToPowerOf2(int initialCapacity) {
    int capacity = 1;
    while (capacity < initialCapacity) {
        capacity <<= 1; // Same as capacity *= 2. <= is more efficient
    }
    return capacity;
}

/** Remove all e from each bucket */
private void removeElements() {
    for (int i = 0; i < capacity; i++) {
        if (table[i] != null) {
            table[i].clear();
        }
    }
}

/** Rehash the set */
private void rehash() {
    java.util.ArrayList<E> list = setToList(); // Copy to a list
    capacity <<= 1; // Same as capacity *= 2. <= is more efficient
    table = new LinkedList[capacity]; // Create a new hash table
    size = 0;
    for (E element: list) {
        add(element); // Add from the old table to the new table
    }
}

/** Copy elements in the hash set to an array list */
private java.util.ArrayList<E> setToList() {
    java.util.ArrayList<E> list = new java.util.ArrayList<>();
    for (int i = 0; i < capacity; i++) {
        if (table[i] != null) {
            for (E e: table[i]) {
                list.add(e);
            }
        }
    }
    return list;
}

@Override /** Return a string representation for this set */
```
```java
public String toString() {
    java.util.ArrayList<E> list = setToList();
    StringBuilder builder = new StringBuilder("[");
    // Add the elements except the last one to the string builder
    for (int i = 0; i < list.size() - 1; i++) {
        builder.append(list.get(i) + ", ");
    }
    // Add the last element in the list to the string builder
    if (list.size() == 0)
        builder.append("]");
    else
        builder.append(list.get(list.size() - 1) + "]");
    return builder.toString();
}
```

The `MyHashSet` class implements the `MySet` interface using separate chaining. Implementing `MyHashSet` is very similar to implementing `MyHashMap` except for the following differences:

1. The elements are stored in the hash table for `MyHashSet`, but the entries (key/value pairs) are stored in the hash table for `MyHashMap`.

2. `MySet` extends `java.lang.Iterable` and `MyHashSet` implements `MySet` and overrides `iterator()`. So the elements in `MyHashSet` are iterable.

Three constructors are provided to construct a set. You can construct a default set with the default capacity and load factor using the no-arg constructor (lines 26–28), a set with the specified capacity and a default load factor (lines 32–34), and a set with the specified capacity and load factor (lines 38–46).

The `clear` method removes all elements from the set (lines 49–52). It invokes `removeElements()`, which clears all table cells (line 190). Each table cell is a linked list that stores the elements with the same hash code. The `removeElements()` method takes \(O(\text{capacity})\) time.

The `contains(element)` method checks whether the specified element is in the set by examining whether the designated bucket contains the element (lines 55–65). This method takes \(O(1)\) time.

The `add(element)` method adds a new element into the set. The method first checks if the element is already in the set (line 69). If so, the method returns false. The method then checks whether the size exceeds the load-factor threshold (line 72). If so, the program invokes `rehash()` (line 76) to increase the capacity and store elements into the new larger hash table.

The `rehash()` method first copies all elements in a list (line 197), doubles the capacity (line 198), creates a new hash table (line 199), and resets the size to 0 (line 200). The method then copies the elements into the new larger hash table (lines 202–204). The `rehash` method takes \(O(\text{capacity})\) time. If no rehash is performed, the `add` method takes \(O(1)\) time to add a new element.

The `remove(element)` method removes the specified element in the set (lines 95–114). This method takes \(O(1)\) time.

The `size()` method simply returns the number of elements in the set (lines 122–124). This method takes \(O(1)\) time.

The `iterator()` method returns an instance of `java.util.Iterator`. The `MyHashSetIterator` class implements `java.util.Iterator` to create a forward iterator. When a `MyHashSetIterator` is constructed, it copies all the elements in the set to a list.
The variable \texttt{current} points to the element in the list. Initially, \texttt{current} is 0 (line 135), which points to the first element in the list. \texttt{MyHashSetIterator} implements the methods \texttt{hasNext()}, \texttt{next()}, and \texttt{remove()} in \texttt{java.util.Iterator}. Invoking \texttt{hasNext()} returns true if \texttt{current < list.size()}. Invoking \texttt{next()} returns the current element and moves \texttt{current} to point to the next element (line 153). Invoking \texttt{remove()} removes the current element in the iterator from the set.

The \texttt{hash()} method invokes the \texttt{supplementalHash} to ensure that the hashing is evenly distributed to produce an index for the hash table (lines 166–174). This method takes \(O(1)\) time.

Table 27.2 summarizes the time complexity of the methods in \texttt{MyHashSet}.

<table>
<thead>
<tr>
<th>Method</th>
<th>Time</th>
</tr>
</thead>
<tbody>
<tr>
<td>clear()</td>
<td>(O(\text{capacity}))</td>
</tr>
<tr>
<td>contains(e: E)</td>
<td>(O(1))</td>
</tr>
<tr>
<td>add(e: E)</td>
<td>(O(1))</td>
</tr>
<tr>
<td>remove(e: E)</td>
<td>(O(1))</td>
</tr>
<tr>
<td>isEmpty()</td>
<td>(O(1))</td>
</tr>
<tr>
<td>size()</td>
<td>(O(1))</td>
</tr>
<tr>
<td>iterator()</td>
<td>(O(\text{capacity}))</td>
</tr>
<tr>
<td>rehash()</td>
<td>(O(\text{capacity}))</td>
</tr>
</tbody>
</table>

Listing 27.6 gives a test program that uses \texttt{MyHashSet}.

**LISTING 27.6 TestMyHashSet.java**

```java
public class TestMyHashSet {
  public static void main(String[] args) {
    // Create a MyHashSet
    MySet<String> set = new MyHashSet<>();
    // Add elements
    set.add("Smith");
    set.add("Anderson");
    set.add("Lewis");
    set.add("Cook");
    set.add("Smith");
    // Display elements
    System.out.println("Elements in set: " + set);
    // Get size
    System.out.println("Number of elements in set: " + set.size());
    // Check if Smith is in set
    System.out.println("Is Smith in set? " + set.contains("Smith"));
    // Remove element
    set.remove("Smith");
    // Print names in uppercase
    System.out.println("Names in set in uppercase are ");
    for (String s: set) { System.out.print(s.toUpperCase() + " "); }
    // Clear set
    set.clear();
    // Display elements after clearing
    System.out.println("Elements in set: " + set);
  }
}
```
The program creates a set using `MyHashSet` (line 4) and adds five elements to the set (lines 5–9). Line 5 adds Smith and line 9 adds Smith again. Since only nonduplicate elements are stored in the set, Smith appears in the set only once. The set actually has four elements. The program displays the elements (line 11), gets its size (line 12), checks whether the set contains a specified element (line 13), and removes an element (line 15). Since the elements in a set are iterable, a foreach loop is used to traverse all elements in the set (lines 17–18). Finally, the program clears the set (line 20) and displays an empty set (line 21).

27.26 Why can you use a foreach loop to traverse the elements in a set?

27.27 Describe how the `add(e)` method is implemented in the `MyHashSet` class.

27.28 In Listing 27.5, the `remove` method in the iterator removes the current element from the set. It also removes the current element from the internal list (line 161):
```
list.remove(current); // Remove current element from the list
```
Is this necessary?

27.29 Replace the code in lines 146-149 In Listing 27.5 using one statement.

**Key Terms**

<table>
<thead>
<tr>
<th>Term</th>
<th>Page</th>
</tr>
</thead>
<tbody>
<tr>
<td>associative array</td>
<td>986</td>
</tr>
<tr>
<td>cluster</td>
<td>990</td>
</tr>
<tr>
<td>dictionary</td>
<td>986</td>
</tr>
<tr>
<td>double hashing</td>
<td>991</td>
</tr>
<tr>
<td>hash code</td>
<td>987</td>
</tr>
<tr>
<td>hash function</td>
<td>986</td>
</tr>
<tr>
<td>hash map</td>
<td>1004</td>
</tr>
<tr>
<td>hash set</td>
<td>1004</td>
</tr>
<tr>
<td>hash table</td>
<td>986</td>
</tr>
<tr>
<td>linear probing</td>
<td>989</td>
</tr>
<tr>
<td>load factor</td>
<td>993</td>
</tr>
<tr>
<td>open addressing</td>
<td>989</td>
</tr>
<tr>
<td>perfect hash function</td>
<td>986</td>
</tr>
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<td>polynomial hash code</td>
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</tr>
<tr>
<td>quadratic probing</td>
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</tr>
<tr>
<td>rehashing</td>
<td>993</td>
</tr>
<tr>
<td>secondary clustering</td>
<td>991</td>
</tr>
<tr>
<td>separate chaining</td>
<td>993</td>
</tr>
</tbody>
</table>

**Chapter Summary**

1. A *map* is a data structure that stores entries. Each entry contains two parts: a *key* and a *value*. The key is also called a *search key*, which is used to search for the corresponding value. You can implement a map to obtain $O(1)$ time complexity on searching, retrieval, insertion, and deletion using the hashing technique.

2. A *set* is a data structure that stores elements. You can use the hashing technique to implement a set to achieve $O(1)$ time complexity on searching, insertion, and deletion for a set.

3. *Hashing* is a technique that retrieves the value using the index obtained from a key without performing a search. A typical *hash function* first converts a search key to
an integer value called a hash code, then compresses the hash code into an index to the hash table.

4. A collision occurs when two keys are mapped to the same index in a hash table. Generally, there are two ways for handling collisions: open addressing and separate chaining.

5. Open addressing is the process of finding an open location in the hash table in the event of collision. Open addressing has several variations: linear probing, quadratic probing, and double hashing.

6. The separate chaining scheme places all entries with the same hash index into the same location, rather than finding new locations. Each location in the separate chaining scheme is called a bucket. A bucket is a container that holds multiple entries.

**Quiz**

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

**Programming Exercises**

**27.1** (Implement MyMap using open addressing with linear probing) Create a new concrete class that implements MyMap using open addressing with linear probing. For simplicity, use \( f(key) = key \% size \) as the hash function, where size is the hash-table size. Initially, the hash-table size is 4. The table size is doubled whenever the load factor exceeds the threshold (0.5).

**27.2** (Implement MyMap using open addressing with quadratic probing) Create a new concrete class that implements MyMap using open addressing with quadratic probing. For simplicity, use \( f(key) = key \% size \) as the hash function, where \( size \) is the hash-table size. Initially, the hash-table size is 4. The table size is doubled whenever the load factor exceeds the threshold (0.5).

**27.3** (Implement MyMap using open addressing with double hashing) Create a new concrete class that implements MyMap using open addressing with double hashing. For simplicity, use \( f(key) = key \% size \) as the hash function, where \( size \) is the hash-table size. Initially, the hash-table size is 4. The table size is doubled whenever the load factor exceeds the threshold (0.5).

**27.4** (Modify MyHashMap with duplicate keys) Modify MyHashMap to allow duplicate keys for entries. You need to modify the implementation for the put(key, value) method. Also add a new method named getAll(key) that returns a set of values that match the key in the map.

**27.5** (Implement MyHashSet using MyHashMap) Implement MyHashSet using MyHashMap. Note that you can create entries with (key, key), rather than (key, value).

**27.6** (Animate linear probing) Write a program that animates linear probing, as shown in Figure 27.3. You can change the initial size of the hash-table in the program. Assume the load-factor threshold is 0.75.

**27.7** (Animate separate chaining) Write a program that animates MyHashMap, as shown in Figure 27.8. You can change the initial size of the table. Assume the load-factor threshold is 0.75.
27.8 (Animate quadratic probing) Write a program that animates quadratic probing, as shown in Figure 27.5. You can change the initial size of the hash-table in program. Assume the load-factor threshold is 0.75.

27.9 (Implement hashCode for string) Write a method that returns a hash code for string using the approach described in Section 27.3.2 with b value 31. The function header is as follows:

```java
public static int hashCodeForString(String s)
```

27.10 (Compare MyHashSet and MyArrayList) MyArrayList is defined in Listing 24.3. Write a program that generates 1000000 random double values between 0 and 999999 and stores them in a MyArrayList and in a MyHashSet. Generate a list of 1000000 random double values between 0 and 1999999. For each number in the list, test if it is in the array list and in the hash set. Run your program to display the total test time for the array list and for the hash set.

27.11 (setToList) Write the following method that returns an ArrayList from a set.

```java
public static <E> ArrayList<E> setToList(Set<E> s)
```
GRAPHS AND APPLICATIONS

Objectives

■ To model real-world problems using graphs and explain the Seven Bridges of Königsberg problem (§28.1).

■ To describe the graph terminologies: vertices, edges, simple graphs, weighted/unweighted graphs, and directed/undirected graphs (§28.2).

■ To represent vertices and edges using lists, edge arrays, edge objects, adjacency matrices, and adjacency lists (§28.3).

■ To model graphs using the Graph interface, the AbstractGraph class, and the UnweightedGraph class (§28.4).

■ To display graphs visually (§28.5).

■ To represent the traversal of a graph using the AbstractGraph.Tree class (§28.6).

■ To design and implement depth-first search (§28.7).

■ To solve the connected-circle problem using depth-first search (§28.8).

■ To design and implement breadth-first search (§28.9).

■ To solve the nine-tail problem using breadth-first search (§28.10).
28.1 Introduction

Many real-world problems can be solved using graph algorithms. Graphs are useful in modeling and solving real-world problems. For example, the problem to find the least number of flights between two cities can be modeled using a graph, where the vertices represent cities and the edges represent the flights between two adjacent cities, as shown in Figure 28.1. The problem of finding the minimal number of connecting flights between two cities is reduced to finding a shortest path between two vertices in a graph.

![Figure 28.1](image1.png)

Figure 28.1 A graph can be used to model the flights between the cities.

The study of graph problems is known as graph theory. Graph theory was founded by Leonhard Euler in 1736, when he introduced graph terminology to solve the famous Seven Bridges of Königsberg problem. The city of Königsberg, Prussia (now Kaliningrad, Russia), was divided by the Pregel River. There were two islands on the river. The city and islands were connected by seven bridges, as shown in Figure 28.2a. The question is, can one take a walk, cross each bridge exactly once, and return to the starting point? Euler proved that it is not possible.

![Figure 28.2](image2.png)

Figure 28.2 Seven bridges connected islands and land.

To establish a proof, Euler first abstracted the Königsberg city map by eliminating all streets, producing the sketch shown in Figure 28.2a. Next, he replaced each land mass with
a dot, called a *vertex* or a *node*, and each bridge with a line, called an *edge*, as shown in Figure 28.2b. This structure with vertices and edges is called a *graph*.

Looking at the graph, we ask whether there is a path starting from any vertex, traversing all edges exactly once, and returning to the starting vertex. Euler proved that for such a path to exist, each vertex must have an even number of edges. Therefore, the Seven Bridges of Königsberg problem has no solution.

Graph problems are often solved using algorithms. Graph algorithms have many applications in various areas, such as in computer science, mathematics, biology, engineering, economics, genetics, and social sciences. This chapter presents the algorithms for depth-first search and breadth-first search, and their applications. The next chapter presents the algorithms for finding a minimum spanning tree and shortest paths in weighted graphs, and their applications.

### 28.2 Basic Graph Terminologies

A graph consists of vertices, and edges that connect the vertices.

This chapter does not assume that you have any prior knowledge of graph theory or discrete mathematics. We use plain and simple terms to define graphs.

**What is a graph?** A graph is a mathematical structure that represents relationships among entities in the real world. For example, the graph in Figure 28.1 represents the flights among cities, and the graph in Figure 28.2b represents the bridges among land masses.

A graph consists of a nonempty set of vertices (also known as nodes or points), and a set of edges that connect the vertices. For convenience, we define a graph as $G = (V, E)$, where $V$ represents a set of vertices and $E$ represents a set of edges. For example, $V$ and $E$ for the graph in Figure 28.1 are as follows:


$$E = \{\{"Seattle", "San Francisco"\},\{"Seattle", "Chicago"\}, \{"Seattle", "Denver"\}, \{"San Francisco", "Denver"\}, \ldots \};$$

A graph may be directed or undirected. In a *directed graph*, each edge has a direction, which indicates that you can move from one vertex to the other through the edge. You can model parent/child relationships using a directed graph, where an edge from vertex $A$ to $B$ indicates that $A$ is a parent of $B$. Figure 28.3a shows a directed graph.

In an *undirected graph*, you can move in both directions between vertices. The graph in Figure 28.1 is undirected.
Edges may be weighted or unweighted. For example, you can assign a weight for each edge in the graph in Figure 28.1 to indicate the flight time between the two cities.

Two vertices in a graph are said to be adjacent if they are connected by the same edge. Similarly, two edges are said to be adjacent if they are connected to the same vertex. An edge in a graph that joins two vertices is said to be incident to both vertices. The degree of a vertex is the number of edges incident to it.

Two vertices are called neighbors if they are adjacent. Similarly, two edges are called neighbors if they are adjacent.

A loop is an edge that links a vertex to itself. If two vertices are connected by two or more edges, these edges are called parallel edges. A simple graph is one that has doesn’t have any loops or parallel edges. In a complete graph, every two pairs of vertices are connected, as shown in Figure 28.3b.

A graph is connected if there exists a path between any two vertices in the graph. A subgraph of a graph \( G \) is a graph whose vertex set is a subset of that of \( G \) and whose edge set is a subset of that of \( G \). For example, the graph in Figure 28.3c is a subgraph of the graph in Figure 28.3b.

Assume that the graph is connected and undirected. A cycle is a closed path that starts from a vertex and ends at the same vertex. A connected graph is a tree if it does not have cycles. A spanning tree of a graph \( G \) is a connected subgraph of \( G \) and the subgraph is a tree that contains all vertices in \( G \).

**Pedagogical Note**

Before we introduce graph algorithms and applications, it is helpful to get acquainted with graphs using the interactive tool at [www.cs.armstrong.edu/liang/animation/GraphLearningTool.html](http://www.cs.armstrong.edu/liang/animation/GraphLearningTool.html), as shown in Figure 28.4. The tool allows you to add/remove/move vertices and draw edges using mouse gestures. You can also find depth-first search (DFS) trees and breadth-first search (BFS) trees, and a shortest path between two vertices.

**Figure 28.4** You can use the tool to create a graph with mouse gestures and show DFS/BFS trees and shortest paths.
28.1 What is the famous Seven Bridges of Königsberg problem?

28.2 What is a graph? Explain the following terms: undirected graph, directed graph, weighted graph, degree of a vertex, parallel edge, simple graph, complete graph, connected graph, cycle, subgraph, tree, and spanning tree.

28.3 How many edges are in a complete graph with 5 vertices? How many edges are in a tree of 5 vertices?

28.4 How many edges are in a complete graph with n vertices? How many edges are in a tree of n vertices?

28.3 Representing Graphs

Representing a graph is to store its vertices and edges in a program. The data structure for storing a graph is arrays or lists.

To write a program that processes and manipulates graphs, you have to store or represent data for the graphs in the computer.

28.3.1 Representing Vertices

The vertices can be stored in an array or a list. For example, you can store all the city names in the graph in Figure 28.1 using the following array:

```java
String[] vertices = {
```

**Note**
The vertices can be objects of any type. For example, you can consider cities as objects that contain the information such as its name, population, and mayor. Thus, you may define vertices as follows:

```java
City city0 = new City("Seattle", 608660, "Mike McGinn");
...
City city11 = new City("Houston", 2099451, "Annise Parker");
City[] vertices = {city0, city1, ... , city11};
```

**public class** City {
    private String cityName;
    private int population;
    private String mayor;

    public City(String cityName, int population, String mayor) {
        this.cityName = cityName;
        this.population = population;
        this.mayor = mayor;
    }

    public String getCityName() {
        return cityName;
    }

    public int getPopulation() {
        return population;
    }
}
The vertices can be conveniently labeled using natural numbers $0, 1, 2, \ldots, n - 1$, for a graph for $n$ vertices. Thus, $\text{vertices}[0]$ represents "Seattle", $\text{vertices}[1]$ represents "San Francisco", and so on, as shown in Figure 28.5.

![Figure 28.5](image)

**Figure 28.5** An array stores the vertex names.

**Note**
You can reference a vertex by its name or its index, whichever is more convenient. Obviously, it is easy to access a vertex via its index in a program.

### 28.3.2 Representing Edges: Edge Array

The edges can be represented using a two-dimensional array. For example, you can store all the edges in the graph in Figure 28.1 using the following array:

```java
int[][] edges = {
    {0, 1}, {0, 3}, {0, 5},
    {1, 0}, {1, 2}, {1, 3},
    {2, 1}, {2, 3}, {2, 4}, {2, 10},
    {3, 0}, {3, 1}, {3, 2}, {3, 4}, {3, 5},
    {4, 2}, {4, 3}, {4, 5}, {4, 7}, {4, 8}, {4, 10},
    {5, 0}, {5, 3}, {5, 4}, {5, 6}, {5, 7},
};
```
{6, 5}, {6, 7},
{7, 4}, {7, 5}, {7, 6}, {7, 8},
{8, 4}, {8, 7}, {8, 9}, {8, 10}, {8, 11},
{9, 8}, {9, 11},
{10, 2}, {10, 4}, {10, 8}, {10, 11},
{11, 8}, {11, 9}, {11, 10}
};

This representation is known as the edge array. The vertices and edges in Figure 28.3a can be represented as follows:

String[] names = {
"Peter", "Jane", "Mark", "Cindy", "Wendy"};

int[][] edges = {
{0, 2}, {1, 2}, {2, 4}, {3, 4}];

28.3.3 Representing Edges: Edge Objects

Another way to represent the edges is to define edges as objects and store the edges in a java.util.ArrayList. The Edge class can be defined as follows:

```java
public class Edge {
    int u;
    int v;

    public Edge(int u, int v) {
        this.u = u;
        this.v = v;
    }

    public boolean equals(Object o) {
        return u == ((Edge)o).u && v == ((Edge)o).v;
    }
}
```

For example, you can store all the edges in the graph in Figure 28.1 using the following list:

```java
java.util.ArrayList<Edge> list = new java.util.ArrayList<>();
list.add(new Edge(0, 1));
list.add(new Edge(0, 3));
list.add(new Edge(0, 5));
...
```

Storing Edge objects in an ArrayList is useful if you don't know the edges in advance.

While representing edges using an edge array or Edge objects in Section 28.3.2 and earlier in this section may be intuitive for input, it's not efficient for internal processing. The next two sections introduce the representation of graphs using adjacency matrices and adjacency lists. These two data structures are efficient for processing graphs.

28.3.4 Representing Edges: Adjacency Matrices

Assume that the graph has n vertices. You can use a two-dimensional n x n matrix, say adjacencyMatrix, to represent the edges. Each element in the array is 0 or 1. adjacencyMatrix[i][j] is 1 if there is an edge from vertex i to vertex j; otherwise, adjacencyMatrix[i][j] is 0. If the graph is undirected, the matrix is symmetric, because adjacencyMatrix[i][j] is the same as adjacencyMatrix[j][i]. For example, the edges in the graph in Figure 28.1 can be represented using an adjacency matrix as follows:

```java
int[][] adjacencyMatrix = {
{0, 1, 0, 0, 0, 0, 0, 0, 0}, // Seattle
{1, 0, 1, 0, 0, 0, 0, 0, 0}, // San Francisco
```
You can represent edges using adjacency vertex lists or adjacency edge lists. An adjacency vertex list for a vertex \( i \) contains the vertices that are adjacent to \( i \) and an adjacency edge list for a vertex \( i \) contains the edges that are adjacent to \( i \). You may define an array of lists. The array has \( n \) entries, and each entry is a list. The adjacency vertex list for vertex \( i \) contains all the vertices \( j \) such that there is an edge from vertex \( i \) to vertex \( j \). For example, to represent the edges in the graph in Figure 28.1, you can create an array of lists as follows:

```java
java.util.List<Integer>[] neighbors = new java.util.List[12];
neighbors[0] contains all vertices adjacent to vertex 0 (i.e., Seattle), neighbors[1] contains all vertices adjacent to vertex 1 (i.e., San Francisco), and so on, as shown in Figure 28.6.

To represent the adjacency edge lists for the graph in Figure 28.1, you can create an array of lists as follows:

```java
java.util.List<Edge>[] neighbors = new java.util.List[12];
neighbors[0] contains all edges adjacent to vertex 0 (i.e., Seattle), neighbors[1] contains all edges adjacent to vertex 1 (i.e., San Francisco), and so on, as shown in Figure 28.7.

You can represent a graph using an adjacency matrix or adjacency lists. Which one is better? If the graph is dense (i.e., there are a lot of edges), using an adjacency matrix is preferred. If the graph is very sparse (i.e., very few edges), using adjacency lists is better, because using an adjacency matrix would waste a lot of space.

Both adjacency matrices and adjacency lists can be used in a program to make algorithms more efficient. For example, it takes \( O(1) \) constant time to check whether two vertices are connected using an adjacency matrix, and it takes linear time \( O(m) \) to print all edges in a graph using adjacency lists, where \( m \) is the number of edges.
28.3 Representing Graphs

Note

Adjacency vertex list is simpler for representing unweighted graphs. However, adjacency edge lists are more flexible for a wide range of graph applications. It is easy to add additional constraints on edges using adjacency edge lists. For this reason, this book will use adjacency edge lists to represent graphs.

You can use arrays, array lists, or linked lists to store adjacency lists. We will use lists instead of arrays, because the lists are easily expandable to enable you to add new vertices. Furthermore, we will use array lists instead of linked lists, because our algorithms only require searching for adjacent vertices in the list. Using array lists is more efficient for our algorithms. Using array lists, the adjacency edge list in Figure 28.6 can be built as follows:

```java
List<ArrayList<Edge>> neighbors = new ArrayList<>();
neighbors.add(new ArrayList<Edge>());
neighbors.get(0).add(new Edge(0, 1));
```
neighbors.get(0).add(new Edge(0, 3));
neighbors.get(0).add(new Edge(0, 5));
neighbors.add(new ArrayList<Edge>());
neighbors.get(1).add(new Edge(1, 0));
neighbors.get(1).add(new Edge(1, 2));
neighbors.get(1).add(new Edge(1, 3));
...
neighbors.get(11).add(new Edge(11, 8));
neighbors.get(11).add(new Edge(11, 9));
neighbors.get(11).add(new Edge(11, 10));

28.5 How do you represent vertices in a graph? How do you represent edges using an edge array? How do you represent an edge using an edge object? How do you represent edges using an adjacency matrix? How do you represent edges using adjacency lists?

28.6 Represent the following graph using an edge array, a list of edge objects, an adjacency matrix, an adjacency vertex list, and an adjacency edge list, respectively.

![Graph](image)

28.4 Modeling Graphs

The Graph interface defines the common operations for a graph.

The Java Collections Framework serves as a good example for designing complex data structures. The common features of data structures are defined in the interfaces (e.g., Collection, Set, List, Queue), as shown in Figure 20.1. Abstract classes (e.g., AbstractCollection, AbstractSet, AbstractList) partially implement the interfaces. Concrete classes (e.g., HashSet, LinkedHashSet, TreeSet, ArrayList, LinkedList, PriorityQueue) provide concrete implementations. This design pattern is useful for modeling graphs. We will define an interface named Graph that contains all the common operations of graphs and an abstract class named AbstractGraph that partially implements the Graph interface. Many concrete graphs can be added to the design. For example, we will define such graphs named UnweightedGraph and WeightedGraph. The relationships of these interfaces and classes are illustrated in Figure 28.8.

![Figure 28.8](image)

Figure 28.8 Graphs can be modeled using interfaces, abstract classes, and concrete classes.

What are the common operations for a graph? In general, you need to get the number of vertices in a graph, get all vertices in a graph, get the vertex object with a specified index, get the index of the vertex with a specified name, get the neighbors for a vertex, get the degree for a vertex, clear the graph, add a new vertex, add a new edge, perform a depth-first search, and...
perform a breadth-first search. Depth-first search and breadth-first search will be introduced in the next section. Figure 28.9 illustrates these methods in the UML diagram.

AbstractGraph does not introduce any new methods. A list of vertices and an edge adjacency list are defined in the AbstractGraph class. With these data fields, it is sufficient to

```
+getSize(): int
+getVertices(): List<V>
+getVertex(index: int): V
+getIndex(v: V): int
+getNeighbors(index: int): List<Integer>
+getDegree(index: int): int
+printEdges(): void
+clear(): void
+addVertex(v, V): boolean
+addEdge(u: int, v: int): boolean
+dfs(v: int): AbstractGraph<V>.Tree
+bfs(v: int): AbstractGraph<V>.Tree
```

Returns the number of vertices in the graph.
Returns the vertices in the graph.
Returns the vertex object for the specified vertex index.
Returns the index for the specified vertex.
Returns the neighbors of vertex with the specified index.
Returns the degree for a specified vertex index.
Prints the edges.
Clears the graph.
Returns true if v is added to the graph. Returns false if v is already in the graph.
Adds an edge from u to v to the graph throws IllegalArgumentException if u or v is invalid. Returns true if the edge is added and false if (u, v) is already in the graph.
Obtains a depth-first search tree starting from v.
Obtains a breadth-first search tree starting from v.

```
«interface»
Graph<V>
```

The generic type V is the type for vertices.

```
#vertices: List<V>
#neighbors: List<List<Edge>>

#AbstractGraph()
#AbstractGraph(verticies: V[], edges: int[][])
#AbstractGraph(verticies: List<V>, edges: List<Edge>)
#AbstractGraph(edges: int[][], numberOfVertices: int)
#AbstractGraph(edges: List<Edge>, numberOfVertices: int)
+addEdge(e: Edge): boolean
```

Vertices in the graph.
Neighbors for each vertex in the graph.
Constructs an empty graph.
Constructs a graph with the specified edges and vertices stored in arrays.
Constructs a graph with the specified edges and vertices stored in lists.
Constructs a graph with the specified edges in an array and the integer vertices 1, 2, ...,
Constructs a graph with the specified edges in a list and the integer vertices 1, 2, ...
Adds an edge into the adjacency edge list.

```
UnweightedGraph<V>
```

Constructs an empty unweighted graph.
Constructs a graph with the specified edges and vertices in arrays.
Constructs a graph with the specified edges and vertices stored in lists.
Constructs a graph with the specified edges in an array and the integer vertices 1, 2, ...
Constructs a graph with the specified edges in a list and the integer vertices 1, 2, ...

**Figure 28.9** The Graph interface defines the common operations for all types of graphs.
implement all the methods defined in the `Graph` interface. For convenience, we assume the graph is a simple graph, i.e., a vertex has no edge to itself and there are no parallel edges from vertex \( u \) to \( v \).

`AbstractGraph` implements all the methods from `Graph`, and it does not introduce any new methods except a convenient `addEdge(edge)` method that adds an `Edge` object to the adjacency edge list. `UnweightedGraph` simply extends `AbstractGraph` with five constructors for creating the concrete `Graph` instances.

**Note**

You can create a graph with any type of vertices. Each vertex is associated with an index, which is the same as the index of the vertex in the vertices list. If you create a graph without specifying the vertices, the vertices are the same as their indices.

**Note**

The `AbstractGraph` class implements all the methods in the `Graph` interface. So why is it defined as abstract? In the future, you may need to add new methods to the `Graph` interface that cannot be implemented in `AbstractGraph`. To make the classes easy to maintain, it is desirable to define the `AbstractGraph` class as abstract.

Assume all these interfaces and classes are available. Listing 28.1 gives a test program that creates the graph in Figure 28.1 and another graph for the one in Figure 28.3a.

**Listing 28.1 TestGraph.java**

```java
public class TestGraph {
    public static void main(String[] args) {
        String[] vertices = {
            "Seattle", "San Francisco", "Los Angeles",
            "Atlanta", "Miami", "Dallas", "Houston"};

        int[][] edges = {
            {0, 1}, {0, 3}, {0, 5},
            {1, 0}, {1, 2}, {1, 3},
            {2, 1}, {2, 3}, {2, 4}, {2, 10},
            {3, 0}, {3, 1}, {3, 2}, {3, 4}, {3, 5},
            {4, 2}, {4, 3}, {4, 5}, {4, 7}, {4, 8}, {4, 10},
            {5, 0}, {5, 3}, {5, 4}, {5, 6}, {5, 7},
            {6, 5}, {6, 7},
            {7, 4}, {7, 5}, {7, 6}, {7, 8},
            {8, 4}, {8, 7}, {8, 9}, {8, 10}, {8, 11},
            {9, 8}, {9, 11},
            {10, 2}, {10, 4}, {10, 8}, {10, 11},
            {11, 8}, {11, 9}, {11, 10}
        };

        Graph<String> graph1 = new UnweightedGraph<>(vertices, edges);
        System.out.println("The number of vertices in graph1: ", graph1.getSize());
        System.out.println("The vertex with index 1 is ", graph1.getVertex(1));
        System.out.println("The index for Miami is ", graph1.getIndex("Miami"));
        graph1.printEdges();

        String[] names = {
            "Peter", "Jane", "Mark", "Cindy", "Wendy"};
```
```java
java.util.ArrayList<AbstractGraph.Edge> edgeList = new java.util.ArrayList<>();
edgestList.add(new AbstractGraph.Edge(0, 2));
edgestList.add(new AbstractGraph.Edge(1, 2));
edgestList.add(new AbstractGraph.Edge(2, 4));
edgestList.add(new AbstractGraph.Edge(3, 4));
// Create a graph with 5 vertices
Graph<String> graph2 = new UnweightedGraph<>(
    java.util.Arrays.asList(names), edgeList);
System.out.println("The number of vertices in graph2: ");
graph2.printEdges();
}
```

The program creates `graph1` for the graph in Figure 28.1 in lines 3–23. The vertices for `graph1` are defined in lines 3–5. The edges for `graph1` are defined in 8–21. The edges are represented using a two-dimensional array. For each row i in the array, `edges[i][0]` and `edges[i][1]` indicate that there is an edge from vertex `edges[i][0]` to vertex `edges[i][1]`. For example, the first row, `{0, 1}`, represents the edge from vertex 0 (`edges[0][0]`) to vertex 1 (`edges[0][1]`). The row `{0, 5}` represents the edge from vertex 0 (`edges[2][0]`) to vertex 5 (`edges[2][1]`). The graph is created in line 23. Line 31 invokes the `printEdges()` method on `graph1` to display all edges in `graph1`.

The program creates `graph2` for the graph in Figure 28.3a in lines 34–43. The edges for `graph2` are defined in lines 37–40. `graph2` is created using a list of `Edge` objects in line 43. Line 47 invokes the `printEdges()` method on `graph2` to display all edges in `graph2`.

Note that both `graph1` and `graph2` contain the vertices of strings. The vertices are associated with indices 0, 1, ..., n-1. The index is the location of the vertex in `vertices`. For example, the index of vertex `Miami` is 9.
Now we turn our attention to implementing the interface and classes. Listings 28.2, 28.3, and 28.4 give the Graph interface, the AbstractGraph class, and the UnweightedGraph class, respectively.

**Listing 28.2  Graph.java**

```java
public interface Graph<V> {
    // Return the number of vertices in the graph */
    public int getSize();
    // Return the vertices in the graph */
    public java.util.List<V> getVertices();
    // Return the object for the specified vertex index */
    public V getVertex(int index);
    // Return the index for the specified vertex object */
    public int getIndex(V v);
    // Return the neighbors of vertex with the specified index */
    public java.util.List<Integer> getNeighbors(int index);
    // Return the degree for a specified vertex */
    public int getDegree(int v);
    // Print the edges */
    public void printEdges();
    // Clear the graph */
    public void clear();
    // Add a vertex to the graph */
    public void addVertex(V vertex);
    // Add an edge to the graph */
    public void addEdge(int u, int v);
    // Obtain a depth-first search tree starting from v */
    public AbstractGraph<V>.Tree dfs(int v);
    // Obtain a breadth-first search tree starting from v */
    public AbstractGraph<V>.Tree bfs(int v);
}
```

**Listing 28.3  AbstractGraph.java**

```java
import java.util.*;

public abstract class AbstractGraph<V> implements Graph<V> {
    protected List<V> vertices = new ArrayList<>(); // Store vertices
    protected List<List<Edge>> neighbors = new ArrayList<>(); // Adjacency lists
    // Construct an empty graph */
    protected AbstractGraph() {
    }
    // Construct a graph from vertices and edges stored in arrays */
    protected AbstractGraph(V[] vertices, int[][] edges) {
```
for (int i = 0; i < vertices.length; i++)
    addVertex(vertices[i]);

createAdjacencyLists(edges, vertices.length);
}

/** Construct a graph from vertices and edges stored in List */
protected AbstractGraph(List<V> vertices, List<Edge> edges) {
    for (int i = 0; i < vertices.size(); i++)
        addVertex(vertices.get(i));

    createAdjacencyLists(edges, vertices.size());
}

/** Construct a graph for integer vertices 0, 1, 2 and edge list */
protected AbstractGraph(List<Edge> edges, int numberOfVertices) {
    for (int i = 0; i < numberOfVertices; i++)
        addVertex((V)(new Integer(i))); // vertices is {0, 1, ...}

    createAdjacencyLists(edges, numberOfVertices);
}

/** Construct a graph from integer vertices 0, 1, 2 and edge array */
protected AbstractGraph(int[][] edges, int numberOfVertices) {
    for (int i = 0; i < numberOfVertices; i++)
        addVertex((V)(new Integer(i))); // vertices is {0, 1, ...}

    createAdjacencyLists(edges, numberOfVertices);
}

/** Create adjacency lists for each vertex */
private void createAdjacencyLists(
    int[][] edges, int numberOfVertices) {
    for (int i = 0; i < edges.length; i++)
        addEdge(edges[i][0], edges[i][1]);
}

/** Create adjacency lists for each vertex */
private void createAdjacencyLists(
    List<Edge> edges, int numberOfVertices) {
    for (Edge edge: edges) {
        addEdge(edge.u, edge.v);
    }

    @Override /** Return the number of vertices in the graph */
    public int getSize() {
        return vertices.size();
    }

    @Override /** Return the vertices in the graph */
    public List<V> getVertices() {
        return vertices;
    }

    @Override /** Return the object for the specified vertex */
    public V getVertex(int index) {
        return vertices.get(index);
    }
@Override /** Return the index for the specified vertex object */

getIndex

public int getIndex(V v) {
    return vertices.indexOf(v);
}

@Override /** Return the neighbors of the specified vertex */

getNeighbors

public List<Integer> getNeighbors(int index) {
    List<Integer> result = new ArrayList<>();
    for (Edge e: neighbors.get(index))
        result.add(e.v);
    return result;
}

@Override /** Return the degree for a specified vertex */

getDegree

public int getDegree(int v) {
    return neighbors.get(v).size();
}

@Override /** Print the edges */

printEdges

public void printEdges() {
    for (int u = 0; u < neighbors.size(); u++) {
        System.out.print(getVertex(u) + " (" + u + "); ");
        for (Edge e: neighbors.get(u))
            System.out.print("(" + getVertex(e.u) + ", " +
                getVertex(e.v) + ") ");
        System.out.println();
    }
}

@Override /** Clear the graph */

clear

public void clear() {
    vertices.clear();
    neighbors.clear();
}

@Override /** Add a vertex to the graph */

addVertex

public boolean addVertex(V vertex) {
    if (!vertices.contains(vertex)) {
        vertices.add(vertex);
        neighbors.add(new ArrayList<Edge>());
        return true;
    } else {
        return false;
    }
}

/** Add an edge to the graph */

addEdge

protected boolean addEdge(Edge e) {
    if (e.u < 0 || e.u > getSize() - 1)
        throw new IllegalArgumentException("No such index: " + e.u);
    if (e.v < 0 || e.v > getSize() - 1)
        throw new IllegalArgumentException("No such index: " + e.v);
    if (!neighbors.get(e.u).contains(e)) {
        neighbors.get(e.u).add(e);
return true;
}
else {
    return false;
}

@Override /** Add an edge to the graph */
public boolean addEdge(int u, int v) {
    return addEdge(new Edge(u, v));
}

/** Edge inner class inside the AbstractGraph class */
public static class Edge {
    public int u; // Starting vertex of the edge
    public int v; // Ending vertex of the edge

    /** Construct an edge for (u, v) */
    public Edge(int u, int v) {
        this.u = u;
        this.v = v;
    }

    public boolean equals(Object o) {
        return u == ((Edge)o).u && v == ((Edge)o).v;
    }
}

@Override /** Obtain a DFS tree starting from vertex v */
/** To be discussed in Section 28.7 */
public Tree dfs(int v) {
    List<Integer> searchOrder = new ArrayList<>();
    int[] parent = new int[vertices.size()];
    for (int i = 0; i < parent.length; i++)
        parent[i] = -1; // Initialize parent[i] to -1

    // Mark visited vertices
    boolean[] isVisited = new boolean[vertices.size()];

    // Recursively search
    dfs(v, parent, searchOrder, isVisited);

    // Return a search tree
    return new Tree(v, parent, searchOrder);
}

/** Recursive method for DFS search */
private void dfs(int u, int[] parent, List<Integer> searchOrder, boolean[] isVisited) {
    // Store the visited vertex
    searchOrder.add(u);
    isVisited[u] = true; // Vertex v visited

    for (Edge e : neighbors.get(u)) {
        if (!isVisited[e.v]) {
            parent[e.v] = u; // The parent of vertex e.v is u
            dfs(e.v, parent, searchOrder, isVisited); // Recursive search
        }
    }
}
public Tree bfs(int v) {
    List<Integer> searchOrder = new ArrayList<>();
    int[] parent = new int[vertices.size()];
    for (int i = 0; i < parent.length; i++)
        parent[i] = -1; // Initialize parent[i] to -1
    java.util.LinkedList<Integer> queue =
        new java.util.LinkedList<>(); // list used as a queue
    boolean[] isVisited = new boolean[vertices.size()];
    queue.offer(v); // Enqueue v
    isVisited[v] = true; // Mark it visited
    while (!queue.isEmpty()) {
        int u = queue.poll(); // Dequeue to u
        searchOrder.add(u); // u searched
        for (Edge e: neighbors.get(u)) {
            if (!isVisited[e.v]) {
                queue.offer(e.v); // Enqueue w
                parent[e.v] = u; // The parent of w is u
                isVisited[e.v] = true; // Mark it visited
            }
        }
    }
    return new Tree(v, parent, searchOrder);
}

/** Tree inner class inside the AbstractGraph class */
/** To be discussed in Section 28.6 */
public class Tree {
    private int root; // The root of the tree
    private int[] parent; // Store the parent of each vertex
    private List<Integer> searchOrder; // Store the search order
    /** Construct a tree with root, parent, and searchOrder */
    public Tree(int root, int[] parent, List<Integer> searchOrder) {
        this.root = root;
        this.parent = parent;
        this.searchOrder = searchOrder;
    }
    /** Return the root of the tree */
    public int getRoot() {
        return root;
    }
    /** Return the parent of vertex v */
    public int getParent(int v) {
        return parent[v];
    }
    /** Return an array representing search order */
    public List<Integer> getSearchOrder() {
        return searchOrder;
    }
    /** Return number of vertices found */
    public int getNumberOfVerticesFound() {
return searchOrder.size();

/** Return the path of vertices from a vertex to the root */
public List<V> getPath(int index) {
    ArrayList<V> path = new ArrayList<>();
    do {
        path.add(vertices.get(index));
        index = parent[index];
    } while (index != -1);
    return path;
}

/** Print a path from the root to vertex v */
public void printPath(int index) {
    List<V> path = getPath(index);
    System.out.print("A path from " + vertices.get(root) + " to " +
        vertices.get(index) + ": ");
    for (int i = path.size() - 1; i >= 0; i--)
        System.out.print(path.get(i) + " ");
}

/** Print the whole tree */
public void printTree() {
    System.out.println("Root is: " + vertices.get(root));
    System.out.print("Edges: ");
    for (int i = 0; i < parent.length; i++) {
        if (parent[i] != -1) {
            // Display an edge
            System.out.print("(" + vertices.get(parent[i]) + ", " +
                vertices.get(i) + ") ");
        }
    }
    System.out.println();
}

Listing 28.4 UnweightedGraph.java

import java.util.*;

public class UnweightedGraph<V> extends AbstractGraph<V> {

    /** Construct an empty graph */
    public UnweightedGraph() {
    }

    /** Construct a graph from vertices and edges stored in arrays */
    public UnweightedGraph(V[] vertices, int[][] edges) {
        super(vertices, edges);
    }

    /** Construct a graph from vertices and edges stored in List */
    public UnweightedGraph(List<V> vertices, List<Edge> edges) {
        super(vertices, edges);
    }

    /** Construct a graph for integer vertices 0, 1, 2 and edge list */
    }
public UnweightedGraph(List<Edge> edges, int numberOfVertices) {
    super(edges, numberOfVertices);
}

/** Construct a graph from integer vertices 0, 1, and edge array */
public UnweightedGraph(int[][] edges, int numberOfVertices) {
    super(edges, numberOfVertices);
}
}

The code in the Graph interface in Listing 28.2 and the UnweightedGraph class in Listing 28.4 are straightforward. Let us digest the code in the AbstractGraph class in Listing 28.3.

The AbstractGraph class defines the data field vertices (line 4) to store vertices and neighbors (line 5) to store edges in adjacency lists. neighbors.get(i) stores all edges adjacent to vertex i. Four overloaded constructors are defined in lines 9–42 to create a default graph, or a graph from arrays or lists of edges and vertices. The createAdjacencyLists(int[][] edges, int numberOfVertices) method creates adjacency lists from edges in an array (lines 45–50). The createAdjacencyLists(List<Edge> edges, int numberOfVertices) method creates adjacency lists from edges in a list (lines 53–58).

The getNeighbors(u) method (lines 81–87) returns a list of vertices adjacent to vertex u. The clear() method (lines 106–110) removes all vertices and edges from the graph. The addVertex(u) method (lines 112–122) adds a new vertex to vertices and returns true. It returns false if the vertex is already in the graph (line 120).

The addEdge(e) method (lines 124–139) adds a new edge the adjacency edge list and returns true. It returns false if the edge is already in the graph. This method may throw IllegalArgumentException if the edge is invalid (lines 126–130).

The printEdges() method (lines 95–104) displays all vertices and edges adjacent to each vertex.

The code in lines 164–293 gives the methods for finding a depth-first search tree and a breadth-first search tree, which will be introduced in Sections 28.7 and 28.9, respectively.

28.7 Describe the relationships among Graph, AbstractGraph, and UnweightedGraph.
28.8 For the code in Listing 28.1, TestGraph.java, what is graph1.getIndex("Seattle")? What is graph1.getDegree(5)? What is graph1.getVertex(4)?

28.5 Graph Visualization

To display a graph visually, each vertex must be assigned a location.

The preceding section introduced how to model a graph using the Graph interface, AbstractGraph class, and UnweightedGraph class. This section discusses how to display graphs graphically. In order to display a graph, you need to know where each vertex is displayed and the name of each vertex. To ensure a graph can be displayed, we define an interface named Displayable that has the methods for obtaining the x- and y-coordinates and their names, and make vertices instances of Displayable, in Listing 28.5.

Listing 28.5 Displayable.java

```java
public interface Displayable {
    public int getX(); // Get x-coordinate of the vertex
    public int getY(); // Get y-coordinate of the vertex
    public String getName(); // Get display name of the vertex
}
```

A graph with Displayable vertices can now be displayed on a pane named GraphView, as shown in Listing 28.6.
To display a graph on a pane, simply create an instance of `GraphView` by passing the graph as an argument in the constructor (line 9). The class for the graph’s vertex must implement the `Displayable` interface in order to display the vertices (lines 13–22). For each vertex index $i$, invoking `graph.getNeighbors(i)` returns its adjacency list (line 26). From this list, you can find all vertices that are adjacent to $i$ and draw a line to connect $i$ with its adjacent vertex (lines 27–34).

Listing 28.7 gives an example of displaying the graph in Figure 28.1, as shown in Figure 28.10.

**LISTING 28.7 DisplayUSMap.java**

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.stage.Stage;

public class DisplayUSMap extends Application {
    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        City[] vertices = {new City("Seattle", 75, 50),
```
new City("San Francisco", 50, 210),
new City("Los Angeles", 75, 275), new City("Denver", 275, 175),
new City("Kansas City", 400, 245),
new City("Chicago", 450, 100), new City("Boston", 700, 80),
new City("New York", 675, 120), new City("Atlanta", 575, 295),
new City("Miami", 600, 400), new City("Dallas", 408, 325),
new City("Houston", 450, 360 });

int[][] edges = {
    {0, 1}, {0, 3}, {0, 5}, {1, 0}, {1, 2}, {1, 3},
    {2, 1}, {2, 3}, {2, 4}, {2, 10},
    {3, 0}, {3, 1}, {3, 2}, {3, 4}, {3, 5},
    {4, 2}, {4, 3}, {4, 5}, {4, 7}, {4, 8}, {4, 10},
    {5, 0}, {5, 3}, {5, 4}, {5, 6}, {5, 7},
    {6, 5}, {6, 7}, {7, 4}, {7, 5}, {7, 6}, {7, 8},
    {8, 4}, {8, 7}, {8, 9}, {8, 10}, {8, 11},
    {9, 8}, {9, 11}, {10, 2}, {10, 4}, {10, 8}, {10, 11},
    {11, 8}, {11, 9}, {11, 10}};

Graph<City> graph = new UnweightedGraph<>(vertices, edges);

// Create a scene and place it in the stage
Scene scene = new Scene(new GraphView(graph), 750, 450);
primaryStage.setTitle("DisplayUSMap"); // Set the stage title
primaryStage.setScene(scene); // Place the scene in the stage
primaryStage.show(); // Display the stage

static class City implements Displayable {
    private int x, y;
    private String name;

    City(String name, int x, int y) {
        this.name = name;
        this.x = x;
        this.y = y;
    }

    @Override
    public int getX() {
        return x;
    }

    @Override
    public int getY() {
        return y;
    }

    @Override
    public String getName() {
        return name;
    }
}

The class City is defined to model the vertices with their coordinates and names (lines 39–63). The program creates a graph with the vertices of the City type (line 30). Since City implements Displayable, a GraphView object created for the graph displays the graph in the pane (line 33).

As an exercise to get acquainted with the graph classes and interfaces, add a city (e.g., Savannah) with appropriate edges into the graph.
28.6 Graph Traversals

Depth-first and breadth-first are two common ways to traverse a graph.

Graph traversal is the process of visiting each vertex in the graph exactly once. There are two popular ways to traverse a graph: depth-first traversal (or depth-first search) and breadth-first traversal (or breadth-first search). Both traversals result in a spanning tree, which can be modeled using a class, as shown in Figure 28.11. Note that Tree is an inner class defined in the AbstractGraph class. AbstractGraph<V>.Tree is different from the Tree interface defined in Section 25.2.5. AbstractGraph.Tree is a specialized class designed for describing the parent–child relationship of the nodes, whereas the Tree interface defines common operations such as searching, inserting, and deleting in a tree. Since there is no need to perform these operations for a spanning tree, AbstractGraph<V>.Tree is not defined as a subtype of Tree.

The Tree class is defined as an inner class in the AbstractGraph class in lines 226–293 in Listing 28.3. The constructor creates a tree with the root, edges, and a search order.

The Tree class defines seven methods. The getRoot() method returns the root of the tree. You can get the order of the vertices searched by invoking the getSearchOrder() method. You can invoke getParent(v) to find the parent of vertex v in the search. Invoking getNumberOfVerticesFound() returns the number of vertices searched. The method getPath(index) returns a list of vertices from the specified vertex index to the root. Invoking printPath(v) displays a path from the root to v. You can display all edges in the tree using the printTree() method.
Section 28.7 and 28.9 will introduce depth-first search and breadth-first search, respectively. Both searches will result in an instance of the `Tree` class.

28.11 Does `AbstractGraph<V>.Tree` implement the `Tree` interface defined in Listing 25.3 Tree.java?

28.12 What method do you use to find the parent of a vertex in the tree?

28.7 Depth-First Search (DFS)

The depth-first search of a graph starts from a vertex in the graph and visits all vertices in the graph as far as possible before backtracking.

The depth-first search of a graph is like the depth-first search of a tree discussed in Section 25.2.4, Tree Traversal. In the case of a tree, the search starts from the root. In a graph, the search can start from any vertex.

A depth-first search of a tree first visits the root, then recursively visits the subtrees of the root. Similarly, the depth-first search of a graph first visits a vertex, then it recursively visits all the vertices adjacent to that vertex. The difference is that the graph may contain cycles, which could lead to an infinite recursion. To avoid this problem, you need to track the vertices that have already been visited.

The search is called depth-first because it searches “deeper” in the graph as much as possible. The search starts from some vertex \( v \). After visiting \( v \), it visits an unvisited neighbor of \( v \). If \( v \) has no unvisited neighbor, the search backtracks to the vertex from which it reached \( v \). We assume that the graph is connected and the search starting from any vertex can reach all the vertices. If this is not the case, see Programming Exercise 28.4 for finding connected components in a graph.

28.7.1 Depth-First Search Algorithm

The algorithm for the depth-first search is described in Listing 28.8.

**Listing 28.8  Depth-First Search Algorithm**

Input: \( G = (V, E) \) and a starting vertex \( v \)
Output: a DFS tree rooted at \( v \)

1. Tree dfs(vertex \( v \)) {
   2. visit \( v \);

for each neighbor w of v
if (w has not been visited) {
    set v as the parent for w in the tree;
    dfs(w);
}

You can use an array named isVisited to denote whether a vertex has been visited. Initially, isVisited[i] is false for each vertex i. Once a vertex, say v, is visited, isVisited[v] is set to true.

Consider the graph in Figure 28.12a. Suppose we start the depth-first search from vertex 0. First visit 0, then any of its neighbors, say 1. Now 1 is visited, as shown in Figure 28.12b. Vertex 1 has three neighbors—0, 2, and 4. Since 0 has already been visited, you will visit either 2 or 4. Let us pick 2. Now 2 is visited, as shown in Figure 28.12c. Vertex 2 has three neighbors: 0, 1, and 3. Since 0 and 1 have already been visited, pick 3. 3 is now visited, as shown in Figure 28.12d. At this point, the vertices have been visited in this order:

0, 1, 2, 3

Since all the neighbors of 3 have been visited, backtrack to 2. Since all the vertices of 2 have been visited, backtrack to 1. 4 is adjacent to 1, but 4 has not been visited. Therefore, visit 4, as shown in Figure 28.12e. Since all the neighbors of 4 have been visited, backtrack to 1. Since all the neighbors of 1 have been visited, backtrack to 0. Since all the neighbors of 0 have been visited, the search ends.

Since each edge and each vertex is visited only once, the time complexity of the dfs method is O(|E| + |V|), where |E| denotes the number of edges and |V| the number of vertices.

![Figure 28.12](image)

**Figure 28.12** Depth-first search visits a node and its neighbors recursively.

### 28.7.2 Implementation of Depth-First Search

The algorithm for DFS in Listing 28.8 uses recursion. It is natural to use recursion to implement it. Alternatively, you can use a stack (see Programming Exercise 28.3).
The `dfs(int v)` method is implemented in lines 164–193 in Listing 28.3. It returns an instance of the `Tree` class with vertex `v` as the root. The method stores the vertices searched in the list `searchOrder` (line 165), the parent of each vertex in the array `parent` (line 166), and uses the `isVisited` array to indicate whether a vertex has been visited (line 171). It invokes the helper method `dfs(v, parent, searchOrder, isVisited)` to perform a depth-first search (line 174).

In the recursive helper method, the search starts from vertex `u`. `u` is added to `searchOrder` in line 184 and is marked as visited (line 185). For each unvisited neighbor of `u`, the method is recursively invoked to perform a depth-first search. When a vertex `e.v` is visited, the parent of `e.v` is stored in `parent[e.v]` (line 189). The method returns when all vertices are visited for a connected graph, or in a connected component.

Listing 28.9 gives a test program that displays a DFS for the graph in Figure 28.1 starting from Chicago. The graphical illustration of the DFS starting from Chicago is shown in Figure 28.13. For an interactive GUI demo of DFS, go to www.cs.armstrong.edu/liang/animation/USMapSearch.html.

```
LISTING 28.9  TestDFS.java
1  public class TestDFS {
2      public static void main(String[] args) {
3          String[] vertices = {
4              "Seattle", "San Francisco", "Los Angeles",
6              "Atlanta", "Miami", "Dallas", "Houston"};
7      int[][] edges = {
8          {0, 1}, {0, 3}, {0, 5},
9          {1, 0}, {1, 2}, {1, 3},
10         {2, 1}, {2, 3}, {2, 4}, {2, 10},
11         {3, 0}, {3, 1}, {3, 2}, {3, 4}, {3, 5},
12         {4, 2}, {4, 3}, {4, 5}, {4, 7}, {4, 8}, {4, 10},
13         {5, 0}, {5, 3}, {5, 4}, {5, 6}, {5, 7},
14         {6, 5}, {6, 7},
15         {7, 4}, {7, 5}, {7, 6}, {7, 8},
16         {8, 4}, {8, 7}, {8, 9}, {8, 10}, {8, 11},
17         {9, 8}, {9, 11},
18         {10, 2}, {10, 4}, {10, 8}, {10, 11},
19         {11, 8}, {11, 9}, {11, 10}
20      };  
21          Graph<String> graph = new UnweightedGraph<>(vertices, edges);
22          AbstractGraph<String>.Tree dfs =
23              graph.dfs(graph.getIndex("Chicago"));
24          java.util.List<Integer> searchOrders = dfs.getSearchOrder();
25          System.out.println(dfs.getNumberVerticesFound() +
26              " vertices are searched in this DFS order:");
27          for (int i = 0; i < searchOrders.size(); i++)
28              System.out.println(graph.getVertex(searchOrders.get(i)) + " ");
29          System.out.println();
30          for (int i = 0; i < searchOrders.size(); i++)
31             if (dfs.getParent(i) != -1)
32                System.out.println("parent of " + graph.getVertex(i) +
33                   " is " + graph.getVertex(dfs.getParent(i)));
34      }
36 }
```
12 vertices are searched in this DFS order:
Chicago Seattle San Francisco Los Angeles Denver
Kansas City New York Boston Atlanta Miami Houston Dallas
parent of Seattle is Chicago
parent of San Francisco is Seattle
parent of Los Angeles is San Francisco
parent of Denver is Los Angeles
parent of Kansas City is Denver
parent of Boston is New York
parent of New York is Kansas City
parent of Atlanta is New York
parent of Miami is Atlanta
parent of Dallas is Houston
parent of Houston is Miami

**Figure 28.13** A DFS search starts from Chicago.

### 28.7.3 Applications of the DFS

The depth-first search can be used to solve many problems, such as the following:

- Detecting whether a graph is connected. Search the graph starting from any vertex.

  If the number of vertices searched is the same as the number of vertices in the graph,
the graph is connected. Otherwise, the graph is not connected. (See Programming Exercise 28.1.)

- Detecting whether there is a path between two vertices (see Programming Exercise 28.5).
- Finding a path between two vertices (see Programming Exercise 28.5).
- Finding all connected components. A connected component is a maximal connected subgraph in which every pair of vertices are connected by a path (see Programming Exercise 28.4).
- Detecting whether there is a cycle in the graph (see Programming Exercise 28.6).
- Finding a cycle in the graph (see Programming Exercise 28.7).
- Finding a Hamiltonian path/cycle. A Hamiltonian path in a graph is a path that visits each vertex in the graph exactly once. A Hamiltonian cycle visits each vertex in the graph exactly once and returns to the starting vertex (see Programming Exercise 28.17).

The first six problems can be easily solved using the dfs method in Listing 28.3. To find a Hamiltonian path/cycle, you have to explore all possible DFSs to find the one that leads to the longest path. The Hamiltonian path/cycle has many applications, including for solving the well-known Knight’s Tour problem, which is presented in Supplement VI.E on the Companion Website.

28.13 What is depth-first search?

28.14 Draw a DFS tree for the graph in Figure 28.3b starting from node A.

28.15 Draw a DFS tree for the graph in Figure 28.1 starting from vertex Atlanta.

28.16 What is the return type from invoking dfs(v)?

28.17 The depth-first search algorithm described in Listing 28.8 uses recursion. Alternatively, you can use a stack to implement it, as shown below. Point out the error in this algorithm and give a correct algorithm.

```cpp
// Wrong version
Tree dfs(vertex v) {
    push v into the stack;
    mark v visited;
    while (the stack is not empty) {
        pop a vertex, say u, from the stack
        visit u;
        for each neighbor w of u
            if (w has not been visited)
                push w into the stack;
    }
}
```

28.8 Case Study: The Connected Circles Problem

The connected circles problem is to determine whether all circles in a two-dimensional plane are connected. This problem can be solved using a depth-first traversal.

The DFS algorithm has many applications. This section applies the DFS algorithm to solve the connected circles problem.

In the connected circles problem, you determine whether all the circles in a two-dimensional plane are connected. If all the circles are connected, they are painted as filled circles, as shown in Figure 28.14a. Otherwise, they are not filled, as shown in Figure 28.14b.
We will write a program that lets the user create a circle by clicking a mouse in a blank area that is not currently covered by a circle. As the circles are added, the circles are repainted filled if they are connected or unfilled otherwise.

We will create a graph to model the problem. Each circle is a vertex in the graph. Two circles are connected if they overlap. We apply the DFS in the graph, and if all vertices are found in the depth-first search, the graph is connected.

The program is given in Listing 28.10.

**Listing 28.10 ConnectedCircles.java**

```java
import javafx.application.Application;
import javafx.geometry.Point2D;
import javafx.scene.Node;
import javafx.scene.Scene;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Circle;
import javafx.stage.Stage;

public class ConnectedCircles extends Application {
    @Override
    public void start(Stage primaryStage) {
        Scene scene = new Scene(new CirclePane(), 450, 350);
        primaryStage.setTitle("ConnectedCircles");
        primaryStage.setScene(scene);
        primaryStage.show();
    }

    public class CirclePane extends Pane {
        public CirclePane() {
            setOnMouseClicked(e -> {
                if (!isInsideACircle(new Point2D(e.getX(), e.getY()))) {
                    getChildren().add(new Circle(e.getX(), e.getY(), 20));
                    colorIfConnected();
                }
            });
        }
    }
}
```

*Figure 28.14* You can apply DFS to determine whether the circles are connected.
```java
/** Returns true if the point is inside an existing circle */
private boolean isInsideACircle(Point2D p) {
    for (Node circle : this.getChildren())
        if (circle.contains(p))
            return true;
    return false;
}

/** Color all circles if they are connected */
private void colorIfConnected() {
    if (getChildren().size() == 0)
        return; // No circles in the pane
    java.util.List<AbstractGraph.Edge> edges = new java.util.ArrayList<>();
    for (int i = 0; i < getChildren().size(); i++)
        for (int j = i + 1; j < getChildren().size(); j++)
            if (overlaps((Circle) getChildren().get(i),
                         (Circle) getChildren().get(j)))
                edges.add(new AbstractGraph.Edge(i, j));
                edges.add(new AbstractGraph.Edge(j, i));
    Graph<Node> graph = new UnweightedGraph<>((java.util.List<Node>) getChildren(), edges);
    AbstractGraph<Node>.Tree tree = graph.dfs(0); // a DFS tree
    boolean isAllCirclesConnected = getChildren().size() == tree.getNumberOfVerticesFound();
    for (Node circle : getChildren())
        if (isAllCirclesConnected) // All circles are connected
            ((Circle) circle).setFill(Color.RED);
        else
            ((Circle) circle).setStroke(Color.BLACK);
            ((Circle) circle).setFill(Color.WHITE);
    }

circle contains the point?
create edges
create a graph
get a search tree
connected?
for (Node circle : getChildren())
    if (isAllCirclesConnected) // All circles are connected
        ((Circle) circle).setFill(Color.RED);
    else
        ((Circle) circle).setStroke(Color.BLACK);
        ((Circle) circle).setFill(Color.WHITE);
not connected
two circles overlap?
public static boolean overlaps(Circle circle1, Circle circle2) {
    return new Point2D(circle1.getCenterX(), circle1.getCenterY()).
        distance(circle2.getCenterX(), circle2.getCenterY())
        <= circle1.getRadius() + circle2.getRadius();
}

The JavaFX Circle class contains the data fields x, y, and radius, which specify the circle’s center location and radius. It also defines the contains for testing if a point is in the circle. The overlaps method (lines 76–80) checks whether two circles overlap.

When the user clicks the mouse outside of any existing circle, a new circle is created centered at the mouse point and the circle is added to the pane (line 26).

To detect whether the circles are connected, the program constructs a graph (lines 46–59). The circles are the vertices of the graph. The edges are constructed in lines 49–55. Two circle
vertices are connected if they overlap (line 51). The DFS of the graph results in a tree (line 60). The tree’s `getNumberOfVerticesFound()` returns the number of vertices searched. If it is equal to the number of circles, all circles are connected (lines 61–62).

28.18 How is a graph created for the connected circles problem?
28.19 When you click the mouse inside a circle, does the program create a new circle?
28.20 How does the program know if all circles are connected?

28.9 Breadth-First Search (BFS)

The breadth-first search of a graph visits the vertices level by level. The first level consists of the starting vertex. Each next level consists of the vertices adjacent to the vertices in the preceding level.

The breadth-first traversal of a graph is like the breadth-first traversal of a tree discussed in Section 25.2.4, Tree Traversal. With breadth-first traversal of a tree, the nodes are visited level by level. First the root is visited, then all the children of the root, then the grandchildren of the root, and so on. Similarly, the breadth-first search of a graph first visits a vertex, then all its adjacent vertices, then all the vertices adjacent to those vertices, and so on. To ensure that each vertex is visited only once, it skips a vertex if it has already been visited.

28.9.1 Breadth-First Search Algorithm

The algorithm for the breadth-first search starting from vertex \( v \) in a graph is described in Listing 28.11.

**Listing 28.11 Breadth-First Search Algorithm**

Input: \( G = (V, E) \) and a starting vertex \( v \)
Output: a BFS tree rooted at \( v \)

```
1 Tree bfs(vertex v) {
2    create an empty queue for storing vertices to be visited;
3    add v into the queue;
4    mark v visited;
5
6    while (the queue is not empty) {
7      dequeue a vertex, say u, from the queue;
8      add u into a list of traversed vertices;
9      for each neighbor w of u
10         if w has not been visited {
11            add w into the queue;
12            set u as the parent for w in the tree;
13            mark w visited;
14         }
15    }
16 }
```

Consider the graph in Figure 28.15a. Suppose you start the breadth-first search from vertex 0. First visit 0, then visit all its neighbors, 1, 2, and 3, as shown in Figure 28.15b. Vertex 1 has three neighbors: 0, 2, and 4. Since 0 and 2 have already been visited, you will now visit just 4, as shown in Figure 28.15c. Vertex 2 has three neighbors, 0, 1, and 3, which have all been visited. Vertex 3 has three neighbors, 0, 2, and 4, which have all been visited. Vertex 4 has two neighbors, 1 and 3, which have all been visited. Hence, the search ends.

Since each edge and each vertex is visited only once, the time complexity of the `bfs` method is \( O(|E| + |V|) \), where \( |E| \) denotes the number of edges and \( |V| \) the number of vertices.
28.9.2 Implementation of Breadth-First Search

The `bfs(int v)` method is defined in the `Graph` interface and implemented in the `AbstractGraph` class in Listing 28.3 (lines 197–222). It returns an instance of the `Tree` class with vertex `v` as the root. The method stores the vertices searched in the list `searchOrder` (line 198), the parent of each vertex in the array `parent` (line 199), uses a linked list for a queue (lines 203–204), and uses the `isVisited` array to indicate whether a vertex has been visited (line 207). The search starts from vertex `v`. `v` is added to the queue in line 206 and is marked as visited (line 207). The method now examines each vertex `u` in the queue (line 210) and adds it to `searchOrder` (line 211). The method adds each unvisited neighbor `e.v` of `u` to the queue (line 214), sets its parent to `u` (line 215), and marks it as visited (line 216).

Listing 28.12 gives a test program that displays a BFS for the graph in Figure 28.1 starting from Chicago. The graphical illustration of the BFS starting from Chicago is shown in Figure 28.16. For an interactive GUI demo of BFS, go to www.cs.armstrong.edu/liang/animation/USMapSearch.html.

**LISTING 28.12 TestBFS.java**

```java
public class TestBFS {
    public static void main(String[] args) {
        String[] vertices = {
            "Seattle", "San Francisco", "Los Angeles",
            "Atlanta", "Miami", "Dallas", "Houston"};
        int[][] edges = {
            {0, 1}, {0, 3}, {0, 5},
            {1, 0}, {1, 2}, {1, 3},
            {2, 1}, {2, 3}, {2, 4}, {2, 10},
            {3, 0}, {3, 1}, {3, 2}, {3, 4}, {3, 5},
            {4, 2}, {4, 3}, {4, 5}, {4, 7}, {4, 8}, {4, 10},
            {5, 0}, {5, 3}, {5, 4}, {5, 6}, {5, 7},
            {6, 5}, {6, 7},
            {7, 4}, {7, 5}, {7, 6}, {7, 8},
            {8, 4}, {8, 7}, {8, 9}, {8, 10}, {8, 11},
            {9, 8}, {9, 11},
            {10, 2}, {10, 4}, {10, 8}, {10, 11},
            {11, 8}, {11, 9}, {11, 10};
        }
        Graph<String> graph = new UnweightedGraph<>(vertices, edges);
        AbstractGraph<String>.Tree bfs =
            graph.bfs(graph.getIndex("Chicago"));
        java.util.List<Integer> searchOrders = bfs.getSearchOrder();
    }
}
```

**FIGURE 28.15**  Breadth-first search visits a node, then its neighbors, then its neighbors’ neighbors, and so on.
```
28.9 Breadth-First Search (BFS)

12 vertices are searched in this order:
   Chicago Seattle Denver Kansas City Boston New York
   San Francisco Los Angeles Atlanta Dallas Miami Houston
   parent of Seattle is Chicago
   parent of San Francisco is Seattle
   parent of Los Angeles is Denver
   parent of Denver is Chicago
   parent of Kansas City is Chicago
   parent of Boston is Chicago
   parent of New York is Chicago
   parent of Atlanta is Kansas City
   parent of Miami is Atlanta
   parent of Dallas is Kansas City
   parent of Houston is Atlanta
```

28.9.3 Applications of the BFS

Many of the problems solved by the DFS can also be solved using the BFS. Specifically, the BFS can be used to solve the following problems:

- Detecting whether a graph is connected. A graph is connected if there is a path between any two vertices in the graph.
- Detecting whether there is a path between two vertices.
- Finding a shortest path between two vertices. You can prove that the path between the root and any node in the BFS tree is a shortest path between the root and the node. (See Check Point Question 28.25.)
- Finding all connected components. A connected component is a maximal connected subgraph in which every pair of vertices are connected by a path.
- Detecting whether there is a cycle in the graph (see Programming Exercise 28.6).
- Finding a cycle in the graph (see Programming Exercise 28.7).
- Testing whether a graph is bipartite. (A graph is bipartite if the vertices of the graph can be divided into two disjoint sets such that no edges exist between vertices in the same set.) (See Programming Exercise 28.8.)

28.21 What is the return type from invoking `bfs(v)`?

28.22 What is breadth-first search?

28.23 Draw a BFS tree for the graph in Figure 28.3b starting from node `A`.

28.24 Draw a BFS tree for the graph in Figure 28.1 starting from vertex `Atlanta`.

28.25 Prove that the path between the root and any node in the BFS tree is a shortest path between the root and the node.
28.10 Case Study: The Nine Tails Problem

The nine tails problem can be reduced to the shortest path problem.

The nine tails problem is as follows. Nine coins are placed in a three-by-three matrix with some face up and some face down. A legal move is to take a coin that is face up and reverse it, together with the coins adjacent to it (this does not include coins that are diagonally adjacent). Your task is to find the minimum number of moves that lead to all coins being face down. For example, start with the nine coins as shown in Figure 28.17a. After you flip the second coin in the last row, the nine coins are now as shown in Figure 28.17b. After you flip the second coin in the first row, the nine coins are all face down, as shown in Figure 28.17c.

We will write a program that prompts the user to enter an initial state of the nine coins and displays the solution, as shown in the following sample run.
Each state of the nine coins represents a node in the graph. For example, the three states in Figure 28.17 correspond to three nodes in the graph. For convenience, we use a $3 \times 3$ matrix to represent all nodes and use 0 for heads and 1 for tails. Since there are nine cells and each cell is either 0 or 1, there are a total of $2^9$ (512) nodes, labeled 0, 1, \ldots, and 511, as shown in Figure 28.18.

<table>
<thead>
<tr>
<th>0</th>
<th>0</th>
<th>0</th>
<th>0</th>
<th>0</th>
<th>0</th>
<th>0</th>
<th>0</th>
<th>1</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
<td>0</td>
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<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

**Figure 28.18** There are total of 512 nodes labeled in this order: 0, 1, 2, \ldots, 511.

We assign an edge from node $v$ to $u$ if there is a legal move from $u$ to $v$. Figure 28.19 shows a partial graph. Note there is an edge from 511 to 47, since you can flip a cell in node 47 to become node 511.

The last node in Figure 28.18 represents the state of nine face-down coins. For convenience, we call this last node the target node. Thus, the target node is labeled 511. Suppose the initial state of the nine tails problem corresponds to the node $s$. The problem is reduced to finding a shortest path from node $s$ to the target node, which is equivalent to finding a shortest path from node $s$ to the target node in a BFS tree rooted at the target node.

Now the task is to build a graph that consists of 512 nodes labeled 0, 1, 2, \ldots, 511, and edges among the nodes. Once the graph is created, obtain a BFS tree rooted at node 511. From the BFS tree, you can find a shortest path from the root to any vertex. We will create a class named NineTailModel, which contains the method to get a shortest path from the target node to any other node. The class UML diagram is shown in Figure 28.20.

Visually, a node is represented in a $3 \times 3$ matrix with the letters H and T. In our program, we use a single-dimensional array of nine characters to represent a node. For example, the node for vertex 1 in Figure 28.18 is represented as {'H', 'H', 'H', 'H', 'H', 'H', 'H', 'T'} in the array.

The getEdges() method returns a list of Edge objects.

The getNode(index) method returns the node for the specified index. For example, getNode(0) returns the node that contains nine Hs. getNode(511) returns the node that contains nine Ts. The getIndex(node) method returns the index of the node.

Note that the data field tree is defined as protected so that it can be accessed from the WeightedNineTail subclass in the next chapter.

The getFlippedNode(char[] node, int position) method flips the node at the specified position and its adjacent positions. This method returns the index of the new node.
The position is a value from 0 to 8, which points to a coin in the node, as shown in the following figure.

For example, for node 56 in Figure 28.19, flip it at position 0, and you will get node 51. If you flip node 56 at position 1, you will get node 47.

The `flipACell(char[] node, int row, int column)` method flips a node at the specified row and column. For example, if you flip node 56 at row 0 and column 0, the new node is 408. If you flip node 56 at row 2 and column 0, the new node is 30.

![Diagram showing the nine tails problem and the flips at different positions](image_url)

**Figure 28.19** If node \( u \) becomes node \( v \) after cells are flipped, assign an edge from \( v \) to \( u \).

**Figure 28.20** The `NineTailModel` class models the nine tails problem using a graph.
Listing 28.13 shows the source code for NineTailModel.java.

```
import java.util.*;

public class NineTailModel {
  public final static int NUMBER_OF_NODES = 512;
  protected AbstractGraph<Integer>.Tree tree; // Define a tree

  /** Construct a model */
  public NineTailModel() {
    // Create edges
    List<AbstractGraph.Edge> edges = getEdges();
    // Create a graph
    UnweightedGraph<Integer> graph = new UnweightedGraph<>(
        edges, NUMBER_OF_NODES);
    // Obtain a BFS tree rooted at the target node
    tree = graph.bfs(511);
  }

  /** Create all edges for the graph */
  private List<AbstractGraph.Edge> getEdges() {
    List<AbstractGraph.Edge> edges = new ArrayList<>(); // Store edges
    for (int u = 0; u < NUMBER_OF_NODES; u++) {
      for (int k = 0; k < 9; k++) {
        char[] node = getNode(u); // Get the node for vertex u
        if (node[k] == 'H') {
          int v = getFlippedNode(node, k);
          // Add edge (v, u) for a legal move from node u to node v
          edges.add(new AbstractGraph.Edge(v, u));
        }
      }
    }
    return edges;
  }

  public static int getFlippedNode(char[] node, int position) {
    int row = position / 3;
    int column = position % 3;
    flipACell(node, row, column);
    flipACell(node, row - 1, column);
    flipACell(node, row + 1, column);
    flipACell(node, row, column - 1);
    flipACell(node, row, column + 1);
    return getIndex(node);
  }

  public static void flipACell(char[] node, int row, int column) {
    if (row >= 0 && row <= 2 && column >= 0 && column <= 2) {
      // Within the boundary
      if (node[row * 3 + column] == 'H')
        node[row * 3 + column] = 'T'; // Flip from H to T
    }
  }
}
```
The constructor (lines 8–18) creates a graph with 512 nodes, and each edge corresponds to the move from one node to the other (line 10). From the graph, a BFS tree rooted at the target node is obtained (line 17).

To create edges, the `getEdges` method (lines 21–37) checks each node `u` to see if it can be flipped to another node `v`. If so, add `(v, u)` to the `Edge` list (line 31). The `getFlippedNode(node, position)` method finds a flipped node by flipping an `H` cell and its neighbors in a node (lines 43–47). The `flipACell(node, row, column)` method actually flips an `H` cell and its neighbors in a node (lines 52–60).

The `getIndex(node)` method is implemented in the same way as converting a binary number to a decimal number (lines 62–72). The `getNode(index)` method returns a node consisting of the letters `H` and `T` (lines 74–87).
The `getShortestPath(nodeIndex)` method invokes the `getPath(nodeIndex)` method to get a vertices in a shortest path from the specified node to the target node (lines 89–91).

The `printNode(node)` method displays a node on the console (lines 93–101).

Listing 28.14 gives a program that prompts the user to enter an initial node and displays the steps to reach the target node.

**LISTING 28.14 NineTail.java**

```java
import java.util.Scanner;

public class NineTail {
    public static void main(String[] args) {
        // Prompt the user to enter nine coins' Hs and Ts
        System.out.print("Enter the initial nine coins Hs and Ts: ");
        Scanner input = new Scanner(System.in);
        String s = input.nextLine();
        char[] initialNode = s.toCharArray();

        NineTailModel model = new NineTailModel();
        java.util.List<Integer> path =
                model.getShortestPath(NineTailModel.getIndex(initialNode));

        System.out.println("The steps to flip the coins are ");
        for (int i = 0; i < path.size(); i++)
            NineTailModel.printNode(NineTailModel.getNode(path.get(i).intValue()));
    }
}
```

The program prompts the user to enter an initial node with nine letters with a combination of Hs and Ts as a string in line 8, obtains an array of characters from the string (line 9), creates a graph model to get a BFS tree (line 11), obtains a shortest path from the initial node to the target node (lines 12–13), and displays the nodes in the path (lines 16–18).

**28.26** How are the nodes created for the graph in `NineTailModel`?

**28.27** How are the edges created for the graph in `NineTailModel`?

**28.28** What is returned after invoking `getIndex("HTHTTHHH".toCharArray())` in Listing 28.13? What is returned after invoking `getNode(46)` in Listing 28.13?

**28.29** If lines 26 and 27 are swapped in Listing 28.13, NineTailModel.java, will the program work? Why?

---

**Key Terms**

- adjacency list 1022
- adjacency matrix 1021
- adjacent vertices 1018
- breadth-first search 1037
- complete graph 1018
- cycle 1018
- degree 1018
- depth-first search 1037
- directed graph 1017
- graph 1016
- incident edges 1018
- parallel edge 1018
- Seven Bridges of Königsberg 1016
- simple graph 1018
- spanning tree 1018
- tree 1018
- undirected graph 1017
- unweighted graph 1018
- weighted graph 1018
CHAPTER SUMMARY

1. A graph is a useful mathematical structure that represents relationships among entities in the real world. You learned how to model graphs using classes and interfaces, how to represent vertices and edges using arrays and linked lists, and how to implement operations for graphs.

2. Graph traversal is the process of visiting each vertex in the graph exactly once. You learned two popular ways for traversing a graph: the depth-first search (DFS) and breadth-first search (BFS).

3. DFS and BFS can be used to solve many problems such as detecting whether a graph is connected, detecting whether there is a cycle in the graph, and finding a shortest path between two vertices.

Quiz

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

PROGRAMMING EXERCISES

Sections 28.6–28.10

*28.1 (Test whether a graph is connected) Write a program that reads a graph from a file and determines whether the graph is connected. The first line in the file contains a number that indicates the number of vertices (n). The vertices are labeled as 0, 1, …, n-1. Each subsequent line, with the format u v1 v2 …, describes edges (u, v1), (u, v2), and so on. Figure 28.21 gives the examples of two files for their corresponding graphs.

Your program should prompt the user to enter the name of the file, then it should read data from the file, create an instance g of UnweightedGraph, invoke g.printEdges() to display all edges, and invoke dfs() to obtain an instance tree of AbstractGraph.Tree. If tree.getNumberofVerticesFound() is the same as the number of vertices in the graph, the graph is connected. Here is a sample run of the program:
Enter a file name: c:\exercise\GraphSample1.txt
The number of vertices is 6
Vertex 0: (0, 1) (0, 2)
Vertex 1: (1, 0) (1, 3)
Vertex 2: (2, 0) (2, 3) (2, 4)
Vertex 3: (3, 1) (3, 2) (3, 4) (3, 5)
Vertex 4: (4, 2) (4, 3) (4, 5)
Vertex 5: (5, 3) (5, 4)
The graph is connected

(Hint: Use new UnweightedGraph(list, numberOfVertices) to create a graph, where list contains a list of AbstractGraph.Edge objects. Use new AbstractGraph.Edge(u, v) to create an edge. Read the first line to get the number of vertices. Read each subsequent line into a string s and use s.split("[\s+]") to extract the vertices from the string and create edges from the vertices.)

*28.2 (Create a file for a graph) Modify Listing 28.1, TestGraph.java, to create a file representing graph1. The file format is described in Programming Exercise 28.1. Create the file from the array defined in lines 8–21 in Listing 28.1. The number of vertices for the graph is 12, which will be stored in the first line of the file. The contents of the file should be as follows:

12
0 1 3 5
1 0 2 3
2 1 3 4 10
3 0 2 4 5
4 2 3 5 7 8 10
5 0 3 4 6 7
6 5 7
7 4 5 6 8
8 4 7 9 10 11
9 8 11
10 2 4 8 11
11 8 9 10

*28.3 (Implement DFS using a stack) The depth-first search algorithm described in Listing 28.8 uses recursion. Design a new algorithm without using recursion. Describe it using pseudocode. Implement it by defining a new class named UnweightedGraphWithNonrecursiveDFS that extends UnweightedGraph and overriding the dfs method.

*28.4 (Find connected components) Create a new class named MyGraph as a subclass of UnweightedGraph that contains a method for finding all connected components in a graph with the following header:

    public List<List<Integer>> getConnectedComponents();

The method returns a List<List<Integer>>. Each element in the list is another list that contains all the vertices in a connected component. For example, for the graph in Figure 28.21b, getConnectedComponents() returns [[0, 1, 2, 3], [4, 5]].
*28.5 (Find paths) Add a new method in AbstractGraph to find a path between two vertices with the following header:

```java
public List<Integer> getPath(int u, int v);
```

The method returns a `List<Integer>` that contains all the vertices in a path from `u` to `v` in this order. Using the BFS approach, you can obtain a shortest path from `u` to `v`. If there isn't a path from `u` to `v`, the method returns `null`.

*28.6 (Detect cycles) Add a new method in AbstractGraph to determine whether there is a cycle in the graph with the following header:

```java
public boolean isCyclic();
```

*28.7 (Find a cycle) Add a new method in AbstractGraph to find a cycle in the graph with the following header:

```java
public List<Integer> getACycle(int u);
```

The method returns a `List` that contains all the vertices in a cycle starting from `u`. If the graph doesn't have any cycles, the method returns `null`.

**28.8 (Test bipartite) Recall that a graph is bipartite if its vertices can be divided into two disjoint sets such that no edges exist between vertices in the same set. Add a new method in AbstractGraph with the following header to detect whether the graph is bipartite:

```java
public boolean isBipartite();
```

**28.9 (Get bipartite sets) Add a new method in AbstractGraph with the following header to return two bipartite sets if the graph is bipartite:

```java
public List<List<Integer>> getBipartite();
```

The method returns a `List` that contains two sublists, each of which contains a set of vertices. If the graph is not bipartite, the method returns `null`.

28.10 (Find a shortest path) Write a program that reads a connected graph from a file. The graph is stored in a file using the same format specified in Programming Exercise 28.1. Your program should prompt the user to enter the name of the file, then two vertices, and should display a shortest path between the two vertices. For example, for the graph in Figure 28.21a, a shortest path between 0 and 5 may be displayed as 0 1 3 5.

Here is a sample run of the program:

```
Enter a file name: c:\exercise\GraphSample1.txt
Enter two vertices (integer indexes): 0 5
The number of vertices is 6
Vertex 0: (0, 1) (0, 2)
Vertex 1: (1, 0) (1, 3)
Vertex 2: (2, 0) (2, 3) (2, 4)
Vertex 3: (3, 1) (3, 2) (3, 4) (3, 5)
Vertex 4: (4, 2) (4, 3) (4, 5)
Vertex 5: (5, 3) (5, 4)
The path is 0 1 3 5
```
**28.11** *(Revise Listing 28.14, NineTail.java)* The program in Listing 28.14 lets the user enter an input for the nine tails problem from the console and displays the result on the console. Write a program that lets the user set an initial state of the nine coins (see Figure 28.22a) and click the Solve button to display the solution, as shown in Figure 28.22b. Initially, the user can click the mouse button to flip a coin. Set a red color on the flipped cells.

![Figure 28.22](image)

The program solves the nine tails problem.

**28.12** *(Variation of the nine tails problem)* In the nine tails problem, when you flip a coin, the horizontal and vertical neighboring cells are also flipped. Rewrite the program, assuming that all neighboring cells including the diagonal neighbors are also flipped.

**28.13** *(4 × 4 16 tails problem)* Listing 28.14, NineTail.java, presents a solution for the nine tails problem. Revise this program for the 4 × 4 16 tails problem. Note that it is possible that a solution may not exist for a starting pattern. If so, report that no solution exists.

**28.14** *(4 × 4 16 tails analysis)* The nine tails problem in the text uses a 3 × 3 matrix. Assume that you have 16 coins placed in a 4 × 4 matrix. Write a program to find out the number of the starting patterns that don’t have a solution.

**28.15** *(4 × 4 16 tails GUI)* Rewrite Programming Exercise 28.14 to enable the user to set an initial pattern of the 4 × 4 16 tails problem (see Figure 28.23a). The user can click the Solve button to display the solution, as shown in Figure 28.23b. Initially, the user can click the mouse button to flip a coin. If a solution does not exist, display a message to report it.

![Figure 28.23](image)

The problem solves the 16 tails problem.
**28.16** (Induced subgraph) Given an undirected graph \( G = (V, E) \) and an integer \( k \), find an induced subgraph \( H \) of \( G \) of maximum size such that all vertices of \( H \) have a degree \( \geq k \), or conclude that no such induced subgraph exists. Implement the method with the following header:

```java
public static Graph maxInducedSubgraph(Graph g, int k)
```

The method returns `null` if such a subgraph does not exist.

*Hint:* An intuitive approach is to remove vertices whose degree is less than \( k \). As vertices are removed with their adjacent edges, the degrees of other vertices may be reduced. Continue the process until no vertices can be removed, or all the vertices are removed.

**28.17** (Hamiltonian cycle) The Hamiltonian path algorithm is implemented in Supplement VI.E. Add the following `getHamiltonianCycle` method in the `Graph` interface and implement it in the `AbstractGraph` class:

```java
/** Return a Hamiltonian cycle
 * Return null if the graph doesn't contain a Hamiltonian cycle */
public List<Integer> getHamiltonianCycle()
```

**28.18** (Knight’s Tour cycle) Rewrite KnightTourApp.java in the case study in Supplement VI.E to find a knight’s tour that visits each square in a chessboard and returns to the starting square. Reduce the Knight’s Tour cycle problem to the problem of finding a Hamiltonian cycle.

**28.19** (Display a DFS/BFS tree in a graph) Modify `GraphView` in Listing 28.6 to add a new data field `tree` with a set method. The edges in the tree are displayed in red. Write a program that displays the graph in Figure 28.1 and the DFS/BFS tree starting from a specified city, as shown in Figures 28.13 and 28.16. If a city not in the map is entered, the program displays an error message in the label.

**28.20** (Display a graph) Write a program that reads a graph from a file and displays it. The first line in the file contains a number that indicates the number of vertices \( n \). The vertices are labeled 0, 1, …, \( n-1 \). Each subsequent line, with the format \( u \ x \ y \ v1 \ v2 \ldots \), describes the position of \( u \) at \((x, y)\) and edges \((u,v1), (u,v2), \ldots\). Figure 28.24 gives an example of the file for their corresponding graph. Your program prompts the user to enter the name of the file, reads data from the file, and displays the graph on a pane using `GraphView`, as shown in Figure 28.24b.

**Figure 28.24** The program reads the information about the graph and displays it visually.
28.21 (Display sets of connected circles) Modify Listing 28.10, ConnectedCircles.java, to display sets of connected circles in different colors. That is, if two circles are connected, they are displayed using the same color; otherwise, they are not in same color, as shown in Figure 28.25. (Hint: See Programming Exercise 28.4.)

28.22 (Move a circle) Modify Listing 28.10, ConnectedCircles.java, to enable the user to drag and move a circle.

28.23 (Connected rectangles) Listing 28.10, ConnectedCircles.java, allows the user to create circles and determine whether they are connected. Rewrite the program for rectangles. The program lets the user create a rectangle by clicking a mouse in a blank area that is not currently covered by a rectangle. As the rectangles are added, the rectangles are repainted as filled if they are connected or unfilled otherwise, as shown in Figure 28.25b–c.

28.24 (Remove a circle) Modify Listing 28.10, ConnectedCircles.java, to enable the user to remove a circle when the mouse is clicked inside the circle.
WEIGHTED GRAPHS
AND APPLICATIONS

Objectives

- To represent weighted edges using adjacency matrices and adjacency lists (§29.2).
- To model weighted graphs using the WeightedGraph class that extends the AbstractGraph class (§29.3).
- To design and implement the algorithm for finding a minimum spanning tree (§29.4).
- To define the MST class that extends the Tree class (§29.4).
- To design and implement the algorithm for finding single-source shortest paths (§29.5).
- To define the ShortestPathTree class that extends the Tree class (§29.5).
- To solve the weighted nine tails problem using the shortest-path algorithm (§29.6).
29.1 Introduction

A graph is a weighted graph if each edge is assigned a weight. Weighted graphs have many practical applications.

Figure 28.1 assumes that the graph represents the number of flights among cities. You can apply the BFS to find the fewest number of flights between two cities. Assume that the edges represent the driving distances among the cities as shown in Figure 29.1. How do you find the minimal total distances for connecting all cities? How do you find the shortest path between two cities? This chapter will address these questions. The former is known as the minimum spanning tree (MST) problem and the latter as the shortest path problem.

Figure 29.1 The graph models the distances among the cities.

The preceding chapter introduced the concept of graphs. You learned how to represent edges using edge arrays, edge lists, adjacency matrices, and adjacency lists, and how to model a graph using the Graph interface, the AbstractGraph class, and the UnweightedGraph class. The preceding chapter also introduced two important techniques for traversing graphs: depth-first search and breadth-first search, and applied traversal to solve practical problems. This chapter will introduce weighted graphs. You will learn the algorithm for finding a minimum spanning tree in Section 29.4 and the algorithm for finding shortest paths in Section 29.5.

Pedagogical Note

Before we introduce the algorithms and applications for weighted graphs, it is helpful to get acquainted with weighted graphs using the GLUI interactive tool at www.cs.armstrong.edu/liang/animation/WeightedGraphLearningTool.html, as shown in Figure 29.2. The tool allows you to enter vertices, specify edges and their weights, view the graph, and find an MST and all shortest paths from a single source, as shown in Figure 29.2.
29.2 Representing Weighted Graphs

Weighted edges can be stored in adjacency lists.

There are two types of weighted graphs: vertex weighted and edge weighted. In a vertex-weighted graph, each vertex is assigned a weight. In an edge-weighted graph, each edge is assigned a weight. Of the two types, edge-weighted graphs have more applications. This chapter considers edge-weighted graphs.

Weighted graphs can be represented in the same way as unweighted graphs, except that you have to represent the weights on the edges. As with unweighted graphs, the vertices in weighted graphs can be stored in an array. This section introduces three representations for the edges in weighted graphs.

29.2.1 Representing Weighted Edges: Edge Array

Weighted edges can be represented using a two-dimensional array. For example, you can store all the edges in the graph in Figure 29.3a using the array in Figure 29.3b.

```
Object[][] edges = {
    {new Integer(0), new Integer(1), new SomeTypeForWeight(2)},
    {new Integer(0), new Integer(3), new SomeTypeForWeight(8)},
    ...
};
```
29.2.2 Weighted Adjacency Matrices

Assume that the graph has $n$ vertices. You can use a two-dimensional $n \times n$ matrix, say $weights$, to represent the weights on edges. $weights[i][j]$ represents the weight on edge $(i, j)$. If vertices $i$ and $j$ are not connected, $weights[i][j]$ is null. For example, the weights in the graph in Figure 29.3a can be represented using an adjacency matrix as follows:

```java
Integer[][] adjacencyMatrix = {
    {null, 2, null, 8, null},
    {2, null, 7, 3, null},
    {null, 7, null, 4, 5},
    {8, 3, 4, null, 6},
    {null, null, 5, 6, null}
};
```

![Figure 29.3](image)

Each edge is assigned a weight in an edge-weighted graph.

29.2.3 Adjacency Lists

Another way to represent the edges is to define edges as objects. The `AbstractGraph.Edge` class was defined to represent an unweighted edge in Listing 28.3. For weighted edges, we define the `WeightedEdge` class as shown in Listing 29.1.

### Listing 29.1 WeightedEdge.java

```java
public class WeightedEdge extends AbstractGraph.Edge implements Comparable<WeightedEdge> {
    public double weight; // The weight on edge (u, v)

    public WeightedEdge(int u, int v, double weight) {
        super(u, v);
        this.weight = weight;
    }

    @Override
    public int compareTo(WeightedEdge edge) {
        if (weight > edge.weight) return 1;
        else if (weight == edge.weight) return 0;
        else return -1;
    }
}
```
AbstractGraph.Edge is an inner class defined in the AbstractGraph class. It represents an edge from vertex \( u \) to \( v \). WeightedEdge extends AbstractGraph.Edge with a new property weight.

To create a WeightedEdge object, use \( \text{new WeightedEdge}(i, j, w) \), where \( w \) is the weight on edge \((i, j)\). Often you need to compare the weights of the edges. For this reason, the WeightedEdge class implements the Comparable interface.

For unweighted graphs, we use adjacency lists to represent edges. For weighted graphs, we still use adjacency lists, the adjacency lists for the vertices in the graph in Figure 29.3a can be represented as follows:

\[
\text{List<WeightedEdge>[] list = new java.util.List[5];}
\]

\|
| list[0] | WeightedEdge(0, 1, 2) |
| list[1] | WeightedEdge(1, 0, 2) |
| list[2] | WeightedEdge(2, 3, 4) |
| list[3] | WeightedEdge(3, 1, 3) |
| list[4] | WeightedEdge(4, 2, 5) |
\|

list[i] stores all edges adjacent to vertex \( i \).

For flexibility, we will use an array list rather than a fixed-sized array to represent list as follows:

\[
\text{List<List<WeightedEdge>> list = new java.util.ArrayList<>();}
\]

29.1 For the codetoLowerCase WeightedEdge edge = new WeightedEdge(1, 2, 3.5), what is edge.u, edge.v, and edge.weight?

29.2 What is the output of the following code?

\[
\text{List<WeightedEdge> list = new ArrayList<>();}
\]
\[
\text{list.add(new WeightedEdge(1, 2, 3.5));}
\]
\[
\text{list.add(new WeightedEdge(2, 3, 4.5));}
\]
\[
\text{WeightedEdge e = java.util.Collections.max(list);}
\]
\[
\text{System.out.println(e.u);}
\]
\[
\text{System.out.println(e.v);}
\]
\[
\text{System.out.println(e.weight);}
\]

29.3 The WeightedGraph Class

The WeightedGraph class extends AbstractGraph.

The preceding chapter designed the Graph interface, the AbstractGraph class, and the UnweightedGraph class for modeling graphs. Following this pattern, we design WeightedGraph as a subclass of AbstractGraph, as shown in Figure 29.4.

WeightedGraph simply extends AbstractGraph with five constructors for creating concrete WeightedGraph instances. WeightedGraph inherits all methods from AbstractGraph, overrides the clear and addVertex methods, implements a new addEdge method for adding a weighted edge, and also introduces new methods for obtaining minimum spanning trees and for finding all single-source shortest paths. Minimum spanning trees and shortest paths will be introduced in Sections 29.4 and 29.5, respectively.

Listing 29.2 implements WeightedGraph. Edge adjacency lists (lines 38–63) are used internally to store adjacent edges for a vertex. When a WeightedGraph is constructed, its edge
adjacency lists are created (lines 47 and 57). The methods `getMinimumSpanningTree()` (lines 99–138) and `getShortestPath()` (lines 156–197) will be introduced in upcoming sections.

**Listing 29.2  WeightedGraph.java**

```java
import java.util.*;

public class WeightedGraph<V> extends AbstractGraph<V> {

/** Construct an empty */
public WeightedGraph() {
}

/** Construct a WeightedGraph from vertices and edged in arrays */
public WeightedGraph(V[] vertices, int[][] edges) {
    createWeightedGraph(java.util.Arrays.asList(vertices), edges);
}

/** Construct a WeightedGraph from vertices and edges in list */
public WeightedGraph(int[][] edges, int numberOfVertices) {
    List<V> vertices = new ArrayList<>();
    for (int i = 0; i < numberOfVertices; i++)
        vertices.add((V)(new Integer(i)));
    createWeightedGraph(vertices, edges);
}

// Other methods...
```

**Figure 29.4**  `WeightedGraph` extends `AbstractGraph`.

- Constructs an empty graph.
- Constructs a weighted graph with the specified edges and the number of vertices in arrays.
- Constructs a weighted graph with the specified edges.
- Constructs a weighted graph with the specified edges in an array and the number of vertices.
- Constructs a weighted graph with the specified edges in a list and the number of vertices.
- Displays all edges and weights.
- Returns the weight on the edge from u to v. Throws an exception if the edge does not exist.
- Adds a weighted edge to the graph and throws an `IllegalArgumentException` if u, v, or w is invalid. If (u, v) is already in the graph, the new weight is set.
- Returns a minimum spanning tree starting from vertex 0.
- Returns a minimum spanning tree starting from vertex v.
- Returns all single-source shortest paths.
/** Construct a WeightedGraph for vertices 0, 1, 2 and edge list */
public WeightedGraph(List<V> vertices, List<WeightedEdge> edges) {
    createWeightedGraph(vertices, edges);
}

/** Construct a WeightedGraph from vertices 0, 1, and edge array */
public WeightedGraph(List<WeightedEdge> edges, int numberOfVertices) {
    List<V> vertices = new ArrayList<>();
    for (int i = 0; i < numberOfVertices; i++)
        vertices.add((V)(new Integer(i)));
    createWeightedGraph(vertices, edges);
}

/** Create adjacency lists from edge arrays */
private void createWeightedGraph(List<V> vertices, int[][] edges) {
    for (int i = 0; i < vertices.size(); i++)
        neighbors.add(new ArrayList<Edge>()); // Create a list for vertices
    for (int i = 0; i < edges.length; i++)
        neighbors.get(edges[i][0]).add(new WeightedEdge(edges[i][0], edges[i][1], edges[i][2]));
}

/** Create adjacency lists from edge lists */
private void createWeightedGraph(List<V> vertices, List<WeightedEdge> edges) {
    for (int i = 0; i < vertices.size(); i++)
        neighbors.add(new ArrayList<Edge>()); // Create a list for vertices
    for (WeightedEdge edge: edges)
        neighbors.get(edge.u).add(edge); // Add an edge into the list
}

/** Return the weight on the edge (u, v) */
public double getWeight(int u, int v) throws Exception {
    for (Edge edge : neighbors.get(u))
        if (edge.v == v) {
            return ((WeightedEdge)edge).weight;
        }
    throw new Exception("Edge does not exist");
}

/** Display edges with weights */
public void printWeightedEdges() {
    for (int i = 0; i < getSize(); i++)
        System.out.print(getVertex(i) + " (" + i + "): ");
    for (Edge edge : neighbors.get(i))
        System.out.print("(" + edge.u + ")");
}
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```java
82         "," + edge.v + "," + ((WeightedEdge)edge).weight + ");
83     }
84     System.out.println();
85 }
86 }
87
88 /** Add edges to the weighted graph */
89 public boolean addEdge(int u, int v, double weight) {
90     return addEdge(new WeightedEdge(u, v, weight));
91 }
92
93 /** Get a minimum spanning tree rooted at vertex 0 */
94 public MST getMinimumSpanningTree() {
95     return getMinimumSpanningTree(0);
96 }
97
98 /** Get a minimum spanning tree rooted at a specified vertex */
99 public MST getMinimumSpanningTree(int startingVertex) {
100     // cost[v] stores the cost by adding v to the tree
101     double[] cost = new double[size()];
102     for (int i = 0; i < cost.length; i++) {
103         cost[i] = Double.POSITIVE_INFINITY; // Initial cost
104     }
105     cost[startingVertex] = 0; // Cost of source is 0
106
107     int[] parent = new int[size()]; // Parent of a vertex
108     parent[startingVertex] = -1; // startingVertex is the root
109     double totalWeight = 0; // Total weight of the tree thus far
110
111     List<Integer> T = new ArrayList<>();
112
113     // Expand T
114     while (T.size() < size()) {
115         // Find smallest cost v in V - T
116         int u = -1; // Vertex to be determined
117         double currentMinCost = Double.POSITIVE_INFINITY;
118         for (int i = 0; i < cost.length; i++) {
119             if (!T.contains(i) && cost[i] < currentMinCost) {
120                 currentMinCost = cost[i];
121                 u = i;
122             }
123         }
124         T.add(u); // Add a new vertex to T
125         totalWeight += cost[u]; // Add cost[u] to the tree
126
127         // Adjust cost[v] for v that is adjacent to u and v in V - T
128         for (Edge e : neighbors.get(u)) {
129             if (!T.contains(e.v) && cost[e.v] > ((WeightedEdge)e).weight) {
130                 cost[e.v] = ((WeightedEdge)e).weight;
131                 parent[e.v] = u;
132             }
133         }
134     } // End of while
135
136     return new MST(startingVertex, parent, T, totalWeight);
137 }
138
139 /** MST is an inner class in WeightedGraph */
140 public class MST extends Tree {
141     /**
142     */
143 
144 ```
private double totalWeight; // Total weight of all edges in the tree

public MST(int root, int[] parent, List<Integer> searchOrder, double totalWeight) {
    super(root, parent, searchOrder);
    this.totalWeight = totalWeight;
}

public double getTotalWeight() {
    return totalWeight;
}

/** Find single source shortest paths */
public ShortestPathTree getShortestPath(int sourceVertex) {
    double[] cost = new double[getSize()];
    for (int i = 0; i < cost.length; i++) {
        cost[i] = Double.POSITIVE_INFINITY; // Initial cost set to infinity
    }
    cost[sourceVertex] = 0; // Cost of source is 0

    int[] parent = new int[getSize()];
    parent[sourceVertex] = -1; // The parent of source is set to -1

    List<Integer> T = new ArrayList<>();

    // Expand T
    while (T.size() < getSize()) {
        int u = -1; // Vertex to be determined
        double currentMinCost = Double.POSITIVE_INFINITY;
        for (int i = 0; i < getSize(); i++) {
            if (!T.contains(i) && cost[i] < currentMinCost) {
                currentMinCost = cost[i];
                u = i;
            }
        }
        T.add(u); // Add a new vertex to T

        // Adjust cost[v] for v that is adjacent to u and v in V - T
        for (Edge e : neighbors.get(u)) {
            if (!T.contains(e.v) && cost[e.v] > cost[u] + ((WeightedEdge)e).weight) {
                cost[e.v] = cost[u] + ((WeightedEdge)e).weight;
                parent[e.v] = u;
            }
        }
    }

    // Create a ShortestPathTree
    return new ShortestPathTree(sourceVertex, parent, T, cost);
}

/** ShortestPathTree is an inner class in WeightedGraph */
public class ShortestPathTree extends Tree {
    private double[] cost; // cost[v] is the cost from v to source

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The **WeightedGraph** class extends the **AbstractGraph** class (line 3). The properties **vertices** and **neighbors** in **AbstractGraph** are inherited in **WeightedGraph**. **neighbors** is a list. Each element in the list is another list that contains edges. For an unweighted graph, each edge is an instance of **AbstractGraph.Edge**. For a weighted graph, each edge is an instance of **WeightedEdge**. **WeightedEdge** is a subtype of **Edge**. So you can add a weighted edge into **neighbors.get(i)** for a weighted graph (line 47).

Listing 29.3 gives a test program that creates a graph for the one in Figure 29.1 and another graph for the one in Figure 29.3a.

**LISTING 29.3  TestWeightedGraph.java**

```java
public class TestWeightedGraph {
    public static void main(String[] args) {
        int[][] edges = {
            {0, 1, 807}, {0, 3, 1331}, {0, 5, 2097},
            {1, 0, 807}, {1, 2, 381}, {1, 3, 1267},
            {2, 1, 381}, {2, 3, 1015}, {2, 4, 1663}, {2, 10, 1435},
            {3, 0, 1331}, {3, 1, 1267}, {3, 2, 1015}, {3, 4, 599},
            {4, 2, 1663}, {4, 3, 599}, {4, 5, 533}, {4, 7, 1260},
            {4, 8, 864}, {4, 10, 496},
            {5, 0, 2097}, {5, 3, 1003}, {5, 4, 533},
            {5, 6, 983}, {5, 7, 787},
            {6, 5, 983}, {6, 7, 214},
            {7, 4, 1260}, {7, 5, 787}, {7, 6, 214}, {7, 8, 888},
            {8, 4, 864}, {8, 7, 888}, {8, 9, 661},
            {8, 10, 781}, {8, 11, 810},
            {9, 8, 661}, {9, 11, 1187},
            {10, 2, 1435}, {10, 4, 496}, {10, 8, 781}, {10, 11, 239},
            {11, 8, 810}, {11, 9, 1187}, {11, 10, 239}
        };
    }
}
```
The program creates `graph1` for the graph in Figure 29.1 in lines 3–27. The vertices for `graph1` are defined in lines 3–5. The edges for `graph1` are defined in lines 7–24. The edges are represented using a two-dimensional array. For each row `i` in the array, `edges[i][0]` and `edges[i][1]` indicate that there is an edge from vertex `edges[i][0]` to vertex `edges[i][1]`. The program creates `graph2` for the graph in Figure 29.1 in lines 43–56. The edges for `graph2` are defined in lines 38–42.
edges[i][1] and the weight for the edge is edges[i][2]. For example, \{0, 1, 807\} (line 8) represents the edge from vertex 0 (edges[0][0]) to vertex 1 (edges[0][1]) with weight 807 (edges[0][2]). \{0, 5, 2097\} (line 8) represents the edge from vertex 0 (edges[2][0]) to vertex 5 (edges[2][1]) with weight 2097 (edges[2][2]). Line 35 invokes the printWeightedEdges() method on graph1 to display all edges in graph1.

The program creates the edges for graph2 for the graph in Figure 29.3a in lines 37–44. Line 46 invokes the printWeightedEdges() method on graph2 to display all edges in graph2.

29.3 If a priority queue is used to store weighted edges, what is the output of the following code?

```java
PriorityQueue<WeightedEdge> q = new PriorityQueue<>();
q.offer(new WeightedEdge(1, 2, 3.5));
q.offer(new WeightedEdge(1, 6, 6.5));
q.offer(new WeightedEdge(1, 7, 1.5));
System.out.println(q.poll().weight);
System.out.println(q.poll().weight);
System.out.println(q.poll().weight);
```

29.4 If a priority queue is used to store weighted edges, what is wrong in the following code? Fix it and show the output.

```java
List<PriorityQueue<WeightedEdge>> queues = new ArrayList<>();
queues.get(0).offer(new WeightedEdge(0, 2, 3.5));
queues.get(0).offer(new WeightedEdge(0, 6, 6.5));
queues.get(0).offer(new WeightedEdge(0, 7, 1.5));
queues.get(1).offer(new WeightedEdge(1, 0, 3.5));
queues.get(1).offer(new WeightedEdge(1, 5, 8.5));
queues.get(1).offer(new WeightedEdge(1, 8, 19.5));
System.out.println(queues.get(0).peek().compareTo(queues.get(1).peek()));
```

29.4 Minimum Spanning Trees

A minimum spanning tree of a graph is a spanning tree with the minimum total weights.

A graph may have many spanning trees. Suppose that the edges are weighted. A minimum spanning tree has the minimum total weights. For example, the trees in Figures 29.5b, 29.5c, 29.5d are spanning trees for the graph in Figure 29.5a. The trees in Figures 29.3c and 29.3d are minimum spanning trees.

The problem of finding a minimum spanning tree has many applications. Consider a company with branches in many cities. The company wants to lease telephone lines to connect all the branches together. The phone company charges different amounts of money to connect different pairs of cities. There are many ways to connect all branches together. The cheapest way is to find a spanning tree with the minimum total rates.

29.4.1 Minimum Spanning Tree Algorithms

How do you find a minimum spanning tree? There are several well-known algorithms for doing so. This section introduces Prim’s algorithm. Prim’s algorithm starts with a spanning tree \(T\) that contains an arbitrary vertex. The algorithm expands the tree by repeatedly adding a vertex with the lowest-cost edge incident to a vertex already in the tree. Prim’s algorithm is a greedy algorithm, and it is described in Listing 29.4.
LISTING 29.4 Prim’s Minimum Spanning Tree Algorithm

Input: A connected undirected weighted $G = (V, E)$ with non-negative weights
Output: MST (a minimum spanning tree)

```plaintext
MST minimumSpanningTree() {
    Let T be a set for the vertices in the spanning tree;
    Initially, add the starting vertex to T;
    
    while (size of T < n) {
        Find u in T and v in V – T with the smallest weight
        on the edge (u, v), as shown in Figure 29.6;
        Add v to T and set parent[v] = u;
    }
}
```

The algorithm starts by adding the starting vertex into $T$. It then continuously adds a vertex (say $v$) from $V - T$ into $T$. $v$ is the vertex that is adjacent to the vertex in $T$ with the smallest weight on the edge. For example, there are five edges connecting vertices in $T$ and $V - T$ as example.
shown in Figure 29.6, and \((u, v)\) is the one with the smallest weight. Consider the graph in Figure 29.7. The algorithm adds the vertices to \(T\) in this order:

1. Add vertex 0 to \(T\).
2. Add vertex 5 to \(T\), since \(\text{Edge}(5, 0, 5)\) has the smallest weight among all edges incident to a vertex in \(T\), as shown in Figure 29.7a. The arrow line from 0 to 5 indicates that 0 is the parent of 5.
3. Add vertex 1 to \(T\), since \(\text{Edge}(1, 0, 6)\) has the smallest weight among all edges incident to a vertex in \(T\), as shown in Figure 29.7b.
4. Add vertex 6 to \(T\), since \(\text{Edge}(6, 1, 7)\) has the smallest weight among all edges incident to a vertex in \(T\), as shown in Figure 29.7c.

\[\text{ Figure 29.7  The adjacent vertices with the smallest weight are added successively to } T.\]
5. Add vertex 2 to T, since Edge(2, 6, 5) has the smallest weight among all edges incident to a vertex in T, as shown in Figure 29.7d.

6. Add vertex 4 to T, since Edge(4, 6, 7) has the smallest weight among all edges incident to a vertex in T, as shown in Figure 29.7e.

7. Add vertex 3 to T, since Edge(3, 2, 8) has the smallest weight among all edges incident to a vertex in T, as shown in Figure 29.7f.

Note
A minimum spanning tree is not unique. For example, both (c) and (d) in Figure 29.5 are minimum spanning trees for the graph in Figure 29.5a. However, if the weights are distinct, the graph has a unique minimum spanning tree.

Note
Assume that the graph is connected and undirected. If a graph is not connected or directed, the algorithm will not work. You can modify the algorithm to find a spanning forest for any undirected graph. A spanning forest is a graph in which each connected component is a tree.

29.4.2 Refining Prim’s MST Algorithm

To make it easy to identify the next vertex to add into the tree, we use cost[v] to store the cost of adding a vertex v to the spanning tree T. Initially cost[s] is 0 for a starting vertex and assign infinity to cost[v] for all other vertices. The algorithm repeatedly finds a vertex u in V – T with the smallest cost[u] and moves u to T. The refined version of the algorithm is given in Listing 29.5.

Listing 29.5 Refined Version of Prim’s Algorithm

Input: A connected undirected weighted G = (V, E) with non-negative weights
Output: a minimum spanning tree with the starting vertex s as the root

```
1 MST getMinimumSpanningTree(s) {
2    Let T be a set that contains the vertices in the spanning tree;
3    Initially T is empty;
4    Set cost[s] = 0; and cost[v] = infinity for all other vertices in V;
5
6    while (size of T < n) {
7      Find u not in T with the smallest cost[u];  // find next vertex
8      Add u to T;  // add a vertex to T
9      for (each v not in T and (u, v) in E)
10         if (cost[v] > w(u, v)) {  // Adjust cost[v]
11            cost[v] = w(u, v); parent[v] = u;  // adjust cost[v]
12         }
13    }
14 }
```

29.4.3 Implementation of the MST Algorithm

The getMinimumSpanningTree(int v) method is defined in the WeightedGraph class. It returns an instance of the MST class, as shown in Figure 29.4. The MST class is defined as an inner class in the WeightedGraph class, which extends the Tree class, as shown in Figure 29.8. The Tree class was shown in Figure 28.11. The MST class was implemented in lines 141–153 in Listing 29.2.
The refined version of the Prim’s algorithm greatly simplifies the implementation. The `getMinimumSpanningTree` method was implemented using the refined version of the Prim’s algorithm in lines 99–138 in Listing 29.2. The `getMinimumSpanningTree(int startingVertex)` method sets `cost[startingVertex]` to `0` (line 105) and `cost[v]` to infinity for all other vertices (lines 102–104). The parent of `startingVertex` is set to `-1` (line 108). `T` is a list that stores the vertices added into the spanning tree (line 111). We use a list for `T` rather than a set in order to record the order of the vertices added to `T`.

Initially, `T` is empty. To expand `T`, the method performs the following operations:

1. Find the vertex `u` with the smallest `cost[u]` (lines 118–123) and add it into `T` (line 125).

After a new vertex is added to `T`, `totalWeight` is updated (line 126). Once all vertices are added to `T`, an instance of `MST` is created (line 137). Note that the method will not work if the graph is not connected. However, you can modify it to obtain a partial MST.

The `MST` class extends the `Tree` class (line 141). To create an instance of `MST`, pass `root`, `parent`, `T`, and `totalWeight` (lines 144–145). The data fields `root`, `parent`, and `searchOrder` are defined in the `Tree` class, which is an inner class defined in `AbstractGraph`.

Note that testing whether a vertex `i` is in `T` by invoking `T.contains(i)` takes $O(n)$ time, since `T` is a list. Therefore, the overall time complexity for this implementation is $O(n^3)$. Interested readers may see Programming Exercise 29.20 for improving the implementation and reduce the complexity to $O(n^2)$.

Listing 29.6 gives a test program that displays minimum spanning trees for the graph in Figure 29.1 and the graph in Figure 29.3a, respectively.

**Listing 29.6 TestMinimumSpanningTree.java**

```java
public class TestMinimumSpanningTree {
    public static void main(String[] args) {
        String[] vertices = {
            "Seattle", "San Francisco", "Los Angeles",
            "Atlanta", "Miami", "Dallas", "Houston"};

        int[][] edges = {
            {0, 1, 807}, {0, 3, 1331}, {0, 5, 2097},
            {1, 0, 807}, {1, 2, 381}, {1, 3, 1267},
            {2, 1, 381}, {2, 3, 1015}, {2, 4, 1663}, {2, 10, 1435},
            {3, 0, 1331}, {3, 1, 1267}, {3, 2, 1015}, {3, 4, 599},
```
29.4 Minimum Spanning Trees

The program creates a weighted graph for Figure 29.1 in line 27. It then invokes `getMinimumSpanningTree()` (line 28) to return an MST that represents a minimum spanning tree for the graph. Invoking `printTree()` (line 30) on the MST object displays the edges in the tree. Note that MST is a subclass of Tree. The `printTree()` method is defined in the Tree class.

The graphical illustration of the minimum spanning tree is shown in Figure 29.9. The vertices are added to the tree in this order: Seattle, San Francisco, Los Angeles, Denver, Kansas City, Chicago, Dallas, Atlanta, and Miami.
29.5 Find a minimum spanning tree for the following graph.

29.6 Is a minimum spanning tree unique if all edges have different weights?

29.7 If you use an adjacency matrix to represent weighted edges, what will be the time complexity for Prim’s algorithm?

29.8 What happens to the getMinimumSpanningTree() method in WeightedGraph if the graph is not connected? Verify your answer by writing a test program that creates an unconnected graph and invokes the getMinimumSpanningTree() method. How do you fix the problem by obtaining a partial MST?

29.5 Finding Shortest Paths

The shortest path between two vertices is a path with the minimum total weights.

Given a graph with nonnegative weights on the edges, a well-known algorithm for finding a shortest path between two vertices was discovered by Edsger Dijkstra, a Dutch computer scientist. In order to find a shortest path from vertex s to vertex v, Dijkstra’s algorithm finds the
shortest path from \( s \) to all vertices. So Dijkstra’s algorithm is known as a single-source shortest path algorithm. The algorithm uses \( \text{cost}[v] \) to store the cost of a shortest path from vertex \( v \) to the source vertex \( s \). \( \text{cost}[s] = 0 \). Initially assign infinity to \( \text{cost}[v] \) for all other vertices. The algorithm repeatedly finds a vertex \( u \) in \( V - T \) with the smallest \( \text{cost}[u] \) and moves \( u \) to \( T \).

The algorithm is described in Listing 29.7.

**Listing 29.7 Dijkstra’s Single-Source Shortest-Path Algorithm**

Input: a graph \( G = (V, E) \) with non-negative weights
Output: a shortest path tree with the source vertex \( s \) as the root

```plaintext
1 ShortestPathTree getShortestPath(s) {
2    Let \( T \) be a set that contains the vertices whose
3        paths to \( s \) are known; Initially \( T \) is empty;
4    Set \( \text{cost}[s] = 0 \); and \( \text{cost}[v] = \text{infinity} \) for all other vertices in \( V \);
5    
6    while (size of \( T \) < \( n \)) {
7        Find \( u \) not in \( T \) with the smallest \( \text{cost}[u] \);  
8            find next vertex
9            Add \( u \) to \( T \);  
10           add a vertex to \( T \)
11            for (each \( v \) not in \( T \) and (\( u \), \( v \)) in \( E \))  
12                if (\( \text{cost}[v] > \text{cost}[u] + \text{w}(u, v) \)) {
13                    \( \text{cost}[v] = \text{cost}[u] + \text{w}(u, v) \); \( \text{parent}[v] = u \);  
14                        adjust \( \text{cost}[v] \)
15            }
16    }
17 }
```

This algorithm is very similar to Prim’s for finding a minimum spanning tree. Both algorithms divide the vertices into two sets: \( T \) and \( V - T \). In the case of Prim’s algorithm, set \( T \) contains the vertices that are already added to the tree. In the case of Dijkstra’s, set \( T \) contains the vertices whose shortest paths to the source have been found. Both algorithms repeatedly find a vertex from \( V - T \) and add it to \( T \). In the case of Prim’s algorithm, the vertex is adjacent to some vertex in the set with the minimum weight on the edge. In Dijkstra’s algorithm, the vertex is adjacent to some vertex in the set with the minimum total cost to the source.

The algorithm starts by setting \( \text{cost}[s] = 0 \) (line 4), sets \( \text{cost}[v] \) to infinity for all other vertices. It then continuously adds a vertex (say \( u \)) from \( V - T \) into \( T \) with smallest \( \text{cost}[u] \) (lines 7–8), as shown in Figure 29.10a. After adding \( u \) to \( T \), the algorithm updates \( \text{cost}[v] \) and \( \text{parent}[v] \) for each \( v \) not in \( T \) if (\( u \), \( v \)) is in \( T \) and \( \text{cost}[v] > \text{cost}[u] + \text{w}(u, v) \) (lines 10–11).

---

**Figure 29.10** (a) Find a vertex \( u \) in \( V - T \) with the smallest \( \text{cost}[u] \). (b) Update \( \text{cost}[v] \) for \( v \) in \( V - T \) and \( v \) is adjacent to \( u \).
Let us illustrate Dijkstra’s algorithm using the graph in Figure 29.11a. Suppose the source vertex is 1. Therefore, cost[1] = 0 and the costs for all other vertices are initially ∞, as shown in Figure 29.11b. We use the parent[i] to denote the parent of i in the path. For convenience, set the parent of the source node to -1.

![Figure 29.11](image1)

**Figure 29.11** The algorithm will find all shortest paths from source vertex 1.

Initially set T is empty. The algorithm selects the vertex with the smallest cost. In this case, the vertex is 1. The algorithm adds 1 to T, as shown in Figure 29.12a. Afterwards, it adjusts the cost for each vertex adjacent to 1. The cost for vertices 2, 0, 6, and 3 and their parents are now updated, as shown, as shown in Figure 29.12b.

![Figure 29.12](image2)

**Figure 29.12** Now vertex 1 is in set T.

Vertices 2, 0, 6, and 3 are adjacent to the source vertex, and vertex 2 is the one in V−T with the smallest cost, so add 2 to T, as shown in Figure 29.13 and update the cost and parent for vertices in V−T and adjacent to 2. cost[0] is now updated to 6 and its parent is set to 2. The arrow line from 1 to 2 indicates that 1 is the parent of 2 after 2 is added into T.
Now $T$ contains \{1, 2\}. Vertex 0 is the one in $V - T$ with the smallest cost, so add 0 to $T$, as shown in Figure 29.14 and update the cost and parent for vertices in $V - T$ and adjacent to 0 if applicable. \textit{cost}[5] is now updated to 10 and its parent is set to 0 and \textit{cost}[6] is now updated to 8 and its parent is set to 0.

Now $T$ contains \{1, 2, 0\}. Vertex 6 is the one in $V - T$ with the smallest cost, so add 6 to $T$, as shown in Figure 29.15 and update the cost and parent for vertices in $V - T$ and adjacent to 6 if applicable.

Now $T$ contains \{1, 2, 0, 6\}. Vertex 1 is the one in $V - T$ with the smallest cost, so add 1 to $T$, as shown in Figure 29.16 and update the cost and parent for vertices in $V - T$ and adjacent to 1 if applicable.
Chapter 29  Weighted Graphs and Applications

Now \( T \) contains \( \{1, 2, 0, 6\} \). Vertex 3 or 5 is the one in \( V-T \) with the smallest cost. You may add either 3 or 5 into \( T \). Let us add 3 to \( T \), as shown in Figure 29.16 and update the cost and parent for vertices in \( V-T \) and adjacent to 3 if applicable. \( \text{cost}[4] \) is now updated to 18 and its parent is set to 3.

![Figure 29.16](image1)

**Figure 29.16** Now vertices \( \{1, 2, 0, 6, 3\} \) are in set \( T \).

Now \( T \) contains \( \{1, 2, 0, 6, 3\} \). Vertex 5 is the one in \( V-T \) with the smallest cost, so add 5 to \( T \), as shown in Figure 29.17 and update the cost and parent for vertices in \( V-T \) and adjacent to 5 if applicable. \( \text{cost}[4] \) is now updated to 10 and its parent is set to 5.

![Figure 29.17](image2)

**Figure 29.17** Now vertices \( \{1, 2, 0, 6, 3, 5\} \) are in set \( T \).

Now \( T \) contains \( \{1, 2, 0, 6, 3, 5\} \). Vertex 4 is the one in \( V-T \) with the smallest cost, so add 4 to \( T \), as shown in Figure 29.18.

As you can see, the algorithm essentially finds all shortest paths from a source vertex, which produces a tree rooted at the source vertex. We call this tree a **single-source all-shortest-path tree** (or simply a **shortest-path tree**). To model this tree, define a class named **ShortestPathTree** that extends the **Tree** class, as shown in Figure 29.19. **ShortestPathTree** is defined as an inner class in **WeightedGraph** in lines 200–224 in Listing 29.2.

The `getShortestPath(int sourceVertex)` method was implemented in lines 156–197 in Listing 29.2. The method sets \( \text{cost[sourceVertex]} \) to 0 (line 162) and \( \text{cost[v]} \) to
29.5 Finding Shortest Paths

Finding Shortest Paths

infinity for all other vertices (lines 159–161). The parent of sourceVertex is set to -1 (line 166). T is a list that stores the vertices added into the shortest path tree (line 169). We use a list for T rather than a set in order to record the order of the vertices added to T.

Initially, T is empty. To expand T, the method performs the following operations:

1. Find the vertex u with the smallest cost[u] (lines 175–181) and add it into T (line 183).

Once all vertices from s are added to T, an instance of ShortestPathTree is created (line 196).

The ShortestPathTree class extends the Tree class (line 200). To create an instance of ShortestPathTree, pass sourceVertex, parent, T, and cost (lines 204–205). sourceVertex becomes the root in the tree. The data fields root, parent, and searchOrder are defined in the Tree class, which is an inner class defined in AbstractGraph.

Note that testing whether a vertex i is in T by invoking T.contains(i) takes O(n) time, since T is a list. Therefore, the overall time complexity for this implementation is O(n^2). Interested readers may see Programming Exercise 29.20 for improving the implementation and reducing the complexity to O(n^2).

Dijkstra’s algorithm is a combination of a greedy algorithm and dynamic programming. It is a greedy algorithm in the sense that it always adds a new vertex that has the shortest distance to the source. It stores the shortest distance of each known vertex to the source and uses it later to avoid redundant computing, so Dijkstra’s algorithm also uses dynamic programming.

FIGURE 29.18 Now vertices {1, 2, 6, 0, 3, 5, 4} are in set T.

FIGURE 29.19 WeightedGraph.ShortestPathTree extends AbstractGraph.Tree.

AbstractGraph.Tree

WeightedGraph.ShortestPathTree

-cost: int[]

+ShortestPathTree(source: int, parent: int[], searchOrder: List<Integer>, cost: int[])
+getCost(v: int): int
+printAllPaths(): void

cost[v] stores the cost for the path from the source to v.

Constructs a shortest path tree with the specified source, parent array, searchOrder, and cost array.

Returns the cost for the path from the source to vertex v.

Displays all paths from the source.
Pedagogical Note
Go to www.cs.armstrong.edu/liang/animation/ShortestPathAnimation.html to use a GUI interactive program to find a shortest path between any two cities, as shown in Figure 29.20.

Figure 29.20  The animation tool displays a shortest path between two cities.

Listing 29.8 gives a test program that displays the shortest paths from Chicago to all other cities in Figure 29.1 and the shortest paths from vertex 3 to all vertices for the graph in Figure 29.3a, respectively.

Listing 29.8  TestShortestPath.java

```java
public class TestShortestPath {
    public static void main(String[] args) {
        String[] vertices = {
        int[][] edges = {
            {0, 1, 807}, {0, 3, 1331}, {0, 5, 2097},
            {1, 0, 807}, {1, 2, 381}, {1, 3, 1267},
            {2, 1, 381}, {2, 3, 1015}, {2, 4, 1663}, {2, 10, 1435},
            {3, 0, 1331}, {3, 1, 1267}, {3, 2, 1015}, {3, 4, 599},
            {3, 5, 1003},
            {4, 2, 1663}, {4, 3, 599}, {4, 5, 533}, {4, 7, 1260},
            {4, 8, 864}, {4, 10, 496},
            {5, 0, 2097}, {5, 3, 1003}, {5, 4, 533},
            {5, 6, 983}, {5, 7, 787},
            {6, 5, 983}, {6, 7, 214},
            {7, 4, 1260}, {7, 5, 787}, {7, 6, 214}, {7, 8, 888},
            {8, 4, 864}, {8, 7, 888}, {8, 9, 661},
            {8, 10, 781}, {8, 11, 810},
            {9, 8, 661}, {9, 11, 1187},
```
29.5 Finding Shortest Paths

```java
{10, 2, 1435}, {10, 4, 496}, {10, 8, 781}, {10, 11, 239},
{11, 8, 810}, {11, 9, 1187}, {11, 10, 239}
}

WeightedGraph<String> graph1 =
    new WeightedGraph<>((vertices, edges));
WeightedGraph<String>.ShortestPathTree tree1 =
    graph1.getShortestPath(graph1.getIndex("Chicago"));
tree1.printAllPaths();
// Display shortest paths from Houston to Chicago
System.out.print("Shortest path from Houston to Chicago: ");
java.util.List<String> path
    = tree1.getPath(graph1.getIndex("Houston"));
for (String s: path) {
    System.out.print(s + " ");
}

edges = new int[][] {
    {0, 1, 2}, {0, 3, 8},
    {1, 0, 2}, {1, 2, 7}, {1, 3, 3},
    {2, 1, 7}, {2, 3, 4}, {2, 4, 5},
    {3, 0, 8}, {3, 1, 3}, {3, 2, 4}, {3, 4, 6},
    {4, 2, 5}, {4, 3, 6}
};
WeightedGraph<Integer> graph2 =
    new WeightedGraph<>(edges, 5);
WeightedGraph<Integer>.ShortestPathTree tree2 =
    graph2.getShortestPath(3);
tree2.printAllPaths();
```

All shortest paths from Chicago are:
A path from Chicago to Seattle: Chicago Seattle (cost: 2097.0)
A path from Chicago to San Francisco:
    Chicago Denver San Francisco (cost: 2270.0)
A path from Chicago to Los Angeles:
    Chicago Denver Los Angeles (cost: 2018.0)
A path from Chicago to Denver: Chicago Denver (cost: 1003.0)
A path from Chicago to Kansas City: Chicago Kansas City (cost: 533.0)
A path from Chicago to Chicago: Chicago (cost: 0.0)
A path from Chicago to Boston: Chicago Boston (cost: 983.0)
A path from Chicago to New York: Chicago New York (cost: 787.0)
A path from Chicago to Atlanta:
    Chicago Kansas City Atlanta (cost: 1397.0)
A path from Chicago to Miami:
    Chicago Kansas City Atlanta Miami (cost: 2058.0)
A path from Chicago to Dallas: Chicago Kansas City Dallas (cost: 1029.0)
A path from Chicago to Houston:
    Chicago Kansas City Dallas Houston (cost: 1268.0)
Shortest path from Houston to Chicago:
    Houston Dallas Kansas City Chicago

All shortest paths from 3 are:
A path from 3 to 0: 3 1 0 (cost: 5.0)
A path from 3 to 1: 3 1 (cost: 3.0)
A path from 3 to 2: 3 2 (cost: 4.0)
A path from 3 to 3: 3 (cost: 0.0)
A path from 3 to 4: 3 4 (cost: 6.0)
The program creates a weighted graph for Figure 29.1 in line 27. It then invokes the `getShortestPath(graph1.getIndex("Chicago"))` method to return a Path object that contains all shortest paths from Chicago. Invoking `printAllPaths()` on the `ShortestPathTree` object displays all the paths (line 30).

The graphical illustration of all shortest paths from Chicago is shown in Figure 29.21. The shortest paths from Chicago to the cities are found in this order: Kansas City, New York, Boston, Denver, Dallas, Houston, Atlanta, Los Angeles, Miami, Seattle, and San Francisco.

![Figure 29.21](image)

The shortest paths from Chicago to all other cities are highlighted.

29.9 Trace Dijkstra’s algorithm for finding shortest paths from Boston to all other cities in Figure 29.1.

29.10 Is a shortest path between two vertices unique if all edges have different weights?

29.11 If you use an adjacency matrix to represent weighted edges, what would be the time complexity for Dijkstra’s algorithm?

29.12 What happens to the `getShortestPath()` method in `WeightedGraph` if the source vertex cannot reach all vertices in the graph? Verify your answer by writing a test program that creates an unconnected graph and invoke the `getShortestPath()` method. How do you fix the problem by obtaining a partial shortest path tree?

29.13 If there is no path from vertex v to the source vertex, what will be `cost[v]`?

29.14 Assume that the graph is connected; will the `getShortestPath` method find the shortest paths correctly if lines 159–161 in `WeightedGraph` are deleted?

29.6 Case Study: The Weighted Nine Tails Problem

The weighted nine tails problem can be reduced to the weighted shortest path problem.

Section 28.10 presented the nine tails problem and solved it using the BFS algorithm. This section presents a variation of the problem and solves it using the shortest-path algorithm.
The nine tails problem is to find the minimum number of the moves that lead to all coins facing down. Each move flips a head coin and its neighbors. The weighted nine tails problem assigns the number of flips as a weight on each move. For example, you can change the coins in Figure 29.22a to those in Figure 29.22b by flipping the first coin in the first row and its two neighbors. Thus, the weight for this move is 3. You can change the coins in Figure 29.22c to Figure 29.22d by flipping the center coin and its four neighbors. So the weight for this move is 5.

![Figure 29.22](image.png)

The weighted nine tails problem can be reduced to finding a shortest path from a starting node to the target node in an edge-weighted graph. The graph has 512 nodes. Create an edge from node \(v\) to \(u\) if there is a move from node \(u\) to node \(v\). Assign the number of flips to be the weight of the edge.

Recall that in Section 28.10 we defined a class `NineTailModel` for modeling the nine tails problem. We now define a new class named `WeightedNineTailModel` that extends `NineTailModel`, as shown in Figure 29.23.

![Figure 29.23](image.png)
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The NineTailModel class creates a Graph and obtains a Tree rooted at the target node 511. WeightedNineTailModel is the same as NineTailModel except that it creates a WeightedGraph and obtains a ShortestPathTree rooted at the target node 511. Weight-
edNineTailModel extends NineTailModel. The method getEdges() finds all edges in
the graph. The getNumberOfFlips(int u, int v) method returns the number of flips
from node u to node v. The getNumberOfFlips(int u) method returns the number of flips
from node u to the target node.

Listing 29.9 implements WeightedNineTailModel.

LISTING 29.9  WeightedNineTailModel.java

```java
import java.util.*;

public class WeightedNineTailModel extends NineTailModel {
    public WeightedNineTailModel() {
        // Create edges
        List<WeightedEdge> edges = getEdges();
        // Create a graph
        WeightedGraph<Integer> graph = new WeightedGraph<>(
            edges, NUMBER_OF_NODES);
        // Obtain a shortest path tree rooted at the target node
        tree = graph.getShortestPath(511);
    }

    private List<WeightedEdge> getEdges() {
        // Store edges
        List<WeightedEdge> edges = new ArrayList<>();
        for (int u = 0; u < NUMBER_OF_NODES; u++) {
            for (int k = 0; k < 9; k++) {
                char[] node = getNode(u); // Get the node for vertex u
                if (node[k] == 'H') {
                    int v = getFlippedNode(node, k);
                    int numberOfFlips = getNumberOfFlips(u, v);
                    edges.add(new WeightedEdge(v, u, numberOfFlips));
                }
            }
        }
        return edges;
    }

    private static int getNumberOfFlips(int u, int v) {
        char[] node1 = getNode(u);
        char[] node2 = getNode(v);
        int count = 0; // Count the number of different cells
        for (int i = 0; i < node1.length; i++)
            if (node1[i] != node2[i]) count++;
        return count;
    }
```

Listing 29.9 implements WeightedNineTailModel.
29.6 Case Study: The Weighted Nine Tails Problem

WeightedNineTailModel extends NineTailModel to build a WeightedGraph to model the weighted nine tails problem (lines 10–11). For each node \( u \), the getEdges() method finds a flipped node \( v \) and assigns the number of flips as the weight for edge \((v, u)\) (line 30). The getNumberOfFlips(int \( u \), int \( v \)) method returns the number of flips from node \( u \) to node \( v \) (lines 38–47). The number of flips is the number of the different cells between the two nodes (line 44).

The WeightedNineTailModel obtains a ShortestPathTree rooted at the target node \( 511 \) (line 14). Note that tree is a protected data field defined in NineTailModel and ShortestPathTree is a subclass of Tree. The methods defined in NineTailModel use the tree property.

The getNumberOfFlips(int \( u \)) method (lines 49–52) returns the number of flips from node \( u \) to the target node, which is the cost of the path from node \( u \) to the target node. This cost can be obtained by invoking the getCost(u) method defined in the ShortestPathTree class (line 51).

Listing 29.10 gives a program that prompts the user to enter an initial node and displays the minimum number of flips to reach the target node.

**Listing 29.10** WeightedNineTail.java

```java
import java.util.Scanner;

public class WeightedNineTail {
    public static void main(String[] args) {
        // Prompt the user to enter the nine coins' Hs and Ts
        System.out.print("Enter an initial nine coins' Hs and Ts: ");
        Scanner input = new Scanner(System.in);
        String s = input.nextLine();
        char[] initialNode = s.toCharArray();
        WeightedNineTailModel model = new WeightedNineTailModel();
        java.util.List<Integer> path = model.getShortestPath(NineTailModel.getIndex(initialNode));
        System.out.println("The steps to flip the coins are ");
        for (int i = 0; i < path.size(); i++)
            NineTailModel.printNode(NineTailModel.getNode(path.get(i)));
        System.out.println("The number of flips is "+
                          model.getNumberOfFlips(NineTailModel.getIndex(initialNode)));
    }
}
```

Enter an initial nine coins Hs and Ts: HHHTTTHHH

The steps to flip the coins are
HHH
TTT
HHH
The program prompts the user to enter an initial node with nine letters with a combination of Hs and Ts as a string in line 8, obtains an array of characters from the string (line 9), creates a model (line 11), obtains the shortest path from the initial node to the target node (lines 12–13), displays the nodes in the path (lines 16–17), and invokes `getNumberOfFlips` to get the number of flips needed to reach the target node (line 20).

29.15 Why is the tree data field in `NineTailModel` in Listing 28.13 defined protected?

29.16 How are the nodes created for the graph in `WeightedNineTailModel`?

29.17 How are the edges created for the graph in `WeightedNineTailModel`?

**KEY TERMS**

- Dijkstra’s algorithm 1078
- edge-weighted graph 1063
- minimum spanning tree 1072
- Prim’s algorithm 1072
- shortest path 1078
- single-source shortest path 1079
- vertex-weighted graph 1063

**CHAPTER SUMMARY**

1. You can use adjacency matrices or lists to store weighted edges in graphs.

2. A spanning tree of a graph is a subgraph that is a tree and connects all vertices in the graph.

3. Prim’s algorithm for finding a minimum spanning tree works as follows: the algorithm starts with a spanning tree that contains an arbitrary vertex. The algorithm expands the tree by adding a vertex with the minimum-weight edge incident to a vertex already in the tree.

4. Dijkstra’s algorithm starts search from the source vertex and keeps finding vertices that have the shortest path to the source until all vertices are found.

**QUIZ**

Answer the quiz for this chapter online at [www.cs.armstrong.edu/liang/intro10e/quiz.html](http://www.cs.armstrong.edu/liang/intro10e/quiz.html).

**PROGRAMMING EXERCISES**

*29.1 (Kruskal’s algorithm) The text introduced Prim’s algorithm for finding a minimum spanning tree. Kruskal’s algorithm is another well-known algorithm for finding a minimum spanning tree. The algorithm repeatedly finds a minimum-weight edge and adds it to the tree if it does not cause a cycle. The process ends
when all vertices are in the tree. Design and implement an algorithm for finding an MST using Kruskal’s algorithm.

**29.2** (Implement Prim’s algorithm using an adjacency matrix) The text implements Prim’s algorithm using lists for adjacent edges. Implement the algorithm using an adjacency matrix for weighted graphs.

**29.3** (Implement Dijkstra’s algorithm using an adjacency matrix) The text implements Dijkstra’s algorithm using lists for adjacent edges. Implement the algorithm using an adjacency matrix for weighted graphs.

**29.4** (Modify weight in the nine tails problem) In the text, we assign the number of the flips as the weight for each move. Assuming that the weight is three times the number of flips, revise the program.

**29.5** (Prove or disprove) The conjecture is that both NineTailModel1 and WeightedNineTailModel result in the same shortest path. Write a program to prove or disprove it. *(Hint: Let tree1 and tree2 denote the trees rooted at node 511 obtained from NineTailModel and WeightedNineTailModel, respectively. If the depth of a node u is the same in tree1 and in tree2, the length of the path from u to the target is the same.)*

**29.6** (Weighted 4 × 4 16 tails model) The weighted nine tails problem in the text uses a 3 × 3 matrix. Assume that you have 16 coins placed in a 4 × 4 matrix. Create a new model class named WeightedTailModel16. Create an instance of the model and save the object into a file named WeightedTailModel16.dat.

**29.7** (Weighted 4 × 4 16 tails) Revise Listing 29.9, WeightedNineTail.java, for the weighted 4 × 4 16 tails problem. Your program should read the model object created from the preceding exercise.

**29.8** (Traveling salesperson problem) The traveling salesperson problem (TSP) is to find a shortest round-trip route that visits each city exactly once and then returns to the starting city. The problem is equivalent to finding a shortest Hamiltonian cycle in Programming Exercise 28.17. Add the following method in the WeightedGraph class:

```java
// Return a shortest cycle
// Return null if no such cycle exists
public List<Integer> getShortestHamiltonianCycle()
```

**29.9** (Find a minimum spanning tree) Write a program that reads a connected graph from a file and displays its minimum spanning tree. The first line in the file contains a number that indicates the number of vertices (n). The vertices are labeled as 0, 1, ..., n-1. Each subsequent line describes the edges in the form of u1, v1, w1 | u2, v2, w2 | .... Each triplet in this form describes an edge and its weight. Figure 29.24 shows an example of the file for the corresponding graph. Note that we assume the graph is undirected. If the graph has

![Figure 29.24](image-url) The vertices and edges of a weighted graph can be stored in a file.
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an edge \((u, v)\), it also has an edge \((v, u)\). Only one edge is represented in the file. When you construct a graph, both edges need to be added.

Your program should prompt the user to enter the name of the file, read data from the file, create an instance \(g\) of \(WeightedGraph\), invoke \(g\).printWeightedEdges() to display all edges, invoke \(getMinimumSpanningTree()\) to obtain an instance \(tree\) of \(WeightedGraph\).MST, invoke \(tree\).getTotalWeight() to display the weight of the minimum spanning tree, and invoke \(tree\).printTree() to display the tree. Here is a sample run of the program:

Enter a file name: c:\exercise\WeightedGraphSample.txt
The number of vertices is 6
Vertex 0: (0, 2, 3) (0, 1, 100)
Vertex 1: (1, 3, 20) (1, 0, 100)
Vertex 2: (2, 4, 2) (2, 3, 40) (2, 0, 3)
Vertex 3: (3, 4, 5) (3, 5, 5) (3, 1, 20) (3, 2, 40)
Vertex 4: (4, 2, 2) (4, 3, 5) (4, 5, 9)
Vertex 5: (5, 3, 5) (5, 4, 9)
Total weight in MST is 35
Root is: 0
Edges: (3, 1) (0, 2) (4, 3) (2, 4) (3, 5)

(Hint: Use \(\text{new WeightedGraph(list, numberOfVertices)}\) to create a graph, where \(list\) contains a list of \(WeightedEdge\) objects. Use \(\text{new WeightedEdge(u, v, w)}\) to create an edge. Read the first line to get the number of vertices. Read each subsequent line into a string \(s\) and use \(s.split(\"[\|]\))\) to extract the triplets. For each triplet, use \(triplet.split(\"[,]\))\) to extract vertices and weight.)

*29.10  (Create a file for a graph) Modify Listing 29.3, TestWeightedGraph.java, to create a file for representing graph1. The file format is described in Programming Exercise 29.9. Create the file from the array defined in lines 7–24 in Listing 29.3. The number of vertices for the graph is 12, which will be stored in the first line of the file. An edge \((u, v)\) is stored if \(u < v\). The contents of the file should be as follows:

*29.11  (Find shortest paths) Write a program that reads a connected graph from a file. The graph is stored in a file using the same format specified in Programming Exercise 29.9. Your program should prompt the user to enter the name of the file then two vertices, and should display a shortest path between the two
vertices. For example, for the graph in Figure 29.23, a shortest path between 0 and 1 can be displayed as 0 2 4 3 1.

Here is a sample run of the program:

```
Enter a file name: WeightedGraphSample2.txt
Enter two vertices (integer indexes): 0 1
The number of vertices is 6
Vertex 0: (0, 2, 3) (0, 1, 100)
Vertex 1: (1, 3, 20) (1, 0, 100)
Vertex 2: (2, 4, 2) (2, 3, 40) (2, 0, 3)
Vertex 3: (3, 4, 5) (3, 5, 5) (3, 1, 20) (3, 2, 40)
Vertex 4: (4, 2, 2) (4, 3, 5) (4, 5, 9)
Vertex 5: (5, 3, 5) (5, 4, 9)
A path from 0 to 1: 0 2 4 3 1
```

**29.12** (Display weighted graphs) Revise `GraphView` in Listing 28.6 to display a weighted graph. Write a program that displays the graph in Figure 29.1 as shown in Figure 29.25. (Instructors may ask students to expand this program by adding new cities with appropriate edges into the graph).

**29.13** (Display shortest paths) Revise `GraphView` in Listing 28.6 to display a weighted graph and a shortest path between the two specified cities, as shown in Figure 29.19. You need to add a data field `path` in `GraphView`. If a `path` is not null, the edges in the path are displayed in red. If a city not in the map is entered, the program displays a text to alert the user.

**29.14** (Display a minimum spanning tree) Revise `GraphView` in Listing 28.6 to display a weighted graph and a minimum spanning tree for the graph in Figure 29.1, as shown in Figure 29.26. The edges in the MST are shown in red.

**29.15** (Dynamic graphs) Write a program that lets the users create a weighted graph dynamically. The user can create a vertex by entering its name and location, as shown in Figure 29.27. The user can also create an edge to connect two vertices. To simplify the program, assume that vertex names are the same as vertex
Chapter 29  Weighted Graphs and Applications

indices. You have to add the vertex indices $0, 1, \ldots, n$, in this order. The user can specify two vertices and let the program display their shortest path in red.

**29.16** (Display a dynamic MST) Write a program that lets the user create a weighted graph dynamically. The user can create a vertex by entering its name and location, as shown in Figure 29.28. The user can also create an edge to connect two vertices. To simplify the program, assume that vertex names are the same as those of vertex indices. You have to add the vertex indices $0, 1, \ldots, n$, in this order. The edges in the MST are displayed in red. As new edges are added, the MST is redisplayed.

**29.17** (Weighted graph visualization tool) Develop a GUI program as shown in Figure 29.2, with the following requirements: (1) The radius of each vertex is 20 pixels. (2) The user clicks the left mouse button to place a vertex centered at the mouse point, provided that the mouse point is not inside or too close to an existing vertex. (3) The user clicks the right mouse button inside an existing vertex to remove the vertex. (4) The user presses a mouse button inside a vertex and drags to another vertex and then releases the button to create an
edge, and the distance between the two vertices is also displayed. (5) The user 
drags a vertex while pressing the \textit{CTRL} key to move a vertex. (6) The verti-
ces are numbers starting from 0. When a vertex is removed, the vertices are 
renumbered. (7) You can click the \textit{Show MST} or \textit{Show All SP From the Source} 
button to display an MST or SP tree from a starting vertex. (8) You can click 
the \textit{Show Shortest Path} button to display the shortest path between the two 
specified vertices. 

***29.18 (Alternative version of Dijkstra algorithm) An alternative version of the Dijk-
stra algorithm can be described as follows:

Input: a weighted graph $G = (V, E)$ with non-negative weights 
Output: A shortest path tree from a source vertex $s$

\begin{algorithm}
\begin{algorithmic}
\Function{getShortestPath}{s}
\State Let $T$ be a set that contains the vertices whose 
\State paths to $s$ are known;
\State Initially $T$ contains source vertex $s$ with $\text{cost}[s] = 0$; \Comment{add initial vertex}
\State for (each $u$ in $V - T$)
\State \hspace{1em} $\text{cost}[u] = \infty$;
\State \While {(size of $T < n$)} \Comment{more vertex}
\State \hspace{1em} Find $v$ in $V - T$ with the smallest $\text{cost}[u] + w(u, v)$ value 
\State \hspace{1em} among all $u$ in $T$;
\State \hspace{1em} Add $v$ to $T$ and set $\text{cost}[v] = \text{cost}[u] + w(u, v)$; \Comment{find next vertex}
\State \hspace{1em} parent[$v$] = $u$;
\State \EndWhile
\State \EndFor
\State \EndWhile
\EndFunction
\end{algorithmic}
\end{algorithm}

The algorithm uses $\text{cost}[v]$ to store the cost of a shortest path from vertex $v$ 
to the source vertex $s$. $\text{cost}[s]$ is 0. Initially assign infinity to $\text{cost}[v]$ to 
indicate that no path is found from $v$ to $s$. Let $V$ denote all vertices in the graph 
and $T$ denote the set of the vertices whose costs are known. Initially, the source 
vertex $s$ is in $T$. The algorithm repeatedly finds a vertex $u$ in $T$ and a vertex $v$ 
in $V - T$ such that $\text{cost}[u] + w(u, v)$ is the smallest, and moves $v$ to $T$. 
The shortest path algorithm given in the text continually update the cost and 
parent for a vertex in $V - T$. This algorithm initializes the cost to infinity for 
each vertex and then changes the cost for a vertex only once when the vertex is 
added into $T$. Implement this algorithm and use Listing 29.7, TestShortestPath. 
java, to test your new algorithm.
(Find \(u\) with smallest \(\text{cost}[u]\) efficiently) The `getShortestPath` method finds a \(u\) with the smallest \(\text{cost}[u]\) using a linear search, which takes \(O(|V|)\). The search time can be reduced to \(O(\log |V|)\) using an AVL tree. Modify the method using an AVL tree to store the vertices in \(V - T\). Use Listing 29.7, TestShortestPath.java, to test your new implementation.

(Test if a vertex \(u\) is in \(T\) efficiently) Since \(T\) is implemented using a list in the `getMinimumSpanningTree` and `getShortestPath` methods in Listing 29.2 WeightedGraph.java, testing whether a vertex \(u\) is in \(T\) by invoking \(T.contains(u)\) takes \(O(n)\) time. Modify these two methods by introducing an array named `isInT`. Set \(\text{isInT}[u]\) to `true` when a vertex \(u\) is added to \(T\). Testing whether a vertex \(u\) is in \(T\) can now be done in \(O(1)\) time. Write a test program using the following code, where `graph1` is created from Figure 29.1.

```java
WeightedGraph<String> graph1 = new WeightedGraph<>(edges, vertices);
WeightedGraph<String>.MST tree1 = graph1.getMinimumSpanningTree();
System.out.println("Total weight is " + tree1.getTotalWeight());
tree1.printTree();
WeightedGraph<String>.ShortestPathTree tree2 =
    graph1.getShortestPath(graph1.getIndex("Chicago"));
tree2.printAllPaths();
```
Objectives

■ To get an overview of multithreading (§30.2).
■ To develop task classes by implementing the `Runnable` interface (§30.3).
■ To create threads to run tasks using the `Thread` class (§30.3).
■ To control threads using the methods in the `Thread` class (§30.4).
■ To control animations using threads and use `Platform.runLater` to run the code in the application thread (§30.5).
■ To execute tasks in a thread pool (§30.6).
■ To use synchronized methods or blocks to synchronize threads to avoid race conditions (§30.7).
■ To synchronize threads using locks (§30.8).
■ To facilitate thread communications using conditions on locks (§§30.9 and 30.10).
■ To use blocking queues (`ArrayBlockingQueue`, `LinkedBlockingQueue`, `PriorityBlockingQueue`) to synchronize access to a queue (§30.11).
■ To restrict the number of concurrent tasks that access a shared resource using semaphores (§30.12).
■ To use the resource-ordering technique to avoid deadlocks (§30.13).
■ To describe the life cycle of a thread (§30.14).
■ To create synchronized collections using the static methods in the `Collections` class (§30.15).
■ To develop parallel programs using the Fork/Join Framework (§30.16).
Chapter 30  Multithreading and Parallel Programming

30.1 Introduction

Multithreading enables multiple tasks in a program to be executed concurrently.

One of the powerful features of Java is its built-in support for multithreading—the concurrent running of multiple tasks within a program. In many programming languages, you have to invoke system-dependent procedures and functions to implement multithreading. This chapter introduces the concepts of threads and how multithreading programs can be developed in Java.

30.2 Thread Concepts

A program may consist of many tasks that can run concurrently. A thread is the flow of execution, from beginning to end, of a task.

A thread provides the mechanism for running a task. With Java, you can launch multiple threads from a program concurrently. These threads can be executed simultaneously in multi-processor systems, as shown in Figure 30.1a.

![Figure 30.1](a) Here multiple threads are running on multiple CPUs. (b) Here multiple threads share a single CPU.

In single-processor systems, as shown in Figure 30.1b, the multiple threads share CPU time, known as time sharing, and the operating system is responsible for scheduling and allocating resources to them. This arrangement is practical because most of the time the CPU is idle. It does nothing, for example, while waiting for the user to enter data.

Multithreading can make your program more responsive and interactive, as well as enhance performance. For example, a good word processor lets you print or save a file while you are typing. In some cases, multithreaded programs run faster than single-threaded programs even on single-processor systems. Java provides exceptionally good support for creating and running threads and for locking resources to prevent conflicts.

You can create additional threads to run concurrent tasks in the program. In Java, each task is an instance of the Runnable interface, also called a runnable object. A thread is essentially an object that facilitates the execution of a task.

30.1 Why is multithreading needed? How can multiple threads run simultaneously in a single-processor system?
30.2 What is a runnable object? What is a thread?

30.3 Creating Tasks and Threads

A task class must implement the Runnable interface. A task must be run from a thread.

Tasks are objects. To create tasks, you have to first define a class for tasks, which implements the Runnable interface. The Runnable interface is rather simple. All it contains is the run method. You need to implement this method to tell the system how your thread is going to run. A template for developing a task class is shown in Figure 30.2a.
30.3 Creating Tasks and Threads

Once you have defined a `TaskClass`, you can create a task using its constructor. For example,

```java
TaskClass task = new TaskClass(...);
```

A task must be executed in a thread. The `Thread` class contains the constructors for creating threads and many useful methods for controlling threads. To create a thread for a task, use

```java
Thread thread = new Thread(task);
```

You can then invoke the `start()` method to tell the JVM that the thread is ready to run, as follows:

```java
thread.start();
```

The JVM will execute the task by invoking the task’s `run()` method. Figure 30.2b outlines the major steps for creating a task, a thread, and starting the thread.

Listing 30.1 gives a program that creates three tasks and three threads to run them.

- The first task prints the letter `a` 100 times.
- The second task prints the letter `b` 100 times.
- The third task prints the integers 1 through 100.

When you run this program, the three threads will share the CPU and take turns printing letters and numbers on the console. Figure 30.3 shows a sample run of the program.

![Image of program output](image)

FIGURE 30.3 Tasks `printA`, `printB`, and `print100` are executed simultaneously to display the letter `a` 100 times, the letter `b` 100 times, and the numbers from 1 to 100.
List 30.1 TaskThreadDemo.java

```java
public class TaskThreadDemo {
    public static void main(String[] args) {
        // Create tasks
        Runnable printA = new PrintChar('a', 100);
        Runnable printB = new PrintChar('b', 100);
        Runnable print100 = new PrintNum(100);

        // Create threads
        Thread thread1 = new Thread(printA);
        Thread thread2 = new Thread(printB);
        Thread thread3 = new Thread(print100);

        // Start threads
        thread1.start();
        thread2.start();
        thread3.start();
    }
}
```

// The task for printing a character a specified number of times

class PrintChar implements Runnable {
    private char charToPrint; // The character to print
    private int times; // The number of times to repeat

    /** Construct a task with a specified character and number of */
    /** times to print the character */
    public PrintChar(char c, int t) {
        charToPrint = c;
        times = t;
    }

    @Override /** Override the run() method to tell the system */
    public void run() {
        for (int i = 0; i < times; i++) {
            System.out.print(charToPrint);
        }
    }
}

// The task class for printing numbers from 1 to n for a given n

class PrintNum implements Runnable {
    private int lastNum;

    /** Construct a task for printing 1, 2, ..., n */
    public PrintNum(int n) {
        lastNum = n;
    }

    @Override /** Tell the thread how to run */
    public void run() {
        for (int i = 1; i <= lastNum; i++) {
            System.out.print(" "+i);
        }
    }
}
```
The program creates three tasks (lines 4–6). To run them concurrently, three threads are created (lines 9–11). The start() method (lines 14–16) is invoked to start a thread that causes the run() method in the task to be executed. When the run() method completes, the thread terminates.

Because the first two tasks, printA and printB, have similar functionality, they can be defined in one task class PrintChar (lines 21–41). The PrintChar class implements Runnable and overrides the run() method (lines 36–40) with the print-character action. This class provides a framework for printing any single character a given number of times. The runnable objects, printA and printB, are instances of the PrintChar class.

The PrintNum class (lines 44–58) implements Runnable and overrides the run() method (lines 53–57) with the print-number action. This class provides a framework for printing numbers from 1 to n, for any integer n. The runnable object print100 is an instance of the class PrintNum class.

**Note**
If you don’t see the effect of these three threads running concurrently, increase the number of characters to be printed. For example, change line 4 to

Runnable printA = new PrintChar('a', 10000);

**Important Note**
The run() method in a task specifies how to perform the task. This method is automatically invoked by the JVM. You should not invoke it. Invoking run() directly merely executes this method in the same thread; no new thread is started.

30.3 How do you define a task class? How do you create a thread for a task?
30.4 What would happen if you replace the start() method with the run() method in lines 14–16 in Listing 30.1?

```java
Runnable print100 = new PrintChar('a', 10000);
```

30.5 What is wrong in the following two programs? Correct the errors.

(a)
```java
public class Test implements Runnable {
    public static void main(String[] args) {
        new Test();
    }

    public Test() {
        Test task = new Test();
        new Thread(task).start();
    }

    public void run() {
        System.out.println("test");
    }
}
```

(b)
```java
public class Test implements Runnable {
    public static void main(String[] args) {
        new Test();
    }

    public Test() {
        Thread t = new Thread(this);
        t.start();
        t.start();
    }

    public void run() {
        System.out.println("test");
    }
}
```
### 30.4 The Thread Class

The **Thread** class contains the constructors for creating threads for tasks and the methods for controlling threads.

Figure 30.4 shows the class diagram for the **Thread** class.

```
java.lang.Thread

+Thread()
+Thread(task: Runnable)
+start(): void
+isAlive(): boolean
+setPriority(p: int): void
+join(): void
+sleep(millis: long): void
+yield(): void
+interrupt(): void

FIGURE 30.4 The **Thread** class contains the methods for controlling threads.
```

**Note** Since the **Thread** class implements **Runnable**, you could define a class that extends **Thread** and implements the **run** method, as shown in Figure 30.5a, and then create an object from the class and invoke its **start** method in a client program to start the thread, as shown in Figure 30.5b.

```
// Custom thread class
public class CustomThread extends Thread {
  ...
  public void run() {
    // Tell system how to perform this task
    ...
  }

  // Create a thread
  CustomThread thread1 = new CustomThread(...);
  thread1.start();

  // Create another thread
  CustomThread thread2 = new CustomThread(...);
  thread2.start();

  // Client class
  public class Client {
    ...
    public void someMethod() {
      ...
    }

    // Create a thread
    CustomThread thread1 = new CustomThread(...);
    thread1.start();

    // Create another thread
    CustomThread thread2 = new CustomThread(...);
    thread2.start();
  }

FIGURE 30.5 Define a thread class by extending the **Thread** class.
```
This approach is, however, not recommended because it mixes the task and the mechanism of running the task. Separating the task from the thread is a preferred design.

**Note**
The Thread class also contains the `stop()`, `suspend()`, and `resume()` methods. As of Java 2, these methods were deprecated (or outdated) because they are known to be inherently unsafe. Instead of using the `stop()` method, you should assign `null` to a Thread variable to indicate that has stopped.

You can use the `yield()` method to temporarily release time for other threads. For example, suppose you modify the code in the `run()` method in lines 53–57 for `PrintNum` in Listing 30.1 as follows:

```java
public void run() {
    for (int i = 1; i <= lastNum; i++) {
        System.out.print(" "+i);
        Thread.yield();
    }
}
```

Every time a number is printed, the thread of the `print100` task is yielded to other threads.

The `sleep(long millis)` method puts the thread to sleep for a specified time in milliseconds to allow other threads to execute. For example, suppose you modify the code in lines 53–57 in Listing 30.1, as follows:

```java
public void run() {
    try {
        for (int i = 1; i <= lastNum; i++) {
            System.out.print(" "+i);
            if (i >= 50) Thread.sleep(1);
        }
    }
    catch (InterruptedException ex) {
        
    }
}
```

Every time a number (\(\geq 50\)) is printed, the thread of the `print100` task is put to sleep for 1 millisecond.

The `sleep` method may throw an `InterruptedException`, which is a checked exception. Such an exception may occur when a sleeping thread’s `interrupt()` method is called. The `interrupt()` method is very rarely invoked on a thread, so an `InterruptedException` is unlikely to occur. But since Java forces you to catch checked exceptions, you have to put it in a `try-catch` block. If a `sleep` method is invoked in a loop, you should wrap the loop in a `try-catch` block, as shown in (a) below. If the loop is outside the `try-catch` block, as shown in (b), the thread may continue to execute even though it is being interrupted.

```java
public void run() {
    try {
        while (...) {
            Thread.sleep(1000);
        }
    }
    catch (InterruptedException ex) {
        ex.printStackTrace();
    }
}
```

(a) correct

```java
public void run() {
    while (...) {
        try {
            ...
            Thread.sleep(sleepTime);
        }
    }
    catch (InterruptedException ex) {
        ex.printStackTrace();
    }
}
```

(b) Incorrect
You can use the `join()` method to force one thread to wait for another thread to finish. For example, suppose you modify the code in lines 53–57 in Listing 30.1 as follows:

```java
public void run() {
    Thread thread4 = new Thread(new PrintChar('c', 40));
    thread4.start();
    try {
        for (int i = 1; i <= lastNum; i++) {
            System.out.print(" "+i);
            if (i == 50) thread4.join();
        }
    } catch (InterruptedException ex) {
    }
}
```

A new `thread4` is created and it prints character `c` 40 times. The numbers from 50 to 100 are printed after thread `thread4` is finished.

Java assigns every thread a priority. By default, a thread inherits the priority of the thread that spawned it. You can increase or decrease the priority of any thread by using the `setPriority` method, and you can get the thread’s priority by using the `getPriority` method. Priorities are numbers ranging from 1 to 10. The `Thread` class has the `int` constants `MIN_PRIORITY`, `NORM_PRIORITY`, and `MAX_PRIORITY`, representing 1, 5, and 10, respectively. The priority of the main thread is `Thread.NORM_PRIORITY`.

The JVM always picks the currently runnable thread with the highest priority. A lower-priority thread can run only when no higher-priority threads are running. If all runnable threads have equal priorities, each is assigned an equal portion of the CPU time in a circular queue. This is called round-robin scheduling. For example, suppose you insert the following code in line 16 in Listing 30.1:

```java
thread3.setPriority(Thread.MAX_PRIORITY);
```

The thread for the `print100` task will be finished first.

**Tip**
The priority numbers may be changed in a future version of Java. To minimize the impact of any changes, use the constants in the `Thread` class to specify thread priorities.

**Tip**
A thread may never get a chance to run if there is always a higher-priority thread running or a same-priority thread that never yields. This situation is known as contention or starvation. To avoid contention, the thread with higher priority must periodically invoke the `sleep` or `yield` method to give a thread with a lower or the same priority a chance to run.

**Check Point**

30.6 Which of the following methods are instance methods in `java.lang.Thread`? Which method may throw an `InterruptedException`? Which of them are deprecated in Java?

- `run`, `start`, `stop`, `suspend`, `resume`, `sleep`, `interrupt`, `yield`, `join`

30.7 If a loop contains a method that throws an `InterruptedException`, why should the loop be placed inside a `try-catch` block?

30.8 How do you set a priority for a thread? What is the default priority?
30.5 Case Study: Flashing Text

You can use a thread to control an animation.

The use of a Timeline object to control animations was introduced in Section 15.11, Animation. Alternatively, you can also use a thread to control animation. Listing 30.2 gives an example that displays flashing text on a label, as shown in Figure 30.6.

![Figure 30.6 The text “Welcome” blinks.](image)

**Listing 30.2 FlashText.java**

```java
import javafx.application.Application;
import javafx.application.Platform;
import javafx.scene.Scene;
import javafx.scene.control.Label;
import javafx.scene.layout.StackPane;
import javafx.stage.Stage;

public class FlashText extends Application {
    private String text = "";

    @Override
    public void start(Stage primaryStage) {
        StackPane pane = new StackPane();
        Label lblText = new Label("Programming is fun");
        pane.getChildren().add(lblText);

        new Thread(new Runnable() {
            @Override
            public void run() {
                try {
                    while (true) {
                        if (lblText.getText().trim().length() == 0) {
                            text = "Welcome";
                        } else {
                            text = "";
                        }
                        Platform.runLater(new Runnable() {
                            @Override
                            public void run() {
                                lblText.setText(text);
                            }
                        });
                        Thread.sleep(200);
                    }
                } catch (InterruptedException ex) {
                }
            }
        }).start();
    }
}
```

Key Point

- **FIGURE 30.6** The text “Welcome” blinks.

- **LISTING 30.2 FlashText.java**

- import javafx.application.Application;
- import javafx.application.Platform;
- import javafx.scene.Scene;
- import javafx.scene.control.Label;
- import javafx.scene.layout.StackPane;
- import javafx.stage.Stage;

- public class FlashText extends Application {
  private String text = "";

- @Override
  public void start(Stage primaryStage) {
    StackPane pane = new StackPane();
    Label lblText = new Label("Programming is fun");
    pane.getChildren().add(lblText);

- new Thread(new Runnable() {
    @Override
    public void run() {
        try {
            while (true) {
                if (lblText.getText().trim().length() == 0) {
                    text = "Welcome";
                } else {
                    text = "";
                }
                Platform.runLater(new Runnable() {
                    @Override
                    public void run() {
                        lblText.setText(text);
                    }
                });
                Thread.sleep(200);
            }
        } catch (InterruptedException ex) {
        }
    }
}).start();
```
42    // Create a scene and place it in the stage
43    Scene scene = new Scene(pane, 200, 50);
44    primaryStage.setTitle("FlashText"); // Set the stage title
45    primaryStage.setScene(scene); // Place the scene in the stage
46    primaryStage.show(); // Display the stage
47    }
48    }

The program creates a Runnable object in an anonymous inner class (lines 17–40). This object is started in line 40 and runs continuously to change the text in the label. It sets a text in the label if the label is blank (line 23) and sets its text blank (line 25) if the label has a text. The text is set and unset to simulate a flashing effect.

JavaFX GUI is run from the JavaFX application thread. The flashing control is run from a separate thread. The code in a nonapplication thread cannot update GUI in the application thread. To update the text in the label, a new Runnable object is created in lines 27–32.

Invoking Platform.runLater(Runnable r) tells the system to run this Runnable object in the application thread.

The anonymous inner classes in this program can be simplified using lambda expressions as follows:

```java
new Thread(() -> { // lambda expression
    try {
        while (true) {
            if (lblText.getText().trim().length() == 0)
                text = "Welcome";
            else
                text = "";

            Platform.runLater(() -> lblText.setText(text)); // lambda exp

            Thread.sleep(200);
        }
    }
    catch (InterruptedException ex) {
    }
}).start();
```

30.9 What causes the text to flash?

30.10 Is an instance of FlashText a runnable object?

30.11 What is the purpose of using Platform.runLater?

30.12 Can you replace the code in lines 27–32 using the following code?

```java
Platform.runLater(e -> lblText.setText(text));
```

30.13 What happens if line 34 (Thread.sleep(200)) is not used?

30.6 Thread Pools

A thread pool can be used to execute tasks efficiently.

In Section 30.3, Creating Tasks and Threads, you learned how to define a task class by implementing java.lang.Runnable, and how to create a thread to run a task like this:

```java
Runnable task = new TaskClass(task);
new Thread(task).start();
```
This approach is convenient for a single task execution, but it is not efficient for a large number of tasks because you have to create a thread for each task. Starting a new thread for each task could limit throughput and cause poor performance. Using a thread pool is an ideal way to manage the number of tasks executing concurrently. Java provides the Executor interface for executing tasks in a thread pool and the ExecutorService interface for managing and controlling tasks. ExecutorService is a subinterface of Executor, as shown in Figure 30.7.

**Figure 30.7** The Executor interface executes threads, and the ExecutorService subinterface manages threads.

![Executor and ExecutorService Interfaces](image)

To create an Executor object, use the static methods in the Executors class, as shown in Figure 30.8. The newFixedThreadPool(int) method creates a fixed number of threads in a pool. If a thread completes executing a task, it can be reused to execute another task. If a thread terminates due to a failure prior to shutdown, a new thread will be created to replace it if all the threads in the pool are not idle and there are tasks waiting for execution. The newCachedThreadPool() method creates a new thread if all the threads in the pool are not idle and there are tasks waiting for execution. A thread in a cached pool will be terminated if it has not been used for 60 seconds. A cached pool is efficient for many short tasks.

![Executors Class](image)

Listing 30.3 shows how to rewrite Listing 30.1 using a thread pool.

**Listing 30.3** ExecutorDemo.java

```java
1 import java.util.concurrent.*;
2
3 public class ExecutorDemo {
```
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```java
public static void main(String[] args) {
    // Create a fixed thread pool with maximum three threads
    ExecutorService executor = Executors.newFixedThreadPool(3);

    // Submit runnable tasks to the executor
    executor.execute(new PrintChar('a', 100));
    executor.execute(new PrintChar('b', 100));
    executor.execute(new PrintNum(100));

    // Shut down the executor
    executor.shutdown();
}
```

Line 6 creates a thread pool executor with a total of three threads maximum. Classes `PrintChar` and `PrintNum` are defined in Listing 30.1. Line 9 creates a task, `new PrintChar('a', 100)`, and adds it to the pool. Similarly, another two runnable tasks are created and added to the same pool in lines 10 and 11. The executor creates three threads to execute three tasks concurrently.

Suppose that you replace line 6 with

```java
ExecutorService executor = Executors.newFixedThreadPool(1);
```

What will happen? The three runnable tasks will be executed sequentially because there is only one thread in the pool.

Suppose you replace line 6 with

```java
ExecutorService executor = Executors.newCachedThreadPool();
```

What will happen? New threads will be created for each waiting task, so all the tasks will be executed concurrently.

The `shutdown()` method in line 14 tells the executor to shut down. No new tasks can be accepted, but any existing tasks will continue to finish.

**Tip**

If you need to create a thread for just one task, use the `Thread` class. If you need to create threads for multiple tasks, it is better to use a thread pool.

**Check Point**

30.14  What are the benefits of using a thread pool?

30.15  How do you create a thread pool with three fixed threads? How do you submit a task to a thread pool? How do you know that all the tasks are finished?

30.7  Thread Synchronization

*Thread synchronization is to coordinate the execution of the dependent threads.*

A shared resource may become corrupted if it is accessed simultaneously by multiple threads. The following example demonstrates the problem.

Suppose you create and launch 100 threads, each of which adds a penny to an account. Define a class named `Account` to model the account, a class named `AddAPennyTask` to add a penny to the account, and a main class that creates and launches threads. The relationships of these classes are shown in Figure 30.9. The program is given in Listing 30.4.
LISTING 30.4 AccountWithoutSync.java

```java
import java.util.concurrent.*;

public class AccountWithoutSync {
    private static Account account = new Account();

    public static void main(String[] args) {
        ExecutorService executor = Executors.newCachedThreadPool();
        // Create and launch 100 threads
        for (int i = 0; i < 100; i++) {
            executor.execute(new AddAPennyTask());
        }
        executor.shutdown();
        // Wait until all tasks are finished
        while (!executor.isTerminated()) {
        }
        System.out.println("What is balance? " + account.getBalance());
    }

    // A thread for adding a penny to the account
    private static class AddAPennyTask implements Runnable {
        public void run() {
            account.deposit(1);
        }
    }

    // An inner class for account
    private static class Account {
        private int balance = 0;

        public int getBalance() {
            return balance;
        }

        public void deposit(int amount) {
            int newBalance = balance + amount;
            // This delay is deliberately added to magnify the
```

Figure 30.9 AccountWithoutSync contains an instance of Account and 100 threads of AddAPennyTask.
The classes AddAPennyTask and Account in lines 24–51 are inner classes. Line 4 creates an Account with initial balance 0. Line 11 creates a task to add a penny to the account and submits the task to the executor. Line 11 is repeated 100 times in lines 10–12. The program repeatedly checks whether all tasks are completed in lines 17 and 18. The account balance is displayed in line 20 after all tasks are completed.

The program creates 100 threads executed in a thread pool executor (lines 10–12). The isTerminated() method (line 17) is used to test whether the thread is terminated.

The balance of the account is initially 0 (line 32). When all the threads are finished, the balance should be 100 but the output is unpredictable. As can be seen in Figure 30.10, the answers are wrong in the sample run. This demonstrates the data-corruption problem that occurs when all the threads have access to the same data source simultaneously.

![Figure 30.10](image)

**Figure 30.10** The AccountWithoutSync program causes data inconsistency.

Lines 39–49 could be replaced by one statement:

```
balance = balance + amount;
```

It is highly unlikely, although plausible, that the problem can be replicated using this single statement. The statements in lines 39–49 are deliberately designed to magnify the data-corruption problem and make it easy to see. If you run the program several times but still do not see the problem, increase the sleep time in line 44. This will increase the chances for showing the problem of data inconsistency.

What, then, caused the error in this program? A possible scenario is shown in Figure 30.11.

```
<table>
<thead>
<tr>
<th>Step</th>
<th>Balance</th>
<th>Task 1</th>
<th>Task 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0</td>
<td>newBalance = balance + 1;</td>
<td>newBalance = balance + 1;</td>
</tr>
<tr>
<td>2</td>
<td>0</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>1</td>
<td>balance = newBalance;</td>
<td>balance = newBalance;</td>
</tr>
<tr>
<td>4</td>
<td>1</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
```

**Figure 30.11** Task 1 and Task 2 both add 1 to the same balance.
In Step 1, Task 1 gets the balance from the account. In Step 2, Task 2 gets the same balance from the account. In Step 3, Task 1 writes a new balance to the account. In Step 4, Task 2 writes a new balance to the account.

The effect of this scenario is that Task 1 does nothing because in Step 4 Task 2 overrides Task 1’s result. Obviously, the problem is that Task 1 and Task 2 are accessing a common resource in a way that causes a conflict. This is a common problem, known as a race condition, in multithreaded programs. A class is said to be thread-safe if an object of the class does not cause a race condition in the presence of multiple threads. As demonstrated in the preceding example, the Account class is not thread-safe.

30.7.1 The synchronized Keyword

To avoid race conditions, it is necessary to prevent more than one thread from simultaneously entering a certain part of the program, known as the critical region. The critical region in Listing 30.4 is the entire deposit method. You can use the keyword synchronized to synchronize the method so that only one thread can access the method at a time. There are several ways to correct the problem in Listing 30.4. One approach is to make Account thread-safe by adding the keyword synchronized in the deposit method in line 38, as follows:

```
public synchronized void deposit(double amount)
```

A synchronized method acquires a lock before it executes. A lock is a mechanism for exclusive use of a resource. In the case of an instance method, the lock is on the object for which the method was invoked. In the case of a static method, the lock is on the class. If one thread invokes a synchronized instance method (respectively, static method) on an object, the lock of that object (respectively, class) is acquired first, then the method is executed, and finally the lock is released. Another thread invoking the same method of that object (respectively, class) is blocked until the lock is released.

With the deposit method synchronized, the preceding scenario cannot happen. If Task 1 enters the method, Task 2 is blocked until Task 1 finishes the method, as shown in Figure 30.12.

![Figure 30.12](image)

**Figure 30.12** Task 1 and Task 2 are synchronized.

30.7.2 Synchronizing Statements

Invoking a synchronized instance method of an object acquires a lock on the object, and invoking a synchronized static method of a class acquires a lock on the class. A synchronized statement can be used to acquire a lock on any object, not just this object, when executing a
synchronized block

block of the code in a method. This block is referred to as a **synchronized block**. The general form of a synchronized statement is as follows:

```
synchronized (expr) {
    statements;
}
```

The expression `expr` must evaluate to an object reference. If the object is already locked by another thread, the thread is blocked until the lock is released. When a lock is obtained on the object, the statements in the synchronized block are executed and then the lock is released.

Synchronized statements enable you to synchronize part of the code in a method instead of the entire method. This increases concurrency. You can make Listing 30.4 thread-safe by placing the statement in line 26 inside a synchronized block:

```
synchronized (account) {
    account.deposit(1);
}
```

**Note**

Any synchronized instance method can be converted into a synchronized statement. For example, the following synchronized instance method in (a) is equivalent to (b):

(a)
```
public synchronized void xMethod() {
    // method body
}
```

(b)
```
public xMethod() {
    synchronized (this) {
        // method body
    }
}
```

**Check Point**

30.16 Give some examples of possible resource corruption when running multiple threads. How do you synchronize conflicting threads?

30.17 Suppose you place the statement in line 26 of Listing 30.4 inside a synchronized block to avoid race conditions, as follows:

```
synchronized (this) {
    account.deposit(1);
}
```

Will it work?

### 30.8 Synchronization Using Locks

*Locks and conditions can be explicitly used to synchronize threads.*

Recall that in Listing 30.4, 100 tasks deposit a penny to the same account concurrently, which causes conflicts. To avoid it, you use the `synchronized` keyword in the `deposit` method, as follows:

```
public synchronized void deposit(double amount)
```

A synchronized instance method implicitly acquires a **lock** on the instance before it executes the method.

Java enables you to acquire locks explicitly, which give you more control for coordinating threads. A lock is an instance of the `Lock` interface, which defines the methods for acquiring and releasing locks, as shown in Figure 30.13. A lock may also use the `newCondition()` method to create any number of **Condition** objects, which can be used for thread communications.
Synchronization Using Locks

ReentrantLock is a concrete implementation of Lock for creating mutually exclusive locks. You can create a lock with the specified fairness policy. True fairness policies guarantee that the longest-waiting thread will obtain the lock first. False fairness policies grant a lock to a waiting thread arbitrarily. Programs using fair locks accessed by many threads may have poorer overall performance than those using the default setting, but they have smaller variances in times to obtain locks and prevent starvation.

Listing 30.5 revises the program in Listing 30.7 to synchronize the account modification using explicit locks.

Listing 30.5 AccountWithSyncUsingLock.java

```java
import java.util.concurrent.*;
import java.util.concurrent.locks.*;

public class AccountWithSyncUsingLock {
    private static Account account = new Account();

    public static void main(String[] args) {
        ExecutorService executor = Executors.newCachedThreadPool();

        // Create and launch 100 threads
        for (int i = 0; i < 100; i++) {
            executor.execute(new AddAPennyTask());
        }

        executor.shutdown();

        // Wait until all tasks are finished
        while (!executor.isTerminated()) {
        }

        System.out.println("What is balance? " + account.getBalance());
    }

    // A thread for adding a penny to the account
    public static class AddAPennyTask implements Runnable {
        public void run() {
            account.deposit(1);
        }
    }
}
```

ReentrantLock is a concrete implementation of Lock for creating mutually exclusive locks.
// An inner class for Account
public static class Account {
    private static Lock lock = new ReentrantLock(); // Create a lock
    private int balance = 0;
    public int getBalance() {
        return balance;
    }
    public void deposit(int amount) {
        lock.lock(); // Acquire the lock
        int newBalance = balance + amount;
        // This delay is deliberately added to magnify the
        // data-corruption problem and make it easy to see.
        Thread.sleep(5);
        balance = newBalance;
        } catch (InterruptedException ex) {
        } finally {
        lock.unlock(); // Release the lock
        }
    }
}

Line 33 creates a lock, line 41 acquires the lock, and line 55 releases the lock.

It is a good practice to always immediately follow a call to lock() with a try-catch block and release the lock in the finally clause, as shown in lines 41–56, to ensure that the lock is always released.

Listing 30.5 can be implemented using a synchronize method for deposit rather than using a lock. In general, using synchronized methods or statements is simpler than using explicit locks for mutual exclusion. However, using explicit locks is more intuitive and flexible to synchronize threads with conditions, as you will see in the next section.

How do you create a lock object? How do you acquire a lock and release a lock?

30.9 Cooperation among Threads

Conditions on locks can be used to coordinate thread interactions.

Thread synchronization suffices to avoid race conditions by ensuring the mutual exclusion of multiple threads in the critical region, but sometimes you also need a way for threads to cooperate. Conditions can be used to facilitate communications among threads. A thread can specify what to do under a certain condition. Conditions are objects created by invoking the newCondition() method on a Lock object. Once a condition is created, you can use its await(), signal(), and signalAll() methods for thread communications, as shown in Figure 30.14. The await() method causes the current thread to wait until the condition is signaled. The signal() method wakes up one waiting thread, and the signalAll() method wakes all waiting threads.
Let us use an example to demonstrate thread communications. Suppose that you create and launch two tasks: one that deposits into an account and one that withdraws from the same account. The withdraw task has to wait if the amount to be withdrawn is more than the current balance. Whenever new funds are deposited into the account, the deposit task notifies the withdraw thread to resume. If the amount is still not enough for a withdrawal, the withdraw thread has to continue to wait for a new deposit.

To synchronize the operations, use a lock with a condition: `newDeposit` (i.e., new deposit added to the account). If the balance is less than the amount to be withdrawn, the withdraw task will wait for the `newDeposit` condition. When the deposit task adds money to the account, the task signals the waiting withdraw task to try again. The interaction between the two tasks is shown in Figure 30.15.

You create a condition from a `Lock` object. To use a condition, you have to first obtain a lock. The `await()` method causes the thread to wait and automatically releases the lock on the condition. Once the condition is right, the thread reacquires the lock and continues executing.

Assume that the initial balance is 0 and the amount to deposit and withdraw are randomly generated. Listing 30.6 gives the program. A sample run of the program is shown in Figure 30.16.

*Figure 30.14* The *Condition* interface defines the methods for performing synchronization.

*Figure 30.15* The condition *newDeposit* is used for communications between the two threads.

*Figure 30.16* The withdraw task waits if there are not sufficient funds to withdraw.
```java
public class ThreadCooperation {
    private static Account account = new Account();

    public static void main(String[] args) {
        // Create a thread pool with two threads
        ExecutorService executor = Executors.newFixedThreadPool(2);
        executor.execute(new DepositTask());
        executor.execute(new WithdrawTask());
        executor.shutdown();

        System.out.println("Thread 1\tThread 2\tBalance");
    }

    public static class DepositTask implements Runnable {
        @Override // Keep adding an amount to the account
        public void run() {
            try {// Purposely delay it to let the withdraw method proceed
                while (true) {
                    account.deposit((int)(Math.random() * 10) + 1);
                    Thread.sleep(1000);
                }
            } catch (InterruptedException ex) {
                ex.printStackTrace();
            }
        }
    }

    public static class WithdrawTask implements Runnable {
        @Override // Keep subtracting an amount from the account
        public void run() {
            while (true) {
                account.withdraw((int)(Math.random() * 10) + 1);
            }
        }
    }

    // An inner class for account
    private static class Account {
        // Create a new lock
        private static Lock lock = new ReentrantLock();

        // Create a condition
        private static Condition newDeposit = lock.newCondition();

        private int balance = 0;

        public int getBalance() {
            return balance;
        }

        public void withdraw(int amount) {
            lock.lock(); // Acquire the lock
            try {
                while (balance < amount) {
                    // Lock is acquired to prevent race conditions
                    balance = 0;
                    lock.unlock(); // Release the lock
                    lock.lock(); // Re-acquire the lock
                }
            } finally {
                lock.unlock(); // Always release the lock
            }
        }
    }
}
```

The code snippet demonstrates how to create two threads to deposit and withdraw funds from an account. It uses a `ReentrantLock` to synchronize access to the account balance. The `DepositTask` thread deposits random amounts into the account, while the `WithdrawTask` thread withdraws random amounts. Both tasks are executed concurrently using an ExecutorService with a fixed thread pool of size 2. The account balance is printed out at the end of the main method to show the final balance after both tasks have completed.
30.9 Cooperation among Threads

```java
30.9 Cooperation among Threads

59          System.out.println("\t\t\tWait for a deposit");
60          newDeposit.await();
61          }
62
63          balance -= amount;
64          System.out.println("\t\t\tWithdraw " + amount + 
65          "\t\t" + getBalance());
66          }
67          catch (InterruptedException ex) {
68              ex.printStackTrace();
69          }
70          finally {
71              lock.unlock(); // Release the lock
72          }
73          }
74
75          public void deposit(int amount) {
76              lock.lock(); // Acquire the lock
77          try {
78                  balance += amount;
79                  System.out.println("Deposit " + amount + 
80                  "\t\t\t\t" + getBalance());
81                  // Signal thread waiting on the condition
82                  newDeposit.signalAll();
83          }
84          finally {
85                  lock.unlock(); // Release the lock
86          }
87          }
88          }
89          }
90          }
```

The example creates a new inner class named `Account` to model the account with two methods, `deposit(int)` and `withdraw(int)`, a class named `DepositTask` to add an amount to the balance, a class named `WithdrawTask` to withdraw an amount from the balance, and a main class that creates and launches two threads.

The program creates and submits the deposit task (line 10) and the withdraw task (line 11). The deposit task is purposely put to sleep (line 23) to let the withdraw task run. When there are not enough funds to withdraw, the withdraw task waits (line 59) for notification of the balance change from the deposit task (line 83).

A lock is created in line 44. A condition named `newDeposit` on the lock is created in line 47. A condition is bound to a lock. Before waiting or signaling the condition, a thread must first acquire the lock for the condition. The withdraw task acquires the lock in line 56, waits for the `newDeposit` condition (line 60) when there is not a sufficient amount to withdraw, and releases the lock in line 71. The deposit task acquires the lock in line 76 and signals all waiting threads (line 83) for the `newDeposit` condition after a new deposit is made.

What will happen if you replace the `while` loop in lines 58–61 with the following `if` statement?

```java
if (balance < amount) {
    System.out.println("\t\t\tWait for a deposit");
    newDeposit.await();
}
```

The deposit task will notify the withdraw task whenever the balance changes. `(balance < amount)` may still be true when the withdraw task is awakened. Using the `if`
statement may lead to an incorrect withdraw. Using the loop statement, the withdraw task will have a chance to recheck the condition before performing a withdraw.

**Caution**

Once a thread invokes `await()` on a condition, the thread waits for a signal to resume. If you forget to call `signal()` or `signalAll()` on the condition, the thread will wait forever.

**Caution**

A condition is created from a `Lock` object. To invoke its method (e.g., `await()`, `signal()`, and `signalAll()`), you must first own the lock. If you invoke these methods without acquiring the lock, an `IllegalMonitorStateException` will be thrown.

Locks and conditions were introduced in Java 5. Prior to Java 5, thread communications were programmed using the object’s built-in monitors. Locks and conditions are more powerful and flexible than the built-in monitor, so you will not need to use monitors. However, if you are working with legacy Java code, you may encounter Java’s built-in monitor.

A *monitor* is an object with mutual exclusion and synchronization capabilities. Only one thread can execute a method at a time in the monitor. A thread enters the monitor by acquiring a lock on it and exits by releasing the lock. *Any object can be a monitor*. An object becomes a monitor once a thread locks it. Locking is implemented using the `synchronized` keyword on a method or a block. A thread must acquire a lock before executing a synchronized method or block. A thread can wait in a monitor if the condition is not right for it to continue executing in the monitor. You can invoke the `wait()` method on the monitor object to release the lock so that some other thread can get in the monitor and perhaps change the monitor’s state. When the condition is right, the other thread can invoke the `notify()` or `notifyAll()` method to signal one or all waiting threads to regain the lock and resume execution. The template for invoking these methods is shown in Figure 30.17.

```java
synchronized (anObject) {
    try {
        // Wait for the condition to become true
        while (!condition)
            anObject.wait();

        // Do something when condition is true
    } catch (InterruptedException ex) {
        ex.printStackTrace();
    }
}
```

```java
synchronized (anObject) {
    // When condition becomes true
    anObject.notify(); or anObject.notifyAll();
    ...
}
```

**FIGURE 30.17** The `wait()`, `notify()`, and `notifyAll()` methods coordinate thread communication.

The `wait()`, `notify()`, and `notifyAll()` methods must be called in a synchronized method or a synchronized block on the receiving object of these methods. Otherwise, an `IllegalMonitorStateException` will occur.

When `wait()` is invoked, it pauses the thread and simultaneously releases the lock on the object. When the thread is restarted after being notified, the lock is automatically reacquired.

The `wait()`, `notify()`, and `notifyAll()` methods on an object are analogous to the `await()`, `signal()`, and `signalAll()` methods on a condition.
30.19 How do you create a condition on a lock? What are the `await()`, `signal()`, and `signalAll()` methods for?

30.20 What would happen if the `while` loop in line 58 of Listing 30.6 was changed to an `if` statement?

Replaced by: `if (balance < amount)`

30.21 Why does the following class have a syntax error?

```java
public class Test implements Runnable {
    public static void main(String[] args) {
        new Test();
    }

    public Test() throws InterruptedException {
        Thread thread = new Thread(this);
        thread.sleep(1000);
    }

    public synchronized void run() {
    }
}
```

30.22 What is a possible cause for `IllegalMonitorStateException`?

30.23 Can the `wait()`, `notify()`, and `notifyAll()` be invoked from any object? What is the purpose of these methods?

30.24 What is wrong in the following code?

```java
synchronized (object1) {
    try {
        while (!condition) object2.wait();
    } catch (InterruptedException ex) {
    }
}
```

30.10 Case Study: Producer/Consumer

This section gives the classic Consumer/Producer example for demonstrating thread coordination.

Suppose you use a buffer to store integers and that the buffer size is limited. The buffer provides the method `write(int)` to add an `int` value to the buffer and the method `read()` to read and delete an `int` value from the buffer. To synchronize the operations, use a lock with two conditions: `notEmpty` (i.e., the buffer is not empty) and `notFull` (i.e., the buffer is not full). When a task adds an `int` to the buffer, if the buffer is full, the task will wait for the `notFull` condition. When a task reads an `int` from the buffer, if the buffer is empty, the task will wait for the `notEmpty` condition. The interaction between the two tasks is shown in Figure 30.18.

Listing 30.7 presents the complete program. The program contains the `Buffer` class (lines 50–101) and two tasks for repeatedly adding and consuming numbers to and from the buffer (lines 16–47). The `write(int)` method (lines 62–79) adds an integer to the buffer. The `read()` method (lines 81–100) deletes and returns an integer from the buffer.
The buffer is actually a first-in, first-out queue (lines 52–53). The conditions notEmpty and notFull on the lock are created in lines 59–60. The conditions are bound to a lock. A lock must be acquired before a condition can be applied. If you use the wait() and notify() methods to rewrite this example, you have to designate two objects as monitors.

**LISTING 30.7  ConsumerProducer.java**

```java
import java.util.concurrent.*;
import java.util.concurrent.locks.*;

public class ConsumerProducer {

private static Buffer buffer = new Buffer();

public static void main(String[] args) {
    // Create a thread pool with two threads
    ExecutorService executor = Executors.newFixedThreadPool(2);
    executor.execute(new ProducerTask());
    executor.execute(new ConsumerTask());
    executor.shutdown();
}

// A task for adding an int to the buffer
private static class ProducerTask implements Runnable {
    public void run() {
        try {
            int i = 1;
            while (true) {
                System.out.println("Producer writes " + i);
                buffer.write(i++); // Add a value to the buffer
                // Put the thread into sleep
                Thread.sleep((int)(Math.random() * 10000));
            }
        }
        catch (InterruptedException ex) {
            ex.printStackTrace();
        }
    }
}

// A task for deleting an int from the buffer
private static class ConsumerTask implements Runnable {
    public void run() {
        while (true) {
            try {
                int i = buffer.read();
                System.out.println("Consumer reads " + i);
            }
            catch (InterruptedException ex) {
                ex.printStackTrace();
            }
        }
    }
}
```

**FIGURE 30.18** The conditions notFull and notEmpty are used to coordinate task interactions.
try {
    while (true) {
        System.out.println("Consumer reads "+ buffer.read());
        // Put the thread into sleep
        Thread.sleep((int)(Math.random() * 10000));
    }
}

catch (InterruptedException ex) {
    ex.printStackTrace();
}

// An inner class for buffer
private static class Buffer {
    private static final int CAPACITY = 1; // buffer size
    private java.util.LinkedList<Integer> queue =
        new java.util.LinkedList<>();

    // Create a new lock
    private static Lock lock = new ReentrantLock();

    // Create two conditions
    private static Condition notEmpty = lock.newCondition();
    private static Condition notFull = lock.newCondition();

    public void write(int value) {
        lock.lock(); // Acquire the lock
        try {
            while (queue.size() == CAPACITY) {
                System.out.println("Wait for notFull condition");
                notFull.await();
            }
            queue.offer(value);
            notFull.signal(); // Signal notFull condition
        }
        catch (InterruptedException ex) {
            ex.printStackTrace();
        }
        finally {
            lock.unlock(); // Release the lock
        }
    }

    public int read() {
        int value = 0;
        lock.lock(); // Acquire the lock
        try {
            while (queue.isEmpty()) {
                System.out.println("Wait for notEmpty condition");
                notEmpty.await();
            }
            value = queue.remove();
            notFull.signal(); // Signal notFull condition
        }
        catch (InterruptedException ex) {
            ex.printStackTrace();
        }
    }
}
release the lock

```java
finally {
    lock.unlock(); // Release the lock
    return value;
}
```

A sample run of the program is shown in Figure 30.19.

**Figure 30.19**  Locks and conditions are used for communications between the Producer and Consumer threads.

**Check Point**

30.25 Can the read and write methods in the Buffer class be executed concurrently?
30.26 When invoking the read method, what happens if the queue is empty?
30.27 When invoking the write method, what happens if the queue is full?

### 30.11 Blocking Queues

*Java Collections Framework provides ArrayBlockingQueue, LinkedBlockingQueue, and PriorityBlockingQueue for supporting blocking queues.*

Queues and priority queues are introduced in Section 20.9. A **blocking queue** causes a thread to block when you try to add an element to a full queue or to remove an element from an empty queue. The **BlockingQueue** interface extends **java.util.Queue** and provides the synchronized **put** and **take** methods for adding an element to the tail of the queue and for removing an element from the head of the queue, as shown in Figure 30.20.

**Figure 30.20**  **BlockingQueue** is a subinterface of **Queue**.
Three concrete blocking queues—`ArrayBlockingQueue`, `LinkedBlockingQueue`, and `PriorityBlockingQueue`—are provided in Java, as shown in Figure 30.21. All are in the `java.util.concurrent` package. `ArrayBlockingQueue` implements a blocking queue using an array. You have to specify a capacity or an optional fairness to construct an `ArrayBlockingQueue`. `LinkedBlockingQueue` implements a blocking queue using a linked list. You can create an unbounded or bounded `LinkedBlockingQueue`. `PriorityBlockingQueue` is a priority queue. You can create an unbounded or bounded priority queue.

![Figure 30.21 ArrayBlockingQueue, LinkedBlockingQueue, and PriorityBlockingQueue are concrete blocking queues.](image)

**Note**

The `put` method will never block an unbounded `LinkedBlockingQueue` or `PriorityBlockingQueue`.

Listing 30.8 gives an example of using an `ArrayBlockingQueue` to simplify the Consumer/Producer example in Listing 30.10. Line 5 creates an `ArrayBlockingQueue` to store integers. The Producer thread puts an integer into the queue (line 22), and the Consumer thread takes an integer from the queue (line 38).

**Listing 30.8 ConsumerProducerUsingBlockingQueue.java**

```java
1 import java.util.concurrent.*;
2
3 public class ConsumerProducerUsingBlockingQueue {
4    private static ArrayBlockingQueue<Integer> buffer =
5        new ArrayBlockingQueue<> (2);  // create a buffer
6
7    public static void main(String[] args) {
8        // Create a thread pool with two threads
9        ExecutorService executor = Executors.newFixedThreadPool(2);  // create two threads
10       executor.execute(new ProducerTask());
11       executor.execute(new ConsumerTask());
12       executor.shutdown();
13    }
14
15    // A task for adding an int to the buffer
16    private static class ProducerTask implements Runnable {
17        public void run() {
18            try {
19                    int i = 1;
20                    while (true) {
21                        System.out.println("Producer writes " + i);
22                        buffer.put(i++);  // Add any value to the buffer, say, 1
23                        // Put the thread into sleep
24                    }
25                    return;
26                }
27            } catch (InterruptedException e) {
28                e.printStackTrace();
29            }
30        }
31    }
```

**Listing 30.8 ConsumerProducerUsingBlockingQueue.java**

```java
1 import java.util.concurrent.*;
2
3 public class ConsumerProducerUsingBlockingQueue {
4    private static ArrayBlockingQueue<Integer> buffer =
5        new ArrayBlockingQueue<> (2);  // create a buffer
6
7    public static void main(String[] args) {
8        // Create a thread pool with two threads
9        ExecutorService executor = Executors.newFixedThreadPool(2);  // create two threads
10       executor.execute(new ProducerTask());
11       executor.execute(new ConsumerTask());
12       executor.shutdown();
13    }
14
15    // A task for adding an int to the buffer
16    private static class ProducerTask implements Runnable {
17        public void run() {
18            try {
19                    int i = 1;
20                    while (true) {
21                        System.out.println("Producer writes " + i);
22                        buffer.put(i++);  // Add any value to the buffer, say, 1
23                        // Put the thread into sleep
24                    }
25                    return;
26                }
27            } catch (InterruptedException e) {
28                e.printStackTrace();
29            }
30        }
31    }
```
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```java
24        Thread.sleep((int)(Math.random() * 10000));
25    }
26    }
27          catch (InterruptedException ex) {
28              ex.printStackTrace();
29          }
30    }
31    }
32
33 // A task for reading and deleting an int from the buffer
34 public static class ConsumerTask implements Runnable {
35    public void run() {
36        try {
37            while (true) {
38                System.out.println("\t\t\tConsumer reads " + buffer.take());
39                // Put the thread into sleep
40                Thread.sleep((int)(Math.random() * 10000));
41            }
42        }
43          catch (InterruptedException ex) {
44              ex.printStackTrace();
45          }
46    }
47    }
48 }
```

In Listing 30.7, you used locks and conditions to synchronize the Producer and Consumer threads. This program does not use locks and conditions, because synchronization is already implemented in `ArrayBlockingQueue`.

### Check Point

**30.28** What is a blocking queue? What blocking queues are supported in Java?

**30.29** What method do you use to add an element to an `ArrayBlockingQueue`? What happens if the queue is full?

**30.30** What method do you use to retrieve an element from an `ArrayBlockingQueue`? What happens if the queue is empty?

### 30.12 Semaphores

Semaphores can be used to restrict the number of threads that access a shared resource.

In computer science, a **semaphore** is an object that controls the access to a common resource. Before accessing the resource, a thread must acquire a permit from the semaphore. After finishing with the resource, the thread must return the permit back to the semaphore, as shown in Figure 30.22.

![Figure 30.22](image-url)

A limited number of threads can access a shared resource controlled by a semaphore.
To create a semaphore, you have to specify the number of permits with an optional fairness policy, as shown in Figure 30.23. A task acquires a permit by invoking the semaphore’s `acquire()` method and releases the permit by invoking the semaphore’s `release()` method. Once a permit is acquired, the total number of available permits in a semaphore is reduced by 1. Once a permit is released, the total number of available permits in a semaphore is increased by 1.

```java
java.util.concurrent.Semaphore
+Semaphore(numberOfPermits: int)
+Semaphore(numberOfPermits: int, fair: boolean)
+acquire(): void
+release(): void
```

This creates a semaphore with the specified number of permits. The fairness policy is false. It creates a semaphore with the specified number of permits and the fairness policy. It acquires a permit from this semaphore. If no permit is available, the thread is blocked until one is available. It releases a permit back to the semaphore.

Figure 30.23 The Semaphore class contains the methods for accessing a semaphore.

A semaphore with just one permit can be used to simulate a mutually exclusive lock. Listing 30.9 revises the Account inner class in Listing 30.9 using a semaphore to ensure that only one thread at a time can access the deposit method.

### Listing 30.9 New Account Inner Class

```java
// An inner class for Account
private static class Account {
    // Create a semaphore
    private static Semaphore semaphore = new Semaphore(1);  // create a semaphore

    private int balance = 0;

    public int getBalance() {
        return balance;
    }

    public void deposit(int amount) {
        try {
            semaphore.acquire(); // Acquire a permit
            int newBalance = balance + amount;
            // This delay is deliberately added to magnify the
            // data-corruption problem and make it easy to see
            Thread.sleep(5);
            balance = newBalance;
        } catch (InterruptedException ex) {
        }
        finally {
            semaphore.release(); // Release a permit
        }
    }
}
```

A semaphore with one permit is created in line 4. A thread first acquires a permit when executing the deposit method in line 13. After the balance is updated, the thread releases the permit in line 25. It is a good practice to always place the `release()` method in the `finally` clause to ensure that the permit is finally released even in the case of exceptions.
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30.31 What are the similarities and differences between a lock and a semaphore?

30.32 How do you create a semaphore that allows three concurrent threads? How do you acquire a semaphore? How do you release a semaphore?

30.13 Avoiding Deadlocks

Deadlocks can be avoided by using a proper resource ordering.

Sometimes two or more threads need to acquire the locks on several shared objects. This could cause a deadlock, in which each thread has the lock on one of the objects and is waiting for the lock on the other object. Consider the scenario with two threads and two objects, as shown in Figure 30.24. Thread 1 has acquired a lock on object1, and Thread 2 has acquired a lock on object2. Now Thread 1 is waiting for the lock on object2, and Thread 2 for the lock on object1. Each thread waits for the other to release the lock it needs and until that happens, neither can continue to run.

Deadlock is easily avoided by using a simple technique known as resource ordering. With this technique, you assign an order to all the objects whose locks must be acquired and ensure that each thread acquires the locks in that order. For the example in Figure 30.24, suppose that the objects are ordered as object1 and object2. Using the resource ordering technique, Thread 2 must acquire a lock on object1 first, then on object2. Once Thread 1 acquires a lock on object1, Thread 2 has to wait for a lock on object1. Thus, Thread 1 will be able to acquire a lock on object2 and no deadlock will occur.

30.33 What is a deadlock? How can you avoid deadlock?

30.14 Thread States

A thread state indicates the status of thread.

Tasks are executed in threads. Threads can be in one of five states: New, Ready, Running, Blocked, or Finished (see Figure 30.25).

When a thread is newly created, it enters the New state. After a thread is started by calling its start() method, it enters the Ready state. A ready thread is runnable but may not be running yet. The operating system has to allocate CPU time to it.

When a ready thread begins executing, it enters the Running state. A running thread can enter the Ready state if its given CPU time expires or its yield() method is called.
A thread can enter the *Blocked* state (i.e., become inactive) for several reasons. It may have invoked the `join()`, `sleep()`, or `wait()` method. It may be waiting for an I/O operation to finish. A blocked thread may be reactivated when the action inactivating it is reversed. For example, if a thread has been put to sleep and the sleep time has expired, the thread is reactivated and enters the *Ready* state.

Finally, a thread is *Finished* if it completes the execution of its `run()` method.

The `isAlive()` method is used to find out the state of a thread. It returns `true` if a thread is in the *Ready*, *Blocked*, or *Running* state; it returns `false` if a thread is new and has not started or if it is finished.

The `interrupt()` method interrupts a thread in the following way: If a thread is currently in the *Ready* or *Running* state, its interrupted flag is set; if a thread is currently blocked, it is awakened and enters the *Ready* state, and a `java.lang.InterruptedException` is thrown.

### 30.15 Synchronized Collections

*Java Collections Framework provides synchronized collections for lists, sets, and maps.*

The classes in the Java Collections Framework are not thread-safe; that is, their contents may become corrupted if they are accessed and updated concurrently by multiple threads. You can protect the data in a collection by locking the collection or by using synchronized collections.

The *Collections* class provides six static methods for wrapping a collection into a synchronized version, as shown in Figure 30.26. The collections created using these methods are called *synchronization wrappers*.

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>synchronizedCollection(c: Collection): Collection</code></td>
<td>Returns a synchronized collection.</td>
</tr>
<tr>
<td><code>synchronizedList(list: List): List</code></td>
<td>Returns a synchronized list from the specified list.</td>
</tr>
<tr>
<td><code>synchronizedMap(m: Map): Map</code></td>
<td>Returns a synchronized map from the specified map.</td>
</tr>
<tr>
<td><code>synchronizedSet(s: Set): Set</code></td>
<td>Returns a synchronized set from the specified set.</td>
</tr>
<tr>
<td><code>synchronizedSortedMap(s: SortedMap): SortedMap</code></td>
<td>Returns a synchronized sorted map from the specified sorted map.</td>
</tr>
<tr>
<td><code>synchronizedSortedSet(s: SortedSet): SortedSet</code></td>
<td>Returns a synchronized sorted set.</td>
</tr>
</tbody>
</table>

*Figure 30.26* You can obtain synchronized collections using the methods in the *Collections* class.
Invoking `synchronizedCollection(Collection c)` returns a new `Collection` object, in which all the methods that access and update the original collection `c` are synchronized. These methods are implemented using the `synchronized` keyword. For example, the `add` method is implemented like this:

```java
public boolean add(E o) {
    synchronized (this) {
        return c.add(o);
    }
}
```

Synchronized collections can be safely accessed and modified by multiple threads concurrently.

**Note**
The methods in `java.util.Vector`, `java.util.Stack`, and `java.util.Hashtable` are already synchronized. These are old classes introduced in JDK 1.0. Starting with JDK 1.5, you should use `java.util.ArrayList` to replace `Vector`, `java.util.LinkedList` to replace `Stack`, and `java.util.Map` to replace `Hashtable`. If synchronization is needed, use a synchronization wrapper.

The synchronization wrapper classes are thread-safe, but the iterator is *fail-fast*. This means that if you are using an iterator to traverse a collection while the underlying collection is being modified by another thread, then the iterator will immediately fail by throwing `java.util.ConcurrentModificationException`, which is a subclass of `RuntimeException`. To avoid this error, you need to create a synchronized collection object and acquire a lock on the object when traversing it. For example, to traverse a set, you have to write the code like this:

```java
Set hashSet = Collections.synchronizedSet(new HashSet());

synchronized (hashSet) { // Must synchronize it
    Iterator iterator = hashSet.iterator();
    while (iterator.hasNext()) {
        System.out.println(iterator.next());
    }
}
```

Failure to do so may result in nondeterministic behavior, such as a `ConcurrentModificationException`.

**30.35** What is a synchronized collection? Is `ArrayList` synchronized? How do you make it synchronized?

**30.36** Explain why an iterator is fail-fast.

### 30.16 Parallel Programming

*The Fork/Join Framework is used for parallel programming in Java.*

The widespread use of multicore systems has created a revolution in software. In order to benefit from multiple processors, software needs to run in parallel. JDK 7 introduces the new Fork/Join Framework for parallel programming, which utilizes the multicore processors.

The Fork/Join Framework is illustrated in Figure 30.27 (the diagram resembles a fork, hence its name). A problem is divided into nonoverlapping subproblems, which can be solved independently in parallel. The solutions to all subproblems are then joined to obtain an overall solution for the problem. This is the parallel implementation of the divide-and-conquer approach. In JDK 7’s Fork/Join Framework, a *fork* can be viewed as an independent task that runs on a thread.
The framework defines a task using the `ForkJoinTask` class, as shown in Figure 30.28 and executes a task in an instance of `ForkJoinPool`, as shown in Figure 30.29.

**Figure 30.27** The nonoverlapping subproblems are solved in parallel.

**Figure 30.28** The `ForkJoinTask` class defines a task for asynchronous execution.

**Figure 30.29** The `ForkJoinPool` executes Fork/Join tasks.

---

### Java Code Snippet

```java
import java.util.concurrent.Future;
import java.util.concurrent.ForkJoinPool;
import java.util.concurrent.ForkJoinTask;
import java.util.concurrent.ExecutorService;
import java.util.concurrent.RecursiveAction;
import java.util.concurrent.RecursiveTask;

// interface java.util.concurrent.Future<V>
public interface Future<V> {
    boolean cancel(boolean interrupt);
    V get();
    boolean isDone();
}

// interface java.util.concurrent.ExecutorService
public interface ExecutorService {
    ForkJoinPool forkJoinPool();
    ForkJoinPool forkJoinPool(int parallelism);
    V invoke(ForkJoinTask<T>);
    void invokeAll(ForkJoinTask<?>...);
}

// interface java.util.concurrent.ForkJoinPool
public interface ForkJoinPool {
    ForkJoinPool();
    ForkJoinPool(parallelism: int);
    T invoke(ForkJoinTask<T>);
    void invokeAll(ForkJoinTask<?>...);
}

// interface java.util.concurrent.RecursiveAction<V>
public interface RecursiveAction<V> {
    void compute();
}

// interface java.util.concurrent.RecursiveTask<V>
public interface RecursiveTask<V> {
    V compute();
}
```

---

**Description**

- `Future<V>` interface defines methods for canceling a task, waiting for completion, and getting the result.
- `ExecutorService` interface provides methods to create and manage `ForkJoinPool` instances.
- `ForkJoinPool` creates instances of `ForkJoinTask` to perform tasks asynchronously.
- `RecursiveAction` and `RecursiveTask` interfaces define how tasks are performed and return the result upon completion.

---

**Notes**

- `Future<V>` attempts to cancel a task, waits if needed for computation to complete, and returns the result.
- `ForkJoinPool` creates instances of `ForkJoinTask` from runnable tasks, arranges asynchronous execution, and returns the result when it is done.
- `RecursiveTask<V>` defines how a task is performed and returns the value after completion.
- `RecursiveAction<V>` defines how a task is performed and is executed without returning a result.

---

**Figure 30.27** The nonoverlapping subproblems are solved in parallel.

**Figure 30.28** The `ForkJoinTask` class defines a task for asynchronous execution.

**Figure 30.29** The `ForkJoinPool` executes Fork/Join tasks.
ForkJoinTask is the abstract base class for tasks. A ForkJoinTask is a thread-like entity, but it is much lighter than a normal thread because huge numbers of tasks and sub-tasks can be executed by a small number of actual threads in a ForkJoinPool. The tasks are primarily coordinated using fork() and join(). Invoking fork() on a task arranges asynchronous execution, and invoking join() waits until the task is completed. The invoke() and invokeAll(tasks) methods implicitly invoke fork() to execute the task and join() to wait for the tasks to complete, and return the result, if any. Note that the static method invokeAll takes a variable number of ForkJoinTask arguments using the ... syntax, which is introduced in Section 7.9.

The ForkJoin Framework is designed to parallelize divide-and-conquer solutions, which are naturally recursive. RecursiveAction and RecursiveTask are two subclasses of ForkJoinTask. To define a concrete task class, your class should extend RecursiveAction or RecursiveTask. RecursiveAction is for a task that doesn’t return a value, and RecursiveTask is for a task that does return a value. Your task class should override the compute() method to specify how a task is performed.

We now use a merge sort to demonstrate how to develop parallel programs using the Fork/Join Framework. The merge sort algorithm (introduced in Section 25.3) divides the array into two halves and applies a merge sort on each half recursively. After the two halves are sorted, the algorithm merges them. Listing 30.10 gives a parallel implementation of the merge sort algorithm and compares its execution time with a sequential sort.

LISTING 30.10  ParallelMergeSort.java

```java
import java.util.concurrent.RecursiveAction;
import java.util.concurrent.ForkJoinPool;

public class ParallelMergeSort {
    public static void main(String[] args) {
        final int SIZE = 7000000;
        int[] list1 = new int[SIZE];
        int[] list2 = new int[SIZE];

        for (int i = 0; i < list1.length; i++)
            list1[i] = list2[i] = (int)(Math.random() * 10000000);

        long startTime = System.currentTimeMillis();
        parallelMergeSort(list1); // Invoke parallel merge sort
        long endTime = System.currentTimeMillis();
        System.out.println("Parallel time with "+Runtime.getRuntime().availableProcessors()+" processors is "+(endTime - startTime)+" milliseconds");

        startTime = System.currentTimeMillis();
        MergeSort.mergeSort(list2); // MergeSort is in Listing 23.5
        endTime = System.currentTimeMillis();
        System.out.println("Sequential time is "+(endTime - startTime)+" milliseconds");
    }

    public static void parallelMergeSort(int[] list) {
        RecursiveAction mainTask = new SortTask(list);
        ForkJoinPool pool = new ForkJoinPool();
        pool.invoke(mainTask);
    }

    private static class SortTask extends RecursiveAction {
        private final int THRESHOLD = 500;
    }
}
```
private int[] list;

SortTask(int[] list) {
    this.list = list;
}

@Override
protected void compute() {
    if (list.length < THRESHOLD)
        java.util.Arrays.sort(list);
    else {
        // Obtain the first half
        int[] firstHalf = new int[list.length / 2];
        System.arraycopy(list, 0, firstHalf, 0, list.length / 2);

        // Obtain the second half
        int secondHalfLength = list.length - list.length / 2;
        int[] secondHalf = new int[secondHalfLength];
        System.arraycopy(list, list.length / 2, secondHalf, 0, secondHalfLength);

        // Recursively sort the two halves
        invokeAll(new SortTask(firstHalf),
                  new SortTask(secondHalf));

        // Merge firstHalf with secondHalf into list
        MergeSort.merge(firstHalf, secondHalf, list);
    }
}

Parallel time with 2 processors is 2829 milliseconds
 Sequential time is 4751 milliseconds

Since the sort algorithm does not return a value, we define a concrete ForkJoinTask class by extending RecursiveAction (lines 33–64). The compute method is overridden to implement a recursive merge sort (lines 42–63). If the list is small, it is more efficient to be solved sequentially (line 44). For a large list, it is split into two halves (lines 47–54). The two halves are sorted concurrently (lines 57 and 58) and then merged (line 61).

The program creates a main ForkJoinTask (line 28), a ForkJoinPool (line 29), and places the main task for execution in a ForkJoinPool (line 30). The invoke method will return after the main task is completed.

When executing the main task, the task is split into subtasks and the subtasks are invoked using the invokeAll method (lines 57 and 58). The invokeAll method will return after all the subtasks are completed. Note that each subtask is further split into smaller tasks recursively. Huge numbers of subtasks may be created and executed in the pool. The Fork/Join Framework automatically executes and coordinates all the tasks efficiently.

The MergeSort class is defined in Listing 23.5. The program invokes MergeSort.merge to merge two sorted sublists (line 61). The program also invokes MergeSort.mergeSort (line 21) to sort a list using merge sort sequentially. You can see that the parallel sort is much faster than the sequential sort.

Note that the loop for initializing the list can also be parallelized. However, you should avoid using Math.random() in the code because it is synchronized and cannot be executed in parallel (see Programming Exercise 30.12). The parallelMergeSort method only sorts
an array of int values, but you can modify it to become a generic method (see Programming Exercise 30.13).

In general, a problem can be solved in parallel using the following pattern:

if (the program is small)
solve it sequentially;
else {
divide the problem into nonoverlapping subproblems;
solve the subproblems concurrently;
combine the results from subproblems to solve the whole problem;
}

Listing 30.11 develops a parallel method that finds the maximal number in a list.

**Listing 30.11 ParallelMax.java**

```java
import java.util.concurrent.*;

public class ParallelMax {
    public static void main(String[] args) {
        // Create a list
        final int N = 9000000;
        int[] list = new int[N];
        for (int i = 0; i < list.length; i++)
            list[i] = i;

        long startTime = System.currentTimeMillis();
        System.out.println("The maximal number is " + max(list));
        long endTime = System.currentTimeMillis();
        System.out.println("The number of processors is " +
            Runtime.getRuntime().availableProcessors());
        System.out.println("Time is " + (endTime - startTime) + " milliseconds");
    }

    public static int max(int[] list) {
        RecursiveTask<Integer> task = new MaxTask(list,
            0, list.length);
        ForkJoinPool pool = new ForkJoinPool();
        return pool.invoke(task);
    }

    private static class MaxTask extends RecursiveTask<Integer> {
        private final static int THRESHOLD = 1000;
        private int[] list;
        private int low;
        private int high;

        public MaxTask(int[] list, int low, int high) {
            this.list = list;
            this.low = low;
            this.high = high;
        }

        @Override
        public Integer compute() {
            if (high - low < THRESHOLD) {
                int max = list[0];
                for (int i = low; i < high; i++)
                    if (list[i] > max)
                        max = list[i];
                return new Integer(max);
            }
        }
    }
}
```

**invoke max**

**create a ForkJoinTask**

**create a ForkJoinPool**

**execute a task**

**define concrete ForkJoinTask**

**perform the task**

**solve a small problem**
Since the algorithm returns an integer, we define a task class for fork join by extending `RecursiveTask<Integer>` (lines 26–58). The `compute` method is overridden to return the maximal element in a list[low..high] (lines 39–57). If the list is small, it is more efficient to be solved sequentially (lines 40–46). For a large list, it is split into two halves (lines 48–50). The tasks `left` and `right` find the maximal element in the left half and right half, respectively. Invoking `fork()` on the task causes the task to be executed (lines 52 and 53). The `join()` method awaits for the task to complete and then returns the result (lines 54 and 55).

30.37 How do you define a ForkJoinTask? What are the differences between `RecursiveAction` and `RecursiveTask`?

30.38 How do you tell the system to execute a task?

30.39 What method can you use to test if a task has been completed?

30.40 How do you create a ForkJoinPool? How do you place a task into a ForkJoinPool?

### Key Terms

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### Chapter Summary

1. Each task is an instance of the `Runnable` interface. A `thread` is an object that facilitates the execution of a task. You can define a task class by implementing the `Runnable` interface and create a thread by wrapping a task using a `Thread` constructor.

2. After a thread object is created, use the `start()` method to start a thread, and the `sleep(long)` method to put a thread to sleep so that other threads get a chance to run.
3. A thread object never directly invokes the `run` method. The JVM invokes the `run` method when it is time to execute the thread. Your class must override the `run` method to tell the system what the thread will do when it runs.

4. To prevent threads from corrupting a shared resource, use `synchronized` methods or blocks. A `synchronized method` acquires a `lock` before it executes. In the case of an instance method, the lock is on the object for which the method was invoked. In the case of a static method, the lock is on the class.

5. A `synchronized statement` can be used to acquire a lock on any object, not just `this` object, when executing a block of the code in a method. This block is referred to as a `synchronized block`.

6. You can use explicit locks and `conditions` to facilitate communications among threads, as well as using the built-in monitor for objects.

7. The `blocking queues (ArrayBlockingQueue, LinkedBlockingQueue, PriorityBlockingQueue)` provided in the Java Collections Framework automatically synchronize access to a queue.

8. You can use semaphores to restrict the number of concurrent tasks that access a shared resource.

9. `Deadlock` occurs when two or more threads acquire locks on multiple objects and each has a lock on one object and is waiting for the lock on the other object. The `resource ordering technique` can be used to avoid deadlock.

10. The JDK 7’s Fork/Join Framework is designed for developing parallel programs. You can define a task class that extends `RecursiveAction` or `RecursiveTask` and execute the tasks concurrently in `ForkJoinPool` and obtains the overall solution after all tasks are completed.

**Quiz**

Answer the quiz for this chapter online at [www.cs.armstrong.edu/liang/intro10e/quiz.html](http://www.cs.armstrong.edu/liang/intro10e/quiz.html).

**PROGRAMMING EXERCISES**

Sections 30.1–30.5

*30.1 (Revise Listing 30.1) Rewrite Listing 30.1 to display the output in a text area, as shown in Figure 30.30.

![Figure 30.30](https://example.com/figure3030.png)

The output from three threads is displayed in a text area.
30.2 *(Racing cars)* Rewrite Programming Exercise 15.29 using a thread to control car racing. Compare the program with Programming Exercise 15.29 by setting the delay time to 10 in both programs. Which one runs the animation faster?

30.3 *(Raise flags)* Rewrite Listing 15.13 using a thread to animate a flag being raised. Compare the program with Listing 15.13 by setting the delay time to 10 in both programs. Which one runs the animation faster?

Sections 30.8–30.12

30.4 *(Synchronize threads)* Write a program that launches 1,000 threads. Each thread adds 1 to a variable `sum` that initially is 0. Define an `Integer` wrapper object to hold `sum`. Run the program with and without synchronization to see its effect.

30.5 *(Display a running fan)* Rewrite Programming Exercise 15.28 using a thread to control the fan animation.

30.6 *(Bouncing balls)* Rewrite Listing 15.17 BallPane.java using a thread to animate bouncing ball movements.

30.7 *(Control a clock)* Rewrite Programming Exercise 15.32 using a thread to control the clock animation.

30.8 *(Account synchronization)* Rewrite Listing 30.6, ThreadCooperation.java, using the object’s `wait()` and `notifyAll()` methods.

30.9 *(Demonstrate ConcurrentModificationException)* The iterator is fail-fast. Write a program to demonstrate it by creating two threads that concurrently access and modify a set. The first thread creates a hash set filled with numbers, and adds a new number to the set every second. The second thread obtains an iterator for the set and traverses the set back and forth through the iterator every second. You will receive a `ConcurrentModificationException` because the underlying set is being modified in the first thread while the set in the second thread is being traversed.

*30.10 *(Use synchronized sets)* Using synchronization, correct the problem in the preceding exercise so that the second thread does not throw a `ConcurrentModificationException`.

Section 30.15

*30.11 *(Demonstrate deadlock)* Write a program that demonstrates deadlock.

Section 30.18

*30.12 *(Parallel array initializer)* Implement the following method using the Fork/Join Framework to assign random values to the list.

```java
public static void parallelAssignValues(double[] list)
```

Write a test program that creates a list with 9,000,000 elements and invokes `parallelAssignValues` to assign random values to the list. Also implement a sequential algorithm and compare the execution time of the two. Note that if you use `Math.random()`, your parallel code execution time will be worse than the sequential code execution time because `Math.random()` is synchronized and cannot be executed in parallel. To fix this problem, create a `Random` object for assigning random values to a small list.
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30.13  *(Generic parallel merge sort)* Revise Listing 30.10, ParallelMergeSort.java, to define a generic `parallelMergeSort` method as follows:

```java
public static <E extends Comparable<E>> void parallelMergeSort(E[] list)
```

*30.14  *(Parallel quick sort)* Implement the following method in parallel to sort a list using quick sort (see Listing 23.7).

```java
public static void parallelQuickSort(int[] list)
```

Write a test program that times the execution time for a list of size 9,000,000 using this parallel method and a sequential method.

*30.15  *(Parallel sum)* Implement the following method using Fork/Join to find the sum of a list.

```java
public static double parallelSum(double[] list)
```

Write a test program that finds the sum in a list of 9,000,000 double values.

*30.16  *(Parallel matrix addition)* Programming Exercise 8.5 describes how to perform matrix addition. Suppose you have multiple processors, so you can speed up the matrix addition. Implement the following method in parallel.

```java
public static double[][] parallelAddMatrix(
    double[][] a, double[][] b)
```

Write a test program that measures the execution time for adding two 2,000 × 2,000 matrices using the parallel method and sequential method, respectively.

*30.17  *(Parallel matrix multiplication)* Programming Exercise 7.6 describes how to perform matrix multiplication. Suppose you have multiple processors, so you can speed up the matrix multiplication. Implement the following method in parallel.

```java
public static double[][] parallelMultiplyMatrix(
    double[][] a, double[][] b)
```

Write a test program that measures the execution time for multiplying two 2,000 × 2,000 matrices using the parallel method and sequential method, respectively.

*30.18  *(Parallel Eight Queens)* Revise Listing 22.11, EightQueens.java, to develop a parallel algorithm that finds all solutions for the Eight Queens problem. *(Hint: Launch eight subtasks, each of which places the queen in a different column in the first row.)*

Comprehensive

***30.19  *(Sorting animation)* Write an animation for selection sort, insertion sort, and bubble sort, as shown in Figure 30.31. Create an array of integers 1, 2, ..., 50. Shuffle it randomly. Create a pane to display the array in a histogram. You should invoke each sort method in a separate thread. Each algorithm uses two nested loops. When the algorithm completes an iteration in the outer loop, put the thread to sleep for 0.5 seconds, and redisplay the array in the histogram. Color the last bar in the sorted subarray.
(Sudoku search animation) Modify Programming Exercise 22.21 to display the intermediate results of the search. Figure 30.32 gives a snapshot of an animation in progress with number 2 placed in the cell in Figure 30.32a, number 3 placed in the cell in Figure 30.32b, and number 3 placed in the cell in Figure 30.32c. The animation displays all the search steps.

**Figure 30.31** Three sorting algorithms are illustrated in the animation.

**Figure 30.32** The intermediate search steps are displayed in the animation for the Sudoku problem.
30.21  (Combine colliding bouncing balls) Rewrite Programming Exercise 20.5 using a thread to animate bouncing ball movements.

***30.22  (Eight Queens animation) Modify Listing 22.11, EightQueens.java, to display the intermediate results of the search. As shown in Figure 30.33, the current row being searched is highlighted. Every one second, a new state of the chess board is displayed.

![Figure 30.33](image)

The intermediate search steps are displayed in the animation for the Eight Queens problem.
NETWORKING

Objectives

■ To explain terms: TCP, IP, domain name, domain name server, stream-based communications, and packet-based communications (§31.2).
■ To create servers using server sockets (§31.2.1) and clients using client sockets (§31.2.2).
■ To implement Java networking programs using stream sockets (§31.2.3).
■ To develop an example of a client/server application (§31.2.4).
■ To obtain Internet addresses using the InetAddress class (§31.3).
■ To develop servers for multiple clients (§31.4).
■ To send and receive objects on a network (§31.5).
■ To develop an interactive tic-tac-toe game played on the Internet (§31.6).
31.1 Introduction

Computer networking is used to send and receive messages among computers on the Internet.

To browse the Web or send an email, your computer must be connected to the Internet. The Internet is the global network of millions of computers. Your computer can connect to the Internet through an Internet Service Provider (ISP) using a dialup, DSL, or cable modem, or through a local area network (LAN).

When a computer needs to communicate with another computer, it needs to know the other computer’s address. An Internet Protocol (IP) address uniquely identifies the computer on the Internet. An IP address consists of four dotted decimal numbers between 0 and 255, such as 130.254.204.31. Since it is not easy to remember so many numbers, they are often mapped to meaningful names called domain names, such as liang.armstrong.edu. Special servers called Domain Name Servers (DNS) on the Internet translate host names into IP addresses. When a computer contacts liang.armstrong.edu, it first asks the DNS to translate this domain name into a numeric IP address and then sends the request using the IP address.

The Internet Protocol is a low-level protocol for delivering data from one computer to another across the Internet in packets. Two higher-level protocols used in conjunction with the IP are the Transmission Control Protocol (TCP) and the User Datagram Protocol (UDP). TCP enables two hosts to establish a connection and exchange streams of data. TCP guarantees delivery of data and also guarantees that packets will be delivered in the same order in which they were sent. UDP is a standard, low-overhead, connectionless, host-to-host protocol that is used over the IP. UDP allows an application program on one computer to send a datagram to an application program on another computer.

Java supports both stream-based and packet-based communications. Stream-based communications use TCP for data transmission, whereas packet-based communications use UDP. Since TCP can detect lost transmissions and resubmit them, transmissions are lossless and reliable. UDP, in contrast, cannot guarantee lossless transmission. Stream-based communications are used in most areas of Java programming and are the focus of this chapter. Packet-based communications are introduced in Supplement III.P, Networking Using Datagram Protocol.

31.2 Client/Server Computing

Java provides the ServerSocket class for creating a server socket and the Socket class for creating a client socket. Two programs on the Internet communicate through a server socket and a client socket using I/O streams.

Networking is tightly integrated in Java. The Java API provides the classes for creating sockets to facilitate program communications over the Internet. Sockets are the endpoints of logical connections between two hosts and can be used to send and receive data. Java treats socket communications much as it treats I/O operations; thus, programs can read from or write to sockets as easily as they can read from or write to files.

Network programming usually involves a server and one or more clients. The client sends requests to the server, and the server responds. The client begins by attempting to establish a connection to the server. The server can accept or deny the connection. Once a connection is established, the client and the server communicate through sockets.

The server must be running when a client attempts to connect to the server. The server waits for a connection request from the client. The statements needed to create sockets on a server and on a client are shown in Figure 31.1.

31.2.1 Server Sockets

To establish a server, you need to create a server socket and attach it to a port, which is where the server listens for connections. The port identifies the TCP service on the socket. Port numbers range from 0 to 65536, but port numbers 0 to 1024 are reserved for privileged services.
For instance, the email server runs on port 25, and the Web server usually runs on port 80. You can choose any port number that is not currently used by other programs. The following statement creates a server socket `serverSocket`:

```java
ServerSocket serverSocket = new ServerSocket(port);
```

**Note**
Attempting to create a server socket on a port already in use would cause a `java.net.BindException`.

### 31.2.2 Client Sockets

After a server socket is created, the server can use the following statement to listen for connections:

```java
Socket socket = serverSocket.accept();
```

This statement waits until a client connects to the server socket. The client issues the following statement to request a connection to a server:

```java
Socket socket = new Socket(serverName, port);
```

This statement opens a socket so that the client program can communicate with the server. `serverName` is the server’s Internet host name or IP address. The following statement creates a socket on the client machine to connect to the host 130.254.204.33 at port 8000:

```java
Socket socket = new Socket("130.254.204.33", 8000);
```

Alternatively, you can use the domain name to create a socket, as follows:

```java
Socket socket = new Socket("liang.armstrong.edu", 8000);
```

When you create a socket with a host name, the JVM asks the DNS to translate the host name into the IP address.

**Note**
A program can use the host name `localhost` or the IP address `127.0.0.1` to refer to the machine on which a client is running.
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Note
The `Socket` constructor throws a `java.net.UnknownHostException` if the host cannot be found.

31.2.3 Data Transmission through Sockets

After the server accepts the connection, communication between the server and the client is conducted in the same way as for I/O streams. The statements needed to create the streams and to exchange data between them are shown in Figure 31.2.

![Figure 31.2](image)

**Figure 31.2** The server and client exchange data through I/O streams on top of the socket.

To get an input stream and an output stream, use the `getInputStream()` and `getOutputStream()` methods on a socket object. For example, the following statements create an `InputStream` stream called `input` and an `OutputStream` stream called `output` from a socket:

```java
InputStream input = socket.getInputStream();
OutputStream output = socket.getOutputStream();
```

The `InputStream` and `OutputStream` streams are used to read or write bytes. You can use `DataInputStream`, `DataOutputStream`, `BufferedReader`, and `PrintWriter` to wrap on the `InputStream` and `OutputStream` to read or write data, such as `int`, `double`, or `String`. The following statements, for instance, create the `DataInputStream` stream `input` and the `DataOutputStream` stream `output` to read and write primitive data values:

```java
DataInputStream input = new DataInputStream(socket.getInputStream());
DataOutputStream output = new DataOutputStream(socket.getOutputStream());
```

The server can use `input.readDouble()` to receive a `double` value from the client and `output.writeDouble(d)` to send the `double` value `d` to the client.

Tip
Recall that binary I/O is more efficient than text I/O because text I/O requires encoding and decoding. Therefore, it is better to use binary I/O for transmitting data between a server and a client to improve performance.
31.2.4 A Client/Server Example

This example presents a client program and a server program. The client sends data to a server. The server receives the data, uses it to produce a result, and then sends the result back to the client. The client displays the result on the console. In this example, the data sent from the client comprise the radius of a circle, and the result produced by the server is the area of the circle (see Figure 31.3).

![Diagram of client and server communication](image)

**Figure 31.3** The client sends the radius to the server; the server computes the area and sends it to the client.

The client sends the radius through a `DataOutputStream` on the output stream socket, and the server receives the radius through the `DataInputStream` on the input stream socket, as shown in Figure 31.4a. The server computes the area and sends it to the client through a `DataOutputStream` on the output stream socket, and the client receives the area through a `DataInputStream` on the input stream socket, as shown in Figure 31.4b. The server and client programs are given in Listings 31.1 and 31.2. Figure 31.5 contains a sample run of the server and the client.

![Diagram showing data flow](image)

**Figure 31.4** (a) The client sends the radius to the server. (b) The server sends the area to the client.

![Sample run of server and client](image)

**Figure 31.5** The client sends the radius to the server. The server receives it, computes the area, and sends the area to the client.

**Listing 31.1 Server.java**

```java
1 import java.io.*;
2 import java.net.*;
3 import java.util.Date;
```
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```java
import javafx.application.Application;
import javafx.application.Platform;
import javafx.scene.Scene;
import javafx.scene.control.ScrollPane;
import javafx.scene.control.TextArea;
import javafx.stage.Stage;

public class Server extends Application {

    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {

        TextArea ta = new TextArea();

        // Create a scene and place it in the stage
        Scene scene = new Scene(new ScrollPane(ta), 450, 200);
        primaryStage.setTitle("Server"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage

        new Thread(() -> {
            try {
                // Create a server socket
                ServerSocket serverSocket = new ServerSocket(8000);
                Platform.runLater(() ->
                        ta.appendText("Server started at " + new Date() + '\n'));

                // Listen for a connection request
                Socket socket = serverSocket.accept();

                // Create data input and output streams
                DataInputStream inputFromClient = new DataInputStream(
                        socket.getInputStream());
                DataOutputStream outputToClient = new DataOutputStream(
                        socket.getOutputStream());

                while (true) {
                    // Receive radius from the client
                    double radius = inputFromClient.readDouble();

                    // Compute area
                    double area = radius * radius * Math.PI;

                    // Send area back to the client
                    outputToClient.writeDouble(area);

                    Platform.runLater(() -> {
                        ta.appendText("Radius received from client: " + radius + '\n');
                        ta.appendText("Area is: " + area + '\n');
                    });
                }
            } catch (IOException ex) {
                ex.printStackTrace();
            }
        }).start();
    }
}
```
import java.io.*;
import java.net.*;
import javafx.application.Application;
import javafx.geometry.Insets;
import javafx.geometry.Pos;
import javafx.scene.Scene;
import javafx.scene.control.Label;
import javafx.scene.control.ScrollPane;
import javafx.scene.control.TextArea;
import javafx.scene.control.TextField;
import javafx.scene.layout.BorderPane;
import javafx.stage.Stage;

public class Client extends Application {

    // IO streams
    DataOutputStream toServer = null;
    DataInputStream fromServer = null;

    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Panel p to hold the label and text field
        BorderPane paneForTextField = new BorderPane();
        paneForTextField.setPadding(new Insets(5, 5, 5, 5));
        paneForTextField.setStyle("-fx-border-color: green");
        paneForTextField.setLeft(new Label("Enter a radius: "));

        TextField tf = new TextField();
        tf.setAlignment(Pos.BOTTOM_RIGHT);
        paneForTextField.setCenter(tf);

        BorderPane mainPane = new BorderPane();
        mainPane.setTop(paneForTextField);

        // Text area to display contents
        TextArea ta = new TextArea();
        mainPane.setCenter(new ScrollPane(ta));
        mainPane.setTop(paneForTextField);

        // Create a scene and place it in the stage
        Scene scene = new Scene(mainPane, 450, 200);
        primaryStage.setTitle("Client"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage

        tf.setOnAction(e -> {
            try {
                // Get the radius from the text field
                double radius = Double.parseDouble(tf.getText().trim());

                // Send the radius to the server
                toServer.writeDouble(radius);
                toServer.flush();

                // Get area from the server
                double area = fromServer.readDouble();

                // Display to the text area
                ta.appendText("Radius is " + radius + "\n");
                ta.appendText("Area received from the server is " + area + "\n");
            } catch (Exception e) {
                e.printStackTrace();
            }
        });
    }
}

@Client/Server Computing
You start the server program first and then start the client program. In the client program, enter a radius in the text field and press Enter to send the radius to the server. The server computes the area and sends it back to the client. This process is repeated until one of the two programs terminates.

The networking classes are in the package java.net. You should import this package when writing Java network programs.

The Server class creates a ServerSocket serverSocket and attaches it to port 8000 using this statement (line 26 in Server.java):

```java
ServerSocket serverSocket = new ServerSocket(8000);
```

The server then starts to listen for connection requests, using the following statement (line 31 in Server.java):

```java
Socket socket = serverSocket.accept();
```

The server waits until the client requests a connection. After it is connected, the server reads the radius from the client through an input stream, computes the area, and sends the result to the client through an output stream. The ServerSocket accept() method takes time to execute. It is not appropriate to run this method in the JavaFX application thread. So, we place it in a separate thread (lines 23–59). The statements for updating GUI need to run from the JavaFX application thread using the Platform.runLater method (lines 27–28, 49–53).

The Client class uses the following statement to create a socket that will request a connection to the server on the same machine (localhost) at port 8000 (line 67 in Client.java).

```java
Socket socket = new Socket("localhost", 8000);
```

If you run the server and the client on different machines, replace localhost with the server machine’s host name or IP address. In this example, the server and the client are running on the same machine.

If the server is not running, the client program terminates with a java.net.ConnectException. After it is connected, the client gets input and output streams—wrapped by data input and output streams—in order to receive and send data to the server.
If you receive a `java.net.BindException` when you start the server, the server port is currently in use. You need to terminate the process that is using the server port and then restart the server.

**Note**
When you create a server socket, you have to specify a port (e.g., 8000) for the socket. When a client connects to the server (line 67 in Client.java), a socket is created on the client. This socket has its own local port. This port number (e.g., 2047) is automatically chosen by the JVM, as shown in Figure 31.6.

![Figure 31.6](image)

**Figure 31.6** The JVM automatically chooses an available port to create a socket for the client.

To see the local port on the client, insert the following statement in line 70 in Client.java.

```java
System.out.println("local port: " + socket.getLocalPort());
```

### 31.1 How do you create a server socket? What port numbers can be used? What happens if a requested port number is already in use? Can a port connect to multiple clients?

### 31.2 What are the differences between a server socket and a client socket?

### 31.3 How does a client program initiate a connection?

### 31.4 How does a server accept a connection?

### 31.5 How are data transferred between a client and a server?

#### 31.3 The InetAddress Class

*The server program can use the InetAddress class to obtain the information about the IP address and host name for the client.*

Occasionally, you would like to know who is connecting to the server. You can use the `InetAddress` class to find the client’s host name and IP address. The `InetAddress` class models an IP address. You can use the following statement in the server program to get an instance of `InetAddress` on a socket that connects to the client.

```java
InetAddress inetAddress = socket.getInetAddress();
```

Next, you can display the client’s host name and IP address, as follows:

```java
System.out.println("Client's host name is " + inetAddress.getHostName());
```
You can also create an instance of `InetAddress` from a host name or IP address using the static `getByName` method. For example, the following statement creates an `InetAddress` for the host `liang.armstrong.edu`.

```java
InetAddress address = InetAddress.getByName("liang.armstrong.edu");
```

Listing 31.3 gives a program that identifies the host name and IP address of the arguments you pass in from the command line. Line 7 creates an `InetAddress` using the `getByName` method. Lines 8 and 9 use the `getHostName` and `getHostAddress` methods to get the host’s name and IP address. Figure 31.7 shows a sample run of the program.

![Figure 31.7](image)

The program identifies host names and IP addresses.

**LISTING 31.3** IdentifyHostNameIP.java

```java
import java.net.*;

public class IdentifyHostNameIP {
    public static void main(String[] args) {
        for (int i = 0; i < args.length; i++) {
            try {
                InetAddress address = InetAddress.getByName(args[i]);
                System.out.print("Host name: ");
                System.out.println(address.getHostName() + " ");
                System.out.println("IP address: ");
                System.out.println(address.getHostAddress());
            } catch (UnknownHostException ex) {
                System.err.println("Unknown host or IP address " + args[i]);
            }
        }
    }
}
```

31.6 How do you obtain an instance of `InetAddress`?

31.7 What methods can you use to get the IP address and hostname from an `InetAddress`?

### 31.4 Serving Multiple Clients

A server can serve multiple clients. The connection to each client is handled by one thread.

Multiple clients are quite often connected to a single server at the same time. Typically, a server runs continuously on a server computer, and clients from all over the Internet can connect to it. You can use threads to handle the server’s multiple clients simultaneously—simply
create a thread for each connection. Here is how the server handles the establishment of a connection:

```java
    while (true) {
        Socket socket = serverSocket.accept(); // Connect to a client
        Thread thread = new ThreadClass(socket);
        thread.start();
    }
```

The server socket can have many connections. Each iteration of the `while` loop creates a new connection. Whenever a connection is established, a new thread is created to handle communication between the server and the new client, and this allows multiple connections to run at the same time.

Listing 31.4 creates a server class that serves multiple clients simultaneously. For each connection, the server starts a new thread. This thread continuously receives input (the radius of a circle) from clients and sends the results (the area of the circle) back to them (see Figure 31.8). The client program is the same as in Listing 31.2. A sample run of the server with two clients is shown in Figure 31.9.

![Figure 31.8](image1.png) Multithreading enables a server to handle multiple independent clients.

![Figure 31.9](image2.png) The server spawns a thread in order to serve a client.

**Listing 31.4** MultiThreadServer.java

```java
    import java.io.*;
    import java.net.*;
    import java.util.Date;
    import javafx.application.Application;
    import javafx.application.Platform;
    import javafx.scene.Scene;
    import javafx.scene.control.ScrollPane;
    import javafx.scene.control.TextArea;
    import javafx.stage.Stage;
```
public class MultiThreadServer extends Application {
    private TextArea ta = new TextArea();

    // Number a client
    private int clientNo = 0;

    @Override
    public void start(Stage primaryStage) {
        Scene scene = new Scene(new ScrollPane(ta), 450, 200);
        primaryStage.setTitle("MultiThreadServer");
        primaryStage.setScene(scene);
        primaryStage.show();

        new Thread( () -> {
            try {
                ServerSocket serverSocket = new ServerSocket(8000);
                ta.appendText("MultiThreadServer started at "+
                        new Date() + '\n');
                while (true) {
                    // Listen for a new connection request
                    Socket socket = serverSocket.accept();
                    clientNo++;
                    Platform.runLater( () -> {
                        // Display the client number
                        ta.appendText("Starting thread for client "+ clientNo +
                                " at "+ new Date() + '\n');
                        // Find the client's host name, and IP address
                        InetAddress inetAddress = socket.getInetAddress();
                        ta.appendText("Client "+ clientNo + ", host name is " +
                                inetAddress.getHostName() + '\n');
                        ta.appendText("Client "+ clientNo + ", IP Address is " +
                                inetAddress.getHostAddress() + '\n');
                    });
                }
            } catch (IOException ex) {
                System.err.println(ex);
            }
        }).start();
    }

    class HandleAClient implements Runnable {
        private Socket socket; // A connected socket

        /** Construct a thread */
        public HandleAClient(Socket socket) {
            this.socket = socket;
        }
    }
}
31.5 Sending and Receiving Objects

A program can send and receive objects from another program.

In the preceding examples, you learned how to send and receive data of primitive types. You can also send and receive objects using `ObjectOutputStream` and `ObjectInputStream` on socket streams. To enable passing, the objects must be serializable. The following example demonstrates how to send and receive objects.

The example consists of three classes: StudentAddress.java (Listing 31.5), StudentClient.java (Listing 31.6), and StudentServer.java (Listing 31.7). The client program collects student information from the client and sends it to a server, as shown in Figure 31.10.

The `StudentAddress` class contains the student information: name, street, city, state, and zip. The `StudentAddress` class implements the `Serializable` interface. Therefore, a `StudentAddress` object can be sent and received using the object output and input streams.
The client sends a `StudentAddress` object through an `ObjectOutputStream` on the output stream socket, and the server receives the `Student` object through the `ObjectInputStream` on the input stream socket, as shown in Figure 31.11. The client uses the `writeObject` method in the `ObjectOutputStream` class to send data about a student to the server, and the server receives the student’s information using the `readObject` method in the `ObjectInputStream` class. The server and client programs are given in Listings 31.6 and 31.7.
31.5 Sending and Receiving Objects

**Listing 31.6 StudentClient.java**

```java
public class StudentClient extends Application {
    private TextField tfName = new TextField();
    private TextField tfStreet = new TextField();
    private TextField tfCity = new TextField();
    private TextField tfState = new TextField();
    private TextField tfZip = new TextField();

    private Button btRegister = new Button("Register to the Server");

    // Host name or ip
    String host = "localhost";

    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        GridPane pane = new GridPane();
        pane.add(new Label("Name"), 0, 0);
        pane.add(tfName, 1, 0);
        pane.add(new Label("Street"), 0, 1);
        pane.add(tfStreet, 1, 1);
        pane.add(new Label("City"), 0, 2);
        pane.add(tfCity, 1, 2);
        pane.add(new Label("State"), 0, 3);
        pane.add(tfState, 1, 3);
        pane.add(new Label("Zip"), 0, 4);
        pane.add(tfZip, 1, 4);
        primaryStage.setTitle("StudentAddress");
        primaryStage.setScene(new Scene(pane));
        primaryStage.show();
    }
}
```

**Figure 31.11** The client sends a `StudentAddress` object to the server.
HBox hBox = new HBox(2);
pane.add(hBox, 1, 2);
hBox.getChildren().addAll(tfCity, new Label("State"), tfState,
   new Label("Zip"), tfZip);
pane.add(btRegister, 1, 3);
GridPane.setAlignment(btRegister, HPos.RIGHT);
pane.setAlignment(Pos.CENTER);
tfName.setPrefColumnCount(15);
tfStreet.setPrefColumnCount(15);
tfCity.setPrefColumnCount(10);
tfState.setPrefColumnCount(2);
tfZip.setPrefColumnCount(3);
btRegister.setOnAction(new ButtonListener());

// Create a scene and place it in the stage
Scene scene = new Scene(pane, 450, 200);
primaryStage.setTitle("StudentClient"); // Set the stage title
primaryStage.setScene(scene); // Place the scene in the stage
primaryStage.show(); // Display the stage

/** Handle button action */
private class ButtonListener implements EventHandler<ActionEvent> {
   @Override
   public void handle(ActionEvent e) {
      try {
         // Establish connection with the server
         Socket socket = new Socket(host, 8000);

         // Create an output stream to the server
         ObjectOutputStream toServer =
            new ObjectOutputStream(socket.getOutputStream());

         // Get text field
         String name = tfName.getText().trim();
         String street = tfStreet.getText().trim();
         String city = tfCity.getText().trim();
         String state = tfState.getText().trim();
         String zip = tfZip.getText().trim();

         // Create a Student object and send to the server
         StudentAddress s =
            new StudentAddress(name, street, city, state, zip);
         toServer.writeObject(s);
      } catch (IOException ex) {
         ex.printStackTrace();
      }
   }
}

LISTING 31.7  StudentServer.java

import java.io.*;
import java.net.*;

public class StudentServer {
31.5 Sending and Receiving Objects

```java
private ObjectOutputStream outputToFile;
private ObjectInputStream inputFromClient;

public static void main(String[] args) {
    new StudentServer();
}

public StudentServer() {
    try {
        // Create a server socket
        ServerSocket serverSocket = new ServerSocket(8000);
        System.out.println("Server started ");

        // Create an object output stream
        outputToFile = new ObjectOutputStream(
            new FileOutputStream("student.dat", true));

        while (true) {
            // Listen for a new connection request
            Socket socket = serverSocket.accept();

            // Create an input stream from the socket
            inputFromClient =
                new ObjectInputStream(socket.getInputStream());

            // Read from input
            Object object = inputFromClient.readObject();

            // Write to the file
            outputToFile.writeObject(object);
            System.out.println("A new student object is stored");
        }
    } catch (ClassNotFoundException ex) {
        ex.printStackTrace();
    } catch (IOException ex) {
        ex.printStackTrace();
    }
    finally {
        try {
            inputFromClient.close();
            outputToFile.close();
        } catch (Exception ex) {
            ex.printStackTrace();
        }
    }
}
```

On the client side, when the user clicks the Register to the Server button, the client creates a socket to connect to the host (line 67), creates an ObjectOutputStream on the output stream of the socket (lines 70 and 71), and invokes the writeObject method to send the StudentAddress object to the server through the object output stream (line 83).

On the server side, when a client connects to the server, the server creates an ObjectInputStream on the input stream of the socket (lines 27 and 28), invokes the readObject method to receive the StudentAddress object through the object input stream (line 31), and writes the object to a file (line 34).
31.9 How does a server receive connection from a client? How does a client connect to a server?

31.10 How do you find the host name of a client program from the server?

31.11 How do you send and receive an object?

31.6 Case Study: Distributed Tic-Tac-Toe Games

This section develops a program that enables two players to play the tic-tac-toe game on the Internet.

In Section 16.12, Case Study: Developing a Tic-Tac-Toe Game, you developed a program for a tic-tac-toe game that enables two players to play the game on the same machine. In this section, you will learn how to develop a distributed tic-tac-toe game using multithreads and networking with socket streams. A distributed tic-tac-toe game enables users to play on different machines from anywhere on the Internet.

You need to develop a server for multiple clients. The server creates a server socket and accepts connections from every two players to form a session. Each session is a thread that communicates with the two players and determines the status of the game. The server can establish any number of sessions, as shown in Figure 31.13.

For each session, the first client connecting to the server is identified as player 1 with token X, and the second client connecting is identified as player 2 with token O. The server notifies the players of their respective tokens. Once two clients are connected to it, the server starts a thread to facilitate the game between the two players by performing the steps repeatedly, as shown in Figure 31.13.

![Figure 31.12](image)

The server does not have to be a graphical component, but creating it in a GUI in which game information can be viewed is user-friendly. You can create a scroll pane to hold a text area in the GUI and display game information in the text area. The server creates a thread to handle a game session when two players are connected to the server.

The client is responsible for interacting with the players. It creates a user interface with nine cells and displays the game title and status to the players in the labels. The client class is very similar to the TicTacToe class presented in the case study in Listing 16.13. However, the client in this example does not determine the game status (win or draw); it simply passes the moves to the server and receives the game status from the server.

Based on the foregoing analysis, you can create the following classes:

- **TicTacToeServer** serves all the clients in Listing 31.9.

- **HandleASession** facilitates the game for two players. This class is defined in TicTacToeServer.java.
31.6 Case Study: Distributed Tic-Tac-Toe Games

- **TicTacToeClient** models a player in Listing 31.10.
- **Cell** models a cell in the game. It is an inner class in **TicTacToeClient**.
- **TicTacToeConstants** is an interface that defines the constants shared by all the classes in the example in Listing 31.8.

The relationships of these classes are shown in Figure 31.14.

**Listing 31.8**  
**TicTacToeConstants.java**

```java
public interface TicTacToeConstants {
    public static int PLAYER1 = 1; // Indicate player 1
    public static int PLAYER2 = 2; // Indicate player 2
    public static int PLAYER1_WON = 1; // Indicate player 1 won
    public static int PLAYER2_WON = 2; // Indicate player 2 won
    public static int DRAW = 3; // Indicate a draw
    public static int CONTINUE = 4; // Indicate to continue
}
```

**Listing 31.9**  
**TicTacToeServer.java**

```java
import java.io.*;
import java.net.*;
import java.util.Date;
import javafx.application.Application;
```
import javafx.application.Platform;
import javafx.scene.Scene;
import javafx.scene.control.ScrollPane;
import javafx.scene.control.TextArea;
import javafx.stage.Stage;

public class TicTacToeServer extends Application implements TicTacToeConstants {
    private int sessionNo = 1; // Number a session

    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        TextArea taLog = new TextArea();

        // Create a scene and place it in the stage
        Scene scene = new Scene(new ScrollPane(taLog), 450, 200);
        primaryStage.setTitle("TicTacToeServer"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage

        new Thread(() -> {
            try {
                // Create a server socket
                ServerSocket serverSocket = new ServerSocket(8000);
            } catch (IOException e) {
                e.printStackTrace();
            }
        });
    }
}

Fig. 31.14  TicTacToeServer creates an instance of HandleASession for each session of two players. TicTacToeClient creates nine cells in the UI.
31.6 Case Study: Distributed Tic-Tac-Toe Games

Platform.runLater(() -> taLog.appendText(new Date() + ": Server started at socket 8000\n"));

// Ready to create a session for every two players
while (true) {
    Platform.runLater(() -> taLog.appendText(new Date() + ": Wait for players to join session " + sessionNo + '\n'));

    // Connect to player 1
    Socket player1 = serverSocket.accept();
    Platform.runLater(() -> {
        taLog.appendText(new Date() + ": Player 1 joined session " + sessionNo + '\n');
        taLog.appendText("Player 1's IP address" + player1.getInetAddress().getHostAddress() + '\n');
    });

    // Notify that the player is Player 1
    new DataOutputStream(player1.getOutputStream()).writeInt(PLAYER1);

    // Connect to player 2
    Socket player2 = serverSocket.accept();
    Platform.runLater(() -> {
        taLog.appendText(new Date() + ": Player 2 joined session " + sessionNo + '\n');
        taLog.appendText("Player 2's IP address" + player2.getInetAddress().getHostAddress() + '\n');
    });

    // Notify that the player is Player 2
    new DataOutputStream(player2.getOutputStream()).writeInt(PLAYER2);

    // Display this session and increment session number
    Platform.runLater(() ->
        taLog.appendText(new Date() + ": Start a thread for session " + sessionNo++ + '\n'));

    // Launch a new thread for this session of two players
    new Thread(new HandleASession(player1, player2)).start();
}

} catch (IOException ex) {
    ex.printStackTrace();
}

} // End method runThread

// Define the thread class for handling a new session for two players

class HandleASession implements Runnable, TicTacToeConstants {

    private Socket player1;
    private Socket player2;

    // Create and initialize cells
    private char[][] cell = new char[3][3];

    private DataInputStream fromPlayer1;

    // Other methods and logic for handling the session

}
private DataOutputStream toPlayer1;
private DataInputStream fromPlayer2;
private DataOutputStream toPlayer2;

// Continue to play
private boolean continueToPlay = true;

/** Construct a thread */
public HandleASession(Socket player1, Socket player2) {
    this.player1 = player1;
    this.player2 = player2;

    // Initialize cells
    for (int i = 0; i < 3; i++)
        for (int j = 0; j < 3; j++)
            cell[i][j] = ' ';    
}

/** Implement the run() method for the thread */
public void run() {
    try {
        // Create data input and output streams
        DataInputStream fromPlayer1 = new DataInputStream(
            player1.getInputStream());
        DataOutputStream toPlayer1 = new DataOutputStream(
            player1.getOutputStream());
        DataInputStream fromPlayer2 = new DataInputStream(
            player2.getInputStream());
        DataOutputStream toPlayer2 = new DataOutputStream(
            player2.getOutputStream());

        // Write anything to notify player 1 to start
        // This is just to let player 1 know to start
        toPlayer1.writeInt(1);

        // Continuously serve the players and determine and report
        // the game status to the players
        while (true) {
            // Receive a move from player 1
            int row = fromPlayer1.readInt();
            int column = fromPlayer1.readInt();
            cell[row][column] = 'X';

            // Check if Player 1 wins
            if (isWon('X')) {
                toPlayer1.writeInt(PLAYER1_WON);
                toPlayer2.writeInt(PLAYER1_WON);
                sendMove(toPlayer2, row, column);
                break; // Break the loop
            }

            else if (isFull()) { // Check if all cells are filled
                toPlayer1.writeInt(DRAW);
                toPlayer2.writeInt(DRAW);
                sendMove(toPlayer2, row, column);
                break;
            }

            else {
                // Notify player 2 to take the turn
                toPlayer2.writeInt(CONTINUE);
            }
        }
    }
}
// Send player 1's selected row and column to player 2
sendMove(toPlayer2, row, column);

// Receive a move from Player 2
row = fromPlayer2.readInt();
column = fromPlayer2.readInt();
cell[row][column] = 'O';

// Check if Player 2 wins
if (isWon('O')) {
    toPlayer1.writeInt(PLAYER2_WON);
    toPlayer2.writeInt(PLAYER2_WON);
    sendMove(toPlayer1, row, column);
    break;
} else {
    // Notify player 1 to take the turn
    toPlayer1.writeInt(CONTINUE);
    // Send player 2's selected row and column to player 1
    sendMove(toPlayer1, row, column);
}

/** Send the move to other player */
private void sendMove(DataOutputStream out, int row, int column) throws IOException {
    out.writeInt(row); // Send row index
    out.writeInt(column); // Send column index
}

/** Determine if the cells are all occupied */
private boolean isFull() {
    for (int i = 0; i < 3; i++)
        for (int j = 0; j < 3; j++)
            if (cell[i][j] == ' ')
                return false; // At least one cell is not filled
    // All cells are filled
    return true;
}

/** Determine if the player with the specified token wins */
private boolean isWon(char token) {
    // Check all rows
    for (int i = 0; i < 3; i++)
        if ((cell[i][0] == token) && (cell[i][1] == token) && (cell[i][2] == token))
            return true;
    // Check all columns
    for (int j = 0; j < 3; j++)
        if ((cell[0][j] == token) && (cell[1][j] == token) && (cell[2][j] == token))
            return true;
if (cell[0][j] == token)
    && (cell[1][j] == token)
    && (cell[2][j] == token)) {
    return true;
}

/** Check major diagonal */
if ((cell[0][0] == token)
    && (cell[1][1] == token)
    && (cell[2][2] == token)) {
    return true;
}

/** Check subdiagonal */
if ((cell[0][2] == token)
    && (cell[1][1] == token)
    && (cell[2][0] == token)) {
    return true;
}

/** All checked, but no winner */
return false;

/** All checked, but no winner */
return false;

/** All checked, but no winner */
return false;

import java.io.*;
import java.net.*;
import java.util.Date;
import javafx.application.Application;
import javafx.application.Platform;
import javafx.scene.Scene;
import javafx.scene.control.Label;
import javafx.scene.control.ScrollPane;
import javafx.scene.control.TextArea;
import javafx.scene.layout.BorderPane;
import javafx.scene.layout.GridPane;
import javafx.scene.layout.Pane;
import javafx.scene.paint.Color;
import javafx.scene.shape.Ellipse;
import javafx.scene.shape.Line;
import javafx.stage.Stage;

public class TicTacToeClient extends Application implements TicTacToeConstants {
    // Indicate whether the player has the turn
    private boolean myTurn = false;

    // Indicate the token for the player
    private char myToken = ' ';

    // Indicate the token for the other player
    private char otherToken = ' ';

    // Create and initialize cells
    private Cell[][] cell = new Cell[3][3];
31.6 Case Study: Distributed Tic-Tac-Toe Games

```java
private Label lblTitle = new Label();

private Label lblStatus = new Label();

private int rowSelected;
private int columnSelected;

private DataInputStream fromServer;
private DataOutputStream toServer;

private boolean continueToPlay = true;

private boolean waiting = true;

private String host = "localhost";

@Override // Override the start method in the Application class
public void start(Stage primaryStage) {
    GridPane pane = new GridPane();
    for (int i = 0; i < 3; i++)
        for (int j = 0; j < 3; j++)
            pane.add(cell[i][j] = new Cell(i, j), j, i);

    BorderPane borderPane = new BorderPane();
    borderPane.setTop(lblTitle);
    borderPane.setCenter(pane);
    borderPane.setBottom(lblStatus);

    Scene scene = new Scene(borderPane, 320, 350);
    primaryStage.setTitle("TicTacToeClient"); // Set the stage title
    primaryStage.setScene(scene); // Place the scene in the stage
    primaryStage.show(); // Display the stage

    connectToServer();
}

private void connectToServer() {
    try {
        Socket socket = new Socket(host, 8000);

        fromServer = new DataInputStream(socket.getInputStream());
        toServer = new DataOutputStream(socket.getOutputStream());
    } catch (Exception ex) {
        ex.printStackTrace();
    }
}
```
// Control the game on a separate thread
new Thread() -> {
    try {
        // Get notification from the server
        int player = fromServer.readInt();

        // Am I player 1 or 2?
        if (player == PLAYER1) {
            myToken = 'X';
            otherToken = 'O';
            Platform.runLater(() -> {
                lblTitle.setText("Player 1 with token 'X'");
                lblStatus.setText("Waiting for player 2 to join");
            });

            // Receive startup notification from the server
            fromServer.readInt(); // Whatever read is ignored

            // The other player has joined
            Platform.runLater(() -> {
                lblStatus.setText("Player 2 has joined. I start first");
            });

            // It is my turn
            myTurn = true;
        } else if (player == PLAYER2) {
            myToken = 'O';
            otherToken = 'X';
            Platform.runLater(() -> {
                lblTitle.setText("Player 2 with token 'O'");
                lblStatus.setText("Waiting for player 1 to move");
            });
        }

        // Continue to play
        while (continueToPlay) {
            if (player == PLAYER1) {
                waitForPlayerAction(); // Wait for player 1 to move
                sendMove(); // Send the move to the server
                receiveInfoFromServer(); // Receive info from the server
            } else if (player == PLAYER2) {
                receiveInfoFromServer(); // Receive info from the server
                waitForPlayerAction(); // Wait for player 2 to move
                sendMove(); // Send player 2's move to the server
            }
        }
        catch (Exception ex) {
            ex.printStackTrace();
        }
    }).start();

    // Continue the game on a separate thread
    new Thread() -> {
        // Get notification from the server
        int player = fromServer.readInt();

        // Am I player 1 or 2?
        if (player == PLAYER1) {
            myToken = 'X';
            otherToken = 'O';
            Platform.runLater(() -> {
                lblTitle.setText("Player 1 with token 'X'");
                lblStatus.setText("Waiting for player 2 to join");
            });

            // Receive startup notification from the server
            fromServer.readInt(); // Whatever read is ignored

            // The other player has joined
            Platform.runLater(() -> {
                lblStatus.setText("Player 2 has joined. I start first");
            });

            // It is my turn
            myTurn = true;
        } else if (player == PLAYER2) {
            myToken = 'O';
            otherToken = 'X';
            Platform.runLater(() -> {
                lblTitle.setText("Player 2 with token 'O'");
                lblStatus.setText("Waiting for player 1 to move");
            });
        }

        // Continue to play
        while (continueToPlay) {
            if (player == PLAYER1) {
                waitForPlayerAction(); // Wait for player 1 to move
                sendMove(); // Send the move to the server
                receiveInfoFromServer(); // Receive info from the server
            } else if (player == PLAYER2) {
                receiveInfoFromServer(); // Receive info from the server
                waitForPlayerAction(); // Wait for player 2 to move
                sendMove(); // Send player 2's move to the server
            }
        }
        catch (Exception ex) {
            ex.printStackTrace();
        }
    }).start();

    /** Wait for the player to mark a cell */
    private void waitForPlayerAction() throws InterruptedException {
        while (waiting) {
            Thread.sleep(100);
        }
    }
waiting = true;

/** Send this player's move to the server */
private void sendMove() throws IOException {
    toServer.writeInt(rowSelected); // Send the selected row
    toServer.writeInt(columnSelected); // Send the selected column
}

/** Receive info from the server */
private void receiveInfoFromServer() throws IOException {
    // Receive game status
    int status = fromServer.readInt();

    if (status == PLAYER1_WON) {
        // Player 1 won, stop playing
        continueToPlay = false;
        if (myToken == 'X') {
            Platform.runLater(() -> lblStatus.setText("I won! (X)"));
        }
    } else if (myToken == 'O') {
        Platform.runLater(() -> lblStatus.setText("Player 1 (X) has won!");
        receiveMove();
    } else if (status == PLAYER2_WON) {
        // Player 2 won, stop playing
        continueToPlay = false;
        if (myToken == 'O') {
            Platform.runLater(() -> lblStatus.setText("I won! (O)"));
        }
    } else if (status == DRAW) {
        // No winner, game is over
        continueToPlay = false;
        Platform.runLater(() -> lblStatus.setText("Game is over, no winner!");
        if (myToken == 'O') {
            receiveMove();
        }
    } else {
        receiveMove();
        Platform.runLater(() -> lblStatus.setText("My turn");
        myTurn = true; // It is my turn
    }
}

private void receiveMove() throws IOException {
    // Get the other player's move
    int row = fromServer.readInt();
    int column = fromServer.readInt();
model a cell

```java
public class Cell extends Pane {
    // An inner class for a cell
    // Indicate the row and column of this cell in the board
    private int row;
    private int column;

    // Token used for this cell
    private char token = ' ';

    public Cell(int row, int column) {
        this.row = row;
        this.column = column;

        this.setPrefSize(2000, 2000); // What happens without this?
        setStyle("-fx-border-color: black"); // Set cell's border
        this.setOnMouseClicked(e -> handleMouseClick());
    }

    /** Return token */
    public char getToken() {
        return token;
    }

    /** Set a new token */
    public void setToken(char c) {
        token = c;
        repaint();
    }

    protected void repaint() {
        if (token == 'X') {
            Line line1 = new Line(10, 10,
                                   this.getWidth() - 10, this.getHeight() - 10);

            line1.endXProperty().bind(this.widthProperty().subtract(10));
            line1.endYProperty().bind(this.heightProperty().subtract(10));

            Line line2 = new Line(10, this.getHeight() - 10,
                                   this.getWidth() - 10, 10);

            line2.startYProperty().bind(this.heightProperty().subtract(10));
            line2.endXProperty().bind(this.widthProperty().subtract(10));

            // Add the lines to the pane
            this.getChildren().addAll(line1, line2);
        }

        else if (token == 'O') {
            Ellipse ellipse = new Ellipse(this.getWidth() / 2,
                                          this.getHeight() / 2,
                                          this.getWidth() / 2 - 10,
                                          this.getHeight() / 2 - 10);

            ellipse.centerXProperty().bind(this.widthProperty().divide(2));
            ellipse.centerYProperty().bind(this.heightProperty().divide(2));

            ellipse.radiusXProperty().bind(ellipse.widthProperty().divide(2).subtract(10));
            ellipse.radiusYProperty().bind(ellipse.heightProperty().divide(2).subtract(10));

            ellipse.setStroke(Color.BLACK);
            ellipse.setFill(Color.WHITE);
        }
    }
}
```

register listener

draw X

draw O
272        getChildren().add(ellipse); // Add the ellipse to the pane
273    }
274  }
275
276  /* Handle a mouse click event */
277  private void handleMouseClick() {
278    // If cell is not occupied and the player has the turn
279    if (token == ' ' && myTurn) {
280      setToken(myToken); // Set the player's token in the cell
281      myTurn = false;
282      rowSelected = row;
283      columnSelected = column;
284      lblStatus.setText("Waiting for the other player to move");
285      waiting = false; // Just completed a successful move
286    }
287  }
288  }
289
The server can serve any number of sessions simultaneously. Each session takes care of two
players. The client can be deployed to run as a Java applet. To run a client as a Java applet
from a Web browser, the server must run from a Web server. Figures 31.15 and 31.16 show
sample runs of the server and the clients.

![TicTacToeServer](image1)
**Figure 31.15** TicTacToeServer accepts connection requests and creates sessions to
serve pairs of players.

![TicTacToeClient](image2)
**Figure 31.16** TicTacToeClient can run as an applet or standalone.

The TicTacToeConstants interface defines the constants shared by all the classes in the
project. Each class that uses the constants needs to implement the interface. Centrally defining
constants in an interface is a common practice in Java.

Once a session is established, the server receives moves from the players in alterna-
tion. Upon receiving a move from a player, the server determines the status of the game. If
the game is not finished, the server sends the status (CONTINUE) and the player’s move to
the other player. If the game is won or a draw, the server sends the status (PLAYER1_WON, 
PLAYER2_WON, or DRAW) to both players.

The implementation of Java network programs at the socket level is tightly synchronized. 
An operation to send data from one machine requires an operation to receive data from the 
other machine. As shown in this example, the server and the client are tightly synchronized 
to send or receive data.

33.11 What would happen if the preferred size for a cell is not set in line 227 in Listing 
31.10?

33.12 If a player does not have the turn but clicks on an empty cell, what will the client 
program in Listing 31.10 do?

**KEY TERMS**

- client socket 1141
- domain name 1140
- domain name server 1140
- localhost 1141
- IP address 1141
- port 1140
- packet-based communication 1140
- server socket 1140
- socket 1140
- stream-based communication 1140
- TCP 1140
- UDP 1140

**CHAPTER SUMMARY**

1. Java supports stream sockets and datagram sockets. *Stream sockets* use TCP (Transmission Control Protocol) for data transmission, whereas *datagram sockets* use UDP (User Datagram Protocol). Since TCP can detect lost transmissions and resubmit them, transmissions are lossless and reliable. UDP, in contrast, cannot guarantee lossless 
transmission.

2. To create a server, you must first obtain a server socket, using `new ServerSocket (port)`. After a server socket is created, the server can start to listen for connections, 
using the `accept()` method on the server socket. The client requests a connection to a 
server by using `new Socket(serverName, port)` to create a client socket.

3. Stream socket communication is very much like input/output stream communication 
after the connection between a server and a client is established. You can obtain an 
input stream using the `getInputStream()` method and an output stream using the 
`getOutputStream()` method on the socket.

4. A server must often work with multiple clients at the same time. You can use threads 
to handle the server’s multiple clients simultaneously by creating a thread for each 
connection.

**Quiz**

Answer the quiz for this chapter online at [www.cs.armstrong.edu/liang/intro10e/quiz.html](http://www.cs.armstrong.edu/liang/intro10e/quiz.html).
Section 31.2

*31.1 (Loan server) Write a server for a client. The client sends loan information (annual interest rate, number of years, and loan amount) to the server (see Figure 31.17a). The server computes monthly payment and total payment, and sends them back to the client (see Figure 31.17b). Name the client Exercise31_01Client and the server Exercise31_01Server.

![Figure 31.17](a) The client in (a) sends the annual interest rate, number of years, and loan amount to the server and receives the monthly payment and total payment from the server in (b).

*31.2 (BMI server) Write a server for a client. The client sends the weight and height for a person to the server (see Figure 31.18a). The server computes BMI (Body Mass Index) and sends back to the client a string that reports the BMI (see Figure 31.18b). See Section 3.8 for computing BMI. Name the client Exercise31_02Client and the server Exercise31_02Server.

![Figure 31.18](a) The client in (a) sends the weight and height of a person to the server and receives the BMI from the server in (b).

Sections 31.3 and 31.4

*31.3 (Loan server for multiple clients) Revise Programming Exercise 31.1 to write a server for multiple clients.

Section 31.5

31.4 (Count clients) Write a server that tracks the number of the clients connected to the server. When a new connection is established, the count is incremented by 1. The count is stored using a random-access file. Write a client program that
receives the count from the server and display a message, such as You are visitor number 11, as shown in Figure 31.19. Name the client Exercise31_04Client and the server Exercise31_04Server.

31.5  *(Send loan information in an object)* Revise Exercise 31.1 for the client to send a loan object that contains annual interest rate, number of years, and loan amount and for the server to send the monthly payment and total payment.

Section 31.6

31.6  *(Display and add addresses)* Develop a client/server application to view and add addresses, as shown in Figure 31.20.

- Use the **StudentAddress** class defined in Listing 31.5 to hold the name, street, city, state, and zip in an object.
- The user can use the buttons **First**, **Next**, **Previous**, and **Last** to view an address, and the **Add** button to add a new address.
- Limit the concurrent connections to two clients.

Name the client Exercise31_06Client and the server Exercise31_06Server.

*31.7  *(Transfer last 100 numbers in an array)* Programming Exercise 22.12 retrieves the last 100 prime numbers from a file **PrimeNumbers.dat**. Write a client program that requests the server to send the last 100 prime numbers in an array. Name the server program Exercise31_07Server and the client program Exercise31_07Client. Assume that the numbers of the **long** type are stored in **PrimeNumbers.dat** in binary format.

*31.8  *(Transfer last 100 numbers in an ArrayList)* Programming Exercise 24.12 retrieves the last 100 prime numbers from a file **PrimeNumbers.dat**. Write a client program that requests the server to send the last 100 prime numbers in an **ArrayList**. Name the server program Exercise31_08Server and the client program Exercise31_08Client. Assume that the numbers of the **long** type are stored in **PrimeNumbers.dat** in binary format.
Section 31.7

**31.9** *(Chat)* Write a program that enables two users to chat. Implement one user as the server (Figure 31.21a) and the other as the client (Figure 31.21b). The server has two text areas: one for entering text and the other (noneditable) for displaying text received from the client. When the user presses the *Enter* key, the current line is sent to the client. The client has two text areas: one (noneditable) for displaying text from the server and the other for entering text. When the user presses the *Enter* key, the current line is sent to the server. Name the client Exercise31_09Client and the server Exercise31_09Server.

![Figure 31.21](image)
The server and client send text to and receive text from each other.

***31.10** *(Multiple client chat)* Write a program that enables any number of clients to chat. Implement one server that serves all the clients, as shown in Figure 31.22. Name the client Exercise31_10Client and the server Exercise31_10Server.

![Figure 31.22](image)
The server starts in (a) with three clients in (b) and (c).
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Objectives

- To understand the concepts of databases and database management systems (§32.2).
- To understand the relational data model: relational data structures, constraints, and languages (§32.2).
- To use SQL to create and drop tables and to retrieve and modify data (§32.3).
- To learn how to load a driver, connect to a database, execute statements, and process result sets using JDBC (§32.4).
- To use prepared statements to execute precompiled SQL statements (§32.5).
- To use callable statements to execute stored SQL procedures and functions (§32.6).
- To explore database metadata using the DatabaseMetaData and ResultSetMetaData interfaces (§32.7).
32.1 Introduction

Java provides the API for developing database applications that works with any relational database systems.

You may have heard a lot about database systems. Database systems are everywhere. Your social security information is stored in a database by the government. If you shop online, your purchase information is stored in a database by the company. If you attend a university, your academic information is stored in a database by the university. Database systems not only store data, they also provide means of accessing, updating, manipulating, and analyzing data. Your social security information is updated periodically, and you can register for courses online. Database systems play an important role in society and in commerce.

This chapter introduces database systems, the SQL language, and how database applications can be developed using Java. If you already know SQL, you can skip Sections 32.2 and 32.3.

32.2 Relational Database Systems

SQL is the standard database language for defining and accessing databases.

A database system consists of a database, the software that stores and manages data in the database, and the application programs that present data and enable the user to interact with the database system, as shown in Figure 32.1.

A database is a repository of data that form information. When you purchase a database system—such as MySQL, Oracle, IBM’s DB2 and Informix, Microsoft SQL Server, or Sybase—from a software vendor, you actually purchase the software comprising a database management system (DBMS). Database management systems are designed for use by professional programmers and are not suitable for ordinary customers. Application programs are built on top of the DBMS for customers to access and update the database. Thus, application programs can be viewed as the interfaces between the database system and its users. Application programs may be stand-alone GUI applications or Web applications and may access several different database systems in the network, as shown in Figure 32.2.

Most of today’s database systems are relational database systems. They are based on the relational data model, which has three key components: structure, integrity, and language.
32.2 Relational Database Systems

Structure defines the representation of the data. Integrity imposes constraints on the data. Language provides the means for accessing and manipulating data.

32.2.1 Relational Structures

The relational model is built around a simple and natural structure. A relation is actually a table that consists of nonduplicate rows. Tables are easy to understand and use. The relational model provides a simple yet powerful way to represent data.

A row of a table represents a record, and a column of a table represents the value of a single attribute of the record. In relational database theory, a row is called a tuple and a column is called an attribute. Figure 32.3 shows a sample table that stores information about the courses offered by a university. The table has eight tuples, and each tuple has five attributes.

<table>
<thead>
<tr>
<th>courseId</th>
<th>subjectId</th>
<th>courseNumber</th>
<th>title</th>
<th>numOfCredits</th>
</tr>
</thead>
<tbody>
<tr>
<td>11111</td>
<td>CSCI</td>
<td>1301</td>
<td>Introduction to Java I</td>
<td>4</td>
</tr>
<tr>
<td>11112</td>
<td>CSCI</td>
<td>1302</td>
<td>Introduction to Java II</td>
<td>3</td>
</tr>
<tr>
<td>11113</td>
<td>CSCI</td>
<td>3720</td>
<td>Database Systems</td>
<td>3</td>
</tr>
<tr>
<td>11114</td>
<td>CSCI</td>
<td>4750</td>
<td>Rapid Java Application</td>
<td>3</td>
</tr>
<tr>
<td>11115</td>
<td>MATH</td>
<td>2750</td>
<td>Calculus I</td>
<td>5</td>
</tr>
<tr>
<td>11116</td>
<td>MATH</td>
<td>3750</td>
<td>Calculus II</td>
<td>5</td>
</tr>
<tr>
<td>11117</td>
<td>EDUC</td>
<td>1111</td>
<td>Reading</td>
<td>3</td>
</tr>
<tr>
<td>11118</td>
<td>ITEC</td>
<td>1344</td>
<td>Database Administration</td>
<td>3</td>
</tr>
</tbody>
</table>

Tables describe the relationship among data. Each row in a table represents a record of related data. For example, “11111,” “CSCI,” “1301,” “Introduction to Java I,” and “4” are related to form a record (the first row in Figure 32.3) in the Course table. Just as the data in the same row are related, so too data in different tables may be related through common attributes. Suppose the database has two other tables, Student and Enrollment, as shown in
Figures 32.4 and 32.5. The Course table and the Enrollment table are related through their common attribute courseId, and the Enrollment table and the Student table are related through ssn.

### Figure 32.4
A Student table stores student information.

<table>
<thead>
<tr>
<th>ssn</th>
<th>firstName</th>
<th>mi</th>
<th>lastName</th>
<th>phone</th>
<th>birthDate</th>
<th>street</th>
<th>zipCode</th>
<th>deptID</th>
</tr>
</thead>
<tbody>
<tr>
<td>444111110</td>
<td>Jacob</td>
<td>R</td>
<td>Smith</td>
<td>9129219434</td>
<td>1985-04-09</td>
<td>Kingston Street</td>
<td>31435</td>
<td>BIOL</td>
</tr>
<tr>
<td>444111111</td>
<td>John</td>
<td>K</td>
<td>Stevenson</td>
<td>9129219434</td>
<td>null</td>
<td>100 Main Street</td>
<td>31411</td>
<td>BIOL</td>
</tr>
<tr>
<td>444111112</td>
<td>George</td>
<td>K</td>
<td>Smith</td>
<td>9129213454</td>
<td>1974-10-10</td>
<td>1200 Abercorn St.</td>
<td>31419</td>
<td>CS</td>
</tr>
<tr>
<td>444111113</td>
<td>Frank</td>
<td>E</td>
<td>Jones</td>
<td>9125919434</td>
<td>1970-09-09</td>
<td>100 Main Street</td>
<td>31411</td>
<td>BIOL</td>
</tr>
<tr>
<td>444111114</td>
<td>Jean</td>
<td>K</td>
<td>Smith</td>
<td>9129219434</td>
<td>1970-02-09</td>
<td>100 Main Street</td>
<td>31411</td>
<td>BIOL</td>
</tr>
<tr>
<td>444111115</td>
<td>Josh</td>
<td>R</td>
<td>Woo</td>
<td>7075989434</td>
<td>1970-02-09</td>
<td>555 Franklin St.</td>
<td>31411</td>
<td>CHEM</td>
</tr>
<tr>
<td>444111116</td>
<td>Josh</td>
<td>R</td>
<td>Smith</td>
<td>9129219434</td>
<td>1973-02-09</td>
<td>100 Main Street</td>
<td>31411</td>
<td>BIOL</td>
</tr>
<tr>
<td>444111117</td>
<td>Joy</td>
<td>P</td>
<td>Kennedy</td>
<td>9129229434</td>
<td>1974-03-19</td>
<td>103 Bay Street</td>
<td>31412</td>
<td>CS</td>
</tr>
<tr>
<td>444111118</td>
<td>Toni</td>
<td>R</td>
<td>Peterson</td>
<td>9129229434</td>
<td>1964-04-29</td>
<td>103 Bay Street</td>
<td>31412</td>
<td>MATH</td>
</tr>
<tr>
<td>444111119</td>
<td>Patrick</td>
<td>R</td>
<td>Stoneman</td>
<td>9129229434</td>
<td>1969-04-29</td>
<td>101 Washington St.</td>
<td>31435</td>
<td>MATH</td>
</tr>
<tr>
<td>444111120</td>
<td>Rick</td>
<td>R</td>
<td>Carter</td>
<td>9129219434</td>
<td>1986-04-09</td>
<td>19 West Ford St.</td>
<td>31411</td>
<td>BIOL</td>
</tr>
</tbody>
</table>

### Figure 32.5
An Enrollment table stores student enrollment information.

<table>
<thead>
<tr>
<th>ssn</th>
<th>courseId</th>
<th>dateRegistered</th>
<th>grade</th>
</tr>
</thead>
<tbody>
<tr>
<td>444111110</td>
<td>11111</td>
<td>2004-03-19</td>
<td>A</td>
</tr>
<tr>
<td>444111110</td>
<td>11112</td>
<td>2004-03-19</td>
<td>B</td>
</tr>
<tr>
<td>444111110</td>
<td>11113</td>
<td>2004-03-19</td>
<td>C</td>
</tr>
<tr>
<td>444111111</td>
<td>11111</td>
<td>2004-03-19</td>
<td>D</td>
</tr>
<tr>
<td>444111111</td>
<td>11112</td>
<td>2004-03-19</td>
<td>F</td>
</tr>
<tr>
<td>444111111</td>
<td>11113</td>
<td>2004-03-19</td>
<td>A</td>
</tr>
<tr>
<td>444111112</td>
<td>11114</td>
<td>2004-03-19</td>
<td>B</td>
</tr>
<tr>
<td>444111112</td>
<td>11115</td>
<td>2004-03-19</td>
<td>C</td>
</tr>
<tr>
<td>444111112</td>
<td>11116</td>
<td>2004-03-19</td>
<td>D</td>
</tr>
<tr>
<td>444111113</td>
<td>11111</td>
<td>2004-03-19</td>
<td>A</td>
</tr>
<tr>
<td>444111113</td>
<td>11113</td>
<td>2004-03-19</td>
<td>A</td>
</tr>
<tr>
<td>444111114</td>
<td>11115</td>
<td>2004-03-19</td>
<td>B</td>
</tr>
<tr>
<td>444111115</td>
<td>11115</td>
<td>2004-03-19</td>
<td>F</td>
</tr>
<tr>
<td>444111115</td>
<td>11116</td>
<td>2004-03-19</td>
<td>F</td>
</tr>
<tr>
<td>444111116</td>
<td>11111</td>
<td>2004-03-19</td>
<td>D</td>
</tr>
<tr>
<td>444111117</td>
<td>11111</td>
<td>2004-03-19</td>
<td>D</td>
</tr>
<tr>
<td>444111118</td>
<td>11111</td>
<td>2004-03-19</td>
<td>A</td>
</tr>
<tr>
<td>444111118</td>
<td>11112</td>
<td>2004-03-19</td>
<td>D</td>
</tr>
<tr>
<td>444111118</td>
<td>11113</td>
<td>2004-03-19</td>
<td>B</td>
</tr>
</tbody>
</table>

### 32.2.2 Integrity Constraints
An integrity constraint imposes a condition that all the legal values in a table must satisfy. Figure 32.6 shows an example of some integrity constraints in the Subject and Course tables.

In general, there are three types of constraints: domain constraints, primary key constraints, and foreign key constraints. Domain constraints and primary key constraints are known as intrarelational constraints meaning that a constraint involves only one relation. The foreign key constraint is interrelational meaning that a constraint involves more than one relation.
32.2 Relational Database Systems

Domain Constraints

Domain constraints specify the permissible values for an attribute. Domains can be specified using standard data types, such as integers, floating-point numbers, fixed-length strings, and variant-length strings. The standard data type specifies a broad range of values. Additional constraints can be specified to narrow the ranges. For example, you can specify that the numOfCredits attribute (in the Course table) must be greater than 0 and less than 5. You can also specify whether an attribute can be null, which is a special value in a database meaning unknown or not applicable. As shown in the Student table, birthDate may be null.

Primary Key Constraints

To understand primary keys, it is helpful to know superkeys, keys, and candidate keys. A superkey is an attribute or a set of attributes that uniquely identifies the relation. That is, no two tuples have the same values on a superkey. By definition, a relation consists of a set of distinct tuples. The set of all attributes in the relation forms a superkey.

A key \( \mathbf{K} \) is a minimal superkey, meaning that any proper subset of \( \mathbf{K} \) is not a superkey. A relation can have several keys. In this case, each of the keys is called a candidate key. The primary key is one of the candidate keys designated by the database designer. The primary key is often used to identify tuples in a relation. As shown in Figure 32.6, courseId is the primary key in the Course table.

Foreign Key Constraints

In a relational database, data are related. Tuples in a relation are related, and tuples in different relations are related through their common attributes. Informally speaking, the common attributes are foreign keys. The foreign key constraints define the relationships among relations.

Formally, a set of attributes \( \mathbf{FK} \) is a foreign key in a relation \( \mathbf{R} \) that references relation \( \mathbf{T} \) if it satisfies the following two rules:

- The attributes in \( \mathbf{FK} \) have the same domain as the primary key in \( \mathbf{T} \).
- A nonnull value on \( \mathbf{FK} \) in \( \mathbf{R} \) must match a primary key value in \( \mathbf{T} \).
As shown in Figure 32.6, courseId is the foreign key in Enrollment that references the primary key courseId in Course. Every courseId value must match a courseId value in Course.

**Enforcing Integrity Constraints**

The database management system enforces integrity constraints and rejects operations that would violate them. For example, if you attempt to insert the new record ("11115," "CSCI," "2490," "C++ Programming," 0) into the Course table, it would fail because the credit hours must be greater than 0; if you attempted to insert a record with the same primary key as an existing record in the table, the DBMS would report an error and reject the operation; if you attempted to delete a record from the Course table whose primary key value is referenced by the records in the Enrollment table, the DBMS would reject this operation.

**Check Point**

32.1 What are superkeys, candidate keys, and primary keys?
32.2 What is a foreign key?
32.3 Can a relation have more than one primary key or foreign key?
32.4 Does a foreign key need to be a primary key in the same relation?
32.5 Does a foreign key need to have the same name as its referenced primary key?
32.6 Can a foreign key value be null?

**32.3 SQL**

*Structured Query Language (SQL) is the language for defining tables and integrity constraints, and for accessing and manipulating data.*

**Key Point**

SQL (pronounced “S-Q-L” or “sequel”) is the universal language for accessing relational database systems. Application programs may allow users to access a database without directly using SQL, but these applications themselves must use SQL to access the database. This section introduces some basic SQL commands.

**Note**

There are many relational database management systems. They share the common SQL language but do not all support every feature of SQL. Some systems have their own extensions to SQL. This section introduces standard SQL supported by all systems.

SQL can be used on MySQL, Oracle, Sybase, IBM DB2, IBM Informix, MS Access, or any other relational database system. This chapter uses MySQL to demonstrate SQL and uses MySQL, Oracle, and Access to demonstrate Java database programming. The Companion Website contains the following supplements on how to install and use three popular databases: MySQL, Oracle, and Access:

- **MySQL Tutorial**
  - Supplement IV.B: Tutorial for MySQL
- **Oracle Tutorial**
  - Supplement IV.C: Tutorial for Oracle
- **Access Tutorial**
  - Supplement IV.D: Tutorial for Microsoft Access
32.3.1 Creating a User Account on MySQL

Assume that you have installed MySQL 5 with the default configuration. To match all the examples in this book, you should create a user named `scott` with the password `tiger`. You can perform the administrative tasks using the MySQL Workbench or using the command line. MySQL Workbench is a GUI tool for managing MySQL databases. Here are the steps to create a user from the command line:

1. From the DOS command prompt, type
   
   ```
   mysql -uroot -p
   ```
   
   You will be prompted to enter the root password, as shown in Figure 32.7.

2. At the mysql prompt, enter
   
   ```
   use mysql;
   ```

3. To create user `scott` with password `tiger`, enter
   
   ```
   create user 'scott'@'localhost' identified by 'tiger';
   ```

4. To grant privileges to `scott`, enter
   
   ```
   grant select, insert, update, delete, create, create view, drop, execute, references on *.* to 'scott'@'localhost';
   ```
   
   - If you want to enable remote access of the account from any IP address, enter
     
     ```
     grant all privileges on *.* to 'scott'@'%' identified by 'tiger';
     ```
   
   - If you want to restrict the account’s remote access to just one particular IP address, enter
     
     ```
     grant all privileges on *.* to 'scott'@'ipAddress' identified by 'tiger';
     ```

5. Enter
   
   ```
   exit;
   ```

   to exit the MySQL console.

---

**Figure 32.7** You can access a MySQL database server from the command window.
By default, the server contains two databases named **mysql** and **test**. The **mysql** database contains the tables that store information about the server and its users. This database is intended for the server administrator to use. For example, the administrator can use it to create users and grant or revoke user privileges. Since you are the owner of the server installed on your system, you have full access to the **mysql** database. However, you should not create user tables in the **mysql** database. You can use the **test** database to store data or create new databases. You can also create a new database using the command `create database databasename` or delete an existing database using the command `drop database databasename`.

### 32.3.2 Creating a Database

To match the examples in this book, you should create a database named **javabook**. Here are the steps to create it:

1. From the DOS command prompt, type
   
   ```
   mysql –uscott -ptiger
   ```
   
   to login to mysql, as shown in Figure 32.8.

2. At the mysql prompt, enter
   
   ```
   create database javabook;
   ```

![Figure 32.8](image)

   **Figure 32.8** You can create databases in MySQL.

For your convenience, the SQL statements for creating and initializing tables used in this book are provided in Supplement IV.A. You can download the script for MySQL and save it to `script.sql`. To execute the script, first switch to the **javabook** database using the following command:

   ```
   use javabook;
   ```

   and then type

   ```
   source script.sql;
   ```

   as shown in Figure 32.9.
32.3 SQL

You can run SQL commands in a script file.

Note
You can populate the javabook database using the script from Supplement IV.A.

32.3.3 Creating and Dropping Tables

Tables are the essential objects in a database. To create a table, use the `create table` statement to specify a table name, attributes, and types, as in the following example:

```sql
create table Course (
    courseId char(5),
    subjectId char(4) not null,
    courseNumber integer,
    title varchar(50) not null,
    numOfCredits integer,
    primary key (courseId)
);
```

This statement creates the `Course` table with attributes `courseId`, `subjectId`, `courseNumber`, `title`, and `numOfCredits`. Each attribute has a data type that specifies the type of data stored in the attribute. `char(5)` specifies that `courseId` consists of five characters. `varchar(50)` specifies that `title` is a variant-length string with a maximum of 50 characters. `integer` specifies that `courseNumber` is an integer. The primary key is `courseId`.

The tables `Student` and `Enrollment` can be created as follows:

```sql
create table Student (
    ssn char(9),
    firstName varchar(25),
    mi char(1),
    lastName varchar(25),
    birthDate date,
    street varchar(25),
    phone char(11),
    zipCode char(5),
    deptId char(4),
    primary key (ssn)
);
```

```sql
create table Enrollment (
    ssn char(9),
    courseId char(5),
    dateRegistered date,
    grade char(1),
    primary key (ssn, courseId),
    foreign key (ssn) references Student(ssn),
    foreign key (courseId) references Course(courseId)
);
```

Note
SQL keywords are not case sensitive. This book adopts the following naming conventions: tables are named in the same way as Java classes, and attributes are named in the same way as Java variables. SQL keywords are named in the same way as Java keywords.
If a table is no longer needed, it can be dropped permanently using the `drop table` command. For example, the following statement drops the `Course` table:

```sql
drop table Course;
```

If a table to be dropped is referenced by other tables, you have to drop the other tables first. For example, if you have created the tables `Course`, `Student`, and `Enrollment` and want to drop `Course`, you have to first drop `Enrollment`, because `Course` is referenced by `Enrollment`.

Figure 32.10 shows how to enter the `create table` statement from the MySQL console.

![Figure 32.10](image_url)

**Figure 32.10** A table is created using the `create table` statement.

If you make typing errors, you have to retype the whole command. To avoid retyping, you can save the command in a file, and then run the command from the file. To do so, create a text file to contain commands, named, for example, `test.sql`. You can create the text file using any text editor, such as Notepad, as shown in Figure 32.11a. To comment a line, precede it with two dashes. You can now run the script file by typing `source test.sql` from the SQL command prompt, as shown in Figure 32.11b.

![Figure 32.11](image_url)

**Figure 32.11** (a) You can use Notepad to create a text file for SQL commands. (b) You can run the SQL commands in a script file from MySQL.

### 32.3.4 Simple Insert, Update, and Delete

Once a table is created, you can insert data into it. You can also update and delete records. This section introduces simple insert, update, and delete statements.

The syntax to insert a record into a table is:

```sql
insert into tableName [(column1, column2, ..., column)]
values (value1, value2, ..., valuen);
```
For example, the following statement inserts a record into the Course table. The new record has the courseId ‘11113’, subjectId ‘CSCI’, courseNumber ‘3720’, title ‘Database Systems’, and creditHours 3.

```sql
insert into Course (courseId, subjectId, courseNumber, title, numOfCredits)
values ('11113', 'CSCI', '3720', 'Database Systems', 3);
```

The column names are optional. If they are omitted, all the column values for the record must be entered, even though the columns have default values. String values are case sensitive and enclosed inside single quotation marks in SQL.

The syntax to update a table is:

```sql
update tableName
set column1 = newValue1 [, column2 = newValue2, ...]  
[where condition];
```

For example, the following statement changes the numOfCredits for the course whose title is Database Systems to 4.

```sql
update Course
set numOfCredits = 4
where title = 'Database Systems';
```

The syntax to delete records from a table is:

```sql
delete from tableName  
[where condition];
```

For example, the following statement deletes the Database Systems course from the Course table:

```sql
delete from Course
where title = 'Database Systems';
```

The following statement deletes all the records from the Course table:

```sql
delete from Course;
```

### 32.3.5 Simple Queries

To retrieve information from tables, use a `select` statement with the following syntax:

```sql
select column-list  
from table-list  
[where condition];
```

The `select` clause lists the columns to be selected. The `from` clause refers to the tables involved in the query. The optional `where` clause specifies the conditions for the selected rows.

**Query 1:** Select all the students in the CS department, as shown in Figure 32.12.

```sql
select firstName, mi, lastName  
from Student  
where deptId = 'CS';
```
32.3.6 Comparison and Boolean Operators

SQL has six comparison operators, as shown in Table 32.1, and three Boolean operators, as shown in Table 32.2.

<table>
<thead>
<tr>
<th>Operator</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>=</td>
<td>Equal to</td>
</tr>
<tr>
<td>&lt;&gt; or !=</td>
<td>Not equal to</td>
</tr>
<tr>
<td>&lt;</td>
<td>Less than</td>
</tr>
<tr>
<td>&lt;=</td>
<td>Less than or equal to</td>
</tr>
<tr>
<td>&gt;</td>
<td>Greater than</td>
</tr>
<tr>
<td>&gt;=</td>
<td>Greater than or equal to</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Operator</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>not</td>
<td>Logical negation</td>
</tr>
<tr>
<td>and</td>
<td>Logical conjunction</td>
</tr>
<tr>
<td>or</td>
<td>Logical disjunction</td>
</tr>
</tbody>
</table>

**Note**
The comparison and Boolean operators in SQL have the same meanings as in Java. In SQL the `equal to` operator is `=`, but in Java it is `==`. In SQL the `not equal to` operator is `<>` or `!=`, but in Java it is `!=`. The `not`, `and`, and `or` operators are `!`, `&&`, and `||` in Java.

**Query 2**: Get the names of the students who are in the CS dept and live in the ZIP code 31411.

```sql
select firstName, mi, lastName
from Student
where deptId = 'CS' and zipCode = '31411';
```

**Note**
To select all the attributes from a table, you don’t have to list all the attribute names in the `select` clause. Instead, you can just use an asterisk (*), which stands for all the attributes. For example, the following query displays all the attributes of the students who are in the CS dept and live in ZIP code 31411.

```sql
select *
from Student
where deptId = 'CS' and zipCode = '31411';
```
32.3.7 The like, between-and, and is null Operators

SQL has a like operator that can be used for pattern matching. The syntax to check whether a string $s$ has a pattern $p$ is

$$ s \text{ like } p \text{ or } s \text{ not like } p $$

You can use the wildcard characters `%` (percent symbol) and `_` (underline symbol) in the pattern $p$. `%` matches zero or more characters, and `_` matches any single character in $s$. For example, `lastName like '_mi%'` matches any string whose second and third letters are m and i. `lastName not like '_mi%'` excludes any string whose second and third letters are m and i.

Note
In earlier versions of MS Access, the wildcard character is *, and the character ? matches any single character.

The between-and operator checks whether a value $v$ is between two other values, $v_1$ and $v_2$, using the following syntax:

$$ v \text{ between } v_1 \text{ and } v_2 \text{ or } v \text{ not between } v_1 \text{ and } v_2 $$

$v$ between $v_1$ and $v_2$ is equivalent to $v \geq v_1$ and $v \leq v_2$, and $v$ not between $v_1$ and $v_2$ is equivalent to $v < v_1$ or $v > v_2$.

The is null operator checks whether a value $v$ is null using the following syntax:

$$ v \text{ is null } \text{ or } v \text{ is not null } $$

Query 3: Get the Social Security numbers of the students whose grades are between ‘C’ and ‘A’.

```
select ssn
from Enrollment
where grade between 'C' and 'A';
```

32.3.8 Column Alias

When a query result is displayed, SQL uses the column names as column headings. Usually the user gives abbreviated names for the columns, and the columns cannot have spaces when the table is created. Sometimes it is desirable to give more descriptive names in the result heading. You can use the column aliases with the following syntax:

```
select columnName [as] alias
```

Query 4: Get the last name and ZIP code of the students in the CS department. Display the column headings as “Last Name” for lastName and “Zip Code” for zipCode. The query result is shown in Figure 32.13.

```
Query 32.13 You can use a column alias in the display.
```
Chapter 32  Java Database Programming

```
select lastName as "Last Name", zipCode as "Zip Code"
from Student
where deptId = 'CS';
```

**Note**
The `as` keyword is optional in MySQL and Oracle, but it is required in MS Access.

### 32.3.9  The Arithmetic Operators

You can use the arithmetic operators `*` (multiplication), `/` (division), `+` (addition), and `-` (subtraction) in SQL.

**Query 5:** Assume that a credit hour is 50 minutes of lectures and get the total minutes for each course with the subject CSCI. The query result is shown in Figure 32.14.

```
select title, 50 * numOfCredits as "Lecture Minutes Per Week"
from Course
where subjectId = 'CSCI';
```

![Figure 32.14](image1)

You can use arithmetic operators in SQL.

### 32.3.10  Displaying Distinct Tuples

SQL provides the `distinct` keyword, which can be used to eliminate duplicate tuples in the result. Figure 32.15a displays all the subject IDs used by the courses, and Figure 32.15b displays all the distinct subject IDs used by the courses using the following statement.

```
select distinct subjectId as "Subject ID"
from Course;
```

![Figure 32.15](image2)

(a) The duplicate tuples are displayed. (b) The distinct tuples are displayed.
When there is more than one column in the `select` clause, the `distinct` keyword applies to the whole tuple in the result. For example, the following statement displays all tuples with distinct `subjectId` and `title`, as shown in Figure 32.16. Note that some tuples may have the same `subjectId` but different `title`. These tuples are distinct.

```sql
select distinct subjectId, title
from Course;
```

![Figure 32.16](image)
The keyword `distinct` applies to the entire tuple.

### 32.3.11 Displaying Sorted Tuples

SQL provides the `order by` clause to sort the output using the following syntax:

```sql
select column-list
from table-list
[where condition]
[order by columns-to-be-sorted];
```

In the syntax, `columns-to-be-sorted` specifies a column or a list of columns to be sorted. By default, the order is ascending. To sort in a descending order, append the `desc` keyword. You could also append the `asc` keyword after `columns-to-be-sorted`, but it is not necessary. When multiple columns are specified, the rows are sorted based on the first column, then the rows with the same values on the first column are sorted based on the second column, and so on.

**Query 6:** List the full names of the students in the CS department, ordered primarily on their last names in descending order and secondarily on their first names in ascending order. The query result is shown in Figure 32.17.

![Figure 32.17](image)
You can sort results using the `order by` clause.
select lastName, firstName, deptId
from Student
where deptId = 'CS'
order by lastName desc, firstName asc;

32.3.12 Joining Tables

Often you need to get information from multiple tables, as demonstrated in the next query. 

Query 7: List the courses taken by the student Jacob Smith. To solve this query, you need to join tables Student and Enrollment, as shown in Figure 32.18.

![Figure 32.18](image)

You can write the query in SQL:

```sql
select distinct lastName, firstName, courseId
from Student, Enrollment
where Student.ssn = Enrollment.ssn and
  lastName = 'Smith' and firstName = 'Jacob';
```

The tables Student and Enrollment are listed in the from clause. The query examines every pair of rows, each made of one item from Student and another from Enrollment and selects the pairs that satisfy the condition in the where clause. The rows in Student have the last name, Smith, and the first name, Jacob, and both rows from Student and Enrollment have the same ssn values. For each pair selected, lastName and firstName from Student and courseId from Enrollment are used to produce the result, as shown in Figure 32.19. Student and Enrollment have the same attribute ssn. To distinguish them in a query, use Student.ssn and Enrollment.ssn.

![Figure 32.19](image)
For more features of SQL, see Supplements IV.H and IV.I.

32.7 Create the tables Course, Student, and Enrollment using the create table statements in Section 32.3.3, Creating and Dropping Tables. Insert rows into the Course, Student, and Enrollment tables using the data in Figures 32.3–32.5.

32.8 List all CSCI courses with at least four credit hours.
32.9 List all students whose last names contain the letter e two times.
32.10 List all students whose birthdays are null.
32.11 List all students who take Math courses.
32.12 List the number of courses in each subject.
32.13 Assume that each credit hour is 50 minutes of lectures. Get the total minutes for the courses that each student takes.

32.4 JDBC

_JDBC is the Java API for accessing relational database._

The Java API for developing Java database applications is called _JDBC_. JDBC is the trade-marked name of a Java API that supports Java programs that access relational databases. JDBC is not an acronym, but it is often thought to stand for Java Database Connectivity.

JDBC provides Java programmers with a uniform interface for accessing and manipulating relational databases. Using the JDBC API, applications written in the Java programming language can execute SQL statements, retrieve results, present data in a user-friendly interface, and propagate changes back to the database. The JDBC API can also be used to interact with multiple data sources in a distributed, heterogeneous environment.

The relationships between Java programs, JDBC API, JDBC drivers, and relational databases are shown in Figure 32.20. The JDBC API is a set of Java interfaces and classes used to write Java programs for accessing and manipulating relational databases. Since a JDBC driver serves as the interface to facilitate communications between JDBC and a proprietary database, JDBC drivers are database specific and are normally provided by the database vendors. You need MySQL JDBC drivers to access the MySQL database, and Oracle JDBC drivers

![Figure 32.20](image-url)
to access the Oracle database. For the Access database, use the JDBC-ODBC bridge driver included in the JDK. ODBC is a technology developed by Microsoft for accessing databases on the Windows platform. An ODBC driver is preinstalled on Windows. The JDBC-ODBC bridge driver allows a Java program to access any ODBC data source.

32.4.1 Developing Database Applications Using JDBC

The JDBC API is a Java application program interface to generic SQL databases that enables Java developers to develop DBMS-independent Java applications using a uniform interface.

The JDBC API consists of classes and interfaces for establishing connections with databases, sending SQL statements to databases, processing the results of SQL statements, and obtaining database metadata. Four key interfaces are needed to develop any database application using Java: **Driver**, **Connection**, **Statement**, and **ResultSet**. These interfaces define a framework for generic SQL database access. The JDBC API defines these interfaces, and the JDBC driver vendors provide the implementation for the interfaces. Programmers use these interfaces.

The relationship of these interfaces is shown in Figure 32.21. A JDBC application loads an appropriate driver using the **Driver** interface, connects to the database using the **Connection** interface, creates and executes SQL statements using the **Statement** interface, and processes the result using the **ResultSet** interface if the statements return results. Note that some statements, such as SQL data definition statements and SQL data modification statements, do not return results.

The JDBC interfaces and classes are the building blocks in the development of Java database programs. A typical Java program takes the following steps to access a database.

1. Loading drivers.

An appropriate driver must be loaded using the statement shown below before connecting to a database.

   ```java
   Class.forName("JDBCDriverClass");
   ```

A driver is a concrete class that implements the **java.sql.Driver** interface. The drivers for Access, MySQL, and Oracle are listed in Table 32.3. If your program accesses several different databases, all their respective drivers must be loaded.

The JDBC-ODBC driver for Access is bundled in JDK. The most recent platform-independent version of MySQL JDBC driver is **mysql-connector-java-5.1.26.jar**. This file is contained in a ZIP file downloadable from dev.mysql.com/downloads/connector/j/. The most recent version of Oracle JDBC driver is **ojdbc6.jar** (downloadable from www.oracle.com/technetwork/database/enterprise-edition/jdbc-112010-090769.html). To use the MySQL and
Oracle drivers, you have to add `mysql-connector-java-5.1.26.jar` and `ojdbc6.jar` in the classpath using the following DOS command on Windows:

```
set classpath=%classpath%;c:\book\lib\mysql-connector-java-5.1.26.jar;
                 c:\book\lib\ojdbc6.jar
```

If you use an IDE such as Eclipse or NetBeans, you need to add these jar files into the library in the IDE.

**Note**

`com.mysql.jdbc.Driver` is a class in `mysql-connector-java-5.1.26.jar`, and `oracle.jdbc.driver.OracleDriver` is a class in `ojdbc6.jar`. `mysql-connector-java-5.1.26.jar`, and `ojdbc6.jar` contains many classes to support the driver. These classes are used by JDBC but not directly by JDBC programmers. When you use a class explicitly in the program, it is automatically loaded by the JVM. The driver classes, however, are not used explicitly in the program, so you have to write the code to tell the JVM to load them.

**Note**

Java 6 supports automatic driver discovery, so you don’t have to load the driver explicitly. At the time of this writing, however, this feature is not supported for all database drivers. To be safe, load the driver explicitly.

2. Establishing connections.

To connect to a database, use the static method `getConnection(databaseURL)` in the `DriverManager` class, as follows:

```
Connection connection = DriverManager.getConnection(databaseURL);
```

where `databaseURL` is the unique identifier of the database on the Internet. Table 32.4 lists the URL patterns for the Access, MySQL, and Oracle databases.

### Table 32.4  JDBC URLs

<table>
<thead>
<tr>
<th>Database</th>
<th>URL Pattern</th>
</tr>
</thead>
<tbody>
<tr>
<td>Access</td>
<td>jdbc:odbc:datasource</td>
</tr>
<tr>
<td>MySQL</td>
<td>jdbc:mysql://hostname/dbname</td>
</tr>
<tr>
<td>Oracle</td>
<td>jdbc:oracle:thin:@hostname:port#::oracleDBSID</td>
</tr>
</tbody>
</table>

For an ODBC data source, the `databaseURL` is `jdbc:odbc:datasource`. An ODBC data source can be created using the ODBC Data Source Administrator on Windows. See Supplement IV.D, Tutorial for Microsoft Access, on how to create an ODBC data source for an Access database.
Suppose a data source named ExampleMDBDataSource has been created for an Access database. The following statement creates a Connection object:

```java
Connection connection = DriverManager.getConnection("jdbc:odbc:ExampleMDBDataSource");
```

The databaseURL for a MySQL database specifies the host name and database name to locate a database. For example, the following statement creates a Connection object for the local MySQL database javabook with username scott and password tiger:

```java
Connection connection = DriverManager.getConnection("jdbc:mysql://localhost/javabook", "scott", "tiger");
```

Recall that by default, MySQL contains two databases named mysql and test. Section 32.3.2, Creating a Database, created a custom database named javabook. We will use javabook in the examples.

The databaseURL for an Oracle database specifies the hostname, the port# where the database listens for incoming connection requests, and the oracleDBSID database name to locate a database. For example, the following statement creates a Connection object for the Oracle database on liang.armstrong.edu with the username scott and password tiger:

```java
Connection connection = DriverManager.getConnection("jdbc:oracle:thin:@liang.armstrong.edu:1521:orcl", "scott", "tiger");
```

3. Creating statements.

If a Connection object can be envisioned as a cable linking your program to a database, an object of Statement can be viewed as a cart that delivers SQL statements for execution by the database and brings the result back to the program. Once a Connection object is created, you can create statements for executing SQL statements as follows:

```java
Statement statement = connection.createStatement();
```

4. Executing statements.

SQL data definition language (DDL) and update statements can be executed using `executeUpdate(String sql)`, and an SQL query statement can be executed using `executeQuery(String sql)`. The result of the query is returned in ResultSet. For example, the following code executes the SQL statement `create table Temp (col1 char(5), col2 char(5))`:

```java
statement.executeUpdate("create table Temp (col1 char(5), col2 char(5))");
```

This next code executes the SQL query `select firstName, mi, lastName from Student where lastName = 'Smith'`:

```java
// Select the columns from the Student table
ResultSet resultSet = statement.executeQuery("select firstName, mi, lastName from Student where lastName = 'Smith'");
```

5. Processing ResultSet.

The ResultSet maintains a table whose current row can be retrieved. The initial row position is null. You can use the next method to move to the next row and the various getter methods to retrieve values from a current row. For example, the following code displays all the results from the preceding SQL query.

```java
// Iterate through the result and print the student names
while (resultSet.next())
```
System.out.println(resultSet.getString(1) + " " +
resultSet.getString(2) + " " + resultSet.getString(3));

The `getString(1)`, `getString(2)`, and `getString(3)` methods retrieve the column values for `firstName`, `mi`, and `lastName`, respectively. Alternatively, you can use `getString("firstName")`, `getString("mi")`, and `getString("lastName")` to retrieve the same three column values. The first execution of the `next()` method sets the current row to the first row in the result set, and subsequent invocations of the `next()` method set the current row to the second row, third row, and so on, to the last row.

Listing 32.1 is a complete example that demonstrates connecting to a database, executing a simple query, and processing the query result with JDBC. The program connects to a local MySQL database and displays the students whose last name is Smith.

**Listing 32.1 SimpleJDBC.java**

```java
ing
import java.sql.*;

public class SimpleJdbc {
  public static void main(String[] args)
    throws SQLException, ClassNotFoundException {
    // Load the JDBC driver
    Class.forName("com.mysql.jdbc.Driver");
    System.out.println("Driver loaded");

    // Connect to a database
    Connection connection = DriverManager.getConnection
      ("jdbc:mysql://localhost/javabook", "scott", "tiger");
    System.out.println("Database connected");

    // Create a statement
    Statement statement = connection.createStatement();

    // Execute a statement
    ResultSet resultSet = statement.executeQuery
      ("select firstName, mi, lastName from Student where lastName " + "+ = 'Smith'");

    // Iterate through the result and print the student names
    while (resultSet.next())
      System.out.println(resultSet.getString(1) + "\t" +
        resultSet.getString(2) + "\t" + resultSet.getString(3));

    // Close the connection
    connection.close();
  }
}
```

The statement in line 7 loads a JDBC driver for MySQL, and the statement in lines 11–13 connects to a local MySQL database. You can change them to connect to an Access or Oracle database. The program creates a `Statement` object (line 16), executes an SQL statement and returns a `ResultSet` object (lines 19–21), and retrieves the query result from the `ResultSet` object (lines 24–26). The last statement (line 29) closes the connection and releases resources related to the connection. You can rewrite this program using the try-with-resources syntax. See [www.cs.armstrong.edu/liang/intro10e/html/SimpleJdbcWithAutoClose.html](http://www.cs.armstrong.edu/liang/intro10e/html/SimpleJdbcWithAutoClose.html).

**Note**

If you run this program from the DOS prompt, specify the appropriate driver in the classpath, as shown in Figure 32.22.
The classpath directory and jar files are separated by commas. The period (.) represents the current directory. For convenience, the driver files are placed under the \c:\book\lib directory.

**Caution**
Do not use a semicolon (;) to end the Oracle SQL command in a Java program. The semicolon may not work with the Oracle JDBC drivers. It does work, however, with the other drivers used in this book.

**Note**
The Connection interface handles transactions and specifies how they are processed. By default, a new connection is in autocommit mode, and all its SQL statements are executed and committed as individual transactions. The commit occurs when the statement completes or the next execute occurs, whichever comes first. In the case of statements returning a result set, the statement completes when the last row of the result set has been retrieved or the result set has been closed. If a single statement returns multiple results, the commit occurs when all the results have been retrieved. You can use the setAutoCommit(false) method to disable autocommit, so that all SQL statements are grouped into one transaction that is terminated by a call to either the commit() or the rollback() method. The rollback() method undoes all the changes made by the transaction.

### 32.4.2 Accessing a Database from JavaFX
This section gives an example that demonstrates connecting to a database from a JavaFX program. The program lets the user enter the SSN and the course ID to find a student’s grade, as shown in Figure 32.23. The code in Listing 32.2 uses the MySQL database on the localhost.

![Figure 32.22](image)

You must include the driver file to run Java database programs.

![Figure 32.23](image)

A JavaFX client can access the database on the server.

**Listing 32.2** FindGrade.java

```java
1 import javafx.application.Application;
2 import javafx.scene.Scene;
3 import javafx.scene.control.Button;
4 import javafx.scene.control.Label;
5 import javafx.scene.control.TextField;
6 import javafx.scene.layout.HBox;
7 import javafx.scene.layout.VBox;
8 import javafx.stage.Stage;
9 import java.sql.*;
```
public class FindGrade extends Application {
    // Statement for executing queries
    private Statement stmt;
    private TextField tfSSN = new TextField();
    private TextField tfCourseId = new TextField();
    private Label lblStatus = new Label();

    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        // Initialize database connection and create a Statement object
        initializeDB();
        Button btShowGrade = new Button("Show Grade");
        HBox hBox = new HBox(5);
        hBox.getChildren().addAll(new Label("SSN"), tfSSN,
                                   new Label("Course ID"), tfCourseId, (btShowGrade));
        VBox vBox = new VBox(10);
        vBox.getChildren().addAll(hBox, lblStatus);
        tfSSN.setPrefColumnCount(6);
        tfCourseId.setPrefColumnCount(6);
        btShowGrade.setOnAction(e -> showGrade());
        // Create a scene and place it in the stage
        Scene scene = new Scene(vBox, 420, 80);
        primaryStage.setTitle("FindGrade"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }

    private void initializeDB() {
        try {
            Class.forName("com.mysql.jdbc.Driver");
            System.out.println("Driver loaded");
            Connection connection = DriverManager.getConnection("jdbc:mysql://localhost/javabook", "scott", "tiger");
            System.out.println("Database connected");
            // Create a statement
            stmt = connection.createStatement();
        } catch (Exception ex) {
            ex.printStackTrace();
        }
    }

    private void showGrade() {
        String ssn = tfSSN.getText();
        String courseId = tfCourseId.getText();
        try {
            String queryString = "select firstName, mi, " +
                                 "lastName, title, grade from Student, Enrollment, Course " +
                                 "where studentId = ? and courseId = ?";
            PreparedStatement pstmt = connection.prepareStatement(queryString);
            pstmt.setString(1, ssn);
            pstmt.setString(2, courseId);
            ResultSet rs = pstmt.executeQuery();
            while (rs.next()) {
                String firstName = rs.getString("firstName");
                String mi = rs.getString("mi");
                String lastName = rs.getString("lastName");
                String title = rs.getString("title");
                int grade = rs.getInt("grade");
                lblStatus.setText("First Name: " + firstName + ", " + mi + ", Last Name: " + lastName + ", Title: " + title + ", Grade: " + grade);
            }
        } catch (SQLException e) {
            e.printStackTrace();
        }
    }
}

button listener
load driver
Oracle driver commented
connect to MySQL database
connect to Oracle commented
create statement
show result
execute statement
"where Student.ssn = "' + ssn + "' and Enrollment.courseId " + "+" = "' + courseId + 
"' and Enrollment.courseId = Course.courseId " + 
" and Enrollment.ssn = Student.ssn";

ResultSet rset = stmt.executeQuery(queryString);

if (rset.next()) {
    String lastName = rset.getString(1);
    String mi = rset.getString(2);
    String firstName = rset.getString(3);
    String title = rset.getString(4);
    String grade = rset.getString(5);

    // Display result in a label
    lblStatus.setText(firstName + " " + mi + 
        " " + lastName + "'s grade on course " + title + " is " + 
        grade);
} else {
    lblStatus.setText("Not found");
}

} catch (SQLException ex) {
    ex.printStackTrace();
}

The initializeDB() method (lines 42–62) loads the MySQL driver (line 45), connects to the MySQL database on host liang.armstrong.edu (lines 50–51) and creates a statement (line 57).

Note
There is a security hole in this program. If you enter '1' or true or '1 in the SSN field, you will get the first student's score, because the query string now becomes

```
select firstName, mi, lastName, title, grade
from Student, Enrollment, Course
where Student.ssn = '1' or true or '1' and
    Enrollment.courseId = '' and
    Enrollment.courseId = Course.courseId and
    Enrollment.ssn = Student.ssn;
```

You can avoid this problem by using the PreparedStatement interface, which is discussed in the next section.

Check Point

32.14 What are the advantages of developing database applications using Java?
32.15 Describe the following JDBC interfaces: Driver, Connection, Statement, and ResultSet.
32.16 How do you load a JDBC driver? What are the driver classes for MySQL, Access, and Oracle?
32.17 How do you create a database connection? What are the URLs for MySQL, Access, and Oracle?
32.18 How do you create a Statement and execute an SQL statement?
32.19 How do you retrieve values in a ResultSet?
32.20 Does JDBC automatically commit a transaction? How do you set autocommit to false?
32.5 PreparedStatement

preparedStatement enables you to create parameterized SQL statements.

Once a connection to a particular database is established, it can be used to send SQL statements from your program to the database. The Statement interface is used to execute static SQL statements that don’t contain any parameters. The PreparedStatement interface, extending Statement, is used to execute a precompiled SQL statement with or without parameters. Since the SQL statements are precompiled, they are efficient for repeated executions.

A PreparedStatement object is created using the prepareStatement method in the Connection interface. For example, the following code creates a PreparedStatement for an SQL insert statement:

```java
PreparedStatement preparedStatement = connection.prepareStatement(
    "insert into Student (firstName, mi, lastName) 
    values (?, ?, ?)");
```

This insert statement has three question marks as placeholders for parameters representing values for firstName, mi, and lastName in a record of the Student table.

As a subinterface of Statement, the PreparedStatement interface inherits all the methods defined in Statement. It also provides the methods for setting parameters in the object of PreparedStatement. These methods are used to set the values for the parameters before executing statements or procedures. In general, the setter methods have the following name and signature:

```java
setX(int parameterIndex, X value);
```

where X is the type of the parameter, and parameterIndex is the index of the parameter in the statement. The index starts from 1. For example, the method setString(int parameterIndex, String value) sets a String value to the specified parameter.

The following statements pass the parameters "Jack", "A", and "Ryan" to the placeholders for firstName, mi, and lastName in preparedStatement:

```java
preparedStatement.setString(1, "Jack");
preparedStatement.setString(2, "A");
preparedStatement.setString(3, "Ryan");
```

After setting the parameters, you can execute the prepared statement by invoking executeQuery() for a SELECT statement and executeUpdate() for a DDL or update statement.

The executeQuery() and executeUpdate() methods are similar to the ones defined in the Statement interface except that they don’t have any parameters, because the SQL statements are already specified in the prepareStatement method when the object of PreparedStatement is created.

Using a prepared SQL statement, Listing 32.2 can be improved as in Listing 32.3.

**Listing 32.3** FindGradeUsingPreparedStatement.java

```java
import javafx.application.Application;
import javafx.scene.Scene;
import javafx.scene.control.Button;
import javafx.scene.control.Label;
import javafx.scene.control.TextField;
import javafx.scene.layout.HBox;
import javafx.scene.layout.VBox;
import javafx.stage.Stage;
import java.sql.*;
```
public class FindGradeUsingPreparedStatement extends Application {
    // PreparedStatement for executing queries
    private PreparedStatement preparedStatement;
    private TextField tfSSN = new TextField();
    private TextField tfCourseId = new TextField();
    private Label lblStatus = new Label();

    @Override // Override the start method in the Application class
    public void start(Stage primaryStage) {
        initializeDB();

        Button btShowGrade = new Button("Show Grade");
        HBox hBox = new HBox(5);
        hBox.getChildren().addAll(new Label("SSN"), tfSSN,
            new Label("Course ID"), tfCourseId, btShowGrade);

        VBox vBox = new VBox(10);
        vBox.getChildren().addAll(hBox, lblStatus);

        tfSSN.setPrefColumnCount(6);
        tfCourseId.setPrefColumnCount(6);
        btShowGrade.setOnAction(e -> showGrade());

        Scene scene = new Scene(vBox, 420, 80);
        primaryStage.setTitle("FindGrade"); // Set the stage title
        primaryStage.setScene(scene); // Place the scene in the stage
        primaryStage.show(); // Display the stage
    }

    private void initializeDB() {
        try {
            Class.forName("com.mysql.jdbc.Driver");
            Connection connection = DriverManager.getConnection("jdbc:mysql://localhost/javabook", "scott", "tiger");
            System.out.println("Database connected");

            String queryString = "select firstName, mi, " +
                                "lastName, title, grade from Student, Enrollment, Course " +
                                "where Student.ssn = ? and Enrollment.courseId = ? " +
                                "and Enrollment.courseId = Course.courseId";

            preparedStatement = connection.prepareStatement(queryString);
        } catch (Exception ex) {
            ex.printStackTrace();
        }
    }

    private void showGrade() {
        String ssn = tfSSN.getText();
71      String courseId = tfCourseId.getText();
72
73    try {
74        preparedStatement.setString(1, ssn);
75        preparedStatement.setString(2, courseId);
76        ResultSet rset = preparedStatement.executeQuery();
77
78        if (rset.next()) {
79            String lastName = rset.getString(1);
80            String mi = rset.getString(2);
81            String firstName = rset.getString(3);
82            String title = rset.getString(4);
83            String grade = rset.getString(5);
84
85            // Display result in a label
86            lblStatus.setText(firstName + " " + mi + " " + lastName + "'s grade on course " + title + " is " + grade);
87        } else {
88            lblStatus.setText("Not found");
89        }
90    } catch (SQLException ex) {
91        ex.printStackTrace();
92    }
93  }
94
This example does exactly the same thing as Listing 32.2 except that it uses the prepared statement to dynamically set the parameters. The code in this example is almost the same as in the preceding example. The new code is highlighted.

A prepared query string is defined in lines 56–59 with ssn and courseId as parameters. An SQL prepared statement is obtained in line 62. Before executing the query, the actual values of ssn and courseId are set to the parameters in lines 73–74. Line 75 executes the prepared statement.


32.22 What are the benefits of using prepared statements?

32.6 CallableStatement

CallableStatement enables you to execute SQL stored procedures.

The CallableStatement interface is designed to execute SQL-stored procedures. The procedures may have IN, OUT or IN OUT parameters. An IN parameter receives a value passed to the procedure when it is called. An OUT parameter returns a value after the procedure is completed, but it doesn’t contain any value when the procedure is called. An IN OUT parameter contains a value passed to the procedure when it is called and returns a value after it is completed. For example, the following procedure in Oracle PL/SQL has IN parameter p1, OUT parameter p2, and IN OUT parameter p3.

    create or replace procedure sampleProcedure
        (p1 in varchar, p2 out number, p3 in out integer) is
    begin
        /* do something */
    end sampleProcedure;
    /
A CallableStatement object can be created using the prepareCall(String call) method in the Connection interface. For example, the following code creates a CallableStatement cstmt on Connection connection for the procedure sampleProcedure.

```java
CallableStatement callableStatement = connection.prepareCall(
    "{call sampleProcedure(?, ?, ?)}"
);
```

{call sampleProcedure(?, ?, ...)} is referred to as the SQL escape syntax, which signals the driver that the code within it should be handled differently. The driver parses the escape syntax and translates it into code that the database understands. In this example, sampleProcedure is an Oracle procedure. The call is translated to the string begin sampleProcedure(? , ?, ?); end and passed to an Oracle database for execution.

You can call procedures as well as functions. The syntax to create an SQL callable statement for a function is:

```java
{? = call functionName(?, ?, ...)}
```

CallableStatement inherits PreparedStatement. Additionally, the CallableStatement interface provides methods for registering the OUT parameters and for getting values from the OUT parameters.

Before calling an SQL procedure, you need to use appropriate setter methods to pass values to IN and IN OUT parameters, and use registerOutParameter to register OUT and IN OUT parameters. For example, before calling procedure sampleProcedure, the following statements pass values to parameters p1 (IN) and p3 (IN OUT) and register parameters p2 (OUT) and p3 (IN OUT):

```java
callableStatement.setString(1, "Dallas"); // Set Dallas to p1
callableStatement.setLong(3, 1); // Set 1 to p3
// Register OUT parameters
callableStatement.registerOutParameter(2, java.sql.Types.DOUBLE);
callableStatement.registerOutParameter(3, java.sql.Types.INTEGER);
```

You can use execute() or executeUpdate() to execute the procedure depending on the type of SQL statement, then use getter methods to retrieve values from the OUT parameters. For example, the next statements retrieve the values from parameters p2 and p3.

```java
double d = callableStatement.getDouble(2);
int i = callableStatement.getInt(3);
```

Let us define a MySQL function that returns the number of the records in the table that match the specified firstName and lastName in the Student table.

```sql
/* For the callable statement example. Use MySQL version 5 */
drop function if exists studentFound;

delimiter //

create function studentFound(first varchar(20), last varchar(20)) returns int begin
    declare result int;
    select count(*) into result
```
from Student
where Student.firstName = first and
   Student.lastName = last;

return result;
end;
//
/* Please note that there is a space between delimiter and ; */

If you use an Oracle database, the function can be defined as follows:

cREATE OR REPLACE FUNCTION studentFound
  (first VARCHAR2, last VARCHAR2)
  /* Do not name firstName and lastName. */
  RETURN NUMBER IS
    numberOfSelectedRows NUMBER := 0;
BEGIN
  SELECT COUNT(*) INTO numberOfSelectedRows
  FROM Student
  WHERE Student.firstName = first and
        Student.lastName = last;

  RETURN numberOfSelectedRows;
END studentFound;
/

Suppose the function studentFound is already created in the database. Listing 32.4 gives an example that tests this function using callable statements.

LISTING 32.4 TestCallableStatement.java

```java
import java.sql.*;

public class TestCallableStatement {
    public static void main(String[] args) throws Exception {
        Class.forName("com.mysql.jdbc.Driver");
        Connection connection = DriverManager.getConnection("jdbc:mysql://localhost/javabook", "scott", "tiger");

        CallableStatement callableStatement = connection.prepareCall("{? = call studentFound(?, ?)}");

        java.util.Scanner input = new java.util.Scanner(System.in);
        System.out.print("Enter student’s first name: ");
        String firstName = input.nextLine();
        System.out.print("Enter student’s last name: ");
        String lastName = input.nextLine();

        callableStatement.setString(2, firstName);
        callableStatement.setString(3, lastName);
        callableStatement.registerOutParameter(1, java.sql.Types.INTEGER);
        callableStatement.execute();
    }
}
```

32.6 CallableStatement 1201
```java
if (callableStatement.getInt(1) >= 1)
    System.out.println(firstName + " " + lastName + " is in the database");
else
    System.out.println(firstName + " " + lastName + " is not in the database");
```

Enter student's first name: Jacob
Enter student's last name: Smith
Jacob Smith is in the database

Enter student's first name: John
Enter student's last name: Smith
John Smith is not in the database

The program loads a MySQL driver (line 6), connects to a MySQL database (lines 7–9), and creates a callable statement for executing the function `studentFound` (lines 15–16).

The function’s first parameter is the return value; its second and third parameters correspond to the first and last names. Before executing the callable statement, the program sets the first name and last name (lines 24–25) and registers the `OUT` parameter (line 26). The statement is executed in line 27.

The function’s return value is obtained in line 29. If the value is greater than or equal to 1, the student with the specified first and last name is found in the table.

32.23 Describe callable statements. How do you create instances of `CallableStatement`? How do you execute a `CallableStatement`? How do you register `OUT` parameters in a `CallableStatement`?

32.7 Retrieving Metadata

The database metadata such as database URL, username, JDBC driver name can be obtained using the `DatabaseMetaData` interface and result set metadata such as table column count and column names can be obtained using the `ResultSetMetaData` interface.

JDBC provides the `DatabaseMetaData` interface for obtaining database-wide information, and the `ResultSetMetaData` interface for obtaining information on a specific `ResultSet`.

32.7.1 Database Metadata

The `Connection` interface establishes a connection to a database. It is within the context of a connection that SQL statements are executed and results are returned. A connection also provides access to database metadata information that describes the capabilities of the database, supported SQL grammar, stored procedures, and so on. To obtain an instance of `DatabaseMetaData` for a database, use the `getMetaData` method on a `Connection` object like this:

```java
DatabaseMetaData dbMetaData = connection.getMetaData();
```

If your program connects to a local MySQL database, the program in Listing 32.5 displays the database information statements shown in Figure 32.24.
Listing 32.5 TestDatabaseMetaData.java

```java
import java.sql.*;

public class TestDatabaseMetaData {
    public static void main(String[] args) throws SQLException, ClassNotFoundException {
        // Load the JDBC driver
        Class.forName("com.mysql.jdbc.Driver");
        System.out.println("Driver loaded");

        // Connect to a database
        Connection connection = DriverManager.getConnection("jdbc:mysql://localhost/javabook", "scott", "tiger");
        System.out.println("Database connected");

        DatabaseMetaData dbMetaData = connection.getMetaData();
        System.out.println("database URL: " + dbMetaData.getURL());
        System.out.println("database username: " + dbMetaData.getUserName());
        System.out.println("database product name: " + dbMetaData.getDatabaseProductName());
        System.out.println("database product version: " + dbMetaData.getDatabaseProductVersion());
        System.out.println("JDBC driver name: " + dbMetaData.getDriverName());
        System.out.println("JDBC driver version: " + dbMetaData.getDriverVersion());
        System.out.println("JDBC driver major version: " + dbMetaData.getDriverMajorVersion());
        System.out.println("JDBC driver minor version: " + dbMetaData.getDriverMinorVersion());
        System.out.println("Max number of connections: " + dbMetaData.getMaxConnections());
        System.out.println("MaxTableNameLength: " + dbMetaData.getMaxTableNameLength());
        System.out.println("MaxColumnsInTable: " + dbMetaData.getMaxColumnsInTable());

        // Close the connection
        connection.close();
    }
}
```

Figure 32.24 The DatabaseMetaData interface enables you to obtain database information.
32.7.2 Obtaining Database Tables

You can identify the tables in the database through database metadata using the `getTables` method. Listing 32.6 displays all the user tables in the javabook database on a local MySQL database. Figure 32.25 shows a sample output of the program.

**Listing 32.6  FindUserTables.java**

```java
import java.sql.*;

public class FindUserTables {
    public static void main(String[] args)
        throws SQLException, ClassNotFoundException {
        // Load the JDBC driver
        Class.forName("com.mysql.jdbc.Driver");
        System.out.println("Driver loaded");

        // Connect to a database
        Connection connection = DriverManager.getConnection("jdbc:mysql://localhost/javabook", "scott", "tiger");
        System.out.println("Database connected");

        DatabaseMetaData dbMetaData = connection.getMetaData();

        ResultSet rsTables = dbMetaData.getTables(null, null, null,
            new String[] {"TABLE"});
        System.out.print("User tables: ");
        while (rsTables.next())
            System.out.print(rsTables.getString("TABLE_NAME") + " ");

        // Close the connection
        connection.close();
    }
}
```

**Figure 32.25** You can find all the tables in the database.

Line 17 obtains table information in a result set using the `getTables` method. One of the columns in the result set is `TABLE_NAME`. Line 21 retrieves the table name from this result set column.

32.7.3 Result Set Metadata

The `ResultSetMetaData` interface describes information pertaining to the result set. A `ResultSetMetaData` object can be used to find the types and properties of the columns in a `ResultSet`. To obtain an instance of `ResultSetMetaData`, use the `getMetaData` method on a result set like this.

```
ResultSetMetaData rsMetaData = resultSet.getMetaData();
```
You can use the `getColumnCount()` method to find the number of columns in the result and the `getColumnName(int)` method to get the column names. For example, Listing 32.7 displays all the column names and contents resulting from the SQL SELECT statement `select * from Enrollment`. The output is shown in Figure 32.26.

**LISTING 32.7  TestResultSetMetaData.java**

```java
import java.sql.*;

public class TestResultSetMetaData {
    public static void main(String[] args) throws SQLException, ClassNotFoundException {
        // Load the JDBC driver
        Class.forName("com.mysql.jdbc.Driver");
        System.out.println("Driver loaded");

        // Connect to a database
        Connection connection = DriverManager.getConnection("jdbc:mysql://localhost/javabook", "scott", "tiger");
        System.out.println("Database connected");

        // Create a statement
        Statement statement = connection.createStatement();

        // Execute a statement
        ResultSet resultSet = statement.executeQuery("select * from Enrollment");

        ResultSetMetaData rsMetaData = resultSet.getMetaData();
        for (int i = 1; i <= rsMetaData.getColumnCount(); i++)
            System.out.printf("%-12s	", rsMetaData.getColumnName(i));
        System.out.println();

        // Iterate through the result and print the students' names
        while (resultSet.next()) {
            for (int i = 1; i <= rsMetaData.getColumnCount(); i++)
                System.out.printf("%-12s	", resultSet.getObject(i));
            System.out.println();
        }

        // Close the connection
        connection.close();
    }
}
```

![Command Prompt output](image)

**Figure 32.26** The `ResultSetMetaData` interface enables you to obtain result set information.
32.24 What is DatabaseMetaData for? Describe the methods in DatabaseMetaData. How do you get an instance of DatabaseMetaData?

32.25 What is ResultSetMetaData for? Describe the methods in ResultSetMetaData. How do you get an instance of ResultSetMetaData?

32.26 How do you find the number of columns in a result set? How do you find the column names in a result set?

### Key Terms

candidate key 1177  integrity constraint 1176
database system 1174  primary key 1177
domain constraint 1177  relational database 1177
foreign key 1177  Structured Query Language (SQL) 1178
foreign key constraint 1177  superkey 1177

### Chapter Summary

1. This chapter introduced the concepts of database systems, relational databases, relational data models, data integrity, and SQL. You learned how to develop database applications using Java.

2. The Java API for developing Java database applications is called JDBC. JDBC provides Java programmers with a uniform interface for accessing and manipulating relational databases.

3. The JDBC API consists of classes and interfaces for establishing connections with databases, sending SQL statements to databases, processing the results of SQL statements, and obtaining database metadata.

4. Since a JDBC driver serves as the interface to facilitate communications between JDBC and a proprietary database, JDBC drivers are database specific. A JDBC-ODBC bridge driver is included in JDK to support Java programs that access databases through ODBC drivers. If you use a driver other than the JDBC-ODBC bridge driver, make sure it is in the classpath before running the program.

5. Four key interfaces are needed to develop any database application using Java: Driver, Connection, Statement, and ResultSet. These interfaces define a framework for generic SQL database access. The JDBC driver vendors provide implementation for them.

6. A JDBC application loads an appropriate driver using the Driver interface, connects to the database using the Connection interface, creates and executes SQL statements using the Statement interface, and processes the result using the ResultSet interface if the statements return results.

7. The PreparedStatement interface is designed to execute dynamic SQL statements with parameters. These SQL statements are precompiled for efficient use when repeatedly executed.

8. Database metadata is information that describes the database itself. JDBC provides the DatabaseMetaData interface for obtaining database-wide information and the ResultSetMetaData interface for obtaining information on the specific ResultSet.
Quiz

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

Programming Exercises

*32.1 (Access and update a Staff table) Write a program that views, inserts, and updates staff information stored in a database, as shown in Figure 32.27a. The View button displays a record with a specified ID. The Insert button inserts a new record. The Update button updates the record for the specified ID. The Staff table is created as follows:

```sql
create table Staff (  
id char(9) not null,  
lastName varchar(15),  
firstName varchar(15),  
mI char(1),  
address varchar(20),  
city varchar(20),  
state char(2),  
telephone char(10),  
email varchar(40),  
primary key (id)
);
```

**32.2 (Visualize data) Write a program that displays the number of students in each department in a pie chart and a bar chart, as shown in Figure 32.27b. The number of students for each department can be obtained from the Student table (see Figure 32.4) using the following SQL statement:

```sql
select deptId, count(*)  
from Student  
where deptId is not null  
group by deptId;
```

*32.3 (Connection dialog) Develop a subclass of BorderPane named DBConnectionPane that enables the user to select or enter a JDBC driver and a URL and to enter a username and password, as shown in Figure 32.28. When the Connect to DB button is clicked, a Connection object for the database is stored in the connection property. You can then use the getConnection() method to return the connection.
*32.4 (Find grades) Listing 32.2, FindGrade.java, presented a program that finds a student’s grade for a specified course. Rewrite the program to find all the grades for a specified student, as shown in Figure 32.29.

*32.5 (Display table contents) Write a program that displays the content for a given table. As shown in Figure 32.30a, you enter a table and click the Show Contents button to display the table contents in the text area.

*32.6 (Find tables and showing their contents) Write a program that fills in table names in a combo box, as shown in Figure 32.30b. You can select a table from the combo box to display its contents in the text area.

**32.7 (Populate Quiz table) Create a table named Quiz as follows:

```java
create table Quiz(
    questionId int,
    question varchar(4000),
    choicea varchar(1000),
);```
The Quiz table stores multiple-choice questions. Suppose the multiple-choice questions are stored in a text file accessible from www.cs.armstrong.edu/liang/data/Quiz.txt in the following format:

1. question1
   a. choice a
   b. choice b
   c. choice c
   d. choice d
   Answer: cd

2. question2
   a. choice a
   b. choice b
   c. choice c
   d. choice d
   Answer: a

... 

Write a program that reads the data from the file and populate it into the Quiz table.

*32.8 (Populate Salary table) Create a table named Salary as follows:

```sql
create table Salary(
    firstName varchar(100),
    lastName varchar(100),
    rank varchar(15),
    salary float);
```

Obtain the data for salary from http://cs.armstrong.edu/liang/data/Salary.txt and populate it into the Salary table in the database.

*32.9 (Copy table) Suppose the database contains a student table defined as follows:

```sql
create table Student1 (
    username varchar(50) not null,
    password varchar(50) not null,
    fullname varchar(200) not null,
    constraint pkStudent primary key (username)
);
```

Create a new table named Student2 as follows:

```sql
create table Student2 (
    username varchar(50) not null,
    password varchar(50) not null,
    firstname varchar(100),
    lastname varchar(100),
    constraint pkStudent primary key (username)
);
```

A full name is in the form of firstname mi lastname or firstname lastname. For example, John K Smith is a full name. Write a program that
copies table Student1 into Student2. Your task is to split a full name into firstname, mi, and lastname for each record in Student1 and store a new record into Student2.

**32.10 (Record unsubmitted exercises)** The following three tables store information on students, assigned exercises, and exercise submission in LiveLab. LiveLab is an automatic grading system for grading programming exercises.

```sql
create table AGSSStudent (  
    username varchar(50) not null,  
    password varchar(50) not null,  
    fullname varchar(200) not null,  
    instructorEmail varchar(100) not null,  
    constraint pkAGSStudent primary key (username)  
);

create table ExerciseAssigned (  
    instructorEmail varchar(100),  
    exerciseName varchar(100),  
    maxscore double default 10,  
    constraint pkCustomExercise primary key (instructorEmail, exerciseName)  
);

create table AGSLog (  
    username varchar(50), /* This is the student's user name */  
    exerciseName varchar(100), /* This is the exercise */  
    score double default null,  
    submitted bit default 0,  
    constraint pkLog primary key (username, exerciseName)  
);
```

The AGSSStudent table stores the student information. The ExerciseAssigned table assigns the exercises by an instructor. The AGSLog table stores the grading results. When a student submits an exercise, a record is stored in the AGSLog table. However, there is no record in AGSLog if a student did not submit the exercise.

Write a program that adds a new record for each student and an assigned exercise to the student in the AGSLog table if a student has not submitted the exercise. The record should have 0 on score and submitted. For example, if the tables contain the following data in AGSLog before you run this program, the AGSLog table now contains the new records after the program runs.

<table>
<thead>
<tr>
<th>AGSSStudent</th>
<th>ExerciseAssigned</th>
</tr>
</thead>
<tbody>
<tr>
<td>username</td>
<td>password</td>
</tr>
<tr>
<td>abc</td>
<td>p1</td>
</tr>
<tr>
<td>cde</td>
<td>p2</td>
</tr>
<tr>
<td>wbc</td>
<td>p3</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
</tbody>
</table>
*32.11 (Baby names) Create the following table:

```sql
create table Babyname (
    year integer,
    name varchar(50),
    gender char(1),
    count integer,
    constraint pkBabyname primary key (year, name, gender)
);
```

The baby name ranking data was described in Programming Exercise 12.31. Write a program to read data from the following URL and store into the Babyname table.

http://www.cs.armstrong.edu/liang/data/babynamesranking2001.txt,
...
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JAVASERVER FACES

Objectives

- To explain what JSF is (§33.1).
- To create a JSF project in NetBeans (§33.2.1).
- To create a JSF page (§33.2.2).
- To create a JSF managed bean (§33.2.3).
- To use JSF expressions in a facelet (§33.2.4).
- To use JSF GUI components (§33.3).
- To obtain and process input from a form (§33.4).
- To develop a calculator using JSF (§33.5).
- To track sessions in application, session, view, and request scopes (§33.6).
- To validate input using the JSF validators (§33.7).
- To bind database with facelets (§33.8).
- To open a new JSF page from the current page (§33.9).
33.1 Introduction

*JavaServer Faces (JSF)* is a new technology for developing server-side Web applications using Java.

JSF enables you to completely separate Java code from HTML. You can quickly build Web applications by assembling reusable UI components in a page, connecting these components to Java programs and wiring client-generated events to server-side event handlers. The application developed using JSF is easy to debug and maintain.

**Note**
This chapter introduces JSF 2.2, the latest standard for JavaServer Faces. You need to know XHTML (eXtensible HyperText Markup Language) and CSS (Cascading Style Sheet) to start this chapter. For information on XHTML and CSS, see Supplements V.A and V.B on the Companion Website.

**Caution**
The examples and exercises in this chapter were tested using NetBeans 7.4, GlassFish 4, JSF 2.2, and J2EE 7. You need to use NetBeans 7.4 or a higher version with GlassFish 4, JSF 2.2, and J2EE to develop your JSF projects.

33.2 Getting Started with JSF

*NetBeans is an effective tool for developing JSF applications.*

We begin with a simple example that illustrates the basics of developing JSF projects using NetBeans. The example is to display the date and time on the server, as shown in Figure 33.1.

**Figure 33.1** The application displays the date and time on the server.

33.2.1 Creating a JSF Project

Here are the steps to create the application.

1. **Create a project**
   - Step 1: Choose *File, New Project* to display the New Project dialog box. In this box, choose *Java Web* in the Categories pane and *Web Application* in the Projects pane. Click *Next* to display the New Web Application dialog box.
   - In the New Web Application dialog box, enter and select the following fields, as shown in Figure 33.2a:
     - **Project Name:** jsf2demo
     - **Project Location:** c:\book

2. **Choose server and J2EE 7**
   - Step 2: Click *Next* to display the dialog box for choosing servers and settings. Select the following fields as shown in Figure 33.2b. (Note: You can use any server such as GlassFish 4.x that supports Java EE 7.)
     - **Server:** GlassFish 4
     - **Java EE Version:** Java EE 7 Web
33.2 Getting Started with JSF

Step 3: Click Next to display the dialog box for choosing frameworks, as shown in Figure 33.3. Check JavaServer Faces and JSF 2.2 as Server Library. Click Finish to create the project, as shown in Figure 33.4.

Figure 33.2 The New Web Application dialog box enables you to create a new Web project.

Figure 33.3 Check JavaServer Faces and JSF 2.2 to create a Web project.

33.2.2 A Basic JSF Page

A new project was just created with a default page named index.xhtml, as shown in Figure 33.4. This page is known as a facelet, which mixes JSF tags with XHTML tags. Listing 33.1 lists the contents of index.xhtml.

Listing 33.1 index.xhtml

```
1 <?xml version='1.0' encoding='UTF-8' ?>
2 <!-- index.xhtml -->
3 <!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Transitional//EN"
4 "http://www.w3.org/TR/xhtml1/DTD/xhtml1-transitional.dtd">
5 <html xmlns="http://www.w3.org/1999/xhtml"
     xmlns:facelet="http://java.sun.com/jsf/facelet">
...
Figure 33.4  A default JSF page is created in a new Web project.

| JSF namespace | 6 | xmlns:h="http://xmlns.jcp.org/jsf/html">
|---------------|---|---------------------------------------------|
| h:head        | 7 | <h:head>
|               | 8 | <title>Facelet Title</title>
|               | 9 | </h:head>
| h:body        | 10| <h:body>
|               | 11| Hello from Facelets
|               | 12| </h:body>
|               | 13| </html>

XML declaration  
Line 1 is an XML declaration to state that the document conforms to the XML version 1.0 and uses the UTF-8 encoding. The declaration is optional, but it is a good practice to use it. A document without the declaration may be assumed of a different version, which may lead to errors. If an XML declaration is present, it must be the first item to appear in the document. This is because an XML processor looks for the first line to obtain information about the document so that it can be processed correctly.

XML comment  
Line 2 is a comment for documenting the contents in the file. XML comment always begins with `<!--` and ends with `-->`.

DOCTYPE  
Lines 3 and 4 specify the version of XHTML used in the document. This can be used by the Web browser to validate the syntax of the document.

element  
An XML document consists of elements described by tags. An element is enclosed between a start tag and an end tag. XML elements are organized in a tree-like hierarchy. Elements may contain subelements, but there is only one root element in an XML document. All the elements must be enclosed inside the root tag. The root element in XHTML is defined using the `html` tag (line 5).

Each tag in XML must be used in a pair of the start tag and the end tag. A start tag begins with `<` followed by the tag name and ends with `>`. An end tag is the same as its start tag except that it begins with `</`. The start tag and end tag for `html` are `<html>` and `</html>`.

The `html` element is the root element that contains all other elements in an XHTML page. The starting `<html>` tag (lines 5 and 6) may contain one or more `xmlns` (XML namespace) attributes to specify the namespace for the elements used in the document. Namespaces are like Java packages. Java packages are used to organize classes and to avoid naming conflict. XHTML namespaces are used to organize tags and resolve naming conflict. If an element with the same name is defined in two namespaces, the fully qualified tag names can be used to differentiate them.
33.2 Getting Started with JSF

Each `xmlns` attribute has a name and a value separated by an equal sign (=). The following declaration (line 5)

```xml
xmlns="http://www.w3.org/1999/xhtml"
```
specifies that any unqualified tag names are defined in the default standard XHTML namespace.

The following declaration (line 6)

```xml
xmlns:h="http://xmlns.jcp.org/jsf/html"
```
allows the tags defined in the JSF tag library to be used in the document. These tags must have a prefix `h`.

An `html` element contains a head and a body. The `h:head` element (lines 7–9) defines an HTML `title` element. The title is usually displayed in the browser window’s title bar.

A `h:body` element defines the page’s content. In this simple example, it contains a string to be displayed in the Web browser.

```
<html>
  <head>
    <title>Hello from Facelets</title>
  </head>
  <body>
    <h:head>
      <title>Hello from Facelets</title>
    </h:head>
    <h:body>
      Hello from Facelets
    </h:body>
  </body>
</html>
```

**Note**
The XML tag names are case sensitive, whereas HTML tags are not. So, `<html>` is different from `<HTML>` in XML. Every start tag in XML must have a matching end tag, whereas some tags in HTML do not need end tags.

You can now display the page in index.xhtml by right-clicking on index.xhtml in the projects pane and choose `Run File`. The page is displayed in a browser, as shown in Figure 33.5.

![Figure 33.5](image)

The index.xhtml is displayed in the browser.

### 33.2.3 Managed JavaBeans for JSF

JSF applications are developed using the Model-View-Controller (MVC) architecture, which separates the application’s data (contained in the model) from the graphical presentation (the view). The controller is the JSF framework that is responsible for coordinating interactions between view and the model.

In JSF, the facelets are the view for presenting data. Data are obtained from Java objects. Objects are defined using Java classes. In JSF, the objects that are accessed from a facelet are JavaBeans objects. A `JavaBean` class is simply a public Java class with a `no-arg` constructor. JavaBeans may contain properties. By convention, a property is defined with a getter and a setter method. If a property only has a getter method, the property is called a read-only property. If a property only has a setter method, the property is called a write-only property. A property does not need to be defined as a data field in the class.

Our example in this section is to develop a JSF facelet to display current time. We will create a `JavaBean` with a `getTime()` method that returns the current time as a string. The facelet will invoke this method to obtain current time.

Here are the steps to create a `JavaBean` named `TimeBean`.

1. Create a `JavaBean` class named `TimeBean`.
2. Add a `getTime()` method that returns the current time as a string.
3. Use the `h:outputText` tag to display the current time from the `TimeBean`.
4. Run the application to display the current time in the browser.
Step 1. Right-click the project node jsf2demo to display a context menu as shown in Figure 33.6. Choose New, JSF Managed Bean to display the New JSF Managed Bean dialog box, as shown in Figure 33.7. (Note: if you don’t see JSF Managed Bean in the menu, choose Other to locate it in the JavaServer Faces category.)

Step 2. Enter and select the following fields, as shown in Figure 33.7:
- Class Name: TimeBean
- Package: jsf2demo
- Name: timeBean
- Scope: request

Click Finish to create TimeBean.java, as shown in Figure 33.8.

Step 3. Add the `getTime()` method to return the current time, as shown in Listing 33.2.

**Figure 33.6** Choose JSF Managed Bean to create a JavaBean for JSF.

**Listing 33.2 TimeBean.java**

```java
package jsf2demo;

import javax.inject.Named;
import javax.enterprise.context.RequestScoped;

@Named
@RequestScoped
public class TimeBean {

    @Named
    @RequestScoped
    public class TimeBean {
```
33.2 Getting Started with JSF

```java
public TimeBean() {
}

public String getTime() {
    return new java.util.Date().toString();
}
```

**Figure 33.7** Specify the name, location, scope for the bean.

**Figure 33.8** A JavaBean for JSF was created.
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**TimeBean** is a JavaBeans with the `@Named` annotation, which indicates that the JSF framework will create and manage the TimeBean objects used in the application. You have learned to use the `@Override` annotation in Chapter 11. The `@Override` annotation tells the compiler that the annotated method is required to override a method in a superclass. The `@Named` annotation tells the compiler to generate the code to enable the bean to be used by JSF facelets.

The `@RequestScope` annotation specifies that the scope of the JavaBeans object is within a request. You can also use `@ViewScope`, `@SessionScope` or `@ApplicationScope` to specify the scope for a session or for the entire application.

### 33.2.4 JSF Expressions

We demonstrate JSF expressions by writing a simple application that displays the current time. You can display current time by invoking the `getTime()` method in a `TimeBean` object using a JSF expression.

To keep index.xhtml intact, we create a new JSF page named CurrentTime.xhtml as follows:

1. Right-click the jsf2demo node in the project pane to display a context menu and choose New, JSF Page to display the New JSF File dialog box, as shown in Figure 33.9.
2. Enter CurrentTime in the File Name field, choose Facelets and click Finish to generate CurrentTime.xhtml, as shown in Figure 33.10.
3. Add a JSF expression to obtain the current time, as shown in Listing 33.3.
4. Right-click on CurrentTime.xhtml in the project to display a context menu and choose Run File to display the page in a browser as shown in Figure 33.1.

**Figure 33.9**  The New JSF Page dialog is used to create a JSF page.

**Listing 33.3  CurrentTime.xhtml**

```xml
<?xml version='1.0' encoding='UTF-8' ?>
<!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Transitional//EN"
  "http://www.w3.org/TR/xhtml1/DTD/xhtml1-transitional.dtd">
<html xmlns="http://www.w3.org/1999/xhtml"
  xmlns:f="http://java.sun.com/jsf/core"
  xmlns:h="http://java.sun.com/jsf/html">
    <h:form id="form1">
      <h:outputText value="Current time: 
          <h:commandLink value="<p:commandLink value="getTime()"/>
          " target="_blank"/>
        ">
    </h:form>
</html>
```

**Figure 33.10**  The New JSF Page dialog after clicking Finish.
33.2 Getting Started with JSF

Line 8 defines a **meta** tag inside the **h:head** tag to tell the browser to refresh every 60 seconds. This line can also be written as:

```
<meta http-equiv="refresh" content="60"/>
```

An element is called an **empty element** if there are no contents between the start tag and end tag. In an empty element, data are typically specified as attributes in the start tag. You can close an empty element by placing a slash immediately preceding the start tag’s right angle bracket, as shown in line 8, for brevity.

Line 11 uses a JSF expression `{timeBean.time}` to obtain the current time. `timeBean` is an object of the `TimeBean` class. The object name can be changed in the `@Named` annotation (line 6 in Listing 33.2) using the following syntax:

```
@Named(name = "anyObjectName")
```

By default, the object name is the class name with the first letter in lowercase.

Note that `time` is a JavaBeans property because the `getTime()` method is defined in `TimeBeans`. The JSF expression can either use the property name or invoke the method to obtain the current time. So the following two expressions are both fine.

```
#{timeBean.time}
#{timeBean.getTime()}
```

The syntax of a JSF expression is

```
#{expression}
```
JSF expressions bind JavaBeans objects with facelets. You will see more use of JSF expressions in the upcoming examples in this chapter.

33.1 What is JSF?
33.2 How do you create a JSF project in NetBeans?
33.3 How do you create a JSF page in a JSF project?
33.4 What is a facelet?
33.5 What is the file extension name for a facelet?
33.6 What is a managed bean?
33.7 What is the @Named annotation for?
33.8 What is the @RequestScope annotation for?

33.3 JSF GUI Components

*JSF provides many elements for displaying GUI components.*

Table 33.1 lists some of the commonly used elements. The tags with the h prefix are in the JSF HTML Tag library. The tags with the f prefix are in the JSF Core Tag library.

<table>
<thead>
<tr>
<th>JSF Tag</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>h:form</td>
<td>inserts an XHTML form into a page.</td>
</tr>
<tr>
<td>h:panelGroup</td>
<td>similar to a JavaFX FlowPane.</td>
</tr>
<tr>
<td>h:panelGrid</td>
<td>similar to a JavaFX GridPane.</td>
</tr>
<tr>
<td>h:inputText</td>
<td>displays a textbox for entering input.</td>
</tr>
<tr>
<td>h:outputText</td>
<td>displays a textbox for displaying output.</td>
</tr>
<tr>
<td>h:inputTextArea</td>
<td>displays a textarea for entering input.</td>
</tr>
<tr>
<td>h:inputSecret</td>
<td>displays a textbox for entering password.</td>
</tr>
<tr>
<td>h:outputLabel</td>
<td>displays a label.</td>
</tr>
<tr>
<td>h:outputLink</td>
<td>displays a hypertext link.</td>
</tr>
<tr>
<td>h:selectOneMenu</td>
<td>displays a combo box for selecting one item.</td>
</tr>
<tr>
<td>h:selectOneRadio</td>
<td>displays a set of radio button.</td>
</tr>
<tr>
<td>h:selectManyCheckbox</td>
<td>displays checkboxes.</td>
</tr>
<tr>
<td>h:selectOneListbox</td>
<td>displays a list for selecting one item.</td>
</tr>
<tr>
<td>h:selectManyListbox</td>
<td>displays a list for selecting multiple items.</td>
</tr>
<tr>
<td>f:selectItem</td>
<td>specifies an item in an h:selectOneMenu, h:selectOneRadio, or h:selectManyListbox.</td>
</tr>
<tr>
<td>h:message</td>
<td>displays a message for validating input.</td>
</tr>
<tr>
<td>h:dataTable</td>
<td>displays a data table.</td>
</tr>
<tr>
<td>h:column</td>
<td>specifies a column in a data table.</td>
</tr>
<tr>
<td>h:graphicImage</td>
<td>displays an image.</td>
</tr>
</tbody>
</table>

Listing 33.4 is an example that uses some of these elements to display a student registration form, as shown in Figure 33.11.
LISTING 33.4  StudentRegistrationForm.xhtml

```xml
<?xml version='1.0' encoding='UTF-8' ?>
<!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Transitional//EN" "http://www.w3.org/TR/xhtml1/DTD/xhtml1-transitional.dtd">
<html xmlns="http://www.w3.org/1999/xhtml"
     xmlns:h="http://xmlns.jcp.org/jsf/html"
     xmlns:f="http://xmlns.jcp.org/jsf/core">
    <h:head>
      <title>Student Registration Form</title>
    </h:head>
    <h:body>
      <h:form>
        <!-- Use h:graphicImage -->
        <h3>Student Registration Form</h3>
        <h:graphicImage name="usIcon.gif" library="image"/>
      </h:form>

      <!-- Use h:panelGrid -->
      <h:panelGrid columns="6" style="color:green">
        <h:outputLabel value="Last Name"/>
        <h:inputText id="lastNameInputText" />
        <h:outputLabel value="First Name"/>
        <h:inputText id="firstNameInputText" />
        <h:outputLabel value="MI"/>
        <h:inputText id="miInputText" size="1" />
      </h:panelGrid>

      <!-- Use radio buttons -->
      <h:panelGrid columns="2">
        <h:outputLabel>Gender</h:outputLabel>
        <h:inputText id="genderInputText" />
      </h:panelGrid>

      <!-- Use select boxes -->
      <h:panelGroup>
        <h:selectOneRadio value="Major">
          <option value="Computer Science">Computer Science</option>
          <option value="Mathematics">Mathematics</option>
          <option value="English">English</option>
        </h:selectOneRadio>
        <h:panelGroup>
          <h:selectOneRadio value="Minor">
            <option value="Computer Science">Computer Science</option>
            <option value="Mathematics">Mathematics</option>
            <option value="English">English</option>
          </h:selectOneRadio>
        </h:panelGroup>

        <!-- Use checkboxes -->
        <h:panelGrid columns="2">
          <h:outputLabel value="Hobby">
            <h:outputText>
              <input type="checkbox" value="Tennis" />
              Tennis
            </h:outputText>
          </h:outputLabel>
          <h:outputText>
            <input type="checkbox" value="Golf" />
            Golf
          </h:outputText>
          <h:outputText>
            <input type="checkbox" value="Ping Pong" />
            Ping Pong
          </h:outputText>
        </h:panelGrid>

        <!-- Use text areas -->
        <h:panelGrid columns="2">
          <h:outputLabel value="Remarks">
            <h:outputText>
              <textarea cols="20" rows="5"></textarea>
            </h:outputText>
          </h:outputLabel>
        </h:panelGrid>

        <h:commandButton name="Register" value="Register"/>
      </h:panelGroup>
    </h:body>
</html>
```

**Figure 33.11**  A student registration form is displayed using JSF elements.
The tags with prefix `f` are in the JSF core tag library. Line 6

```xml
xmlns:f="http://xmlns.jcp.org/jsf/core"
```

locates the library for these tags.

The `h:graphicImage` tag displays an image in the file usIcon.gif (line 14). The file is located in the /resources/image folder. In JSF 2.2, all resources (image files, audio files, CCS files) should be placed under the resources folder under the Web Pages node. You can create these folders as follows:

Step 1: Right-click the Web Pages node in the project pane to display a context menu and choose New, Folder to display the New Folder dialog box. (If Folder is not in the context menu, choose Other to locate it.)
33.3 JSF GUI Components

Step 2: Enter **resources** as the Folder Name and click **Finish** to create the **resources** folder, as shown in Figure 33.12.

Step 3: Right-click the **resources** node in the project pane to create the image folder under resources. You can now place usIcon.gif under the image folder.

![Image of the resources folder created](image)

**Figure 33.12** The resources folder was created.

JSF provides **h:panelGrid** and **h:panelGroup** elements to contain and layout subelements. **h:panelGrid** places the elements in a grid like the JavaFX **GridPane**. **h:panelGroup** places the elements like a JavaFX **FlowPane**. Lines 18–25 places six elements (labels and input texts) are in a **h:panelGrid**. The **columns** attribute specifies that each row in the grid has 6 columns. The elements are placed into a row from left to right in the order they appear in the facelet. When a row is full, a new row is created to hold the elements. We used **h:panelGrid** in this example. You may replace it with **h:panelGroup** to see how the elements would be arranged.

You may use the **style** attribute with a JSF html tag to specify the CSS style for the element and its subelements. The **style** attribute in line 18 specifies color green for all elements in this **h:panelGrid** element.

The **h:outputLabel** element is for displaying a label (line 19). The **value** attribute specifies the label’s text.

The **h:inputText** element is for displaying a text input box for the user to enter a text (line 20). The **id** attribute is useful for other elements or the server program to reference this element.

The **h:selectOneRadio** element is for displaying a group of radio buttons (line 30). Each radio button is defined using an **f:selectItem** element (lines 31–34).

The **h:selectOneMenu** element is for displaying a combo box (line 41). Each item in the combo box is defined using an **f:selectItem** element (lines 42 and 43).

The **h:selectManyListbox** element is for displaying a list for the user to choose multiple items in a list (line 46). Each item in the list is defined using an **f:selectItem** element (lines 47–49).

The **h:selectManyCheckbox** element is for displaying a group of check boxes (line 56). Each item in the check box is defined using an **f:selectItem** element (lines 57–59).

The **h:selectTextarea** element is for displaying a text area for multiple lines of input (line 66). The **style** attribute is used to specify the width and height of the text area (line 67).

The **h:commandButton** element is for displaying a button (line 71). When the button is clicked, an action is performed. The default action is to request the same page from the server. The next section shows how to process the form.
33.9 What is the name space for JSF tags with prefix h and prefix f?

33.10 Describe the use of the following tags?

- h:form, h:panelGroup, h:inputText, h:outputText, h:inputTextArea, h:inputSecret, h:outputLabel, h:outputLink, h:selectOneMenu, h:selectOneRadio, h:selectManyCheckbox, h:selectOneListbox, h:selectManyListbox, h:selectItem, h:message, h:dataTable, h:column, h:graphicImage

33.4 Processing the Form

Processing forms is a common task for Web programming. JSF provides tools for processing forms.

The preceding section introduced how to display a form using common JSF elements. This section shows how to obtain and process the input.

To obtain input from the form, simply bind each input element with a property in a managed bean. We now define a managed bean named registration as shown in Listing 33.5.

**Listing 33.5 RegistrationJSFBean.java**

```java
package jsf2demo;

import javax.enterprise.context.RequestScoped;
import javax.inject.Named;

@Named(value = "registration")
@RequestScoped
public class RegistrationJSFBean {
    private String lastName;
    private String firstName;
    private String mi;
    private String gender;
    private String major;
    private String[] minor;
    private String[] hobby;
    private String remarks;

    public RegistrationJSFBean() {
    }

    public String getLastName() {
        return lastName;
    }

    public void setLastName(String lastName) {
        this.lastName = lastName;
    }

    public String getFirstName() {
        return firstName;
    }

    public void setFirstName(String firstName) {
        this.firstName = firstName;
    }
}
```
public String getMi() {
    return mi;
}

public void setMi(String mi) {
    this.mi = mi;
}

public String getGender() {
    return gender;
}

public void setGender(String gender) {
    this.gender = gender;
}

public String getMajor() {
    return major;
}

public void setMajor(String major) {
    this.major = major;
}

public String[] getMinor() {
    return minor;
}

public void setMinor(String[] minor) {
    this.minor = minor;
}

public String[] getHobby() {
    return hobby;
}

public void setHobby(String[] hobby) {
    this.hobby = hobby;
}

public String getRemarks() {
    return remarks;
}

public void setRemarks(String remarks) {
    this.remarks = remarks;
}

public String getResponse() {
    if (lastName == null)
        return ""; // Request has not been made
    else {
        String allMinor = "";
        for (String s: minor)
            allMinor += s + " ";
        String allHobby = "";
        for (String s: hobby)
            allHobby += s + " ";
        getResponse()
return "<p style="color:red">You entered <br />
" +
"Last Name: " + lastName + "<br />
"First Name: " + firstName + "<br />
"MI: " + mi + "<br />
"Gender: " + gender + "<br />
"Major: " + major + "<br />
"Minor: " + allMinor + "<br />
"Hobby: " + allHobby + "<br />
"Remarks: " + remarks + "</p>";

The RegistrationJSFBean class is a managed bean that defines the properties lastName, firstName, mi, gender, major, minor, and remarks, which will be bound to the elements in the JSF registration form.

The registration form can now be revised as shown in Listing 33.6. Figure 33.13 shows that new JSF page displays the user input upon clicking the Register button.

**LISTING 33.6 ProcessStudentRegistrationForm.xhtml**

```xml
<?xml version='1.0' encoding='UTF-8' ?>
<!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Transitional//EN"
  "http://www.w3.org/TR/xhtml1/DTD/xhtml1-transitional.dtd">
<html xmlns="http://www.w3.org/1999/xhtml"
     xmlns:h="http://xmlns.jcp.org/jsf/html"
     xmlns:f="http://xmlns.jcp.org/jsf/core">
  <h:head>
    <title>Student Registration Form</title>
  </h:head>
  <h:body>
    <h:form>
      <!-- Use h:graphicImage -->
      <h:outputLabel value="Last Name"/>
      <h:inputText id="lastNameInputText" value="#{registration.lastName}"/>
      <h:outputLabel value="First Name"/>
      <h:inputText id="firstNameInputText" value="#{registration.firstName}"/>
      <h:outputLabel value="MI"/>
      <h:inputText id="miInputText" value="#{registration.mi}" size="1"/>
      <!-- Use radio buttons -->
      <h:outputLabel>Gender</h:outputLabel>
      <h:selectOneRadio id="genderSelectOneRadio" value="#{registration.gender}"
        <f:selectItem itemValue="Male" itemLabel="Male"/>
        <f:selectItem itemValue="Female" itemLabel="Female"/>
        </h:selectOneRadio>
    </h:form>
  </h:body>
</html>
```
<h:panelGrid columns="4">
  <!-- Use combo box and list -->
  <h:outputLabel value="Major "/>
  <h:selectOneMenu id="majorSelectOneMenu" value="#{registration.major}">
    <f:selectItem itemValue="Computer Science"/>
    <f:selectItem itemValue="Mathematics"/>
  </h:selectOneMenu>
  <h:outputLabel value="Minor "/>
  <h:selectManyListbox id="minorSelectManyListbox" value="#{registration.minor}">
    <f:selectItem itemValue="Computer Science"/>
    <f:selectItem itemValue="Mathematics"/>
    <f:selectItem itemValue="English"/>
  </h:selectManyListbox>
</h:panelGrid>

<!-- Use check boxes -->
<h:panelGrid columns="4">
  <h:outputLabel value="Hobby: "/>
  <h:selectManyCheckbox id="hobbySelectManyCheckbox" value="#{registration.hobby}">
    <f:selectItem itemValue="Tennis"/>
    <f:selectItem itemValue="Golf"/>
    <f:selectItem itemValue="Ping Pong"/>
  </h:selectManyCheckbox>
</h:panelGrid>

<!-- Use text area -->
<h:panelGrid columns="1">
  <h:outputLabel>Remarks:</h:outputLabel>
  <h:inputTextarea id="remarksInputTextarea" style="width:400px; height:50px;" value="#{registration.remarks}"/>
</h:panelGrid>

<!-- Use command button -->
<h:commandButton value="Register"/>
<br />
<h:outputText escape="false" style="color:red" value="#{registration.response}" />
The \texttt{h:selectManyCheckbox} element is bound to the \texttt{hobby} property (line 63). When the page is sent to the server, the checked boxes are returned as an array of \texttt{itemValues} and set to the \texttt{hobby} property.

The \texttt{h:selectTextarea} element is bound to the \texttt{remarks} property (line 75). When the page is sent to the server, the content in the text area is returned as a string and set to the \texttt{remarks} property.

The \texttt{h:outputText} element is bound to the \texttt{response} property (line 82). This is a read-only property in the bean. It is "" if \texttt{lastName} is \texttt{null} (lines 86–87 in Listing 33.5). When the page is returned to the client, the \texttt{response} property value is displayed in the output text element (line 82).

The \texttt{h:outputText} element’s \texttt{escape} attribute is set to \texttt{false} (line 81) to enable the contents to be displayed in HTML. By default, the \texttt{escape} attribute is \texttt{true}, which indicates the contents are considered as regular text.

\begin{itemize}
\item \textbf{33.11} In the \texttt{h:outputText} tag, what is the \texttt{escape} attribute for?
\item \textbf{33.12} Does every GUI component tag in JSF have the \texttt{style} attribute?
\end{itemize}

\section*{33.5 Case Study: Calculator}

\textit{This section gives a case study on using GUI elements and processing forms.}

This section uses JSF to develop a calculator to perform addition, subtraction, multiplication, and division, as shown in Figure 33.14.
Here are the steps to develop this project:

Step 1. Create a new managed bean named `calculator` with the request scope as shown in Listing 33.7, CalculatorJSFBean.java.

Step 2. Create a JSF facelet in Listing 33.8, Calculator.xhtml.

**LISTING 33.7 CalculatorJSFBean.java**

```java
package jsf2demo;

import javax.inject.Named;
import javax.enterprise.context.RequestScoped;

@Named(value = "calculator")
@RequestScoped
public class CalculatorJSFBean {
  private Double number1;
  private Double number2;
  private Double result;

  public CalculatorJSFBean() {
  }

  public Double getNumber1() {
    return number1;
  }

  public Double getNumber2() {
    return number2;
  }

  public Double getResult() {
    return result;
  }

  public void setNumber1(Double number1) {
    this.number1 = number1;
  }

  public void setNumber2(Double number2) {
    this.number2 = number2;
  }

  public void setResult(Double result) {
    this.result = result;
  }
```

**Figure 33.14** This JSF application enables you to perform addition, subtraction, multiplication, and division.
add

```java
public void add() {
    result = number1 + number2;
}
```

subtract

```java
public void subtract() {
    result = number1 - number2;
}
```

divide

```java
public void divide() {
    result = number1 / number2;
}
```

multiply

```java
public void multiply() {
    result = number1 * number2;
}
```

The managed bean has three properties `number1`, `number2`, and `result` (lines 9–38). The methods `add()`, `subtract()`, `divide()`, and `multiply()` add, subtract, multiply, and divide `number1` with `number2` and assigns the result to `result` (lines 40–54).

**Listing 33.8 Calculator.xhtml**

```xml
<?xml version='1.0' encoding='UTF-8' ?>
<!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Transitional//EN"
    "http://www.w3.org/TR/xhtml1/DTD/xhtml1-transitional.dtd">
<html xmlns="http://www.w3.org/1999/xhtml"
        xmlns:h="http://xmlns.jcp.org/jsf/html">
    <h:head>
      <title>Calculator</title>
    </h:head>
    <h:body>
      <h:form>
        <h:panelGrid columns="6">
          <h:outputLabel value="Number 1"/>
          <h:inputText id="number1InputText" size="4"
                       style="text-align: right"
                       value="#{calculator.number1}"/>
          <h:outputLabel value="Number 2" />
          <h:inputText id="number2InputText" size="4"
                        style="text-align: right"
                        value="#{calculator.number2}"/>
          <h:outputLabel value="Result" />
          <h:inputText id="resultInputText" size="4"
                        style="text-align: right"
                        value="#{calculator.result}"/>
        </h:panelGrid>

        <h:panelGrid columns="4">
          <h:commandButton value="Add"
                            action="#{calculator.add}"/>
          <h:commandButton value="Subtract"
                            action="#{calculator.subtract}"/>
          <h:commandButton value="Multiply"
                            action="#{calculator.multiply}"/>
          <h:commandButton value="Divide"
                            action="#{calculator.divide}"/>
        </h:panelGrid>

      </h:form>
    </h:body>
</html>
```
Three text input components along with their labels are placed in the grid panel (lines 11–24). Four button components are placed in the grid panel (lines 26–35).

The bean property `number1` is bound to the text input for Number 1 (line 15). The CSS style `text-align: right` (line 14) specifies that the text is right-aligned in the input box.

The `action` attribute for the `Add` button is set to the `add` method in the calculator bean (line 28). When the `Add` button is clicked, the `add` method in the bean is invoked to add `number1` with `number2` and assign the result to `result`. Since the `result` property is bound to the Result input text (line 23), the new result is now displayed in the text input field.

### 33.6 Session Tracking

*You can create a managed bean at the application scope, session scope, view scope, or request scope.*

JSF supports session tracking using JavaBeans at the application scope, session scope, view scope, and request scope. The **scope** is the lifetime of a bean. A **request-scoped** bean is alive in a single HTTP request. After the request is processed, the bean is no longer alive. A **view-scoped** bean lives as long as you are in the same JSF page. A **session-scoped** bean is alive for the entire Web session between a client and the server. An **application-scoped** bean lives as long as the Web application runs. In essence, a request-scoped bean is created once for a request; a view-scoped bean is created once for the view; a session-scoped bean is created once for the entire session; and an application-scoped bean is created once for the entire application.

Consider the following example that prompts the user to guess a number. When the page starts, the program randomly generates a number between 0 and 99. This number is stored in a bean. When the user enters a guess, the program checks the guess with the random number in the bean and tells the user whether the guess is too high, too low, or just right, as shown in Figure 33.15.

Here are the steps to develop this project:

1. Create a new managed bean named `guessNumber` with the view scope as shown in Listing 33.9, `GuessNumberJSFBean.java`.

2. Create a JSF facelet in Listing 33.10, `GuessNumber.xhtml`.

#### Listing 33.9  GuessNumberJSFBean.java

```java
package jsf2demo;

import javax.inject.Named;
import javax.faces.view.ViewScoped;

@Named(value = "guessNumber")
@ViewScoped
public class GuessNumberJSFBean {

private int number;
private String guessString;

public GuessNumberJSFBean() {
    number = (int)(Math.random() * 100);
}

public String getGuessString() {
    return guessString;
}

public void setGuessString(String guessString) {
    this.guessString = guessString;
}
}
```
public String getResponse() {
    if (guessString == null) {
        return ""; // No user input yet
    }

    int guess = Integer.parseInt(guessString);
    if (guess < number) {
        return "Too low";
    } else if (guess == number) {
        return "You got it";
    } else {
        return "Too high";
    }
}

The managed bean uses the @ViewScope annotation (line 7) to set up the view scope for the bean. The view scope is most appropriate for this project. The bean is alive as long as the view is not changed. The bean is created when the page is displayed for the first time. A random number between 0 and 99 is assigned to number (line 13) when the bean is created. This number will not change as long as the bean is alive in the same view.
The `getResponse` method converts `guessString` from the user input to an integer (line 28) and determines if the guess is too low (line 30), too high (line 34), and just right (line 32).

**Listing 33.10**  GuessNumber.xhtml

```xml
<?xml version='1.0' encoding='UTF-8' ?>
<!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Transitional//EN"
  "http://www.w3.org/TR/xhtml1/DTD/xhtml1-transitional.dtd">
<html xmlns="http://www.w3.org/1999/xhtml"
     xmlns:h="http://xmlns.jcp.org/jsf/html">
  <h:head>
    <title>Guess a number</title>
  </h:head>
  <h:body>
    <h:form>
      <h:outputLabel value="Enter you guess: "/>
      <h:inputText style="text-align: right; width: 50px"
                    id="guessInputText"
                    value="#{guessNumber.guessString}"/>
      <h:commandButton style="margin-left: 60px" value="Guess" />
      <br />
      <h:outputText style="color: red"
                    value="#{guessNumber.response}" />
    </h:form>
  </h:body>
</html>
```

The bean property `guessString` is bound to the text input (line 14). The CSS style `text-align: right` (line 13) specifies that the text is right-aligned in the input box.

The CSS style `margin-left: 60px` (line 15) specifies that the command button has a left margin of 60 pixels.

The bean property `response` is bound to the text output (line 18). The CSS style `color: red` (line 17) specifies that the text is displayed in red in the output box.

The project uses the `view` scope. What happens if the scope is changed to the request scope? Every time the page is refreshed, JSF creates a new bean with a new random number. What happens if the scope is changed to the `session` scope? The bean will be alive as long as the browser is alive. What happens if the scope is changed to the `application` scope? The bean will be created once when the application is launched from the server. So every client will use the same random number.

33.13 What is a scope? What are the available scopes in JSF? Explain request scope, view scope, session scope, and application scope. How do you set a request scope, view scope, session scope, and application scope in a managed bean?

33.14 What happens if the bean scope in Listing 33.9 GuessNumberJSFBean.java is changed to request?

33.15 What happens if the bean scope in Listing 33.9 GuessNumberJSFBean.java is changed to session?

33.16 What happens if the bean scope in Listing 33.9 GuessNumberJSFBean.java is changed to application?

33.7 Validating Input

*JSF provides tools for validating user input.*

In the preceding GuessNumber page, an error would occur if you entered a noninteger in the input box before clicking the Guess button. One way to fix the problem is to check the text field before processing any event. But a better way is to use the validators. You can use the
standard validator tags in the JSF Core Tag Library or create custom validators. Table 33.2 lists some JSF input validator tags.

**Table 33.2 JSF Input Validator Tags**

<table>
<thead>
<tr>
<th>JSF Tag</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>f:validateLength</td>
<td>validates the length of the input.</td>
</tr>
<tr>
<td>f:validateDoubleRange</td>
<td>validates whether numeric input falls within acceptable range of double values.</td>
</tr>
<tr>
<td>f:validateLongRange</td>
<td>validates whether numeric input falls within acceptable range of long values.</td>
</tr>
<tr>
<td>f:validateRequired</td>
<td>validates whether a field is not empty.</td>
</tr>
<tr>
<td>f:validateRegex</td>
<td>validates whether the input matches a regular expression.</td>
</tr>
<tr>
<td>f:validateBean</td>
<td>invokes a custom method in a bean to perform custom validation.</td>
</tr>
</tbody>
</table>

Consider the following example that displays a form for collecting user input as shown in Figure 33.16. All text fields in the form must be filled. If not, error messages are displayed. The SSN must be formatted correctly. If not, an error is displayed. If all input are correct, clicking Submit displays the result in an output text, as shown in Figure 33.17.

![Form Image](image)

(a) The required messages are displayed if input is required, but empty.

(b) Error messages are displayed if input is incorrect.

**Figure 33.16** The input fields are validated.

Here are the steps to create this project.

1. Create a new page in Listing 33.11, ValidateForm.xhtml.
2. Create a new managed bean named `validateForm`, as shown in Listing 33.12.
LISTING 33.11 ValidateForm.xhtml

```xml
<?xml version='1.0' encoding='UTF-8'?>
<!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Transitional//EN" "http://www.w3.org/TR/xhtml1/DTD/xhtml1-transitional.dtd">
<html xmlns="http://www.w3.org/1999/xhtml"
     xmlns:h="http://xmlns.jcp.org/jsf/html"
     xmlns:f="http://xmlns.jcp.org/jsf/core">
    <h:head>
      <title>Validate Form</title>
    </h:head>
    <h:body>
      <h:form>
        <h:panelGrid columns="3">
          <h:outputLabel value="Name:">
            <h:inputText id="nameInputText" required="true"
                          requiredMessage="Name is required"
                          validatorMessage="Name must have 1 to 10 chars"
                          value="#{validateForm.name}"
            >>> validateLength minimum="1" maximum="10" />
            <f:validateLength minimum="1" maximum="10" />
            <h:message for="nameInputText" style="color:red"/>
            message element
          </h:inputText>
          <h:outputLabel value="SSN:">
            <h:inputText id="ssnInputText" required="true"
                          requiredMessage="SSN is required"
                          validatorMessage="Invalid SSN"
                          value="#{validateForm.ssn}"
            >>> validateRegex pattern="\{3}-\{2}-\{4}"
            validate regex
            </h:inputText>
            <f:validateRegex pattern="\{3}-\{2}-\{4}"
            validate integer range
          </h:inputText>
          <h:outputLabel value="Age:">
            <h:inputText id="ageInputText" required="true"
                          requiredMessage="Age is required"
                          validatorMessage="Age must be between 16 and 120"
                          value="#{validateForm.ageString}"
            >>> validateLongRange minimum="16" maximum="120"
            validate integer range
            </h:inputText>
            <f:validateLongRange minimum="16" maximum="120" />
            <h:message for="ageInputText" style="color:red"/>
            message element
          </h:inputText>
          <h:outputLabel value="Height:">
            <h:inputText id="heightInputText" required="true"
                          requiredMessage="Height is required"
                          validatorMessage="Height must have 1 to 10 chars"
                          value="#{validateForm.height}
            >>> validateLength minimum="1" maximum="10"
            validate length
            </h:inputText>
            <f:validateLength minimum="1" maximum="10" />
            <h:message for="heightInputText" style="color:red"/>
            message element
          </h:inputText>
        </h:outputLabel>
      </h:form>
    </h:body>
</html>
```

Figure 33.17 The correct input values are displayed.
For each input text field, set its `required` attribute `true` (lines 14, 23, 32, 41) to indicate that an input value is required for the field. When a required input field is empty, the `requiredMessage` is displayed (lines 15, 24, 33, 42).

The `validatorMessage` attribute specifies a message to be displayed if the input field is invalid (line 16). The `f:validateLength` tag specifies the minimum or maximum length of the input (line 18). JSF will determine whether the input length is valid.

The `h:message` element displays the `validatorMessage` if the input is invalid. The element’s `for` attribute specifies the `id` of the element for which the message will be displayed (line 20).

The `f:validateRegex` tag specifies a regular expression for validating the input (line 27). For information on regular expression, see Appendix H.

The `f:validateLongRange` tag specifies a range for an integer input using the `minimum` and `maximum` attribute (line 36). In this project, a valid age value is between 16 and 120.

The `f:validateDoubleRange` tag specifies a range for a double input using the `minimum` and `maximum` attribute (line 45). In this project, a valid height value is between 3.5 and 9.5.

### Listing 33.12 ValidateFormJSFBean.java

```java
package jsf2demo;

import javax.enterprise.context.RequestScoped;
import javax.inject.Named;

@Named(value = "validateForm")
@RequestScoped
public class ValidateFormJSFBean {
    private String name;
    private String ssn;
    private String ageString;
    private String heightString;

    public String getName() {
        return name;
    }

    public void setName(String name) {
        this.name = name;
    }

    public String getSsn() {
        return ssn;
    }
```
public void setSsn(String ssn) {
    this.ssn = ssn;
}

public String getAgeString() {
    return ageString;
}

public void setAgeString(String ageString) {
    this.ageString = ageString;
}

public String getHeightString() {
    return heightString;
}

public void setHeightString(String heightString) {
    this.heightString = heightString;
}

public String getResponse() {
    if (name == null || ssn == null || ageString == null
        || heightString == null) {
        return "";
    }
    else {
        return "You entered " +
            " Name: " + name +
            " SSN: " + ssn +
            " Age: " + ageString +
            " Height: " + heightString;
    }
}

If an input is invalid, its value is not set to the bean. So only when all input are correct, the
getResponse() method will return all input values (lines 46–58)

33.17 Write a tag that validates an input text with minimal length of 2 and maximum 12.
33.18 Write a tag that validates an input text for SSN using a regular expression.
33.19 Write a tag that validates an input text for a double value with minimal 4.5 and
maximum 19.9.
33.20 Write a tag that validates an input text for an integer value with minimal 4 and
maximum 20.
33.21 Write a tag that makes an input text required.

33.8 Binding Database with Facelets

You can bind a database in JSF applications.

Often you need to access a database from a Web page. This section gives examples of building
Web applications using databases.

Consider the following example that lets the user choose a course, as shown in Figure 33.18.
After a course is selected in the combo box, the students enrolled in the course are displayed
in the table, as shown in Figure 33.19. In this example, all the course titles in the Course table
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are bound to the combo box and the query result for the students enrolled in the course is bound to the table.

Here are the steps to create this project:

Step 1. Create a managed bean named **courseName** with application scope, as shown in Listing 33.13.

Step 2. Create a JSF page in Listing 33.14, DisplayStudent.xhtml.

Step 3. Create a cascading style sheet for formatting the table as follows:

Step 3.1. Right-click the **resources** node to choose **New, Others** to display the New File dialog box, as shown in Figure 33.20.

Step 3.2. Choose **Other** in the Categories section and **Cascading Style Sheet** in the File Types section to display the New Cascading Style Sheet dialog box, as shown in Figure 33.21.
Step 3.3. Enter `tablestyle` as the File Name and click *Finish* to create `tablestyle.css` under the resources node.

Step 3.4. Define the CSS style as shown in Listing 33.15.

*Figure 33.20* You can create CSS files for Web project in NetBeans.

*Figure 33.21* The New Cascading Style Sheet dialog box creates a new style sheet file.
LISTING 33.13  CourseNameJSFBean.java

```java
package jsf2demo;

import java.sql.*;
import java.util.ArrayList;
import javax.enterprise.context.ApplicationScoped;
import javax.inject.Named;

@Named(value = "courseName")
@ApplicationScoped
public class CourseNameJSFBean {

private PreparedStatement studentStatement = null;
private String choice; // Selected course
private String[] titles; // Course titles

/** Creates a new instance of CourseName */
public CourseNameJSFBean() {
    initializeJdbc();
}

/** Initialize database connection */
private void initializeJdbc() {
    try {
        Class.forName("com.mysql.jdbc.Driver");
        System.out.println("Driver loaded");

        // Connect to the sample database
        Connection connection = DriverManager.getConnection("jdbc:mysql://localhost/javabook", "scott", "tiger");

        // Get course titles
        PreparedStatement statement = connection.prepareStatement("select title from course");
        ResultSet resultSet = statement.executeQuery();

        ArrayList<String> list = new ArrayList<>();
        while (resultSet.next()) {
            list.add(resultSet.getString(1));
        }
        titles = new String[list.size()]; // Array for titles
        list.toArray(titles); // Copy strings from list to array

        // Define a SQL statement for getting students
        studentStatement = connection.prepareStatement("select Student.ssn, " + "student.firstName, Student.mi, Student.lastName, " + "Student.phone, Student.birthDate, Student.street, " + "Student.zipCode, Student.deptId " + "from Student, Enrollment, Course " + "where Course.title = ? " + "and Student.ssn = Enrollment.ssn " + "and Enrollment.courseId = Course.courseId;";
    }
    catch (Exception ex) {
        ex.printStackTrace();
    }
}
```

33.8 Binding Database with Facelets

```java
public String[] getTitles() {
    return titles;
}

public String getChoice() {
    return choice;
}

public void setChoice(String choice) {
    this.choice = choice;
}

public ResultSet getStudents() throws SQLException {
    if (choice == null) {
        if (titles.length == 0)
            return null;
    } else {
        studentStatement.setString(1, titles[0]);
    }
    else {
        studentStatement.setString(1, choice); // Set course title
    }
    return studentStatement.executeQuery();
}
```

We use the same MySQL database `javabook` created in Chapter 32, “Java Database Programming.” The scope for this managed bean is `application`. The bean is created when the project is launched from the server. The `initializeJdbc` method loads the JDBC driver for MySQL (lines 23–24), connects to the MySQL database (lines 27–28), creates statement for obtaining course titles (lines 31–32), and creates a statement for obtaining the student information for the specified course (lines 45–53). Lines 31–42 execute the statement for obtaining course titles and store them in array `titles`.

The `getStudents()` method returns a `ResultSet` that consists of all students enrolled in the specified course (lines 72–85). The choice for the title is set in the statement to obtain the student for the specified title (line 80). If choice is `null`, the first title in the titles array is set in the statement (line 77). If no titles in the course, `getStudents()` returns `null` (line 75).

**TIP**
In order to use the MySQL database from this project, you have to add the MySQL JDBC driver from the Libraries node in the Project pane in NetBeans.

### Listing 33.14 DisplayStudent.xhtml

```xml
<?xml version='1.0' encoding='UTF-8' ?>
<!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Transitional//EN"
  "http://www.w3.org/TR/xhtml1/DTD/xhtml1-transitional.dtd">
<html xmlns="http://www.w3.org/1999/xhtml"
     xmlns:h="http://xmlns.jcp.org/jsf/html"
     xmlns:f="http://xmlns.jcp.org/jsf/core">
  <h:head>
    <title>Display Student</title>
    <h:outputStylesheet name="tablestyle.css" />
  </h:head>
  <h:body>
```

add MySQL in the Libraries node

style sheet
Line 9 specifies that the style sheet tablestyle.css created in Step 3 is used in this XMTML file. The **rowClasses = "oddTableRow, evenTableRow"** attribute specifies the style applied to the rows alternately using `oddTableRow` and `evenTableRow` (line 23). The **headerClasses = "tableHeader"** attribute specifies that the `tableHeader` class is used for header style (line 24). The **styleClasses = "table"** attribute specifies that the `table` class is used for the style of all other elements in the table (line 25).
Line 14 binds the `choice` property in the `courseName` bean with the combo box. The selection values in the combo box are bound with the `titles` array property (line 15).

Line 22 binds the table value with a database result set using the attribute `value="#{courseName.students}"`. The `var="student"` attribute associates a row in the result set with `student`. Lines 26–59 specify the column values using `student.ssn` (line 28), `student.firstName` (line 33), `student.mi` (line 38), `student.lastName` (line 33), `student.phone` (line 48), `student.birthDate` (line 53), and `student.deptId` (line 58).

**Listing 33.15 tablestyle.css**

```css
/* Style for table */

.tableHeader {
  font-family:"Trebuchet MS", Arial, Helvetica, sans-serif;
  border-collapse:collapse;
  font-size:1.1em;
  text-align:left;
  padding-top:5px;
  padding-bottom:4px;
  background-color:#A7C942;
  color:white;
  border:1px solid #98bf21;
}

.oddTableRow {
  border:1px solid #98bf21;
}

.evenTableRow {
  background-color: #e4f2d4;
  font-size:1em;
  padding:3px 7px 2px 7px;
  color:#000000;
  background-color:#EAF2D3;
}

.table {
  border:1px solid green;
}
```

The style sheet file defines the style classes `tableHeader` (line 2) for table header style, `oddTableRow` for odd table rows (line 14), `evenTableRow` for even table rows (line 18), and `table` for all other table elements (line 28).

### 33.9 Opening New JSF Pages

*You can open new JSF pages from the current JSF pages.*

All the examples you have seen so far use only one JSF page in a project. Suppose you want to register student information to the database. The application first displays the page as shown in Figure 33.22 to collect student information. After the user enters the information and clicks the `Submit` button, a new page is displayed to ask the user to confirm the input, as shown in Figure 33.23. If the user clicks the `Confirm` button, the data are stored into the database and the status page is displayed, as shown in Figure 33.24. If the user clicks the `Go Back` button, it goes back to the first page.
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**Figure 33.22** This page lets the user enter input.

**Figure 33.23** This page lets the user confirm the input.

**Figure 33.24** This page displays the status of the user input.
For this project, you need to create three JSF pages named AddressRegistration.xhtml, ConfirmAddress.xhtml, AddressStoredStatus.xhtml in Listings 33.16–33.18. The project starts with AddressRegistration.xhtml. When clicking the Submit button, the action for the button returns "ConfirmAddress" if the last name and first name are not empty, which causes ConfirmAddress.xhtml to be displayed. When clicking the Confirm button, the status page AddressStoredStatus is displayed. When clicking the Go Back button, the first page AddressRegistration is now displayed.

**Listing 33.16 AddressRegistration.xhtml**

```xml
<?xml version='1.0' encoding='UTF-8' ?>
<!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Transitional//EN"
  "http://www.w3.org/TR/xhtml1/DTD/xhtml1-transitional.dtd">
<html xmlns="http://www.w3.org/1999/xhtml"
     xmlns:h="http://xmlns.jcp.org/jsf/html"
     xmlns:f="http://xmlns.jcp.org/jsf/core">
  <h:head>
    <title>Student Registration Form</title>
  </h:head>
  <h:body>
    <h:form>
      <!-- Use h:graphicImage -->
      <h:outputLabel value="Last Name" style="color:red"/>
      <h:inputText id="lastNameInputText" value="#{addressRegistration.lastName}" bind="lastName"/>
      <h:outputLabel value="First Name" style="color:red"/>
      <h:inputText id="firstNameInputText" value="#{addressRegistration.firstName}" bind="firstName"/>
      <h:outputLabel value="MI"/>
      <h:inputText id="miInputText" size="1" value="#{addressRegistration.mi}" bind="mi"/>
      <h:panelGrid columns="4">
        <h:outputLabel value="Telephone"/>
        <h:inputText id="telephoneInputText" value="#{addressRegistration.telephone}" bind="telephone"/>
        <h:outputLabel value="Email"/>
        <h:inputText id="emailInputText" value="#{addressRegistration.email}" bind="email"/>
      </h:panelGrid>
      <h:panelGrid columns="4">
        <h:outputLabel value="Street"/>
        <h:inputText id="streetInputText" value="#{addressRegistration.street}" bind="street"/>
      </h:panelGrid>
      <h:panelGrid columns="6">
        <h:outputLabel value="City"/>
        <h:inputText id="cityInputText" value="#{addressRegistration.city}" bind="city"/>
      </h:panelGrid>
    </h:form>
    Please register to your instructor's student address book.
    <!-- Use h:panelGrid -->
    <h:panelGrid columns="6">
      <h:outputLabel value="Last Name" style="color:red"/>
      <h:inputText id="lastNameInputText" value="#{addressRegistration.lastName}" bind="lastName"/>
      <h:outputLabel value="First Name" style="color:red"/>
      <h:inputText id="firstNameInputText" value="#{addressRegistration.firstName}" bind="firstName"/>
      <h:outputLabel value="MI" />
      <h:inputText id="miInputText" size="1" value="#{addressRegistration.mi}" bind="mi"/>
      <h:panelGrid columns="4">
        <h:outputLabel value="Telephone"/>
        <h:inputText id="telephoneInputText" value="#{addressRegistration.telephone}" bind="telephone"/>
        <h:outputLabel value="Email"/>
        <h:inputText id="emailInputText" value="#{addressRegistration.email}" bind="email"/>
      </h:panelGrid>
      <h:panelGrid columns="4">
        <h:outputLabel value="Street"/>
        <h:inputText id="streetInputText" value="#{addressRegistration.street}" bind="street"/>
      </h:panelGrid>
    </h:panelGrid>
    <h:panelGrid columns="6">
      <h:outputLabel value="City"/>
      <h:inputText id="cityInputText" value="#{addressRegistration.city}" bind="city"/>
    </h:panelGrid>
  </h:body>
</html>
```
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bind state

bind zip

process register

JavaServer Faces
50
51
52
53
54
55
56
57
58
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62
63
64
65
66
67
68
69
70

<h:outputLabel value="State"/>
<h:selectOneMenu id="stateSelectOneMenu"
value="#{addressRegistration.state}">
<f:selectItem itemLabel="Georgia-GA" itemValue="GA" />
<f:selectItem itemLabel="Oklahoma-OK" itemValue="OK" />
<f:selectItem itemLabel="Indiana-IN" itemValue="IN"/>
</h:selectOneMenu>
<h:outputLabel value="Zip"/>
<h:inputText id="zipInputText"
value="#{addressRegistration.zip}"/>
</h:panelGrid>
<!-- Use command button -->
<h:commandButton value="Register"
action="#{addressRegistration.processSubmit()}"/>
<br />
<h:outputText escape="false" style="color:red"
value="#{addressRegistration.requiredFields}" />
</h:form>
</h:body>
</html>

LISTING 33.17 ConfirmAddress.xhtml

process confirm
go to AddressRegistration
page

1
2
3
4
5
6
7
8
9
10
11
12
13
14
15
16
17
18
19
20
21

<?xml version='1.0' encoding='UTF-8' ?>
<!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Transitional//EN"
"http://www.w3.org/TR/xhtml1/DTD/xhtml1-transitional.dtd">
<html xmlns="http://www.w3.org/1999/xhtml"
xmlns:h="http://xmlns.jcp.org/jsf/html">
<h:head>
<title>Confirm Student Registration</title>
</h:head>
<h:body>
<h:form>
<h:outputText escape="false" style="color:red"
value="#{registration1.input}" />
<h:panelGrid columns="2">
<h:commandButton value="Confirm"
action = "#{registration1.storeStudent()}"/>
<h:commandButton value="Go Back"
action = "AddressRegistration"/>
</h:panelGrid>
</h:form>
</h:body>
</html>

LISTING 33.18 AddressStoredStatus.xhtml

display status

1
2
3
4
5
6
7
8
9
10
11
12

<?xml version='1.0' encoding='UTF-8' ?>
<!DOCTYPE html PUBLIC "-//W3C//DTD XHTML 1.0 Transitional//EN"
"http://www.w3.org/TR/xhtml1/DTD/xhtml1-transitional.dtd">
<html xmlns="http://www.w3.org/1999/xhtml"
xmlns:h="http://xmlns.jcp.org/jsf/html">
<h:head>
<title>Address Stored?</title>
</h:head>
<h:body>
<h:form>
<h:outputText escape="false" style="color:green"
value="#{registration1.status}" />


LISTING 33.19 AddressRegistrationJSFBean.java

```java
package jsf2demo;

import javax.inject.Named;
import javax.enterprise.context.SessionScoped;
import java.sql.*;
import java.io.Serializable;

@Named(value = "addressRegistration")
@SessionScoped
public class AddressRegistrationJSFBean implements Serializable {
    private String lastName;
    private String firstName;
    private String mi;
    private String telephone;
    private String email;
    private String street;
    private String city;
    private String state;
    private String zip;
    private String status = "Nothing stored";

    private PreparedStatement pstmt;

    public AddressRegistrationJSFBean() {
        initializeJdbc();
    }

    public String getLastName() {
        return lastName;
    }

    public void setLastName(String lastName) {
        this.lastName = lastName;
    }

    public String getFirstName() {
        return firstName;
    }

    public void setFirstName(String firstName) {
        this.firstName = firstName;
    }

    public String getMi() {
        return mi;
    }

    public void setMi(String mi) {
        this.mi = mi;
    }

    public String getTelephone() {
        return telephone;
    }

    public AddressRegistrationJSFBean() {
        initializeJdbc();
    }
```

---

LISTING 33.19 AddressRegistrationJSFBean.java

```java
package jsf2demo;

import javax.inject.Named;
import javax.enterprise.context.SessionScoped;
import java.sql.*;
import java.io.Serializable;

@Named(value = "addressRegistration")
@SessionScoped
public class AddressRegistrationJSFBean implements Serializable {
    private String lastName;
    private String firstName;
    private String mi;
    private String telephone;
    private String email;
    private String street;
    private String city;
    private String state;
    private String zip;
    private String status = "Nothing stored";

    private PreparedStatement pstmt;

    public AddressRegistrationJSFBean() {
        initializeJdbc();
    }

    public String getLastName() {
        return lastName;
    }

    public void setLastName(String lastName) {
        this.lastName = lastName;
    }

    public String getFirstName() {
        return firstName;
    }

    public void setFirstName(String firstName) {
        this.firstName = firstName;
    }

    public String getMi() {
        return mi;
    }

    public void setMi(String mi) {
        this.mi = mi;
    }

    public String getTelephone() {
        return telephone;
    }

    public AddressRegistrationJSFBean() {
        initializeJdbc();
    }
```
public void setTelephone(String telephone) {
    this.telephone = telephone;
}

public String getEmail() {
    return email;
}

public void setEmail(String email) {
    this.email = email;
}

public String getStreet() {
    return street;
}

public void setStreet(String street) {
    this.street = street;
}

public String getCity() {
    return city;
}

public void setCity(String city) {
    this.city = city;
}

public String getState() {
    return state;
}

public void setState(String state) {
    this.state = state;
}

public String getZip() {
    return zip;
}

public void setZip(String zip) {
    this.zip = zip;
}

private boolean isRequiredFieldsFilled() {
    return !(lastName == null || firstName == null
              || lastName.trim().length() == 0
              || firstName.trim().length() == 0);
}

public String processSubmit() {
    if (isRequiredFieldsFilled())
        return "ConfirmAddress";
    else
        return ""
}

public String getRequiredFields() {
    if (isRequiredFieldsFilled())
check required fields
33.9 Opening New JSF Pages

    return "";
    else
        return "Last Name and First Name are required";
    }

    public String getInput() {
        return "<p style="color:red">You entered <br />
          + "Last Name: " + lastName + "<br />
          + "First Name: " + firstName + "<br />
          + "MI: " + mi + "<br />
          + "Telephone: " + telephone + "<br />
          + "Email: " + email + "<br />
          + "Street: " + street + "<br />
          + "City: " + city + "<br />
          + "State: " + state + "<br />
          + "Zip: " + zip + "</p>";
    }

    /** Initialize database connection */
    private void initializeJdbc() {
        try {
            // Explicitly load a MySQL driver
            Class.forName("com.mysql.jdbc.Driver");
            System.out.println("Driver loaded");

            // Establish a connection
            Connection conn = DriverManager.getConnection("jdbc:mysql://localhost/javabook", "scott", "tiger");

            // Create a Statement
            pstmt = conn.prepareStatement("insert into Address (lastName,
              + " firstName, mi, telephone, email, street, city, 
              + "state, zip) values (?, ?, ?, ?, ?, ?, ?, ?)");
        } catch (Exception ex) {
            System.out.println(ex);
        }
    }

    /** Store an address to the database */
    public String storeStudent() {
        try {
            pstmt.setString(1, lastName);
            pstmt.setString(2, firstName);
            pstmt.setString(3, mi);
            pstmt.setString(4, telephone);
            pstmt.setString(5, email);
            pstmt.setString(6, street);
            pstmt.setString(7, city);
            pstmt.setString(8, state);
            pstmt.setString(9, zip);
            pstmt.executeUpdate();
            status = firstName + " " + lastName
              + " is now registered in the database.";
        } catch (Exception ex) {
            status = ex.getMessage();
        }
    }
go to a new page

A session-scoped managed bean must implement the `java.io.Serializable` interface. So, the `AddressRegistration` class is defined as a subtype of `java.io.Serializable`.

The action for the `Register` button in the `AddressRegistration` JSF page is `processSubmit()` (line 64 in `AddressRegistration.xhtml`). This method checks if last name and first name are not empty (lines 106–111 in `AddressRegistrationJSFBean.java`). If so, it returns a string "ConfirmAddress", which causes the `ConfirmAddress` JSF page to be displayed.

The `ConfirmAddress` JSF page displays the data entered from the user (line 12 in `ConfirmAddress.xhtml`). The `getInput()` method (lines 120–133 in `AddressRegistrationJSFBean.java`) collects the input.

The action for the `Confirm` button in the `ConfirmAddress` JSF page is `storeStudent()` (line 15 in `ConfirmAddress.xhtml`). This method stores the address in the database (lines 157–177 in `AddressRegistrationJSFBean.java`) and returns a string "AddressStoredStatus", which causes the `AddressStoredStatus` page to be displayed. The status message is displayed in this page (line 12 in `AddressStoredStatus.xhtml`).

The action for the `Go Back` button in the `ConfirmAddress` page is "AddressRegistration" (line 17 in `ConfirmAddress.xhtml`). This causes the `AddressRegistration` page to be displayed for the user to reenter the input.

The scope of the managed bean is session (line 9 `AddressRegistrationJSFBean.java`) so the multiple pages can share the same bean.

Note that this program loads the database driver explicitly (line 139 `AddressRegistrationJSFBean.java`). Sometimes, an IDE such as NetBeans is not able to find a suitable driver. Loading a driver explicitly can avoid this problem.

### Key Terms

- application scope 1233
- JavaBean 1217
- request scope 1233
- scope 1233
- session scope 1233
- view scope 1233

### Chapter Summary

1. JSF enables you to completely separate Java code from HTML.

2. A **facelet** is an XHTML page that mixes JSF tags with XHTML tags.

3. JSF applications are developed using the Model-View-Controller (MVC) architecture, which separates the application’s data (contained in the model) from the graphical presentation (the view).

4. The controller is the JSF framework that is responsible for coordinating interactions between view and the model.
5. In JSF, the faces are the view for presenting data. Data are obtained from Java objects. Objects are defined using Java classes.

6. In JSF, the objects that are accessed from a facelet are JavaBeans objects.

7. The JSF expression can either use the property name or invoke the method to obtain the current time.

8. JSF provides many elements for displaying GUI components. The tags with the h prefix are in the JSF HTML Tag library. The tags with the f prefix are in the JSF Core Tag library.

9. You can specify the JavaBeans objects at the application scope, session scope, view scope, or request scope.

10. The view scope keeps the bean alive as long as you stay on the view. The view scope is between session and request scopes.

11. JSF provides several convenient and powerful ways for input validation. You can use the standard validator tags in the JSF Core Tag Library or create custom validators.

**Quiz**

Answer the quiz for this chapter online at www.cs.armstrong.edu/liang/intro10e/quiz.html.

**Programming Exercises**

**33.1** *(Factorial table in JSF)* Write a JSF page that displays a factorial page as shown in Figure 33.25. Display the table in an h:outputText component. Set its escape property to false to display it as HTML contents.

**33.2** *(Multiplication table)* Write a JSF page that displays a multiplication table as shown in Figure 33.26.

**33.3** *(Calculate tax)* Write a JSF page to let the user enter taxable income and filing status, as shown in Figure 33.27a. Clicking the Compute Tax button computes and displays the tax, as shown in Figure 33.27b. Use the computeTax method introduced in Listing 3.5, ComputeTax.java, to compute tax.

**33.4** *(Calculate loan)* Write a JSF page that lets the user enter loan amount, interest rate, and number of years, as shown in Figure 33.28a. Click the Compute Loan Payment button to compute and display the monthly and total loan payments, as shown in Figure 33.28b. Use the Loan class given in Listing 10.2, Loan.java, to compute the monthly and total payments.

**33.5** *(Addition quiz)* Write a JSF program that generates addition quizzes randomly, as shown in Figure 33.29a. After the user answers all questions, it displays the result, as shown in Figure 33.29b.

**33.6** *(Large factorial)* Rewrite Exercise 33.1 to handle large factorial. Use the BigInteger class introduced in Section 10.9.

**33.7** *(Guess birthday)* Listing 4.3, GuessBirthday.java, gives a program for guessing a birthday. Write a JSF program that displays five sets of numbers, as shown in Figure 33.30a. After the user checks the appropriate boxes and clicks the Guess Birthday button, the program displays the birthday, as shown in Figure 33.30b.
Figure 33.25  The JSF page displays factorials for the numbers from 0 to 10 in a table.

Figure 33.26  The JSF page displays the multiplication table.
**33.8** (*Guess capitals*) Write a JSF that prompts the user to enter a capital for a state, as shown in Figure 33.31a. Upon receiving the user input, the program reports whether the answer is correct, as shown in Figure 33.31b. You can click the Next button to display another question. You can use a two-dimensional array to store the states and capitals, as proposed in Exercise 8.37. Create a list from the array and apply the shuffle method to reorder the list so the questions will appear in random order.

**33.9** (*Access and update a Staff table*) Write a JSF program that views, inserts, and updates staff information stored in a database, as shown in Figure 33.32. The view button displays a record with a specified ID. The Staff table is created as follows:

```sql
create table Staff (  
    id     char(9) not null,  
    lastName varchar(15),  
    firstName varchar(15),  
    mi     char(1),  
    address varchar(20),  
    city   varchar(20),  
);  
```
state char(2),
    telephone char(10),
    email varchar(40),
    primary key (id)
);

*33.10 (Random cards) Write a JSF that displays four random cards from a deck of 52 cards, as shown in Figure 33.33. When the user clicks the Refresh button, four new random cards are displayed.

***33.11 (Game: the 24-point card game) Rewrite Exercise 20.13 using JSF, as shown in Figure 33.34. Upon clicking the Refresh button, the program displays four random cards and displays an expression if a 24-point solution exists. Otherwise, it displays No solution.

***33.12 (Game: the 24-point card game) Rewrite Exercise 20.17 using JSF, as shown in Figure 33.35. The program lets the user enter four card values and finds a solution upon clicking the Find a Solution button.

Figure 33.28 The JSF page computes the loan payment.
Figure 33.29  The program displays addition questions in (a) and answers in (b).

*33.13  (Day of week) Write a program that displays the day of the week for a given day, month, and year, as shown in Figure 33.36. The program lets the user select a day, month, and year, and click the Get Day of Week button to display the day of week. The Time field displays Future if it is a future day or Past otherwise. Use the Zeller’s congruence to find the day of the week (See Programming Exercise 3.21).
Figure 33.30  (a) The program displays five sets of numbers for the user to check the boxes. (b) The program displays the date.

Figure 33.31  (a) The program displays a question. (b) The program displays the answer to the question.
Figure 33.32  The web page lets you view, insert, and update staff information.

Figure 33.33  This JSF application displays four random cards.
Figure 33.34  The JSF application solves a 24-Point card game.

Figure 33.35  The user enters four numbers and the program finds a solution.
FIGURE 33.36  The user enters a day, month, and year and the program finds the day of the week.
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APPENDIXES

Appendix A
Java Keywords

Appendix B
The ASCII Character Set

Appendix C
Operator Precedence Chart

Appendix D
Java Modifiers

Appendix E
Special Floating-Point Values

Appendix F
Number Systems

Appendix G
Bitwise Operations

Appendix H
Regular Expressions

Appendix I
Enumerated Types
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Java Keywords

The following fifty keywords are reserved for use by the Java language:

<table>
<thead>
<tr>
<th>abstract</th>
<th>double</th>
<th>int</th>
<th>super</th>
</tr>
</thead>
<tbody>
<tr>
<td>assert</td>
<td>else</td>
<td>interface</td>
<td>switch</td>
</tr>
<tr>
<td>boolean</td>
<td>enum</td>
<td>long</td>
<td>synchronized</td>
</tr>
<tr>
<td>break</td>
<td>extends</td>
<td>native</td>
<td>this</td>
</tr>
<tr>
<td>byte</td>
<td>final</td>
<td>new</td>
<td>throw</td>
</tr>
<tr>
<td>case</td>
<td>finally</td>
<td>package</td>
<td>throws</td>
</tr>
<tr>
<td>catch</td>
<td>float</td>
<td>private</td>
<td>transient</td>
</tr>
<tr>
<td>char</td>
<td>for</td>
<td>protected</td>
<td>try</td>
</tr>
<tr>
<td>class</td>
<td>goto</td>
<td>public</td>
<td>void</td>
</tr>
<tr>
<td>const</td>
<td>if</td>
<td>return</td>
<td>volatile</td>
</tr>
<tr>
<td>continue</td>
<td>implements</td>
<td>short</td>
<td>while</td>
</tr>
<tr>
<td>default</td>
<td>import</td>
<td>static</td>
<td></td>
</tr>
<tr>
<td>do</td>
<td>instanceof</td>
<td>strictfp*</td>
<td></td>
</tr>
</tbody>
</table>

The keywords `goto` and `const` are C++ keywords reserved, but not currently used in Java. This enables Java compilers to identify them and to produce better error messages if they appear in Java programs.

The literal values `true`, `false`, and `null` are not keywords, just like literal value `100`. However, you cannot use them as identifiers, just as you cannot use `100` as an identifier.

In the code listing, we use the keyword color for `true`, `false`, and `null` to be consistent with their coloring in Java IDEs.

---

*The `strictfp` keyword is a modifier for a method or class that enables it to use strict floating-point calculations. Floating-point arithmetic can be executed in one of two modes: strict or nonstrict. The strict mode guarantees that the evaluation result is the same on all Java Virtual Machine implementations. The nonstrict mode allows intermediate results from calculations to be stored in an extended format different from the standard IEEE floating-point number format. The extended format is machine-dependent and enables code to be executed faster. However, when you execute the code using the nonstrict mode on different JVMs, you may not always get precisely the same results. By default, the nonstrict mode is used for floating-point calculations. To use the strict mode in a method or a class, add the `strictfp` keyword in the method or the class declaration. Strict floating-point may give you slightly better precision than nonstrict floating-point, but the distinction will only affect some applications. Strictness is not inherited; that is, the presence of `strictfp` on a class or interface declaration does not cause extended classes or interfaces to be strict.*
Appendix B

The ASCII Character Set

Tables B.1 and B.2 show ASCII characters and their respective decimal and hexadecimal codes. The decimal or hexadecimal code of a character is a combination of its row index and column index. For example, in Table B.1, the letter A is at row 6 and column 5, so its decimal equivalent is 65; in Table B.2, letter A is at row 4 and column 1, so its hexadecimal equivalent is 41.
### Table B.1  ASCII Character Set in the Decimal Index

<table>
<thead>
<tr>
<th></th>
<th>0</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>nul</td>
<td>soh</td>
<td>stx</td>
<td>etx</td>
<td>etx</td>
<td>eot</td>
<td>enq</td>
<td>ack</td>
<td>bel</td>
<td>bs</td>
</tr>
<tr>
<td>1</td>
<td>nl</td>
<td>vt</td>
<td>ff</td>
<td>cr</td>
<td>so</td>
<td>si</td>
<td>dle</td>
<td>dcl</td>
<td>dc2</td>
<td>dc3</td>
</tr>
<tr>
<td>2</td>
<td>dc4</td>
<td>nak</td>
<td>syn</td>
<td>etb</td>
<td>can</td>
<td>em</td>
<td>sub</td>
<td>esc</td>
<td>fs</td>
<td>gs</td>
</tr>
<tr>
<td>3</td>
<td>rs</td>
<td>us</td>
<td>sp</td>
<td>!</td>
<td>&quot;</td>
<td>#</td>
<td>$</td>
<td>%</td>
<td>&amp;</td>
<td>'</td>
</tr>
<tr>
<td>4</td>
<td>(</td>
<td>)</td>
<td>*</td>
<td>+</td>
<td>,</td>
<td>-</td>
<td>.</td>
<td>/</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>5</td>
<td>2</td>
<td>3</td>
<td>4</td>
<td>5</td>
<td>6</td>
<td>7</td>
<td>8</td>
<td>9</td>
<td>:</td>
<td>;</td>
</tr>
<tr>
<td>6</td>
<td>&lt;</td>
<td>=</td>
<td>&gt;</td>
<td>?</td>
<td>@</td>
<td>A</td>
<td>B</td>
<td>C</td>
<td>D</td>
<td>E</td>
</tr>
<tr>
<td>7</td>
<td>F</td>
<td>G</td>
<td>H</td>
<td>I</td>
<td>J</td>
<td>K</td>
<td>L</td>
<td>M</td>
<td>N</td>
<td>O</td>
</tr>
<tr>
<td>8</td>
<td>P</td>
<td>Q</td>
<td>R</td>
<td>S</td>
<td>T</td>
<td>U</td>
<td>V</td>
<td>W</td>
<td>X</td>
<td>Y</td>
</tr>
<tr>
<td>9</td>
<td>Z</td>
<td>[</td>
<td>\</td>
<td>]</td>
<td>^</td>
<td>-</td>
<td>’</td>
<td>a</td>
<td>b</td>
<td>c</td>
</tr>
<tr>
<td>10</td>
<td>d</td>
<td>e</td>
<td>f</td>
<td>g</td>
<td>h</td>
<td>i</td>
<td>j</td>
<td>k</td>
<td>l</td>
<td>m</td>
</tr>
<tr>
<td>11</td>
<td>n</td>
<td>o</td>
<td>p</td>
<td>q</td>
<td>r</td>
<td>s</td>
<td>t</td>
<td>u</td>
<td>v</td>
<td>w</td>
</tr>
<tr>
<td>12</td>
<td>x</td>
<td>y</td>
<td>z</td>
<td>{</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

### Table B.2  ASCII Character Set in the Hexadecimal Index

|   | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | A | B | C | D | E | F |
|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|---|
| 0 | nul| soh| stx| etx| etx| eot| enq| ack| bel| bs | ht | nl | vt | ff | cr | so | si |
| 1 | dle| dcl| dc2| dc3| dc4| nak| syn| etb| can| em | sub| esc| fs | gs | rs | us |
| 2 | sp | !  | "  | #  | $  | %  | &  | '  | (  | )  | *  | +  | ,  | -  | .  | /  |
| 3 | 0  | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | :  | ;  | <  | =  | >  | ?  |
| 4 | @  | A  | B  | C  | D  | E  | F  | G  | H  | I  | J  | K  | L  | M  | N  | O  |
| 5 | P  | Q  | R  | S  | T  | U  | V  | W  | X  | Y  | Z  | [  | \ | ]  | ^  | -  |
| 6 | ’  | a  | b  | c  | d  | e  | f  | g  | h  | i  | j  | k  | l  | m  | n  | o  |
| 7 | p  | q  | r  | s  | t  | u  | v  | w  | x  | y  | z  | {  | |  | |  | ¬ | del |
# Operator Precedence Chart

The operators are shown in decreasing order of precedence from top to bottom. Operators in the same group have the same precedence, and their associativity is shown in the table.

<table>
<thead>
<tr>
<th>Operator</th>
<th>Name</th>
<th>Associativity</th>
</tr>
</thead>
<tbody>
<tr>
<td>(</td>
<td>Parentheses</td>
<td>Left to right</td>
</tr>
<tr>
<td>)</td>
<td>Function call</td>
<td>Left to right</td>
</tr>
<tr>
<td>[</td>
<td>Array subscript</td>
<td>Left to right</td>
</tr>
<tr>
<td>]</td>
<td>Object member access</td>
<td>Left to right</td>
</tr>
<tr>
<td>.</td>
<td>Postincrement</td>
<td>Left to right</td>
</tr>
<tr>
<td>++</td>
<td>Postdecrement</td>
<td>Left to right</td>
</tr>
<tr>
<td>++</td>
<td>Preincrement</td>
<td>Right to left</td>
</tr>
<tr>
<td>--</td>
<td>Predecrement</td>
<td>Right to left</td>
</tr>
<tr>
<td>+</td>
<td>Unary plus</td>
<td>Right to left</td>
</tr>
<tr>
<td>-</td>
<td>Unary minus</td>
<td>Right to left</td>
</tr>
<tr>
<td>!</td>
<td>Unary logical negation</td>
<td>Right to left</td>
</tr>
<tr>
<td>(type)</td>
<td>Unary casting</td>
<td>Right to left</td>
</tr>
<tr>
<td>new</td>
<td>Creating object</td>
<td>Right to left</td>
</tr>
<tr>
<td>*</td>
<td>Multiplication</td>
<td>Left to right</td>
</tr>
<tr>
<td>/</td>
<td>Division</td>
<td>Left to right</td>
</tr>
<tr>
<td>%</td>
<td>Remainder</td>
<td>Left to right</td>
</tr>
<tr>
<td>+</td>
<td>Addition</td>
<td>Left to right</td>
</tr>
<tr>
<td>-</td>
<td>Subtraction</td>
<td>Left to right</td>
</tr>
<tr>
<td>&lt;&lt;</td>
<td>Left shift</td>
<td>Left to right</td>
</tr>
<tr>
<td>&gt;&gt;</td>
<td>Right shift with sign extension</td>
<td>Left to right</td>
</tr>
<tr>
<td>&gt;&gt;&gt;</td>
<td>Right shift with zero extension</td>
<td>Left to right</td>
</tr>
<tr>
<td>&lt;</td>
<td>Less than</td>
<td>Left to right</td>
</tr>
<tr>
<td>&lt;=</td>
<td>Less than or equal to</td>
<td>Left to right</td>
</tr>
<tr>
<td>&gt;</td>
<td>Greater than</td>
<td>Left to right</td>
</tr>
<tr>
<td>&gt;=</td>
<td>Greater than or equal to</td>
<td>Left to right</td>
</tr>
<tr>
<td>instanceof</td>
<td>Checking object type</td>
<td>Left to right</td>
</tr>
<tr>
<td>Operator</td>
<td>Name</td>
<td>Associativity</td>
</tr>
<tr>
<td>----------</td>
<td>-----------------------</td>
<td>---------------</td>
</tr>
<tr>
<td>==</td>
<td>Equal comparison</td>
<td>Left to right</td>
</tr>
<tr>
<td>!=</td>
<td>Not equal</td>
<td>Left to right</td>
</tr>
<tr>
<td>&amp;</td>
<td>(Unconditional AND)</td>
<td>Left to right</td>
</tr>
<tr>
<td>^</td>
<td>(Exclusive OR)</td>
<td>Left to right</td>
</tr>
<tr>
<td></td>
<td></td>
<td>(Unconditional OR)</td>
</tr>
<tr>
<td>&amp;&amp;</td>
<td>Conditional AND</td>
<td>Left to right</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>?:</td>
<td>Ternary condition</td>
<td>Right to left</td>
</tr>
<tr>
<td>=</td>
<td>Assignment</td>
<td>Right to left</td>
</tr>
<tr>
<td>+=</td>
<td>Addition assignment</td>
<td>Right to left</td>
</tr>
<tr>
<td>-=</td>
<td>Subtraction assignment</td>
<td>Right to left</td>
</tr>
<tr>
<td>*=</td>
<td>Multiplication assignment</td>
<td>Right to left</td>
</tr>
<tr>
<td>/=</td>
<td>Division assignment</td>
<td>Right to left</td>
</tr>
<tr>
<td>%=</td>
<td>Remainder assignment</td>
<td>Right to left</td>
</tr>
</tbody>
</table>
Java Modifiers

Modifiers are used on classes and class members (constructors, methods, data, and class-level blocks), but the `final` modifier can also be used on local variables in a method. A modifier that can be applied to a class is called a *class modifier*. A modifier that can be applied to a method is called a *method modifier*. A modifier that can be applied to a data field is called a *data modifier*. A modifier that can be applied to a class-level block is called a *block modifier*. The following table gives a summary of the Java modifiers.

<table>
<thead>
<tr>
<th>Modifier</th>
<th>Class</th>
<th>Constructor</th>
<th>Method</th>
<th>Data</th>
<th>Block</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>(default)*</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>A class, constructor, method, or data field is visible in this package.</td>
</tr>
<tr>
<td>public</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td></td>
<td>A class, constructor, method, or data field is visible to all the programs in any package.</td>
</tr>
<tr>
<td>private</td>
<td></td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td></td>
<td>A constructor, method, or data field is only visible in this class.</td>
</tr>
<tr>
<td>protected</td>
<td></td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td></td>
<td>A constructor, method, or data field is visible in this package and in subclasses of this class in any package.</td>
</tr>
<tr>
<td>static</td>
<td></td>
<td></td>
<td>✓</td>
<td>✓</td>
<td>✓</td>
<td>Define a class method, a class data field, or a static initialization block.</td>
</tr>
<tr>
<td>final</td>
<td>✓</td>
<td></td>
<td>✓</td>
<td>✓</td>
<td></td>
<td>A final class cannot be extended. A final method cannot be modified in a subclass. A final data field is a constant.</td>
</tr>
<tr>
<td>abstract</td>
<td>✓</td>
<td></td>
<td></td>
<td>✓</td>
<td></td>
<td>An abstract class must be extended. An abstract method must be implemented in a concrete subclass.</td>
</tr>
<tr>
<td>native</td>
<td></td>
<td></td>
<td></td>
<td>✓</td>
<td></td>
<td>A native method indicates that the method is implemented using a language other than Java.</td>
</tr>
</tbody>
</table>

*Default access doesn’t have a modifier associated with it. For example: `class Test {}`
The modifiers default (no modifier), **public**, **private**, and **protected** are known as *visibility* or *accessibility modifiers* because they specify how classes and class members are accessed.

The modifiers **public**, **private**, **protected**, **static**, **final**, and **abstract** can also be applied to inner classes.

<table>
<thead>
<tr>
<th>Modifier</th>
<th>Class</th>
<th>Constructor</th>
<th>Method</th>
<th>Data</th>
<th>Block</th>
<th>Explanation</th>
</tr>
</thead>
<tbody>
<tr>
<td>synchronized</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Only one thread at a time can execute this method.</td>
</tr>
<tr>
<td>strictfp</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Use strict floating-point calculations to guarantee that the evaluation result is the same on all JVMs.</td>
</tr>
<tr>
<td>transient</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Mark a nonserializable instance data field.</td>
</tr>
</tbody>
</table>
APPENDIX E

Special Floating-Point Values

Dividing an integer by zero is invalid and throws \texttt{ArithmeticException}, but dividing a floating-point value by zero does not cause an exception. Floating-point arithmetic can overflow to infinity if the result of the operation is too large for a \texttt{double} or a \texttt{float}, or underflow to zero if the result is too small for a \texttt{double} or a \texttt{float}. Java provides the special floating-point values \texttt{POSITIVE_INFINITY}, \texttt{NEGATIVE_INFINITY}, and \texttt{NaN} (Not a Number) to denote these results. These values are defined as special constants in the \texttt{Float} class and the \texttt{Double} class.

If a positive floating-point number is divided by zero, the result is \texttt{POSITIVE_INFINITY}. If a negative floating-point number is divided by zero, the result is \texttt{NEGATIVE_INFINITY}. If a floating-point zero is divided by zero, the result is \texttt{NaN}, which means that the result is undefined mathematically. The string representations of these three values are \texttt{Infinity}, \texttt{-Infinity}, and \texttt{NaN}. For example,

\begin{verbatim}
System.out.print(1.0 / 0); // Print Infinity
System.out.print(-1.0 / 0); // Print -Infinity
System.out.print(0.0 / 0); // Print NaN
\end{verbatim}

These special values can also be used as operands in computations. For example, a number divided by \texttt{POSITIVE_INFINITY} yields a positive zero. Table E.1 summarizes various combinations of the \texttt{/}, \texttt{*}, \texttt{\%}, \texttt{+}, and \texttt{-} operators.

\begin{table}[h]
\centering
\caption{Special Floating-Point Values}
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline
x & y & x/y & x*y & x\%y & x + y & x - y \\
\hline
Finite & \pm 0.0 & \pm \text{ infinity} & \pm 0.0 & \text{NaN} & \text{Finite} & \text{Finite} \\
Finite & \pm \text{ infinity} & \pm 0.0 & \pm 0.0 & x & \pm \text{ infinity} & \text{ infinity} \\
\pm 0.0 & \pm 0.0 & \text{NaN} & \pm 0.0 & \text{NaN} & \pm 0.0 & \pm 0.0 \\
\pm \text{ infinity} & \text{Finite} & \pm \text{ infinity} & \pm 0.0 & \text{NaN} & \pm \text{ infinity} & \pm \text{ infinity} \\
\pm \text{ infinity} & \pm \text{ infinity} & \text{NaN} & \pm 0.0 & \text{NaN} & \pm \text{ infinity} & \text{ infinity} \\
\pm 0.0 & \pm \text{ infinity} & \pm 0.0 & \text{NaN} & \pm 0.0 & \pm \text{ infinity} & \pm 0.0 \\
\text{NaN} & \text{Any} & \text{NaN} & \text{NaN} & \text{NaN} & \text{NaN} & \text{NaN} \\
\text{Any} & \text{NaN} & \text{NaN} & \text{NaN} & \text{NaN} & \text{NaN} & \text{NaN} \\
\hline
\end{tabular}
\end{table}

\textbf{Note}

If one of the operands is \texttt{NaN}, the result is \texttt{NaN}.

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F.1 Introduction

Computers use binary numbers internally, because computers are made naturally to store and process 0s and 1s. The binary number system has two digits, 0 and 1. A number or character is stored as a sequence of 0s and 1s. Each 0 or 1 is called a *bit* (binary digit).

In our daily life we use decimal numbers. When we write a number such as 20 in a program, it is assumed to be a decimal number. Internally, computer software is used to convert decimal numbers into binary numbers, and vice versa.

We write computer programs using decimal numbers. However, to deal with an operating system, we need to reach down to the “machine level” by using binary numbers. Binary numbers tend to be very long and cumbersome. Often hexadecimal numbers are used to abbreviate them, with each hexadecimal digit representing four binary digits. The hexadecimal number system has 16 digits: 0–9 and A–F. The letters A, B, C, D, E, and F correspond to the decimal numbers 10, 11, 12, 13, 14, and 15.

The digits in the decimal number system are 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9. A decimal number is represented by a sequence of one or more of these digits. The value that each digit represents depends on its position, which denotes an integral power of 10. For example, the digits 7, 4, 2, and 3 in decimal number 7423 represent 7000, 400, 20, and 3, respectively, as shown below:

\[
\begin{array}{cccc}
7 & 4 & 2 & 3 \\
10^3 & 10^2 & 10^1 & 10^0 \\
7000 & 400 & 20 & 3 \\
\end{array}
\]

The decimal number system has ten digits, and the position values are integral powers of 10. We say that 10 is the *base* or *radix* of the decimal number system. Similarly, since the binary number system has two digits, its base is 2, and since the hex number system has 16 digits, its base is 16.

If 1101 is a binary number, the digits 1, 1, 0, and 1 represent \(1 \times 2^3, 1 \times 2^2, 0 \times 2^1, \text{ and } 1 \times 2^0\), respectively:

\[
\begin{array}{cccc}
1 & 1 & 0 & 1 \\
2^3 & 2^2 & 2^1 & 2^0 \\
8 & 4 & 0 & 1 \\
\end{array}
\]

If 7423 is a hex number, the digits 7, 4, 2, and 3 represent \(7 \times 16^3, 4 \times 16^2, 2 \times 16^1, \text{ and } 3 \times 16^0\), respectively:

\[
\begin{array}{cccc}
7 & 4 & 2 & 3 \\
16^3 & 16^2 & 16^1 & 16^0 \\
28672 & 1024 & 32 & 3 \\
\end{array}
\]

\[= 29731\]
F.2 Conversions Between Binary and Decimal Numbers

Given a binary number $b_n b_{n-1} b_{n-2} \ldots b_2 b_1 b_0$, the equivalent decimal value is

$$ b_n \times 2^n + b_{n-1} \times 2^{n-1} + b_{n-2} \times 2^{n-2} + \ldots + b_2 \times 2^2 + b_1 \times 2^1 + b_0 \times 2^0 $$

Here are some examples of converting binary numbers to decimals:

<table>
<thead>
<tr>
<th>Binary</th>
<th>Conversion Formula</th>
<th>Decimal</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>$1 \times 2^1 + 0 \times 2^0$</td>
<td>2</td>
</tr>
<tr>
<td>1000</td>
<td>$1 \times 2^3 + 0 \times 2^2 + 0 \times 2^1 + 0 \times 2^0$</td>
<td>8</td>
</tr>
<tr>
<td>101011</td>
<td>$1 \times 2^6 + 0 \times 2^5 + 1 \times 2^4 + 0 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$</td>
<td>171</td>
</tr>
</tbody>
</table>

To convert a decimal number $d$ to a binary number is to find the bits $b_n, b_{n-1}, b_{n-2}, \ldots, b_2, b_1$ and $b_0$ such that

$$ d = b_n \times 2^n + b_{n-1} \times 2^{n-1} + b_{n-2} \times 2^{n-2} + \ldots + b_2 \times 2^2 + b_1 \times 2^1 + b_0 \times 2^0 $$

These bits can be found by successively dividing $d$ by 2 until the quotient is 0. The remainders are $b_n, b_1, b_2, \ldots, b_{n-2}, b_{n-1}$, and $b_n$.

For example, the decimal number 123 is 1110111 in binary. The conversion is done as follows:

<table>
<thead>
<tr>
<th>Quotient</th>
<th>Remainder</th>
</tr>
</thead>
<tbody>
<tr>
<td>123</td>
<td>1</td>
</tr>
<tr>
<td>61</td>
<td>1</td>
</tr>
<tr>
<td>30</td>
<td>1</td>
</tr>
<tr>
<td>15</td>
<td>1</td>
</tr>
<tr>
<td>7</td>
<td>1</td>
</tr>
<tr>
<td>3</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>1</td>
</tr>
</tbody>
</table>

**Tip**

The Windows Calculator, as shown in Figure F.1, is a useful tool for performing number conversions. To run it, search for Calculator from the Start button and launch Calculator, then under View select Scientific.

![Figure F.1](image.png)
F.3 Conversions Between Hexadecimal and Decimal Numbers

Given a hexadecimal number $h_nh_{n-1}h_{n-2}\ldots h_2h_1h_0$, the equivalent decimal value is

$$h_n \times 16^n + h_{n-1} \times 16^{n-1} + h_{n-2} \times 16^{n-2} + \ldots + h_2 \times 16^2 + h_1 \times 16^1 + h_0 \times 16^0$$

Here are some examples of converting hexadecimal numbers to decimals:

<table>
<thead>
<tr>
<th>Hexadecimal</th>
<th>Conversion Formula</th>
<th>Decimal</th>
</tr>
</thead>
<tbody>
<tr>
<td>7F</td>
<td>$7 \times 16^1 + 15 \times 16^0$</td>
<td>127</td>
</tr>
<tr>
<td>FFFF</td>
<td>$15 \times 16^3 + 15 \times 16^2 + 15 \times 16^1 + 15 \times 16^0$</td>
<td>65535</td>
</tr>
<tr>
<td>431</td>
<td>$4 \times 16^2 + 3 \times 16^1 + 1 \times 16^0$</td>
<td>1073</td>
</tr>
</tbody>
</table>

To convert a decimal number $d$ to a hexadecimal number is to find the hexadecimal digits $h_n, h_{n-1}, h_{n-2}, \ldots, h_2, h_1, h_0$ such that

$$d = h_n \times 16^n + h_{n-1} \times 16^{n-1} + h_{n-2} \times 16^{n-2} + \ldots + h_2 \times 16^2 + h_1 \times 16^1 + h_0 \times 16^0$$

These numbers can be found by successively dividing $d$ by 16 until the quotient is 0. The remainders are $h_0, h_1, h_2, \ldots, h_{n-2}, h_{n-1}$, and $h_n$.

For example, the decimal number 123 is 7B in hexadecimal. The conversion is done as follows:

\[ \begin{array}{c|c}
16 & 123 \\
--- & --- \\
7 & 112 \\
0 & 11 \\
\end{array} \]

F.4 Conversions Between Binary and Hexadecimal Numbers

To convert a hexadecimal to a binary number, simply convert each digit in the hexadecimal number into a four-digit binary number, using Table F.1.

For example, the hexadecimal number 7B is 1111011, where 7 is 111 in binary, and B is 1011 in binary.

To convert a binary number to a hexadecimal, convert every four binary digits from right to left in the binary number into a hexadecimal number.

For example, the binary number 1110001101 is 38D, since 1101 is D, 1000 is 8, and 11 is 3, as shown below.
Appendix F

Note

Octal numbers are also useful. The octal number system has eight digits, 0 to 7. A decimal number 8 is represented in the octal system as 10.

Here are some good online resources for practicing number conversions:

- [http://people.sinclair.edu/nickreeder/Flash/binDec.htm](http://people.sinclair.edu/nickreeder/Flash/binDec.htm)
- [http://people.sinclair.edu/nickreeder/Flash/binHex.htm](http://people.sinclair.edu/nickreeder/Flash/binHex.htm)

Table F.1  Converting Hexadecimal to Binary

<table>
<thead>
<tr>
<th>Hexadecimal</th>
<th>Binary</th>
<th>Decimal</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0000</td>
<td>0</td>
</tr>
<tr>
<td>1</td>
<td>0001</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>0010</td>
<td>2</td>
</tr>
<tr>
<td>3</td>
<td>0011</td>
<td>3</td>
</tr>
<tr>
<td>4</td>
<td>0100</td>
<td>4</td>
</tr>
<tr>
<td>5</td>
<td>0101</td>
<td>5</td>
</tr>
<tr>
<td>6</td>
<td>0110</td>
<td>6</td>
</tr>
<tr>
<td>7</td>
<td>0111</td>
<td>7</td>
</tr>
<tr>
<td>8</td>
<td>1000</td>
<td>8</td>
</tr>
<tr>
<td>9</td>
<td>1001</td>
<td>9</td>
</tr>
<tr>
<td>A</td>
<td>1010</td>
<td>10</td>
</tr>
<tr>
<td>B</td>
<td>1011</td>
<td>11</td>
</tr>
<tr>
<td>C</td>
<td>1100</td>
<td>12</td>
</tr>
<tr>
<td>D</td>
<td>1101</td>
<td>13</td>
</tr>
<tr>
<td>E</td>
<td>1110</td>
<td>14</td>
</tr>
<tr>
<td>F</td>
<td>1111</td>
<td>15</td>
</tr>
</tbody>
</table>

F.1 Convert the following decimal numbers into hexadecimal and binary numbers: 100; 4340; 2000

F.2 Convert the following binary numbers into hexadecimal and decimal numbers: 1000111010; 10000000; 10011

F.3 Convert the following hexadecimal numbers into binary and decimal numbers: FEFA9; 93; 2000
Bitwise Operations

To write programs at the machine-level, often you need to deal with binary numbers directly and perform operations at the bit-level. Java provides the bitwise operators and shift operators defined in Table G.1.

The bit operators apply only to integer types (byte, short, int, and long). A character involved in a bit operation is converted to an integer. All bitwise operators can form bitwise assignment operators, such as =, |=, <<=, and >>>=.

### Table G.1

<table>
<thead>
<tr>
<th>Operator</th>
<th>Name</th>
<th>Example (using bytes in the example)</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>&amp;</td>
<td>Bitwise AND</td>
<td>10101110 &amp; 10010010 yields 10000010</td>
<td>The AND of two corresponding bits yields a 1 if both bits are 1.</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>Bitwise inclusive OR</td>
<td>10101110</td>
<td>The OR of two corresponding bits yields a 1 if either bit is 1.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>10010010 yields 10111110</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Bitwise exclusive OR</td>
<td>10101110 ^ 10010010 yields 00111100</td>
<td>The XOR of two corresponding bits yields a 1 only if two bits are different.</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>One’s complement</td>
<td>~10101110 yields 01010001</td>
<td>The operator toggles each bit from 0 to 1 and from 1 to 0.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>01010001</td>
<td></td>
</tr>
<tr>
<td>&lt;&lt;</td>
<td>Left shift</td>
<td>10101110 &lt;&lt; 2 yields 10111000</td>
<td>The operator shifts bits in the first operand left by the number of bits specified in the second operand, filling with 0s on the right.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>10111000</td>
<td></td>
</tr>
<tr>
<td>&gt;&gt;</td>
<td>Right shift with sign extension</td>
<td>10101110 &gt;&gt; 2 yields 11101011</td>
<td>The operator shifts bit in the first operand right by the number of bits specified in the second operand, filling with the highest (sign) bit on the left.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>11101011</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>00101110 &gt;&gt; 2 yields 00001011</td>
<td></td>
</tr>
<tr>
<td>&gt;&gt;&gt;</td>
<td>Unsigned right shift with zero extension</td>
<td>10101110 &gt;&gt;&gt; 2 yields 00101011</td>
<td>The operator shifts bit in the first operand right by the number of bits specified in the second operand, filling with 0s on the left.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>00101011</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>00101110 &gt;&gt;&gt; 2 yields 00001011</td>
<td></td>
</tr>
</tbody>
</table>
Regular Expressions

Often you need to write the code to validate user input such as to check whether the input is a number, a string with all lowercase letters, or a social security number. How do you write this type of code? A simple and effective way to accomplish this task is to use the regular expression.

A regular expression (abbreviated regex) is a string that describes a pattern for matching a set of strings. Regular expression is a powerful tool for string manipulations. You can use regular expressions for matching, replacing, and splitting strings.

H.1 Matching Strings

Let us begin with the `matches` method in the `String` class. At first glance, the `matches` method is very similar to the `equals` method. For example, the following two statements both evaluate to `true`.

```java
"Java".matches("Java");
"Java".equals("Java");
```

However, the `matches` method is more powerful. It can match not only a fixed string, but also a set of strings that follow a pattern. For example, the following statements all evaluate to `true`.

```java
"Java is fun".matches("Java.*")
"Java is cool".matches("Java.*")
"Java is powerful".matches("Java.*")
```

"Java.*" in the preceding statements is a regular expression. It describes a string pattern that begins with Java followed by any zero or more characters. Here, the substring `.*` matches any zero or more characters.

H.2 Regular Expression Syntax

A regular expression consists of literal characters and special symbols. Table H.1 lists some frequently used syntax for regular expressions.

**Note**
Backslash is a special character that starts an escape sequence in a string. So you need to use `\d` in Java to represent `\d`.

**Note**
Recall that a whitespace character is `' '`, `'\t'`, `'\n'`, `'\r'`, or `'\f'`. So `\s` is the same as `[ \t\n\r\f]`, and `\S` is the same as `[^ \t\n\r\f]`. 
**Table H.1** Frequently Used Regular Expressions

<table>
<thead>
<tr>
<th>Regular Expression</th>
<th>Matches</th>
<th>Example</th>
</tr>
</thead>
<tbody>
<tr>
<td>x</td>
<td>a specified character x</td>
<td>Java matches Java</td>
</tr>
<tr>
<td>.</td>
<td>any single character</td>
<td>Java matches J.a</td>
</tr>
<tr>
<td>(ab</td>
<td>cd)</td>
<td>ab or cd</td>
</tr>
<tr>
<td>[abc]</td>
<td>a, b, or c</td>
<td>Java matches Ja[uvwx]a</td>
</tr>
<tr>
<td>[^abc]</td>
<td>any character except a, b, or c</td>
<td>Java matches Ja[^ars]a</td>
</tr>
<tr>
<td>[a-z]</td>
<td>a through z</td>
<td>Java matches [A-M]av[a-d]</td>
</tr>
<tr>
<td>[^a-z]</td>
<td>a through z</td>
<td>Java matches Jav[^b-d]</td>
</tr>
<tr>
<td>[a-e[m-p]]</td>
<td>a through e or m through p</td>
<td>Java matches [A-G[I-M]]av[a-d]</td>
</tr>
<tr>
<td>[a-e&amp;&amp;[c-p]]</td>
<td>intersection of a-e with c-p</td>
<td>Java matches [A-P&amp;&amp;[I-M]]jav[a-d]</td>
</tr>
<tr>
<td>\d</td>
<td>a digit, same as [0-9]</td>
<td>Java2 matches &quot;Java[\d]&quot;</td>
</tr>
<tr>
<td>\D</td>
<td>a non-digit</td>
<td>$Java matches &quot;[\D][\D]ava&quot;</td>
</tr>
<tr>
<td>\w</td>
<td>a word character</td>
<td>Java1 matches &quot;[\w]ava[\w]&quot;</td>
</tr>
<tr>
<td>\W</td>
<td>a non-word character</td>
<td>$Java matches &quot;[\W]ava[\W]ava&quot;</td>
</tr>
<tr>
<td>\s</td>
<td>a whitespace character</td>
<td>&quot;Java 2&quot; matches &quot;Java\s2&quot;</td>
</tr>
<tr>
<td>\S</td>
<td>a non-whitespace char</td>
<td>Java matches &quot;[\S]ava&quot;</td>
</tr>
<tr>
<td>p*</td>
<td>zero or more occurrences of pattern p</td>
<td>aaaaabb matches &quot;a<em>b</em>b&quot;, ababab matches &quot;(ab)**&quot;</td>
</tr>
<tr>
<td>p+</td>
<td>one or more occurrences of pattern p</td>
<td>a matches &quot;a+b*&quot;, able matches &quot;(ab)+.*&quot;</td>
</tr>
<tr>
<td>p?</td>
<td>zero or one occurrence of pattern p</td>
<td>Java matches &quot;J?Java&quot;, Java matches &quot;J?ava&quot;</td>
</tr>
<tr>
<td>p{n}</td>
<td>exactly n occurrences of pattern p</td>
<td>Java matches &quot;Ja{1}.*&quot;, Java does not match &quot;.{2}&quot;</td>
</tr>
<tr>
<td>p{n,}</td>
<td>at least n occurrences of pattern p</td>
<td>aaaa matches &quot;a{1,}&quot;</td>
</tr>
<tr>
<td>p{n,m}</td>
<td>between n and m occurrences (inclusive)</td>
<td>aaaa matches &quot;a{1,9}&quot;, abb does not match &quot;a{2,9}bb&quot;</td>
</tr>
</tbody>
</table>

**Note**

A word character is any letter, digit, or the underscore character. So \w is the same as [a-zA-Z][0-9_] or simply [a-zA-Z][0-9_]. and \W is the same as [^a-zA-Z0-9_].

**Note**

The last six entries *, +, ?, {n}, {n,}, and {n, m} in Table H.1 are called quantifiers that specify how many times the pattern before a quantifier may repeat. For example, A* matches zero or more A’s, A+ matches one or more A’s, A? matches zero or one A’s. A{3} matches exactly AAA, A{3,} matches at least three A’s, and A{3,6} matches between 3 and 6 A’s. * is the same as {0,}, + is the same as {1,}, ? is the same as {0,1}. quantifiers
Caution
Do not use spaces in the repeat quantifiers. For example, $A\{3, 6\}$ cannot be written as $A\{3, 6\}$ with a space after the comma.

Note
You may use parentheses to group patterns. For example, $(ab)\{3\}$ matches ababab, but $ab\{3\}$ matches abbb.

Let us use several examples to demonstrate how to construct regular expressions.

Example 1
The pattern for social security numbers is $xxx-xx-xxxx$, where $x$ is a digit. A regular expression for social security numbers can be described as

$$[\d] \{3\}-[\d] \{2\}-[\d] \{4\}$$

For example,


Example 2
An even number ends with digits 0, 2, 4, 6, or 8. The pattern for even numbers can be described as

$$[\d]*[02468]$$

For example,

"123".matches("[\d]*[02468]") returns false.
"122".matches("[\d]*[02468]") returns true.

Example 3
The pattern for telephone numbers is $(xxx) xxx-xxxx$, where $x$ is a digit and the first digit cannot be zero. A regular expression for telephone numbers can be described as

$$\((1-9) [\d] \{2\}\) [\d] \{3\}-[\d] \{4\}$$

Note that the parentheses symbols ( and ) are special characters in a regular expression for grouping patterns. To represent a literal ( or ) in a regular expression, you have to use \( and \).

For example,

"(912) 921-2728".matches("\((1-9) [\d] \{2\}\) \([\d] \{3\}-[\d] \{4\}\)" returns true.
"921-2728".matches("\((1-9) [\d] \{2\}\) \([\d] \{3\}-[\d] \{4\}\)" returns false.

Example 4
Suppose the last name consists of at most 25 letters and the first letter is in uppercase. The pattern for a last name can be described as

$$[A-Z][a-zA-Z] \{1, 24\}$$

Note that you cannot have arbitrary whitespace in a regular expression. For example, $[A-Z][a-zA-Z] \{1, 24\}$ would be wrong.
For example,

"Smith".matches("[A-Z][a-zA-Z]{1,24}") returns true.
"Jones123".matches("[A-Z][a-zA-Z]{1,24}") returns false.

Example 5
Java identifiers are defined in Section 2.4, “Identifiers.”

- An identifier must start with a letter, an underscore (_), or a dollar sign ($). It cannot start with a digit.
- An identifier is a sequence of characters that consists of letters, digits, underscores (_), and dollar signs ($).

The pattern for identifiers can be described as

[a-zA-Z_$][\w$]*

Example 6
What strings are matched by the regular expression "Welcome to (Java|HTML)"? The answer is Welcome to Java or Welcome to HTML.

Example 7
What strings are matched by the regular expression "A.*"? The answer is any string that starts with letter A.

H.3 Replacing and Splitting Strings
The matches method in the String class returns true if the string matches the regular expression. The String class also contains the replaceAll, replaceFirst, and split methods for replacing and splitting strings, as shown in Figure H.1.

<table>
<thead>
<tr>
<th>java.lang.String</th>
</tr>
</thead>
<tbody>
<tr>
<td>+matches(regex: String): boolean Returns true if this string matches the pattern.</td>
</tr>
<tr>
<td>+replaceAll(regex: String, replacement: String): String Returns a new string that replaces all matching substrings with the replacement.</td>
</tr>
<tr>
<td>+replaceFirst(regex: String, replacement: String): String Returns a new string that replaces the first matching substring with the replacement.</td>
</tr>
<tr>
<td>+split(regex: String): String[] Returns an array of strings consisting of the substrings split by the matches.</td>
</tr>
<tr>
<td>+split(regex: String, limit: int): String[] Same as the preceding split method except that the limit parameter controls the number of times the pattern is applied.</td>
</tr>
</tbody>
</table>

The replaceAll method replaces all matching substring and the replaceFirst method replaces the first matching substring. For example, the following code

    System.out.println("Java Java Java".replaceAll("v\w", "wi"));

displays

    Jawi Jawi Jawi
The following code

```java
System.out.println("Java Java Java.replaceAll("v\w", "wi");
```

displays

**Java Java Java**

There are two overloaded `split` methods. The `split(regex)` method splits a string into substrings delimited by the matches. For example, the following statement

```java
String[] tokens = "Java1HTML2Perl".split("\d");
```

In the `split(regex, limit)` method, the `limit` parameter determines how many times the pattern is matched. If `limit <= 0`, `split(regex, limit)` is same as `split(regex)`. If `limit > 0`, the pattern is matched at most `limit - 1` times. Here are some examples:

- "Java1HTML2Perl".split("\d", 0); splits into Java, HTML, Perl
- "Java1HTML2Perl".split("\d", 1); splits into Java1HTML2Perl
- "Java1HTML2Perl".split("\d", 2); splits into Java, HTML2Perl
- "Java1HTML2Perl".split("\d", 3); splits into Java, HTML, Perl
- "Java1HTML2Perl".split("\d", 4); splits into Java, HTML, Perl
- "Java1HTML2Perl".split("\d", 5); splits into Java, HTML, Perl

**Note**

By default, all the quantifiers are greedy. This means that they will match as many occurrences as possible. For example, the following statement displays `JRvaa`, since the first match is `aaa`.

```java
System.out.println("Jaaavaa".replaceFirst("a+", "R"));
```

You can change a qualifier’s default behavior by appending a question mark (?) after it. The quantifier becomes reluctant, which means that it will match as few occurrences as possible. For example, the following statement displays `JRaavaa`, since the first match is `a`.

```java
System.out.println("Jaaavaa".replaceFirst("a+?", "R");
```
I.1 Simple Enumerated Types

An enumerated type defines a list of enumerated values. Each value is an identifier. For example, the following statement declares a type, named `MyFavoriteColor`, with values `RED`, `BLUE`, `GREEN`, and `YELLOW` in this order.

```java
enum MyFavoriteColor {RED, BLUE, GREEN, YELLOW};
```

A value of an enumerated type is like a constant and so, by convention, is spelled with all uppercase letters. So, the preceding declaration uses `RED`, not `red`. By convention, an enumerated type is named like a class with first letter of each word capitalized.

Once a type is defined, you can declare a variable of that type:

```java
MyFavoriteColor color;
```

The variable `color` can hold one of the values defined in the enumerated type `MyFavoriteColor` or `null`, but nothing else. Java enumerated type is type-safe, meaning that an attempt to assign a value other than one of the enumerated values or `null` will result in a compile error.

The enumerated values can be accessed using the syntax

```
EnumeratedTypeName.valueName
```

For example, the following statement assigns enumerated value `BLUE` to variable `color`:

```java
color = MyFavoriteColor.BLUE;
```

Note that you have to use the enumerated type name as a qualifier to reference a value such as `BLUE`.

As with any other type, you can declare and initialize a variable in one statement:

```java
MyFavoriteColor color = MyFavoriteColor.BLUE;
```

An enumerated type is treated as a special class. An enumerated type variable is therefore a reference variable. An enumerated type is a subtype of the `Object` class and the `Comparable` interface. Therefore, an enumerated type inherits all the methods in the `Object` class and the `compareTo` method in the `Comparable` interface. Additionally, you can use the following methods on an enumerated object:

- **public String name();**
  
  Returns a name of the value for the object.

- **public int ordinal();**
  
  Returns the ordinal value associated with the enumerated value. The first value in an enumerated type has an ordinal value of 0, the second has an ordinal value of 1, the third one 3, and so on.
Listing I.1 gives a program that demonstrates the use of enumerated types.

**LISTING I.1 EnumeratedTypeDemo.java**

```java
public class EnumeratedTypeDemo {
    static enum Day {SUNDAY, MONDAY, TUESDAY, WEDNESDAY, THURSDAY,
                    FRIDAY, SATURDAY};

    public static void main(String[] args) {
        Day day1 = Day.FRIDAY;
        Day day2 = Day.THURSDAY;

        System.out.println("day1's name is "+ day1.name());
        System.out.println("day2's name is "+ day2.name());

        System.out.println("day1's ordinal is "+ day1.ordinal());
        System.out.println("day2's ordinal is "+ day2.ordinal());

        System.out.println("day1.equals(day2) returns "+
                            day1.equals(day2));
        System.out.println("day1.toString() returns "+
                            day1.toString());
        System.out.println("day1.compareTo(day2) returns "+
                            day1.compareTo(day2));
    }
}
```

An enumerated type `Day` is defined in lines 2–3. Variables `day1` and `day2` are declared as the `Day` type and assigned enumerated values in lines 6–7. Since `day1`’s value is FRIDAY, its ordinal value is 5 (line 11). Since `day2`’s value is THURSDAY, its ordinal value is 4 (line 12).

Since an enumerated type is a subclass of the `Object` class and the `Comparable` interface, you can invoke the methods `equals`, `toString`, and `compareTo` from an enumerated object reference variable (lines 14–19). `day1.equals(day2)` returns true if `day1` and `day2` have the same ordinal value. `day1.compareTo(day2)` returns the difference between `day1`’s ordinal value to `day2`’s.

Alternatively, you can rewrite the code in Listing I.1 into Listing I.2.

**LISTING I.2 StandaloneEnumTypeDemo.java**

```java
public class StandaloneEnumTypeDemo {
    public static void main(String[] args) {
        Day day1 = Day.FRIDAY;
        Day day2 = Day.THURSDAY;

        System.out.println("day1's name is "+ day1.name());
        System.out.println("day2's name is "+ day2.name());
        System.out.println("day1's ordinal is "+ day1.ordinal());
    }
}
```
System.out.println("day2's ordinal is " + day2.ordinal());
System.out.println("day1.equals(day2) returns " +
        day1.equals(day2));
System.out.println("day1.toString() returns " +
        day1.toString());
System.out.println("day1.compareTo(day2) returns " +
        day1.compareTo(day2));
}
}

enum Day {SUNDAY, MONDAY, TUESDAY, WEDNESDAY, THURSDAY,
FRIDAY, SATURDAY}

An enumerated type can be defined inside a class, as shown in lines 2–3 in Listing I.1, or
standalone as shown in lines 20–21 Listing I.2. In the former case, the type is treated as an
inner class. After the program is compiled, a class named EnumeratedTypeDemo$Day.class
is created. In the latter case, the type is treated as a standalone class. After the program is
compiled, a class named Day.class is created.

**Note**
When an enumerated type is declared inside a class, the type must be declared as a
member of the class and cannot be declared inside a method. Furthermore, the type is
always `static`. For this reason, the `static` keyword in line 2 in Listing I.1 may be
omitted. The visibility modifiers on inner class can be also be applied to enumerated
types defined inside a class.

**Tip**
Using enumerated values (e.g., `Day.MONDAY`, `Day.TUESDAY`, and so on) rather than
literal integer values (e.g., 0, 1, and so on) can make program easier to read and maintain.

### 1.2 Using if or switch Statements with an
Enumerated Variable

An enumerated variable holds a value. Often your program needs to perform a specific action
depending on the value. For example, if the value is `Day.MONDAY`, play soccer; if the value is
`Day.TUESDAY`, take piano lesson, and so on. You can use an `if` statement or a `switch` state-
ment to test the value in the variable, as shown in (a) and (b)

```java
if (day.equals(Day.MONDAY)) {
    // process Monday
} else if (day.equals(Day.TUESDAY)) {
    // process Tuesday
} else
    ...
```

```java
switch (day) {
    case MONDAY:
        // process Monday
        break;
    case TUESDAY:
        // process Tuesday
        break;
    ...
}
```

In the `switch` statement in (b), the case label is an unqualified enumerated value (e.g.,
`MONDAY`, but not `Day.MONDAY`).
I.3 Processing Enumerated Values Using a Foreach Loop

Each enumerated type has a static method `values()` that returns all enumerated values for the type in an array. For example,

```java
Day[] days = Day.values();
```

You can use a regular for loop in (a) or a foreach loop in (b) to process all the values in the array.

(a) ```java
for (int i = 0; i < days.length; i++)
    System.out.println(days[i]);
```
(b) ```java
for (Day day : days)
    System.out.println(day);
```

I.4 Enumerated Types with Data Fields, Constructors, and Methods

The simple enumerated types introduced in the preceding section define a type with a list of enumerated values. You can also define an enumerate type with data fields, constructors, and methods, as shown in Listing I.3.

**Listing I.3** TrafficLight.java

```java
public enum TrafficLight {
    RED ("Please stop"), GREEN ("Please go"),
    YELLOW ("Please caution");

    private String description;

    private TrafficLight(String description) {
        this.description = description;
    }

    public String getDescription() {
        return description;
    }
}
```

The enumerated values are defined in lines 2–3. The value declaration must be the first statement in the type declaration. A data field named `description` is declared in line 5 to describe an enumerated value. The constructor `TrafficLight` is declared in lines 7–9. The constructor is invoked whenever an enumerated value is accessed. The enumerated value’s argument is passed to the constructor, which is then assigned to `description`.

Listing I.4 gives a test program to use `TrafficLight`.

**Listing I.4** TestTrafficLight.java

```java
public class TestTrafficLight {
    public static void main(String[] args) {
        TrafficLight light = TrafficLight.RED;
        System.out.println(light.getDescription());
    }
}
```
An enumerated value `TrafficLight.red` is assigned to variable `light` (line 3). Accessing `TrafficLight.RED` causes the JVM to invoke the constructor with argument “please stop”. The methods in enumerated type are invoked in the same way as the methods in a class. `light.getDescription()` returns the description for the enumerated value (line 4).

**Note**
The Java syntax requires that the constructor for enumerated types be private to prevent it from being invoked directly. The `private` modifier may be omitted. In this case, it is considered private by default.
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### Console Input
```java
Scanner input = new Scanner(System.in);
int intValue = input.nextInt();
long longValue = input.nextLong();
double doubleValue = input.nextDouble();
String string = input.next();
String line = input.nextLine();
```

### Console Output
```java
System.out.println(anyValue);
```

### Primitive Data Types
<table>
<thead>
<tr>
<th>Type</th>
<th>Size</th>
</tr>
</thead>
<tbody>
<tr>
<td>byte</td>
<td>8 bits</td>
</tr>
<tr>
<td>short</td>
<td>16 bits</td>
</tr>
<tr>
<td>int</td>
<td>32 bits</td>
</tr>
<tr>
<td>long</td>
<td>64 bits</td>
</tr>
<tr>
<td>float</td>
<td>32 bits</td>
</tr>
<tr>
<td>double</td>
<td>64 bits</td>
</tr>
<tr>
<td>char</td>
<td>16 bits</td>
</tr>
<tr>
<td>boolean</td>
<td>true/false</td>
</tr>
</tbody>
</table>

### Arithmetic Operators
<table>
<thead>
<tr>
<th>Operator</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>+</td>
<td>addition</td>
</tr>
<tr>
<td>-</td>
<td>subtraction</td>
</tr>
<tr>
<td>*</td>
<td>multiplication</td>
</tr>
<tr>
<td>/</td>
<td>division</td>
</tr>
<tr>
<td>%</td>
<td>remainder</td>
</tr>
<tr>
<td>++var</td>
<td>preincrement</td>
</tr>
<tr>
<td>--var</td>
<td>predecrement</td>
</tr>
<tr>
<td>var++</td>
<td>postincrement</td>
</tr>
<tr>
<td>var--</td>
<td>postdecrement</td>
</tr>
</tbody>
</table>

### Logical Operators
<table>
<thead>
<tr>
<th>Operator</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>&amp;&amp;</td>
<td>short circuit AND</td>
</tr>
<tr>
<td></td>
<td></td>
</tr>
<tr>
<td>!</td>
<td>NOT</td>
</tr>
<tr>
<td>^</td>
<td>exclusive OR</td>
</tr>
</tbody>
</table>

### Relational Operators
<table>
<thead>
<tr>
<th>Operator</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>&lt;</td>
<td>less than</td>
</tr>
<tr>
<td>&lt;=</td>
<td>less than or equal to</td>
</tr>
<tr>
<td>&gt;</td>
<td>greater than</td>
</tr>
<tr>
<td>&gt;=</td>
<td>greater than or equal to</td>
</tr>
<tr>
<td>==</td>
<td>equal to</td>
</tr>
<tr>
<td>!=</td>
<td>not equal</td>
</tr>
</tbody>
</table>

### Conditional Expression
```java
boolean-expression ? expression1 : expression2
```
```java
y = (x > 0) ? 1 : -1
System.out.println(number % 2 == 0 ? "number is even" : "number is odd");
```

### Assignment Operators
<table>
<thead>
<tr>
<th>Operator</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>=</td>
<td>assignment</td>
</tr>
<tr>
<td>+=</td>
<td>addition assignment</td>
</tr>
<tr>
<td>-=</td>
<td>subtraction assignment</td>
</tr>
<tr>
<td>*=</td>
<td>multiplication assignment</td>
</tr>
<tr>
<td>/=</td>
<td>division assignment</td>
</tr>
<tr>
<td>%=</td>
<td>remainder assignment</td>
</tr>
<tr>
<td>-=</td>
<td>predecrement</td>
</tr>
<tr>
<td>var++</td>
<td>postincrement</td>
</tr>
<tr>
<td>var--</td>
<td>postdecrement</td>
</tr>
</tbody>
</table>

### Switch Statements
```java
switch (intExpression) {
    case value1:
        statements;
        break;
    ...
    case valueN:
        statements;
        break;
    default:
        statements;
}
```

### If Statements
```java
if (condition) {
    statements;
}
```
```java
if (condition) {
    statements;
} else {
    statements;
}
```
```java
if (condition1) {
    statements;
} else if (condition2) {
    statements;
} else {
    statements;
}
```

### Do While Loop
```java
do {
    statements;
} while (condition);
```

### For Loop
```java
for (init; condition; adjustment) {
    statements;
}
```

### Java Quick Reference
- **Conditional Expression**: `boolean-expression ? expression1 : expression2`
- **Assignment Operators**:
  - `=`: assignment
  - `+=`: addition assignment
  - `-=`: subtraction assignment
  - `*=`: multiplication assignment
  - `/=`: division assignment
  - `%=`: remainder assignment
- **Logical Operators**: `&&` (short circuit AND), `||` (short circuit OR), `!` (NOT), `^` (exclusive OR)
- **Relational Operators**: `<` (less than), `<=` (less than or equal to), `>` (greater than), `>=` (greater than or equal to), `==` (equal to), `!=` (not equal)
- **Switch Statements**: `switch (intExpression) {
    case value1:
        statements;
        break;
    ...
    case valueN:
        statements;
        break;
    default:
        statements;
}
- **If Statements**: `if (condition) {
    statements;
} else {
    statements;
} if (condition) {
    statements;
} else if (condition2) {
    statements;
} else {
    statements;
}
- **Do While Loop**: `do {
    statements;
} while (condition);`
- **For Loop**: `for (init; condition; adjustment) {
    statements;
}`

**Companion Web site**: www.pearsonhighered.com/liang
Frequently Used Static Constants/Methods

- Math.PI
- Math.random()
- Math.pow(a, b)
- Math.abs(a)
- Math.max(a, b)
- Math.min(a, b)
- Math.sqrt(a)
- Math.sin(radians)
- Math.asin(a)
- Math.toRadians(degrees)
- Math.toDegrees(radians)
- System.currentTimeMillis()
- Integer.parseInt(string)
- Integer.parseInt(string, radix)
- Double.parseDouble(string)
- Arrays.sort(type[] list)
- Arrays.binarySearch(type[] list, type key)

Array/Length/Initializer

```
int[] list = new int[10];
list.length;
int[] list = {1, 2, 3, 4};
```

Multidimensional Array/Length/Initializer

```
int[][] list = new int[10][10];
list.length;
list[0].length;
int[][] list = {{1, 2}, {3, 4}};
```

Ragged Array

```
int[][] m = {{1, 2, 3, 4},
            {1, 2, 3},
            {1, 2},
            {1}};
```

String Class

```
String s = "Welcome";
String s = new String(char[]);
int length = s.length();
char ch = s.charAt(index);
int d = s.compareTo(s1);
boolean b = s.equals(s1);
boolean b = s.startsWith(s1);
boolean b = s.endsWith(s1);
boolean b = s.contains(s1);
String s1 = s.trim();
String s1 = s.toUpperCase();
String s1 = s.toLowerCase();
int index = s.indexOf(ch);
int index = s.lastIndexOf(ch);
String s1 = s.substring(ch);
String s1 = s.substring(i,j);
char[] chars = s.toCharArray();
boolean b = s.matches(regex);
String s1 = s.replaceAll(regex,repl);
String[] tokens = s.split(regex);
```

Text File Output

```
PrintWriter output =
    new PrintWriter(filename);
output.println(...) ;
output.print(...);
```

Text File Input

```
Scanner input = new Scanner(
    new File(filename));
```

File Class

```
File file = new File(filename);
file.exists();
file.renameTo(file);
file.delete();
```

Object Class

```
Object o = new Object();
o.toString();
o.equals(o1);
```

FileReader

```
FileReader reader = new FileReader(filename);
```

Comparable Interface

```
c.compareTo(Comparable)
c is a Comparable object
```

ArrayList Class

```
ArrayList<E> list = new ArrayList();
list.add(object);
list.add(index, object);
list.clear();
o = list.get(index);
boolean b = list.isEmpty();
boolean b = list.contains(object);
int i = list.size();
list.remove(index);
list.set(index, object);
i = list.indexOf(object);
i = list.lastIndexOf(object);
```

printf Method

```
System.out.printf("%b %c %d %f %e %s",
   true, 'A', 45, 45.5, 45.5, "Welcome");
System.out.printf("%-5d %10.2f %10.2e %8s",
   45, 45.5, 45.5, "Welcome");
```

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